

Charmful two-body antitriplet b -baryon decays

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We study the charmful decays of the two-body $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ decays, where \mathcal{B}_b represents the antitriplet of $(\Lambda_b, \Xi_b^0, \Xi_b^-)$, \mathcal{B}_n stands for the baryon octet, and M_c denotes the charmed meson of $D_{(s)}^{(*)}$, η_c and J/ψ . Explicitly, we predict that $\mathcal{B}(\Lambda_b \rightarrow D_s^- p) = (1.8 \pm 0.3) \times 10^{-5}$, which is within the measured upper bound of $\mathcal{B}(\Lambda_b \rightarrow D_s^- p) < 4.8(5.3) \times 10^{-4}$ at 90% (95%) C.L., and reproduce $\mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda) = (3.3 \pm 2.0) \times 10^{-4}$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-) = (5.1 \pm 3.2) \times 10^{-4}$ in agreement with the data. Moreover, we find that $\mathcal{B}(\Lambda_b \rightarrow \Lambda \eta_c) = (1.5 \pm 0.9) \times 10^{-4}$, $\mathcal{B}(\Xi_b^- \rightarrow \Xi^- \eta_c) = (2.4 \pm 1.5) \times 10^{-4}$ and $\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 \eta_c, \Xi^0 J/\psi) = (2.3 \pm 1.4, 4.9 \pm 3.0) \times 10^{-4}$, which are accessible to the experiments at the LHCb.

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I. INTRODUCTION

The two-body decays of $\Lambda_b \rightarrow \Lambda_c^+ K^-$, $\Lambda_c^+ \pi^-$, $\Lambda_c^+ D^-$, and $\Lambda_c^+ D_s^-$ can be viewed through the $\Lambda_b \rightarrow \Lambda_c$ transition along with the recoiled mesons K^- , π^- , D_s^- , and D^- , respectively, such that one may use the factorization ansatz to get the fractions of the branching ratios as

$$\begin{aligned} \mathcal{R}_{K/\pi} &\equiv \frac{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ K^-)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \pi^-)} \simeq \frac{(|V_{us}|f_K)^2}{(|V_{ud}|f_\pi)^2} = 0.073, \\ \mathcal{R}_{D/D_s} &\equiv \frac{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ D^-)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ D_s^-)} \simeq \frac{(|V_{cd}|f_D)^2}{(|V_{cs}|f_{D_s})^2} = 0.034, \end{aligned} \quad (1)$$

which are in agreement with the data, given by [1,2]

$$\begin{aligned} \mathcal{R}_{K/\pi} &= 0.0731 \pm 0.0016 \pm 0.0016, \\ \mathcal{R}_{D/D_s} &= 0.042 \pm 0.003 \pm 0.003. \end{aligned} \quad (2)$$

In the same picture, the measured $\mathcal{B}(\Lambda_b \rightarrow pK^-, p\pi)$ can also be explained [3,4]. In addition, the direct charge-conjugation parity (CP) violating asymmetry of $\Lambda_b \rightarrow pK^{*-}$ is predicted to be as large as 20% [5].

On the other hand, the branching ratios of $\Lambda_b \rightarrow D_s^- p$, $\Lambda_b \rightarrow J/\psi \Lambda$ and $\Xi_b^- \rightarrow J/\psi \Xi^-$ are shown as [4,6]

$$\begin{aligned} \mathcal{B}(\Lambda_b \rightarrow D_s^- p) &= (2.7 \pm 1.4 \pm 0.2 \pm 0.7 \pm 0.1 \pm 0.1) \\ &\times 10^{-4} \quad \text{or} \\ &< 4.8(5.3) \times 10^{-4} \quad \text{at 90\% (95\%) C.L.}, \\ \mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda) &= (3.0 \pm 1.1) \times 10^{-4}, \\ \mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-) &= (2.0 \pm 0.9) \times 10^{-4}, \end{aligned} \quad (3)$$

with $\mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda)$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-)$ converted from the partial observations of $\mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda) f_{\Lambda_b} = (5.8 \pm 0.8) \times 10^{-5}$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-) f_{\Xi_b^-} = (1.02_{-0.21}^{+0.26}) \times 10^{-5}$, where $f_{\Lambda_b} = 0.175 \pm 0.106$ and $f_{\Xi_b} = 0.019 \pm 0.013$ are the fragmentation fractions of the b quark to b baryons of Λ_b and Ξ_b [7], respectively. Nonetheless, for these $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ decays in Eq. (3), the theoretical understanding is still lacking. Since the factorization approach is expected to be reliable in studying the branching ratios of $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$, in this article we systematically analyze the branching ratios for all possible $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ decays, and compare them with the experimental data at the B -factories, as well as the LHCb, where \mathcal{B}_b , \mathcal{B}_n , and M_c correspond to the antitriplet b baryon of $(\Lambda_b, \Xi_b^0, \Xi_b^-)$, baryon octet, and charmed meson, respectively.

