Leptonic g - 2 moments, CP phases, and the Higgs boson mass constraint

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Higgs boson mass measurement at ~125 GeV points to a high scale for supersymmetry (SUSY) specifically the scalar masses. If all the scalars are heavy, the supersymmetric contribution to the leptonic g - 2 moments will be significantly reduced. On the other hand, the Brookhaven experiment indicates a ~3 σ deviation from the standard model prediction. Here we analyze the leptonic g - 2 moments in an extended minimal supersymmetric standard model (MSSM) with inclusion of a vectorlike leptonic generation which brings in new sources of *CP* violation. In this work we consider the contributions to the leptonic g - 2 moments arising from the exchange of charginos and neutralinos, sleptons and mirror sleptons, and from the exchange of *W* and *Z* bosons and of leptons and mirror leptons. We focus specifically on the g - 2 moments for the muon and the electron where sensitive measurements exist. Here it is shown that one can get consistency with the current data on g - 2 under the Higgs boson mass constraint. Dependence of the moments on *CP* phases from the exchanded sector are analyzed and it is shown that they are sensitively dependent on the phases from the new sector. It is shown that the corrections to the leptonic moments arising from the extended MSSM sector will be nonvanishing even if the SUSY

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I. INTRODUCTION

The observation by ATLAS [1] and by CMS [2] of the Higgs boson with a mass of ~125 GeV has put very stringent constraints on low scale supersymmetry. Since the tree level mass of the Higgs boson lies below M_Z , a large loop correction from the supersymmetric sector is needed which in turn implies a high scale for the weak scale supersymmetry and specifically for the scalar masses. A large supersymmetry (SUSY) scale also has direct implications for the $g_{\mu} - 2$ of the muon. Thus the current experimental result gives for the muon q - 2 [3]

$$\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{\rm SM} = (26.2 \pm 8.5) \times 10^{-10}, \qquad (1)$$

which is about a three sigma deviation from the standard model prediction. Similarly for the electron the experimental determination of $g_e - 2$ is very accurate and the uncertainty is rather small, i.e., one has [4]

$$\Delta a_e = a_e^{\exp} - a_e^{\rm SM} = -10.5(8.1) \times 10^{-13}.$$
 (2)

This result relies on a QED calculation up to four loops. Thus along with Eq. (1), Eq. (2) also acts as a constraint on the standard model extensions. Supersymmetric theories with low weak scale mass can make corrections to $g_{\mu} - 2$ which

could be as large as the standard model electroweak corrections and even larger and have strong *CP* phase dependence [5-7] (for early work see [8]). These arise largely from the chargino and sneutrino exchange diagram with the neutralino and smuon exchange diagram making a relatively small contribution. However, if the scalar masses are large, the supersymmetric exchange contributions will be small due to the largeness of the sneutrino and the smuon masses.

In this work we give an analysis of the q - 2 for the muon and for the electron in an extended minimal supersymmetric standard model (MSSM) with a vectorlike leptonic generation. We note that vectorlike multiplets are anomaly free and they appear in a variety of settings which include grand unified models, strings and D brane models [9–13]. Further, it is known that q - 2 has a sharp dependence on CP phases [5–7]. For this reason we investigate also the dependence of the muon and the electron q-2 on the CP phases in the extended MSSM model. Here we are particularly interested in the dependence on the CP phases that arise from the new sector involving vectorlike leptons. We note that the CPphases are constrained in this case by the electric dipole moment of the electron which currently has the value $|d_e| <$ 8.7×10^{-29} ecm [14] while the upper limit on the muon electric dipole moment (EDM) is $|d_u| < 1.9 \times 10^{-19} \text{ ecm}$ [3] and is rather weak. As discussed in several works even with large phases the EDMs can be suppressed either by mass suppression [15,16] or via the cancellation mechanism [17–21]. Several analyses of the vectorlike extensions of MSSM already exist in the literature [22–33].

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The outline of the rest of the paper is as follows: In Sec. II we give an analytical computation for the contribution of the vectorlike lepton generation to g - 2of the muon and of the electron. In Sec. III we give a numerical analysis of the contributions arising from MSSM and from the extended MSSM with a vectorlike leptonic generation. Conclusions are given in Sec. IV. Details of the extended MSSM model with a vectorlike leptonic generation are given in the Appendix. The explanation of the muon anomaly with vectorlike leptons was considered previously in [31] within a nonsupersymmetric framework. Our analysis is within a supersymmetric framework where we carry out a simultaneous fit to both the muon as well as the electron anomaly. Further, we explore the implications of the *CP* phases arising from the new sector.

II. ANALYSIS OF $g_{\mu} - 2$ AND $g_e - 2$ WITH EXCHANGE OF VECTORLIKE LEPTONS

The extended MSSM with a vectorlike leptonic generation is discussed in detail in the Appendix. Using the formalism described there we compute the contribution to the anomalous magnetic moment of a charged lepton ℓ_{α} . We discuss now in detail the various contributions. The contribution arising from the exchange of the charginos, sneutrinos and mirror sneutrinos as shown in the left diagram of Fig. 1 is given by

$$\begin{aligned} a_{\alpha}^{\chi^{+}} &= -\sum_{i=1}^{2} \sum_{j=1}^{10} \frac{m_{\tau_{\alpha}}}{16\pi^{2} m_{\chi_{i}^{-}}} \operatorname{Re}(C_{\alpha i j}^{L} C_{\alpha i j}^{R*}) F_{3}\left(\frac{m_{\tilde{\nu}_{j}}^{2}}{m_{\chi_{i}^{-}}^{2}}\right) \\ &+ \sum_{i=1}^{2} \sum_{j=1}^{10} \frac{m_{\tau_{\alpha}}^{2}}{96\pi^{2} m_{\chi_{i}^{-}}^{2}} [|C_{\alpha i j}^{L}|^{2} + |C_{\alpha i j}^{R}|^{2}] F_{4}\left(\frac{m_{\tilde{\nu}_{j}}^{2}}{m_{\chi_{i}^{-}}^{2}}\right), \end{aligned}$$

$$(3)$$

where $m_{\chi_i^-}$ is the mass of chargino χ_i^- and $m_{\tilde{\nu}_j}$ is the mass of sneutrino $\tilde{\nu}_j$ and where the form factors F_3 and F_4 are given by

$$F_3(x) = \frac{1}{(x-1)^3} [3x^2 - 4x + 1 - 2x^2 \ln x], \qquad (4)$$



FIG. 1. The diagrams that contribute to the leptonic (τ_{α}) magnetic dipole moment via exchange of charginos (χ_i^-) , sneutrinos and mirror sneutrinos $(\tilde{\nu}_j)$ (left diagram) inside the loop and from the exchange of neutralinos (χ_i^0) , sleptons and mirror sleptons $(\tilde{\tau}_i)$ (right diagram) inside the loop.

and

$$F_4(x) = \frac{1}{(x-1)^4} \left[2x^3 + 3x^2 - 6x + 1 - 6x^2 \ln x \right].$$
 (5)

The couplings appearing in Eq. (3) are given by

$$C_{aij}^{L} = g(-\kappa_{\tau}U_{i2}^{*}D_{R1\alpha}^{\tau*}\tilde{D}_{1j}^{\nu} - \kappa_{\mu}U_{i2}^{*}D_{R3\alpha}^{\tau*}\tilde{D}_{5j}^{\nu} - \kappa_{e}U_{i2}^{*}D_{R4\alpha}^{\tau*}\tilde{D}_{7j}^{\nu} - \kappa_{4\ell}U_{i2}^{*}D_{R5\alpha}^{\tau*}\tilde{D}_{9j}^{\nu} + U_{i1}^{*}D_{R2\alpha}^{\tau*}\tilde{D}_{4j}^{\nu} - \kappa_{N}U_{i2}^{*}D_{R2\alpha}^{\tau*}\tilde{D}_{2j}^{\nu}),$$
(6)

$$C_{aij}^{R} = g(-\kappa_{\nu_{\tau}}V_{i2}D_{L1a}^{\tau*}\tilde{D}_{3j}^{\nu} - \kappa_{\nu_{\mu}}V_{i2}D_{L3a}^{\tau*}\tilde{D}_{6j}^{\nu} - \kappa_{\nu_{e}}V_{i2}D_{L4a}^{\tau*}\tilde{D}_{8j}^{\nu} + V_{i1}D_{L1a}^{\tau*}\tilde{D}_{1j}^{\nu} + V_{i1}D_{L3a}^{\tau*}\tilde{D}_{5j}^{\nu} - \kappa_{\nu_{4}}V_{i2}D_{L5a}^{\tau*}\tilde{D}_{10j}^{\nu} + V_{i1}D_{L4a}^{\tau*}\tilde{D}_{7j}^{\nu} - \kappa_{E}V_{i2}D_{L2a}^{\tau*}\tilde{D}_{4j}^{\nu}),$$
(7)

where $D_{L,R}^{\tau}$ and \tilde{D}^{ν} are the charged lepton and sneutrino diagonalizing matrices and are defined by Eqs. (A13) and (A23) and U and V are the matrices that diagonalize the chargino mass matrix M_C so that [34]

$$U^* M_C V^{-1} = \text{diag}(m_{\chi_1^{\pm}} m_{\chi_2^{\pm}}).$$
(8)

Further,

$$(\kappa_N, \kappa_\tau, \kappa_\mu, \kappa_e, \kappa_{4\ell}) = \frac{(m_N, m_\tau, m_\mu, m_e, m_{4\ell})}{\sqrt{2}m_W \cos\beta}, \quad (9)$$

$$(\kappa_E, \kappa_{\nu_{\tau}}, \kappa_{\nu_{\mu}}, \kappa_{\nu_e}, \kappa_{\nu_4}) = \frac{(m_E, m_{\nu_{\tau}}, m_{\nu_{\mu}}, m_{\nu_e}, m_{\nu_4})}{\sqrt{2}m_W \sin\beta}, \quad (10)$$

where m_W is the mass of the W boson and $\tan \beta = \langle H_2^2 \rangle / \langle H_1^1 \rangle$ where H_1 , H_2 are the two Higgs doublets of MSSM.

