Hidden confining world on the 750 GeV diphoton excess

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We explain the recent diphoton excesses around 750 GeV by both ATLAS and CMS as a singlet scalar Φ which couples to SM gluon and neutral gauge bosons only through higher-dimensional operators. A natural explanation is that Φ is a pseudo-Nambu-Goldstone boson (pNGB) which receives parity violation through anomaly if there exists a hidden strong dynamics. The singlet and other light pNGBs will decay into two SM gauge bosons and even serves as the metastable colored states which can be probed in the future. By accurately measuring their relative decay and the total production rate in the future, we will learn the underlying strong dynamics parameter. The lightest baryon in this confining theory could serve as a viable dark matter candidate.

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I. INTRODUCTION

Very recently, ATLAS and CMS Collaborations have announced their first host of new results based on 3.2 fb^{-1} and 2.6 fb⁻¹ integrated luminosity at LHC run II \sqrt{s} = 13 TeV [1.2]. Among various channels in searching for 13 TeV [\[1,2\].](#page-6-0) Among various channels in searching for new physics, there is an intriguing existence of diphoton excess around 750 GeV, with a local significance of 3.6σ and 2.6σ , respectively, in ATLAS and CMS. With more data accumulating, it will soon be revealed whether this is due to a statistical fluctuation or some manifestation of new physics. Nevertheless, as theorists, we should always be aware that this could be the first light that changes our current understanding of microscopic physics.

The first appearance of this anomalous diphoton resonance at LHC run II would unambiguously tell us some information. First, due to the Landau-Yang theorem [\[3\]](#page-6-1), this resonance can only be spin zero or two instead of one. Second, the resonance decay into diphoton process can only be through the higher-dimensional operators [\[4\]](#page-6-2). Therefore, an unsuppressed total decay width would require an unconventional large production rate and one might need to try hard to hide its main decay channel into the SM backgrounds. Third, according to the 8 TeV LHC run I results, the CMS search [\[5\]](#page-6-3) sets a 95% C.L. observed upper limit of $\sigma(pp \to \Phi)Br(\Phi \to \gamma\gamma) < 1.5$ fb, and the ATLAS search [\[6\]](#page-6-4) also imposes similar constraints on RS gravitons. In order to accommodate both LHC run I and run II results, a larger enhancement on the diphoton signal from 8 to 13 TeV is

needed, and the gluon initial state is preferred. Collecting all the above hints, we consider a singlet scalar Φ with only SM higher-dimensional couplings to gluon and neutral gauge bosons as perhaps the optimal solution.

While the process $qq \to \Phi \to \gamma \gamma$ looks simple, it does have a very rich and deep physics behind it. If the Φ is pseudoscalar, or even a pseudo-Nambu-Goldstone boson (pNGB), then the only existence of higher-dimensional couplings to gluon and neutral gauge bosons is a natural consequence of Φ parity violation due to anomaly [\[7\]](#page-6-5). The anomaly-induced process at the IR, which affects the Φ production and decay, is proportional to the number of color N_n in the underlying confining strong dynamics. Therefore, if this excess continues to exist in the future, by accurately measuring the diphoton resonance rate and the relative rate among different SM diboson decay channels, we could learn N_n and the hypercharge of the confining vector fermions. This provides us another example of learning the ultraviolet physics at the infrared just like a rediscovery of color $N_c = 3$ in QCD through $\pi_0 \rightarrow \gamma \gamma$. If one of the confining vector fermions ψ is a SM singlet, the baryon which is made of N_n copies of ψ could be a composite dark matter candidate if ψ is the lightest confining vector fermions. Therefore, we use this particular choice of charge assignment as the benchmark of our model in the phenomenology discussion.

The layout of this paper is as follows. In Sec. [II,](#page-1-0) we parametrize our setup in terms of effective theory and give a numerical fit to the 13 TeV diphoton excess. In Sec. [III,](#page-2-0) we build up the simplest hidden QCD model with the required singlet couplings through anomaly based on $SU(4)$ flavor symmetry and discuss the related phenomenology. The benchmark model with a composite dark matter (DM)

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candidate from the hidden baryon is highlighted. We make conclusions in Sec. [IV.](#page-4-0) We provide in the Appendix to derive the effective Wess-Zumino-Witten (WZW) terms of the simplest confining model.