II. FORMALISM

As the studies in Refs. [8–14] are based on the factorization approach, the amplitudes for the two-body charmful b -baryon decays are presented in terms of the decaying process of the $\mathcal{B}_b \rightarrow \mathcal{B}_n$ transition with the recoiled charmed meson M_c . From Fig. 1(a), the amplitudes of $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ via the quark-level $b \rightarrow u\bar{c}q$ transition are factorized as

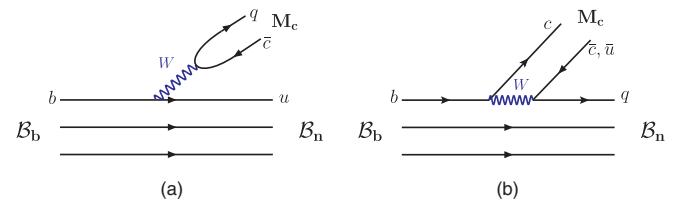


FIG. 1 (color online). Diagrams for two-body charmful $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ decays.

$$\begin{aligned} \mathcal{A}_1(\mathcal{B}_b \rightarrow \mathcal{B}_n M_c) &= \frac{G_F}{\sqrt{2}} V_{ub} V_{cq}^* a_1 \langle M_c | \bar{q} \gamma^\mu (1 - \gamma_5) c | 0 \rangle \\ &\quad \times \langle \mathcal{B}_n | \bar{u} \gamma_\mu (1 - \gamma_5) b | \mathcal{B}_b \rangle, \end{aligned} \quad (4)$$

where G_F is the Fermi constant, $V_{ub,cq}$ are the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements, and the explicit decay modes are

$$\Lambda_b \rightarrow p M_c, \quad \Xi_b^- \rightarrow \Lambda(\Sigma^0) M_c, \quad \Xi_b^0 \rightarrow \Sigma^+ M_c \quad (5)$$

with $q = d(s)$ for $M_c = D^{(*)-}(D_s^{(*)-})$. On the other hand, the amplitudes via the quark-level $b \rightarrow c \bar{u} q$ ($b \rightarrow c \bar{c} q$) transition in Fig. 1(b) can be written as

$$\begin{aligned} \mathcal{A}_2(\mathcal{B}_b \rightarrow \mathcal{B}_n M_c) &= \frac{G_F}{\sqrt{2}} V_{cb} V_{q_1 q}^* a_2 \langle M_c | \bar{c} \gamma^\mu (1 - \gamma_5) q_1 | 0 \rangle \\ &\quad \times \langle \mathcal{B}_n | \bar{q} \gamma_\mu (1 - \gamma_5) b | \mathcal{B}_b \rangle, \end{aligned} \quad (6)$$

with $q_1 = u$ for $M_c = D^{(*)0}$ and $q_1 = c$ for $M_c = \eta_c$ and J/ψ , where the decays of $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ are

$$\begin{aligned} \Lambda_b &\rightarrow n M_c, & \Xi_b^- &\rightarrow \Sigma^- M_c, \\ \Xi_b^0 &\rightarrow \Lambda(\Sigma^0) M_c & \text{for } q_2 = d, \\ \Lambda_b &\rightarrow \Lambda(\Sigma^0) M_c, & \Xi_b^- &\rightarrow \Xi^- M_c, \\ \Xi_b^0 &\rightarrow \Xi^0 M_c & \text{for } q_2 = s. \end{aligned} \quad (7)$$

In this article, we exclude the study of $\Lambda_b \rightarrow n M_c$ due to the elusive neutron in the B -factories. The amplitudes $\mathcal{A}_{1,2}$ via the W -boson exchange diagrams are led to be the color-allowed and color-suppressed processes. The parameters a_1 and a_2 in Eqs. (4) and (6) are presented as [15,16]

$$a_1 = c_1^{\text{eff}} + \frac{c_2^{\text{eff}}}{N_c}, \quad a_2 = c_2^{\text{eff}} + \frac{c_1^{\text{eff}}}{N_c}, \quad (8)$$

