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Dark matter in the Higgs triplet model

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The inability to predict neutrino masses and the existence of dark matter are two essential shortcomings of the Standard Model. The Higgs triplet model provides an elegant resolution of neutrino masses via the seesaw mechanism. We show here that introducing vectorlike leptons in the model also provides a resolution to the problem of dark matter. We investigate constraints, including the invisible decay width of the Higgs boson and the electroweak precision variables, and impose restrictions on model parameters. We analyze the effect of the relic density constraint on the mass and Yukawa coupling of dark matter. We also calculate the cross sections for indirect and direct dark matter detection and show our model predictions for the neutrino and muon fluxes from the Sun, and the restrictions they impose on the parameter space. With the addition of vectorlike leptons, the model is completely consistent with dark matter constraints, in addition to improving electroweak precision and doubly charged mass restrictions, which are rendered consistent with present experimental data.

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I. INTRODUCTION

The LHC discovery of the Higgs boson [1] with properties consistent with that of the Standard Model (SM) Higgs, while providing a spectacular experimental confirmation of the SM, continues to raise questions about SM completeness and about scenarios responsible for new physics beyond the SM. In addition, noncollider experimental results confront the SM with two major puzzles: neutrino masses and the existence of dark matter.

The phenomenon of neutrino oscillations shows that at least two neutrinos have nonzero but small masses, located around the sub-eV scale [2]. The fact that the neutrino flavor structure is so different from that of quarks and leptons is a puzzle and may indicate that neutrinos are Majorana particles. Many models have been proposed to explain tiny neutrino masses. The seesaw mechanism, in which right-handed neutrinos are introduced with large Majorana masses [3,4], is perhaps the simplest way to explain tiny neutrino masses. The most direct way for implementation of this mechanism for generating neutrino masses is to enlarge the particle content of the SM by a complex triplet scalar field, vielding the so-called Higgs triplet model (HTM) [5,6]. The neutrino mass problem is resolved at the cost of introducing only this additional Higgs representation, together with its associated vacuum expectation value (VEV), but without extending the symmetry of the model. The triplet scalar field also plays a role in leptogenesis [7].

At the same time, evidence from astrophysics and cosmology indicates that the ordinary baryonic matter is

not dominant in the Universe. Rather, about 25% of the energy density of the Universe is comprised of a nonluminous and nonabsorbing matter, called dark matter (DM). While current observations indicate that most of the matter in the Universe is nonbaryonic dark matter, they do not provide information on what this dark matter consists of. Since the SM, which has been extremely successful in describing all current collider data, does not contain any dark matter candidates, a great deal of effort has gone into providing viable candidates, or alternatives scenarios (models which include a DM candidate naturally). The latter types of models do so at the expense of extra symmetries and a much enriched particle content. For models lacking natural candidates, a common method is to consider the simplest additions to the SM that can account for dark matter. In these models, the SM particle content is extended by a small number of fields, and a new discrete symmetry is introduced to guarantee the stability of the dark matter particle. Several variations can be obtained depending on the number and type of new fields [e.g., a scalar, a fermion, or a vector, a singlet, or a doublet under SU(2), etc.] and on the discrete symmetry imposed $(Z_2, Z_3, ...)$.

In this work, we look at the Higgs triplet model for a resolution to both neutrino masses and dark matter problems. The resolution to neutrino masses, alluded to in the above, is well known [5]. The complex triplet couples to left-handed leptons, yielding Majorana masses for the neutrinos through L = 2 lepton flavor violating terms [6], while also contributing to type II leptogenesis [8]. In addition, extra degrees of freedom that couple to the SM Higgs at tree level ensure cancellation of quadratic divergences to the Higgs mass [9], a mechanism where scalars are favored. Additional support for the model comes from

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the observation that heavy particles with strong couplings to the Higgs field can strengthen the electroweak phase transition, through the entropy release mechanism from both bosons and fermions [10].

Unfortunately, as it stands, the Higgs triplet model lacks a dark matter candidate. Resolutions to this problems were proposed: some with additional Higgs triplets, where the neutral component of the additional (real) Higgs representation can act as a DM candidate [11], another where an *additional* $SU(2)_L$ triplet scalar fields with hypercharge Y = 1 is added [12]. In this work, we investigate the possibility that the DM candidate is provided through the introduction of a complete fourth generation of vectorlike leptons, comprised of $SU(2)_L$ doublets plus charged and neutral $SU(2)_L$ singlets [13]. A simpler extension of the SM with only one fourth generation vectorlike lepton doublet coupling to a triplet Higgs field, which gives Majorana mass to a pseudo-Dirac fourth neutrino, was considered in [14].

Vectorlike pairs of fermions, unlike their chiral counterparts, are able to have mass explicitly through the gaugeinvariant bilinear interaction in the Lagrangian $M_f f^{\dagger} f$. There is no reason why such pairs of vectorlike fermions do not exist, and many theories—such as string theories and D-brane theories—often give rise generically to vectorlike states [15]. Since the masses of the vectorlike fermions are not generated through the Yukawa couplings, the loop contributions involving the Higgs decouple faster than for chiral fermions. Thus the constraints from the current Higgs data, precision electroweak observables, and direct searches are less severe for vectorlike fermions than for chiral fermions.

Originally, there was a great deal of interest in vectorlike leptons as a resolution to preliminary data indicating an enhanced Higgs decay rate to diphotons, while the Higgs production cross section was in agreement with expectations from the SM. The diphoton rate is increased through loops of mixed vectorlike leptons. A vectorlike doublet and a vectorlike singlet allow for both Yukawa couplings and Dirac masses. The resulting mixing leads to a sign flip of the coupling of the lightest lepton to the Higgs field, yielding constructive interference with the SM amplitude for $h \rightarrow \gamma\gamma$.

This does not have to be so in the Higgs triplet model, where contributions from vectorlike leptons can be offset by contributions from charged and doubly charged Higgs bosons. However, new effects of vectorlike leptons can arise. Previous analyses have shown that their presence affects the mass bounds and decay patterns of the doubly charged Higgs boson [16], improving consistency with the present experimental data.

We extend our previous considerations in [16] to explore the possibility that, introducing a new parity symmetry making all new vectorlike leptons odd and prohibiting the mixing with the ordinary SM leptons, the lightest particle which is odd under this symmetry (a singlet neutrino) becomes stable on cosmological time scales and could have properties consistent with its being a candidate for the dark matter of the Universe. Note that in a simple heavy fourth generation extension of the SM, the heavy neutrino does not qualify as dark matter due to its rapid annihilation to SM particles via Z boson exchange [17]. Leptonic dark matter candidates with unsuppressed couplings to the Z boson, such as ordinary fourth generation neutrinos, are also excluded by limits from direct detection [18]. This constraint can be relaxed in the model considered here, as the two singlet neutrinos in the model have no couplings—or very small couplings—to the Z boson.

