

UV complete partially composite pseudo-Nambu Goldstone boson HiggsJamison Galloway,^{1,*} Alexander L. Kagan,^{2,†} and Adam Martin^{3,‡}¹*Center for Cosmology and Particle Physics, Department of Physics, New York University,
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We explore an electroweak symmetry breaking (EWSB) scenario based on the mixture of a fundamental Higgs doublet and an $SU(4)/Sp(4)$ composite pseudo-Nambu-Goldstone doublet—a particular manifestation of bosonic technicolor/induced EWSB. Taking the fundamental Higgs mass parameter to be positive, EWSB is triggered by the mixing of the doublets. This setup has several attractive features and phenomenological consequences, which we highlight: (i) Unlike traditional bosonic technicolor models, the hierarchy between Λ_{TC} and the electroweak scale depends on vacuum (mis)alignment and can be sizable, yielding an attractive framework for natural EWSB; (ii) As the strong sector is based on $SU(4)/Sp(4)$, a fundamental (UV-complete) description of the strong sector is possible, that is informed by the lattice; (iii) The lightest vector resonances occur in the 10-plet, 5-plet and singlet of $Sp(4)$. Misalignment leads to a 10-plet “parity-doubling” cancellation in the S parameter, and a suppressed 5-plet contribution; (iv) Higgs coupling deviations are typically of $\mathcal{O}(1\%)$; (v) The 10-plet isotriplet resonances decay dominantly to a massive technipion and a gauge boson, or to technipion pairs, rather than to gauge boson or fermion pairs; moreover, their couplings to fermions are small. Thus, the bounds on this setup from conventional heavy-vector-triplet searches are weak. A supersymmetric $U(1)_R$ symmetric realization is briefly described.

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The minimal supersymmetric standard model (MSSM) provides an elegant mechanism for stabilizing the Higgs mass, and benefits from the simplicity of the Yukawa coupling paradigm for fermion mass generation. However, naturalness in the MSSM is challenged by LHC bounds on colored superpartners. Technicolor (TC) provides a beautiful mechanism for electroweak symmetry breaking (EWSB), based on asymptotically free gauge theories, but a light Higgs is difficult to accommodate. The pseudo-Nambu Goldstone boson (pNGB) composite Higgs improves on TC by providing a large gap between the Higgs mass and other strong interaction resonances, via vacuum (mis)alignment. However, it is not obvious that a sufficiently light pNGB Higgs obtains in explicit strong interaction constructions, and a UV complete model of fermion masses is difficult to achieve, as in TC.

We introduce a promising framework for naturalness, which combines the advantages of the three approaches, without the potential drawbacks. It is based on bosonic technicolor (BTC)/induced electroweak symmetry breaking [1–24], with $SU(2)_{TC}$ gauge group and two fundamental flavors ($n_f = 2$). In BTC, the vacuum expectation

value of a fundamental Higgs (with Yukawa couplings to the standard model fermions) is induced from TC dynamics, via its Yukawa couplings to the technifermions; and supersymmetry (SUSY) is introduced to protect the Higgs mass [2–7,13,15–17,19–21]. The TC superpartners decouple above the TC chiral symmetry breaking scale, Λ_{TC} . From the point of view of the low energy scalar potential, BTC can accommodate a wide range of Higgs masses, including $m_h = 125$ GeV, without fine-tuned cancellations.

The strong sector of minimal BTC has an $SU(4)/Sp(4)$ coset description in the IR, allowing for nontrivial vacuum alignment between the $SU(2)_L$ conserving (EW vacuum) and $SU(2)_L$ breaking (TC vacuum) limits, thus yielding a composite pNGB Higgs [25–30]. Prior BTC studies have existed in the TC vacuum, where the would-be pNGB Higgs decouples. In this work, we explore small misalignment from the EW vacuum, exploiting the interplay between EW conserving and EW breaking constituent masses. The fundamental and pNGB scalars mix, yielding a partially composite-pNGB Higgs. There are several benefits: (i) vacuum misalignment yields a separation of scales, allowing Λ_{TC} to be raised well into the multi-TeV region; (ii) the Higgs mass parameter m_H is also increased. In a supersymmetric realization, raising Λ_{TC} and m_H would allow the SUSY breaking scale to be raised, which is desirable for natural EWSB. A $U(1)_R$ -symmetric example is briefly discussed in the concluding remarks; (iii) vacuum misalignment reduces deviations from the SM in the Higgs

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couplings and precision EW parameters, the latter due in large measure to $SU(2)_{L\leftrightarrow R}$ parity doubling in the vector sector.

II. THE UV THEORY

In this paper our focus is on the impact of the UV theory on the BTC vacuum structure, and the resulting scalar and vector meson masses and interactions. For this purpose it suffices to consider minimal nonsupersymmetric BTC, with a single Higgs doublet H . The extension to two Higgs doublets is straightforward. The minimal TC sector contains the gauge group $SU(2)_{\text{TC}}$, together with an $SU(2)_L$ doublet and two singlet technifermions, i.e. $n_f = 2$, see Table I. All of the technifermions are treated as left-handed Weyl fields, transforming under the $(1/2, 0)$ representation of the Lorentz group $SU(2) \times SU(2) \sim SO(3, 1)$. With weak interactions turned off, the model possesses a global $SU(4)$ symmetry under which the four-component object

$$\Psi = (T_1 T_2 U D)^T \quad (1)$$

transforms as a fundamental.