with the effective Wilson coefficients $(c_1^{\text{eff}}, c_2^{\text{eff}}) = (1.168, -0.365)$, respectively, where the color number N_c should be taken as a floating number from $2 \rightarrow \infty$ to account for the nonfactorizable effects in the generalized factorization instead of $N_c = 3$. The matrix elements for $P_c = (\eta_c, D)$ and $V_c = J(/\psi, D^*)$ productions read

$$\begin{aligned} \langle P_c | A_\mu^c | 0 \rangle &= -i f_{P_c} q_\mu, \\ \langle V_c | V_\mu^c | 0 \rangle &= m_{V_c} f_{V_c} \varepsilon_\mu^*, \end{aligned} \quad (9)$$

with $V_\mu^c(A_\mu^c) = \bar{q} \gamma^\mu (\gamma_5) c$ or $\bar{c} \gamma^\mu (\gamma_5) q_1$, where q_μ and ε_μ^* are the four-momentum and polarization, respectively. Those of the $\mathcal{B}_b \rightarrow \mathcal{B}_n$ baryon transition in Eq. (4) have the general forms

$$\begin{aligned} \langle \mathcal{B}_n | \bar{q} \gamma_\mu b | \mathcal{B}_b \rangle &= \bar{u}_{\mathcal{B}_n} \left[f_1 \gamma_\mu + \frac{f_2}{m_{\mathcal{B}_b}} i \sigma_{\mu\nu} q^\nu + \frac{f_3}{m_{\mathcal{B}_b}} q_\mu \right] u_{\mathcal{B}_b}, \\ \langle \mathcal{B}_n | \bar{q} \gamma_\mu \gamma_5 b | \mathcal{B}_b \rangle &= \bar{u}_{\mathcal{B}_n} \left[g_1 \gamma_\mu + \frac{g_2}{m_{\mathcal{B}_b}} i \sigma_{\mu\nu} q^\nu + \frac{g_3}{m_{\mathcal{B}_b}} q_\mu \right] \gamma_5 u_{\mathcal{B}_b}, \end{aligned} \quad (10)$$

where f_j (g_j) ($j = 1, 2, 3$) are the form factors. We are able to relate the different $\mathcal{B}_b \rightarrow \mathcal{B}_n$ transition form factors based on the $SU(3)$ flavor and $SU(2)$ spin symmetries, which have been used to connect the spacelike $\mathcal{B}_n \rightarrow \mathcal{B}'_n$ transition form factors in the neutron decays [17], and the timelike $0 \rightarrow \mathcal{B}_n \bar{\mathcal{B}}'_n$ baryonic form factors as well as the $B \rightarrow \mathcal{B}_n \bar{\mathcal{B}}'_n$ transition form factors in the baryonic B decays [18–22]. Specifically, $V_\mu^q = \bar{q} \gamma_\mu b$ and $A_\mu^q = \bar{q} \gamma_\mu \gamma_5 b$ as the two currents in Eq. (10) can be combined as the right-hand chiral current, that is, $J_{\mu,R}^q = (V_\mu^q + A_\mu^q)/2$. Consequently, we have [17]

$$\begin{aligned} \langle \mathcal{B}_{n,\uparrow+\downarrow} | J_{\mu,R}^q | \mathcal{B}_{b,\uparrow+\downarrow} \rangle &= \bar{u}_{\mathcal{B}_n} \left[\gamma_\mu \frac{1 + \gamma_5}{2} G^\uparrow(q^2) + \gamma_\mu \frac{1 - \gamma_5}{2} G^\downarrow(q^2) \right] u_{\mathcal{B}_b}, \end{aligned} \quad (11)$$

where the baryon helicity states $|\mathcal{B}_{n(b),\uparrow+\downarrow}\rangle \equiv |\mathcal{B}_{n(b),\uparrow}\rangle + |\mathcal{B}_{n(b),\downarrow}\rangle$ are regarded as the baryon chiral states $|\mathcal{B}_{n(b),R+L}\rangle$ at the large momentum transfer, while $G^\uparrow(q^2)$ and $G^\downarrow(q^2)$ are the right-hand and left-hand form factors, defined by

$$\begin{aligned} G^\uparrow(q^2) &= e_{\parallel}^\uparrow G_{\parallel}(q^2) + e_{\parallel}^\downarrow G_{\parallel}(q^2), \\ G^\downarrow(q^2) &= e_{\parallel}^\downarrow G_{\parallel}(q^2) + e_{\parallel}^\uparrow G_{\parallel}(q^2), \end{aligned} \quad (12)$$

with the constants $e_{\parallel(\bar{\parallel})}^\uparrow$ and $e_{\parallel(\bar{\parallel})}^\downarrow$ to sum over the chiral charges via the $\mathcal{B}_b \rightarrow \mathcal{B}_n$ transition, given by