Suppression of the lightest neutrino couplings to the Zboson can also evade present experimental limits from LEP on masses of new charged and neutral particles [2]. Measurements of the Z boson width restrict the number of active neutrinos to three, which further restricts the mass of the new neutrino to $M_N > 39$ GeV for a Majorana, and $M_N > 45$ GeV for a Dirac neutrino, precluding the viability of a neutrino which couples to the Z boson as a candidate for light dark matter. While, as we will show, we can relax these constraints here, the new states will have an effect on the precision electroweak parameters, which we calculate and use to restrict the parameter space. We then analyze the consequences of the model by requiring consistency with the invisible Higgs width and noncollider experimental data, particularly with direct and indirect dark matter searches. The relic density-an indication of the abundance of dark matter in the early Universe, as measured by the Planck satellite [19]—is one of the most stringent constraints on any model of DM, as well as direct detection experiment searches for spin-independent (SI) or spin-dependent (SD) interactions with target nuclei, which can be detected by nuclear recoil experiments. Indirect detection experiments searches looking for gamma ray excesses measure the annihilation products of DM, and their predictions must also be tested in a model of DM. Finally, ultrahigh energy neutrino experiments measure the neutrino flux and the flavor composition at astrophysical sources. We analyze the predictions for all of these in our model and indicate the constraints on vectorlike neutrino mass and coupling which restrict our parameter space.

Our work is organized as follows. In the next section, Sec. II, we summarize the basic features of the Higgs triplet model with vectorlike leptons. We proceed by examining the electroweak precision constraints in the HTM in Sec. III, where we present a numerical analysis on restrictions coming from the oblique parameters on the masses of the doubly charged Higgs bosons and the relevant Yukawa coupling. We discuss the invisible decay width of the Higgs boson in Sec. IV. Then in Sec. V, we calculate the dark matter relic density and indicate the restrictions it imposes on the mass of the dark matter and on the Yukawa couplings. These restrictions are then

TABLE I. Representations of vectorlike leptons, together with their quantum numbers under $SU(3)_C \times SU(2)_L \times U(1)_Y$.

Name	$\mathcal{L'}_L$	\mathcal{L}''_R	e'_R	e''_L	ν'_R	ν''_L
Quantum number	(1, 2, -1/2)	(1, 2, -1/2)	(1, 1, -1)	(1, 1, -1)	(1,1,0)	(1,1,0)

applied to the evaluation of the spin-dependent and spinindependent interactions in the direct detection of dark matter in Sec. VI, and of the annihilation cross section of dark matter in Sec. VII. We discuss detection of DM at colliders in Sec. VIII, and then investigate the fluxes of muons and neutrinos from the Sun in Sec. IX. We summarize our findings and conclude in Sec. X.

II. THE HIGGS TRIPLET MODEL WITH VECTORLIKE LEPTONS

Here we review briefly the HTM with vectorlike leptons, a more detailed version which has appeared in our previous work [16]. The symmetry group of the HTM is the same as that of the SM, with the particle content enriched by (a) the addition of one triplet scalar field Δ with hypercharge Y = 1, and with VEV v_{Δ} :

$$\Delta = \begin{bmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \frac{1}{\sqrt{2}} (\delta + v_\Delta + i\eta) & -\frac{\Delta^+}{\sqrt{2}} \end{bmatrix}, \quad (2.1)$$

and (b) a vectorlike fourth generation of leptons,¹ to include one $SU(2)_L$ left-handed lepton doublet $L'_L = (\nu'_L, e'_L)$;

right-handed charged and neutral lepton singlets, ν'_R and e'_R ; the mirror right-handed lepton doublet, $L''_R = (\nu''_R, e''_R)$; and left-handed charged and neutral lepton singlets ν''_L and e''_L , as listed in Table I. Note that v_{Δ} is kept small by the seesaw mechanism, which requires generation of small neutrino masses, and by the ρ parameter. In general we can assume, conservatively, $v_{\Delta} \lesssim 5$ GeV [20].

The Lagrangian density for this model contains, in addition to the SM terms, kinetic, Yukawa for ordinary leptons, explicit terms for the vectorlike leptons, and potential terms:

$$\mathcal{L}_{\text{HTM}} = \mathcal{L}_{\text{kin}} + \mathcal{L}_{Y} + \mathcal{L}_{\text{VL}} - V(\Phi, \Delta), \qquad (2.2)$$

where

$$\mathcal{L}_{Y} = -[\bar{L}_{L}^{i}h_{e}^{ij}\Phi e_{R}^{j} + \text{H.c.}] - [h_{ij}\overline{L_{L}^{ic}}i\tau_{2}\Delta L_{L}^{j} + \text{H.c.}] \quad (2.3)$$

are the Yukawa interaction terms for the ordinary leptons, with h_e^{ij} being a 3 × 3 complex matrix and h_{ij} a 3 × 3 complex symmetric Yukawa matrix. Additionally, with the vectorlike family of leptons as defined above,

$$\mathcal{L}_{\rm VL} = -[M_L \bar{L}'_L L''_R + M_E \bar{e}'_R e''_L + M_\nu \bar{\nu}'_R \nu''_L + \frac{1}{2} M'_\nu \bar{\nu}'_R \nu''_R + \frac{1}{2} M''_\nu \bar{\nu}''_L \nu''_L + h'_E (\bar{L}'_L \Phi) e'_R + h''_E (\bar{L}'_R \Phi) e''_L + h'_\nu (\bar{L}'_L \tau \Phi^{\dagger}) \nu'_R + h''_\nu (\bar{L}''_R \tau \Phi^{\dagger}) \nu''_L + h'_{ij} \overline{L_L^{'c}} i \tau_2 \Delta L'_L + h''_{ij} \overline{L_R^{''}} i \tau_2 \Delta L''_R + \lambda^i_E (\bar{L}'_L \Phi) e^i_R + \lambda^i_L (\bar{L}_L^i \Phi) e'_R + \lambda'_{ij} \overline{L_L^{'c}} i \tau_2 \Delta L'_L + \lambda''_{ij} \overline{L_R^{'c}} i \tau_2 \Delta L''_R + \text{H.c.}]$$
(2.4)

is the Yukawa interaction term for vectorlike leptons and their interactions with ordinary leptons, and

$$V(\Phi, \Delta) = m^2 \Phi^{\dagger} \Phi + M^2 \operatorname{Tr}(\Delta^{\dagger} \Delta) + [\mu \Phi^T i \tau_2 \Delta^{\dagger} \Phi + \text{H.c.}] + \lambda_1 (\Phi^{\dagger} \Phi)^2 + \lambda_2 [\operatorname{Tr}(\Delta^{\dagger} \Delta)]^2 + \lambda_3 \operatorname{Tr}[(\Delta^{\dagger} \Delta)^2] + \lambda_4 (\Phi^{\dagger} \Phi) \operatorname{Tr}(\Delta^{\dagger} \Delta) + \lambda_5 \Phi^{\dagger} \Delta \Delta^{\dagger} \Phi$$
(2.5)

is the scalar potential for the SM doublet $\Phi(\langle \Phi \rangle = \frac{v_{\Phi}}{\sqrt{2}})$ and triplet Δ Higgs fields. The triplet and doublet Higgs VEVs are related through $v^2 = v_{\Phi}^2 + 2v_{\Delta}^2 \approx (246 \text{ GeV})^2$. The scalar potential in Eq. (2.5) induces mixing among the physical states for the singly charged, the *CP*-odd, and the *CP*-even neutral scalar sectors, which are always small $\mathcal{O}(v_{\Delta}/v_{\Phi})$ for the first two sectors, but not necessarily so for the latter one,

$$\begin{pmatrix} \varphi \\ \delta \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}, \quad (2.6)$$

where the mixing angle is given in terms of the parameters in $V(\Phi, \Delta)$ as

¹We assume vectorlike quarks to be heavy [2] and decouple them from the spectrum.

