Primordial black holes as dark matter in supergravity inflation models

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We propose a novel scenario to produce abundant primordial black holes (PBHs) in new inflation which is a second phase of a double inflation in the supergravity framework. In our model, some preinflation phase before the new inflation is assumed and it would be responsible for the primordial curvature perturbations on the cosmic microwave background scale, while the new inflation produces only the small scale perturbations. Our new inflation model has linear, quadratic, and cubic terms in its potential and PBH production corresponds with its flat inflection point. The linear term can be interpreted to come from a supersymmetry-breaking sector, and with this assumption, the vanishing cosmological constant condition after inflation and the flatness condition for the inflection point can be consistently satisfied.

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I. INTRODUCTION

The primordial black holes (PBHs), which might be formed in the early radiation dominated universe, have attracted scientists for more than 40 years and are recently refocused on more and more. Theoretically they can be formed by the gravitational collapse of the Hubble patch if the mean energy density in that patch is higher by $\mathcal{O}(0.1)$ than its surroundings $[1-3]$. One of the main motivations of PBHs is dark matter (DM). Since they behave as a matter component, they can be a main component of DM without introducing other elementary particles. However PBHs are still not detected by any observation, and their abundance is constrained [4–[11\]](#page-7-1), except in a mass window of 10^{21-24} g, where PBHs can still account for all dark matter. Some recent attempts to close this window relied on assumptions that are difficult to justify. For example, the existence of neutron stars in globular clusters could help constrain the remaining window, if the density of dark matter exceeded the average by more than 2 orders of magnitude [\[12\]](#page-7-2). However, observations of globular clusters show no evidence of significant dark matter content in such systems [\[13,14\]](#page-7-3). Furthermore, it was suggested that tidal deformation of a neutron star could lead to an efficient energy dissipation and capture of a black hole, leading to stronger constraints [\[15\]](#page-7-4), but such energy losses are uncertain, and they are likely to be suppressed for realistic parameters and velocities in excess of the speed of sound [\[16,17\],](#page-7-5) so that no new constraints can be derived, and the window for PBH dark matter remains open.

As one of the series of the PBH production works, several authors have studied the PBH formation in the double inflation in the supergravity framework $[18-24]$ ¹ Following this stream, we propose a novel new inflation model as the second phase of the double inflation, where PBHs can be produced on mass $\sim 10^{22}$ g enough to constitute the bulk of DM in this paper.² As the preinflation before the new inflation, which is responsible for the curvature perturbations on the cosmic microwave background (CMB) scale, any specific model is not required to be supposed. The potential of our new inflation model consists of the linear, quadratic, and nth moment terms and we found that PBHs can be produced on \sim 10²² g enough to be a main component of DM. Our model is based on the discrete R symmetry Z_{2nR} and we find that only the $n = 3$ case could produce the desired spectrum of PBHs. It is remarkable that the linear term can be consistently interpreted to come from the supersymmetry (SUSY)-breaking sector in the case of $n = 3$ under the flatness condition at the inflection point and the vanishing cosmological constant condition. While we propose the abundant PBHs of ~10²² g as DM, we can make another peak in the PBH mass spectrum on ~30 M_{\odot} . Those PBHs would have contributed to gravitational waves which were recently detected by the LIGO/Virgo collaboration [\[25,26\]](#page-7-7) as discussed in [\[27](#page-7-8)–30].

The rest of this paper is organized as follows. In Sec. [II](#page-1-0), we describe the constitution method of new inflation in

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¹For other PBH production models, see the recent review of Ref. [\[11\].](#page-7-9)

 \rm{H}^2 In the supersymmetric framework, the lightest supersymmetric particle (LSP) can be a candidate of weakly interacting massive particle DM. Here we assume that the R parity is broken and the LSP is not stable; then we need PBH DM instead.

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supergravity and introduce our model. Then we concretely evaluate the current PBH abundance in Sec. [III.](#page-3-0) We make our conclusions in Sec. [IV.](#page-5-0) In the Appendix, we describe the treatments for the modes which exit the horizon at near the beginning of the second new inflation.

II. NEW INFLATION WITH INFLECTION POINT IN SUPERGRAVITY

Let us briefly review the composition of new inflation in supergravity first. Here we adopt the model proposed in Ref. $[31,32]$. In this model, we assume a discrete R symmetry Z_{2nR} which is broken down to a discrete Z_{2R} during and after the inflation. The inflaton superfield ϕ has an R charge 2. These assumptions lead the following effective superpotential at the leading order,

$$
W(\phi) = v^2 \phi - \frac{g}{n+1} \phi^{n+1}.
$$
 (1)

Here and hereafter we use the Planck units where the reduced Planck mass $M_p \approx 2.4 \times 10^{18}$ GeV is set to be unity. The R-invariant effective Kähler potential can be written as

$$
K(\phi) = |\phi|^2 + \frac{\kappa}{4} |\phi|^4 + \dots
$$
 (2)