The contribution arising from the exchange of neutralinos, charged sleptons and charged mirror sleptons as shown in the right diagram of Fig. 1 is given by

$$\begin{aligned} a_{\alpha}^{\chi^{0}} &= \sum_{i=1}^{4} \sum_{j=1}^{10} \frac{m_{\tau_{\alpha}}}{16\pi^{2} m_{\chi_{i}^{0}}} \operatorname{Re}(C_{\alpha i j}^{\prime L} C_{\alpha i j}^{\prime R*}) F_{1}\left(\frac{m_{\tilde{\tau}_{j}}^{2}}{m_{\chi_{i}^{0}}^{2}}\right) \\ &+ \sum_{i=1}^{4} \sum_{j=1}^{10} \frac{m_{\tau_{\alpha}}^{2}}{96\pi^{2} m_{\chi_{i}^{0}}^{2}} [|C_{\alpha i j}^{\prime L}|^{2} + |C_{\alpha i j}^{\prime R}|^{2}] F_{2}\left(\frac{m_{\tilde{\tau}_{j}}^{2}}{m_{\chi_{i}^{0}}^{2}}\right), \end{aligned}$$

$$(11)$$

where the form factors are

$$F_1(x) = \frac{1}{(x-1)^3} [1 - x^2 + 2x \ln x], \qquad (12)$$

and

$$F_2(x) = \frac{1}{(x-1)^4} \left[-x^3 + 6x^2 - 3x - 2 - 6x \ln x \right].$$
(13)

The couplings that enter in Eq. (11) are given by

$$C_{aij}^{\prime L} = \sqrt{2} (\alpha_{\tau i} D_{R1a}^{\tau *} \tilde{D}_{1j}^{\tau} - \delta_{Ei} D_{R2a}^{\tau *} \tilde{D}_{2j}^{\tau} - \gamma_{\tau i} D_{R1a}^{\tau *} \tilde{D}_{3j}^{\tau} + \beta_{Ei} D_{R2a}^{\tau *} \tilde{D}_{4j}^{\tau} + \alpha_{\mu i} D_{R3a}^{\tau *} \tilde{D}_{5j}^{\tau} - \gamma_{\mu i} D_{R3a}^{\tau *} \tilde{D}_{6j}^{\tau} + \alpha_{ei} D_{R4a}^{\tau *} \tilde{D}_{7j}^{\tau} - \gamma_{ei} D_{R4a}^{\tau *} \tilde{D}_{8j}^{\tau} + \alpha_{4\ell i} D_{R5a}^{\tau *} \tilde{D}_{9j}^{\tau} - \gamma_{4\ell i} D_{R5a}^{\tau *} \tilde{D}_{10j}^{\tau}), \qquad (14)$$

$$C_{aij}^{\prime R} = \sqrt{2} (\beta_{\tau i} D_{L1a}^{\tau *} \tilde{D}_{1j}^{\tau} - \gamma_{Ei} D_{L2a}^{\tau *} \tilde{D}_{2j}^{\tau} - \delta_{\tau i} D_{L1a}^{\tau *} \tilde{D}_{3j}^{\tau} + \alpha_{Ei} D_{L2a}^{\tau *} \tilde{D}_{4j}^{\tau} + \beta_{\mu i} D_{L3a}^{\tau *} \tilde{D}_{5j}^{\tau} - \delta_{\mu i} D_{L3a}^{\tau *} \tilde{D}_{6j}^{\tau} + \beta_{ei} D_{L4a}^{\tau *} \tilde{D}_{7j}^{\tau} - \delta_{ei} D_{L4a}^{\tau *} \tilde{D}_{8j}^{\tau} + \beta_{4\ell i} D_{L5a}^{\tau *} \tilde{D}_{9j}^{\tau} - \delta_{4\ell i} D_{L5a}^{\tau *} \tilde{D}_{10j}^{\tau}),$$
(15)

where

$$\alpha_{Ei} = \frac{gm_E X_{4i}^*}{2m_W \sin\beta};$$

$$\beta_{Ei} = eX'_{1i} + \frac{g}{\cos\theta_W} X'_{2i} \left(\frac{1}{2} - \sin^2\theta_W\right) \qquad (16)$$

$$\gamma_{Ei} = eX_{1i}^{\prime*} - \frac{g \sin^2 \theta_W}{\cos \theta_W} X_{2i}^{\prime*}; \qquad \delta_{Ei} = -\frac{g m_E X_{4i}}{2m_W \sin \beta}, \quad (17)$$

and

$$\alpha_{\tau i} = \frac{gm_{\tau}X_{3i}}{2m_{W}\cos\beta}; \qquad \alpha_{\mu i} = \frac{gm_{\mu}X_{3i}}{2m_{W}\cos\beta};$$

$$\alpha_{ei} = \frac{gm_{e}X_{3i}}{2m_{W}\cos\beta}; \qquad \alpha_{4\ell i} = \frac{gm_{4\ell}X_{3i}}{2m_{W}\cos\beta}$$
(18)

$$\delta_{\tau i} = -\frac{gm_{\tau}X_{3i}^{*}}{2m_{W}\cos\beta}; \qquad \delta_{\mu i} = -\frac{gm_{\mu}X_{3i}^{*}}{2m_{W}\cos\beta}; \\ \delta_{ei} = -\frac{gm_{e}X_{3i}^{*}}{2m_{W}\cos\beta}; \qquad \delta_{4\ell i} = -\frac{gm_{4\ell}X_{3i}^{*}}{2m_{W}\cos\beta}, \tag{19}$$

and where

$$\beta_{\tau i} = \beta_{\mu i} = \beta_{ei} = \beta_{4\ell i} = -eX_{1i}^{\prime *} + \frac{g}{\cos \theta_W} X_{2i}^{\prime *} \left(-\frac{1}{2} + \sin^2 \theta_W \right), \quad (20)$$

$$\gamma_{\tau i} = \gamma_{\mu i} = \gamma_{ei} = \gamma_{4\ell i} = -eX'_{1i} + \frac{g \sin^2 \theta_W}{\cos \theta_W} X'_{2i}.$$
 (21)

Here X' are defined by

$$X'_{1i} = X_{1i}\cos\theta_W + X_{2i}\sin\theta_W, \qquad (22)$$



FIG. 2. The W loop (the left diagram) involving the exchange of sequential and vectorlike neutrinos ψ_i and the Z loop (the right diagram) involving the exchange of sequential and vectorlike charged leptons τ_{β} that contribute to the magnetic dipole moment of the charged lepton τ_{α} .

$$X'_{2i} = -X_{1i}\sin\theta_W + X_{2i}\cos\theta_W, \qquad (23)$$

where X diagonalizes the neutralino mass matrix, i.e.,

$$X^{T}M_{\chi^{0}}X = \operatorname{diag}(m_{\chi^{0}_{1}}, m_{\chi^{0}_{2}}, m_{\chi^{0}_{3}}, m_{\chi^{0}_{4}}).$$
(24)

Further, \tilde{D}^{τ} that enter in Eqs. (14) and (15) is a matrix which diagonalizes the charged slepton mass squared matrix and is defined in Eq. (A19).