II. THE EFFECTIVE THEORIES

We first consider the general dimension-five couplings between a singlet (pseudo)scalar and the gauge fields,

$$
-\left(\frac{\alpha_s C_g^S}{16\pi F} G_{\mu\nu}^a G^{\mu\nu,a} + \frac{\alpha C_\gamma^S}{2\pi F} F_{\mu\nu} F^{\mu\nu}\right) \Phi_S, \tag{1a}
$$

$$
-\left(\frac{\alpha_s C_g^P}{16\pi F} G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} + \frac{\alpha C_f^P}{2\pi F} F_{\mu\nu} \tilde{F}^{\mu\nu}\right) \Phi_P, \qquad (1b)
$$

respectively. Here, $G_{\mu\nu}^a$ and $F_{\mu\nu}$ are $SU(3)_c$ and $U(1)_{em}$
field strength tensors. E is expected to be the energy scale field strength tensors. F is expected to be the energy scale of the underlying new physics model. The decay widths of (pseudo)scalar $\Phi_{S}(\Phi_{P})$ to gluon and photon pairs could be obtained from Eq. [1](#page-1-1),

$$
\Gamma(\Phi_{S/P} \to \gamma \gamma) = \frac{M_{\Phi_{S/P}}^3 \alpha^2}{16\pi^3 F^2} (C^{S/P}_\gamma)^2, \tag{2a}
$$

$$
\Gamma(\Phi_{S/P} \to gg) = \frac{M_{\Phi_{S/P}}^3 \alpha_s^2}{128\pi^3 F^2} (C_g^{S/P})^2.
$$
 (2b)

There can be different origins for obtaining the operators in Eq. [\(1\)](#page-1-1). The first example is analogous to the Higgs effective couplings to gluons and photons. One may consider a set of vectorlike color-charged and/or electriccharged fermions F_k coupling with the singlet scalars such that $\sum_k \bar{F}_k (\lambda_k \Phi_S + i \gamma_5 \hat{\lambda}_k \Phi_P) F_k$. Integrating out the heavy
fermions F_k , the Wilson coefficients in the effective fermions F_k , the Wilson coefficients in the effective Lagrangian, Eq. [\(1b\),](#page-1-2) are calculated to be

$$
C_{\gamma}^{S} = \sum_{k} \frac{\lambda_{k} N_{c}(k) Q_{k}^{2}}{3}, \qquad C_{\gamma}^{P} = \sum_{k} \frac{\hat{\lambda}_{k} N_{c}(k) Q_{k}^{2}}{2},
$$

$$
C_{g}^{S} = \sum_{k} \frac{4\lambda_{k}}{3}, \qquad C_{g}^{P} = \sum_{k} 2\hat{\lambda}_{k},
$$
(3)

with $N_c(k)$ and Q_k being the SU(3)_c color degrees of freedom and charges carried by F_k . We assume degenerate masses of $M_k = F$ for simplicity. In the following, we will denote the couplings and charges of vectorlike fermions collectively as $\lambda_F = {\lambda_k, \hat{\lambda}_k}$ and $Q_F = {Q_k}$. In addition, the effective coupling for the *CP*-odd operator can be the effective coupling for the CP-odd operator can be induced by the anomaly of the chiral symmetry breaking. This is nothing but the effective WZW term [\[8,9\]](#page-6-6). In the next section, a specific model construction will be given.

Due to the couplings, we expect the following relations [\[10\]:](#page-6-7)

$$
\Gamma(\Phi_{S/P} \to gg) \propto (C_g/F)^2,\tag{4a}
$$

$$
\Gamma(\Phi_{S/P} \to \gamma \gamma) \propto (C_{\gamma}/F)^2. \tag{4b}
$$

The cross section of the production process of $gg \to \Phi_{S/P}$ should only depend on $(C_g/F)^2$; hence, the following semianalytic formula for the signal process could be expected, $\sigma[gg \to \Phi_{S/P} \to \gamma\gamma] \sim (C_g/F)^2 (C_f^2 f_2)/(C_f^2 f_2 + C_g^2 f_1)$. Here (f, f) are constants and one sympate $f, f \neq g$ $C_g^2 f_1$). Here (f_1, f_2) are constants and one expects $f_1/f_2 \propto$
 $(g_1/g_1^2)(10^2-10^3)$ (potiac that the eberge Q is a beerhed $\left(\frac{\alpha_s}{\alpha}\right)^2 \sim (10^2 - 10^3)$ (notice that the charge Q_k is absorbed into C_γ . We find $\sigma[gg \to \Phi_{S/P}] \approx (6.2 \text{ fb}) \times C_g^2(\frac{1 \text{ TeV}}{F})^2$.