The TC condensate

$$\langle \Psi^a \Psi^{T,b} \epsilon C^{-1} \rangle \propto \Phi^{ab} \quad (2)$$

is antisymmetric in the $SU(4)$ flavor indices a, b ; the matrix C is defined momentarily. We assume that Φ breaks $SU(4)$ to its maximal vectorlike subgroup $Sp(4)$, yielding an $SU(4)/Sp(4)$ coset structure. The most general $Sp(4)$ preserving condensate is [25]

$$\Phi = \begin{pmatrix} e^{i\alpha} \epsilon \cos \theta & \mathbb{1}_2 \sin \theta \\ -\mathbb{1}_2 \sin \theta & -e^{-i\alpha} \epsilon \cos \theta \end{pmatrix}, \quad (3)$$

where $\theta \in [0, \pi]$ and α is a CP violating phase [$\Phi \mapsto -\Phi^\dagger$ under CP , see (10)]. At $\sin \theta = 0$ electroweak symmetry is unbroken, while at $\sin \theta = 1$ the condensate is purely $SU(2)_L$ breaking. These limits are referred to as the electroweak (EW) and TC vacua, respectively.

The $Sp(4)$ vacuum degeneracy is lifted by the UV technifermion interactions. Previous BTC studies only included the Higgs Yukawa couplings, which selects the TC vacuum, $\sin \theta = 1$. We will explore the benefits of misalignment from the electroweak vacuum, or small to

TABLE I. Technifermion gauge quantum numbers.

	$SU(2)_{\text{TC}}$	$SU(2)_W$	$U(1)_Y$
$(\Psi^1 \Psi^2)^T \equiv T_{1,2}$	$(\square \square)^T$	\square	0
$\Psi^3 \equiv U$	\square	1	-1/2
$\Psi^4 \equiv D$	\square	1	+1/2.

moderate $\sin \theta$. This is minimally accomplished by adding gauge singlet technifermion masses of $\mathcal{O}(v_W)$. (They can be linked to SUSY breaking and, therefore, to Λ_{TC} .) The UV potential in $SU(4)$ notation is

$$V_{\text{UV}} = -\Psi^T \epsilon C^{-1} (M + \lambda) \Psi + \text{H.c.} \\ + m_H^2 |H|^2 + \lambda_h |H|^4 \quad (4)$$

where $C^{-1} = \text{diag}[i\sigma_2, i\sigma_2, i\sigma_2, i\sigma_2]$ acts on the LH Weyl spinors in Ψ , ϵ acts on the TC indices, and H is the SM Higgs doublet with $m_H^2 > 0$ and quartic coupling λ_h . The 4×4 matrices M and λ contain the gauge singlet masses $m_{1,2}$ and the Higgs Yukawa couplings, respectively,

$$M = \frac{1}{2} \begin{pmatrix} m_1 \epsilon & 0 \\ 0 & -m_2 \epsilon \end{pmatrix}, \quad \lambda = \frac{1}{2} \begin{pmatrix} 0 & -H_\Lambda \\ H_\Lambda^T & 0 \end{pmatrix}, \quad (5)$$

where

$$H_\Lambda = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_U (\sigma_h + v^* - i\pi_h^3) & \lambda_D (-i\pi_h^1 + \pi_h^2) \\ -\lambda_U (i\pi_h^1 + \pi_h^2) & \lambda_D (\sigma_h + v + i\pi_h^3) \end{pmatrix}. \quad (6)$$

σ_h ($\vec{\pi}_h$) are the scalar (pseudoscalar) components of H , with $v \equiv |\langle H \rangle|$. The fermion masses are

$$m_1 T_2 T_1 + m_2 U D + m_U T_1 U + m_D T_2 D, \quad (7)$$

where $m_U = \lambda_U v^* / \sqrt{2}$, $m_D = \lambda_D v / \sqrt{2}$. Under $SU(4)$ rotations, $(M + \lambda) \mapsto U^* (M + \lambda) U^T$ with $U \in SU(4)$.

The gauge-kinetic term for Ψ , including the electroweak and TC interactions is

$$\mathcal{L}_{\text{KE}} = i\Psi^\dagger \bar{\sigma}^\mu (\partial_\mu - iA_\mu - iG_\mu^a \tau^a / 2 \mathbb{1}_4) \Psi, \quad (8)$$

where $\bar{\sigma}_\mu = (1, -\vec{\sigma}_\mu^i)$ and

$$A_\mu = \text{diag} \left[g_2 W_\mu^a \frac{1}{2} \tau^a, -g_1 B_\mu \frac{1}{2} \tau^3 \right]. \quad (9)$$

We preface our analysis of the IR with a brief discussion of discrete symmetries in the UV theory. With the weak interactions turned off, the only discrete symmetry of the gauge-kinetic Lagrangian lying outside of $SU(4)$ is CP , under which Ψ transforms as

$$CP: \Psi(x^\mu) \mapsto i\epsilon C^{-1} \Psi^*(x_\mu). \quad (10)$$

Due to the pseudoreality of the $SU(2)_{\text{TC}}$ fundamental, P and C are separately unphysical, only being defined up to arbitrary $SU(4)$ rotations. The EW interactions in (8) are CP invariant, with $A_\mu \mapsto A_\mu^T$ under CP . For simplicity, we take real $m_{1,2}$, $\lambda_{U,D}$, i.e. CP invariant V_{UV} . We have checked to $\mathcal{O}(p^4)$ in the chiral expansion [31] that this

yields $\alpha = \arg(v) = 0$ at the minimum of the potential (if NDA is not grossly violated), which we assume below.

G_{LR} -parity interchanges the generators of $SU(2)_L$ and $SU(2)_R$. It is an element of the unbroken $Sp(4)$, transforming $\Psi \mapsto \mathcal{G}_{LR}\Psi$, with

$$\mathcal{G}_{LR} = -\begin{pmatrix} 0 & \sigma_2 \\ \sigma_2 & 0 \end{pmatrix}, \quad (11)$$

up to an overall phase. This can be seen by extending to the left-right symmetric gauge group, i.e. replacing $g_1 B_\mu \tau^3 \mapsto g_{2R} W_{R\mu}^a \tau^a$, and requiring that under G_{LR} the top and bottom two components of Ψ are exchanged, and $g_{2L} W_L \leftrightarrow g_{2R} W_R$. G_{LR} invariance of V_{UV} would imply $m_1 = m_2$ and $\lambda_U = \lambda_D$.