Next we compute the contribution from the exchange of the W and Z bosons. Thus the exchange of the W and the exchange of neutrinos and mirror neutrinos as shown in the left diagram of Fig. 2 gives

$$a_{\tau_{\alpha}}^{W} = \frac{m_{\tau_{\alpha}}^{2}}{16\pi^{2}m_{W}^{2}} \sum_{i=1}^{5} [|C_{Li\alpha}^{W}|^{2} + |C_{Ri\alpha}^{W}|^{2}] F_{W}\left(\frac{m_{\psi_{i}}^{2}}{m_{W}^{2}}\right) + \frac{m_{\psi_{i}}}{m_{\tau_{\alpha}}} \operatorname{Re}(C_{Li\alpha}^{W}C_{Ri\alpha}^{W*}) G_{W}\left(\frac{m_{\psi_{i}}^{2}}{m_{W}^{2}}\right),$$
(25)

where the form factors are given by

$$F_W(x) = \frac{1}{6(x-1)^4} [4x^4 - 49x^3 + 18x^3 \ln x + 78x^2 - 43x + 10],$$
(26)

and

$$G_W(x) = \frac{1}{(x-1)^3} [4 - 15x + 12x^2 - x^3 - 6x^2 \ln x].$$
(27)

The couplings that enter in Eq. (25) are given by

$$C_{L_{i\alpha}}^{W} = \frac{g}{\sqrt{2}} \left[D_{L1i}^{\nu*} D_{L1\alpha}^{\tau} + D_{L3i}^{\nu*} D_{L3\alpha}^{\tau} + D_{L4i}^{\nu*} D_{L4\alpha}^{\tau} + D_{L5i}^{\nu*} D_{L5\alpha}^{\tau} \right],$$
(28)

$$C_{R_{i\alpha}}^{W} = \frac{g}{\sqrt{2}} [D_{R2i}^{\nu*} D_{R2\alpha}^{\tau}].$$
(29)

Here $D_{L,R}^{\nu}$ are matrices of a biunitary transformation that diagonalizes the neutrino mass matrix and are defined in Eq. (A9).

Finally the exchange of the Z and the exchange of leptons and mirror leptons as shown in the right diagram of Fig. 2 gives

$$a_{\tau_{\alpha}}^{Z} = \frac{m_{\tau_{\alpha}}^{2}}{32\pi^{2}m_{Z}^{2}} \sum_{\beta=1}^{5} [|C_{L\beta\alpha}^{Z}|^{2} + |C_{R\beta\alpha}^{Z}|^{2}]F_{Z}\left(\frac{m_{\tau_{\beta}}^{2}}{m_{Z}^{2}}\right) + \frac{m_{\tau_{\beta}}}{m_{\tau_{\alpha}}} \operatorname{Re}(C_{L\beta\alpha}^{Z}C_{R\beta\alpha}^{Z*})G_{Z}\left(\frac{m_{\tau_{\beta}}^{2}}{m_{Z}^{2}}\right),$$
(30)

where

$$F_Z(x) = \frac{1}{3(x-1)^4} [-5x^4 + 14x^3 - 39x^2 + 18x^2 \ln x + 38x - 8],$$
(31)

and

$$G_Z(x) = \frac{2}{(x-1)^3} [x^3 + 3x - 6x \ln x - 4], \quad (32)$$

and m_Z is the Z boson mass. The couplings that enter in Eq. (30) are given by

$$C_{L_{\alpha\beta}}^{Z} = \frac{g}{\cos\theta_{W}} [x(D_{L\alpha1}^{\tau\dagger}D_{L1\beta}^{\tau} + D_{L\alpha2}^{\tau\dagger}D_{L2\beta}^{\tau} + D_{L\alpha3}^{\tau\dagger}D_{L3\beta}^{\tau} + D_{L\alpha4}^{\tau\dagger}D_{L4\beta}^{\tau} + D_{L\alpha5}^{\tau\dagger}D_{L5\beta}^{\tau}) - \frac{1}{2}(D_{L\alpha1}^{\tau\dagger}D_{L1\beta}^{\tau} + D_{L\alpha3}^{\tau\dagger}D_{L3\beta}^{\tau} + D_{L\alpha4}^{\tau\dagger}D_{L4\beta}^{\tau} + D_{L\alpha5}^{\tau\dagger}D_{L5\beta}^{\tau})], \quad (33)$$

and

$$C_{R_{\alpha\beta}}^{Z} = \frac{g}{\cos\theta_{W}} [x(D_{R\alpha1}^{\tau\dagger}D_{R1\beta}^{\tau} + D_{R\alpha2}^{\tau\dagger}D_{R2\beta}^{\tau} + D_{R\alpha3}^{\tau\dagger}D_{R3\beta}^{\tau} + D_{R\alpha4}^{\tau\dagger}D_{R4\beta}^{\tau} + D_{R\alpha5}^{\tau\dagger}D_{R5\beta}^{\tau}) - \frac{1}{2}(D_{R\alpha2}^{\tau\dagger}D_{R2\beta}^{\tau})]. \quad (34)$$

III. ESTIMATES OF Δa_{μ} AND Δa_{e}

We begin by discussing the prediction for Δa_{μ} and Δa_{e} for MSSM when the scalar masses are large lying in the several TeV region. In Tables I and II we exhibit the results for two benchmark points where we assume universality

TABLE I. The contribution of the vectorlike multiplet vs the contribution from the MSSM sector to the anomalous magnetic moments of the muon for two illustrative benchmark points (a) and (b). They are: (a) $m_N = 5$, $m_{4\ell} = 450$, $|f'_3| = 0.62$, $|f''_3| = 6.62 \times 10^{-3}$, $|f'_4| = 20$, $|h_6| = 230$, $|h_8| = 730$ and (b) $m_N = 200$, $m_{4\ell} = 250$, $|f'_3| = 0.73$, $|f''_3| = 5.23 \times 10^{-3}$, $|f'_4| = 30$, $|h_6| = 66$, $|h_8| = 180$. Other parameters have the values $\tan \beta = 15$, $m_0 = m_0^{\tilde{\nu}} = 5000$, $|A_0^{\tilde{\nu}}| = |A_0| = 6000$, $|m_1| = 224$, $|m_2| = 407$, $|\mu| = 2124$, $m_E = 320$, $m_{\nu 4} = 350$, $m_{h^0} = 124.66$, $|f_3| = 1 \times 10^{-4}$, $|f_4| = 1 \times 10^{-5}$, $|f''_4| = 38$, $|f_5| = 1 \times 10^{-4}$, $|f'_5| = 5.0 \times 10^{-4}$, $|f''_5| = 3.0 \times 10^{-3}$, $|h_7| = 34$, $\alpha_{A_0} = \pi$, $\alpha_{A_0^{\tilde{\nu}}} = \pi$, $\xi_1 = \xi_2 = \theta_{\mu} = \chi_3 = \chi'_3 = \chi''_3 = \chi_4 = \chi'_4 = \chi''_4 = \chi'_5 = \chi'_5 = \chi''_5 = \chi_6 = \chi_7 = \chi_8 = 0$. All masses are in GeV and phases in rad.

		(a)		(b)	
Contribution		MSSM	Vectorlike	MSSM	Vectorlike
Chargino	$a_{\mu}^{\chi^{\pm}}$	$+1.68 \times 10^{-11}$	$+1.07 \times 10^{-11}$	$+1.68 \times 10^{-11}$	-8.54×10^{-11}
Neutralino	$a_{\mu}^{\chi^0}$	-3.09×10^{-13}	-1.50×10^{-12}	-3.09×10^{-13}	-6.58×10^{-13}
W boson	a^{μ}_{μ}	0	$+1.53 \times 10^{-9}$	0	$+2.56 \times 10^{-9}$
Z boson	a_{μ}^{Z}	0	$+5.12 \times 10^{-10}$	0	$+8.76 \times 10^{-10}$
Total	Δa_{μ}	$+1.65 \times 10^{-11}$	$+2.05 \times 10^{-9}$	$+1.65 \times 10^{-11}$	$+3.35 \times 10^{-9}$

TABLE II. The contribution of the vectorlike multiplet vs the contribution from the MSSM sector to the anomalous magnetic moments of the electron for two illustrative benchmark points (a) and (b) as given in Table I.

		(a)		(b)	
Contribution		MSSM	Vectorlike	MSSM	Vectorlike
Chargino	$a_e^{\chi^{\pm}}$	$+3.92 \times 10^{-16}$	-2.88×10^{-16}	$+3.92 \times 10^{-16}$	-6.31×10^{-15}
Neutralino	$a_e^{\chi^0}$	-7.25×10^{-18}	-1.69×10^{-16}	-7.25×10^{-18}	-3.12×10^{-17}
W boson	a_e^W	0	$+1.99 \times 10^{-13}$	0	$+1.71 \times 10^{-13}$
Z boson	a_e^Z	0	$+5.89 \times 10^{-14}$	0	$+5.11 \times 10^{-14}$
Total	Δa_e	$+3.85 \times 10^{-16}$	$+2.58 \times 10^{-13}$	$+3.85 \times 10^{-16}$	$+2.16 \times 10^{-13}$

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and take the scalar masses and the trilinear couplings to be all equal. Table I exhibits the result of the computation for Δa_{μ} where individual contributions arising from the chargino exchange, neutralino exchange, W exchange and Z exchange are listed. The entries exhibit the contributions over and above what one expects from the standard model and so the entries for the W and Z exchanges show a null value. Thus the entire contribution in this case arises from the chargino and the neutralino exchange and their sum gives a value $\mathcal{O}(10^{-11})$ which is 2 orders of magnitude smaller than the experimental result of Eq. (1). A very similar analysis is given in Table II for Δa_e where again the contribution to Δa_e arises from the exchange of charginos and neutralinos and their sum is $\mathcal{O}(10^{-16})$ which is 3 orders of magnitude smaller than the result of Eq. (2). Thus with a high scale of the scalar masses one cannot explain the results of Eqs. (1) and (2).