We perform the numerical analysis of the diphoton excess by using the implementation of the dimension-five operators, Eq. [\(1\),](#page-4-1) in FeynRules [\[11\]](#page-6-8) and generate events with MadGraph [\[12\],](#page-6-9) interfaced with Pythia [\[13\]](#page-6-10) and Delphes [\[14\]](#page-6-11) for the parton shower, hadronization and the fast detector simulations. The analysis is conducted based on the CMS cuts in Ref. [\[2\].](#page-6-12) The diphoton events are reconstructed by selecting photons such that $p_T(\gamma) \geq 75$ GeV, $|\eta(\gamma)| \leq 2.5$ and $|\eta(\gamma)|$ not within (1.4442, 1.566). At least one photon should be in the barrel region, i.e., $|\eta| \leq 1.4442$. The diphoton invariant mass should be $m_{\gamma\gamma} \geq 230$ GeV. For events with one photon in the end-cap region such that $|\eta(\gamma)| \ge 1.566$, we require $m_{\gamma\gamma} \geq 320$ GeV. Furthermore, only the events with the diphoton invariant mass in the range of $m_{\gamma\gamma} \in (650$ and 800 GeV) are selected. In order to account for the diphoton excess at the LHC, the cross section of $\sigma(pp \to$ $\Phi \rightarrow \gamma \gamma$) at the LHC 13 TeV should be around 3–13 fb, while the run I constraints tell us that the cross section at the LHC 8 TeV should be less than 1.5 fb. Figure [1](#page-1-3) shows the contour plot on the $(C_{\gamma}/C_g, C_g)$ plane for the $\sigma(pp \to$ $\Phi \rightarrow \gamma \gamma$) at the 8 and 13 TeV LHC, from which we can

FIG. 1. The cross sections of $\sigma [pp \rightarrow \Phi \rightarrow \gamma \gamma]$ (unit: fb) on the $(C/C-C)$ plane at 8 (green dashed) and 14 TeV (blue solid) $(C_y/C_a, C_a)$ plane at 8 (green dashed) and 14 TeV (blue solid) with $F = 1$ TeV. The pink region represents the region that can explain the LHC 13 TeV results while remaining unconstrained from LHC run-I bound.

infer that small $C_q \lesssim 3$ requires a large ratio $C_\gamma/C_q \gtrsim 8$. Notice that in the case of degenerate coupling and charge for the vectorlike fermions, $C_{\gamma}/C_g = N_c Q_F^2/4$; therefore, from the plot, we can see that our theory even remains to have small coupling $\lambda_F \lesssim 1$ for $Q_F \gtrsim 3$ when we fix $M_F =$ 1 TeV $[C_g^S = 4\lambda_F N_f/3$ and $C_g^P = 2\lambda_F N_f$ through Eq. [\(3\)](#page-1-4)].

III. THE MODEL WITH NEW STRONG DYNAMICS

Next, we turn to a specific model setup by assuming a new QCD-like strong sector with the gauge symmetry of $SU(N_n)$. The new strong dynamics possesses the properties of confinement and the asymptotic freedom. We denote the pion decay constant of new strong dynamics as f_{Π} and the dynamical scale as Λ_n . They are related as $\Lambda_n \simeq$ $4\pi f_{\Pi}/\sqrt{N_n}$ by the large-N scaling relation. Unlike the technicolor theories [15–[17\],](#page-6-13) the strong sector is not necessarily related to the electroweak symmetry breaking. As a result, we are free to consider the case where only gauge bosons of unbroken gauge symmetries, namely, gluons and photons, can talk directly to the new sector. We assume a set of vectorlike fermions (ψ^1, ψ^2) under the fundamental representation of the new gauge group $SU(N_n)$. We are especially interested in the case where only the SU(3)_c and U(1)_Y fields have the anomaly in order to account for the diphoton excess. This can be realized by assuming that the fundamental fermions (ψ^1, ψ^2) in the new strong sector belong to the singlets of the SM $SU(2)_I$ gauge group. In order to embed the $SU(3)_c$ group and have the color-singlet pNGBs, we consider the minimal case with $N_f = 4$ and gauge the subgoup $SU(3)_c \times U(1)_Y$ of SU(4). The quantum numbers of (ψ^1, ψ^2) are summarized in Table. [I](#page-2-1). More general discussions of the global symmetry breaking patterns in different representations under the new gauge symmetries can be found in Ref. [\[18\]](#page-6-14). The LHC phenomenology of the models with vectorlike confinement were studied in Refs. [\[19,20\]](#page-6-15).