For these super and Kähler potentials, the inflaton potential in supergravity is given by

$$
V(\phi) = e^{K} (D_{\phi} W K^{\phi \bar{\phi}} (D_{\phi} W)^{*} - 3|W|^{2}), \quad (3)
$$

where $D_{\phi}W = W_{\phi} + K_{\phi}W$. Defining the inflaton by the real part of ϕ , namely $\varphi = \sqrt{2} \text{Re}\phi$, it can be expanded as

$$
V(\varphi) \simeq v^4 - \frac{\kappa}{2}v^4\varphi^2 - \frac{g}{2^{n-1}}v^2\varphi^n + \frac{g^2}{2^n}\varphi^{2n},\qquad(4)
$$

and the slow-roll inflation can be driven either by the quadratic or nth moment term. Also it has a negative minimum at $\varphi_{\min} \simeq \sqrt{2} \left(\frac{v^2}{g}\right)^{\frac{1}{n}}$ as

$$
\langle V \rangle \simeq -3 \langle e^K |W|^2 \rangle \simeq -3 \left(\frac{n}{n+1}\right)^2 v^4 \left(\frac{v^2}{g}\right)^{\frac{2}{n}}.\tag{5}
$$

This negative energy is canceled out after inflation with a positive contribution μ_{SUSY}^4 due to a SUSY-breaking effect. Therefore the gravitino mass can be related with the new inflation scale as

$$
m_{3/2} \simeq \frac{\mu_{\text{SUSY}}^2}{\sqrt{3}} \simeq \frac{n}{n+1} v^2 \left(\frac{v^2}{g}\right)^{\frac{1}{n}}.\tag{6}
$$

The inflaton mass around the potential minimum is given by

$$
m_{\varphi} \simeq n v^2 \left(\frac{v^2}{g}\right)^{-\frac{1}{n}}.\tag{7}
$$

Therefore, if the inflaton decays into standard model particles simply by Planck suppressed operators, the reheating temperature can be evaluated by

$$
T_R \simeq 0.1 m_\varphi^{3/2} \simeq 0.1 n^{\frac{3}{2}} g^{\frac{3}{2n}} v^{3-\frac{3}{n}}.\tag{8}
$$

In the next section, we use this reheating temperature to calculate the PBH mass spectrum.³

Now let us consider the initial condition for this inflation. Small field new inflation generally suffers from a severe initial condition problem. That is, both the inflaton initial field value and its time derivative should be extremely small to have a sufficiently long inflation, but originally there is no reason to stabilize the inflaton field to the potential origin since the inflaton potential should be flat enough to satisfy the slow-roll conditions. Moreover, even if one can introduce some stabilizing term in the potential, new inflation realizes eternal inflation if the inflaton's initial field value is much smaller than the Hubble fluctuation $\frac{H}{2\pi}$ and it should continue much longer than 60 e-
folds (we want new inflation to contribute only to small folds (we want new inflation to contribute only to small scale perturbations as we mention). As proposed in [\[32\]](#page-7-11), these problems can be naturally solved in the supergravity framework by introducing a preinflation phase before the new inflation and adding a constant term to superpotential $W_{\text{const}} = c$.⁴ During the preinflation, the inflation of the new inflation can have a Hubble induced mass term new inflation can have a Hubble induced mass term $\frac{1}{2}V_{\text{pre}}\varphi^2 \approx \frac{3}{2}H^2\varphi^2$ through the coefficient e^K of the poten-
tial Moreover the constant term in the superpotential leads tial. Moreover the constant term in the superpotential leads the linear term $2\sqrt{2}cv^2\varphi$ in the potential, which shifts
the potential minimum from 0 to $2\sqrt{2}cv^2$. The Hybble the potential minimum from 0 to $2\sqrt{2} \frac{cv^2}{V_{\text{pre}}^2}$. The Hubble induced mass keeps stabilizing the inflaton even after the preinflation until the beginning of the second new inflation $V_{\text{pre}} \simeq v^4$, and therefore the initial field value of φ is given by

$$
\varphi_i \simeq 2\sqrt{2}\frac{c}{v^2}.\tag{9}
$$

The new inflation can avoid eternal inflation as long as φ_i is sufficiently larger than the Hubble fluctuation $\frac{H}{2\pi}$ at the beginning of the new inflation.

Taking the above things, we consider the PBH formation in the following model:

³For the parameters which we use in the next section, the reheating temperature can be estimated as $T_R \sim 8.8 \times 10^8$ GeV with the above assumption. This value may be marginal to realize the thermal leptogenesis [\[33\].](#page-7-12) However we have checked that desired PBH mass spectra can be achieved even for a higher reheating temperature e.g. $T_R \sim 10^{10}$ GeV.

⁴Note that, in the original model [\[32\]](#page-7-11), hybrid inflation is assumed as a preinflation, which gives a nonzero superpotential and leads the linear term in the potential of the new inflation. However, since we have already introduced the constant term in the superpotential, the preinflation does not need to give a nonzero superpotential in our model.