We turn now to the analysis within the extended MSSM with a vectorlike leptonic generation. As in the analysis within MSSM here also we assume the universality of the soft parameters so that we set $m_0^2 = \tilde{M}_{\tau L}^2 = \tilde{M}_{\tau}^2 = \tilde{M}_{\tau}^2$ $\tilde{M}_{\chi}^2 = \tilde{M}_{\mu L}^2 = \tilde{M}_{\mu}^2 = \tilde{M}_{eL}^2 = \tilde{M}_e^2 = \tilde{M}_{4L}^2 = \tilde{M}_4^2$ and $A_0 =$ $A_{\tau} = A_E = A_{\mu} = A_e = A_{4\ell}$ in the computation of the charged slepton mass squared matrix. Similarly we assume $m_0^{\tilde{\nu}^2} = \tilde{M}_N^2 = \tilde{M}_{\nu_{\tau}}^2 = \tilde{M}_{\nu_{\mu}}^2 = \tilde{M}_{\nu_e}^2 = \tilde{M}_{4L}^2 = \tilde{M}_{\nu 4}^2$ and $A_{\nu_{\tau}} =$ $A_{\nu_{\mu}} = A_{\nu_{\mu}} = A_N = A_{4\nu} = A_0^{\tilde{\nu}}$ for the computation of the sneutrino mass squared matrix (see the Appendix). The contributions from the chargino exchange, the neutralino exchange, and the W and Z exchange are listed in Tables I and II for two benchmark points. In this case the Wboson and the Z boson exchange contributions are nonvanishing and the contributions listed are those over and above what one expects in the standard model. As in the MSSM case here also one finds that the contributions from the chargino exchange and from the neutralino exchange fall significantly below the experimental results of Eqs. (1) and (2). However, in this case including the contributions from the W exchange and from the Z boson exchange one finds that consistency with Eqs. (1) and (2) is achieved. At the same time one has the Higgs boson mass in the model for both benchmarks (a) and (b) at ~125 GeV consistent with the experimental measurements by ATLAS [1] and by CMS [2]. Here the loop correction that gives mass to the Higgs boson comes from the MSSM sector while the extra vectorlike leptonic generation makes a negligible contribution.

In the analysis of Δa_{μ} and Δa_{e} the exchange of both the sequential leptons and the mirrors play a role with the mirror exchange being the more dominant. The analysis requires diagonalization of a 5 × 5 mass matrix in the charged lepton-charged mirror lepton sector and diagonalization of a 5 × 5 mass matrix in the neutrino-mirror neutrino sector. Parameter choices are made to ensure that the eigenvalues in the charged lepton sector give the desired

TABLE III. The mass of the heavy particles obtained after diagonalizing the lepton and neutrino mass matrices for benchmark points (a) and (b) of Table I.

	Mass spectrum (GeV)		
Particles	(a)	(b)	
Mirror neutrino	208	207	
Fourth sequential neutrino	816	395	
Mirror lepton	253	349	
Fourth sequential lepton	545	226	

experimental values for e, μ and τ along with two additional masses, one for the sequential fourth generation lepton and the other for the mirror charged lepton. Their values are listed in Table III for the case of two benchmark points (a) and (b). A similar analysis holds for the neutrino-mirror neutrino sector where we get two additional eigenvalues, one for the fourth generation neutrino and the other for the mirror neutrino. Their values are also listed in Table III for two benchmark points. The analysis also requires diagonalization of a 10×10 matrix in the charged slepton and charged mirror slepton sector, as well as diagonalization of a 10×10 matrix in the sneutrino and the mirror sneutrino sector.

We discuss now some further features of the analysis which includes the vectorlike leptonic generation. In Fig. 3 we show the variation of Δa_{μ} as a function of m_E the mass of the mirror lepton as given by Eq. (A11), for four tan β values. A remarkable feature of this graph is the dependence on tan β it exhibits. Notice that for a fixed m_E , Δa_{μ} decreases



FIG. 3. Δa_{μ} as a function of m_E when $\tan \beta = 20, 25, 30, 35$. Other parameters are $m_0 = m_0^{\tilde{\nu}} = 5000$, $|A_0^{\tilde{\nu}}| = |A_0| = 6000$, $|m_1| = 224$, $|m_2| = 407$, $|\mu| = 2124$, $m_{4\ell} = 250$, $m_N = 300$, $m_{\nu 4} = 350$, $m_{h^0} = 124.66$, $|f_3| = 1 \times 10^{-5}$, $|f'_3| = 8.18$, $|f''_3| = 4.32 \times 10^{-2}$, $|f_4| = 1 \times 10^{-3}$, $|f'_4| = 3.61$, $|f''_4| = 3.85$, $|f_5| = 1 \times 10^{-4}$, $|f'_5| = 5.0 \times 10^{-4}$, $|f''_5| = 3.0 \times 10^{-6}$, $|h_6| = 10$, $|h_7| = 19$, $|h_8| = 10$, $\alpha_{A_0} = \pi$, $\alpha_{A_0^{\tilde{\nu}}} = \pi$, $\xi_1 = \xi_2 = \theta_{\mu} = \chi_3 = \chi'_3 = \chi'_3 = \chi'_4 = \chi'_4 = \chi'_4 = \chi'_4 = \chi'_5 = \chi'_5 = \chi'_5 = \chi'_5 = \chi_7 = \chi_8 = 0$. All masses are in GeV and phases in rad.



FIG. 4. Δa_{μ} (left panel) and Δa_{e} (right panel) as a function of χ'_{3} in the range $[-\pi, +\pi]$ when $\chi'_{4} = -3.14, -2.14, +0.36, +2.26$. Other parameters are $\tan \beta = 15$, $m_{0} = m_{0}^{\tilde{\nu}} = 5000$, $|A_{0}^{\tilde{\nu}}| = |A_{0}| = 6000$, $|m_{1}| = 224$, $|m_{2}| = 407$, $|\mu| = 2124$, $m_{N} = 5$, $m_{\nu 4} = 350$, $m_{E} = 320$, $m_{4\ell'} = 450$, $m_{h^{0}} = 124.66$, $|f_{3}| = 1 \times 10^{-4}$, $|f'_{3}| = 0.62$, $|f''_{3}| = 6.62 \times 10^{-3}$, $|f_{4}| = 1 \times 10^{-5}$, $|f'_{4}| = 20$, $|f''_{4}| = 38$, $|f_{5}| = 1 \times 10^{-4}$, $|f'_{5}| = 5.0 \times 10^{-4}$, $|f''_{5}| = 3.0 \times 10^{-6}$, $|h_{6}| = 230$, $|h_{7}| = 34$, $|h_{8}| = 730$, $\alpha_{A_{0}} = \pi$, $\alpha_{A_{0}^{\tilde{\nu}}} = \pi$, $\xi_{1} = \xi_{2} = \theta_{\mu} = \chi_{3} = \chi''_{3} = \chi_{4} = \chi''_{4} = \chi_{5} = \chi'_{5} = \chi''_{5} = \chi_{6} = \chi_{7} = \chi_{8} = 0$. All masses are in GeV and phases in rad.

for increasing values of $\tan \beta$ as $\tan \beta$ varies from 20 to 35. Now we recall that the Yukawa coupling of a charged lepton has a $1/\cos\beta$ dependence and as a consequence the contribution of the charged lepton to Δa_{μ} becomes larger for larger $\tan\beta$ which is a well-known result. However, the Yukawa coupling of the mirror lepton goes like $1/\sin\beta$ [9] and so Δa_{μ} decreases for larger values of $\tan\beta$. This feature explains the $\tan\beta$ dependence in Fig. 3. It also shows that the W and Z exchange contributions in this case are being controlled by exchange of the mirror particles. A very similar dependence on $\tan\beta$ is exhibited by Δa_e .

