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Previous studies of a three family Yukawa unified supersymmetric (SUSY) grand unified theory with SO(10) or Pati-Salam (PS) gauge symmetry proposed by Raby and students show that this model is able to fit low energy and inflation observables. However, the fit to low energy observables is not great especially for $\sin 2\beta$, and up and down quark masses. In this paper, we show that by choosing PS as the gauge group and modifying the Yukawa sector, the low energy fit improves significantly while other qualities of the model are maintained. In particular, the lightest SUSY particle is the neutralino with mass of order 300–500 GeV, the lightest stop and sbottom have mass of order 3–5 TeV, and the CP -odd Higgs mass is of order 5–6 TeV, so we are in the decoupling limit for the light Higgs boson. In addition, we reinterpret gluino simplified model analyses by the ATLAS and CMS collaborations and find that the most stringent gluino mass bound for our model is $M_{\tilde{g}} \sim 1.9$ TeV. The current best fit point, consistent with this bound, with gluino mass $M_{\tilde{g}} = 1.9$ TeV has $\chi^2/\text{dof} \approx 1.12$, compared to the best fit point of the previous model with $\chi^2/\text{dof} = 1.90$. We find that predictions for the electric dipole moment of the electron, the branching ratio $\text{BR}(\mu \rightarrow e\gamma)$ and the CP violating angle in the lepton sector, $\sin \delta$, are affected significantly as compared to previous results. In summary, we are unable to rule out this model or place an upper bound on gluino mass accessible by this run of the LHC because the χ^2/dof of this model is well below 2σ even for a gluino mass as high as 2.7 TeV. On the bright side, this means that this model is still viable and we might find low energy SUSY particles in the near future.

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I. INTRODUCTION

Supersymmetric grand unified theories (SUSY GUTs) are highly constrained, yet very natural extensions of the standard model (SM). To maintain the possibility of deriving a SUSY GUT from a more fundamental theory such as heterotic string theory, we are interested in SUSY GUTs without large GUT representations. In particular, this paper discusses a complete three family Yukawa unified SUSY GUT model with either SO(10) or Pati-Salam (PS) $SU(4)_C \times SU(2)_L \times SU(2)_R$ gauge symmetry and a $D_3 \times [U(1) \times \mathbb{Z}_2 \times \mathbb{Z}_3]$ family symmetry.¹ Previous analyses showed that this model fits reasonably well to low energy observables such as gauge couplings, gauge boson masses, fermion masses, Cabibbo-Kobayashi-Maskawa (CKM) matrix elements, neutrino mass differences and mixing angles [3–6]. In addition, by including an inflation sector in the PS model, this model can fit the tensor-to-scalar ratio, the scalar spectral index, and the scalar power spectrum [7].

Despite the success of this model, as the lower bound on the gluino mass increases, the best chi-squared χ^2 fit of this

model to low energy observables is forced to have a chi-squared per degree of freedom $\chi^2/\text{dof} = 1.90$ [6]. The main contributions to such a large χ^2/dof are the poor fits (with pull $\gtrsim 3$) to $\sin 2\beta$, and the up and down quark masses, m_u, m_d . Another major crisis for the model is that supersymmetric partners have not been observed and the most stringent gluino mass bound of a simplified model is $M_{\tilde{g}} \sim 1.9$ TeV [8]. This leads to the question of what the gluino mass bound is for this model. Is this model already ruled out by this bound? If not, can this model be tested from this run of the LHC? To answer these questions, recent ATLAS and CMS analyses in signal regions with high jet and b -jet multiplicity, leptons, and missing transverse momentum are reinterpreted based on this model.

The primary goal of this paper is to show that by modifying only the Yukawa sector of the model, the low energy fits can be improved significantly from a $\chi^2/\text{dof} \geq 2.2$ for $M_{\tilde{g}} = 1.6$ TeV [6] to a $\chi^2/\text{dof} = 1.12$ for $M_{\tilde{g}} = 1.9$ TeV. In addition, we also found that the most recent ATLAS and CMS data require that $M_{\tilde{g}} \gtrsim 1.9$ TeV. For more details on the model, the analysis procedure and the phenomenology aspects of the model, please refer to the following references: [3–6,9,10].

The rest of the paper is organized as follows. In Sec. II, the superpotential of the Yukawa sector of this model along with the Yukawa matrices are given. We show explicitly the differences between the Yukawa sector of this model and that

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¹The PS model that we consider in this paper is a GUT because it can be obtained from orbifolding a higher dimensional GUT [1,2].

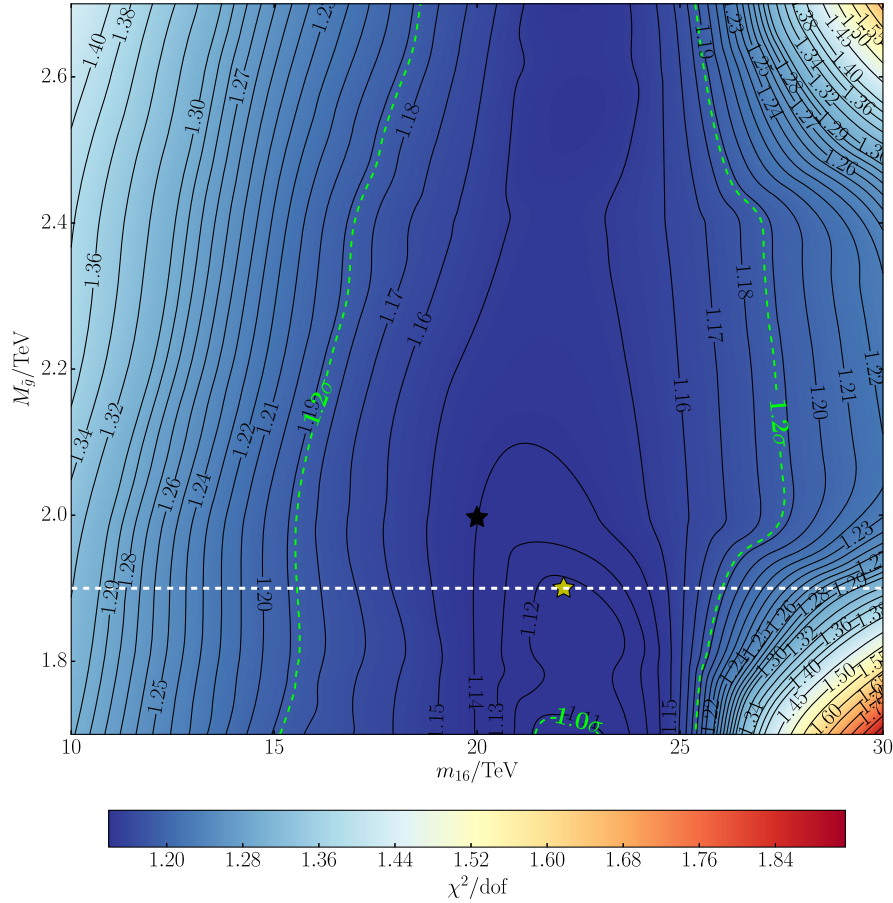


FIG. 1. A plot of the χ^2/dof contour lines as a function of gluino mass, $M_{\tilde{g}}$, and the universal scalar mass at the GUT scale, m_{16} . The numbers on the black contour lines are χ^2/dof while the green dotted lines are the 1.0 and 1.2 σ bound from the χ^2 analysis with 27 dof. This plot has 27 dof because m_{16} and $M_{1/2}$ are fixed as the x and y axis. The horizontal white dotted line is the current gluino mass bound of our model; see Sec. IV. The yellow star is the point with the lowest χ^2 for gluino mass above the current bound. The black star is a benchmark point where its input parameters and low energy fits are shown in the appendix. Since the global χ^2 minimum is below the lower limit of the plot, our model prefers low gluino mass. However, this plot also shows that our model is not very sensitive to the gluino mass, because χ^2 increases relatively slowly as the gluino mass increases.

in previous analyses, and provide some insight on why the modification to the superpotential can improve the low energy fit. The procedure and the results of a global χ^2 analysis of fitting low energy observables are presented in Sec. III. Our analysis shows that a huge region in the scalar mass and gluino mass parameter space is $< 1.2\sigma$. Hence, this model is not ruled out by the data. In Sec. IV, we reinterpret the ATLAS and CMS gluino simplified model analyses to obtain the current gluino mass bounds of this model. The gluino mass bound for our model is $M_{\tilde{g}} \sim 1.9$ TeV, which also provides the best fit point (see Fig. 1). Finally, the discovery prospects and predictions of this model are discussed in Sec. V and we conclude in Sec. VI.

