

# $\eta_c$ production in photon-induced interactions at a fixed target experiment at LHC as a probe of the odderon

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One of the open questions of the strong interaction theory is the existence of the odderon, which is an unambiguous prediction of quantum chromodynamics, but still not confirmed experimentally. An alternative to probe the odderon is the exclusive  $\eta_c$  photoproduction in hadronic collisions. As the Pomeron exchange cannot contribute to this process, its observation would indicate the existence of the odderon. In this paper we estimate the  $\eta_c$  production in photon-induced interactions in hadronic collisions at the AFTER@LHC experiment. We demonstrate that the experimental analysis of this process is feasible in the AFTER@LHC experiment and that the observation of the  $\eta_c$  production in nuclear collisions is an unambiguous signature of the odderon.

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## I. INTRODUCTION

The AFTER@LHC experiment opens a new kinematical regime where several questions related to the description of quantum chromodynamics (QCD) remain without satisfactory answers [1]. One of these open questions is the odderon, which is a natural prediction of the QCD and which determines the hadronic cross section difference between the direct and crossed channel processes at very high energies. (For a review see Ref. [2].) The current experimental evidence for the odderon is rather scarce. A recent study of the data on the differential elastic  $pp$  scattering shows that one needs the odderon to describe the cross sections in the dip region [3] (see also Refs. [4,5]). The difficulties inherent in the description of  $pp$  and  $p\bar{p}$  collisions and the lack of further data have made it impossible to establish the existence of the odderon in these processes beyond a reasonable doubt.

An alternative to probe the odderon is the study of the diffractive photoproduction of pseudoscalar mesons in hadronic collisions [6]. As the real photon emitted by one of the incident hadrons carries negative  $C$  parity, its transformation into a diffractive final state system of positive  $C$  parity requires the  $t$ -channel exchange of an object of negative  $C$  parity. In perturbative QCD, the odderon is a  $C$ -odd ( $C$  being the charge conjugation) compound state of three Reggeized gluons, with evolution described by the Bartels-Kwiecinski-Praszalowicz (BKP) equation [7], which resums terms of the order  $\alpha_s(\alpha_s \log s)^n$  with arbitrary  $n$  in which three gluons in a  $C = -1$  state are exchanged in the  $t$  channel. In contrast, the Pomeron corresponds to a  $C$ -even parity compound state of two  $t$ -channel Reggeized gluons, given by the solution

of the Balitsky-Fadin-Kuraev-Lipatov equation [8]. Consequently, the Pomeron exchange cannot contribute to the production of pseudoscalar mesons and this process can only be mediated by the exchange of an odderon. A particularly promising process is the exclusive  $\eta_c$  photoproduction, since the meson mass provides a hard scale that makes a perturbative calculation possible [9,10].

In what follows we extend the analysis performed in Ref. [6] for the kinematical range probed by the AFTER@LHC experiment. In particular, we estimate the cross sections for the  $\eta_c$  production in photon-induced interactions present in  $pp$ ,  $pA$  and  $AA$  collisions. The basic idea is that in hadron-hadron collisions at large impact parameter ( $b > R_{h_1} + R_{h_2}$ ) and at ultrarelativistic energies the electromagnetic interaction is dominant [11]. In heavy ion collisions, the heavy nuclei give rise to strong electromagnetic fields due to the coherent action of all protons in the nucleus, which can interact with each other. In a similar way, it also occurs when considering ultrarelativistic protons in  $pp$  collisions. The photon stemming from the electromagnetic field of one of the two colliding hadrons can interact with one photon of the other hadron (the two-photon process) or can interact directly with the other hadron (the photon-hadron process). Consequently, the  $\eta_c$  can be produced in photon-hadron ( $\gamma h$ ) and photon-photon ( $\gamma\gamma$ ) interactions, with both processes generating two rapidity gaps in the final state. While the  $\eta_c$  production in  $\gamma h$  interactions represented in Fig. 1 is a direct probe of the odderon, its production in  $\gamma\gamma$  interactions (see Fig. 2) is an important background, which should be estimated in order to separate the signal associated with the odderon.