The anomalous magnetic moments are quite sensitive to *CP* phases as first demonstrated in the analysis of [5–7] for the case of *CP* phases that arise in N = 1 supergravity [5,7] and more generally for the case of MSSM [6]. In those

analyses it was also found that large *CP* phases could be made consistent with the experimental constraints on the EDMs by the cancellation mechanism [17–21]. In the present analysis the contribution from the MSSM sector is suppressed and the dominant contribution arises from the *W* and *Z* exchanges. For the case of three generations this sector does not have any *CP* phases in the leptonic sector. However, the extended MSSM with a vectorlike leptonic multiplet allows for *CP* phases which cannot be removed by field redefinitions. It is of interest then to discuss the dependence of Δa_{μ} and Δa_{e} on the *CP* phases that arise in the extended MSSM. We discuss now the dependence of Δa_{μ} and Δa_{e} on such phases. In Fig. 4 we exhibit the dependence of Δa_{μ} and Δa_{e} on χ'_{3} , which is the phase of f'_{3} (see the Appendix). A sharp dependence on χ_{3}' is seen for



FIG. 5. Δa_{μ} (left panel) and Δa_{e} (right panel) as a function of χ_{6} in the range $[-\pi, +\pi]$ when $|f'_{4}|=20, 25, 30, 35$. Other parameters are $\tan \beta = 15$, $m_{0} = m_{0}^{\tilde{\nu}} = 5000$, $|A_{0}^{\tilde{\nu}}| = |A_{0}| = 6000$, $|m_{1}|=224$, $|m_{2}|=407$, $|\mu|=2124$, $m_{N}=5$, $m_{\nu4}=350$, $m_{E}=320$, $m_{4\ell}=450$, $m_{h^{0}}=124.66$, $|f_{3}|=1\times10^{-4}$, $|f'_{3}|=0.627$, $|f''_{3}|=6.605\times10^{-3}$, $|f_{4}|=1\times10^{-3}$, $|f''_{4}|=38$, $|f_{5}|=1\times10^{-4}$, $|f'_{5}|=5.0\times10^{-4}$, $|f''_{5}|=3.0\times10^{-6}$, $|h_{6}|=230$, $|h_{7}|=34$, $|h_{8}|=730$, $\alpha_{A_{0}}=\pi$, $\alpha_{A_{0}^{\tilde{\nu}}}=\pi$, $\xi_{1}=\xi_{2}=\theta_{\mu}=\chi_{3}=\chi_{4}=\chi_{5}=\chi'_{5}=\chi''_{5}=0$, $\chi'_{3}=2.96$, $\chi''_{3}=-1.54$, $\chi'_{4}=2.86$, $\chi''_{4}=1.46$, $\chi_{7}=-2.94$, $\chi_{8}=0.6$. All masses are in GeV and phases in rad.



FIG. 6. Δa_{μ} (left panel) and Δa_{e} (right panel) as a function of $|h_{6}|$ when $m_{N} = 100, 150, 200, 250$. Other parameters are $\tan \beta = 15$, $m_{0} = m_{0}^{\tilde{\nu}} = 5000, |A_{0}^{\tilde{\nu}}| = |A_{0}| = 6000, |m_{1}| = 224, |m_{2}| = 407, |\mu| = 2124, m_{\nu 4} = 350, m_{E} = 320, m_{4\ell} = 250, m_{h^{0}} = 124.66, |f_{3}| = 1 \times 10^{-5}, |f_{3}'| = 0.73, |f_{3}''| = 5.23 \times 10^{-3}, |f_{4}| = 1 \times 10^{-3}, |f_{4}'| = 20, |f_{4}''| = 38, |f_{5}| = 1 \times 10^{-4}, |f_{5}'| = 5.0 \times 10^{-4}, |f_{5}''| = 3.0 \times 10^{-6}, |h_{7}| = 34, |h_{8}| = 180, \alpha_{A_{0}} = \pi, \alpha_{A_{0}^{\tilde{\nu}}} = \pi, \xi_{1} = \xi_{2} = \theta_{\mu} = \chi_{3} = \chi_{4} = \chi_{5} = \chi_{5}' = \chi_{5}'' = 0, \chi_{3}' = 2.96, \chi_{3}'' = -1.54, \chi_{4}' = 2.86, \chi_{4}'' = 1.46, \chi_{6} = 3.06, \chi_{7} = -2.94, \chi_{8} = 0.6$. All masses are in GeV and phases in rad.



FIG. 7. Left panel: Variation of Δa_e as a function of $|f_3''|$ for four values of $|h_7|$ when $|h_7| = 50, 100, 200, 300$. Other parameters are tan $\beta = 15$, $m_0 = m_0^{\tilde{\nu}} = 5000$, $|A_0^{\tilde{\nu}}| = |A_0| = 6000$, $|m_1| = 224$, $|m_2| = 407$, $|\mu| = 2124$, $m_N = 200$, $m_{\nu 4} = 350$, $m_E = 320$, $m_{4\ell} = 250$, $m_{h^0} = 124.66$, $|f_3| = 1 \times 10^{-5}$, $|f_3'| = 0.73$, $|f_4| = 1 \times 10^{-3}$, $|f_4'| = 20$, $|f_4''| = 38$, $|f_5| = 1 \times 10^{-4}$, $|f_5'| = 5.0 \times 10^{-4}$, $|f_5''| = 3.0 \times 10^{-6}$, $|h_6| = 66$, $|h_8| = 180$, $\alpha_{A_0} = \pi$, $\alpha_{A_0^{\tilde{\nu}}} = \pi$, $\xi_1 = \xi_2 = \theta_\mu = \chi_3 = \chi_4 = \chi_5 = \chi_5' = \chi_5'' = 0$, $\chi_3' = 2.96$, $\chi_3'' = -1.54$, $\chi_4' = 2.86$, $\chi_4'' = 1.46$, $\chi_6 = 3.06$, $\chi_7 = -2.94$, $\chi_8 = 0.6$. All masses are in GeV and phases in rad. Right panel: A plot of Δa_μ as a function of the common scalar mass m_0 exhibiting a residual correction Δa_μ even when m_0 lies in the PeV region. The parameters used in the plot are for benchmark (a) in Table I.

both Δa_{μ} and for Δa_e . A very similar sensitivity to the *CP* phase χ_6 which is the phase of h_6 (see the Appendix) is exhibited in Fig. 5. To explore further the sensitivity of Δa_{μ} and of Δa_e to parameters in the vectorlike sector we exhibit in Fig. 6 the dependence of Δa_{μ} and Δa_e on h_6 which is the coefficient of the term $\epsilon_{ij} \hat{\chi}^{ci} \hat{\psi}_{4L}^{j}$ in the superpotential [see Eq. (A3)]. One can see in Fig. 6 the strong dependence of Δa_{μ} and Δa_e on h_6 . In the analyses given so far both Δa_{μ} and Δa_e have very significant dependence on the parameters arising from inclusion of the vectorlike sector. However, there are parameters which affect Δa_e and Δa_{μ} differently. This is the case for $|f_3''|$. Here as seen in the left panel of Fig. 7, Δa_e is a sensitive function of $|f_3''|$

but not so for the case for Δa_{μ} (not exhibited) because of its much larger size. Finally we note that even if the SUSY scale lies in the PeV region, the contributions from the *W* and *Z* exchange arising from Fig. 2 survive while the diagrams of Fig. 1 give a vanishingly small contribution. This is illustrated in the right panel of Fig. 7.

IV. CONCLUSION

The Higgs boson mass measurement at 126 GeV indicates a high SUSY scale, and specifically a high scale for the scalar masses. If the scalar masses are all heavy, the contribution to the leptonic moments and specifically to $\Delta a_{\ell} = a_{\ell}^{\text{exp}} - a_{\ell}^{\text{SM}}$ becomes negligible in this case. In this work we have investigated leptonic g-2 moments within an extended MSSM model with an extra vectorlike generation and *CP* phase dependent couplings. It is found that one can achieve consistency with the experimental measurements of Δa_{μ} and Δa_{e} under the constraint of the Higgs boson mass. The dependence of the moments on *CP* phases from the new sector are also investigated and shown to have a very sensitive dependence. Further, it is shown that Δa_{μ} and Δa_{e} will be nonvanishing even when the SUSY scale lies in the PeV region. The model presented here can be made UV complete by including a full generation of vectorlike matter including both quarks and leptons. Finally we note that the work presented here has some overlap with [35] which appeared after this work was finished. For other recent work on this topic see [36].

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APPENDIX: APPENDIX ON THE EXTENDED MSSM WITH A VECTORLIKE LEPTONIC GENERATION

In this Appendix we define the notation for the vector generation and their properties under $SU(3)_C \times SU(2)_L \times U(1)_Y$. For the four sequential families we use the notation

$$\psi_{iL} \equiv \begin{pmatrix} \nu_{iL} \\ \ell_{iL} \end{pmatrix} \sim \left(1, 2, -\frac{1}{2}\right),$$

$$\ell_{iL}^c \sim (1, 1, 1), \qquad \nu_{iL}^c \sim (1, 1, 0), \qquad (A1)$$

where the last entry on the right-hand side of each ~ is the value of the hypercharge Y defined so that $Q = T_3 + Y$ and we have included in our analysis the singlet field ν_i^c , where *i* runs from 1–4. For the mirrors we use the notation

$$\chi^{c} \equiv \begin{pmatrix} E_{\mu L}^{c} \\ N_{L}^{c} \end{pmatrix} \sim \left(1, 2, \frac{1}{2}\right),$$
$$E_{\mu L} \sim (1, 1, -1), \qquad N_{L} \sim (1, 1, 0).$$
(A2)

The main difference between the leptons and the mirrors is that while the leptons have V - A type interactions with $SU(2)_L \times U(1)_V$ gauge bosons the mirrors have V + Atype interactions. In the analysis we assume R parity conservation. All of the neutral scalar fields in the new sector carry odd R parity and giving them a vacuum expectation value (VEV) will violate R parity conservation. For that reason only the Higgs fields are given VEVs. Further, in MSSM one can make field redefinitions to make the VEVs of both of the neutral Higgs fields to be real. One of these can become complex at the loop level leading to mixing of CP even-CP odd neutral Higgs. The induced phases are, however, small. An analysis including the CP even-*CP* odd Higgs mixing requires a separate treatment (see, e.g., [33]). We do not include loop induced CP phases in our analysis. Their effects of the analysis would in any case be negligible.