II. MODEL

The complete three family Yukawa unified SUSY GUT that some of the present authors studied extensively has a

SO(10) gauge symmetry with a $D_3 \times [\text{U}(1) \times \mathbb{Z}_2 \times \mathbb{Z}_3]$ family symmetry [3–6,10]. In this paper we focus solely on the Yukawa sector as the other sectors of the model such as the right-handed neutrino sector are identical to previous analyses. The Yukawa sector superpotential of this model is

$$W = \lambda \mathbf{16}_3 \mathbf{10} \mathbf{16}_3 + \mathbf{16}_a \mathbf{10} \chi_a + \bar{\chi}_a \left(M_\chi \chi_a + 45 \frac{\phi_a}{M} \mathbf{16}_3 + 45 \frac{\tilde{\phi}_a}{M} \mathbf{16}_a + \mathbf{A} \mathbf{16}_a \right), \quad (1)$$

where $\mathbf{16}_i$ is the spinor representation of SO(10), which contains a family of fermions and their supersymmetric partners, and $i = 1, 2, 3$ is the family index. $\mathbf{16}_3$ is a singlet under D_3 symmetry, while $\mathbf{16}_a$, $a = 1, 2$ are doublets under D_3 symmetry. $\mathbf{10}$ is the ten-dimensional representation of SO(10), which contains a pair of Higgs doublets. 45 is the

adjoint representation of $SO(10)$ that is assumed to obtain vacuum expectation value (VEV) in the $\mathbf{B} - \mathbf{L}$ direction. χ_a and $\bar{\chi}_a$ for $a = 1, 2$ are Froggatt-Neilson states [11] and are doublets under D_3 symmetry. \hat{M} is trivial under all groups while $M_\chi = M_0(1 + \alpha\mathbf{X} + \beta\mathbf{Y})$, where \mathbf{X} and \mathbf{Y} are generators of $SO(10)$, and α and β are some constant. \mathbf{A} is a $SO(10)$ singlet “flavon” field and a nontrivial singlet under D_3 symmetry. Finally, ϕ_a and $\tilde{\phi}_a$ are $SO(10)$ singlet flavon fields, which are assumed to obtain VEVs of the form

$$\langle \phi_a \rangle = \begin{pmatrix} \phi_a \\ \phi_b \end{pmatrix}, \quad \langle \tilde{\phi}_a \rangle = \begin{pmatrix} 0 \\ \tilde{\phi}_2 \end{pmatrix}. \quad (2)$$

After integrating out the Froggatt-Neilson states, χ_a and $\bar{\chi}_a$, and defining

$$G_{x,y} = \frac{M_0}{M_\chi} = \frac{1}{1 + \alpha x + \beta y}, \quad (3)$$

along with

$$G_{x_1,y_1;x_2,y_2}^\pm = G_{x_1,y_1} \pm G_{x_2,y_2}, \quad (4)$$

where x and y are the eigenvalues of \mathbf{X} and \mathbf{Y} , we obtain the following Yukawa matrices,²

$$Y_u = \begin{pmatrix} 0 & \epsilon' G_{1,-\frac{4}{3},1,\frac{1}{3}}^- & -\epsilon \xi G_{1,-\frac{4}{3}} \\ -\epsilon' G_{1,-\frac{4}{3},1,\frac{1}{3}}^- & \tilde{\epsilon} G_{1,-\frac{4}{3},1,\frac{1}{3}}^- & -\epsilon G_{1,-\frac{4}{3}} \\ \epsilon \xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \quad (5)$$

$$Y_d = \begin{pmatrix} 0 & \epsilon' G_{-3,\frac{2}{3},1,\frac{1}{3}}^- & -\epsilon \xi G_{-3,\frac{2}{3}} \\ -\epsilon' G_{-3,\frac{2}{3},1,\frac{1}{3}}^- & \tilde{\epsilon} G_{-3,\frac{2}{3},1,\frac{1}{3}}^- & -\epsilon G_{-3,\frac{2}{3}} \\ \epsilon \xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \quad (6)$$

$$Y_e = \begin{pmatrix} 0 & -\epsilon' G_{-3,-1;1,2}^- & 3\epsilon \xi G_{1,2} \\ \epsilon' G_{-3,-1;1,2}^- & 3\tilde{\epsilon} G_{-3,-1;1,2}^- & 3\epsilon G_{1,2} \\ -3\epsilon \xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix}, \quad (7)$$

$$Y_\nu = \begin{pmatrix} 0 & -\epsilon' G_{-3,-1;5,0}^- & 3\epsilon \xi G_{5,0} \\ \epsilon' G_{-3,-1;5,0}^- & 3\tilde{\epsilon} G_{-3,-1;5,0}^- & 3\epsilon G_{5,0} \\ -3\epsilon \xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix}, \quad (8)$$

where

²In previous analyses, we took the limit of $\alpha \gg \beta$ in $G_{x,y}$ [5,6]. This limit simplifies the interpretation of the Yukawa matrices but does not reduce the number of input parameters. Since previous attempts in fitting low energy observables do not produce a good fit, we have decided to include the full $G_{x,y}$ in this analysis.

$$\epsilon = -\frac{1}{6} \frac{M_G \phi_1}{M_0 \hat{M}}, \quad (9)$$

$$\tilde{\epsilon} = +\frac{1}{6} \frac{M_G \tilde{\phi}_2}{M_0 \hat{M}}, \quad (10)$$

$$\epsilon' = -\frac{1}{2} \frac{A}{M_0}, \quad (11)$$

$$\xi = \frac{\phi_2}{\phi_1}. \quad (12)$$

Of these parameters, ϵ' , ξ , α and β are complex while λ , ϵ and $\tilde{\epsilon}$ are real. Instead of writing the superpotential in $SO(10)$ notation, we can rewrite it using PS fields,

$$\begin{aligned} W_{\text{PS}} = & \lambda Q_3 \mathcal{H} Q_3^c + Q_a \mathcal{H} F_a^c + F_a \mathcal{H} Q_a^c \\ & + \bar{F}_a^c \left(M_F F_a^c + 15 \frac{\phi_a}{\hat{M}} Q_3^c + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a^c + \mathbf{A} Q_a^c \right) \\ & + \bar{F}_a \left(M_F F_a + 15 \frac{\phi_a}{\hat{M}} Q_3 + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a + \mathbf{A} Q_a \right), \end{aligned} \quad (13)$$

where $\{Q_i, F_a\} = (4, 2, 1)$, $\{Q_i^c, F_a^c\} = (\bar{4}, 1, \bar{2})$ and $\mathcal{H} = (1, 2, \bar{2})$ under PS symmetry. 15 is the adjoint representation of $SU(4)_c$ that is assumed to obtain VEV in the $\mathbf{B} - \mathbf{L}$ direction. In addition, \bar{F}_a and \bar{F}_a^c are the conjugate of F_a and F_a^c , and $M_F = M_\chi$. By requiring a PS instead of a $SO(10)$ gauge symmetry, we have more freedom in adding new terms to the superpotential.

In previous global χ^2 analyses, $\sin 2\beta$ is too small while m_u and m_d are too large [5,6]. In this analysis, we find that changing ϵ' to a complex parameter and $\tilde{\epsilon}$ to a real parameter produces a much better fit for $\sin 2\beta$ (see Sec. III).³ To improve the fit of m_u and m_d , we introduce the following terms to the superpotential⁴:

$$\bar{F}_a^c \Theta' Q_a^c + \bar{F}_a \Theta' Q_a + \bar{F}_a^c \tilde{\Theta}_a Q_a^c - \bar{F}_a \tilde{\Theta}_a Q_a, \quad (14)$$

where Θ' transforms as a trivial singlet and $\tilde{\Theta}_a$, $a = 1, 2$ transforms as doublets under D_3 symmetry. In addition, we assume that $\tilde{\Theta}_a$ obtains a VEV of the form

$$\langle \tilde{\Theta}_a \rangle = \begin{pmatrix} \tilde{\Theta}_1 \\ 0 \end{pmatrix}, \quad (15)$$

³In previous analyses, $\tilde{\epsilon}$ is a complex parameter and ϵ' is a real parameter.