This paper is organized as follows. In Sec. II we present a brief review of the main concepts and formulas used in the description of  $\gamma\gamma$  and  $\gamma h$  interactions in hadronic collisions and in the exclusive  $\eta_c$  photoproduction, which are required

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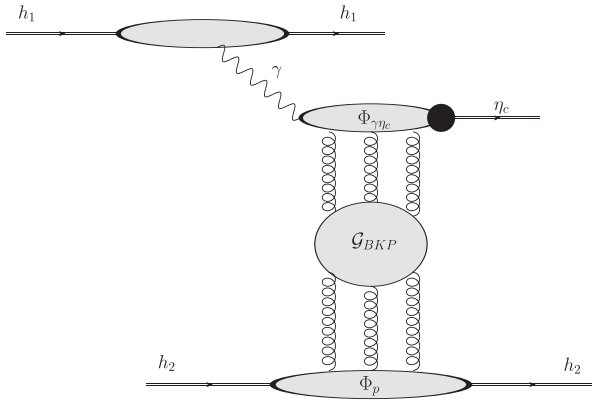


FIG. 1.  $\eta_c$  production in photon-hadron interactions at the AFTER@LHC experiment.

to explain our results, which will be presented in Sec. III. Finally, in Sec. IV we summarize our main conclusions.

## II. PHOTON-INDUCED INTERACTIONS IN HADRONIC COLLIDERS

In hadronic collisions at large impact parameter and at ultrarelativistic energies the photon-induced cross sections for a given process can be factorized in terms of the equivalent flux of photons of the incident hadrons and the photon-photon or photon-target production cross section [11]. The recent experimental results from CDF [12] at Tevatron, STAR [13] and PHENIX [14] at RHIC and ALICE [15,16] and LHCb [17,18] at LHC for photon-induced processes in hadronic collisions have demonstrated that a detailed analysis is feasible and that the data can be used to constrain the description of the hadronic structure at high energies [19] as well as to probe possible scenarios for the physics beyond the Standard Model [20]. These results motivate a detailed analysis of other final states in photon-induced interactions.

Let us initially consider the  $\eta_c$  production in  $\gamma\gamma$  interactions. The cross section for the exclusive  $\eta_c$  production in the two-photon fusion process, Fig. 2, is given by [21]

$$\begin{aligned} \sigma[h_1 h_2 \xrightarrow{(\gamma\gamma)} h_1 \otimes \eta_c \otimes h_2] \\ = \int_0^\infty \frac{d\omega_1}{\omega_1} \int_0^\infty \frac{d\omega_2}{\omega_2} F(\omega_1, \omega_2) \hat{\sigma}_{\gamma\gamma \rightarrow \eta_c}(\omega_1, \omega_2) \end{aligned} \quad (1)$$

where  $\otimes$  represents a rapidity gap in the final state,  $\omega_1$  and  $\omega_2$  the energy of the photons which participate in the hard process and  $\hat{\sigma}_{\gamma\gamma \rightarrow \eta_c}$  is the cross section for the subprocess  $\gamma\gamma \rightarrow \eta_c$ , given by

$$\sigma_{\gamma\gamma \rightarrow \eta_c} = 8\pi^2 (2J + 1) \frac{\Gamma_{\eta_c \rightarrow \gamma\gamma}}{m_{\eta_c}} \delta(4\omega_1 \omega_2 - m_{\eta_c}^2), \quad (2)$$

where  $J$ ,  $m_{\eta_c}$  and  $\Gamma_{\eta_c \rightarrow \gamma\gamma}$  are the spin, the mass and the photon-photon partial decay width of the  $\eta_c$ , respectively,