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$$
W_{\text{new}} = v^2 \phi - \frac{g}{n+1} \phi^{n+1} + c,
$$

\n
$$
K_{\text{new}} = |\phi|^2 + \frac{\kappa}{4} |\phi|^4 + ...,
$$

\n
$$
V(\varphi) \simeq v^4 - 2\sqrt{2}cv^2 \varphi - \frac{\kappa}{2} v^4 \varphi^2 - \frac{g}{2^{\frac{n}{2}-1}} v^2 \varphi^n + \frac{g^2}{2^n} \varphi^{2n} + V_{\text{pre}} \left(1 + \frac{1}{2} \varphi^2 \right).
$$
 (10)

Here note that, if $\kappa < 0$, the linear, quadratic, and *n*th moment terms can have an inflection point for $\varphi > 0$. Since V' is locally maximized at that inflection point, if the maximum of V' is still negative but quite close to 0, the slow-roll inflation is not spoiled and moreover very large curvature perturbations can be produced. The inflection point φ_* can be obtained as

$$
V''(\varphi_*) \simeq |\kappa| v^4 - \frac{n(n-1)}{2^{\frac{n}{2}-1}} g v^2 \varphi_*^{n-2} = 0
$$

$$
\Rightarrow \varphi_* = \left(\frac{2^{\frac{n}{2}-1}}{n(n-1)} \frac{|\kappa| v^2}{g}\right)^{\frac{1}{n-2}}.
$$
 (11)

Then we require the flat inflection condition as

$$
V'(\varphi_*) \simeq -2\sqrt{2}cv^2
$$

+ $\frac{n-2}{n-1} \left(\frac{2^{\frac{n}{2}-1}}{n(n-1)}\right)^{\frac{1}{n-1}} \frac{|\kappa|^{\frac{n-1}{n-2}}v^{\frac{4n-6}{n-2}}}{g^{\frac{1}{n-2}}} \sim 0,$
 $\Rightarrow g \sim \frac{1}{n(n-2)} \left(\frac{n-2}{2(n-1)}\right)^{n-2} \frac{|\kappa|^{n-1}v^{2(n-1)}}{c^{n-2}},$ (12)

neglecting V_{pre} and the higher order term. With this condition, the curvature perturbations generated around ϕ_* are large enough to produce abundant PBHs, and the concrete successful parameters are shown in the next section. Here note that the inflection point can be written as $\varphi_* = \frac{n-1}{n-2} \frac{1}{|\kappa|} \varphi_i$ under this condition and therefore it is automatically set to be slightly larger than the initial field value for $|\kappa| \sim \mathcal{O}(0.1)$. That is because the initial field value φ_i is determined by the balance between the linear term
 $\varphi_i^2 \varphi$ and the proinflation induced mass term $\varphi_i^4 \varphi_i^2$, while $cv^2\varphi$ and the preinflation-induced mass term $v^4\varphi^2$, while the flat inflection is the point where the linear term is comparable with the self-induced mass term $\kappa v^4 \varphi^2$ which is smaller than the preinflation-induced mass term by a factor $|\kappa|$.

If the new inflation is assumed to realize both small perturbations like those on the CMB scale and large perturbations which would cause the formation of PBHs, it generally takes too many e-folds in the transition from small to large perturbations since the time derivative of the slow-roll parameter itself is suppressed by the slow-roll parameters, $\frac{d}{dN} \log \epsilon_V \sim \mathcal{O}(\epsilon_V, \eta_V)$, where N denotes the elow-roll e-folding number and ϵ_V and η_V represent the slow-roll parameters $\frac{1}{2}(\frac{V'}{V})^2$ and $\frac{V''}{V}$, respectively. However, since we
have already introduced double inflation, the new inflation have already introduced double inflation, the new inflation can be free from the COBE normalization by simply assuming that the preinflation is responsible for the CMB scale perturbations, and then the new inflation can end in sufficiently short time in that case. Indeed we show in the next section that there are parameter regions where PBHs can be produced enough to be a main component of DM and the constraints for large scale perturbations like the CMB spectral distortion can be avoided. Here if one assumes that the curvature perturbations generated in the new inflation are large even apart from the inflection point, the linear term itself is required to be small enough. Letting A_{lin} denote the amplitude of the power spectrum of the curvature perturbations during the linear term in the potential dominantly contributes to the perturbations; the constant superpotential c is determined through the following relation:

$$
A_{\rm lin} = \frac{1}{12\pi^2} \frac{V^3}{V'^2} \simeq \frac{1}{96\pi^2} \frac{v^8}{c^2}, \Leftrightarrow c \simeq \frac{1}{\sqrt{96\pi^2 A_{\rm lin}}} v^4. \quad (13)
$$

Therefore, for $A_{lin} \sim 10^{-3}$, c is required to be as small as v^4 .