III. THE VACUUM ALIGNMENT AND SCALARS

The $SU(4)/Sp(4)$ coset contains five broken generators X^a in the 5-plet of $Sp(4)$, and ten unbroken ones T^a in the adjoint, satisfying $X\Phi - \Phi X^T = 0$, $T\Phi + \Phi T^T = 0$ [25]. The isotriplets are $T^{a=1,2,3} = \text{diag}[\tau^a, (-)^a \tau^a]/2\sqrt{2}$,

$$T^{a=4,5,6} = \frac{1}{2\sqrt{2}} \begin{pmatrix} c_\theta \tau^{a-3} & -i s_\theta \tau^{a-3} \tau^2 \\ -i (-)^a s_\theta \tau^{a-3} \tau^2 & (-)^a c_\theta \tau^{a-3} \end{pmatrix}, \quad (12)$$

and $X^{a=1,2,3}$, obtained via $c_\theta \rightarrow s_\theta$, $s_\theta \rightarrow -c_\theta$ in T^{a+3} . The other generators are listed in [25] (with $T^{7,\dots,10}$ denoted $T_{\parallel}^{1,\dots,4}$). The 5-plet decomposes as $(2, 2) + (1, 1)$ under the $Sp(4)$ subgroup $SU(2)_1 \times SU(2)_2$, where $SU(2)_{1,2}$ are identified with the generators $(T^a \pm T^{a+3})/\sqrt{2}$, $a = 1, 2, 3$, and reduce to $SU(2)_{L,R}$ in the $\sin \theta \rightarrow 0$ limit. $T^{1,2,3}$ are the generators of the isospin group $SU(2)_V = SU(2)_{L+R} = SU(2)_{1+2}$.

Following [32], the $Sp(4) \cong SO(5)$ 5-plet of Nambu-Goldstone bosons (NGB's) $\vec{\pi}$ appears in the exponential

$$\xi = \exp(\sqrt{2}i\pi^a X^a/f) \mapsto U\xi V^\dagger, \quad (13)$$

where f is the TC decay constant in the chiral limit and the transformation applies to the global rotations $U \in SU(4)$, $V \in Sp(4)$, thus $V\Phi V^T = \Phi$. The π^a transform under CP like the vector currents $\Psi^\dagger \bar{\sigma}_\mu X^a \Psi$, see (10), and similarly for G_{LR} , yielding CP -odd (even) $\pi^{1,3,5}$ ($\pi^{2,4}$), and G_{LR} -odd (even) $\pi^{1,2,3,5}$ (π^4).

The kinetic terms are expressed in terms of $C_\mu = i\xi^\dagger D_\mu \xi$. Projecting onto the broken and unbroken directions defines ($C_\mu = d_\mu + E_\mu$)

$$\begin{aligned} d_\mu &= 2\text{tr}(C_\mu X^a)X^a \mapsto V d_\mu V^\dagger, \\ E_\mu &= 2\text{tr}(C_\mu T^a)T^a \mapsto V(E_\mu + \partial_\mu)V^\dagger, \end{aligned} \quad (14)$$

which, respectively, are a 5-plet and 10-plet of $Sp(4)$, transforming homogeneously and like a gauge field, as indicated. We further define the building blocks

$$\chi_\pm = \xi^T(M + \lambda)\xi\Phi \pm \text{H.c.}, \quad (15)$$

transforming as $\chi_\pm \mapsto V\chi_\pm V^\dagger$ under $Sp(4)$.

The leading $\mathcal{O}(p^2)$ chiral Lagrangian is

$$\mathcal{L}^{(2)} = \frac{f^2}{2} \text{tr}(d_\mu d^\mu) + 4\pi f^3 Z_2 \text{tr}(\chi_+), \quad (16)$$

where $Z_2 \approx 1.47 \pm 0.26$ at this order, according to a recent $N_c = n_f = 2$ lattice study [33].¹ The TC and Higgs gauge-kinetic terms yield the EW scale ($v_W = 246$ GeV)

$$v_W^2 = f^2 \sin^2 \theta + v^2. \quad (17)$$

Minimizing the $\mathcal{O}(p^2)$ potential ($m_{12} = m_1 + m_2$, $\lambda_{UD} = \lambda_U + \lambda_D$)

$$\begin{aligned} V_{\text{eff}}^{(2)} &= 8\pi f^3 Z_2 (m_{12} \cos \theta - \lambda_{UD} v \sin \theta / \sqrt{2}) \\ &+ m_H^2 v^2 / 2, \end{aligned} \quad (18)$$

yields ($m_{UD}, m_{12} > 0$ and $\theta \in [\pi/2, \pi]$)

$$\begin{aligned} \tan \theta &= -\frac{m_{UD}}{m_{12}}, \quad v = \frac{4\sqrt{2}\lambda_{UD} \sin \theta f^3 \pi Z_2}{m_H^2} \\ \Rightarrow \sin \theta &= \sqrt{1 - \frac{m_{12}^2}{\lambda_{UD}^4} \frac{m_H^4}{16\pi^2 f^6 Z_2^2}}. \end{aligned} \quad (19)$$

For simplicity, we have ignored the quartic in (18), motivated by SUSY BTC where it is a small perturbation. The effects of EW gauge boson loops, which favor a vacuum alignment $\sin \theta \rightarrow 0$ [34,35], also constitute a small perturbation provided $m_{12}/f \gg \alpha_{EW}$; this is indeed the case in the numerical examples below and thus we ignore such effects in what follows. The limit $m_{12}/f \lesssim \alpha_{EW}$ is also of interest,² and will be considered elsewhere [31].