All gauge anomalies are canceled since the fermions (ψ^1, ψ^2) are vectorlike under both the SU (N_n) and the SM gauge groups. The requirement of the asymptotical freedom of the new gauge theory $SU(N_n)$ bounds the number of flavor to be $N_f \leq 11N_n/2$, which is easily satisfied for $N_f = 4$ and $N_n \geq 3$ in our model [\[21\]](#page-6-16). In addition, the asymptotical freedom of QCD should be retained, which bounds the color degrees of freedom in the new strong sector as $N_n \leq 10$.

In the limit of vanishing SM gauge couplings, the strong sector possesses the global chiral symmetry of $SU(4)_L\times$ $SU(4)_R \times U(1)_A \times U(1)_{B_n}$, where $U(1)_{B_n}$ denotes the

TABLE I. The field content of the minimal model. $\forall Y_{1,2} \in \mathbb{Q}$.

	$SU(N_n)$	$SU(3)_c$	SU(2) _L	U(1) v
$\psi^1_{L,R}$	\mathbf{w}_n			
$\psi^2_{L,R}$	$1 \mathbf{v}_n$			

baryon number symmetry in the new strong sector. The axial symmetry of $U(1)_A$ is broken by the instanton effects and will be neglected henceforth. The confinement of the theory at a new scale Λ_n will induce spontaneous chiral symmetry breaking of $SU(4)_L \times SU(4)_R \rightarrow SU(4)_V$, which results in 15 pNGBs Π^A . They can be decomposed into representations of the SM gauge goup $SU(3)_c \times$ $SU(2)_L \times U(1)_Y$ as follows:

$$
15 \to (8,1)_0 + (3,1)_{Y_1 - Y_2} + (\bar{3},1)_{Y_2 - Y_1} + (1,1)_0. \quad (5)
$$

Below we label the color octet, triplet and singlet pNGBs as Φ_8 , Φ_3 and Φ_1 , respectively. The masses of pNGBs arise from the gauge-invariant mass terms of $-m_O(\bar{\psi}^1\psi^1 +$ $\bar{\psi}^2 \psi^2$) for vectorlike fermions. Such mass terms provide the dominant mass source and the gauging of the SM group only splits the color octets Φ_8 and singlets Φ_1 . The meson masses are given by the Gell-Mann–Oakes-Renner relation [\[22\]](#page-6-17)

$$
M_{\Phi_8}^2 \sim 2m_Q \Lambda_n^3 / f_\Pi^2 + \left(\frac{3g_s^2}{16\pi^2}\right) \Lambda_n^2,
$$

\n
$$
M_{\Phi_3}^2 \sim 2m_Q \Lambda_n^3 / f_\Pi^2 + \left(\frac{g_s^2}{24\pi^2} + \frac{(Y_1 - Y_2)^2 g'^2}{16\pi^2}\right) \Lambda_n^2,
$$

\n
$$
M_{\Phi_1}^2 \sim 2m_Q \Lambda_n^3 / f_\Pi^2.
$$
\n(6)

The singlet remains the lightest as a result of the Witten theorem [\[23\]](#page-6-18) and is a good candidate for the diphoton excess. Below, we focus on a benchmark model with $f_{\Pi} \approx$ 2.5 TeV with $N_n = 10$ for a composite DM candidate in the spectrum. The corresponding vectorlike fermion mass is found to be $m_Q \approx 1$ GeV to accommodate a 750 GeV singlet in the new strong dynamical sector. Note, the benchmark model given here is made by assuming the unitarity bound to the DM mass is saturated. More generic choices of the pion decay constant of f_{Π} and the gauge symmetries can be expected. Correspondingly, the vectorlike fermion mass range spanning from $\mathcal{O}(1)$ to $\mathcal{O}(10)$ GeV is also natural.

The pion-number violating interactions arise from the effective WZW term,

$$
\mathcal{L}_{\text{WZW}} = -\frac{N_n g_B g_C}{8\pi^2} \frac{\Pi_A}{f_{\Pi}} F^{\mu\nu,B} \tilde{F}^C_{\mu\nu} \text{Tr}[T^A T^B T^C], \quad (7)
$$

where $g_{B,C}$ are the gauge couplings associated with the SM gauge field strength tensors $F_{\mu\nu}^{B,C}$, and the dual field strength tensor is defined as $\tilde{F}^A_{\mu\nu} \equiv \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} F^{\rho\sigma,A}$. Here, the trace is performed over the SM indices.