$$\tan 2\alpha = \frac{v_{\Delta}}{v_{\Phi}} \frac{2v_{\Phi}^2(\lambda_4 + \lambda_5) - 4(v_{\Phi}^2\mu/\sqrt{2}v_{\Delta})^2}{2v_{\Phi}^2\lambda_1 - (v_{\Phi}^2\mu/\sqrt{2}v_{\Delta})^2 - 2v_{\Delta}^2(\lambda_2 + \lambda_3)}.$$
(2.7)

In our previous work [21], we showed that the Higgs masses and coupling strengths are consistent with choosing h to be the SM-like state at 125 GeV, while the state H is a lighter state, perhaps the state observed at LEP [22].² The masses of the neutral h and H are given by

$$m_h^2 = 2v_{\Phi}^2 \lambda_1 \cos^2 \alpha + \left[(v_{\Phi}^2 \mu / \sqrt{2} v_{\Delta})^2 + 2v_{\Delta}^2 (\lambda_2 + \lambda_3) \right] \sin^2 \alpha + \left[\frac{v_{\Phi}^3 \mu^2}{v_{\Delta}} - v_{\Phi} v_{\Delta} (\lambda_4 + \lambda_5) \right] \sin 2\alpha, \qquad (2.8)$$

$$m_H^2 = 2v_{\Phi}^2 \lambda_1 \sin^2 \alpha + \left[(v_{\Phi}^2 \mu / \sqrt{2} v_{\Delta})^2 + 2v_{\Delta}^2 (\lambda_2 + \lambda_3) \right] \cos^2 \alpha$$
$$- \left[\frac{v_{\Phi}^3 \mu^2}{v_{\Delta}} - v_{\Phi} v_{\Delta} (\lambda_4 + \lambda_5) \right] \sin 2\alpha.$$
(2.9)

The expressions relating the λ_1 - λ_5 parameters to the Higgs masses can be found in [21]. In particular, the doubly charged Higgs boson mass is

$$m_{H^{++}}^2 = \frac{v_{\Phi}^2 \mu}{\sqrt{2} v_{\Delta}} - v_{\Delta}^2 \lambda_3 - \frac{\lambda_5}{2} v_{\Phi}^2 \simeq \left(\frac{\mu}{\sqrt{2} v_{\Delta}} - \frac{\lambda_5}{2}\right) v_{\Phi}^2,$$
(2.10)

where we used $v_{\Delta} \ll v_{\Phi}$. As we choose $v_{\Delta} = 1$ GeV for consistency with the value of the ρ parameter, the doubly charged mass is approximately $m_{H^{++}} \simeq (\mu - \lambda_5/\sqrt{2})^{1/2}$ (207 GeV). The coupling λ_5 is expected to be ≤ 1 and for light doubly charged masses, the μ parameter is small,³ $\mu \sim v_{\Delta} \sim \mathcal{O}(\text{GeV})$.

New symmetries can be introduced to restrict the interactions of the vector leptons. For instance, we can impose (i) a symmetry under which all of the new SU(2) singlet fields are odd while the new SU(2) doublets are even, which forces all Yukawa couplings involving new

leptons to vanish, $h'_E = h''_E = h'_\nu = h''_\nu = h''_{ii} = h''_{ii} = 0$, and the vector lepton masses arise only from explicit terms in the Lagrangian [13], and/or (ii) impose a new parity symmetry which disallows mixing between the ordinary leptons and the new lepton fields, under which all of the mirror fields are odd, while the others are even [23], such that $\lambda^i_E = \lambda^i_L = \lambda'_{ij} = \lambda'_{ij} = \lambda''_{ij} = 0$. The latter are important for light vectorlike leptons, as this scenario would satisfy restrictions from lepton-flavor-violating decays, which otherwise would either force the new leptons to be very heavy, $\sim 10-100$ TeV, or reduce the branching ratio for the Higgs into dileptons to 30%-40% of the SM prediction. In addition, if all vectorlike leptons are odd under this symmetry, the lightest particle can become stable and act as all, or part of, the dark matter in the Universe. Thus the assumption (ii) has all of the attractive features we like for this analysis and we adopt it here, while allowing $h'_{E}, h''_{E}, h'_{\nu}, h''_{\nu}, h''_{\mu}, h''_{\mu} \neq 0$.

As we concentrate on the possibility that the lightest neutral component of the new vectorlike leptons is a dark matter candidate, we are primarily interested in light states. The 2×2 mass matrix \mathcal{M}_E for the charged sector is defined as [13,16]

$$(\bar{e}'_L \bar{e}''_L)(\mathcal{M}_E) \begin{pmatrix} e'_R \\ e''_R \end{pmatrix}$$
, with $\mathcal{M}_E = \begin{pmatrix} m'_E & M_L \\ M_E & m''_E \end{pmatrix}$,
(2.11)

with $m'_E = h'_E v_{\Phi}/\sqrt{2}$ and $m''_E = h''_E v_{\Phi}/\sqrt{2}$, from the Lagrangian equation (2.4). The mass matrix can be diagonalized by two unitary matrices, U^L and U^R , as follows:

$$U^{L\dagger}\mathcal{M}_E U^R = \begin{pmatrix} M_{E_1} & 0\\ 0 & M_{E_2} \end{pmatrix}.$$
 (2.12)

The mass eigenvalues are (by convention the order is $M_{E_1} > M_{E_2}$)

$$M_{E_1,E_2}^2 = \frac{1}{2} \left[(M_L^2 + m_E'^2 + M_E^2 + m_E''^2) \pm \sqrt{(M_L^2 + m_E'^2 - M_E^2 - m_E''^2)^2 + 4(m_E''M_L + m_E'M_E)^2} \right],$$
(2.13)

while in the neutral sector the mass matrix is

$$\frac{1}{2} (\bar{\nu_L'} \, \bar{\nu_R''} \, \bar{\nu_L''}) (\mathcal{M}_{\nu}) \begin{pmatrix} \nu_L'^c \\ \nu_R' \\ \nu_R'' \\ \nu_L''' \end{pmatrix}, \quad \text{with} \quad \mathcal{M}_{\nu} = \begin{pmatrix} 0 & m_{\nu}' & M_L & 0 \\ m_{\nu}' & M_{\nu}' & 0 & M_{\nu} \\ M_L & 0 & 0 & m_{\nu}'' \\ 0 & M_{\nu} & m_{\nu}'' & M_{\nu}'' \end{pmatrix},$$
(2.14)

²This scenario was imposed by the requirement of an enhanced diphoton signal for the Higgs of mass 125 GeV, so it can be relaxed here.