To elucidate the structure of the vacuum and scalar mass matrices, we project $(M + \lambda)$ onto the $Sp(4)$ singlet ($\alpha\Phi$ below) and vector directions, yielding

¹The value of Z_2 is obtained by comparing chiral limit pion masses following from Eq. (16) with analogous expressions in [33]. In the notation of the latter, $m_\pi^2 = 2Bm_f$, yielding the translation $Z_2 = B/(8\pi f)$. The lattice results for B and f are quoted with fractional errors of $\approx 8\%$ and $\approx 16\%$, respectively, corresponding to a fractional error $\delta Z_2/Z_2 \approx 0.26$. This uncertainty is sufficiently small so as not to qualitatively impact the spectra and associated tunings we examine below, i.e. variation of Z_2 within the given error can be compensated in physical quantities by $\mathcal{O}(10\%)$ modifications of other free parameters.

²In this case, $\tan \theta = \mathcal{O}(m_{UD}/\alpha_W f)$, and small to moderate $\sin \theta$ would correspond to $m_{UD} = \mathcal{O}(\text{few})$ GeV, or $\lambda_{UD} = \mathcal{O}(10^{-2})$.

$$M + \lambda = -\frac{1}{2} \left(\hat{m} + \frac{\lambda_{UD}\sigma_h + i\delta\lambda_{UD}\pi_h^3}{2\sqrt{2}} s_\theta \right) \Phi + \frac{i}{2} \Phi (\lambda_{UD}\chi_\theta^a + i\delta\lambda_{UD}\chi_\theta'^a) X^a, \quad (20)$$

where the $Sp(4)$ singlet fermion mass and vectors are

$$\begin{aligned} \hat{m} &\equiv \frac{1}{2} (-m_{12}c_\theta + m_{UD}s_\theta) = 2\pi f^3 Z_2 \lambda_{UD}^2 / m_H^2 |_{\theta < \pi} \\ \vec{\chi}_\theta &= (\pi_h^1, \pi_h^2, \pi_h^3, \sigma_h c_\theta + v c_\theta + \sqrt{2} m_{12} s_\theta / \lambda_{UD}, 0) \\ &= (\pi_h^1, \pi_h^2, \pi_h^3, \sigma_h c_\theta, 0) \\ \vec{\chi}'_\theta &= (-\pi_h^2, \pi_h^1, \sigma_h + v, \pi_h^3 c_\theta, \delta m_{12} / \delta \lambda_{UD}), \end{aligned} \quad (21)$$

$c_\theta \equiv \cos \theta$, $\delta m_{12} \equiv m_1 - m_2$, etc., and the $O(4)$ components of $\vec{\chi}_\theta, \vec{\chi}'_\theta$ have opposite CP [36]. The constant terms in $\vec{\chi}_\theta$ must cancel to avoid a constant $\times \pi^4$ term in V_{eff} , induced by operators $\propto \vec{\chi}_\theta \cdot \vec{\pi}$. Thus, $t_\theta = -m_{UD}/m_{12}$ holds to all orders. $\vec{\pi}_h$ and $\pi^{1,2,3}$ are aligned, being $SU(2)_V$ triplets, however π^4 is rotated by θ relative to σ_h .

The $\mathcal{O}(p^2)$ charged scalar and neutral Higgs mass matrices are

$$\begin{aligned} M_{\pi^\pm}^2 &= m_H^2 \begin{pmatrix} 1 & -t_\beta \\ -t_\beta & t_\beta^2 \end{pmatrix}, \\ M_h^2 &= m_H^2 \begin{pmatrix} c_\theta^2 & -c_\theta t_\beta \\ -c_\theta t_\beta & t_\beta^2 \end{pmatrix} + \begin{pmatrix} m_H^2 s_\theta^2 & 0 \\ 0 & 0 \end{pmatrix}, \end{aligned} \quad (22)$$

in the bases (π_h^\pm, π^+) and (σ_h, π^4) , respectively, where

$$t_\beta \equiv \tan \beta = v / (f \sin \theta). \quad (23)$$

$M_{\pi^\pm}^2$ and the first term in M_h^2 are related by $Sp(4)$ invariance: their (1,1), (1,2), and (2,2) entries are $\propto \vec{\chi}_\theta \cdot \vec{\chi}_\theta, \vec{\chi}_\theta \cdot \vec{\pi}$, and $\vec{\pi} \cdot \vec{\pi}$, respectively. [The (2,2) entries correspond to the Gell-Mann-Oakes-Renner pion mass relation for fermion mass \hat{m} , i.e. $m_\pi^2 = m_H^2 t_\beta^2 = 16\pi f Z_2 \hat{m}$.] Both matrices have massless eigenstates: the eaten NGB's G^a and would-be light Higgs. The latter's mass is lifted by the contribution of the second term in M_h^2 to the $Sp(4)$ singlet, $\propto (\sigma_h s_\theta)^2$. The mass eigenstates are

$$\begin{aligned} G^\pm &= s_\beta \pi_h^\pm + c_\beta \pi^\pm, & \tilde{\pi}^\pm &= -c_\beta \pi_h^\pm + s_\beta \pi^\pm, \\ h_1 &= c_\alpha \sigma_h - s_\alpha \pi^4, & h_2 &= s_\alpha \sigma_h + c_\alpha \pi^4, \end{aligned} \quad (24)$$

where $\tan 2\alpha = \cos \theta \tan 2\beta$. The nonzero masses are

$$\begin{aligned} m_\pi^2 &= m_H^2 / c_\beta^2, \\ m_{h_{1,2}}^2 &= m_H^2 \left(1 \mp \sqrt{1 - s_\theta^2 s_{2\beta}^2} \right) / (2c_\beta^2), \end{aligned} \quad (25)$$

where h_1 and h_2 are the light and heavy neutral Higgs, respectively. There are additionally two neutral pion states, G^0 and $\tilde{\pi}^0$, and an isosinglet, π^5 , with mass $m_H^2 t_\beta^2$. In the limit³ $s_\theta^2 c_\beta^2 \ll 1$,

$$m_{h_1}^2 = m_H^2 \sin^2 \beta \sin^2 \theta. \quad (26)$$

Thus, a dominantly fundamental Higgs with subleading composite pNGB component (π^4 is massless for $m_{1,2}, \lambda_{U,D} \rightarrow 0$) acquires its mass from strong sector vacuum misalignment, as in composite pNGB Higgs models, see e.g. [37–39].

