Improved determination of the 235 U and 239 Pu reactor antineutrino cross sections per fission

C. Giunti

INFN, Sezione di Torino, Via P. Giuria 1, I-10125 Torino, Italy (Received 10 April 2017; revised manuscript received 10 May 2017; published 30 August 2017)

We present the results of a combined fit of the reactor antineutrino rates and the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$. The combined fit leads to a better determination of the two cross sections per fission: $\sigma_{f,235} = 6.29 \pm 0.08$ and $\sigma_{f,239} = 4.24 \pm 0.21$ in units of 10^{-43} cm²/fission, with respective uncertainties of about 1.2% and 4.9%. Since the respective deviations from the theoretical cross sections per fission are 2.5 σ and 0.7 σ , we conclude that, if the reactor antineutrino anomaly is not due to active-sterile neutrino oscillations, it is likely that it can be solved with a revaluation of the 235 U reactor antineutrino flux. However, the ²³⁸U, ²³⁹Pu, and ²⁴¹Pu fluxes, which have larger uncertainties, could also be significantly different from the theoretical predictions.

DOI: [10.1103/PhysRevD.96.033005](https://doi.org/10.1103/PhysRevD.96.033005)

The flux of electron antineutrinos produced in nuclear reactors is generated by the β decays of the fission products of 235 U, 238 U, 239 Pu, and 241 Pu. The 2011 recalculation [\[1,2\]](#page-3-0) of the four fluxes led to the discovery of the reactor antineutrino anomaly [\[3\]](#page-3-1), which is a deficit of the rate of electron antineutrinos measured in several reactor neutrino experiments. There are two known possible explanations of the reactor antineutrino anomaly: (1) a miscalculation of one or more of the four electron antineutrino fluxes [\[4,5\]](#page-3-2) and (2) active-sterile neutrino oscillations (see Ref. [\[6\]](#page-3-3) and references therein). In this paper, we consider the first possibility and we present an improvement of the results presented in Refs. [\[4,5\]](#page-3-2) on the determination of the cross sections per fission $\sigma_{f,235}$ and $\sigma_{f,239}$, which are, respectively, the integrals of the products of the 235 U and 239 Pu electron antineutrino fluxes and the detection cross section [see Eq. [\(8\)](#page-1-0) of Ref. [\[3\]](#page-3-1)].

The cross section per fission $\sigma_{f,235}$ of the ²³⁵U electron antineutrino flux was determined in Ref. [\[4\]](#page-3-2) with a fit of the reactor rates by taking into account the different fuel compositions. Recently the Daya Bay Collaboration presented a determination of $\sigma_{f,235}$ and $\sigma_{f,239}$ obtained by measuring the correlations between the reactor core fuel evolution and the changes in the reactor antineutrino flux and energy spectrum [\[5\].](#page-3-4) In this paper we present a combined fit of the reactor rates and the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ which leads to a better determination of both cross sections per fission.

In the analysis of the reactor rates, we consider the theoretical ratios [\[4\]](#page-3-2)

$$
R_a^{\text{th}} = \frac{\sum_k f_k^a r_k \sigma_{f,k}^{\text{SH}}}{\sum_k f_k^a \sigma_{f,k}^{\text{SH}}},\tag{1}
$$

where f_k^a is the antineutrino flux fraction from the fission of the isotope with atomic mass k and the coefficient r_k is the corresponding correction of the theoretical cross section per fission $\sigma_{f,k}^{\text{SH}}$ which is needed to fit the data ($k = 235, 238$, 239, 241, denotes, respectively, the ²³⁵U, ²³⁸U, ²³⁹Pu, ²⁴¹Pu electron antineutrino fluxes). The theoretical cross sections per fission $\sigma_{f,k}^{\text{SH}}$ are the Saclay + Huber (SH) [\[2,3\]](#page-3-5) cross sections per fission listed in Table 1 of Ref. [\[4\].](#page-3-2) The index a labels the reactor neutrino experiments listed in Table 1 of Ref. [\[6\]:](#page-3-3) Bugey-4 [\[7\]](#page-3-6), Rovno91 [\[8\],](#page-3-7) Bugey-3 [\[9\]](#page-3-8), Gosgen [\[10\]](#page-3-9), ILL [\[11,12\]](#page-3-10), Krasnoyarsk87 [\[13\]](#page-3-11), Krasnoyarsk94 [\[14,15\]](#page-3-12), Rovno88 [\[16\]](#page-3-13), SRP [\[17\],](#page-3-14) Nucifer [\[18\],](#page-3-15) Chooz [\[19\]](#page-3-16), Palo Verde [\[20\]](#page-3-17), Daya Bay [\[21\],](#page-3-18) RENO [\[22\],](#page-3-19) and Double Chooz [\[23\].](#page-3-20)