The above two conditions [\(12\)](#page-2-0) and [\(13\)](#page-2-1) are required for PBH formation. Now combining them clarifies the v dependence of g as $g \sim |\kappa|^{n-1}v^{6-2n}$. Therefore, in the case
of $n-3$, $g \propto |x|^2$ does not depend on the new inflation of $n = 3$, $g \sim |\kappa|^2$ does not depend on the new inflation scale *v* and could be smaller than unity. On the other hand scale v and could be smaller than unity. On the other hand, for $n \geq 4$, g becomes much larger than unity for $v \ll 1$ and such a large g spoils unitarity of the theory for example [\[34\]](#page-7-13). Moreover for large n the duration of the new inflation after the inflection point is short due to its steep potential and it tends to make the PBH mass small. Indeed we have checked that the PBH mass spectrum is tilted to the lighter mass and conflicts with the constraints on the PBH abundance for $n \geq 4$. For those reasons, we concentrate on the case of $n = 3$ hereafter.⁵

As an interesting fact, the small constant term c in the superpotential can be interpreted to come from the SUSY-breaking sector in the case of $n = 3$ [\[36\]](#page-7-14).⁶ The
SUSY-breaking E-term order u^2 a naively grises from SUSY-breaking F-term order μ_{SUSY}^2 naively arises from the term like

$$
W_{\text{SUSY}} = \mu_{\text{SUSY}}^2 Z. \tag{14}
$$

If Z obtains a vacuum expectation value $\langle Z \rangle \sim \mu_{\text{SUSY}}$, this term can lead the constant superpotential $c \sim \mu_{\text{SUSY}}^3$. Indeed
it can be realized in the dynamical SUSY-breaking models it can be realized in the dynamical SUSY-breaking models proposed in Ref. [\[37,38\]](#page-7-15) if the origin of Z is destabilized due to a large Yukawa coupling (\sim 4π), and the estimated

⁵In addition, $n = 3$ is uniquely favored by the anomaly free ordinations for supersymmetric standard gauge groups with the conditions for supersymmetric standard gauge groups with the discrete R symmetry Z_{2nR} [\[35\].](#page-7-16)

⁶Note that the case of $n = 4$ is considered in Ref. [\[36\]](#page-7-14) since the authors' motivation is not to produce PBHs but to modify the spectral index in new inflation and therefore the required condition is different.

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constant term is given by $c \sim \frac{\Lambda^3}{(4\pi)^2}$ where the dynamical scale Λ is related with μ_{SUSY} by $\mu_{SUSY}^2 = \frac{\Lambda^2}{4\pi}$. On the other hand, under the flat inflection condition [\(12\)](#page-2-0) and the large curvature perturbation condition [\(13\)](#page-2-1), the vanishing cosmological constant condition [\(6\)](#page-1-1) gives the parameter dependence of the SUSY-breaking scale as $\mu_{\text{SUSY}} \sim |\kappa|^{\frac{1-n}{2n}} v^{2n-1}$, neglecting numerical factors.
Therefore the scale dependence of the constant term Therefore the scale dependence of the constant term c is consistent with the above assumption if and only if $n = 3$ as

$$
c \sim v^4 \sim \mu_{\text{SUSY}}^3. \tag{15}
$$

It can be checked that this consistency is retained for the concrete parameter values which we show in the next section even if numerical factors are included.

III. FORMATION OF PRIMORDIAL BLACK HOLES

In this section, we calculate the PBH abundance and exemplify parameter sets where PBHs constitute the main component of DM. At first, given the inflation scale v and the reheating temperature T_R , the perturbation scale can be related with the backward e -folds by $[39]$

$$
\log\left(\frac{k}{0.002 \text{ Mpc}^{-1}}\right) \simeq -N + 56 + \frac{2}{3} \log\left(\frac{v}{10^{16} \text{ GeV}}\right) + \frac{1}{3} \log\left(\frac{T_R}{10^9 \text{ GeV}}\right). \tag{16}
$$

We use Eq. (8) as the reheating temperature hereafter. Then, with the potential [\(4\)](#page-1-3) and the Hubble induced mass $\frac{1}{2}V_{\text{pre}}\varphi^2$, we can calculate the power spectrum of the curvature perturbations $\mathcal{P}_k(k)$ in the standard linear theory curvature perturbations $P_{\zeta}(k)$ in the standard linear theory

FIG. 1. The power spectra of the curvature perturbations for parameters [\(17\)](#page-3-3) (solid line) and [\(26\)](#page-4-0) (dashed line). The red line represents the constraints on the power spectrum from the nondetection of the CMB μ distortion estimated by Eq. [\(18\).](#page-3-4) The modes $k \lesssim 10^6$ Mpc⁻¹ actually reenter the horizon between the two inflations and the treatments for them are described in the Appendix.

and the result is shown in Fig. [1](#page-3-1) as the black thick line for the following parameter values:

$$
v = 10^{-4}
$$
, $\kappa = -0.44$, $c = 1.838 \times 10^{-16}$,
\n $g = 5.036 \times 10^{-3}$. (17)

In this calculation, we have simply assumed that the preinflation potential behaves as a matter component $V_{\text{pre}} \propto a^{-3}$ after the preinflation. For these parameters, the vanishing cosmological constant [\(6\)](#page-1-1) and the SUSY-breaking assumption [\(15\)](#page-3-2) consistently predict $m_{3/2} \sim$ $10⁸$ GeV which suggests the pure gravity mediation [\[40\]](#page-7-18). In this figure, we also show the constraints from the CMB spectral μ distortion as the red region. The CMB μ distortion from the Silk damping of a single k-mode can be approximated by [\[41\]](#page-7-19)

$$
\mu \sim 2.2 \mathcal{P}_{\zeta}(k) \left[\exp \left[-\frac{k_{\text{Mpc}^{-1}}}{5400} \right] - \exp \left[-\left(\frac{k_{\text{Mpc}^{-1}}}{31.6} \right)^2 \right] \right],
$$
 (18)

where $k_{\text{Mpc}^{-1}}$ represent the wave number in Mpc⁻¹. We have used the current 2σ upper limit $\mu \leq 9 \times 10^{-5}$ by the COBE/FIRAS experiment [\[42\].](#page-7-20) Finally, the modes $k \lesssim$ 106 Mpc[−]¹ actually reenter the horizon between the preinflation and the second new inflation. We describe the treatments of these modes in the Appendix.