We assume that the mirrors of the vectorlike generation escape acquiring mass at the grand unified theory scale and remain light down to the electroweak scale where the superpotential of the model for the lepton part may be written in the form

$$W = -\mu\epsilon_{ij}\hat{H}_{1}^{i}\hat{H}_{2}^{j} + \epsilon_{ij}[f_{1}\hat{H}_{1}^{i}\hat{\psi}_{L}^{j}\hat{\tau}_{L}^{c} + f_{1}'\hat{H}_{2}^{j}\hat{\psi}_{L}^{i}\hat{\nu}_{\tau L}^{c} + f_{2}\hat{H}_{1}^{i}\hat{\chi}^{cj}\hat{N}_{L} + f_{2}'\hat{H}_{2}^{j}\hat{\chi}^{ci}\hat{E}_{L} + h_{1}\hat{H}_{1}^{i}\hat{\psi}_{\mu L}^{j}\hat{\mu}_{L}^{c} + h_{1}'\hat{H}_{2}^{j}\hat{\psi}_{\mu L}^{i}\hat{\nu}_{\mu L}^{c} + h_{2}\hat{H}_{1}^{i}\hat{\psi}_{\mu L}^{j}\hat{e}_{L}^{c}\hat{e}_{L} + f_{2}\hat{H}_{1}^{j}\hat{\psi}_{\mu L}^{i}\hat{\mu}_{L}^{c}\hat{\mu}_{L}^{c} + h_{2}\hat{H}_{1}^{i}\hat{\psi}_{\mu L}^{j}\hat{e}_{L}^{c}\hat{e}_{L}^{c} + h_{2}\hat{H}_{1}^{j}\hat{\psi}_{\mu L}^{i}\hat{\nu}_{\tau L}^{c} + f_{2}\hat{H}_{1}^{j}\hat{\psi}_{\mu L}^{i}\hat{\nu}_{L}^{c}\hat{\mu}_{L}^{c}$$

where $\hat{}$ implies superfields, $\hat{\psi}_L$ stands for $\hat{\psi}_{3L}$, $\hat{\psi}_{\mu L}$ stands for $\hat{\psi}_{2L}$ and $\hat{\psi}_{eL}$ stands for $\hat{\psi}_{1L}$.

The mass terms for the neutrinos, mirror neutrinos, leptons and mirror leptons arise from the term

$$\mathcal{L} = -\frac{1}{2} \frac{\partial^2 W}{\partial A_i \partial A_j} \psi_i \psi_j + \text{H.c.}, \tag{A4}$$

where ψ and A stand for generic two-component fermion and scalar fields. After spontaneous breaking of the electroweak symmetry, $(\langle H_1^1 \rangle = v_1/\sqrt{2} \text{ and } \langle H_2^2 \rangle = v_2/\sqrt{2})$, we have the following set of mass terms written in the 4-component spinor notation so that

$$-\mathcal{L}_m = \bar{\xi}_R^T(M_f)\xi_L + \bar{\eta}_R^T(M_\ell)\eta_L + \text{H.c.}, \tag{A5}$$

where the basis vectors in which the mass matrix is written is given by

$$\bar{\xi}_{R}^{T} = (\bar{\nu}_{\tau R} \bar{N}_{R} \bar{\nu}_{\mu R} \bar{\nu}_{eR} \bar{\nu}_{4R}), \\ \xi_{L}^{T} = (\nu_{\tau L} N_{L} \nu_{\mu L} \nu_{eL} \nu_{4L}), \\ \bar{\eta}_{R}^{T} = (\bar{\tau}_{R} \bar{E}_{R} \bar{\mu}_{R} \bar{e}_{R} \bar{\ell}_{4R}), \\ \eta_{L}^{T} = (\tau_{L} E_{L} \mu_{L} e_{L} \ell_{4L}),$$
(A6)

and the mass matrix M_f of neutrinos is given by

LEPTONIC g - 2 MOMENTS, CP PHASES, AND THE ...

$$M_{f} = \begin{pmatrix} f_{1}'v_{2}/\sqrt{2} & f_{5} & 0 & 0 & 0\\ -f_{3} & f_{2}v_{1}/\sqrt{2} & -f_{3}' & -f_{3}'' & -h_{6} \\ 0 & f_{5}' & h_{1}'v_{2}/\sqrt{2} & 0 & 0\\ 0 & f_{5}'' & 0 & h_{2}'v_{2}/\sqrt{2} & 0\\ 0 & h_{8} & 0 & 0 & y_{5}'v_{2}/\sqrt{2} \end{pmatrix}.$$
 (A7)

We define the matrix element (22) of the mass matrix as m_N so that

$$m_N = f_2 v_1 / \sqrt{2}. \tag{A8}$$

The mass matrix is not Hermitian and thus one needs biunitary transformations to diagonalize it. We define the biunitary transformation so that

$$D_R^{\nu_{\uparrow}}(M_f)D_L^{\nu} = \text{diag}(m_{\psi_1}, m_{\psi_2}, m_{\psi_3}, m_{\psi_4}, m_{\psi_5}).$$
(A9)

where $\psi_1, \psi_2, \psi_3, \psi_4, \psi_5$ are the mass eigenstates for the neutrinos. In the limit of no mixing we identify ψ_1 as the light tau neutrino, ψ_2 as the heavier mass mirror eigenstate, ψ_3 as the muon neutrino, ψ_4 as the electron neutrino and ψ_5 as the other heavy four-sequential generation neutrino. A similar analysis goes to the lepton mass matrix M_ℓ where

$$M_{f} = \begin{pmatrix} f_{1}v_{1}/\sqrt{2} & f_{4} & 0 & 0 & 0\\ f_{3} & f_{2}'v_{2}/\sqrt{2} & f_{3}' & f_{3}'' & h_{6}\\ 0 & f_{4}' & h_{1}v_{1}/\sqrt{2} & 0 & 0\\ 0 & f_{4}'' & 0 & h_{2}v_{1}/\sqrt{2} & 0\\ 0 & h_{7} & 0 & 0 & y_{5}v_{1}/\sqrt{2} \end{pmatrix}.$$
 (A10)

We introduce now the mass parameter m_E for the (22) element of the mass matrix above so that

$$m_E = f'_2 v_2 / \sqrt{2}.$$
 (A11)

CP phases that arise from the new sector are defined so that

$$f_{i} = |f_{i}|e^{i\chi_{i}}, \qquad f'_{i} = |f'_{i}|e^{i\chi'_{i}},$$

$$f''_{i} = |f''_{i}|e^{i\chi''_{i}} \qquad (i = 3, 4, 5)$$

$$h_{k} = |h_{k}|e^{i\chi_{k}}, \qquad k = 6, 7, 8.$$
(A12)

As in the neutrino mass matrix case, the charged slepton mass matrix is not Hermitian and thus one needs again a biunitary transformation to diagonalize it. We define the biunitary transformation so that

$$D_{R}^{\tau^{\dagger}}(M_{\ell})D_{L}^{\tau} = \text{diag}(m_{\tau_{1}}, m_{\tau_{2}}, m_{\tau_{3}}, m_{\tau_{4}}, m_{\tau_{5}}), \quad (A13)$$

where τ_{α} ($\alpha = 1-5$) are the mass eigenstates for the charged lepton matrix.

The mass squared matrices of the slepton-mirror slepton and sneutrino-mirror sneutrino sectors come from three sources: the F term, the D term of the potential and the soft SUSY breaking terms. After spontaneous breaking of the electroweak symmetry the Lagrangian is given by

$$\mathcal{L} = \mathcal{L}_F + \mathcal{L}_D + \mathcal{L}_{\text{soft}}, \qquad (A14)$$

where \mathcal{L}_F is deduced from $-\mathcal{L}_F = F_i F_i^*$, while the \mathcal{L}_D is given by