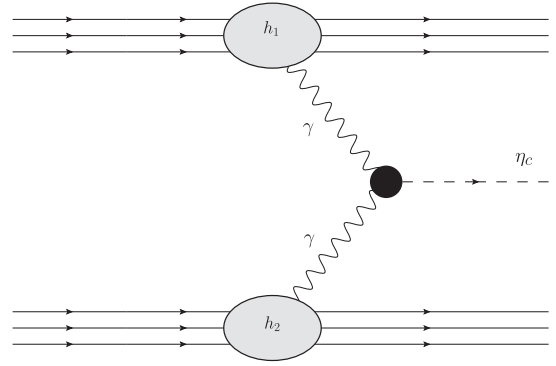


FIG. 2.  $\eta_c$  production in photon-photon interactions at the AFTER@LHC experiment.

and the  $\delta$  function enforces energy conservation. Moreover, the function  $F$  is the folded spectra of the incoming particles (which corresponds to an ‘‘effective luminosity’’ of photons) which we assume to be given by [22]

$$\begin{aligned} F(\omega_1, \omega_2) = 2\pi \int_{R_{h_1}}^\infty db_1 b_1 \int_{R_{h_2}}^\infty db_2 b_2 \int_0^{2\pi} d\phi N_1(\omega_1, b_1) \\ \times N_2(\omega_2, b_2) \Theta(b - R_{h_1} - R_{h_2}) \end{aligned} \quad (3)$$

where  $b_i$  are the impact parameters of the hadrons in relation to the photon interaction point,  $\phi$  is the angle between  $\mathbf{b}_1$  and  $\mathbf{b}_2$ ,  $R_i$  are the projectile radii and  $b^2 = b_1^2 + b_2^2 - 2b_1 b_2 \cos \theta$ . The theta function in Eq. (3) ensures that the hadrons do not overlap [22]. The Weizsäcker-Williams photon spectrum for a given impact parameter is given in terms of the nuclear charge form factor  $F(k_\perp^2)$ , where  $k_\perp$  is the four-momentum of the quasireal photon, as follows [11]:

$$N(\omega, \mathbf{b}) = \frac{\alpha Z^2}{\pi^2 \omega} \left| \int_0^{+\infty} dk_\perp k_\perp^2 \frac{F\left(\frac{(\omega/\gamma)^2 + \vec{b}^2}{(\omega/\gamma)^2 + \vec{b}^2}\right) \cdot J_1(bk_\perp)}{(\omega/\gamma)^2 + \vec{b}^2} \right|^2, \quad (4)$$

where  $J_1$  is the Bessel function of the first kind. For a pointlike nucleus one obtains that [11]

$$N(\omega, \mathbf{b}) = \frac{\alpha_{\text{em}} Z^2}{\pi^2} \left(\frac{\xi}{b}\right)^2 \left\{ K_1^2(\xi) + \frac{1}{\gamma^2} K_0^2(\xi) \right\}, \quad (5)$$

with  $K_{0,1}$  being the modified Bessel function of the second kind,  $\xi = \omega b / \gamma v$ ,  $v$  the velocity of the hadron,  $\gamma$  the Lorentz factor and  $\alpha_{\text{em}}$  the electromagnetic coupling constant. This expression has been derived considering a semiclassical description of the electromagnetic interactions in peripheral collisions, which works very well for heavy ions (see e.g. [21]). For protons, it is more appropriate to obtain the equivalent photon spectrum from its elastic form factors in the dipole approximation

(see e.g. [23]). An alternative is to use Eq. (5) assuming  $R_p = 0.7$  fm for the proton radius, which implies good agreement with the parametrization of the luminosity obtained in [24] for proton-proton collisions (for a more detailed discussion see Ref. [25]).

In the case of  $\eta_c$  production in photon-hadron interactions the total cross section is given by

$$\sigma[h_1 h_2 \xrightarrow{(\gamma h)} h_1 \otimes \eta_c \otimes h_2] = \sum_{i=1,2} \int dY \frac{d\sigma_i}{dY}, \quad (6)$$

where  $d\sigma_i/dY$  is the rapidity distribution for the photon-target interaction induced by the hadron  $h_i$ , which can be expressed as

$$\frac{d\sigma_i}{dY} = \omega n_{\gamma/h_i}(\omega) \cdot \sigma_{\gamma h_j \rightarrow \eta_c h_j}(W_{\gamma h_j}^2) \quad (i \neq j), \quad (7)$$