Note that small values of s_θ require tuning, cf. (19). The largest irreducible tuning of s_θ is due to λ_{UD} , and can be quantified as $|d \log s_\theta / d \log \lambda_{UD}| = 2 \cot^2 \theta$. The tuning due to f is, in principle, 50% larger. However, this is significantly reduced if f and m_H are correlated, e.g. via SUSY breaking (thus accounting for their proximity, see Table II and concluding remarks).

The light Higgs $h_1 VV$ ($V = W^\pm, Z$) and $h_1 \tilde{f} f$ couplings normalized to the SM ones, κ_V and κ_F , and their $s_\theta^2 \ll 1$ limits are

$$\begin{aligned} \kappa_V &= c_\alpha s_\beta - s_\alpha c_\beta c_\theta \rightarrow 1 - c_\beta^2 s_\theta^2 / 2, \\ \kappa_F &= c_\alpha / s_\beta \rightarrow 1 - c_{2\beta} c_\beta^2 s_\theta^2 / 2; \end{aligned} \quad (27)$$

constraints on these couplings from the LHC are at the level of 15% and 25% respectively [40].

There are two $Sp(4)$ covariant gauge field strengths [25],

$$\mathcal{D}_{\mu\nu} = \nabla_{[\mu} d_{\nu]}, \quad \mathcal{F}_{\mu\nu} = -i[\nabla_\mu, \nabla_\nu]. \quad (28)$$

$\nabla_\mu \mathcal{O} = \partial_\mu \mathcal{O} - i[E_\mu, \mathcal{O}]$ is the $Sp(4)$ covariant derivative. They transform homogeneously under $Sp(4)$, with $\mathcal{D}_{\mu\nu}$ a 5-plet and $\mathcal{F}_{\mu\nu}$ a 10-plet. The effective operator

$$\mathcal{L}_{\chi\mathcal{F}\mathcal{F}} = \frac{\lambda_\chi \sec \beta \sin \theta}{64\pi^3 v_W} \text{tr}(\chi^+ \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}) \quad (29)$$

$[\lambda_\chi = \mathcal{O}(1)$ in NDA] induces an $h_1 \gamma \gamma$ coupling

$$\mathcal{L} = c_\gamma^{\text{TC}} \frac{\alpha}{\pi v_W} h_1 A_{\mu\nu} A^{\mu\nu}, \quad c_\gamma^{\text{TC}} = \frac{\lambda_\chi \lambda_{UD} c_\alpha}{32\sqrt{2}\pi c_\beta} s_\theta^2, \quad (30)$$

compared to $c_\gamma^{\text{SM}} \simeq .23$. Including the modified Higgs couplings to t, W in the $h_1 \rightarrow \gamma \gamma$ decay rate [41], we obtain

³The Higgs quartic is included in (22) by substituting $m_H^2 \rightarrow m_H^2 + \lambda_h^2 v^2 / 2$ and, additionally, shifting $(M_h^2)_{1,1}$ by $\lambda_h v^2$, thus perturbing $m_{h_1}^2$ by $\approx \lambda_h v^2$ and $\tan \alpha$ by $\approx t_\alpha c_\beta^2 \lambda_h v^2 / m_H^2$.

TABLE II. Examples of vacuum alignment, scalar spectrum, and R_{10} properties, see text (all masses are in GeV).

f	m_{12}	m_H	λ_{UD}	s_θ	c_β	s_α	v	\hat{m}	$m_{\tilde{\pi}}$	m_{h_2}	M_{10}	F_{10}	$\sigma_{pp \rightarrow r_1^+}$ [fb]	$\sigma_{pp \rightarrow r_2^+}$ [fb]	$\text{Br}_{r_1^+ \rightarrow WZ}$	$\text{Br}_{r_2^+ \rightarrow h_1 W}$	$\Gamma_{r_1^+}$	$\Gamma_{r_2^+}$
93	190	212	0.84	0.6	0.23	0.19	240	119	930	922	1585	167	5.28	3.38	0.089	0.072	29	23
165	200	323	0.52	0.4	0.27	0.25	237	109	1199	1193	2504	282	0.50	0.42	0.06	0.06	115	106
232	240	433	0.45	0.3	0.28	0.27	236	126	1531	1526	3429	392	0.054	0.049	0.04	0.04	279	271
261	50	341	0.14	0.4	0.43	0.41	223	27	802	792	3538	427	0.046	0.039	0.043	0.039	1228	1219
367	60	463	0.12	0.3	0.45	0.44	220	31	1033	1025	4950	599	0.001	0.001	0.05	0.05	1799	1793

$$\Gamma_{\gamma\gamma}/\Gamma_{\gamma\gamma}^{\text{SM}} \simeq 1.52|\kappa_F c_\gamma^{\text{SM}} - 1.04\kappa_V + c_\gamma^{\text{TC}}|^2. \quad (31)$$

Thus, the TC shift in $\Gamma_{\gamma\gamma}$ is suppressed by s_θ^2 , like $\Gamma_{VV, \tilde{f}f}$.

Significant effects enter beyond $\mathcal{O}(p^2)$, away from the chiral limit, e.g. in examples with $\hat{m} \sim f$. However, our conclusions are not qualitatively altered [31]: $t_\theta = -m_{UD}/m_{12}$ holds to all orders, as already argued; v , $\sin\theta$ and m_h^2 retain the forms given in (19) and (26), up to negligible corrections from cubic and higher order Higgs couplings, with $Z_2 \rightarrow Z_2[1 + \mathcal{O}(\hat{m}/2\pi f)]$ and $m_H^2 \rightarrow m_H^2 + \mathcal{O}(\lambda_{UD}^2 f^2)$. As at $\mathcal{O}(p^2)$, $m_{h_1}^2$ is suppressed by s_θ^2 . In (17) and (23), f is replaced by the full TC-pion decay constant, $f \rightarrow f[1 + \mathcal{O}(\hat{m}/4\pi)]$. Isospin and G_{LR} combined imply that $\tilde{\pi}^3 - \pi^5$ mass mixing would be $\propto \delta m_{12} \delta \lambda_{UD} \times (f \sin\theta, v)$, thus first entering at $\mathcal{O}(\chi^{\pm 2})$, or $\mathcal{O}(p^4)$.