In principle, we can freely choose the hypercharges of $SU(3)$, triplet and singlet. The singlet couplings to the hypercharge fields lead to the possible diphoton signals, given that $Y_1 \neq Y_2$. Note that topological interactions between the color-triplet and the SM gauge bosons are forbidden by the $SU(3)_c$ symmetry. An interesting and special case is $Y_2 = 0$ where ψ^2 is a SM singlet. In this case, the baryonic composites $(\psi^2)^{N_n} \equiv \epsilon^{a_1...a_{N_n}} \psi^2_{a_1} \dots \psi^2_{a_N}$ could be a dark matter candidate. Therefore, we will use $Y_2 = 0$ as our benchmark model in the later discussions.

According to the effective WZW terms in Eq. [\(7\)](#page-2-2) for the singlet Φ_1 , we expect its couplings to the $(gg, \gamma\gamma, \gamma Z, ZZ)$ final states. Likewise, the color octet Φ_8 can couple to $(gq, q\gamma, qZ)$. The explicit expressions for the WZW effective terms are given in Eqs. [\(A4\)](#page-5-0) and [\(A5\),](#page-5-1) with the corresponding partial decay widths of Φ_1 and Φ_8 given in Eqs. [\(A7\)](#page-5-2) and [\(A8\).](#page-5-3) In Fig. [2](#page-3-0), we display the decay branching fractions of the singlet Φ_1 with the varying inputs of $|Y_1|$ by assuming that $Y_2 = 0$. The increasing $|Y_1|$ apparently leads to the enhancement of the decay modes of $(\gamma \gamma, \gamma Z, ZZ)$.

If the future LHC experiments discover both singlet Φ_1 and octet Φ_8 , one may measure the signal rates to $\gamma\gamma$ and dijets for Φ_1 , and the signal rates of γ plus jets and dijets for Φ_8 . Obviously, these signal rates can be used to determine the hypercharges in the minimal model. From Eqs. [\(A7\)](#page-5-2) and [\(A8\)](#page-5-3), one has

$$
Y_1^2 = \frac{5}{96} \frac{\alpha_s}{\alpha} \frac{\Gamma[\Phi_8 \to g\gamma]}{\Gamma[\Phi_8 \to g g]},
$$

$$
Y_2^2 = Y_1^2 \pm \frac{\alpha_s}{\alpha} \left(\frac{2}{9} \cdot \frac{\Gamma[\Phi_1 \to \gamma\gamma]}{\Gamma[\Phi_1 \to g g]}\right)^{1/2}.
$$
 (8)

Note from the meson mass spectrum in Eq. [\(6\)](#page-2-3), the octets are typically $\mathcal{O}(1)$ TeV heavier than the singlets.

The total production cross sections can be obtained by mapping the EFT parameter C_g into the minimal model, which is $C_g = \frac{2N_n}{\sqrt{6}}$ from Eqs. [\(7\)](#page-2-2) and [\(A4\)](#page-5-0). It is crucial to note the production of the color singlet Φ_1 is proportional to the number of colors in the new confining strong dynamics. Based on our numerical simulations by following the approaches described in the previous section and the decay branching ratios displayed in Fig. [2,](#page-3-0) we plot the signal predictions of $\sigma[pp \to \Phi_1 \to \gamma\gamma]$ on the $(f_{\Pi}, |Y_1|)$ plane in
Fig. 3 by fixing $Y_2 = 0$ for SU(10) hidden gauge Fig. [3](#page-3-1) by fixing $Y_2 = 0$ for SU(10) hidden gauge

FIG. 2. The decay branching ratios into various final states for the singlet Φ_1 .

FIG. 3. The diphoton cross section of $\sigma[p p \rightarrow \Phi_1 \rightarrow \gamma p]$ (unit:
fb) on the $(f_{\text{rel}} | Y, \cdot)$ plane for $Y_0 = 0$ with $K = 1.6$ [25] for the fb) on the $(f_\Pi, |Y_1|)$ plane for $Y_2 = 0$, with $K = 1.6$ [\[25\]](#page-6-23) for the NLO QCD correction. The blue and green curves correspond to the 13 TeV and 8 TeV predictions, respectively. The total decay width of Φ_1 in unit of GeV is shown by purple contours. Cyan region are allowed region of $Z\gamma$ final states from CMS run I, and magenta region is favored by 13 TeV diphoton excess and allowed by 8 TeV CMS diphoton limits. The color number in the hidden strong sector is chosen as $N_n = 10$. A benchmark point marked by star correspond to $f_{\Pi} \approx 2.5$ TeV, $|Y_1| = 4/3$, and the diphoton signal cross section of 5.4 fb.

symmetry. The parameter region with large $|Y_1|$ and small f_{Π} inputs have been excluded by the ATLAS searches for Zγ [\[24\].](#page-6-19) Furthermore, the total decay width of Φ_1 is found to be hardly larger than 0.1 GeV for parameter regions favored by the LHC 13 and 8 TeV data sets. Therefore, the limits on cross section of the spin-0 resonance to diphoton in the narrow width hypothesis with $\Gamma_X = 0.1$ GeV [\[5\]](#page-6-3) is applicable to some extent.