We analyze the data of the reactor rates with the leastsquares statistic

$$
\chi_{\mathcal{R}}^{2} = \sum_{a,b} (R_{a}^{\text{th}} - R_{a}^{\text{exp}})(V_{\mathcal{R}}^{-1})_{ab} (R_{b}^{\text{th}} - R_{b}^{\text{exp}})
$$

$$
+ \sum_{k=238,241} \left(\frac{1 - r_{k}}{\Delta r_{k}}\right)^{2}, \tag{2}
$$

where R_a^{exp} are the measured reactor rates listed in Table 1 of Ref. [\[6\]](#page-3-3) and V_R is the covariance matrix constructed with the corresponding uncertainties. The second term in Eq. [\(2\)](#page-0-0) serves to keep under control the variation of the rates of the minor fissionable isotopes ²³⁸U and ²⁴¹Pu, which are not well determined by the fit [\[4\]](#page-3-2). We consider $\Delta r_{238} = 15\%$ and $\Delta r_{241} = 10\%$, which are significantly larger than the nominal theoretical uncertainties (respectively, 8.15% and 2.15% [\[2,3\]](#page-3-5)) and the 5% estimate in Ref. [\[24\]](#page-3-21).

The fit of the data gives $(\chi^2_R)_{\text{min}} = 17.7$ with 22 degrees of freedom, which correspond to an excellent 72% good-ness of fit. Figure [1](#page-1-1) shows the marginal $\Delta \chi^2_{\rm R} = \chi^2_{\rm R} - (\chi^2_{\rm R})_{\rm min}$ for the coefficients r_k of the four antineutrino fluxes, for which we obtain

FIG. 1. Marginal $\Delta \chi^2_{\rm R} = \chi^2_{\rm R} - (\chi^2_{\rm R})_{\rm min}$ for the coefficients r_k of the four antineutrino fluxes obtained from the fit of the reactor rates.

$$
r_{235} = 0.950 \pm 0.014,\tag{3}
$$

$$
r_{238} = 1.009 \pm 0.147, \tag{4}
$$

$$
r_{239} = 0.869 \pm 0.097, \tag{5}
$$

$$
r_{241} = 1.005 \pm 0.100. \tag{6}
$$

These values and Fig. [1](#page-1-1) are different from the corresponding ones in Ref. [\[4\],](#page-3-2) because of the different second term in Eq. [\(2\)](#page-0-0) with respect to that in Eq. [\(8\)](#page-1-0) of Ref. [\[4\]](#page-3-2), which constrained all the r_k 's. The best-fit values and uncertainties of $\sigma_{f,235}$ and $\sigma_{f,239}$ are given in the second column of Table [I](#page-1-2). The value of $\sigma_{f,235}$ is determined by the fit with a precision of about 1.4% and differs from the theoretical value $\sigma_{f,235}^{\text{SH}}$ by 2.0 σ . This confirms the necessity of a revaluation of the theoretical value of $\sigma_{f,235}$ found in Ref. [\[4\].](#page-3-2) The value of $\sigma_{f,239}$ is also determined by the fit, but with the worse precision of about 11.2%, which

TABLE I. Comparison of the theoretical Saclay $+$ Huber (SH) values of the cross sections per fission $\sigma_{f,235}$ and $\sigma_{f,239}$ with those obtained from the fit of the reactor rates, from the Daya Bay data [\[5\],](#page-3-4) and from the combined fit. The units are 10^{-43} cm²/fission.