There are two $Sp(4)$ singlet C -even scalar resonances of note, with masses of $\mathcal{O}(\Lambda)$: the P -even σ and P -odd η' . The σ is not broad if $\sigma \rightarrow \tilde{\pi} \tilde{\pi}, h_2 h_2$ are kinematically forbidden; the η' has a gluonic component due to the TC axial $U(1)$ anomaly. They have well defined C and P transformations, possessing dimension-5 σAA and anomaly induced $\eta' A \tilde{A}$ couplings, unlike the π^a (however, anomalous $\pi^5(W\tilde{W}, Z\tilde{Z}, A\tilde{Z})$ couplings exist [26,30]). The σ induces the NDA shifts $\delta m_h^2 \sim -\lambda_{UD}^2 f^2 s_\theta^2$; $\delta \kappa_V \sim \lambda_{UD} c_\beta s_\theta^2/(4\pi)$; negligible $\delta \kappa_F$; and $\delta c_\gamma^{\text{TC}}/c_\gamma^{\text{TC}} \sim 1$ [31].

IV. THE VECTOR RESONANCES

All resonances appear in representations of $Sp(4)$. We consider the lowest lying 10- and 5-plet vectors (we do not consider the singlet here),

$$\hat{R}_{10} = R_{10}^a T^a, \quad \hat{R}_5 = R_5^a X^a, \quad (32)$$

with $\hat{R} \mapsto V \hat{R} V^\dagger$ under $Sp(4)$ (see also Ref. [42]). Under $SU(2)_1 \times SU(2)_2$, the 10 = (3, 1) + (1, 3) + (2, 2), where $R_{10}^{a\pm} = (R_{10}^a \pm R_{10}^{a+3})/\sqrt{2}$, $a = 1, 2, 3$, are the two triplets. $R_{10}^{1,2,3}, R_{10}^{4,5,6}$, and $R_5^{1\dots 3}$ are triplets under $SU(2)_V$. G_{LR} interchanges $SU(2)_{1 \leftrightarrow 2}$, in addition to $SU(2)_{L \leftrightarrow R}$, and $R_{10}^+ \leftrightarrow R_{10}^-$. The transformations of $\Psi^\dagger \tilde{\sigma}_\mu T^a \Psi$ imply G_{LR} -even (odd) $R_{10}^{1,2,3}$ ($R_{10}^{4,5,6}$); and CP -even (odd) $R_{10}^{2,5}$ ($R_{10}^{1,3,4,6}$). R_5^a transforms like π^a . The Lorentz vector indices are also raised/lowered under CP . Based on the vector

currents for $R_{10}^{1,2,3}$ and $R_5^{1,2,3}$ at $\theta = \pi/2$, \hat{R}_{10} and \hat{R}_5 generalize the QCD $\vec{\rho}$ and \vec{a}_1 triplets, respectively. However, R_{10}^a and R_{10}^{a+3} , $a = 1, 2, 3$, are the G_{LR} ‘‘parity doubling partners.’’

We use the antisymmetric tensor formalism for vectors [36,43,44]. It is convenient for describing vector interactions with electroweak gauge fields, and avoids field redefinitions. The kinetic terms are

$$\mathcal{L}_{\text{kin}} = -\frac{1}{2} \text{tr} \left(\nabla^\lambda \hat{R}_{\lambda\mu} \nabla_\nu \hat{R}^{\nu\mu} - \frac{1}{2} M_R^2 \hat{R}_{\mu\nu} \hat{R}^{\mu\nu} \right), \quad (33)$$

where M_R^2 is the mass in the chiral limit, and R denotes R_5 or R_{10} . A related object,

$$R_\mu = -M_R^{-1} \nabla^\nu R_{\nu\mu}, \quad (34)$$

satisfies the massive Proca equation, and $\langle 0 | R_\mu | R \rangle = \epsilon_\mu$.

The most general $\mathcal{O}(p^2)$ Lagrangian, linear in $\hat{R}_{5,10}$,

$$\mathcal{L}_R^{(2)} = \text{tr} \left(\hat{R}_{10,\mu\nu} \left[\frac{F_{10}}{\sqrt{2}} \mathcal{F}^{\mu\nu} + i G_{10} d^\mu d^\nu \right] + \frac{F_5}{\sqrt{2}} \hat{R}_{5,\mu\nu} \mathcal{D}^{\mu\nu} \right) \quad (35)$$

yields the bilinears ($a = 1, 2, 3$)

$$\begin{aligned} \mathcal{L}_{\text{bilinear}} = & -\frac{1}{4} F_{10} R_{10}^a (g_2 W^a + g_1 B \delta^{a3}) \\ & -\frac{1}{4} (F_{10} c_\theta R_{10}^{a+3} - F_5 s_\theta R_5^a) (g_2 W^a - g_1 B \delta^{a3}), \end{aligned} \quad (36)$$

where $F_{10,5}$ are the vector decay constants,

$$\langle R_{10(5)}^a | \Psi^\dagger \tilde{\sigma}_\mu T^a \Psi | 0 \rangle = -i F_{10(5)} M_{10(5)} \epsilon_\mu^*, \quad (37)$$

with $M_{10,5}$ the total masses. They induce $R_{5,10}$ couplings to the SM fermions, responsible for vector Drell-Yan (DY) production, and obtained via the following substitutions in the SM couplings,

$$\begin{aligned}
W_\mu^a &\rightarrow W_\mu^a - \frac{g_2 F_{10}}{2M_{10}} (R_{10,\mu}^a + R_{10,\mu}^{a+3} c_\theta) + \frac{g_2 F_5}{2M_5} R_{5,\mu}^a s_\theta \\
B_\mu &\rightarrow B_\mu - \frac{g_1 F_{10}}{2M_{10}} (R_{10,\mu}^3 - R_{10,\mu}^6 c_\theta) - \frac{g_1 F_5}{2M_5} R_{5,\mu}^3 s_\theta. \quad (38)
\end{aligned}$$