⁴By adding only the Θ' terms, we are able to fit m_u and modestly improve the fit of m_d . Having both the Θ' and $\tilde{\Theta}$ terms significantly improves the fit of both m_u and m_d .

and both Θ' and $\tilde{\Theta}_1$ are real parameters. With these terms, the Yukawa sector superpotential of this model is

$$\begin{aligned}
W_{\text{PS}} = & \lambda Q_3 \mathcal{H} Q_3^c + Q_a \mathcal{H} F_a^c + F_a \mathcal{H} Q_a^c \\
& + \bar{F}_a^c \left(M_F F_a^c + \mathbf{15} \frac{\phi_a}{\bar{M}} Q_3^c + \mathbf{15} \frac{\tilde{\phi}_a}{\bar{M}} Q_a^c + \mathbf{A} Q_a^c + \Theta' Q_a^c + \tilde{\Theta}_a Q_a^c \right) \\
& + \bar{F}_a \left(M_F F_a + \mathbf{15} \frac{\phi_a}{\bar{M}} Q_3 + \mathbf{15} \frac{\tilde{\phi}_a}{\bar{M}} Q_a + \mathbf{A} Q_a + \Theta' Q_a - \tilde{\Theta}_a Q_a \right). \tag{16}
\end{aligned}$$

Notice that we want to have a PS gauge symmetry because of the last term in the last two lines of the above equation. With SO(10) gauge symmetry, we are unable to make these two terms have opposite sign without introducing a VEV in the $\mathbf{B} - \mathbf{L}$ direction. We find that when we introduce such a VEV, we are able to fit the electron mass, but both m_u and m_d are too large as in our previous analysis.

With the new terms in the Yukawa sector, the Yukawa matrices of this model become⁵

$$Y_u = \begin{pmatrix} -\tilde{\theta} G_{1,-\frac{4}{3};1,\frac{1}{3}}^- & \epsilon' G_{1,-\frac{4}{3};1,\frac{1}{3}}^- + \theta' G_{1,-\frac{4}{3};1,\frac{1}{3}}^+ & -\epsilon \xi G_{1,-\frac{4}{3}} \\ -\epsilon' G_{1,-\frac{4}{3};1,\frac{1}{3}}^- + \theta' G_{1,-\frac{4}{3};1,\frac{1}{3}}^+ & \tilde{\epsilon} G_{1,-\frac{4}{3};1,\frac{1}{3}}^- & -\epsilon G_{1,-\frac{4}{3}} \\ \epsilon \xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \tag{17}$$

$$Y_d = \begin{pmatrix} -\tilde{\theta} G_{-3,\frac{2}{3};1,\frac{1}{3}}^- & \epsilon' G_{-3,\frac{2}{3};1,\frac{1}{3}}^- + \theta' G_{-3,\frac{2}{3};1,\frac{1}{3}}^+ & -\epsilon \xi G_{-3,\frac{2}{3}} \\ -\epsilon' G_{-3,\frac{2}{3};1,\frac{1}{3}}^- + \theta' G_{-3,\frac{2}{3};1,\frac{1}{3}}^+ & \tilde{\epsilon} G_{-3,\frac{2}{3};1,\frac{1}{3}}^- & -\epsilon G_{-3,\frac{2}{3}} \\ \epsilon \xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \tag{18}$$

$$Y_e = \begin{pmatrix} \tilde{\theta} G_{-3,-1;1,2}^- & -\epsilon' G_{-3,-1;1,2}^- + \theta' G_{-3,-1;1,2}^+ & 3\epsilon \xi G_{1,2} \\ \epsilon' G_{-3,-1;1,2}^- + \theta' G_{-3,-1;1,2}^+ & 3\tilde{\epsilon} G_{-3,-1;1,2}^- & 3\epsilon G_{1,2} \\ -3\epsilon \xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix}, \tag{19}$$

$$Y_\nu = \begin{pmatrix} \tilde{\theta} G_{-3,-1;5,0}^- & -\epsilon' G_{-3,-1;5,0}^- + \theta' G_{-3,-1;5,0}^+ & 3\epsilon \xi G_{5,0} \\ \epsilon' G_{-3,-1;5,0}^- + \theta' G_{-3,-1;5,0}^+ & 3\tilde{\epsilon} G_{-3,-1;5,0}^- & 3\epsilon G_{5,0} \\ -3\epsilon \xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix}, \tag{20}$$

where

$$\theta' = -\frac{1}{2} \frac{\Theta'}{M_0}, \tag{21}$$

$$\tilde{\theta} = +\frac{1}{2} \frac{\tilde{\Theta}_1}{M_0}. \tag{22}$$

The GUT scale boundary conditions of our model are shown in Table I. They are the GUT scale M_G

⁵Notice that the neutrino Yukawa matrix elements are of the same order of magnitude as that of the charged fermions. The light neutrino masses are a result of the seesaw mechanism with hierarchical right-handed neutrino masses [3,5]. In our model $M_{R_1} \sim 10^9$ GeV, $M_{R_2} \sim 10^{11}$ GeV and $M_{R_3} \sim 10^{13}$ GeV.

(defined where $\alpha_1 = \alpha_2$), the gauge coupling $\alpha_G(M_G)$, and a GUT scale threshold correction ϵ_3 satisfying $\alpha_3(M_G) = \alpha_G(1 + \epsilon_3)$. The GUT scale threshold correction in a complete theory would result from the massive states at the GUT scale, but here is parametrized to fit the experimentally measured value of $\alpha_{\text{strong}}(M_Z)$. In addition, we have also parametrized the SUSY breaking sector with the soft SUSY breaking parameters. The soft SUSY breaking parameters of our model are universal scalar masses m_{16} , universal gaugino masses $M_{1/2}$, a universal trilinear coupling A_0 and nonuniversal Higgs masses m_{H_u} , m_{H_d} . This set of soft SUSY breaking parameters represents a minimal set of parameters needed for a robust electroweak symmetry breaking. In addition, our model also has 13 Yukawa texture parameters, three right-handed neutrino masses, and $\tan \beta$ and μ . All the

TABLE I. Our model has 26 input parameters.

Sector	Input parameters	No.
Gauge	$\alpha_G, M_G, \epsilon_3$	3
SUSY (GUT scale)	$m_{16}, M_{1/2}, A_0, m_{H_u}, m_{H_d}$	5
Yukawa textures	$\lambda, \epsilon, \tilde{\epsilon}, \epsilon', \xi, \alpha, \beta, \theta',$ $\tilde{\theta}, \phi_{\epsilon'}, \phi_{\tilde{\epsilon}}, \phi_{\alpha}, \phi_{\beta}$	13
Neutrino	$M_{R_1}, M_{R_2}, M_{R_3}$	3
SUSY (EW scale)	$\tan\beta, \mu$	2
Total		26

parameters other than $\tan\beta$ and μ are defined at the GUT scale.⁶

In summary, our model has 26 input parameters (see Table I). The fermion sector has 17 parameters—13 Yukawa parameters, $\tan\beta$, and three right-handed neutrino masses, while the SM has 19 observables—nine fermion masses, four CKM matrix elements, two neutrino mass differences, three real neutrino mixing angles, and one neutrino CP violating phase. Hence, our model has two predictions in the fermion sector. As a comparison with previous analyses, we have added two new real input parameters in the Yukawa sector.

III. GLOBAL CHI-SQUARED ANALYSIS

A. Procedure

The program that performs the renormalization group equation (RGE) running and calculation of low energy observables, `maton`, is developed in house by Radovan Dermišek. This program adopts a top-down approach; that is, the program starts with input parameters at the GUT scale and uses two-loop RGEs along with one-loop threshold corrections to run to the low energy scale where observables are calculated. The calculated observables are then compared with experimental measurements in a chi-squared equation,

$$\chi^2 = \sum_i \frac{|x_i^{\text{th}} - x_i^{\text{exp}}|^2}{\sigma_i^2}, \quad (23)$$

where x_i^{th} are the calculated values, x_i^{exp} are the measured values, and σ_i^2 is the sum of the squares of theoretical and experimental uncertainties. The program then uses the `Minuit` package [13] to minimize this χ^2 function. The details of the program can be found in previous analyses [5,6].