In addition to the diphoton signal predictions we explored above, the minimal model also predicts several other experimental signatures. We note above that the color singlet Φ_1 decays also to *gg*. Correspondingly, one would envision the future dijet searches around the mass resonance of ∼750 GeV. Expressed in terms of the effective couplings defined in Eq. [\(1\)](#page-1-1), the ratio between the diphoton and gluon pair signals are determined by $(C_{\gamma}/C_q)^2$ = $\frac{9}{16}(Y_1^2 - Y_2^2)^2$. Therefore, the future observation and measurements of the dijet signals are not only useful for justifying the model, but also crucial for determining the hypercharge differences for the underlying model.

The other experimental constraints related to the minimal model are the searches for the vectorlike quarks ψ^1 and the color triplet Φ_3 in the spectrum. They can be pair produced and hadronize with quarks and gluons to form the R hadrons. The R-hadron searches at the LHC thus place mass limits on the color triplet, and the color triplet mass is bound above around 845 GeV by LHC run I results [\[26,27\]](#page-6-20). The LHC run II at 13 TeV would set the bound more stringent [\[28\]](#page-6-21). The analysis in Ref. [\[29\]](#page-6-22) set an exclusion to charged stable particles to ∼900 GeV for sufficiently long decay lengths of $c\tau \ge 10$ m.

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The color triplet Φ_3 has hypercharge $Y_1 - Y_2$, so that it can decay to SM lepton-quark pair through higherdimensional operators for specific choices of $Y_1 - Y_2$. Examples include

$$
Y_1 - Y_2 = \frac{2}{3} : \frac{1}{\Lambda^2} (\bar{\psi}^2 \gamma^{\mu} \gamma_5 \psi^1) (\bar{d}_R \gamma_{\mu} e_R),
$$

\n
$$
Y_1 - Y_2 = \frac{5}{3} : \frac{1}{\Lambda^2} (\bar{\psi}^2 \gamma^{\mu} \gamma_5 \psi^1) (\bar{u}_R \gamma_{\mu} e_R).
$$
 (9)

For the benchmark in Fig. [3,](#page-3-1) one may look for the pairproduced lepton-quark signals of $ji\ell\ell$ to search for this resonance. The current mass exclusion of Φ_3 is ∼1 TeV from the ATLAS 8 TeV searches [\[30\]](#page-6-24). For sufficiently small Λ , the metastable Φ_3 is expected to decay before the era of the big bang nucleosynthesis (BBN) [\[31](#page-6-25)–33] through Eq. [\(9\).](#page-4-2) This is different from the case in Ref. [\[34\]](#page-6-26) where small symmetry-breaking Yukawa couplings between the new fermions and the Higgs doublet are expected to avoid the tension with BBN induced by the metastable charged meson. We left the careful study of BBN to future work.

There are also baryonic composites in the $SU(N_n)$ confining gauge theory since $\pi_3(SU(4)^2/SU(4)) = \mathbb{Z}$. Such baryonic composites usually saturate the cut off scale $4\pi f_{\Pi}$ and thus are heavy. They are also the topological objects, which in general get more suppressed production rate besides of the heavy mass kinematical suppression. Therefore, we only expect very tiny production rate at the LHC. In the case of $m_{w_1} \ge m_{w_1}$ and $Y_2 = 0$ [\[35\],](#page-6-27) the $(w^2)^{N_n}$ baryonic composites would be a composite DM candidate. The thermally averaged annihilation rate of the dark baryons could be estimated using partial wave unitarity [\[34,36,37\]](#page-6-26), and the dark baryon mass could be bounded from above as $m_B \lesssim 100$ TeV [\[38\].](#page-6-28) When this bound is saturated, we find $f_{\Pi} \approx 2.5$ TeV with $N_n = 10$ as our benchmark model marked by star in Fig. [3.](#page-3-1) The estimation is made by employing the large-N scaling for the composite baryon mass of $m_B \sim N_n \Lambda_n$ [\[39,40\]](#page-6-29). In the early universe, once it is thermally produced, the correct abundance of baryonic dark matter could be obtained with a relatively strong coupling. One may ask whether this baryonic dark matter is metastable through instanton effects [\[41\]](#page-6-30). However, the enormous suppression factor which is proportional to $\exp(-8\pi^2/g_s^2)$ will make its life time much longer
than the age of our Universe. And the consequence of than the age of our Universe. And the consequence of topological dark matter on cosmic ray signals and the decay of the DM through higher-dimension operators is highly related with the choice of N_n [\[42,43\]](#page-6-31), which is beyond the scope of this work. For more generic case without considering a hypothetical composite DM candidate with $Y_2 = 0$ as in the minimal model, the 750 GeV diphoton signals can be accommodated by varying f_{Π} from several hundred GeV to $\mathcal{O}(1)$ TeV with $3 \leq N_n \leq 10$.