where  $W_{\gamma h}^2 = 2\omega\sqrt{s_{NN}}$  and  $s_{NN}$  are the c.m. system energy squared of the photon-hadron and hadron-hadron system, respectively. Moreover,  $n_{\gamma/h_i}(\omega)$  is the  $\mathbf{b}$ -integrated photon flux associated with the hadron  $h_i$ , which can be obtained considering the requirement that the photon-induced processes are not accompanied by a hadronic interaction (an ultraperipheral collision). An analytic approximation for the equivalent photon flux of a nucleus can be calculated, which is given by [11]

$$\begin{aligned} n_{\gamma/A}(\omega) &= \int_{b_{\min}} d^2\mathbf{b} N(\omega, \mathbf{b}) \\ &= \frac{2Z^2\alpha_{\text{em}}}{\pi\omega} \left[ \bar{\eta} K_0(\bar{\eta}) K_1(\bar{\eta}) + \frac{\bar{\eta}^2}{2} \mathcal{U}(\bar{\eta}) \right] \end{aligned} \quad (8)$$

where  $\bar{\eta} = \omega b_{\min}/\gamma_L$  (with  $\gamma_L$  being the Lorentz boost of a single beam),  $b_{\min} = R_{h_1} + R_{h_2}$  and  $\mathcal{U}(\bar{\eta}) = K_1^2(\bar{\eta}) - K_0^2(\bar{\eta})$ . On the other hand, for proton-proton collisions, we assume that the photon spectrum of a relativistic proton is given by [26]

$$\begin{aligned} n_{\gamma/p}(\omega) &= \frac{\alpha_{\text{em}}}{2\pi\omega} \left[ 1 + \left( 1 - \frac{2\omega}{\sqrt{s_{NN}}} \right)^2 \right] \\ &\cdot \left( \ln \Omega - \frac{11}{6} + \frac{3}{\Omega} - \frac{3}{2\Omega^2} + \frac{1}{3\Omega^3} \right), \end{aligned} \quad (9)$$

where  $\Omega = 1 + [(0.71 \text{ GeV}^2)/Q_{\min}^2]$  and  $Q_{\min}^2 = \omega^2/[\gamma_L^2(1 - 2\omega/\sqrt{s_{NN}})] \approx (\omega/\gamma_L)^2$ .

The exclusive  $\eta_c$  photoproduction, which is the main input in our calculations [see Eq. (7)] can be obtained using the impact factor representation, proposed by Cheng and Wu [27] many years ago. In this representation, the amplitude for a large- $s$  hard collision process can be factorized in three parts: the two impact factors of the colliding particles and the Green's function for the three interacting Reggeized gluons, which is determined by the

BKP equation and is represented by  $\mathcal{G}_{\text{BKP}}$  hereafter. The differential cross section for the process  $\gamma + h \rightarrow \eta_c + h$  is given by [9]

$$\frac{d\sigma}{dt} = \frac{1}{32\pi} \sum_{i=1,2} |\mathcal{A}^i|^2, \quad (10)$$

where  $\mathcal{A}^i$  is the amplitude for a given transverse polarization  $i$  of the photon, which can be expressed as a convolution of the impact factors for the proton ( $\Phi_p$ ) and for the  $\gamma\eta_c$  transition ( $\Phi_{\gamma\eta_c}^i$ ) with the odderon Green's function:

$$\mathcal{A}^i = \frac{5}{1152} \frac{1}{(2\pi)^8} \langle \Phi_{\gamma\eta_c}^i | \mathcal{G}_{\text{BKP}} | \Phi_p \rangle. \quad (11)$$