⁶To ensure radiative electroweak symmetry breaking, we require tadpole diagrams to vanish at one-loop level (see [12] for discussion and [5] for more details of our analysis). By imposing this condition, M_Z is fit exactly and the magnitude of the parameter μ is also fixed.

In this paper, we fit this model to 51 observables listed in Table II. As a comparison with previous analyses, we have included m_u and m_d in the list of observables. In addition, we have updated all experimental values to the latest value available in the Particle Data Group (PDG) and Heavy Flavor Averaging Group [14,15]. The value of $|V_{cb}|$ and $|V_{ub}|$ used is the average of the inclusive and exclusive values from the PDG with error bars overlapping the inclusive and exclusive error bars. We also updated the publicly available software, `SUPERISO` and `SUSY_FLAVOR` [16,17]. Every χ^2 minimization of this paper is done by fixing m_{16} and $M_{1/2}$ in a grid of points and then minimizing with respect to the other 24 parameters. Since we are fitting to 51 observables, for each fixed value of m_{16} and $M_{1/2}$, we have 27 dof.

A way to visualize the gluino mass that this model favors is to make a χ^2/dof contour plot of the gluino mass as a function of the scalar mass at the GUT scale, m_{16} . To produce this plot, we perform the χ^2 minimization for gluino mass ranges from 1.6 to 2.8 TeV with an increment of 0.2 TeV and scalar mass at the GUT scale ranging from 10 to 30 TeV with an increment of 5 TeV. We control the gluino mass by selecting the appropriate value of $M_{1/2}$ at the GUT scale. We then perform a two-dimensional cubic spline interpolation on these 30 points to obtain a two-dimensional surface of χ^2/dof . To increase the likelihood that each of these 30 points is at the minimum, we perform minimization repeatedly until the change in χ^2 after five repetitions is lower than 0.001. After the χ^2 value settles down, we make a small shift in the values of input parameters other than $M_{1/2}$ and m_{16} and reperform the minimization to make sure that the shifted parameters eventually return to the original value. With this procedure, we are confident that the points that we obtain are at least in a very deep local minimum, if not the global minimum.

B. Results

Figure 1 shows the χ^2/dof contour plot with gluino mass ranging from 1.7 to 2.7 TeV and the scalar mass at the GUT scale ranging from 10 to 30 TeV. The black contour lines are the contour lines of χ^2/dof , which ranges from 1.10 to 1.89. The black contour lines show that our model prefers small gluino mass because the minimum χ^2 value occurs at gluino mass below the lower limit of the plot. The green dotted lines are the 1.0 and 1.2 σ bound. These lines show that even with $M_{\tilde{g}} = 2.7$ TeV, χ^2/dof can still be as low as ≈ 1.15 , which is well within the 2 σ bound.⁷ Since the χ^2 contour lines are very flat in the gluino mass direction, this model is not very sensitive to gluino mass. Hence, this

⁷In fact, even with gluino mass as high as 3.1 TeV and $m_{16} = 25$ TeV, $\chi^2/\text{dof} = 1.33$, which is also below the 2 σ bound.

TABLE II. 51 low energy observables that are fitted in the global χ^2 analysis.

Observable	Experimental value	Reference	Program	Theoretical error
M_Z	91.1876 ± 0.0021 GeV	[14]	Input	0.0%
M_W	80.385 ± 0.015 GeV	[14]	MATON	0.5%
α_{em}	$1/137.035999139(31)$	[14]	MATON	0.5%
G_μ	$1.1663787(6) \times 10^{-5}$ GeV ⁻²	[14]	MATON	1.0%
$\alpha_3(M_Z)$	0.1181 ± 0.0006	[14]	MATON	0.5%
M_t	$173.21 \pm 0.51 \pm 0.71$ GeV	[14]	MATON	1.1%
$m_b(m_b)$	4.185 ± 0.035 GeV	[14]	MATON	3.0%
M_τ	1776.86 ± 0.12 MeV	[14]	MATON	1.1%
$m_b - m_c$	3.45 ± 0.05 GeV	[14]	MATON	10.8%
$m_c(m_c)$	1.27 ± 0.03 GeV	[14]	MATON	1.1%
$m_s(2\text{GeV})$	98 ± 6 MeV	[14]	MATON	1.1%
$m_s/m_d(2\text{GeV})$	19.5 ± 2.5	[14]	MATON	0.5%
Q	23 ± 2	[14]	MATON	5.0%
$m_u(2\text{ GeV})$	2.3 ± 0.5 MeV	[14]	MATON	1.1%
$m_d(2\text{ GeV})$	4.75 ± 0.45 MeV	[14]	MATON	1.1%
M_μ	$105.6583745(24)$ MeV	[14]	MATON	2.1%
M_e	$0.5109989461(31)$ MeV	[14]	MATON	1.1%
$ V_{ud} $	0.97417 ± 0.00021	[14]	MATON	0.5%
$ V_{us} $	0.2248 ± 0.0006	[14]	MATON	0.5%
$ V_{ub} $	$(4.13 \pm 0.60) \times 10^{-3}$	[14]	MATON	2.1%
$ V_{cd} $	0.220 ± 0.005	[14]	MATON	0.5%
$ V_{cs} $	0.995 ± 0.016	[14]	MATON	0.5%
$ V_{cb} $	$(40.75 \pm 2.25) \times 10^{-3}$	[14]	MATON	2.1%
$ V_{td} $	$(8.2 \pm 0.6) \times 10^{-3}$	[14]	MATON	2.1%
$ V_{ts} $	$(40.0 \pm 2.7) \times 10^{-3}$	[14]	MATON	2.1%
$ V_{tb} $	1.009 ± 0.031	[14]	MATON	0.5%
$\sin 2\beta$	0.691 ± 0.017	[14]	MATON	0.5%
ϵ_K	$(2.233 \pm 0.015) \times 10^{-3}$	[14]	SUSY_FLAVOR [17]	10.0%
$\Delta m_{B_s}/\Delta m_{B_d}$	34.8479 ± 0.2324	[14]	SUSY_FLAVOR [17]	20.2%
Δm_{B_d}	$(3.354 \pm 0.022) \times 10^{-10}$ MeV	[14]	SUSY_FLAVOR [17]	20.0%
Δm_{21}^2	$(7.375 \pm 0.165) \times 10^{-5}$ eV ²	[18]	MATON	5.0%
Δm_{31}^2	$(2.50 \pm 0.04) \times 10^{-3}$ eV ²	[18]	MATON	5.0%
$\sin^2 \theta_{12}$	0.2975 ± 0.0165	[18]	MATON	0.5%
$\sin^2 \theta_{23}$	0.4435 ± 0.0265	[18]	MATON	0.5%
$\sin^2 \theta_{13}$	0.0215 ± 0.0010	[18]	MATON	0.5%
M_h	125.90 ± 0.24 GeV	[14]	SPLIT_SUSPECT [19]	3.8%
$\text{BR}(b \rightarrow s\gamma)$	$(332 \pm 16) \times 10^{-6}$	[15]	SUSY_FLAVOR [17]	47.3%
$\text{BR}(B_s \rightarrow \mu^+\mu^-)$	$(2.94 \pm 0.65) \times 10^{-9}$	[15]	SUSY_FLAVOR [17]	22.4%
$\text{BR}(B_d \rightarrow \mu^+\mu^-)$	$(0.40 \pm 0.15) \times 10^{-9}$	[15]	SUSY_FLAVOR [17]	21.5%
$\text{BR}(B \rightarrow \tau\nu)$	$(106 \pm 19) \times 10^{-6}$	[15]	SUSY_FLAVOR [17]	50.4%
$\text{BR}(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	$(0.34 \pm 0.06) \times 10^{-7}$	[20]	SUPERISO [16]	105.1%
$\text{BR}(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	$(0.56 \pm 0.10) \times 10^{-7}$	[20]	SUPERISO [16]	190.0%
$q_0^2(A_{\text{FB}}(B \rightarrow K^*\mu^+\mu^-))$	4.9 ± 0.9 GeV ²	[20]	SUPERISO [16]	25.3%
$F_L(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.65 ± 0.09	[20]	SUPERISO [16]	45.0%
$F_L(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	0.33 ± 0.09	[20]	SUPERISO [16]	80.0%
$-2P_2 = A_T^{\text{Re}}(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	-0.66 ± 0.24	[20]	SUPERISO [16]	198.2%
$-2P_2 = A_T^{\text{Re}}(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	0.50 ± 0.03	[20]	SUPERISO [16]	45.0%
$P_4^+(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.58 ± 0.36	[21]	SUPERISO [16]	30.4%
$P_4^+(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	-0.18 ± 0.70	[21]	SUPERISO [16]	35.0%
$P_5^+(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.21 ± 0.21	[21]	SUPERISO [16]	45.9%
$P_5^+(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	-0.79 ± 0.27	[21]	SUPERISO [16]	60.0%

model cannot be ruled out even if the gluino is not seen during the current run of the LHC.