³Specifically, for our parameter space, $\mu = 0.2$ GeV and $\lambda_5 < 0$.

with $m'_{\nu} = h'_{\nu} v_{\Phi} / \sqrt{2}$ and $m''_{\nu} = h''_{\nu} v_{\Phi} / \sqrt{2}$. This mass matrix can be diagonalized by a unitary matrix V:

$$V^{\dagger} \mathcal{M}_{\nu} V = \begin{pmatrix} M_{\nu_{1}} & 0 & 0 & 0\\ 0 & M_{\nu_{2}} & 0 & 0\\ 0 & 0 & M_{\nu_{3}} & 0\\ 0 & 0 & 0 & M_{\nu_{4}} \end{pmatrix}.$$
 (2.15)

In the limit where the explicit mass terms M_L , M_E , and M_{ν} in the interaction Lagrangian vanish, after electroweak symmetry breaking there are two charged leptons with masses m'_E and m''_E , and four neutrinos with masses

$$M_{\nu_{1,2}} = \sqrt{\frac{M_{\nu}^{\prime 2}}{4} + m_{\nu}^{\prime 2}} \pm \frac{M_{\nu}^{\prime}}{2}$$
(2.16)

$$M_{\nu_{3,4}} = \sqrt{\frac{M_{\nu}^{\prime\prime 2}}{4} + m_{\nu}^{\prime\prime 2}} \pm \frac{M_{\nu}^{\prime\prime}}{2}.$$
 (2.17)

The lightest of these eigenvalues will be the dark matter candidate and, as it is odd under the additional parity symmetry (ii), it is stable. For the vanishing h'_{ν} , h''_{ν} Yukawa couplings, the two singlet vectorlike neutrinos have vanishing couplings with the Z boson. Lifting the Yukawa couplings slightly from 0 allows mixing between the singlet neutrinos and the neutral components of the doublet vectorlike leptons, inducing a (small) coupling to the Z boson. For simplicity, we adopt the scenario in [13] where $h'_{\nu} \neq 0$ but $h''_{\nu} = 0$, as well as setting the explicit neutrino mass in the Lagrangian as $M_{\nu} = 0$. This scenario is sufficient to provide a single DM candidate and a single Yukawa coupling, and it is transparent enough to yield consequences. It corresponds to one neutrino state which does not mix and is sterile [the mirror $SU(2)_L$ doublet ν''_L , while the remaining neutral sector consists of three neutrinos which mix, with the mixing matrix in the $(\nu_L^{\prime c}, \nu_R^{\prime}, \nu_R^{\prime \prime})$ basis given by

$$\mathcal{M}_{3\nu} = \begin{pmatrix} 0 & m'_{\nu} & M_L \\ m'_{\nu} & M'_{\nu} & 0 \\ M_L & 0 & 0 \end{pmatrix}.$$
 (2.18)

The Yukawa coupling h'_{ν} must remain small to ensure smallness of the couplings to the Z boson. In the limit $h'_{\nu} = 0$, the matrix has two degenerate eigenvalues of mass M_L , predominantly $SU(2)_L$ doublets, and one state with mass M'_{ν} and predominantly singlet. For $h'_{\nu} \neq 0$, these three states mix, generating a small mixing coupling to the Z boson. The lightest neutrino state M_{ν_1} emerges as being dominantly ν'_R and is the dark matter candidate. For the charged lepton sector, we take $M_L = 205$ GeV and $M_E = 300$ GeV and $h'_E =$ $h''_E = 0.8$ [13]. In this case the lightest charged lepton will be $M_{E_2} \sim 108$ GeV—close to the LEP limit, $M_E > 102.6$ GeV [2]—which imposes an upper limit on the mass of the dark matter candidate, $M_{DM} \equiv M_{\nu_1} < M_{E_2}$.

Next, we analyze the effects of the new states on electroweak precision parameters in the HTM and, consequently, the restrictions imposed on its parameter space.

III. VECTORLIKE LEPTON CONTRIBUTIONS TO THE S and T PARAMETERS

Adding new particles to the model spectrum affects quantum corrections on the propagators of W and Z bosons. The corrections are parametrized by two oblique parameters, S and T⁴, which encapsulate the model restrictions coming from electroweak precision data. For a Higgs state with mass $m_h = 125$ GeV, the allowed ranges are [20]

$$\Delta S = S - S_{\rm SM} = 0.05 \pm 0.09,$$

$$\Delta T = T - T_{\rm SM} = 0.08 \pm 0.07,$$
 (3.1)

with errors correlated by a factor of 0.88. The explicit expressions for the *S*, *T*, and *U* parameters for the HTM are given in [16]. The addition of vectorlike leptons modifies these by the following contributions. For the *S* parameter [13],

$$S = \frac{1}{\pi} \left\{ \sum_{j,k=1}^{2} (|U_{1j}^{L}|^{2} |U_{1k}^{L}|^{2} + |U_{2j}^{R}|^{2} |U_{2k}^{R}|^{2}) b_{2}(M_{E_{j}}, M_{E_{k}}, 0) + \sum_{j,k=1}^{2} \operatorname{Re}(U_{1j}^{L} U_{1k}^{L\star} U_{2j}^{R\star} U_{2k}^{R}) f_{3}(M_{E_{j}}, M_{E_{k}}) \right. \\ \left. + \sum_{j,k=1}^{3} (|V_{1j}|^{2} |V_{1k}|^{2} + |V_{3j}|^{2} |V_{3k}|^{2}) b_{2}(M_{\nu_{j}}, M_{\nu_{k}}, 0) + \sum_{j,k=1}^{3} \operatorname{Re}(V_{1j} V_{1k}^{\star} V_{3j} V_{3k}^{\star}) f_{3}(M_{\nu_{j}}, M_{\nu_{k}}) \right. \\ \left. - 2 \sum_{j=1}^{2} (|U_{1j}^{L}|^{2} + |U_{2j}^{R}|^{2}) b_{2}(M_{E_{j}}, M_{E_{j}}, 0) + \frac{1}{3} \right\},$$

$$(3.2)$$

while the oblique correction parameter T for vectorlike leptons is [13]

⁴We set U = 0.

$$T = \frac{1}{4\pi s_W^2 c_W^2 M_Z^2} \left\{ -2 \sum_{j=1}^2 \sum_{k=1}^3 (|U_{1j}^L|^2 |V_{1k}|^2 + |U_{2j}^R|^2 |V_{3k}|^2) b_3(M_{\nu_k}, M_{E_j}, 0) \right. \\ \left. + 2 \sum_{j=1}^2 \sum_{k=1}^3 \operatorname{Re}(U_{1j}^L U_{2j}^{R\star} V_{1k} V_{3k}^\star) M_{E_j} M_{\nu_k} b_0(M_{E_j}, M_{\nu_k}, 0) \right. \\ \left. + \sum_{j,k=1}^3 (|V_{1j}|^2 |V_{1k}|^2 + |V_{3j}|^2 |V_{3k}|^2) b_3(M_{\nu_j} M_{\nu_k}, 0) \right. \\ \left. - \sum_{j,k=1}^3 \operatorname{Re}(V_{1j} V_{1k}^\star V_{3j} V_{3k}^\star) M_{\nu_j} M_{\nu_k} b_0(M_{\nu_j}, M_{\nu_k}, 0) \right. \\ \left. + (|U_{11}^L|^4 + |U_{21}^R|^4) M_{E_1}^2 b_1(M_{E_1}, M_{E_1}, 0) + (|U_{12}^L|^4 + |U_{22}^R|^4) M_{E_2}^2 b_1(M_{E_2}, M_{E_2}, 0) \right. \\ \left. + (2|U_{11}^L|^2 |U_{21}^L|^2 + 2|U_{12}^R|^2 |U_{22}^R|^2) b_3(M_{E_1}, M_{E_2}, 0) \right] \right\},$$

$$(3.3)$$

where the Passarino-Veltmann functions are

$$b_0(M_1, M_2, q^2) = \int_0^1 \log\left(\frac{\Delta}{\Lambda^2}\right) dx, \qquad (3.4)$$

$$b_1(M_1, M_2, q^2) = \int_0^1 x \log\left(\frac{\Delta}{\Lambda^2}\right) dx, \qquad (3.5)$$

$$b_2(M_1, M_2, q^2) = \int_0^1 x(1-x) \log\left(\frac{\Delta}{\Lambda^2}\right) dx$$

= $b_2(M_2, M_1, q^2),$ (3.6)

$$b_3(M_1, M_2, 0) = \frac{M_2^2 b_1(M_1, M_2, 0) + M_1^2 b_1(M_2, M_1, 0)}{2},$$
(3.7)

$$f_3(M_1, M_2) = M_1 M_2 \frac{M_2^4 - M_1^4 + 2M_1^2 M_2^2 \log(\frac{M_1^2}{M_2^2})}{2(M_1^2 - M_2^2)^3}.$$
 (3.8)

We defined $\Delta = M_2^2 x + M_1^2(1-x) - x(1-x)q^2$ and, in the above, Λ^2 is an arbitrary regularization scale that will not affect physical observables. The function $f_3(M_1, M_2) = -1/6$ remains well defined in the limit $M_2 \rightarrow M_1$. As in the HTM without vectorlike leptons, the *S* parameter does not impose any restrictions on the parameter space of the model, while the *T* parameter is very restrictive. The reason is that *T* depends quadratically on mass differences, while *S* depends only logarithmically.