$$-\mathcal{L}_{D} = \frac{1}{2} m_{Z}^{2} \cos^{2} \theta_{W} \cos 2\beta \{ \tilde{\nu}_{\tau L} \tilde{\nu}_{\tau L}^{*} - \tilde{\tau}_{L} \tilde{\tau}_{L}^{*} + \tilde{\nu}_{\mu L} \tilde{\nu}_{\mu L}^{*} - \tilde{\mu}_{L} \tilde{\mu}_{L}^{*} + \tilde{\nu}_{eL} \tilde{\nu}_{eL}^{*} - \tilde{e}_{L} \tilde{e}_{L}^{*} + \tilde{E}_{R} \tilde{E}_{R}^{*} - \tilde{N}_{R} \tilde{N}_{R}^{*} + \tilde{\nu}_{4L} \tilde{\nu}_{4L}^{*} - \tilde{\ell}_{4L} \tilde{\ell}_{4L}^{*} \} + \frac{1}{2} m_{Z}^{2} \sin^{2} \theta_{W} \cos 2\beta \{ \tilde{\nu}_{\tau L} \tilde{\nu}_{\tau L}^{*} + \tilde{\tau}_{L} \tilde{\tau}_{L}^{*} + \tilde{\nu}_{\mu L} \tilde{\nu}_{\mu L}^{*} + \tilde{\mu}_{L} \tilde{\mu}_{L}^{*} + \tilde{\nu}_{eL} \tilde{\nu}_{eL}^{*} + \tilde{e}_{L} \tilde{e}_{L}^{*} + \tilde{\nu}_{4L} \tilde{\nu}_{4L}^{*} + \tilde{\ell}_{4L} \tilde{\ell}_{4L}^{*} - \tilde{E}_{R} \tilde{E}_{R}^{*} - \tilde{N}_{R} \tilde{N}_{R}^{*} + 2\tilde{E}_{L} \tilde{E}_{L}^{*} - 2\tilde{\tau}_{R} \tilde{\tau}_{R}^{*} - 2\tilde{\mu}_{R} \tilde{\mu}_{R}^{*} - 2\tilde{e}_{R} \tilde{e}_{R}^{*} - 2\tilde{\ell}_{4R} \tilde{\ell}_{4R}^{*} \}.$$
(A15)

For $\mathcal{L}_{\text{soft}}$ we assume the following form:

$$-\mathcal{L}_{\text{soft}} = \tilde{M}_{\tau L}^{2} \tilde{\psi}_{\tau L}^{i*} \tilde{\psi}_{\tau L}^{i} + \tilde{M}_{\chi}^{2} \tilde{\chi}^{ci*} \tilde{\chi}^{ci} + \tilde{M}_{\mu L}^{2} \tilde{\psi}_{\mu L}^{i*} \tilde{\psi}_{\mu L}^{i} + \tilde{M}_{e L}^{2} \tilde{\psi}_{e L}^{i*} \tilde{\psi}_{e L}^{i} + \tilde{M}_{\nu_{\tau}}^{2} \tilde{\nu}_{\tau L}^{c*} \tilde{\nu}_{\tau L}^{c} + \tilde{M}_{\nu_{\mu}}^{2} \tilde{\nu}_{\mu L}^{c*} \tilde{\nu}_{e L}^{c} + \tilde{M}_{\nu_{\mu}}^{2} \tilde{\psi}_{e L}^{i*} \tilde{\nu}_{\tau L}^{c} + \tilde{M}_{\mu L}^{2} \tilde{\psi}_{e L}^{i*} \tilde{\psi}_{e L}^{i} + \tilde{M}_{e L}^{2} \tilde{\psi}_{e L}^{c*} \tilde{\nu}_{\tau L}^{c} + \tilde{M}_{\mu L}^{2} \tilde{\psi}_{e L}^{i*} \tilde{\nu}_{L}^{c} + \tilde{M}_{e L}^{2} \tilde{\psi}_{e L}^{c*} \tilde{\psi}_{e L}^{c} \tilde{\psi}_{e L}^{c} + \tilde{M}_{e L}^{2} \tilde{\psi}_{e L}^{c*} \tilde{\psi}_{e L}^{c} \tilde{\psi}_{e L}^{c} + \tilde{M}_{e L}^{2} \tilde{\psi}_{e L}^{c*} \tilde{\psi}_{e L}^{c} \tilde{$$

We define the scalar mass squared matrix $M^2_{\tilde{\tau}}$ in the basis

$$(\tilde{\tau}_L, \tilde{E}_L, \tilde{\tau}_R, \tilde{E}_R, \tilde{\mu}_L, \tilde{\mu}_R, \tilde{e}_L, \tilde{e}_R, \tilde{\ell}_{4L}, \tilde{\ell}_{4R}).$$
(A17)

We label the matrix elements of these as $(M^2_{\tilde{\tau}})_{ij} = M^2_{ij}$ where the elements of the matrix are given by

$$\begin{split} M_{11}^2 &= \tilde{M}_{\tau L}^2 + \frac{v_1^2 |f_1|^2}{2} + |f_3|^2 - m_Z^2 \cos 2\beta \left(\frac{1}{2} - \sin^2 \theta_W\right), \\ M_{22}^2 &= \tilde{M}_L^2 + \frac{v_2^2 |f_2|^2}{2} + |f_4|^2 + |f_4'|^2 + |f_4''|^2 + |h_7|^2 + m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{33}^2 &= \tilde{M}_\tau^2 + \frac{v_1^2 |f_1|^2}{2} + |f_4|^2 - m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{44}^2 &= \tilde{M}_\chi^2 + \frac{v_2^2 |f_2'|^2}{2} + |f_3|^2 + |f_3'|^2 + |f_3''|^2 + |h_6|^2 + m_Z^2 \cos 2\beta \left(\frac{1}{2} - \sin^2 \theta_W\right), \\ M_{55}^2 &= \tilde{M}_{\mu L}^2 + \frac{v_1^2 |h_1|^2}{2} + |f_3'|^2 - m_Z^2 \cos 2\beta \left(\frac{1}{2} - \sin^2 \theta_W\right), \\ M_{66}^2 &= \tilde{M}_\mu^2 + \frac{v_1^2 |h_1|^2}{2} + |f_3'|^2 - m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{77}^2 &= \tilde{M}_{eL}^2 + \frac{v_1^2 |h_2|^2}{2} + |f_3'|^2 - m_Z^2 \cos 2\beta (\frac{1}{2} - \sin^2 \theta_W), \\ M_{88}^2 &= \tilde{M}_e^2 + \frac{v_1^2 |h_2|^2}{2} + |f_3'|^2 - m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{99}^2 &= \tilde{M}_{4L}^2 + \frac{v_1^2 |h_2|^2}{2} + |h_6|^2 - m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{1010}^2 &= \tilde{M}_4^2 + \frac{v_1^2 |y_3|^2}{2} + |h_7|^2 - m_Z^2 \cos 2\beta \sin^2 \theta_W, \\ M_{121}^2 &= M_{21}^2 + \frac{v_2 f_2 f_3^*}{\sqrt{2}} + \frac{v_1 f_4 f_1^*}{\sqrt{2}}, \\ M_{13}^2 &= M_{31}^2 = \frac{f_1^*}{\sqrt{2}} (v_1 A_\tau^* - \mu v_2), \\ M_{14}^2 &= M_{61}^2 = 0, \qquad M_{17}^2 = M_{71}^2 = f_3' f_3^*, \qquad M_{18}^2 = M_{81}^2 = 0, \qquad M_{23}^2 = M_{32}^2 = 0, \\ M_{24}^2 &= M_{62}^2 = 0, \qquad M_{27}^2 = M_{22}^2 = \frac{v_2 f_3' f_2''}{\sqrt{2}} + \frac{v_1 h_1 f_4''}{\sqrt{2}}, \\ M_{26}^2 &= M_{62}^2 = 0, \qquad M_{27}^2 = M_{27}^2 = \frac{v_2 f_3' f_2''}{\sqrt{2}} + \frac{v_1 h_1 f_4''}{\sqrt{2}}, \qquad M_{28}^2 = M_{28}^2 = 0, \\ M_{34}^2 &= M_{43}^2 = \frac{v_2 f_2 f_2''}{\sqrt{2}} + \frac{v_1 f_1 f_3''}{\sqrt{2}}, \qquad M_{35}^2 = M_{25}^2 = 0, \end{aligned}$$

$$\begin{split} &M_{36}^2 = M_{63}^2 = f_4 f_4'^*, \\ &M_{37}^2 = M_{73}^{2*} = 0, \qquad M_{38}^2 = M_{83}^{2*} = f_4 f_4''^*, \qquad M_{45}^2 = M_{54}^{2*} = 0, \qquad M_{46}^2 = M_{64}^{2*} = \frac{v_2 f_2' f_4''}{\sqrt{2}} + \frac{v_1 f_3' h_1^*}{\sqrt{2}}, \\ &M_{47}^2 = M_{74}^{2*} = 0, \qquad M_{48}^2 = M_{84}^{2*} = \frac{v_2 f_2' f_4''}{\sqrt{2}} + \frac{v_1 f_3'' h_2^*}{\sqrt{2}}, \\ &M_{56}^2 = M_{65}^{2*} = \frac{h_1^*}{\sqrt{2}} (v_1 A_{\mu}^* - \mu v_2), \qquad M_{57}^2 = M_{75}^{2*} = f_3'' f_3'', \qquad M_{58}^2 = M_{85}^{2*} = 0, \qquad M_{67}^2 = M_{76}^{2*} = 0, \\ &M_{68}^2 = M_{86}^{2*} = f_4' f_4''', \qquad M_{78}^2 = M_{87}^{2*} = \frac{h_2^*}{\sqrt{2}} (v_1 A_e^* - \mu v_2) \\ &M_{19}^2 = M_{91}^2 = f_3^* h_6, \qquad M_{110}^2 = M_{101}^{2*} = 0, \\ &M_{29}^2 = M_{93}^{2*} = \frac{v_{15} h_7'}{\sqrt{2}} + \frac{v_{2} h_0 f_2''}{\sqrt{2}}, \qquad M_{210}^2 = M_{102}^{2*} = 0, \\ &M_{39}^2 = M_{93}^2 = 0, \qquad M_{410}^2 = M_{104}^{2*} = \frac{v_2 f_2' h_1^*}{\sqrt{2}} + \frac{v_1 h_6 y_5^*}{\sqrt{2}}, \\ &M_{39}^2 = M_{93}^2 = 0, \qquad M_{410}^2 = M_{104}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = f_3'' h_6, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = f_3'' h_6, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = f_3'' h_6, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = f_3'' h_6, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{210}^2 = M_{105}^{2*} = 0, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{210}^2 = M_{105}^{2*} = f_3' h_7, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{310}^2 = M_{105}^{2*} = f_3' h_7, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{310}^2 = M_{105}^2 = f_3' h_7, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{310}^2 = M_{105}^{2*} = f_3' h_7, \\ &M_{29}^2 = M_{95}^2 = 0, \qquad M_{310}^2 = M_{105}^{2*} = f_3' h_7, \\ &M_{210}^2 = M_{109}^{2*} = \frac{y_5}{\sqrt{2}} (v_1 A_{4'}^* - \mu v_2). \end{aligned}$$