Also shown in Fig. 1 are a horizontal white line, and a black and a yellow star. The horizontal white line is the current gluino mass bound obtained by reinterpreting the most recent gluino mass bound from the ATLAS and CMS collaborations (see the next section). The black star is a benchmark point. The input parameters and the low energy fits of this benchmark point are shown in the appendix. The yellow star is the point with the minimum χ^2 with gluino mass still allowed by current bound. Notice that this point is exactly on the current mass bound indicating that even though the χ^2/dof is relatively small for large gluino mass, our model still prefers small gluino mass.

IV. CURRENT LHC BOUNDS

The typical search for supersymmetry is performed under the assumption of a simplified model, such as the T1tttt or Gtt model, in which the gluino decays 100% of the time to $t\bar{t}\tilde{\chi}_1^0$. On the other hand, gluinos in this model do not decay via a single channel (see Table III for typical branching ratios of gluino of this model). Hence, to obtain the current gluino bound for this model, the analyses performed by the ATLAS and CMS collaborations has to be reinterpreted.

The most stringent gluino mass bound is from ATLAS-CONF-2016-052, where the gluino mass bound of the Gtt simplified model is around 1.9 TeV with the lightest neutralino mass $m_{\tilde{\chi}_1^0} = 200$ GeV [8]. ATLAS-CONF-2016-052 considers the signal region with zero or more leptons, b -jets and missing transverse momentum. The most stringent gluino mass bound from the CMS collaboration is from CMS-SUS-16-014, where the gluino mass bound of the T1tttt simplified model is 1.75 TeV for $m_{\tilde{\chi}_1^0} = 200$ GeV [22]. CMS-SUS-16-021 considers the signal region with jets and missing transverse momentum. In this paper, these two analyses are reinterpreted with our model.

In addition, a CMS analysis, CMS-SUS-16-021, which considers the signal region of two opposite-sign same-flavor leptons with jets and missing transverse momentum, found a $2.1(1.1)\sigma$ local (global) deviation in the number of observed events compared to the SM background [23]. Since our model produces signal in this region, we include this analysis in this paper. To be impartial, we also reinterpret a CMS analysis that considers signal region with same-sign dilepton events, CMS-SUS-16-020 [24].

The experimental data, for all the analyses mentioned above, are obtained at the center-of-mass energy $\sqrt{s} = 13$ TeV. The integrated luminosity for the ATLAS analysis is 14.8 fb^{-1} , while that of the CMS analyses is 12.9 fb^{-1} .

TABLE III. Branching ratios of gluinos, charginos and neutralinos for two benchmark points of our model. This table shows that gluino branching ratios of our model are not even close to that of the simplified model. Hence, it is important to reinterpret the ATLAS and CMS simplified model analysis to obtain the gluino mass bounds of our model. The chargino and neutralino masses and compositions are shown in Table V.

Benchmark point	A	B
m_{16}/TeV	20	25
$M_{\tilde{g}}/\text{TeV}$	2.00	2.00
$\text{BR}(\tilde{g} \rightarrow g\tilde{\chi}_1^0)$	0.000	0.000
$\text{BR}(\tilde{g} \rightarrow g\tilde{\chi}_2^0)$	0.002	0.001
$\text{BR}(\tilde{g} \rightarrow g\tilde{\chi}_3^0)$	0.005	0.006
$\text{BR}(\tilde{g} \rightarrow g\tilde{\chi}_4^0)$	0.001	0.003
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_1^\pm)$	0.288	0.207
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_2^\pm)$	0.219	0.301
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_3^0)$	0.017	0.021
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_4^0)$	0.073	0.045
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_3^0)$	0.116	0.109
$\text{BR}(\tilde{g} \rightarrow t\tilde{\chi}_4^0)$	0.078	0.102
$\text{BR}(\tilde{g} \rightarrow b\tilde{\chi}_1^0)$	0.009	0.010
$\text{BR}(\tilde{g} \rightarrow b\tilde{\chi}_2^0)$	0.073	0.058
$\text{BR}(\tilde{g} \rightarrow b\tilde{\chi}_3^0)$	0.083	0.082
$\text{BR}(\tilde{g} \rightarrow b\tilde{\chi}_4^0)$	0.034	0.052
$\text{BR}(\tilde{\chi}_1^+ \rightarrow W^+\tilde{\chi}_1^0)$	1.000	1.000
$\text{BR}(\tilde{\chi}_2^+ \rightarrow Z\tilde{\chi}_1^+)$	0.218	0.256
$\text{BR}(\tilde{\chi}_2^+ \rightarrow h\tilde{\chi}_1^+)$	0.025	0.000
$\text{BR}(\tilde{\chi}_2^+ \rightarrow W^+\tilde{\chi}_1^0)$	0.058	0.335
$\text{BR}(\tilde{\chi}_2^+ \rightarrow W^+\tilde{\chi}_2^0)$	0.299	0.408
$\text{BR}(\tilde{\chi}_2^+ \rightarrow W^+\tilde{\chi}_3^0)$	0.399	0.000
$\text{BR}(\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0)$	0.081	0.094
$\text{BR}(\tilde{\chi}_2^0 \rightarrow h\tilde{\chi}_1^0)$	0.919	0.906
$\text{BR}(\tilde{\chi}_3^0 \rightarrow Z\tilde{\chi}_1^0)$	0.563	0.537
$\text{BR}(\tilde{\chi}_3^0 \rightarrow h\tilde{\chi}_1^0)$	0.437	0.563
$\text{BR}(\tilde{\chi}_4^0 \rightarrow Z\tilde{\chi}_1^0)$	0.011	0.039
$\text{BR}(\tilde{\chi}_4^0 \rightarrow Z\tilde{\chi}_2^0)$	0.002	0.000
$\text{BR}(\tilde{\chi}_4^0 \rightarrow h\tilde{\chi}_1^0)$	0.085	0.263
$\text{BR}(\tilde{\chi}_4^0 \rightarrow h\tilde{\chi}_2^0)$	0.028	0.000
$\text{BR}(\tilde{\chi}_4^0 \rightarrow W^\mp\tilde{\chi}_1^\pm)$	0.874	0.698

A. Analysis procedure

In a nutshell, the analyses are reperformed by focusing on the 95% upper limit of the number of events allowed, N_{UL} , calculated from the SM background and the number of observed events. N_{UL} is the 95% Bayesian upper limit for a Poisson parameter calculated using a uniform prior. By focusing on the number of events allowed, we do not need to perform background simulation. Instead, we only need to simulate events produced by the models in consideration, such as the simplified model and our model. To validate our analysis, we first ensure that the simplified mass bound obtained from our analysis matches those from

the ATLAS and CMS analyses. Mass bounds are obtained by ruling out masses where the 95% lower limit on the number of events passing all cuts exceeds N_{UL} . Once our analysis is validated, we can reperform the analysis based on our model to obtain the gluino mass bound of our model.

For analysis of a simplified model, events are simulated by supplying PYTHIA 8.219 with an SLHA file that contains the SUSY spectrum, mixing angles and decay tables [25]. For each mass point, 10,000 events are simulated. The simulated events are then passed to Delphes 3.4.0, a detector simulator that outputs events as recorded by the detector [26]. The card files of Delphes, which specifies various detector specific parameters such as the triggering and candidate selection requirements, are modified according to the selection criteria of the ATLAS and CMS analyses. The output of Delphes then goes through a cutflow code that we wrote. The number of events passing all cuts is then normalized by the ratio of the number of events produced at the LHC to the number of simulated events. The number of events produced at the LHC equals the product of the luminosity and the production cross section, which is obtained from the LHC SUSY Cross Section Working Group [27]. The normalized number of events passing all cuts is then compared to N_{UL} to produce the mass bound.