The leading R_{10} decays originate from the $\mathcal{L}_R^{(2)}$ trilinears,

$$\begin{aligned}
& - \frac{G_{10} M_{10}}{2\sqrt{2} f^2} (\epsilon^{abc} R_{10,\mu}^a \pi^b \partial^\mu \pi^c + R_{10,\mu}^{a+3} [\pi^5 \partial^\mu \pi^a - \pi^a \partial^\mu \pi^5]) \\
& + \dots, \quad (39)
\end{aligned}$$

where the ellipses denote couplings of $R_{10}^{7,\dots,10}$. In the vector meson dominance (VMD) approximation, $G_{10} = -2\sqrt{2} f^2 / F_{10}$ (the VMD $\rho\pi\pi$ coupling, $g_{\rho\pi\pi} = -m_\rho / f_\rho$, is 16% below experiment; ϕKK is within a few %). Projecting (39) onto the G^a gives couplings to longitudinal W_L, Z_L . For $\hat{m} \sim f$, $R_{10}^{1,2,3,(4,5,6)} \rightarrow \tilde{\pi} \tilde{\pi}, (h_2 \tilde{\pi})$ are closed, and $R_{10}^{1,2,3,(4,5,6)} \rightarrow \tilde{\pi} W_L / Z_L, (\tilde{\pi} h_1, h_2 W_L / Z_L)$ dominate.

The UV contribution to the S parameter can be parametrized in terms of the effective Lagrangian coupling, $-g_1 g_2 S_{UV} / (32\pi) W_{\mu\nu}^3 B^{\mu\nu}$. Tree-level $R_{10}^{3,6}, R_5^3$ exchange, cf. (36), thus yields

$$\Delta S_{\text{tree}} = 4\pi (F_{10}^2 / M_{10}^2 - F_5^2 / M_5^2) \sin^2 \theta. \quad (40)$$

The s_θ^2 suppression is a feature of misalignment [37–39,45,46] (S_{UV} is $\Delta I = 1$, and the underlying operators $\text{tr}(2\mathcal{F}^2), \text{tr}(\mathcal{D}^2) \supset \pm g_1 g_2 W_{\mu\nu}^3 B^{\mu\nu} s_\theta^2 / 2$ [25]). It has an explicit origin in (40): $R_{10}^{3,6}$ parity doubling cancelation $\propto 1 - c_\theta^2$; and s_θ suppression of the R_5^3 couplings. The scalar loops in S are log divergent, due to a c_θ factor in the π^4 gauge boson couplings. After subtracting the SM Higgs,

$$\Delta S_{\text{loop}} = \frac{1}{24\pi} \left(s_\theta^2 \log \frac{\Lambda^2}{m_{h_1}^2 s_\alpha^2 m_{h_2}^2 c_\alpha^2} + F_{\text{fin}} \right), \quad (41)$$

where F_{fin} contains finite loop contributions [31]. The first term receives a s_α^2 suppression that is not present in the composite Higgs case, due to projection of π^4 onto h . For cutoff $\Lambda \leq 8\pi f$, we find $\Delta S_{\text{loop}} < 0.01$ in our examples. A more refined dispersion integral approach containing higher order $R_{5,10}$ contributions [47] would eliminate the divergence, with S remaining a small effect.

The T parameter arises from: (i) scalar loops with isospin breaking entering via $\tilde{\pi}^3 - \eta', \pi^5$ mixings, and $\tilde{\pi}^3 - \tilde{\pi}^+$ mass splitting; (ii) G^+ wave function renormalization via $B - R_{5,10}^{1,2,4,5}$ loops. The loops in (i) vanish in the $\delta\lambda_{UD} \rightarrow 0$ limit, and in (ii) they are c_θ^2 suppressed (due to projection onto G^+) compared to the composite Higgs and TC analogs [47–49]. Thus, S and T reasonably lie within the allowed 1σ ellipse [50,51].

Fermion mass corrections to $M_{10,5}$ arise from terms $\propto \text{tr}(\hat{R}_{10,5}^2 \chi_\pm)$ at $\mathcal{O}(p^2)$, and larger χ^+ multiplicities at higher orders. In the limit $\delta m_{12}, \delta m_{UD} \rightarrow 0$ they respect $Sp(4)$, and are θ -independent polynomials in \hat{m} , as seen from (20). This is true of all corrections to the chiral limit. Thus, the $\theta = \pi/2$ lattice measurements [33] (also see [52]) of f_π (full decay constant), m_π^2 , and $M_{10,5}$ hold for arbitrary θ . F_{10} can be estimated by scaling a fit to the quark mass dependence of QCD vector decay constants, normalized to the observed pion decay constant. Using $f_{\rho,\omega,\phi}$, and the lattice heavyonium decay constant between $m_{J/\Psi}$ and m_Υ [53,54], yields a function \mathcal{F} such that $F_{10}/f \approx \mathcal{F}[\hat{m}/f] (f_\rho/f_\pi)_{\text{QCD}}$ (or $F_{10}/f \approx [1.6, 1.8]$ for $\hat{m}/f = [0, 1.5]$) [20,31]. The contribution of R_5 in (40) is bounded via the approximate upper and lower bounds, $M_5 < M_{10} m_{a_1} / m_\rho$ (M_5/M_{10} decreases beyond the chiral limit, approximated by the QCD ratio) and $F_5 > f_{a_1} f / f_\pi^{\text{qcd}}$ (F_5 increases away from the chiral limit, obtained by scaling from QCD). We take $f_{a_1} = 152$ MeV [55] for the poorly known decay constant, using an updated $\text{Br}(\tau^+ \rightarrow \nu_\tau \pi^+ \pi^+ \pi^-)$.