$$\begin{aligned} e_{\parallel}^\uparrow &= \langle \mathcal{B}_{n,\uparrow} | \mathbf{Q}_{\parallel} | \mathcal{B}_{b,\uparrow} \rangle, & e_{\bar{\parallel}}^\uparrow &= \langle \mathcal{B}_{n,\uparrow} | \mathbf{Q}_{\bar{\parallel}} | \mathcal{B}_{b,\uparrow} \rangle, \\ e_{\parallel}^\downarrow &= \langle \mathcal{B}_{n,\downarrow} | \mathbf{Q}_{\parallel} | \mathcal{B}_{b,\downarrow} \rangle, & e_{\bar{\parallel}}^\downarrow &= \langle \mathcal{B}_{n,\downarrow} | \mathbf{Q}_{\bar{\parallel}} | \mathcal{B}_{b,\downarrow} \rangle. \end{aligned} \quad (13)$$

Note that $\mathbf{Q}_{\parallel(\bar{\parallel})} = \sum_i \mathcal{Q}_{\parallel(\bar{\parallel})}(i)$ with $i = 1, 2, 3$ as the the chiral charge operators are from $\mathcal{Q}_R^q \equiv J_{0,R}^q = q_R^\dagger b_R$, converting the b quark in $|\mathcal{B}_{b,\uparrow,\downarrow}\rangle$ into the q one, while the converted q quark can be parallel or antiparallel to the \mathcal{B}_b 's helicity, denoted as the subscript \parallel or $\bar{\parallel}$. By comparing Eq. (10) with Eqs. (11)–(13), we obtain

$$\begin{aligned} f_1 &= (e_{\parallel}^\uparrow + e_{\bar{\parallel}}^\downarrow) G_{\parallel} + (e_{\bar{\parallel}}^\uparrow + e_{\parallel}^\downarrow) G_{\bar{\parallel}}, \\ g_1 &= (e_{\parallel}^\uparrow - e_{\bar{\parallel}}^\downarrow) G_{\parallel} + (e_{\bar{\parallel}}^\uparrow - e_{\parallel}^\downarrow) G_{\bar{\parallel}}, \end{aligned} \quad (14)$$

with $f_{2,3} = 0$ and $g_{2,3} = 0$ due to the helicity conservation, as those derived in Refs. [8,10,23]. It is interesting to see that, like the helicity-flip terms, the theoretical calculations

TABLE I. Relations between the transition matrix elements.

$\langle \mathcal{B}_n (\bar{q}b) \mathcal{B}_b \rangle$	$f_1(0) = g_1(0)$
$\langle p (\bar{u}b) \Lambda_b \rangle$	$-\sqrt{\frac{3}{2}}C_{\parallel}$
$\langle \Lambda (\bar{u}b) \Xi_b^- \rangle$	$\frac{1}{2}C_{\parallel}$
$\langle \Sigma^0 (\bar{u}b) \Xi_b^- \rangle$	$-\sqrt{\frac{3}{4}}C_{\parallel}$
$\langle \Sigma^+ (\bar{u}b) \Xi_b^0 \rangle$	$-\sqrt{\frac{3}{2}}C_{\parallel}$
$\langle \Sigma^- (\bar{d}b) \Xi_b^- \rangle$	$\sqrt{\frac{3}{2}}C_{\parallel}$
$\langle \Lambda (\bar{d}b) \Xi_b^0 \rangle$	$-\frac{1}{2}C_{\parallel}$
$\langle \Sigma^0 (\bar{d}b) \Xi_b^0 \rangle$	$\sqrt{\frac{3}{4}}C_{\parallel}$
$\langle \Lambda (\bar{s}b) \Lambda_b \rangle$	C_{\parallel}
$\langle \Sigma^0 (\bar{s}b) \Lambda_b \rangle$	0
$\langle \Xi^- (\bar{s}b) \Xi_b^- \rangle$	$\sqrt{\frac{3}{2}}C_{\parallel}$
$\langle \Xi^0 (\bar{s}b) \Xi_b^0 \rangle$	$-\sqrt{\frac{3}{2}}C_{\parallel}$

from the loop contributions to $f_{2,3}$ ($g_{2,3}$) indeed result in the values being 1 order of magnitude smaller than that of f_1 (g_1), which can be safely neglected. In the double-pole momentum dependences, f_1 and g_1 can be given as [3]

$$f_1(q^2) = \frac{f_1(0)}{(1 - q^2/m_{B_b}^2)^2}, \quad g_1(q^2) = \frac{g_1(0)}{(1 - q^2/m_{B_b}^2)^2}, \quad (15)$$