IV. CONCLUSION

We have studied the possibility that a singlet scalar (CP-even or CP-odd) accounts for the recent diphoton excess observed by ATLAS and CMS which has attracted a lot of interest [\[31,44](#page-6-25)–78]. We focused on the gluon-gluon initiated process and studied it in an effective field theory approach, where the corresponding higher-dimension operators can be generated through the heavy vectorlike fermions. We then consider a natural example that the singlet scalar is a pseudo-Goldstone boson from chiral symmetry breaking of a new strong sector and the interactions with SM gauge bosons (the gluon, photon and Z) are purely topological and arising from anomaly. We consider the minimal flavor symmetry group $SU(4) \times$ $SU(4)$ with 15 pNGBs and find the lightest pNGB is color-singlet, which is a good candidate for the diphoton excess. Our model also predicts the color-octet, color-triplet scalars and composite baryons. For the color-triplet, there is no topological interaction arising from anomaly due to the $SU(3)$ _c symmetry; therefore, it could be metastable due to higher-dimensional operators and generates R-hadron-like signal at the LHC. Other anomaly decays of color-octet scalars are also discussed. The lightest neutral baryon could be a viable composite dark matter. If the diphoton excess is confirmed in the near future, the discovery of these resonances and the precise production and decay will provide us with a strong test of our scenario.

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Note added.—Recently, Ref. [\[31\]](#page-6-25) appeared, which also discusses a singlet pNGB production and decay through anomaly. Nevertheless, our model considers a more general charge assignment and focuses on the case where the second confining fermion ψ^2 is a SM singlet, where N_n copies of ψ^2 could be a composite dark matter candidate. We also consider the possibility that the color triplet scalar is metastable, which results in an R-hadron-like signal at the LHC run II (its decay pattern through the higherdimensional operator is also different). Moreover, we calculate the predicted hypercharge of the two confining fermions and the confining color number N_n in terms of the pNGB's different diboson decay rate.

APPENDIX: THE SU(4) GENERATORS AND WZW EFFECTIVE TERMS

We use the generalized Gell-Mann matrices as our generators,

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$$
T^{a} = \frac{1}{2} \begin{pmatrix} \lambda^{a} & 0 \\ 0 & 0 \end{pmatrix}, \qquad T^{15} = \frac{1}{2\sqrt{6}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -3 \end{pmatrix},
$$
\n(A1)

where λ^a for $a = 1, ..., 8$ are the SU(3) Gell-Mann matrices with $\text{Tr}(\lambda^a \lambda^b) = 2\delta^{ab}$, and T^{15} is the third Cartan generator. T^i with $i = 9, \ldots 14$ are not used in our evaluation, and their expressions are neglected. Collectively, we write down the pNGBs as

$$
\Pi_A T^A = \Phi_8^a T^a + \Phi_3^i \hat{T}^i + (\Phi_3^i \hat{T}^i)^{\dagger} + \Phi_1 T^{15}.
$$
 (A2)