With use of this power spectrum, the PBH abundance can be calculated as follows. At first, the mass of PBH is almost given by the horizon mass when the overdensity reenters the horizon; let γ denote the ratio between them here. That is, the PBH mass corresponding with the scale k is given by

$$
M_{\rm PBH}(k) = \gamma \frac{4\pi}{3} \rho H^{-3} \Big|_{k=aH} = \gamma M_{\rm eq} \left(\frac{g_{* \rm eq}}{g_*}\right)^{1/2} \left(\frac{T_{\rm eq}}{T}\right)^2
$$

$$
= \gamma M_{\rm eq} \left(\frac{g_{* \rm eq}}{g_*}\right)^{1/6} \left(\frac{k_{\rm eq}}{k}\right)^2, \tag{19}
$$

where M_{eq} denotes the horizon mass at the matter-radiation equality calculated as

$$
M_{\text{eq}} = \frac{4\pi}{3} \rho_{\text{eq}} H_{\text{eq}}^{-3} = \frac{8\pi}{3} \frac{\rho_r^0}{a_{\text{eq}} k_{\text{eq}}^3}.
$$
 (20)

Also we have used an approximation that the effective degrees of freedom for energy density g_* is almost
equal to that for entropy density g_* Using $g^0 = 7.84 \times$ equal to that for entropy density g_{*s} . Using $\rho_r^0 = 7.84 \times 10^{-34}$ g cm⁻³ $k = 0.070$ h^2 Mpc⁻¹ $g^{-1} = 240000$ h^2 10⁻³⁴ gcm⁻³, $k_{eq} = 0.07 \Omega_m h^2$ Mpc⁻¹, $a_{eq}^{-1} = 24000 \Omega_m h^2$, and $g_{*eq} = 3.36$, we can finally obtain [\[4\]](#page-7-1)

$$
M_{\rm PBH}(k) = 3.6 M_{\odot} \left(\frac{\gamma}{0.2}\right) \left(\frac{g_{*}|_{k=aH}}{106.75}\right)^{-1/6} \left(\frac{k}{10^6 \,\rm{Mpc}^{-1}}\right)^{-2},\tag{21}
$$

where $M_{\odot} \simeq 2 \times 10^{33}$ g is the solar mass. In the simple analytic calculation [\[3\]](#page-7-21), γ is evaluated as $\gamma = 3^{-3/2} \approx 0.2$ and we use this value hereafter.

The formation rate of PBHs β is given by the probability of excess over the threshold. That is, under the assumption that the density perturbations follow the Gaussian distribution,

$$
\beta(M_{\rm PBH}) = \int_{\delta_c} d\delta \frac{1}{\sqrt{2\pi\sigma^2(k)}} e^{-\frac{\delta^2}{2\sigma^2(k)}} = \frac{1}{2} \text{Erfc}\left(\frac{\delta_c}{\sqrt{2}\sigma(k)}\right). \tag{22}
$$

Here δ_c represents the threshold density perturbation and we adopt the simple analytic estimation $\delta_c = p_r / \rho_r = 1/3$ [\[3\]](#page-7-21). $\sigma^2(k)$ is the variance of the comoving density perturbations coarse grained on k^{-1} , which is given by [\[46\]](#page-7-22)

$$
\sigma^{2}(k) = \int d\log k' W^{2}(k'/k) \frac{16}{81} (k'/k)^{4} \mathcal{P}_{\zeta}(k). \tag{23}
$$

 $W(z)$ represents the Fourier transformed window function and we adopt the Gaussian window $W(z) = e^{-z^2/2}$ in the following calculations. Note that the PBH mass and coarsegraining scale k are related by Eq. [\(21\).](#page-3-5) The formation rate directly gives the ratio of the PBH energy density to the total energy density at the horizon reentering, $\beta(M_{\text{PBH}})$ = $\rho_{\text{PBH}}/\rho|_{k=aH}$. Therefore the current PBH fraction to DM for a single mass mode can be derived as

$$
f_{\rm PBH}(M_{\rm PBH}) = \frac{\Omega_{\rm PBH}h^2}{\Omega_{\rm DM}h^2} = \frac{\Omega_m h^2}{\Omega_{\rm DM}h^2} \frac{\rho_{\rm PBH}(M_{\rm PBH})}{\rho} \Big|_{\rm eq}
$$

=
$$
\frac{\Omega_m h^2}{\Omega_{\rm DM}h^2} \frac{T}{T_{\rm eq}} \beta (M_{\rm PBH})
$$