The above procedure yields $\Delta S_{\text{tree}}/s_\theta^2 < [0.11, 0.09]$ ($[0.19, 0.13]$ for R_{10}) for $\hat{m}/f = [0, 1.5]$, confirming that agreement with the observed 1σ range $\Delta S = 0.10 \pm 0.08$ [50], 0.00 ± 0.08 [51] is reasonable. The significant decrease in the R_{10} contribution away from the chiral limit reflects the greater vector mass vs. decay constant quark mass dependence observed in QCD.

V. EXAMPLES

The vector masses can span a wide range, due to the freedom to vary $\sin \theta$ and the TC fermion masses. This is illustrated in the representative examples of Table II, for different values of the UV inputs $f, m_H, m_{12}, \lambda_{UD}$ (with $\delta m_{12}, \delta \lambda_{UD} = 0$), where the two isotriplet charged vectors are defined as $r_{1(2)}^\pm \equiv (R_{10}^{1(4)} \mp i R_{10}^{2(5)}) / \sqrt{2}$. The vacuum alignment and scalar spectrum have been obtained at $\mathcal{O}(p^2)$, with $Z_2 = 1.47$ [33], imposing the $m_{h_1} = 125$ GeV, $v_W = 246$ GeV, and neglecting the Higgs quartic for simplicity. The tuning of $s_\theta = .6, .4, .3$ (due to λ_{UD}) is approximately 30%, 10%, 5%, respectively. Note that m_H is essentially fixed by $\sin \theta$; both m_H and f (or $\Lambda_{\text{TC}} \sim 4\pi f$) increase as $\sin \theta$ decreases; while for given $\sin \theta$, f increases as m_{12} and \hat{m} decrease. In all of the examples, the deviations in κ_V and κ_F from 1 (SM) are $< 1\%$, and the deviations in the Higgs diphoton decay width from its SM value are $< 2\%$ for $|\lambda_\chi| \leq 2$, cf. (30), (31) (with the exception of the first example, where a deviation as large as 6% is possible).

M_{10} follows from [33] and F_{10} from the scaling described above. The vector decay widths follow from the VMD estimate for G_{10} . The narrow width approximation is used throughout. In the first example, the $R_{10} \rightarrow \tilde{\pi} \tilde{\pi}, h_2 \tilde{\pi}$ channels are closed, yielding relatively

narrow widths. In the last two examples, with $\hat{m}/f \sim 0.1$, the phase space suppression in the $R_{10} \rightarrow \tilde{\pi} \tilde{\pi}, h_2 \tilde{\pi}$ channels is small, yielding very large widths, thus the narrow width approximation is rough. In general, the combination of $F_{10}/M_{10} \sim 0.1$ and small branching fractions to pairs of gauge bosons implies that the vector resonances are safe (by at least $\mathcal{O}(10\text{--}100)$ for $M_{10} \sim 1\text{--}3$ TeV) from current LHC bounds.

VI. DISCUSSION

BTC with $N_c = n_f = 2$ provides the minimal UV complete realization of the partially composite-pNGB Higgs. Several other noteworthy features are summarized below: (i) $\Lambda_{TC} \gtrsim 3$ TeV and an enhanced Higgs mass parameter, e.g. $m_H \sim 3m_h$, are accessible with moderate s_θ , or tuning. (In the TC-vacuum, sub-10% deviations in the Higgs couplings would require $f < 100$ GeV, or $\Lambda_{TC} \lesssim 1$ TeV [20,21]); (ii) deviations from the SM Higgs couplings of $\mathcal{O}(1\%)$ are typical, due to suppression by $s_\theta^2 c_\beta^2$; (iii) The ratio f/M_{10} on the lattice suggests that agreement with the S parameter at 1σ is realized at moderate s_θ ; while potentially dangerous T parameter loops are $c_\beta^2 = \mathcal{O}(0.1)$ suppressed; (iv) detection of vector mesons at the LHC will be challenging.

Our ultimate goal is natural EW symmetry breaking. In the present context this would involve linking the size of the Higgs mass parameter to the TC scale, $\Lambda_{TC} = \mathcal{O}(3\text{ TeV})$. One direction that we are exploring is embedding our setup into a supersymmetric theory with Dirac gauginos. Supersymmetrized minimal BTC is formulated as supersymmetric QCD with $N_c = n_f = 2$ and one adjoint matter superfield. This theory is known to have a strong IR fixed point, with unbroken chiral symmetry [56,57]; a two-loop estimate yields a fixed point coupling $\alpha^* \approx 1.8$. A direct

link between the scale of TC superpartner masses and Λ_{TC} can be realized if the Dirac TC-gaugino and scalar matter fields decouple in the superconformal region [15,16].⁴ Integrating out these massive states triggers a confining phase with $\Lambda_{TC} \lesssim m_{\tilde{g}_{TC}}$. The Higgs mass, $m_H \sim m_{\tilde{W}}/4\pi$ generated with finite loops of Dirac EW gauginos [59,60], can then naturally be of order $f \sim \Lambda_{TC}/4\pi$ if the SM gaugino masses satisfy $m_{\tilde{W}} \sim m_{\tilde{g}_{QCD}} \lesssim m_{\tilde{g}_{TC}}$. Furthermore, the resulting effective theory contains 4-technifermion operators which affect the vacuum alignment and may allow a construction without the explicit singlet masses $m_{1,2}$.

Further study of potential UV completions, as well as detailed collider phenomenology will be presented elsewhere.

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⁴Majorana gaugino masses would undergo power law running $m_{\tilde{g}}(\mu) \propto (\mu/\Lambda)^{\gamma'}$ with $\gamma' > 0$ in the superconformal region [58]. Remarkably, we find $\gamma' < 0$ in the Dirac case, with moderate $\gamma' \approx -0.41$ at two loops, rendering the solution to the scale coincidence problem a viable one.

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