We proceed to analyze restrictions on the relevant masses and couplings in the model coming from the *T* parameter. In Fig. 1 we show the effects on the *T* parameter as a contour in a $m_{H^{\pm\pm}} - \sin \alpha$ plane (with $\sin \alpha$ being the mixing angle in the neutral Higgs sector) for two values of dark matter masses, $M_{DM} = 30$ GeV and $M_{DM} = 50$ GeV. The allowed values for this parameter, -0.2 < ΔT < 0.4, are given in the code bars (colored contours in the figure). The maximum doubly charged mass values allowed are $m_{H^{\pm\pm}} \sim (280-290)$ GeV for dark matter masses in the 24–30 and 70–90 GeV regions, and approximately 250–270 GeV for dark matter masses in the 30–70 and 90–103 GeV ranges. We have selected the particular values for $M_{DM} = 30$ GeV and $h'_{\nu} = 0.65$ (left panel) and $M_{DM} = 50$ GeV and $h'_{\nu} = 0.28$ (right panel) to belong to the parameter space where the relic density is within experimental bounds, as explained in detail in Sec. V. As the figure indicates, the *T* parameter depends only slightly on sin α , but it is extremely sensitive to the mass of the doubly charged Higgs boson.

In Fig. 2 we show the variation of the T parameter as a contour in an $m_{H^{\pm\pm}} - h'_{\nu}$ plane (left panel) and $h'_{\nu} - \sin \alpha$ (middle and right panels). For the left panel, we chose an illustrative example with $M_{DM} = 30$ GeV and $\sin \alpha = 0.5$; the T parameter does not depend sensitively on varying these, but again it is very sensitive to the mass of the doubly charged Higgs boson, as shown in the middle and right side panels, where increasing the value of $m_{H^{\pm\pm}}$ from 240 to 260 GeV places significant restrictions on the T parameter. Increasing the mass of the doubly charged Higgs boson and decreasing $\sin \alpha$ (the mixing angle) impose restrictions on h'_{ν} (the vectorlike neutrino Yukawa coupling) from the T parameter. Note that the T parameter is not sensitive to the mass of the dark matter candidate and it affects it only indirectly, through the restrictions on the Yukawa couplings.

IV. INVISIBLE DECAY WIDTH OF THE HIGGS BOSON

The existence of the vectorlike neutrino ν_1 as a dark matter candidate will have an effect on the branching ratio



FIG. 1 (color online). Contour graphs showing the contribution to the *T* parameter in the HTM (as given in the code bars) with vectorlike leptons, as a function of the doubly charged Higgs mass $m_{H^{\pm\pm}}$ and the mixing angle sin α , for fixed values of the neutrino Yukawa coupling h'_{ν} . We take (left panel) $M_{DM} = 30$ GeV, $h'_{\nu} = 0.65$, (right panel) $M_{DM} = 50$ GeV, $h'_{\nu} = 0.28$. The allowed range of the T parameter is $-0.2 < \Delta T < 0.4$. The white region represents the parameter region ruled out by the constraints.

of the Higgs boson, if $m_h \ge 2M_{\nu_1}$. Given that ν_1 is stable, the decays $h \to \nu_1 \nu_1, h \to \nu_1 \bar{\nu}_1$ will contribute to the invisible Higgs branching ratio, which is constrained by combined CMS and ATLAS measurements to be $BR_{inv} <$ 58% for a SM Higgs with a mass of 125 GeV [24], and more stringently by global fits to be BR_{inv} of 29% with 95% C.L. [25].

In the Higgs triplet model, the tree-level decay width of the Higgs boson into vectorlike neutrinos is [21,26]

where

$$C^{h}_{\nu_{1}\bar{\nu_{1}}} = \sqrt{2}h'_{\nu}Re(V_{11}V_{21}) \tag{4.2}$$

is the Higgs coupling to the lightest vectorlike neutrino (ν_1) . In addition, the component from the neutral triplet Higgs field violates the lepton number and can decay into two neutrinos as



FIG. 2 (color online). Contour graphs showing the contribution to the *T* parameter in the HTM with vectorlike leptons (values as given in the code bars, within the allowed range $-0.2 < \Delta T < 0.4$) as a function of the parameters of the model. In the left panel, we show the combined dependence on h'_{ν} and $m_{H^{\pm\pm}}$ (for $M_{DM} = 30$ GeV and $\sin \alpha = 0.5$); in the middle (right) panel, the dependence on h'_{ν} and $\sin \alpha$ for $M_{DM} = 50$ GeV and $m_{H^{\pm\pm}} = 240$ GeV ($m_{H^{\pm\pm}} = 260$ GeV). The white region represents the parameter region ruled out by the constraints.



FIG. 3 (color online). Contour graphs showing the invisible branching ratio of the Higgs boson (BR_{inv}) in the HTM with vectorlike leptons, as functions of the dark matter mass $M_{DM} = M_{\nu_1}$ (GeV) and the neutrino Yukawa coupling h'_{ν} , for $h'_{\nu_1\nu_1} = 0.01$. We compare our results to the upper limit of $BR_{inv} = 29\%$ from global fits to the ATLAS and CMS data [25] and we chose sin $\alpha = 0.1$ (left panel), sin $\alpha = 0.5$ (middle panel), and sin $\alpha = 0.8$ (right panel). If the mass of the DM neutrino is in the white region, it does not contribute to the Higgs invisible decay width.

where $h'_{\nu_1\nu_1}$ is the triplet coupling constant from Eq. (2.4). The invisible branching ratio of the Higgs boson is defined as

$$BR_{\rm inv} = \frac{[\Gamma(h \to \nu_1 \bar{\nu_1})]_{HTM} + [\Gamma(h \to \nu_1 \nu_1)]_{HTM}}{[\Gamma(h \to \nu_1 \bar{\nu_1})]_{HTM} + [\Gamma(h \to \nu_1 \nu_1)]_{HTM} + [\Gamma(h)]_{HTM}},$$

$$(4.4)$$

where $[\Gamma(h)]_{HTM}$ is the total Higgs decay width in the HTM without vectorlike leptons.