We assume that the masses that enter the mass squared matrix for the scalars are all of electroweak size. This mass squared matrix is Hermitian and can be diagonalized with a unitary transformation,

$$\tilde{D}^{\tau\dagger} M^2_{\tilde{\tau}} \tilde{D}^{\tau} = \text{diag}(M^2_{\tilde{\tau}_1}, M^2_{\tilde{\tau}_2}, M^2_{\tilde{\tau}_3}, M^2_{\tilde{\tau}_4}, M^2_{\tilde{\tau}_5}, M^2_{\tilde{\tau}_6}, M^2_{\tilde{\tau}_7}, M^2_{\tilde{\tau}_8} M^2_{\tilde{\tau}_9}, M^2_{\tilde{\tau}_{10}}).$$
(A19)

The mass squared matrix in the sneutrino sector has a similar structure. In the basis

$$(\tilde{\nu}_{\tau L}, \tilde{N}_L, \tilde{\nu}_{\tau R}, \tilde{N}_R, \tilde{\nu}_{\mu L}, \tilde{\nu}_{\mu R}, \tilde{\nu}_{eL}, \tilde{\nu}_{eR}, \tilde{\nu}_{4L}, \tilde{\nu}_{4R}),$$
(A20)

the sneutrino mass squared matrix $(M^2_{ ilde{
u}})_{ij}=m^2_{ij}$ has elements given by

$$\begin{split} m_{11}^2 &= \tilde{M}_{\tau L}^2 + \frac{v_2^2}{2} |f_1'|^2 + |f_3|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{22}^2 &= \tilde{M}_N^2 + \frac{v_1^2}{2} |f_2|^2 + |f_5|^2 + |f_3'|^2 + |f_3''|^2 + |f_3''|^2 + |f_3''|^2 + |f_3'|^2 + |f_3''|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{55}^2 &= \tilde{M}_{\mu L}^2 + \frac{v_2^2}{2} |h_1'|^2 + |f_3'|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{66}^2 &= \tilde{M}_{\nu_{\mu}}^2 + \frac{v_2^2}{2} |h_1'|^2 + |f_3''|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{66}^2 &= \tilde{M}_{\nu_{\mu}}^2 + \frac{v_2^2}{2} |h_2'|^2 + |f_3''|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{88}^2 &= \tilde{M}_{\nu_{e}}^2 + \frac{v_2^2}{2} |h_2'|^2 + |f_3''|^2, \\ m_{99}^2 &= \tilde{M}_{4L}^2 + \frac{v_2^2}{2} |y_5'|^2 + |h_6|^2 + \frac{1}{2} m_Z^2 \cos 2\beta, \\ m_{1010}^2 &= \tilde{M}_{24}^2 + |h_8|^2 + \frac{v_2^2}{2} |y_5'|^2, \\ m_{12}^2 &= m_{21}^{2*} = \frac{v_2 f_5 f_1''}{\sqrt{2}} - \frac{v_1 f_2 f_3^*}{\sqrt{2}}, \\ m_{13}^2 &= m_{31}^2 = \frac{f_1''}{\sqrt{2}} (v_2 A_{\nu_e}^* - \mu v_1), \qquad m_{14}^2 = m_{41}^{2*} = 0, \\ m_{15}^2 &= m_{32}^2 = 0, \qquad m_{24}^2 = m_{42}^{2*} = \frac{f_2^*}{\sqrt{2}} (v_1 A_N^* - \mu v_2), \\ m_{25}^2 &= m_{32}^2 = -\frac{v_1 f_2^2 f_3'}{\sqrt{2}} + \frac{h_1' v_2 f_3''}{\sqrt{2}}, \\ m_{26}^2 &= m_{62}^{2*} = 0, \\ m_{27}^2 &= m_{72}^2 = -\frac{v_1 f_2^2 f_3'}{\sqrt{2}} + \frac{h_2' v_2 f_3'''}{\sqrt{2}}, \end{aligned}$$
(A21)

$$\begin{split} m_{28}^2 &= m_{82}^{2*} = 0, \qquad m_{34}^2 = m_{43}^{2*} = \frac{v_1 f_2^* f_5}{\sqrt{2}} - \frac{v_2 f_1' f_3^*}{\sqrt{2}}, \\ m_{35}^2 &= m_{53}^{2*} = 0, \qquad m_{36}^2 = m_{63}^{2*} = f_5 f_5''', \\ m_{37}^2 &= m_{73}^{2*} = 0, \qquad m_{38}^2 = m_{83}^{2*} = f_5 f_5''', \\ m_{45}^2 &= m_{54}^{2*} = 0, \qquad m_{46}^2 = m_{64}^{2*} = -\frac{h_1'^* v_2 f_3'}{\sqrt{2}} + \frac{v_1 f_2 f_5''}{\sqrt{2}}, \\ m_{47}^2 &= m_{74}^{2*} = 0, \qquad m_{48}^2 = m_{84}^{2*} = \frac{v_1 f_2 f_5''}{\sqrt{2}} - \frac{v_2 h_2' f_3''}{\sqrt{2}}, \\ m_{47}^2 &= m_{75}^{2*} = \frac{h_1'^*}{\sqrt{2}} (v_2 A_{\nu_{\mu}}^* - \mu v_1), \\ m_{57}^2 &= m_{75}^{2*} = f_3' f_3'', \qquad m_{58}^2 = m_{85}^{2*} = 0, \qquad m_{67}^2 = m_{76}^{2*} = 0, \\ m_{68}^2 &= m_{86}^{2*} = f_5' f_5''', \qquad m_{78}^2 = m_{87}^{2*} = \frac{h_2''}{\sqrt{2}} (v_2 A_{\nu_e}^* - \mu v_1), \\ m_{19}^2 &= m_{91}^2 = h_6 f_3^*, \qquad m_{110}^2 = m_{101}^{2*} = 0, \\ m_{29}^2 &= m_{92}^{2*} = -\frac{f_2 v_1 h_6}{\sqrt{2}} + \frac{v_2 h_8 y_5^*}{\sqrt{2}}, \qquad m_{210}^2 = m_{102}^{2*} = 0, \\ m_{39}^2 &= m_{93}^{2*} = 0, \qquad m_{310}^2 = m_{103}^{2*} = f_5 h_8^*, \\ m_{49}^2 &= m_{94}^{2*} = 0, \qquad m_{410}^2 = m_{104}^{2*} = -\frac{v_2 y_5' h_6}{\sqrt{2}} + \frac{v_1 h_8^* f_2}{\sqrt{2}}, \\ m_{59}^2 &= m_{95}^{2*} = h_6 f_3'', \qquad m_{710}^2 = m_{105}^{2*} = 0, \\ m_{69}^2 &= m_{96}^{2*} = 0, \qquad m_{610}^2 = m_{106}^{2*} = 0, \\ m_{69}^2 &= m_{96}^{2*} = 0, \qquad m_{610}^2 = m_{108}^{2*} = f_5' h_8^*, \\ m_{79}^2 &= m_{97}^{2*} = h_6 f_3'', \qquad m_{710}^2 = m_{107}^{2*} = 0, \\ m_{89}^2 &= m_{98}^{2*} = 0, \qquad m_{810}^2 = m_{108}^{2*} = f_5' h_8^*, \\ m_{910}^2 &= m_{109}^{2*} = \frac{y_5'}{\sqrt{2}} (v_2 A_{4\nu}^* - \mu v_1). \end{aligned}$$

Again as in the charged lepton sector we assume that all the masses are of the electroweak size so all the terms enter in the mass squared matrix. This mass squared matrix can be diagonalized by the unitary transformation,

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