such that it is reasonable to parametrize the chiral form factors to be $(1 - q^2/m_{B_b}^2)^2 G_{\parallel(\parallel)} = C_{\parallel(\parallel)}$. Subsequently, from

$$\begin{aligned} (e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}, e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}) &= (-\sqrt{3/2}, 0, 0, 0) \quad \text{for } \langle p | J_{\mu,R}^u | \Lambda_b \rangle, \\ (e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}, e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}) &= (1, 0, 0, 0) \quad \text{for } \langle \Lambda | J_{\mu,R}^s | \Lambda_b \rangle, \\ (e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}, e_{\parallel}^{\uparrow}, e_{\parallel}^{\downarrow}) &= (0, 0, 0, 0) \quad \text{for } \langle \Sigma^0 | J_{\mu,R}^s | \Lambda_b \rangle, \end{aligned} \quad (16)$$

we get $f_1(0) = g_1(0) = -\sqrt{3/2}C_{\parallel}$ for $\langle p | \bar{u}\gamma_{\mu}(\gamma_5)b | \Lambda_b \rangle$, $f_1(0) = g_1(0) = C_{\parallel}$ for $\langle \Lambda | \bar{s}\gamma_{\mu}(\gamma_5)b | \Lambda_b \rangle$, and $f_1(0) = g_1(0) = 0$ for $\langle \Sigma^0 | \bar{s}\gamma_{\mu}(\gamma_5)b | \Lambda_b \rangle$, similar to the results based on the heavy-quark and large-energy symmetries in Ref. [23] for the $\Lambda_b \rightarrow (p, \Lambda, \Sigma)$ transitions. When we further extend the study to the antitriplet b baryons, ($\Xi_b^-, \Xi_b^0, \Lambda_b^0$) shown in Table I, we find that the relation of $f_1 = g_1$ is uniquely determined for the antitriplet b -baryon transitions.

III. NUMERICAL RESULTS AND DISCUSSIONS

For the numerical analysis, the CKM matrix elements in the Wolfenstein parametrization taken from the PDG [4] are given by

$$\begin{aligned} (V_{ub}, V_{cb}) &= (A\lambda^3(\rho - i\eta), A\lambda^2), \\ (V_{cd} = -V_{us}, V_{cs} = V_{ud}) &= (-\lambda, 1 - \lambda^2/2), \end{aligned} \quad (17)$$

with $(\lambda, A, \rho, \eta) = (0.225, 0.814, 0.120 \pm 0.022, 0.362 \pm 0.013)$. The meson decay constants are adopted as $(f_{\eta_c}, f_{J/\psi}) = (387 \pm 7, 418 \pm 9)$ MeV [24], $(f_D, f_{D_s}) = (204.6 \pm 5.0, 257.5 \pm 4.6)$ MeV [4], and $(f_{D^*}, f_{D_s^*}) = (252.2 \pm 22.7, 305.5 \pm 27.3)$ MeV [25]. As given in Ref. [3] to explain the branching ratios and CP violating asymmetries of $\Lambda_b \rightarrow p(K^-, \pi^-)$, we have $|\sqrt{3/2}C_{\parallel}| = 0.136 \pm 0.009$ for $\langle p | \bar{u}\gamma_{\mu}(\gamma_5)b | \Lambda_b \rangle$, which is consistent with the value of 0.14 ± 0.03 in the light-cone sum rules [23] and the theoretical calculations in Refs. [8,10]. With $\mathcal{B}(\Lambda_b \rightarrow J/\psi\Lambda)$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-)$ in Eq. (3) as the experimental inputs, we can estimate the nonfactorizable effects by deviating the color number $N_c = 3$ to be between 2 and ∞ , such that we obtain $N_c = 2.15 \pm 0.17$, representing controllable nonfactorizable effects [26] with $(a_1, a_2) = (1.00 \pm 0.01, 0.18 \pm 0.05)$ from Eq. (8). We list the branching ratios of all possible two-body antitriplet b -baryon decays in Tables II–III, where the uncertainties are fitted with those from (ρ, η, N_c) , the decay constants and $|\sqrt{3/2}C_{\parallel}|$.