=
$$
1.3 \times 10^8 \beta (M_{\rm PBH}) \left(\frac{\Omega_{\rm DM}h^2}{0.12}\right)^{-1} \left(\frac{\gamma}{0.2}\right)^{1/2}
$$

$$
\times \left(\frac{g_*}{106.75}\right)^{-1/4} \left(\frac{M_{\rm PBH}}{M_{\odot}}\right)^{-1/2}, \tag{24}
$$

where $\Omega_{DM}h^2$ represents the current DM abundance $\Omega_{\text{DM}} h^2 \sim 0.12$ [\[47\].](#page-7-23) The resultant PBH fraction is plotted in Fig. [2](#page-4-1) as the black thick line. We also show several observational constraints for PBH abundance as red regions [5–[11\].](#page-7-24) Here we have not used the constraints from the existence of neutron stars [\[12,15\]](#page-7-2) and white dwarfs [\[48\]](#page-7-25) in globular clusters since they require the high DM-density assumption whose validity seems questionable as mentioned in the introduction. Although the shown PBH fraction does not reach unity in each logarithmic mass bin, the total PBH fraction

$$
f_{\rm PBH,tot} = \int d\log M f_{\rm PBH}(M) \tag{25}
$$

reaches unity with the current parameters. Therefore our model can describe the formation of sufficient PBHs to be a main component of DM. One might think that the PBH mass spectrum can be shifted to the more massive direction and even the neutron star constraints could be avoided for some parameters. However we have checked that the μ -distortion constraints shown in Fig. [1](#page-3-1) as the red line cannot be satisfied in that case.

Before ending this section, let us concentrate on the sharp peaks of the power spectrum around $k \sim 10^6$ Mpc⁻¹ shown in Fig. [1](#page-3-1). This peak comes from the fact that at the beginning of the new inflation the Hubble induced mass $\frac{1}{2}V_{\text{pre}}\varphi^2$ cannot be neglected yet and the inflaton potential is
heing slightly flattened due to its stabilizing effect at first being slightly flattened due to its stabilizing effect at first. For a slightly smaller c (namely a slightly flatter linear potential), this peak can be enlarged and another peak of the fraction for more massive PBHs can be shown. For the following parameters,

$$
v = 10^{-4}
$$
, $\kappa = -0.182$, $c = 5.53 \times 10^{-17}$,
\n $g = 4.26 \times 10^{-3}$, (26)

the resultant power spectrum and PBH fraction are plotted in Figs. [1](#page-3-1) and [2](#page-4-1) as the black dashed lines. Again the total

FIG. 2. The PBH fraction to DM in each logarithmic mass bin with the parameters [\(17\)](#page-3-3) (solid line) and [\(26\)](#page-4-0) (dashed line). Several constraints for PBH abundance are also shown as red regions: from left to right, extragalactic γ rays from evapolation [\[5,11\],](#page-7-24) femtolensing of γ -ray bursts [\[8\]](#page-7-26), existence of white dwarfs in our local galaxy [\[10\],](#page-7-27) Kepler microlensing and millilensing [\[9\],](#page-7-28) EROS and MACHO collaborations [\[6\],](#page-7-29) and accretion effects on CMB [\[7\]](#page-7-30). For both the solid and dashed lines, the total integrated fraction is about unity; therefore these models predicts abundant PBHs as a main component of DM. Moreover in the dashed line case there is another peak at ~30 M_{\odot} , which might cause GW150914 [\[29,30\]](#page-7-31).

 $\sqrt{7}$ Note that the non-Gaussianity (NG) is expected to be small since the second new inflation is driven almost only by a single scalar field around the inflection point. Indeed we have briefly checked that the local nonlinearity parameter f_{NL} is as small as ∼0.1 and for such a small NG it is known that the predicted PBH abundance is hardly affected [43–[45\].](#page-7-32) However the second peak on ∼30 M_{\odot} which we show later might be modified by NG effects since it corresponds with the phase of the beginning of the new inflation. We leave this problem for future works.

PBH fraction is about unity ($f_{\text{PBH,tot}} \approx 1$) for them, but they show another peak at $M_{\text{PBH}} \sim 30 M_{\odot}$. Recently the LIGO/ Virgo collaboration succeeded in the first direct detection of gravitational waves GW150914, which came from an inspiral and merger of a black hole binary [\[25\]](#page-7-7). The masses of these black holes are estimated as 36^{+5}_{-4} and $29^{+4}_{-4}M_{\odot}$.
Taking this the binary formation rate of PRHs whose Taking this, the binary formation rate of PBHs whose masses are around 30 M_{\odot} has been evaluated by several authors [\[27](#page-7-8)–30], and the authors of [\[29\]](#page-7-31) claimed that the binary formation rate of PBHs satisfying current constraints $[f_{PBH}(\sim 30 M_{\odot}) \lesssim 10^{-4}]$ is high enough to be consistent with the black hole merger rate $2-400$ Gpc⁻³ yr⁻¹ inferred from LIGO observations [\[26\]](#page-7-33) (however it was claimed in [\[30\]](#page-7-34) that the binary formation rate might be smaller than that evaluated in [\[29\]](#page-7-31)). Therefore our model might explain both the DM whose main component is as $\sim 10^{24}$ g PBHs and GW150914 from the merger of the ∼30 M_{\odot} PBH binary.⁸

However, the existence of the peak around 30 M_{\odot} in our model should be examined more carefully since the corresponding fluctuation modes reenter the horizon between the preinflation and the new inflation and in such a case effects of the metric perturbations that are not included in the present analysis might be important. So we need to solve full evolutions of fluctuations of scalar fields and metric perturbations, which will be investigated in future work.