The analysis of our model is almost identical to that of the simplified model. The only difference is that the SLHA file of the simplified model is simple and can be written directly by hand, while that of our model is very complicated. Luckily, maton is also a spectrum generator. After obtaining the SUSY spectrum along with all the mixing angles and couplings of the model, we use SUSY-HIT 1.5a to calculate the decay tables [28]. The output of SUSY-HIT is then used as input to PYTHIA and the procedure of the simplified model analysis outlined in the previous paragraph is repeated.

B. Results

Out of all the signal regions in the four analyses that we studied, the most constrained bound comes from the 0 lepton with large mass splitting signal region in the ATLAS analysis, ATLAS-CONF-2016-52. The events in this signal region are required to have $N^{\text{signal lepton}} = 0$, $N^{\text{jet}} \geq 8$, $N_{b\text{-jet}} \geq 3$, $p_T^{\text{jet}} > 30 \text{ GeV}$, $E_T^{\text{miss}} > 400 \text{ GeV}$, $\Delta\phi_{\text{min}}^{A_j} > 0.4 \text{ rad}$, $m_{T,\text{min}}^{b\text{-jets}} > 80 \text{ GeV}$, $m_{\text{eff}}^{\text{incl}} > 2000 \text{ GeV}$ and $M_{\tilde{g}}^{\Sigma} > 200 \text{ GeV}$. These parameters are defined in [8]. Hence, in this section, we only show the results of this specific analysis.

Figure 2 is the validation plot from our analysis of the Gtt simplified model with $m_{\tilde{\chi}_1^0} = 200 \text{ GeV}$. The red horizontal line is the 95% upper limit of the number of events allowed, $N_{\text{UL}} = 3.8$. The vertical blue bars are the normalized number of events passing all cuts. The error bars represent the 95% upper and lower limits of the number of events passing all cuts. These limits are derived from the

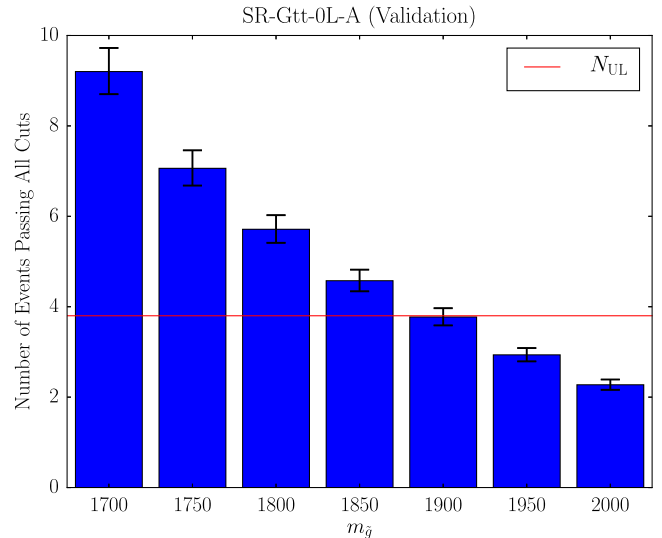


FIG. 2. The validation plot for the Gtt simplified model with $m_{\tilde{\chi}_1^0} = 200 \text{ GeV}$ in the 0 lepton with large mass splitting signal region of the ATLAS analysis [8]. The vertical blue bars show the number of events passing all cuts while the horizontal red line is the 95% upper limit of the number of events allowed. The gluino mass bound obtained from this plot, $M_{\tilde{g}} \sim 1.875 \text{ TeV}$, is in agreement with the gluino mass bound from the ATLAS collaboration, $M_{\tilde{g}} \sim 1.9 \text{ TeV}$.

uncertainties in the gluino production cross section and the counting experiment. The size of the error bars shrinks as the gluino mass increases because the number of simulated events stays constant but the gluino production

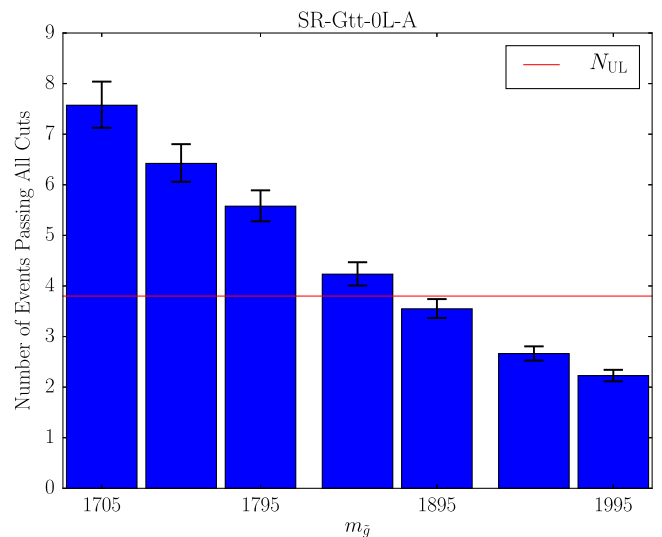


FIG. 3. Number of events passing all cuts for our model in the 0 lepton with large mass splitting signal region of the ATLAS analysis [8]. The scalar mass of all the points in this plot is $m_{16} = 20 \text{ TeV}$. The gluino mass bound obtained from this plot, $M_{\tilde{g}} \sim 1.875 \text{ TeV}$, is the same as that from the validation plot. Hence, we conclude that the gluino mass bound of our model is the same as that of the simplified model.

TABLE IV. SUSY mass spectrum from four benchmark points of our model. Benchmark points A and B have $M_{\tilde{g}} = 2.0$ TeV while benchmark points C and D have $M_{\tilde{g}} = 2.6$ TeV. The compositions of the charginos and neutralinos of benchmark points A and B are shown in Table V. The input parameters of these benchmark points are in the appendix. In addition, the prediction of the electron dipole moment, the branching ratio of $\mu \rightarrow e\gamma$ and the neutrino CP violating phase are also presented in this table.

Benchmark point	A	B	C	D
m_{16}/TeV	20	25	20	25
$M_{\tilde{g}}/\text{TeV}$	2.00	2.00	2.60	2.60
χ^2/dof	1.14	1.16	1.16	1.17
$m_{\tilde{\tau}_1}/\text{TeV}$	3.68	4.70	3.70	4.65
$m_{\tilde{\tau}_2}/\text{TeV}$	4.38	5.52	4.43	5.49
$m_{\tilde{b}_1}/\text{TeV}$	4.17	5.32	4.17	5.23
$m_{\tilde{b}_2}/\text{TeV}$	4.32	5.47	4.36	5.43
$m_{\tilde{\nu}_1}/\text{TeV}$	7.47	9.30	7.52	9.27
$m_{\tilde{\nu}_2}/\text{TeV}$	12.2	15.2	12.2	15.2
$m_{\tilde{\chi}_1^0}/\text{GeV}$	352	352	474	474
$m_{\tilde{\chi}_2^0}/\text{GeV}$	586	636	650	665
$m_{\tilde{\chi}_1^+}/\text{GeV}$	585	636	646	661
$m_{\tilde{\chi}_2^+}/\text{GeV}$	710	751	911	914
$(M_A \approx M_{H^0} \approx M_{H^\pm})/\text{TeV}$	5.18	6.39	5.39	6.67
$\text{edm}_e/10^{-32} \text{ e cm}$	-3.46	-1.77	-4.47	-2.28
$\text{BR}(\mu \rightarrow e\gamma)/10^{-17}$	2.08	0.922	1.84	0.869
$\sin \delta$	0.759	0.935	0.644	0.993

cross section decreases. Figure 2 shows that the gluino mass bound from our analysis is $M_{\tilde{g}} \sim 1.875$ TeV, which is well within 20% of the gluino mass bounds from the ATLAS analysis, $M_{\tilde{g}} \sim 1.9$ TeV. This is the expected precision because we do not have the state of the art

analysis tools available to the ATLAS collaboration, such as the detector simulator. From this, we conclude that our analysis is in agreement with the ATLAS analysis.

On the other hand, Fig. 3 is the plot for our model. The scalar mass for all points in this plot is $m_{16} = 20$ TeV. We have checked that points with $m_{16} = 25$ TeV produce the same gluino mass bound, since the gluino mass bound of our model is very similar to that of the simplified model. We conclude that the current gluino mass bound of our model $M_{\tilde{g}} \gtrsim 1.9$ TeV.

With this gluino mass bound, our model is unable to fit the excess CMS found in the two opposite-sign same-flavor leptons analysis [23]. Hence, we predict that this excess is a statistical fluctuation.