The decay branching ratios in Table II are given by a_1 with $N_c = (2.15 \pm 0.17, \infty)$ as the theoretical inputs to demonstrate the insensitive nonfactorizable effects. Note that $N_c = 2.15 \pm 0.17$ is fitted from $\mathcal{B}(\Lambda_b \rightarrow J/\psi\Lambda)$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-)$, while $N_c = \infty$ results in $a_1 \simeq c_1^{\text{eff}}$, wildly used in the generalized factorization. As the first measurement for the color-allowed decay mode, the predicted $\mathcal{B}(\Lambda_b \rightarrow D_s^- p) = (1.8 \pm 0.3) \times 10^{-5}$ or $(2.5 \pm 0.4) \times 10^{-5}$ in Table II seems to disagree with the data in Eq. (3). Nonetheless, the predicted numbers driven by a_1 can be reliable as it is insensitive to the nonfactorizable effects, whereas the data with the upper bound have a large uncertainty. Despite the color-allowed modes, the decay branching ratios of $D^{(*)-}$ are found to be 30 times smaller than the $D_s^{(*)-}$ counterparts. This can be simply understood by the relation of $(V_{cd}/V_{cs})^2(f_{D^{(*)}}/f_{D_s^{(*)}})^2 \simeq 0.03$. It is also interesting to note that the vector meson modes are two times as large as their pseudoscalar meson counterparts.

For the decay modes driven by a_2 as shown in Table III, we only list the results with $a_2 = 0.18 \pm 0.05$ ($N_c = 2.15 \pm 0.17$). The reason is that $a_2 \simeq c_2^{\text{eff}} = -0.365$ with $N_c = \infty$ yields $\mathcal{B}(\Lambda_b \rightarrow J/\psi\Lambda) = (1.4 \pm 0.2) \times 10^{-3}$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-) = (2.1 \pm 0.3) \times 10^{-3}$, which are in disagreement with the data in Eq. (3), demonstrating that the decays are

TABLE II. The branching ratios of all possible two-body antitriplet b -baryon decays with a_1 fitted by $N_c = (2.15 \pm 0.17, \infty)$.

$M_c =$	D^-	D^{*-}
$\mathcal{B}(\Lambda_b \rightarrow pM_c)$	$(6.0 \pm 1.0, 8.2 \pm 1.4) \times 10^{-7}$	$(1.2 \pm 0.3, 1.6 \pm 0.4) \times 10^{-6}$
$\mathcal{B}(\Xi_b^- \rightarrow \Lambda M_c)$	$(1.1 \pm 0.2, 1.5 \pm 0.2) \times 10^{-7}$	$(2.2 \pm 0.6, 3.0 \pm 0.8) \times 10^{-7}$
$\mathcal{B}(\Xi_b^- \rightarrow \Sigma^0 M_c)$	$(3.3 \pm 0.5, 4.5 \pm 0.7) \times 10^{-7}$	$(6.6 \pm 1.6, 9.0 \pm 2.2) \times 10^{-7}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Sigma^+ M_c)$	$(6.3 \pm 1.0, 8.6 \pm 1.4) \times 10^{-7}$	$(1.3 \pm 0.3, 1.7 \pm 0.4) \times 10^{-6}$
$M_c =$	D_s^-	D_s^{*-}
$\mathcal{B}(\Lambda_b \rightarrow pM_c)$	$(1.8 \pm 0.3, 2.5 \pm 0.4) \times 10^{-5}$	$(3.5 \pm 0.9, 4.7 \pm 1.2) \times 10^{-5}$
$\mathcal{B}(\Xi_b^- \rightarrow \Lambda M_c)$	$(3.4 \pm 0.5, 4.6 \pm 0.7) \times 10^{-6}$	$(6.4 \pm 1.6, 8.8 \pm 2.2) \times 10^{-6}$
$\mathcal{B}(\Xi_b^- \rightarrow \Sigma^0 M_c)$	$(9.9 \pm 1.5, 13.6 \pm 2.1) \times 10^{-6}$	$(1.9 \pm 0.5, 2.6 \pm 0.6) \times 10^{-5}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Sigma^+ M_c)$	$(1.9 \pm 0.3, 2.6 \pm 0.4) \times 10^{-5}$	$(3.6 \pm 0.9, 4.9 \pm 1.2) \times 10^{-5}$

sensitive to the nonfactorizable effects. From Table III, we see that both $\mathcal{B}(\Lambda_b \rightarrow J/\psi\Lambda)$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-)$ are reproduced to agree with the data in Eq. (3) within errors. Note that $\mathcal{B}(\Lambda_b \rightarrow J/\psi\Lambda)/\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-) \simeq 0.65$ in our calculation results from $(C_{\parallel})^2/(\sqrt{3}/2C_{\parallel})^2 \simeq 0.67$ as the ratio of their form factors in Table I, which is in accordance with the $SU(3)$ flavor and $SU(2)$ spin symmetries. The more precise measurement of this ratio in the future will test the validity of the symmetries. As $\mathcal{B}(\Xi_b^- \rightarrow J/\psi\Xi^-) = O(10^{-4})$, we emphasize that more experimental searches should be done for the two-body Ξ_b decays, while most of the recent observations are from the Λ_b decays. Since