In Fig. 3, we show the invisible branching ratio of the Higgs boson (BR_{inv}) in the HTM with vectorlike leptons as a contour plot in an $M_{DM} - h'_{\nu}$ plane for triplet Yukawa coupling $h'_{\nu_1\nu_1} = 0.01$. We compare the calculation with the upper limit on BR_{inv} derived from global fits to the ATLAS and CMS data [25].⁵ As expected, the region restricted is only for $M_{DM} < m_h/2$, where the Higgs can decay to pairs of dark matter with a sizable width. The left panel depicts the invisible width for the mixing angle in the neutral *CP*-even Higgs sector, $\sin \alpha = 0.1$, the middle panel for $\sin \alpha = 0.5$, and the right panel for $\sin \alpha = 0.8$. The figures show that increasing the Yukawa coupling (h'_{μ}) results in an increase of the invisible branching ratio of the Higgs boson (BR_{inv}) as the decay into DM is enhanced, while decreasing $\sin \alpha$ imposes more restrictions on h'_{ν} in order to get the correct BR_{inv} , indicating that both the doublet and the triplet Higgs components play an important role in the invisible decay.

V. DARK MATTER RELIC DENSITY

Global fits to a number of cosmological data (cosmic microwave background, large scale structure, and type Ia supernovae) determine very precisely the amount of nonbaryonic DM in the energy matter of the Universe at $\Omega_{DM}h^2 = 0.1123 \pm 0.0035$ [27], where Ω_{DM} is the energy density of the DM with respect to the critical energy density of the Universe and *h* is the reduced Hubble parameter. Any analysis of DM must correctly replicate this value.

To this end, we used CalcHEP [28] to implement the Lagrangian of the HTM with vectorlike leptons into micrOMEGAs [29], which we used to calculate the relic density ($\Omega_{DM}h^2$), spin-dependent cross section (σ^{SD}), spin-independent cross section (σ^{SD}), annihilation cross section ($\langle \sigma v \rangle$), and the flux of neutrino and muon predicted by the model. For the purpose of comparison with the data, we consider the 2σ allowed range of relic density: 0.1144 $\leq \Omega_{DM}h^2 \leq 0.1252$, as constrained by WMAP [27] and Planck [19].

In Fig. 4, we present the allowed range of the relic density of dark matter as a function of the dark matter mass M_{DM} (GeV) and the Yukawa coupling h'_{ν} for two different values of the mixing angle, $\sin \alpha = 0$ (left panel) and $\sin \alpha = 0.8$ (right panel). Because of resonant annihilation into the Z bosons or Higgs boson h, respectively, we can see two dips at $M_{DM} \sim 45$ GeV and $M_{DM} \sim 62$ GeV. For a fixed Yukawa coupling (h'_{ν}) the cross section becomes enhanced at the Z pole and similarly at the Higgs pole, with a dominant decay into quark/antiquark. As the dark matter relic density is inversely proportional to the annihilation cross section, the relic density decreases in these regions. Thus, in order to produce the correct dark matter relic density, we need to decrease the value of Yukawa coupling h'_{ν} to compensate for the effects of the Z and h resonances,

⁵These global fits, though more restrictive, are completely consistent with our analyses and do not restrict the parameter space unnecessarily.



FIG. 4 (color online). Contour graphs showing the correct relic density of dark matter, as a function of the dark matter mass M_{DM} (in GeV) and the neutrino Yukawa coupling h'_{ν} in the HTM with vectorlike leptons, for $\sin \alpha = 0$ (left panel) and $\sin \alpha = 0.8$ (right panel). We impose the restriction $0.1144 \le \Omega_{DM}h^2 \le 0.1252$. The relic density is insensitive to the doubly charged Higgs boson mass, chosen here to be 240 GeV.

which produces the two dips at $M_{DM} = M_Z/2$ and $M_{DM} = m_h/2$. Above $M_{DM} = 80$ GeV, annihilation into the W^+W^- pairs (and later also the Z bosons) becomes kinematically accessible. Finally, the relic density becomes dramatically suppressed for $M_{DM} \sim 100$ GeV due to coannihilation with the lightest charged vectorlike lepton [13,26]. The effect of the Higgs resonance at $M_{DM} \sim$ 62 GeV is slightly more pronounced for $\sin \alpha = 0.8$ than for $\sin \alpha = 0$ (this is the effect of increasing the triplet component contribution) and, above $M_{DM} = 80$ GeV for $\sin \alpha = 0.8$, the relic abundance decrease is slightly more pronounced than in the case with $\sin \alpha = 0$, but the changes are small. Overall, the graph for $\sin \alpha = 0.8$ shows no marked difference from the one with $\sin \alpha = 0$. The results shown are for $m_{H^{\pm\pm}} = 240$ GeV. We calculated relic density for different values of the doubly charged Higgs boson mass and found that it is insensitive to variations in this parameter. Relic density constraints restrict the dark matter mass to be heavier than 23 and lighter than 103 GeV in our model, independent of any other parameters, such as Yukawa couplings or mixing angles.

VI. DIRECT DETECTION

Dark matter is spread over the whole Universe. This provides the opportunity to detect it as it passes through and scatters off normal matter (neutrons or protons), producing detectable signals. Though direct detection is the most straightforward method of detecting DM, such events are very rare and the deposited energies very small; thus, direct detection requires very sensitive detectors with highly accurate background rejection. The expected signals depend on the nature of the DM. For vectorlike neutrinos, annihilation through the Higgs or Z boson exchange is expected to yield significant rates for direct detection. The interaction of DM with nuclear matter can be classified as elastic or inelastic, and as spin dependent or spin independent.

In elastic scattering the DM interacts with the nucleus as a whole, causing the nucleus to recoil, while in inelastic scattering some of the energy goes into recoil and some is used to excite the nucleus to a higher energy state, from which it decays by emitting a photon. The dark matter detection experiments (DAMA/LIBRA [30], CoGeNT [31], and CRESST-II [32]) have reported signals consistent with a light DM candidate and with an elastic cross section with nucleons of $O(10^{-41}-10^{-40} \text{ cm}^2)$.

In spin-dependent (axial vector) scattering, the DM spin couples with the spin of the nucleon, while in spinindependent (scalar) scattering, the cross section does not depend on spin, and thus it is larger for larger nuclei because of the coherence of DM interacting with the nucleus as a whole. We analyze the predictions of our model for the spin-dependent and spin-independent cross sections in turn, and compare them with the experimental predictions.

In Fig. 5, in the upper panels, we present the SD cross section of dark matter scattering off nucleons, as a function of the dark matter mass M_{DM} for sin $\alpha = 0$. The left panel is for the proton, the right one for the neutron. The red lines show points of the parameter space, with restricted M_{DM} and h'_{ν} values, which reproduce acceptable relic density. The areas above the pink dashed line and the green dash-dotted line are ruled out by the COUPP [33] and XENON100 [34] measurements, respectively. As the panels show, to obtain the correct relic density, the resonantly enhanced annihilation rate implies a suppressed Yukawa coupling for the neutrino DM, which leads to a suppressed cross section. Here again we observe the two dips surrounding the Z resonance and the h resonance. The limits on the SD cross section from the COUPP and XENON100 results do not restrict the parameter space of our model. In



FIG. 5 (color online). (Top panels) The spin-dependent cross section of the nucleon in the HTM with vectorlike leptons, as a function of the dark matter mass M_{DM} (GeV) for sin $\alpha = 0$. We show (left panel) the spin-dependent cross section of the proton (the red line) with XENON100 (dash-dotted green line) and COUPP (dashed pink line) [34] results, (right panel) the spin-dependent cross section of the neutron (red line) with XENON100 (dash-dotted green line) results [34]. The area above the pink dashed line and the green dash-dotted line are ruled out by the COUPP and XENON100 results, respectively. (Bottom panels) Contour plots showing the spin-dependent cross section of the nucleons in the HTM with vectorlike leptons, as functions of the dark matter mass M_{DM} and the Yukawa coupling h'_{ν} , for sin $\alpha = 0$. We show the spin-dependent cross section of the proton (left panel) and the spin-dependent cross section of the neutron (right panel). The panels at the right indicate the color-coded values of the cross section along each slice, and the dash-dotted yellow line represents the only parameter points with an acceptable relic density, $0.1144 \le \Omega_{DM} h^2 \le 0.1252$.

the bottom panel, we plot contour graphs for the spindependent cross sections of the nucleon as functions of the dark matter mass M_{DM} and the Yukawa coupling h'_{ν} , for sin $\alpha = 0$. Again we show the spin-dependent cross section of the proton and the neutron in the left and right panels, respectively. All of the points are consistent with experimental bounds from XENON100 on the spin-dependent nucleon cross sections, as indicated by the color-coded panels, but only parameter points situated along the dashdotted yellow lines in the bottom panels give the correct dark matter relic density. These cross sections are not sensitive to variations in sin α .