SH	Reactor Rates Daya Bay Combined		
	$\sigma_{f,235}$ 6.69 ± 0.14 6.35 ± 0.09 6.17 ± 0.17 6.29 ± 0.08		
$\sigma_{f,239}$ 4.40 \pm 0.11	3.82 ± 0.43	4.27 ± 0.26 4.24 ± 0.21	

renders it compatible with the theoretical value $\sigma_{f,239}^{SH}$ within 1.3σ .

In order to take into account the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ [\[5\]](#page-3-4), we consider the least-squares statistic

$$
\chi_{\text{tot}}^2 = \tilde{\chi}_{\text{R}}^2 + \sum_{k,j=235,239} (\sigma_{f,k}^{\text{th}} - \sigma_{f,k}^{\text{DB}})(V_{\text{DB}}^{-1})_{kj} (\sigma_{f,j}^{\text{th}} - \sigma_{f,j}^{\text{DB}}),
$$
\n(7)

where $\tilde{\chi}_{\rm R}^2$ is given by Eq. [\(2\)](#page-0-0) without considering the Daya Bay rate [\[21\],](#page-3-18) in order to avoid considering the Daya Bay data twice. The cross sections per fission $\sigma_{f,235}^{DB}$ and $\sigma_{f,239}^{DB}$ are those measured in Daya Bay [\[5\]](#page-3-4) and listed in the third column of Table [I](#page-1-2). We obtained the Daya Bay covariance matrix V_{DB} with a Gaussian approximation of the χ^2 distribution in Fig. 3 of Ref. [\[5\]](#page-3-4). The theoretical cross sections per fission $\sigma_{f,k}^{\text{th}}$ are given by

$$
\sigma_{f,k}^{\text{th}} = r_k \sigma_{f,k}^{\text{SH}},\tag{8}
$$

with the same coefficients r_k that are present in the definition of R_a^{th} in Eq. [\(1\)](#page-0-1).

The minimization of χ^2_{tot} gives $(\chi^2_{\text{tot}})_{\text{min}} = 19.5$ with 23 degrees of freedom, which correspond to a 67% goodness of fit, which is practically as good as that obtained in the analysis of the reactor rates with χ^2 χ^2 in Eq. [\(2\).](#page-0-0) Figure 2 shows the marginal $\Delta \chi^2_{\text{tot}} = \chi^2_{\text{tot}} - (\chi^2_{\text{tot}})_{\text{min}}$ for the coefficients r_k of the four antineutrino fluxes, for which we obtain

FIG. 2. Marginal $\Delta \chi^2_{\text{tot}} = \chi^2_{\text{tot}} - (\chi^2_{\text{tot}})_{\text{min}}$ for the coefficients r_k of the four antineutrino fluxes obtained from the fit of the reactor rates and the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ [\[5\].](#page-3-4)

$$
r_{235} = 0.940 \pm 0.011,\tag{9}
$$

$$
r_{238} = 0.906 \pm 0.103,\tag{10}
$$

$$
r_{239} = 0.964 \pm 0.047, \tag{11}
$$

$$
r_{241} = 0.983 \pm 0.097. \tag{12}
$$

The corresponding best-fit values and uncertainties of $\sigma_{f,235}$ and $\sigma_{f,239}$ are given in the fourth column of Table [I](#page-1-2). The value of $\sigma_{f,235}$ is determined by the fit with a precision which is slightly better than that obtained from the fit of the reactor rates, and significantly better than the precision of the Daya Bay measurement [\[5\]](#page-3-4). The combined fit results in a substantial improvement of the precision of the determination of $\sigma_{f,239}$ with respect to the fit of the reactor rates alone: the value of $\sigma_{f,239}$ is determined with a precision of about 4.9%, which is also better than that of the Daya Bay measurement [\[5\].](#page-3-4) Since the deviation from the theoretical value $\sigma_{f,239}^{SH}$ is only of 0.7 σ , there is no compelling necessity of a revaluation of its theoretical value.