the result of $\mathcal{B}(\Lambda_b \rightarrow \Sigma^0 M_c) = 0$ is from the $SU(3)$ flavor and $SU(2)$ spin symmetries as well as the heavy flavor symmetry, a non-zero measurement will break the symmetries. Through the $b \rightarrow c\bar{c}s$ transition at the quark level, $\mathcal{B}(\Lambda_b \rightarrow \Lambda M_c)$, $\mathcal{B}(\Xi_b^- \rightarrow \Xi^- M_c)$, and $\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 M_c)$ with $M_c = \eta_c$ and J/ψ are all $O(10^{-4})$ as shown in the bottom right of Table II. In contrast, the neutral $D^{(*)0}$ modes via the $b \rightarrow c\bar{c}d$ transition have the branching ratios of order 10^{-6} caused by the suppression of $(V_{cb}V_{cd})^2/(V_{cb}V_{cs})^2 \simeq 0.225^2$. Finally, we remark that $\mathcal{B}(\Xi_b^- \rightarrow \Xi^- M_c) \simeq \mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 M_c)$ is due to the isospin symmetry.

TABLE III. The branching ratios of all possible two-body antitriplet b -baryon decays with a_2 fitted by $N_c = 2.15 \pm 0.17$.

$M_c =$	D^0	D^{*0}
$\mathcal{B}(\Xi_b^- \rightarrow \Sigma^- M_c)$	$(5.3 \pm 3.3) \times 10^{-5}$	$(1.1 \pm 0.7) \times 10^{-4}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Lambda^0 M_c)$	$(8.6 \pm 5.3) \times 10^{-6}$	$(1.7 \pm 1.1) \times 10^{-5}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Sigma^0 M_c)$	$(2.5 \pm 1.6) \times 10^{-5}$	$(5.0 \pm 3.4) \times 10^{-5}$
$\mathcal{B}(\Lambda_b \rightarrow \Lambda M_c)$	$(1.6 \pm 1.0) \times 10^{-6}$	$(3.3 \pm 2.2) \times 10^{-6}$
$\mathcal{B}(\Lambda_b \rightarrow \Sigma^0 M_c)$	0	0
$\mathcal{B}(\Xi_b^- \rightarrow \Xi^- M_c)$	$(2.7 \pm 1.7) \times 10^{-6}$	$(5.5 \pm 3.6) \times 10^{-6}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 M_c)$	$(2.6 \pm 1.6) \times 10^{-6}$	$(5.2 \pm 3.5) \times 10^{-6}$
$M_c =$	η_c	J/ψ
$\mathcal{B}(\Xi_b^- \rightarrow \Sigma^- M_c)$	$(1.4 \pm 0.8) \times 10^{-5}$	$(2.9 \pm 1.8) \times 10^{-5}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Lambda^0 M_c)$	$(2.3 \pm 1.4) \times 10^{-6}$	$(4.7 \pm 2.9) \times 10^{-6}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Sigma^0 M_c)$	$(6.6 \pm 4.1) \times 10^{-6}$	$(1.4 \pm 0.8) \times 10^{-5}$
$\mathcal{B}(\Lambda_b \rightarrow \Lambda M_c)$	$(1.5 \pm 0.9) \times 10^{-4}$	$(3.3 \pm 2.0) \times 10^{-4}$
$\mathcal{B}(\Lambda_b \rightarrow \Sigma^0 M_c)$	0	0
$\mathcal{B}(\Xi_b^- \rightarrow \Xi^- M_c)$	$(2.4 \pm 1.5) \times 10^{-4}$	$(5.1 \pm 3.2) \times 10^{-4}$
$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 M_c)$	$(2.3 \pm 1.4) \times 10^{-4}$	$(4.9 \pm 3.0) \times 10^{-4}$