V. PREDICTIONS AND DISCOVERY PROSPECTS

From the analysis in the previous section, the current gluino mass bound of our model is $M_{\tilde{g}} > 1.9$ TeV. Even with this mass bound, Fig. 1 shows that a wide range of parameter space still is $< 1.2\sigma$. Hence, our model is not ruled out by low energy data and current LHC bounds. Since our χ^2 analysis is well below 2σ even for a gluino as heavy as 2.7 TeV, see Fig. 1, this model will, unfortunately, not be ruled out, even if the gluino is not found in this run of the LHC.

The SUSY mass spectrum for four benchmark points is given in Tables IV and V. Also in Table V are compositions of charginos and neutralinos of benchmark points A and B. The benchmark points have $m_{16} = 20$ and 25 TeV, and $M_{\tilde{g}} = 2.0$ and 2.6 TeV. The lightest scalar mass of our model, $m_{\tilde{\tau}_1}$, ranges from 3–5 TeV while the first two family scalar masses are either around 20 or 25 TeV depending on the value of m_{16} at the GUT scale. The scalars of the first

TABLE V. Neutralino and chargino masses in GeV and their composition in percentage for the two benchmark points of our model. The lightest neutralino of our model is mainly the bino. Hence, the lightest neutralino cannot be the dark matter candidate of our model. However, this problem can be alleviated if the gaugino masses are nonuniversal (see [29]).

		Mass in GeV	Composition in percentage							
			\tilde{B}	\tilde{W}^0	\tilde{H}_d^0	\tilde{H}_u^0	\tilde{W}^+	\tilde{H}_u^+	\tilde{W}^-	\tilde{H}_d^-
Benchmark point A	$\tilde{\chi}_1^0$	352	0.98	0.00	0.01	0.00
	$\tilde{\chi}_2^0$	586	0.01	0.28	0.37	0.33
	$\tilde{\chi}_3^0$	621	0.00	0.00	0.50	0.50
	$\tilde{\chi}_4^0$	711	0.00	0.71	0.12	0.16
	$\tilde{\chi}_1^+$	585	0.32	0.68
	$\tilde{\chi}_2^+$	710	0.68	0.32
	$\tilde{\chi}_1^-$	585	0.24	0.76
Benchmark point B	$\tilde{\chi}_1^0$	352	0.99	0.00	0.01	0.00
	$\tilde{\chi}_2^0$	636	0.00	0.61	0.21	0.17
	$\tilde{\chi}_3^0$	707	0.00	0.00	0.50	0.50
	$\tilde{\chi}_4^0$	752	0.00	0.39	0.29	0.32
	$\tilde{\chi}_1^+$	636	0.65	0.35
	$\tilde{\chi}_2^+$	751	0.35	0.65
	$\tilde{\chi}_1^-$	636	0.57	0.43

two families are decoupled from the low energy theory while the third family scalars are not. Hence, SUSY is not completely decoupled from the SM. The CP -odd Higgs, A , the heavy Higgs, H^0 , and the charged Higgs, H^\pm , all have masses around 5–6 TeV showing that we are in the decoupling limit where the light Higgs boson behaves like a SM Higgs boson. Table IV also shows our prediction for the electron electric dipole moment, edm_e , the branching ratio $BR(\mu \rightarrow e\gamma)$ and the CP violating phase in the neutrino sector, $\sin\delta$. These values are consistent with current experiment bounds. Note, however, that these predictions differ significantly from our previous results. In particular, the electric dipole moment of the electron and the branching ratio, $BR(\mu \rightarrow e\gamma)$, are significantly smaller than before. In addition, the CP violating angle in the lepton sector is now of order 90° for $m_{16} = 25$ TeV.

VI. CONCLUSION

In this paper, we modify the Yukawa sector of a SUSY GUT with SO(10) or PS gauge symmetry that some of the present authors have studied in the past. This paper aims to improve the fits to low energy observables, such as $\sin 2\beta$, m_u and m_d . By shifting the phase from one Yukawa texture to another, we are able to improve the fit to $\sin 2\beta$. On the other hand, to fit m_u and m_d , we choose PS gauge symmetry, due to higher flexibility than SO(10), and introduce two real parameters to the 11 and 12/21 entries of the Yukawa matrices. This increases the number of parameters of our model to 26 parameters; see Table I.

By fitting to 51 low energy observables, see Table II, our global χ^2 analysis has 27 dof. The modification to the Yukawa sector, see Sec. II, improves the best fit from $\chi^2/\text{dof} = 1.90$ [30] to $\chi^2/\text{dof} = 1.12$; see Fig. 1. Even for gluinos as heavy as $M_{\tilde{g}} = 2.7$ TeV, our analysis shows that $\chi^2/\text{dof} \approx 1.15$. Thus, our model is not ruled out even if gluinos are not found during this LHC run. On the bright side, our model indicates that low energy SUSY is still a viable model and the LHC might hopefully find gluinos in the near future.

In addition to the global χ^2 analysis, we also reinterpreted ATLAS and CMS analyses in signal regions with high jet multiplicities and large missing transverse momentum. Since gluinos of our model do not decay via a single decay channel, see Table III, the gluino mass bound of our model might be different from that of a simplified model. Gluinos of our model decay predominantly via $t\tilde{b}\tilde{\chi}_{1,2}^+$, $t\tilde{t}\tilde{\chi}_{1,2,3,4}^0$ and $b\tilde{b}\tilde{\chi}_{1,2,3,4}^0$. However, we found that the gluino mass bound of our model is very similar to that of a simplified model where $M_{\tilde{g}} \sim 1.9$ TeV. The most constraining signal region that we found is also the same as that of the simplified model, which is from the ATLAS analysis in the signal region with 0-lepton, large jet multiplicities and large missing transverse momentum (Gtt-0L-A) of ATLAS-CONF-2016-052 [8].

Previous analysis by Bryant *et al.* shows that this model can be extended to fit inflation observables measured by the

BICEP2/Keck and Planck joint collaboration via a sub-critical hybrid inflation [7]. Further studies of the consequences of this model for the early Universe are warranted.

Since SUSY particles have not been observed at the LHC and natural SUSY models prefer light superpartners, one might think that low energy SUSY models are no longer attractive on the grounds of naturalness. However, previous analysis by Poh *et al.* showed that the fine-tuning of this model can be of the order of 1 part in 500 [6], assuming that some soft SUSY breaking boundary conditions defined at M_{GUT} can be obtained from a more fundamental theory. Thus, although this model is not the most natural model, it is much more natural than the SM. In addition, by construction, this model uses small GUT representations; thus the model has the potential for a UV completion to a higher dimensional string theory.

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APPENDIX: BENCHMARK POINT

Input parameters of benchmark point A

Sector	Input parameter	Best fit
Gauge	$1/\alpha_G$	26.0
	$M_G/10^{16}$ GeV	2.25
SUSY (GUT scale)	$\epsilon_3/\%$	-1.68
	m_{16}/TeV	20.0
	$m_{1/2}/\text{GeV}$	660
	A_0/TeV	-40.6
	$(m_{H_d}/m_{16})^2$	1.98
Neutrino	$(m_{H_u}/m_{16})^2$	1.61
	$M_{R_1}/10^9$ GeV	4.62
	$M_{R_2}/10^{11}$ GeV	8.32
SUSY (EW scale)	$M_{R_3}/10^{13}$ GeV	4.71
	$\tan\beta$	50.4
	μ/GeV	630
Yukawa textures	λ	0.617
	$\lambda\epsilon$	0.0326
	$\lambda\tilde{\epsilon}$	0.0100
	$\lambda\epsilon'$	-0.00300
	$\lambda\xi$	0.00201
	α	0.138
	β	0.0277
	$\theta'/10^{-5}$	5.03
	$\tilde{\theta}/10^{-5}$	2.92
	ϕ_e/rad	-0.277
	ϕ_ξ/rad	3.41
	ϕ_α/rad	0.963
ϕ_β/rad	-1.26	