Figure [3](#page-2-0) shows the correlation between the determinations of $\sigma_{f,235}$ and $\sigma_{f,239}$. The values of $\sigma_{f,235}$ and $\sigma_{f,239}$

FIG. 3. Allowed regions in the $\sigma_{f,235} - \sigma_{f,239}$ plane obtained from the combined fit of the reactor rates and the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ [\[5\].](#page-3-4) The red, blue, and black curves enclose, respectively, the allowed regions obtained from the fit of the reactor rates, the allowed regions corresponding to the Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ [\[5\]](#page-3-4), and the theoretical Saclay + Huber allowed regions at 1σ (solid), 2σ (dashed), and 3σ (dotted). The best-fit points are indicated by crosses.

obtained from the fit of the reactor rates are slightly anticorrelated, whereas the Daya Bay values are significantly correlated and have a larger uncertainty for $\sigma_{f,235}$ and smaller uncertainty for $\sigma_{f,239}$. The combined fit results in an allowed region with practically uncorrelated values of $\sigma_{f,235}$ and $\sigma_{f,239}$ and significantly smaller uncertainties.

The 2.5 σ deviation of $\sigma_{f,235}$ from the theoretical $Saclay + Huber [2,3] cross sections per fission confirms$ $Saclay + Huber [2,3] cross sections per fission confirms$ $Saclay + Huber [2,3] cross sections per fission confirms$ the indications obtained in Refs. [\[4,5\]](#page-3-2) that the reactor antineutrino anomaly is most probably mainly due to the $235U$ electron antineutrino flux (if is not due to active-sterile neutrino oscillations). This possibility may be connected with a ²³⁵U origin of the 5 MeV bump of the reactor antineutrino spectrum measured in the RENO [\[25,26\]](#page-3-22), Double Chooz [\[27\],](#page-3-23) Daya Bay [\[21\],](#page-3-18) and NEOS [\[28\]](#page-3-24) experiments, as indicated by the analysis in Ref. [\[29\]](#page-3-25) and by the hint of a correlation in the RENO experiment [\[22\]](#page-3-19). The new reactor experiments PROSPECT [\[30\],](#page-3-26) SoLid [\[31\]](#page-3-27), and STEREO [\[32\]](#page-3-28) which are in preparation for the search of short-baseline neutrino oscillations with highly enriched ²³⁵U research reactors, will improve the determination of the ²³⁵U electron antineutrino flux.

Since the 238 U and 241 Pu fuel composition in power reactors is small (see Table 1 of Ref. [\[6\]\)](#page-3-3), the antineutrino data do not give precise information on the corresponding cross sections per fission. From Fig. [2](#page-1-3) one can see that $r_{238} = 0.906 \pm 0.103$ and $r_{241} = 0.983 \pm 0.097$. Hence, there is an indication that $\sigma_{f,238}$ may be substantially smaller than the theoretical $\sigma_{f,238}^{SH}$ value, but the discrepancy is less than 1σ . On the other hand, the fit favors a value of $\sigma_{f,241}$ close to the theoretical $\sigma_{f,241}^{SH}$ value, but the uncertainty is large.

The calculations of the 235 U, 239 Pu, and 241 Pu antineutrino fluxes were performed through the inversion of the corresponding electron spectra measured at ILL in the 80's [\[33,34\]](#page-3-29). A possible explanation of the discrepancy between the calculated and measured values of $\sigma_{f,235}$ alone could be some unknown systematic error in the measurement of the ²³⁵U electron spectrum which was not present in the measurements of the 239 Pu and 241 Pu electron spectra. It is clear that it would be very important to check these measurements with new experiments.

In conclusion, we performed a combined fit of the reactor antineutrino rates [\[4\]](#page-3-2) and the recent Daya Bay measurement of $\sigma_{f,235}$ and $\sigma_{f,239}$ [\[5\].](#page-3-4) The combined fit leads to the better determination of $\sigma_{f,235}$ and $\sigma_{f,239}$ in Table [I,](#page-1-2) with respective uncertainties of about 1.2% and 4.9%. The respective deviations from the theoretical Saclay + Huber [\[2,3\]](#page-3-5) cross sections per fission are 2.5σ and 0.7σ . Therefore, we confirm the conclusion already reached in Refs. [\[4,5\]](#page-3-2) that the 235 U reactor antineutrino flux is the most probable main contributor to the reactor antineutrino anomaly [\[3\]](#page-3-1) if the anomaly is not due to active-sterile neutrino oscillations. However, also the ²³⁹Pu flux, which is constrained by the cross section per fission in Table [I](#page-1-2), and the 238 U and 241 Pu fluxes, for which the data do not provide stringent constraints, could be significantly different from the theoretical predictions. Let us finally emphasize that the knowledge of the reactor antineutrino fluxes is useful not only for applications in fundamental physics research, but also for practical applications as antineutrino monitoring of reactors (see Refs. [35–[37\]\)](#page-3-30).