IV. CONCLUSIONS

In this paper, we proposed a new inflation model as a second phase of a double inflation consistently constituted in the supergravity framework, where sufficient PBHs can be produced to be a main component of DM. Any specific inflationary model is not required for the preinflation which is responsible for the large scale curvature perturbations, as long as it is consistent with the observations of, e.g., the CMB. The potential of the new inflation in our model consists of the linear, quadratic, and cubic terms and has a flat inflection point where PBHs can be produced. The specific power spectra of the curvature perturbations and the resultant PBH mass spectra are shown in Figs. [1](#page-3-1) and [2](#page-4-1) for two parameter sets [\(17\)](#page-3-3) and [\(26\).](#page-4-0) The inflection point corresponds with $\sim 10^{22}$ g PBHs and they constitute the bulk of DM in our model. In addition, we can make another peak for the PBH mass spectrum on \sim 30 M_{\odot} as indicated by the black dashed line in Fig. [2](#page-4-1). Such a peak corresponds with the beginning of the new inflation and those PBHs might cause the gravitational waves detected by the LIGO/ Virgo collaboration.

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APPENDIX: MULTIPLE HORIZON CROSSING MODES

In this appendix, we describe the treatments for the modes which exit the horizon at the end of the preinflation once, enter the horizon between two inflations, and then reexit the horizon at the beginning of the second new inflation. They correspond with the modes for $k \lesssim 10^6$ Mpc⁻¹ in our parameters. Their dynamics are nontrivial due to their multiple horizon crossing and the amplitudes of them at the second horizon exit which determine the curvature perturbations in the new inflation have to be evaluated carefully. To do so, one must solve equations of motion (EoM) for perturbations continuously over the two inflations and connection phase, including the effects of the metric perturbations. However here let us roughly estimate them in the superand subhorizon limit without metric perturbations.

The linear EoM for perturbations which have a Hubble induced mass $\frac{3}{2}H^2\varphi^2$ is given by

$$
0 = \delta \ddot{\varphi} + 3H \delta \dot{\varphi} + \left(3H^2 + \frac{k^2}{a^2} \right) \delta \varphi
$$

$$
\sim \begin{cases} \delta \ddot{\varphi} + 3H \delta \dot{\varphi} + 3H^2 \delta \varphi, & k \ll aH, \\ \delta \ddot{\varphi} + 3H \delta \dot{\varphi} + \frac{k^2}{a^2} \delta \varphi, & k \gg aH. \end{cases}
$$
(A1)

In the second line, we have used the super- and subhorizon limit. The subhorizon EoM can be always rewritten, with use of the conformal time $a d\eta = d\eta$ and in the subhorizon limit as

$$
\partial_{\eta}^{2}(a\delta\varphi) + \frac{k^{2}}{a^{2}}(a\delta\varphi) \simeq 0, \qquad (A2)
$$

and therefore it only has oscillating solutions whose

amplitudes decrease as a^{-1} . On the other hand, assuming that the background equation of state (EoS) is given by $\omega = p/\rho > -1$ (*a* $\propto t^{\frac{2}{3(1+\omega)}}$), the superhorizon EoM reads

$$
\delta \ddot{\varphi} + \frac{2}{(1+\omega)t} \delta \dot{\varphi} + \frac{4}{3(1+\omega)^2 t^2} \delta \varphi = 0. \quad (A3)
$$

It can be easily solved by assuming the power-law solution t^n and the real part of the power is given by $Re[n] = \frac{-1+3\omega}{2(1+\omega)}$.

⁸ Recently, in Ref. [\[49\]](#page-7-35), it has also been proposed that a 30 M_{\odot}
H could be produced by the gauge field production with the PBH could be produced by the gauge field production with the Chern-Simons coupling $\phi F_{\mu\nu}\tilde{F}^{\mu\nu}$.

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FIG. 3. The schematic image of the relation between the horizon scale aH and the multiple horizon crossing mode k. The time before $a_{\text{pre,f}}$ corresponds with that during the preinflation, while $a_{\text{new},i}$ represents the beginning of the new inflation. Between the two inflations, the horizon scale generally decreases as $aH \propto a^{-\frac{1+3\omega}{2}}$ with $\omega = p/\rho$. Therefore the modes which exit
the horizon near the end of the preinflation can reenter the the horizon near the end of the preinflation can reenter the horizon during the preinflaton oscillation phase, and then reexit the horizon at the beginning of the new inflation. Those modes contribute to the sharp peaks of the power spectra around $k \sim 10^6$ Mpc⁻¹ shown in Fig. [1,](#page-3-1) which can lead the second peak to the PBH fraction on ~30 M_{\odot} . In the super- or subhorizon limits, it can be shown that the amplitude of the perturbations at the second horizon exit a_3 is equal to the standard value $\frac{H_{\text{new}}}{2\pi}$ in spite of their complicated horizon crossing process.