Different from  $\Phi_{\gamma\eta_c}^i$ , which can be calculated perturbatively [10], the impact factor  $\Phi_p$  that describes the coupling of the odderon to the proton is nonperturbative and should be modeled. In our calculations we consider the model used in Refs. [9,10]. Moreover, we assume that the odderon Green's function  $\mathcal{G}_{\text{BKP}}$  is described in terms of the solution of the BKP equation [7], with the energy dependence being determined by the odderon intercept  $\alpha_{IO}$ . In particular, we consider the solution obtained by Bartels, Lipatov and Vacca [28] that have found a solution for the BKP equation with intercept  $\alpha_{IO}$  exactly equal to one. For comparison we also consider the solution obtained by Kwiecinski and his collaborators in Ref. [10] (the Czyzewski-Kwiecinski-Motyka-Sadzikowski (CKMS) model hereafter), which has considered a simplified three gluon exchange model for the odderon that implies an energy independent cross section. In our calculations we will use a realistic value for  $\alpha_s (= 0.3)$ .

### III. RESULTS

In what follows we present our predictions for the  $\eta_c$  production in  $\gamma h$  and  $\gamma\gamma$  interactions considering the kinematical range which will be probed by the AFTER@LHC experiment. Basically, we assume  $\sqrt{s_{NN}} = 115/72/72$  GeV for  $pp/Pbp/PbPb$  collisions, which implies that  $\sqrt{s_{\gamma h}} \leq 44/12/9$  GeV, respectively. Similarly, it is possible to obtain that  $\sqrt{s_{\gamma\gamma}} \leq 17/2.0/1.0$  GeV. Consequently, the  $\eta_c$  production in  $\gamma\gamma$  interactions only is present in  $pp$  collisions. In other words, the measurement of the exclusive  $\eta_c$  production in  $Pbp$  and  $PbPb$  collisions can be considered a direct probe of the odderon. Moreover, in our calculations we take into account that the typical rapidity range which is expected to be reachable by the AFTER@LHC experiment is  $-3.0 \leq Y_{c.m.} \leq 0.5$ .

In Table I we present our predictions for the total cross sections. We predict cross sections for the  $\eta_c$  production in  $Pbp$  and  $PbPb$  collisions that are a factor  $\geq 10^4$  larger than the  $pp$  predictions. This enhancement is directly associated with the nuclear photon flux and the nuclear dependence of the photon-hadron cross section. As the photon flux is

proportional to  $Z^2$ , because the electromagnetic field surrounding the ion is very much larger than the proton one due to the coherent action of all the protons in the nucleus, the  $Pbp$  and  $PbPb$  cross sections are amplified by this factor. Moreover, our predictions for the  $\eta_c$  production in  $PbPb$  collisions also are amplified by the mass number  $A$ , since in our calculations for the nuclear case we are assuming in a first approximation that  $\sigma(\gamma A \rightarrow \eta_c A) = A \cdot \sigma(\gamma p \rightarrow \eta_c p)$ . For the exclusive  $\eta_c$  production in  $pp$  collisions we predict values of the order of a fraction of a pb, with the Bartels-Braun-Colferai-Vacca (BBVC) prediction being a factor of  $\approx 6$  larger than the CKMS one. This enhancement is directly associated with the energy dependence present in the BBVC model, which implies that the  $\gamma h$  cross section increases at smaller energies, while the CKMS predicts an energy independent cross section. For the  $\eta_c$  production in  $Pbp$  and  $PbPb$  collisions, we predict cross sections of the order of a nb for the exclusive  $\eta_c$  photoproduction in  $PbPb$  collisions at the AFTER@LHC experiment. Moreover, we predict that the  $Pbp$  cross sections are 2 orders of magnitude smaller than those predicted for  $PbPb$  collisions.