- [1] T. A. Mueller et al., Phys. Rev. C 83[, 054615 \(2011\)](https://doi.org/10.1103/PhysRevC.83.054615).
- [2] P. Huber, Phys. Rev. C **84**[, 024617 \(2011\).](https://doi.org/10.1103/PhysRevC.84.024617)
- [3] G. Mention et al., Phys. Rev. C 83[, 073006 \(2011\)](https://doi.org/10.1103/PhysRevD.83.073006).
- [4] C. Giunti, [Phys. Lett. B](https://doi.org/10.1016/j.physletb.2016.11.028) 764, 145 (2017).
- [5] F. P. An et al. (Daya Bay Collaboration), [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.118.251801) 118[, 251801 \(2017\).](https://doi.org/10.1103/PhysRevLett.118.251801)
- [6] S. Gariazzo, C. Giunti, M. Laveder, and Y. Li, [J. High](https://doi.org/10.1007/JHEP06(2017)135) [Energy Phys. 06 \(2017\) 135.](https://doi.org/10.1007/JHEP06(2017)135)
- [7] Y. Declais et al. (Bugey Collaboration), [Phys. Lett. B](https://doi.org/10.1016/0370-2693(94)91394-3) 338, [383 \(1994\)](https://doi.org/10.1016/0370-2693(94)91394-3).
- [8] A. Kuvshinnikov, L. Mikaelyan, S. Nikolaev, M. Skorokhvatov, and A. Etenko, JETP Lett. 54, 253 (1991).
- [9] B. Achkar et al. (Bugey Collaboration), [Nucl. Phys.](https://doi.org/10.1016/0550-3213(94)00513-E) **B434**, [503 \(1995\)](https://doi.org/10.1016/0550-3213(94)00513-E).
- [10] G. Zacek et al. (CalTech-SIN-TUM Collaboration), [Phys.](https://doi.org/10.1103/PhysRevD.34.2621) Rev. D 34[, 2621 \(1986\).](https://doi.org/10.1103/PhysRevD.34.2621)
- [11] H. Kwon, F. Boehm, A. A. Hahn, H. E. Henrikson, J.-L. Vuilleumier, J.-F. Cavaignac, D. H. Koang, B. Vignon, F. v. Feilitzsch, and R. L. Mössbauer, Phys. Rev. D 24[, 1097 \(1981\).](https://doi.org/10.1103/PhysRevD.24.1097)
- [12] A. Hoummada, S. Lazrak Mikou, G. Bagieu, J. Cavaignac, and D. Holm Koang, [Appl. Radiat. Isot.](https://doi.org/10.1016/0969-8043(95)00048-8) 46, 449 (1995).
- [13] G. S. Vidyakin et al. (Krasnoyarsk Collaboration), Sov. Phys. JETP 66, 243 (1987).
- [14] G. S. Vidyakin et al. (Krasnoyarsk Collaboration), Sov. Phys. JETP 71, 424 (1990).
- [15] G. S. Vidyakin et al. (Krasnoyarsk Collaboration), JETP Lett. 59, 390 (1994).
- [16] A. I. Afonin et al., Sov. Phys. JETP 67, 213 (1988).
- [17] Z.D. Greenwood *et al.*, *Phys. Rev. D* 53[, 6054 \(1996\)](https://doi.org/10.1103/PhysRevD.53.6054).
- [18] G. Boireau et al. (NUCIFER Collaboration), [Phys. Rev. D](https://doi.org/10.1103/PhysRevD.93.112006) 93[, 112006 \(2016\).](https://doi.org/10.1103/PhysRevD.93.112006)
- [19] M. Apollonio et al. (CHOOZ Collaboration), [Eur. Phys. J. C](https://doi.org/10.1140/epjc/s2002-01127-9) 27[, 331 \(2003\).](https://doi.org/10.1140/epjc/s2002-01127-9)
- [20] F. Boehm et al. (Palo Verde Collaboration), [Phys. Rev. D](https://doi.org/10.1103/PhysRevD.64.112001) 64, [112001 \(2001\).](https://doi.org/10.1103/PhysRevD.64.112001)
