

**Usefulness of effective field theory for boosted Higgs production**

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The Higgs + jet channel at the LHC is sensitive to the effects of new physics both in the total rate and in the transverse momentum distribution at high  $p_T$ . We examine the production process using an effective field theory (EFT) language and discussing the possibility of determining the nature of the underlying high-scale physics from boosted Higgs production. The effects of heavy color triplet scalars and top partner fermions with TeV scale masses are considered as examples and Higgs-gluon couplings of dimension five and dimension seven are included in the EFT. As a byproduct of our study, we examine the region of validity of the EFT. Dimension-seven contributions in realistic new physics models give effects in the high  $p_T$  tail of the Higgs signal which are so tiny that they are likely to be unobservable.

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**I. INTRODUCTION**

The recently discovered Higgs boson has all the generic characteristics of a Standard Model (SM) Higgs boson and measurements of the production and decay rates agree to the  $\sim 20\%$  level with Standard Model predictions [1–4]. Precision measurements of Higgs couplings are essential for understanding whether there exist small deviations from the Standard Model predictions which could be indications of undiscovered high-scale physics. If there are no weak-scale particles beyond those of the SM, then effective field theory (EFT) techniques can be used to probe the beyond the Standard Model (BSM) physics [5–7]. The EFT is the most general description of low-energy processes and new physics manifests itself as small deviations from the SM predictions. In the electroweak sector, this approach has been extensively studied [8–12]. The effects of BSM operators affecting Higgs production in the strong sector have been less studied [13–15].

The largest contribution to Standard Model Higgs boson production at the LHC comes from gluon fusion through a top quark loop, and we examine new physics effects in this channel, along with the related Higgs + jet channel. We consider an effective Lagrangian containing the SM fermions and gauge bosons, along with a single Higgs boson,  $h$ . At dimension four, the fermion-Higgs couplings can be altered from the SM couplings by a simple rescaling,

$$-\mathcal{L}_f = \kappa_f \left( \frac{m_f}{v} \right) \bar{f} f h + \text{H.c.}, \quad (1)$$

where  $\kappa_f = 1$  in the SM. In models with new physics, the gluon fusion rate can also be altered by new heavy particles

interacting with the Higgs boson at one loop, which contribute to an effective dimension-five operator [16–18],

$$\mathcal{L}_5 = C_1 G^{A,\mu\nu} G_{\mu\nu}^A h, \quad (2)$$

where  $C_1 = \alpha_s / (12\pi v)$  for an infinitely heavy fermion with  $\kappa_f = 1$ . For convenience, we define  $\kappa_g$  to be the ratio of  $C_1$  to this reference value,

$$\kappa_g \equiv C_1 / \left( \frac{\alpha_s}{12\pi v} \right). \quad (3)$$

We compute the top quark contribution to scattering processes exactly using Eq. (1) (i.e., not in the infinite top quark mass limit) and consider  $C_1$  to be only the contribution from new physics. The measurement of gluon fusion by itself can determine a combination of  $\kappa_g$  and the top quark Yukawa coupling,  $\kappa_t$ , but cannot distinguish between the two for  $m_t \gg m_h$  [19–22]. Including the dimension-five operator of Eq. (2), the cross section is generically,

$$\mu_{ggh} \equiv \frac{\sigma(gg \rightarrow h)}{\sigma(gg \rightarrow h)_{\text{SM}}} \sim |\kappa_t + \kappa_g|^2 + \mathcal{O}\left(\frac{m_h^2}{m_t^2}\right). \quad (4)$$

The requirement that  $|\mu_{ggh} - 1| < 10\%$  (or 5%) is shown in Fig. 1, where top quark mass effects are included exactly. The SM corresponds to the point  $\kappa_g = 0$ ,  $\kappa_t = 1$ . The contribution from  $b$ -quarks is small and has been neglected.