In Fig. 6, we plot the SI cross section of the nucleon, as a function of the dark matter mass M_{DM} (in GeV) for sin $\alpha = 0$ (left panel). The red line includes all points yielding a consistent relic density. The regions above the dash-dotted black line, dash-dotted green line, dash-dotted orange line, dash-dotted blue line, dash-dotted purple line, and

dash-dotted pink line are ruled out by XENON100 [35], XENON100 with 2σ expected sensitivity, CRESST-II [32], CDMS-II [36], TEXONO [37], and DAMIC100 (expected for 2014) [38] results, respectively. The cross section is enhanced at the Z pole and the h pole and there, for a suppressed direct rate, the Yukawa coupling must be suppressed to compensate for the resonant production effect. This is seen as two dips at $M_{DM} \sim M_Z/2$ and $M_{DM} \sim m_h/2$. The limit on the SI cross section from XENON100 strongly constrains our model, while the updated results from the other experimental results do not restrict the parameter space. As the left panel of the figure shows, the XENON100 results (with 2σ expected sensitivity) restrict the dark matter mass to be in the 37-52 or 57-63 GeV ranges, or heavier than 95 GeV. In the middle panel, we show the spin-independent cross section of the proton as a graph in $M_{DM} - h'_{\nu}$ space, constrained by all of the experiments with the exception of XENON100,



FIG. 6 (color online). (Left panel) The spin-independent cross section of the proton as a function of the dark matter mass M_{DM} (GeV) in the HTM (the red line). We also show the restrictions from XENON100 [35] (dash-dotted black line), XENON100 with 2σ expected sensitivity (dash-dotted green line), CRESST-II [32] (dash-dotted orange line), CDMS-II [36] (dash-dotted blue line), TEXONO [37] (dash-dotted purple line), and DAMIC100 (expected in 2014) [38] (dash-dotted pink line) results. (Middle panel) Contour graph showing the spin-independent cross section of the nucleon in the HTM with vectorlike leptons, as a function of the dark matter mass M_{DM} and h'_{ν} , for sin $\alpha = 0$, considering all of the experimental constraints except XENON100. (Right panel) Same as the middle panel, but including constraints for the XENON100 (with $+2\sigma$ expected sensitivity) [35] upper limit. The values of the cross section are indicated on the attached color bar. The contours indicate points consistent with the respective experimental constraints, while the dash-dotted line includes only those points with an acceptable relic density, $0.1144 \le \Omega_{DM}h^2 \le 0.1252$, some of which are ruled out by XENON100.

while in the right panel we include the XENON100 (with 2σ expected sensitivity) measurements. The latter rules out large regions of parameter space (in white), while in both panels colored contours (as coded in the attached bars) are allowed by the spin-independent experiments. In both the middle and the right panels, the dash-dotted line represents the only parameter points with an acceptable relic density. Note here that, in agreement with the left panel, there are regions of the parameter space where no combination of M_{DM} and h'_{ν} satisfy *both* relic density *and* XENON100 SI cross section restrictions. Here too, the cross sections are not sensitive to the mixing angle or to other parameters in the model.

VII. INDIRECT DETECTION

Pairs of dark matter particles annihilate, producing high energy particles (antimatter, neutrinos, or photons). Indirect detection experiments for dark matter look for signatures of annihilations of DM originating from particles in the flux of cosmic rays and are sensitive to DM interactions with all of the SM particles. The most stringent constraints on DM annihilation cross sections have been derived from the Fermi Gamma-ray Space Telescope (Fermi-LAT) [39], used to search for DM annihilation products from dwarf spheroidal galaxies and the Galactic center, which probe annihilation cross sections into photons of $\langle \sigma v \rangle \sim 3 \times 10^{-26}$ cm³/s. These searches have attracted a lot of attention due to the unexpected high flux of cosmic ray positrons observed by the PAMELA experiment [40], and confirmed by AMS [41]. We test our model predictions and compare them to the experimental results.

In Fig. 7, we present the annihilation cross section of DM as a function of the dark matter mass M_{DM} and compare it with the constraints on the dark matter annihilation cross section for the e^+e^- channel, the $\mu^+\mu^-$ channel, the $\tau^+\tau^$ channel, $u\bar{u}$, the $b\bar{b}$ channel, and the W^+W^- channel at 95% C.L., derived from a combined analysis of 15 dwarf spheroidal galaxies from Fermi-LAT Collaboration results [39] (left panel). As the figure shows, the limit on the annihilation cross section from the Fermi-LAT Collaboration results imposes some restrictions on our model parameters. Again, the annihilation cross section is enhanced at the Z pole around $M_{DM} = M_Z/2$. The regions around $M_{DM} = M_Z/2$ can be brought into agreement with the relic density constraint by modifying the Yukawa coupling h'_{μ} . In order to include the regions where the annihilation cross section is enhanced, we need to decrease the value of the Yukawa coupling. A suppressed coupling leads to suppression of the annihilation rates [13,26]. The effect of the Higgs pole at $M_{DM} \sim h/2$ is more dramatic than the effect of the Z pole. The dominant annihilation modes of the dark matter pair in this region are coming from decays into quark/antiquark (mainly $b \bar{b}$, which gives a relative contribution of ~77% to $1/\Omega_{DM}h^2$) and also a small contribution from $c\bar{c}$ and $\tau\bar{\tau}$ to obtain the correct dark matter relic density. In the right panel, we show the annihilation cross section as a contour plot in the dark matter mass M_{DM} and Yukawa coupling h'_{μ} plane. Here, as in the previous figures, the contours, according to the color coding in the attached bar, represent the regions of the



FIG. 7 (color online). (Left panel) The annihilation cross section of DM as a function of the dark matter mass M_{DM} (GeV) (the red line). We show the constraints on the dark matter annihilation cross section for the e^+e^- channel (the dash-dotted green line), the $\mu^+\mu^-$ channel (the dash-dotted orange line), the $\tau^+\tau^-$ channel (the dash-dotted pink line), $u\bar{u}$ (the dash-dotted blue line), the $b\bar{b}$ channel (the dash-dotted purple line), and the W^+W^- channel (the dash-dotted black line) at 95% C.L. derived from the combined analysis of the Fermi-LAT Collaboration [39]. (Right panel) Contour plot showing the annihilation cross section as a function of the dark matter mass M_{DM} and its Yukawa coupling, h'_{ν} . The contours are consistent with the experimental values for the cross sections, indicated by the color-coded bar, while the white regions are ruled out. Only the points along the dash-dotted yellow line give the correct dark matter relic density, $0.1144 \le \Omega_{DM}h^2 \le 0.1252$.

parameter space consistent with the experimental results, while the white regions are excluded. Only points along the dash-dotted line have an acceptable relic density.