Low energy observables fit of benchmark point A

Observable	Fit value	Experimental value	Pull	σ
M_Z/GeV	91.1876	91.1876	0.0000	0.4514
M_W/GeV	80.4734	80.3850	0.2238	0.3949
$1/\alpha_{\text{em}}$	137.3435	137.0360	0.4478	0.6867
$G_\mu/10^{-5} \text{ GeV}^{-2}$	1.1761	1.1664	0.8264	0.0118
$\alpha_3(M_Z)$	0.1177	0.1181	0.4791	0.0008
M_t/GeV	174.0978	173.2100	0.4161	2.1338
$m_b(m_b)/\text{GeV}$	4.3264	4.1850	1.0388	0.1362
m_τ/MeV	1776.0100	1776.8600	0.0428	19.8568
$(M_b - M_c)/\text{GeV}$	3.3028	3.4500	0.4098	0.3592
$m_c(m_c)/\text{GeV}$	1.2685	1.2700	0.0442	0.0332
$m_s(2\text{GeV})/\text{MeV}$	97.7602	98.0000	0.0393	6.0987
$m_s/m_d(2\text{GeV})$	18.5692	19.5000	0.3843	2.0519
Q	21.5785	23.0000	0.6256	2.2725
$m_u(2\text{GeV})/\text{MeV}$	2.6880	2.3000	0.7758	0.5002
$m_d(2\text{GeV})/\text{MeV}$	5.2646	4.7500	1.1417	0.4508
M_μ/MeV	105.2131	105.6584	0.2053	2.1690
M_e/MeV	0.5108	0.5110	0.0278	0.0057
$ V_{ud} $	0.9745	0.9742	0.0622	0.0049
$ V_{us} $	0.2245	0.2248	0.2615	0.0013
$ V_{ub} /10^{-3}$	3.9904	4.1300	0.2305	0.6056
$ V_{cd} $	0.2244	0.2200	0.8509	0.0051
$ V_{cs} $	0.9735	0.9950	1.2853	0.0167
$ V_{cb} /10^{-3}$	44.1574	40.7500	1.4038	2.4272
$ V_{td} /10^{-3}$	7.9898	8.2000	0.3378	0.6222
$ V_{ts} /10^{-3}$	43.6115	40.0000	1.2691	2.8458
$ V_{tb} $	0.9990	1.0090	0.3179	0.0314
$\sin 2\beta$	0.6922	0.6910	0.0672	0.0173
$\epsilon_K/10^{-3}$	2.0225	2.2330	1.0379	0.2028
$\Delta M_{B_s}/\Delta M_{B_d}$	43.7269	34.8479	1.0037	8.8463
$\Delta M_{B_d}/10^{-10} \text{ MeV}$	2.9005	3.3540	0.7802	0.5812
$m_{21}^2/10^{-5} \text{ eV}^2$	7.3484	7.3750	0.0658	0.4044
$m_{31}^2/10^{-3} \text{ eV}^2$	2.5096	2.5000	0.0726	0.1323
$\sin^2 \theta_{12}$	0.2960	0.2975	0.0915	0.0166
$\sin^2 \theta_{23}$	0.4419	0.4435	0.0599	0.0266
$\sin^2 \theta_{13}$	0.0217	0.0215	0.1493	0.0010
M_h/GeV	122.7975	125.0900	0.4854	4.7225
$\text{BR}(b \rightarrow s\gamma)/10^{-6}$	299.9500	332.0000	0.2243	142.9017
$\text{BR}(B_s \rightarrow \mu^+\mu^-)/10^{-9}$	5.1836	2.9500	1.6808	1.3289
$\text{BR}(B_d \rightarrow \mu^+\mu^-)/10^{-9}$	0.1223	0.4000	1.8234	0.1523
$\text{BR}(B \rightarrow \tau\nu)/10^{-6}$	96.4950	106.0000	0.1822	52.1761
$\text{BR}(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}/10^{-7}$	0.5456	0.3400	0.3567	0.5765
$\text{BR}(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}/10^{-7}$	0.7904	0.5600	0.1531	1.5055
$q_0^2(A_{\text{FB}}(B \rightarrow K^*\mu^+\mu^-))/\text{GeV}^2$	3.8492	4.9000	0.7921	1.3265
$F_L(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.7522	0.6500	0.2917	0.3503
$F_L(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	0.3514	0.3300	0.0725	0.2952
$P_2(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.0679	0.3300	1.4536	0.1803
$P_2(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	-0.4333	-0.5000	0.3381	0.1973
$P_4^l(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	0.5788	0.5800	0.0029	0.4007
$P_4^l(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	1.2177	-0.1800	1.7055	0.8195
$P_5^l(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$	-0.3221	0.2100	2.0721	0.2568
$P_5^l(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$	-0.7119	-0.7900	0.1545	0.5053
Total χ^2			30.9061	

Input parameters of benchmark point B

Sector	Input parameter	Best fit
Gauge	$1/\alpha_G$	26.0
	$M_G/10^{16}$ GeV	2.25
SUSY (GUT scale)	$\epsilon_3/\%$	-1.70
	m_{16}/TeV	25.0
	$m_{1/2}/\text{GeV}$	620
	A_0/TeV	-51.0
	$(m_{H_d}/m_{16})^2$	1.97
	$(m_{H_u}/m_{16})^2$	1.61
Neutrino	$M_{R_1}/10^9$ GeV	4.66
	$M_{R_2}/10^{11}$ GeV	8.28
	$M_{R_3}/10^{13}$ GeV	4.70
SUSY (EW scale)	$\tan\beta$	50.5
	μ/GeV	704
	λ	0.618
	$\lambda\epsilon$	0.0326
	$\lambda\tilde{\epsilon}$	0.0100
	$\lambda e'$	-0.00300
	$\lambda\xi$	0.00202
	α	0.138
	β	0.0280
	Yukawa textures	$\theta'/10^{-5}$
$\tilde{\theta}/10^{-5}$		2.89
$\phi_{e'}/\text{rad}$		-0.266
ϕ_{ξ}/rad		3.40
ϕ_{α}/rad		0.962
ϕ_{β}/rad		-1.27

Input parameters of benchmark point C

Sector	Input parameter	Best fit
Gauge	$1/\alpha_G$	26.1
	$M_G/10^{16}$ GeV	2.16
SUSY (GUT scale)	$\epsilon_3/\%$	-1.65
	m_{16}/TeV	20.0
	$m_{1/2}/\text{GeV}$	940
	A_0/TeV	-40.5
	$(m_{H_d}/m_{16})^2$	1.99
	$(m_{H_u}/m_{16})^2$	1.61
Neutrino	$M_{R_1}/10^9$ GeV	4.65
	$M_{R_2}/10^{11}$ GeV	8.42
	$M_{R_3}/10^{13}$ GeV	4.75
SUSY (EW scale)	$\tan\beta$	50.3
	μ/GeV	650
	λ	0.612
	$\lambda\epsilon$	0.0325
	$\lambda\tilde{\epsilon}$	0.0100
	$\lambda e'$	-0.00301
	$\lambda\xi$	0.00200
	α	0.137
	β	0.0278
	Yukawa textures	$\theta'/10^{-5}$
$\tilde{\theta}/10^{-5}$		2.93
$\phi_{e'}/\text{rad}$		-0.282
ϕ_{ξ}/rad		3.40
ϕ_{α}/rad		0.965
ϕ_{β}/rad		-1.26

Input parameters of benchmark point D

Sector	Input parameter	Best fit
Gauge	$1/\alpha_G$	26.2
	$M_G/10^{16}$ GeV	2.00
	$\epsilon_3/\%$	-1.21
SUSY (GUT scale)	m_{16}/TeV	25.0
	$m_{1/2}/\text{GeV}$	895
	A_0/TeV	-50.9
	$(m_{H_d}/m_{16})^2$	1.98
	$(m_{H_u}/m_{16})^2$	1.61
Neutrino	$M_{R_1}/10^9$ GeV	4.83
	$M_{R_2}/10^{11}$ GeV	8.40
	$M_{R_3}/10^{13}$ GeV	4.79
SUSY (EW scale)	$\tan\beta$	50.5
	μ/GeV	673
	λ	0.618
	$\lambda\epsilon$	0.0329
	$\lambda\tilde{\epsilon}$	0.0100
	$\lambda\epsilon'$	-0.00302
	$\lambda\xi$	0.00207
	α	0.138
	β	0.0287
	Yukawa textures	$\theta'/10^{-5}$
$\tilde{\theta}/10^{-5}$		2.74
$\phi_{\epsilon'}/\text{rad}$		-0.257
ϕ_{ξ}/rad		3.40
ϕ_{α}/rad		0.971
ϕ_{β}/rad		-1.27

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