The boosted production of the Higgs boson through the process  $pp \rightarrow h + \text{jet}$  is sensitive to the Higgs-gluon effective coupling [20–25] and offers the possibility of disentangling new physics effects and hence breaking the

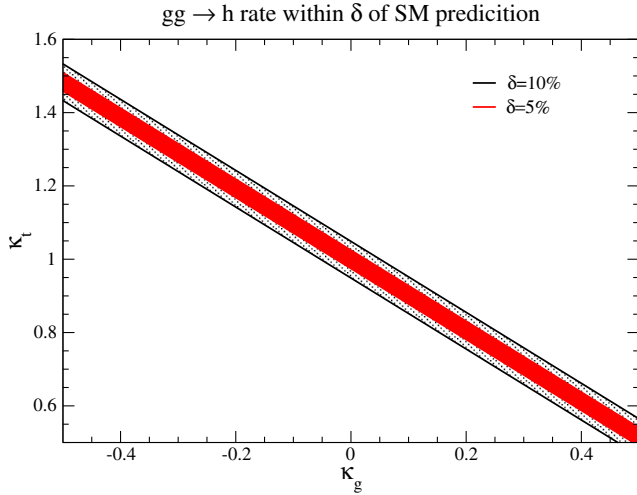


FIG. 1 (color online). Allowed values of the EFT coefficients when the total gluon fusion rate,  $gg \rightarrow h$ , is within  $\pm 10\%$  ( $\pm 5\%$ ) of the SM prediction, ( $\kappa_g \equiv 12\pi v C_1/\alpha_s$ ).

degeneracy between  $\kappa_t$  and  $\kappa_g$ . An effective Lagrangian approach is useful for studying this high  $p_T$  BSM physics and the Higgs-parton interactions can be described as a sum of higher-dimension operators,

$$\mathcal{L}_{\text{EFT}} \sim \mathcal{L}_4 + \mathcal{L}_5 + \mathcal{L}_6 + \mathcal{L}_7 + \dots, \quad (5)$$

where  $\mathcal{L}_n$  includes all dimension- $n$  operators. At dimension five and assuming  $CP$  conservation, there is only the single operator of Eq. (2) modifying the Higgs-gluon interactions. The dimension-five operator has been broadly used to obtain higher-order QCD corrections to Higgs rates [17,18,26–32].

Dimension-seven operators affecting Higgs-gluon interactions from QCD interactions have received less attention [14,33,34]. Because their contributions are proportional to the strong coupling,  $g_s$ , these operators can have numerically significant effects. In a previous work [13], we considered the effects of dimension-seven operators affecting Higgs-gluon interactions and demonstrated the importance of including these operators along with the NLO QCD corrections in order to obtain realistic predictions of boosted Higgs spectra. The largest contribution to Higgs + jet production is from the  $O_1$  operators in the  $gg$  initial channel. The NLO QCD corrections to this channel are relatively flat in  $p_T$  and lead to an enhancement of roughly a factor of 2 in the rate at the 14 TeV LHC. The contributions from  $O_3$  to Higgs + jet production are suppressed at lowest-order QCD (LO) for large  $p_T$  since they vanish in the soft Higgs limit. These contributions receive large NLO corrections, but remain numerically small and are never important. The contributions from the interference of the  $O_1$  and  $O_5$  operators can be important for large  $p_T \sim 300$  GeV and receive NLO QCD corrections which are again fairly  $p_T$  independent and increase the rate by a factor of  $\sim 1.2$ .

In this paper, we examine the expected size of the coefficients of the Higgs-gluon EFT dimension-five and dimension-seven operators in several representative UV models with heavy colored scalars and fermions. We are particularly interested in the question of whether the measurement of the boosted Higgs  $p_T$  distribution can distinguish the nature of the underlying UV physics, should there be any deviation from the SM. We then demonstrate how the inclusion of the dimension-seven operators affects fit to EFT Higgs parameters from gluon fusion. We work at LO QCD.

In Sec. II, we review the EFT. The heavy colored scalar and fermion models which we study are introduced in Sec. III and the matching coefficients of the EFT are presented. Phenomenological results at the LHC are given in Sec. IV, and some conclusions about the usefulness of the EFT in this channel are presented in Sec. V.

## II. EFFECTIVE LAGRANGIAN

In this section, we review the effective Lagrangian relevant for Higgs + jet production containing non-SM Higgs-gluon interactions. We consider a  $CP$ -conserving Lagrangian, with no new Higgs particles,

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + (\kappa_t - 1)(-1)\bar{t}th + \mathcal{L}_5 + \mathcal{L}_7 + \dots, \quad (6)$$

where

$$\mathcal{L}_5 + \mathcal{L}_7 \equiv \hat{C}_1 O_1 + \sum_{i=2,3,4,5} \hat{C}_i O_i. \quad (7)$$

Note that there are no relevant dimension-six operators of the type we are considering.