Our hypercharge generator is defined by

$$
Y \equiv \text{diag}(Y_1, Y_1, Y_1, Y_2). \tag{A3}
$$

With the conventions listed above, it is straightforward to write down the WZW term between the pNGB Π_A and the SM gauge fields according to Eq. [\(7\)](#page-2-2). For the singlet Φ_1 , they read

$$
\mathcal{L}_{\Phi_1} = -\frac{N_n g_s^2}{8\pi^2} \frac{\Phi_1}{f_{\Pi}} G_{\mu\nu}^a \tilde{G}^{b,\mu\nu} \text{Tr}[T^{15}T^a T^b]
$$

$$
- \frac{N_n g'^2}{8\pi^2} \frac{\Phi_1}{f_{\Pi}} B_{\mu\nu} \tilde{B}^{\mu\nu} \text{Tr}[T^{15}Y^2]
$$

$$
= -\frac{N_n \alpha_s}{8\sqrt{6}\pi f_{\Pi}} \Phi_1 G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}
$$

$$
- \sqrt{6}(Y_1^2 - Y_2^2) \frac{N_n \alpha}{8\pi f_{\Pi}} \Phi_1 (\tilde{A}_{\mu\nu} A^{\mu\nu})
$$

$$
- 2t_W \tilde{Z}_{\mu\nu} A^{\mu\nu} + t_W^2 \tilde{Z}_{\mu\nu} Z^{\mu\nu}), \tag{A4}
$$

where $t_W \equiv \sin \theta_W / \cos \theta_W$. For octets Φ_8 , they read

$$
\mathcal{L}_{\Phi_8} = -\frac{N_n g_s^2}{8\pi^2} \frac{\Phi_8^a}{f_{\Pi}} G_{\mu\nu}^b \tilde{G}^{c,\mu\nu} \text{Tr}[T^a T^b T^c]
$$

$$
-\frac{N_n g' g_s}{8\pi^2} \frac{\Phi_8^a}{f_{\Pi}} G_{\mu\nu}^b \tilde{B}^{\mu\nu} \text{Tr}[T^a T^b Y]
$$

$$
= -\frac{N_n \alpha_s}{8\pi f_{\Pi}} d^{abc} \Phi_8^a G_{\mu\nu}^b \tilde{G}^c_{\mu\nu}
$$

$$
-\frac{Y_1 N_n \sqrt{\alpha \alpha_s}}{4\pi f_{\Pi}} \Phi_8^a G_{\mu\nu}^a (-t_W \tilde{Z}^{\mu\nu} + \tilde{A}^{\mu\nu}), \qquad (A5)
$$

where the symmetric tensor d^{abc} is given by

$$
\{T^a, T^b\} = \frac{1}{3}\delta^{ab} + d^{abc}T^c.
$$
 (A6)

The partial decay widths for the singlet Φ_1 can be obtained from the WZW term between the pNGB Π_A and gauge fields from Eq. [\(A4\),](#page-5-0)

$$
\Gamma[\Phi_1 \to gg] = \frac{N_n^2 \alpha_s^2}{192\pi^3 f_\Pi^2} M_{\Phi_1}^3,
$$

\n
$$
\Gamma[\Phi_1 \to \gamma\gamma] = \frac{3N_n^2 \alpha^2}{128\pi^3 f_\Pi^2} (Y_1^2 - Y_2^2)^2 M_{\Phi_1}^3,
$$

\n
$$
\Gamma[\Phi_1 \to \gamma Z] = \frac{3N_n^2 \alpha^2 t_W^2}{64\pi^3 f_\Pi^2} (Y_1^2 - Y_2^2)^2 M_{\Phi_1}^3
$$

\n
$$
\times \left(1 - \frac{m_Z^2}{M_{\Phi_1}^2}\right)^3,
$$

\n
$$
\Gamma[\Phi_1 \to ZZ] = \frac{3N_n^2 \alpha^2 t_W^4}{128\pi^3 f_\Pi^2} (Y_1^2 - Y_2^2)^2 M_{\Phi_1}^3
$$

\n
$$
\times \left(1 - \frac{4m_Z^2}{M_{\Phi_1}^2}\right)^{3/2},
$$
 (A7)

and also the partial widths of the octet Φ_8 from Eq. [\(A5\)](#page-5-1),

$$
\Gamma[\Phi_8 \to gg] = \frac{5}{4} \frac{M_{\Phi_8}^3}{M_{\Phi_1}^3} \Gamma[\Phi_1 \to gg],
$$

\n
$$
\Gamma[\Phi_8 \to gg] = 24 \frac{\alpha Y_1^2}{\alpha_s} \frac{M_{\Phi_8}^3}{M_{\Phi_1}^3} \Gamma[\Phi_1 \to gg],
$$

\n
$$
\Gamma[\Phi_8 \to gZ] = 24 \frac{\alpha t_W^2 Y_1^2 M_{\Phi_8}^3}{\alpha_s M_{\Phi_1}^3}
$$

\n
$$
\times \left(1 - \frac{m_Z^2}{M_{\Phi_8}^2}\right)^3 \Gamma[\Phi_1 \to gg].
$$
 (A8)

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