Let us now estimate the background associated with the  $\eta_c$  production in  $\gamma\gamma$  interactions for  $pp$  collisions. Assuming that the photon spectrum for the proton is given by Eq. (5), with  $R_p = 0.7$  fm,  $m_{\eta_c} = 2.983$  GeV and  $\Gamma(\eta_c \rightarrow \gamma\gamma) = 5.0$  keV, we predict that  $\sigma[pp \xrightarrow{(\gamma\gamma)} p \otimes \eta_c \otimes p] = 2.2$  pb, which is a factor  $\gtrsim 8$  larger than the predictions for the  $\eta_c$  production in photon-hadron interactions. As both processes generate two rapidity gaps in the final state, the detection of the gaps is not, in the first analysis, an efficient trigger for the separation of the  $\gamma h$  production of the  $\eta_c$ . An alternative is the reconstruction of the entire event with a cut on the summed transverse momentum of the event [23]. As the typical photon virtualities are very small, the hadron scattering angles are very low. Consequently, we expect that a different transverse momentum distribution of the scattered hadron, with  $\gamma h$  interactions predicting larger  $p_T$  values. In contrast, the background is not present in nuclear collisions, since the maximum  $\gamma\gamma$  center-of-mass energies in  $Pbp$  and  $PbPb$  collisions are smaller than the threshold of production.

Considering the design luminosities at the AFTER@LHC for  $pp$  ( $\mathcal{L}_{pp} = 2 \times 10^4$  pb $^{-1}$  yr $^{-1}$ ),  $Pbp$  ( $\mathcal{L}_{Pbp} = 1.1$  pb $^{-1}$  yr $^{-1}$ ) and  $PbPb$  collisions ( $\mathcal{L}_{PbPb} = 7.0 \times 10^{-3}$  pb $^{-1}$  yr $^{-1}$ ) we can calculate the production rates (see Table I). Although the cross section for the exclusive  $\eta_c$  photoproduction in  $PbPb$  collisions is much larger than in  $pp$  collisions, the event rates are higher in the  $pp$  mode due to its larger luminosity. In particular, we predict that the event rates/year for  $pp$  collisions at  $\sqrt{s} = 115$  GeV should be larger than 1000. On the other

TABLE I. Cross sections (event rates/year) for the exclusive  $\eta_c$  photoproduction in  $pp/Pbp/PbPb$  collisions at the AFTER@LHC experiment.

$h_1 h_2$	CKMS	BBVC
$pp(\sqrt{s} = 115 \text{ GeV})$	0.05 pb (1000.0)	0.30 pb (6000.0)
$Pbp(\sqrt{s} = 72 \text{ GeV})$	28.1 pb (31.0)	356.6 pb (393.0)
$PbPb(\sqrt{s} = 72 \text{ GeV})$	5870.0 pb (41.0)	74366.0 pb (520.0)

hand, for  $Pbp$  and  $PbPb$  collisions at  $\sqrt{s} = 72$  GeV we predict that the event rates/year should be larger than 30. Although smaller than the  $pp$  predictions, the observation of the  $\eta_c$  production in nuclear collisions would clearly indicate the existence of the odderon.

#### IV. SUMMARY

In recent years, the physics of the odderon has become an increasingly active subject of research, from both theoretical and experimental points of view. On the theoretical side, the investigation of the odderon in pQCD has led to the discovery of relations of high energy QCD to the theory of integrable models [29] and two leading solutions of the BKP evolution equation were obtained [28,30], with the intercept being close to or exactly one, depending on the scattering process (see also Ref. [31]). In contrast, on the experimental side, the current evidence for the odderon is very unsatisfactory.

In Ref. [6] we have proposed the study of the exclusive  $\eta_c$  production in hadronic collisions at LHC energies as a probe of the odderon (for other possibilities see Ref. [32]). In this paper we extend that previous analysis for the kinematical region which would be probed by the AFTER@LHC experiment. As the exclusive  $\eta_c$  photoproduction is only possible if the odderon is exchanged between the vector meson and the hadron, the observation of such processes would clearly indicate the existence of the odderon. We have estimated the  $\eta_c$  cross section considering photon-hadron interactions in  $pp/Pbp/PbPb$  collisions. Moreover, the background associated with the  $\eta_c$  production by  $\gamma\gamma$  interactions was calculated. We have the background present only in  $pp$  collisions, which makes the observation of the exclusive  $\eta_c$  production in  $Pbp$  and  $PbPb$  a signature of the odderon. We predict total cross sections of an order of pb (nb) for  $pp(PbPb)$  collisions and large values for the event rates/year, which makes, in principle, the experimental analysis of this process feasible at the AFTER@LHC experiment.

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