IV. CONCLUSIONS

In sum, we have studied all possible antitriplet \mathcal{B}_b decays of the two-body charmful $\mathcal{B}_b \rightarrow \mathcal{B}_n M_c$ decays. We have found $\mathcal{B}(\Lambda_b \rightarrow D_s^- p) = (1.8 \pm 0.3) \times 10^{-5}$, which is within the measured upper bound of $\mathcal{B}(\Lambda_b \rightarrow D_s^- p) < 4.8(5.3) \times 10^{-4}$ at 90% (95%) C.L., and reproduced $\mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda) = (3.3 \pm 2.0) \times 10^{-4}$ and $\mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-) = (5.1 \pm 3.2) \times 10^{-4}$ in agreement with the data. Moreover, we have predicted $\mathcal{B}(\Lambda_b \rightarrow \Lambda \eta_c) = (1.5 \pm 0.9) \times 10^{-4}$, $\mathcal{B}(\Xi_b^- \rightarrow \Xi^- \eta_c) = (2.4 \pm 1.5) \times 10^{-4}$, and $\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 \eta_c, \Xi^0 J/\psi) = (2.3 \pm 1.4, 4.9 \pm 3.0) \times 10^{-4}$, which are accessible to the

experiments at the LHCb, while $\mathcal{B}(\Xi_b^- \rightarrow \Xi^- M_c) \simeq \mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 M_c)$ is due to the isospin symmetry.

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- [1] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. D* **89**, 032001 (2014).
- [2] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **112**, 202001 (2014).
- [3] Y. K. Hsiao and C. Q. Geng, *Phys. Rev. D* **91**, 116007 (2015).
- [4] K. A. Olive *et al.* (Particle Data Group Collaboration), *Chin. Phys. C* **38**, 090001 (2014).
- [5] C. Q. Geng, Y. K. Hsiao, and J. N. Ng, *Phys. Rev. Lett.* **98**, 011801 (2007).
- [6] R. Aaij *et al.* (LHCb Collaboration), *J. High Energy Phys.* **04** (2014) 087.
- [7] Y. K. Hsiao, P. Y. Lin, L. W. Luo, and C. Q. Geng, *Phys. Lett. B* **751**, 127 (2015).
- [8] T. Gutsche, M. A. Ivanov, J. G. Körner, V. E. Lyubovitskij, and P. Santorelli, *Phys. Rev. D* **88**, 114018 (2013).
- [9] Y. Liu, X. H. Guo, and C. Wang, *Phys. Rev. D* **91**, 016006 (2015).
- [10] Z. T. Wei, H. W. Ke, and X. Q. Li, *Phys. Rev. D* **80**, 094016 (2009).
- [11] Fayyazuddin and Riazuddin, *Phys. Rev. D* **58**, 014016 (1998).
- [12] C. H. Chou, H. H. Shih, S. C. Lee, and H. n. Li, *Phys. Rev. D* **65**, 074030 (2002).
- [13] M. A. Ivanov, J. G. Körner, V. E. Lyubovitskij, and A. G. Rusetsky, *Phys. Rev. D* **57**, 5632 (1998).
- [14] H. Y. Cheng, *Phys. Rev. D* **56**, 2799 (1997).
- [15] Y. H. Chen, H.-Yang Cheng, B. Tseng, and K.-Chou Yang, *Phys. Rev. D* **60**, 094014 (1999); H. Y. Cheng and K. C. Yang, *ibid.* **62**, 054029 (2000).
- [16] A. Ali, G. Kramer, and C. D. Lu, *Phys. Rev. D* **58**, 094009 (1998).
- [17] G. P. Lepage and S. J. Brodsky, *Phys. Rev. Lett.* **43**, 545 (1979); G. P. Lepage and S. J. Brodsky, *ibid.* **43**, 1625 (1979).
- [18] C. K. Chua, W. S. Hou, and S. Y. Tsai, *Phys. Rev. D* **66**, 054004 (2002).
- [19] C. K. Chua and W. S. Hou, *Eur. Phys. J. C* **29**, 27 (2003).
- [20] C. H. Chen, H. Y. Cheng, C. Q. Geng, and Y. K. Hsiao, *Phys. Rev. D* **78**, 054016 (2008).
- [21] C. Q. Geng and Y. K. Hsiao, *Phys. Rev. D* **85**, 017501 (2012).
- [22] Y. K. Hsiao and C. Q. Geng, *Phys. Rev. D* **91**, 077501 (2015).
- [23] A. Khodjamirian, Ch. Klein, Th. Mannel, and Y.-M. Wang, *J. High Energy Phys.* **09** (2011) 106; T. Mannel and Y. M. Wang, *J. High Energy Phys.* **12** (2011) 067.
- [24] D. Becirevic, G. Duplancić, B. Klajn, B. Melić, and F. Sanfilippo, *Nucl. Phys.* **B883**, 306 (2014).
- [25] W. Lucha, D. Melikhov, and S. Simula, *Phys. Lett. B* **735**, 12 (2014).
- [26] M. Neubert and A. A. Petrov, *Phys. Rev. D* **68**, 014004 (2003).