- [21] F. An et al. (Daya Bay Collaboration), [Chin. Phys. C](https://doi.org/10.1088/1674-1137/41/1/013002) 41, [013002 \(2017\).](https://doi.org/10.1088/1674-1137/41/1/013002)
- [22] H. Seo, AAP 2016, Applied Antineutrino Physics, 2016, Liverpool, UK (unpublished).
- [23] Double Chooz Collaboration (private communication).
- [24] A. C. Hayes and P. Vogel, [Annu. Rev. Nucl. Part. Sci.](https://doi.org/10.1146/annurev-nucl-102115-044826) 66, [219 \(2016\)](https://doi.org/10.1146/annurev-nucl-102115-044826).
- [25] S.-H. Seo (RENO Collaboration), [AIP Conf. Proc.](https://doi.org/10.1063/1.4915563) 1666, [080002 \(2015\).](https://doi.org/10.1063/1.4915563)
- [26] J. Choi et al. (RENO Collaboration), [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.116.211801) 116, [211801 \(2016\).](https://doi.org/10.1103/PhysRevLett.116.211801)
- [27] Y. Abe et al. (Double Chooz Collaboration), [J. High Energy](https://doi.org/10.1007/JHEP10(2014)086) [Phys. 10 \(2014\) 086;](https://doi.org/10.1007/JHEP10(2014)086) [02 \(2015\) 74\(E\).](https://doi.org/10.1007/JHEP02(2015)074)
- [28] Y. Ko et al. (NEOS Collaboration), [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.118.121802) 118, [121802 \(2017\).](https://doi.org/10.1103/PhysRevLett.118.121802)
- [29] P. Huber, Phys. Rev. Lett. **118**[, 042502 \(2017\).](https://doi.org/10.1103/PhysRevLett.118.042502)
- [30] J. Ashenfelter et al. (PROSPECT Collaboration), [J. Phys. G](https://doi.org/10.1088/0954-3899/43/11/113001) 43[, 113001 \(2016\).](https://doi.org/10.1088/0954-3899/43/11/113001)
- [31] N. Ryder (SoLid Collaboration), Proc. Sci., EPS-HEP2015 (2015) 071 [[arXiv:1510.07835\].](http://arXiv.org/abs/1510.07835)
- [32] V. Helaine (STEREO Collaboration), [arXiv:1604.08877.](http://arXiv.org/abs/1604.08877)
- [33] K. Schreckenbach, G. Colvin, W. Gelletly, and F. Von Feilitzsch, Phys. Lett. 160B[, 325 \(1985\).](https://doi.org/10.1016/0370-2693(85)91337-1)
- [34] A. A. Hahn, K. Schreckenbach, W. Gelletly, F. von Feilitzsch, G. Colvin, and B. Krusche, [Phys. Lett. B](https://doi.org/10.1016/0370-2693(89)91598-0) 218, [365 \(1989\)](https://doi.org/10.1016/0370-2693(89)91598-0).
- [35] A. C. Hayes, H. R. Trellue, M. M. Nieto, and W. B. WIlson, Phys. Rev. C 85[, 024617 \(2012\).](https://doi.org/10.1103/PhysRevC.85.024617)
- [36] E. Christensen, P. Huber, P. Jaffke, and T. Shea, [Phys. Rev.](https://doi.org/10.1103/PhysRevLett.113.042503) Lett. 113[, 042503 \(2014\)](https://doi.org/10.1103/PhysRevLett.113.042503).
- [37] A. C. Hayes, [Rep. Prog. Phys.](https://doi.org/10.1088/1361-6633/80/2/026301) **80**, 026301 (2017).