VIII. DETECTION AT PARTICLE COLLIDERS

If dark matter has a significant coupling to nuclear matter it can be produced in high energy collisions at the LHC or at future colliders. Once produced, as it is neutral and weakly interacting, DM will not be observed directly, but it could be inferred from the missing transverse momentum. Collider searches provide the opportunity to study DM production in a controlled environment. They are particularly sensitive to the region of low mass dark matter, where backgrounds are smaller. At the LHC, dark matter can be produced directly, together with additional radiation from the quarks or gluons participating in the reaction, which results in a single jet (a monojet) plus the missing momentum. High energy lepton colliders could create dark matter through a similar process. Assuming that DM couples to quarks and gluons and couplings the order of the electroweak size, the LHC excludes DM masses up to 500 GeV and, for DM coupling to electrons with the samesize couplings, LEP excludes DM with a mass below 90 GeV. Neither of these restrictions are applicable here, as vectorlike neutrinos do not couple directly to either quarks or leptons.

IX. THE FLUX OF MUONS AND NEUTRINOS FROM THE SUN

The recent observations of ultrahigh energy neutrino events at IceCube [42] seem to indicate a possible deficit in the muon track (known as the muon deficit problem) and an apparent energy gap in the three-year high energy neutrino data, challenging a simple explanation in terms of atmospheric neutrinos and suggesting an extraterrestrial origin. These astrophysical neutrinos are assumed to have originated from the decays of charged particles produced in pp or $p\gamma$ collisions. While the data obtained is largely consistent with SM predictions, the flux shows a mild deficiency in muons at high energies, prompting alternative explanations involving dark matter.

In Fig. 8, we show the neutrino (left panel) and muon (right panel) fluxes as functions of the dark matter mass M_{DM} (GeV). In the top panels, we plot our results as a red curve and include the upper limits on the neutrino and muon flux for the $b\bar{b}$ channel, the $\tau^+\tau^-$ channel, and the $\nu_e \bar{\nu_e}$, $\nu_\mu \bar{\nu}_\mu$, $\nu_\tau \bar{\nu}_\tau$ channels from the Baikal NT200 detector results [43]. While the limit on the muon flux from the Baikal results does not impose restrictions on our model,⁶ the neutrino flux excludes DM particles with a mass in the 74-85 GeV region. The figures show again the two dips at $M_{DM} \sim 45$ GeV and $M_{DM} \sim 62$ GeV. Unlike the annihilation cross section, here the effect of the Z pole is more dramatic than that of the Higgs pole at $M_{DM} \sim h/2$. The bottom panels show the fluxes of neutrino and muon as contour plots in the dark matter mass M_{DM} and the Yukawa coupling h'_{ν} . Note that here, as before, the contours are consistent with the experimental values for the measured flux of muons and neutrinos. However, only points along

⁶Because of limited space in the figure, we only show the recent results of Baikal NT200. However, our results are also consistent with those from the Baksan Neutrino Observatory [44].



FIG. 8 (color online). (Top panels) The fluxes of neutrinos (left panel) and muons (right panel) in the HTM with vectorlike leptons, as functions of the dark matter mass M_{DM} (GeV) (the red line). We also show the upper limits on the neutrino and muon flux for the $b\bar{b}$ channel (the dash-dotted green line), the $\tau^+\tau^-$ channel (the dash-dotted orange line), the $\nu_e\bar{\nu}_e$ channel (the dash-dotted pink line), the $\nu_\mu\bar{\nu}_\mu$ channel (the dash-dotted blue line), and the $\nu_\tau\bar{\nu}_\tau$ channel (the dash-dotted purple line) from the Baikal NT200 detector results [43]. (Bottom panels) Contour plots showing the flux of neutrinos (left panel) and muons (right panel) in the HTM with vectorlike leptons, as functions of the dark matter mass M_{DM} and the Yukawa coupling h'_{ν} . The flux values are color coded as in the bar attached. The contours indicate points consistent with the respective experimental constraints, while the dash-dotted yellow line includes the only points with an acceptable relic density, $0.1144 \le \Omega_{DM} h^2 \le 0.1252$.

the dash-dotted yellow line are consistent with the dark matter relic density exclusion limit.

X. SUMMARY AND CONCLUSION

In this work we analyzed the effects of introducing vectorlike leptons in the Higgs triplet model. Our aim was to provide a scenario that can explain both neutrino masses and provide a DM candidate, problems unresolved in the SM. We chose a full generation of vectorlike leptons (one left-handed doublet and two right-handed singlets, together with their mirror representations). We ensured that a new symmetry differentiates between ordinary leptons and the new states, forbidding unwanted lepton flavor violation. Opting for a simplified Yukawa coupling structure, a mostly singlet right-handed vectorlike neutrino emerges as a single DM candidate. Introducing vectorlike leptons in the HTM relaxes the severe constraints on the mass of the doubly charged Higgs boson coming from electroweak precision tests. We revisited precision observables in this work and showed that, while the S parameter does not impose constraints on the parameter space, the T parameter is restrictive, allowing only certain combinations of doubly charged mass, Yukawa couplings, and mixing angles between the neutral Higgs bosons. Of these, the most sensitive parameter is the mass of the doubly charged Higgs boson, required to be less than about 280 GeV, but here, this boson has different branching ratios than in the minimal HTM. The T parameter is insensitive to the mass of the dark matter candidate.

We verified that the invisible decay width of the Higgs boson is consistent not only with the experimental data, but with the more restrictive limits imposed by global fits to the Higgs data. The invisible width is a relevant constraint for dark matter masses less than one half of the Higgs mass, and all of these survive. More stringent constraints come from direct detection experiments, especially from a restriction on the spin-independent nucleon cross section, and from the relic density. The latter restricts the combination between the dark matter mass and its Yukawa coupling to narrow bands in the parameter space, and it disallows entirely regions where the DM candidate is lighter than 23 or heavier than 103 GeV. If one includes constraints from XENON100 on the spin-independent scattering of dark matter off nucleons, these further restrict the dark matter mass to be in the ranges 37–52 or 57–63 GeV, or heavier than 95 GeV, all for points satisfying the relic density constraints. In addition, consistent with direct detection experiments, the neutrino flux excludes DM particles with a mass in the 74–85 GeV range. These are the most stringent restrictions, and they are insensitive to other model parameters, such as other masses (particularly the doubly charged Higgs boson) and the mixing angle between the neutral Higgs bosons.

To summarize, we presented a simple model that accounts for neutrino masses and dark matter and is consistent with the relic density and all direct and indirect searches. This model assumes a single dark matter particle, and the experimental data restricts its mass to be confined to limited regions in the parameter space. If the dark matter is as light as 1 or a few GeV, as some experiments suggest, this scenario is ruled out. However, for a DM mass of around 30 GeV, allowing small deviations from direct detection, the HTM with vectorlike leptons provides a viable explanation. This analysis assumed the DM candidate to be light and set an upper bound on its mass of 108 GeV, by the choice of the mass of the lightest verctorlike charged lepton. One can extend this scenario to a more complicated one, involving several DM particles. This model would be less constrained, but it loses the predictability of the simple scenario presented here. Given the importance of DM in understanding the Universe, as well as the effort going into direct and indirect detection and the collider experiments, simple models such as this one can help in elucidating the nature of DM.

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SAHAR BAHRAMI AND MARIANA FRANK

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