That is, the amplitude of the solutions damps as the Hubble parameter is constant and the two solutions are $\frac{-1+\omega}{2(1+\omega)} \propto a^{-\frac{3(1-\omega)}{4}}$. Also, in the exact de Sitter background, soon found as $\delta\varphi \propto \exp\left(-\frac{3}{2}Ht \pm \frac{\sqrt{3}}{2}iHt\right)$. Namely the perturbations damp as $a^{-3/2}$ [therefore the damping factor $a^{-3(1-\omega)}$ for $\omega > -1$ can be used also for the de Sitter case in which $\omega = -11$ In summary the amplitude of the perturwhich $\omega = -1$. In summary, the amplitude of the perturbations decreases as a^{-1} in the subhorizon limit and as $a^{-\frac{3(1-\omega)}{4}}$ in the superhorizon limit.
Now let us evaluate the con-

Now let us evaluate the concrete amplitude of the multiple horizon crossing modes at the horizon exit during the new inflation. Letting $aH|_{\text{pre},f}$ and $aH|_{\text{new},i}$ denote the horizon scale at the end of the preinflation and the beginning of the new inflation, such modes correspond with $aH|_{\text{new},i} < k < aH|_{\text{pre},f}$. We illustrate a schematic image about the relation between the wavelength k and the horizon scale aH in Fig. [3](#page-6-0) as the solid and dot-dashed lines, respectively. At the first horizon exit during the preinflation, the perturbation amplitude is given by the standard one, $\delta \varphi \sim \frac{H_{\text{pre}}}{2\pi}$. After that, the amplitude decreases until the second horizon exit during the new inflation as

$$
\delta\varphi|_{3} \sim \frac{H_{\text{pre}}}{2\pi} \left(\frac{a_{\text{pre},f}}{a_{1}}\right)^{-3/2} \left(\frac{a_{2}}{a_{\text{pre},f}}\right)^{-\frac{3(1-\omega)}{4}}
$$

$$
\times \left(\frac{a_{\text{new},i}}{a_{2}}\right)^{-1} \left(\frac{a_{3}}{a_{\text{new},i}}\right)^{-1}, \tag{A4}
$$

following the scale factor dependences which we showed previously. Here the subscript 1, 2, and 3 represents each horizon crossing time during the preinflation, between two inflations, and during the new inflation, respectively. Also we have referred to the EoS between two inflations as ω . Noting that the horizon scale *aH* is proportional to $a^{-\frac{1+3\omega}{2}}$, it can be rewritten as can be rewritten as

$$
\delta\varphi|_{3} \sim \frac{H_{\text{pre}}}{2\pi} \left(\frac{aH|_{\text{pre},f}}{k}\right)^{-3/2} \left(\frac{k}{aH|_{\text{pre},f}}\right)^{\frac{3(1-\omega)}{2(1+3\omega)}}
$$

$$
\times \left(\frac{aH|_{\text{new},i}}{k}\right)^{\frac{2}{1+3\omega}} \left(\frac{k}{aH|_{\text{new},i}}\right)^{-1}
$$

$$
= \frac{H_{\text{pre}}}{2\pi} \left(\frac{aH|_{\text{pre},f}}{aH|_{\text{new},i}}\right)^{\frac{3(1+\omega)}{1+3\omega}}.
$$
(A5)

Finally, using $aH \propto a^{-\frac{1+3\omega}{2}} \propto \rho^{5(1+\omega)}$, we can obtain

$$
\delta\varphi|_{3} \sim \frac{H_{\rm pre}}{2\pi} \left(\frac{\rho_{\rm pre}}{\rho_{\rm new}}\right)^{-1/2} \simeq \frac{H_{\rm new}}{2\pi}.\tag{A6}
$$

That is, the resultant amplitude is eventually identical with the standard one even though they experienced a complicated process.

The results obtained in this appendix would be changed by the effects of, e.g., the metric perturbations or the resonance. For example, if one assumes the mass term chaotic inflation as the preinflation, the Hubble induced mass $\frac{1}{2}V_{\text{pre}}\varphi^2 = \frac{1}{4}m^2\chi^2\varphi^2$ where χ represents the inflaton
of the preinflation leads the parametric resonance [50] of the preinflation leads the parametric resonance [\[50\]](#page-7-36). However this problem is solved by introducing a Kähler coupling $K \supset |X|^2 |\phi|^2$ where X is the preinflaton super-
field since this Kähler potential brings $\dot{x}^2 \omega^2$ coupling for field, since this Kähler potential brings $\dot{\chi}^2 \varphi^2$ coupling for example and it cancels and reduces the oscillation of the Hubble induced mass. Also the metric perturbations would also grow density perturbations on subhorizon scales [\[51,52\]](#page-7-37). However the peak of the PBH mass spectrum on ∼30 M_{\odot} is mainly caused by the largest scale mode $k \sim aH|_{\text{new,i}}$ which is hardly affected by the subhorizon effect. Moreover, even if the amplitude of the perturbations is slightly modified, it could be absorbed into the parameter tuning. Anyway, more strict analysis for those modes is postponed to future works.

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