At dimension five, the unique operator is

$$O_1 = G_{\mu\nu}^A G^{\mu\nu,A} h, \quad (8)$$

where  $G_{\mu\nu}^A$  is the gluon field strength tensor. The dimension-seven operators needed for the gluon fusion production of Higgs are [33–35]

$$O_2 = D_\sigma G_{\mu\nu}^A D^\sigma G^{A,\mu\nu} h \quad (9)$$

$$O_3 = f_{ABC} G_\nu^{A,\mu} G_\sigma^{B,\nu} G_\mu^{C,\sigma} h \quad (10)$$

$$O_4 = g_s^2 h \sum_{i,j=1}^{n_{lf}} \bar{\psi}_i \gamma_\mu T^A \psi_i \bar{\psi}_j \gamma^\mu T^A \psi_j \quad (11)$$

$$O_5 = g_s h \sum_{i=1}^{n_{lf}} G_{\mu\nu}^A D^\mu \bar{\psi}_i \gamma^\nu T^A \psi_i, \quad (12)$$

where our convention for the covariant derivative is  $D^\sigma = \partial^\sigma - ig_s T^A G^{A,\sigma}$ ,  $\text{Tr}(T^A T^B) = \frac{1}{2} \delta_{AB}$ , and  $n_{lf} = 5$  is the number of light fermions. Including light quarks,  $O_4$  and  $O_5$  are needed, which are related by the equations of motion (eom) to gluon-Higgs operators,

$$\begin{aligned} O_4|_{\text{eom}} &\rightarrow D^\sigma G_{\sigma\nu}^A D_\rho G^{A,\rho\nu} h \equiv O'_4 \\ O_5|_{\text{eom}} &\rightarrow G_{\sigma\nu}^A D^\nu D^\rho G_\rho^{A,\sigma} h \equiv O'_5. \end{aligned} \quad (13)$$

Since  $O_4$  involves four light fermions, the operator only contributes to Higgs + jet production starting at NLO.

A different dimension-seven operator is useful,

$$O_6 = -D^\rho D_\rho (G_{\mu\nu}^A G^{\mu\nu,A}) h = -\partial^\rho \partial_\rho (G_{\mu\nu}^A G^{\mu\nu,A}) h = m_h^2 O_1, \quad (14)$$

where the last equal sign is only valid for on-shell Higgs production. Using the Jacobi identities,

$$O_6 = m_h^2 O_1 = -2O_2 + 4g_s O_3 + 4O_5. \quad (15)$$

Therefore, we can choose  $O_6 = m_h^2 O_1$ ,  $O_3$ ,  $O_4$ , and  $O_5$  as a complete basis for the dimension-seven Higgs-gluon-light quark operators. We rewrite Eq. (7) as

$$\mathcal{L}_{\text{eff}} = C_1 O_1 + (C_3 O_3 + C_4 O_4 + C_5 O_5). \quad (16)$$

The lowest-order amplitudes for Higgs + jet production including all fermion mass dependence (bottom and top) are given in Refs. [36,37]. A study of Higgs + jet production at LO QCD in the EFT approximation involves only  $C_1$ ,  $C_3$  and  $C_5$  [13,38]. At the lowest order in  $\alpha_s$ ,  $O_3$  is the only dimension-seven operator which contributes to the  $gg \rightarrow gh$  channel, while  $O_5$  is the only dimension-seven operator which contributes to channels with initial state quarks. The lowest-order amplitudes in the EFT for Higgs + jet production can be found in Ref. [13], along with the NLO results including the effects of dimension-seven operators. For Higgs + jet production at NLO in BSM models, the EFT description also needs to include the higher-dimensional three-gluon effective vertex generated at one loop [13,39], which could affect dijet and top quark rates [40].

### III. UV PHYSICS AND THE EFT

In this section, we discuss several prototype BSM physics models which have heavy particles contributing to Higgs + jet production and we compute the matching coefficients for the EFT in these models. This will allow us to estimate the size of BSM contributions.

#### A. Heavy colored scalars

We consider the addition of either real or complex  $SU(3)$  scalars,  $\phi_i$  [41–45]. Our numerical results are all derived for a complex scalar triplet. The scalar portion of the Lagrangian involving a new complex scalar,  $\phi_i$ , and the SM-like Higgs doublet,  $H$ , is,

$$V_{\text{complex}} = V_{\text{SM}}(H) + m_i^2 \phi_i^\dagger \phi_i + \frac{C_h}{v} \phi_i^\dagger \phi_i (H^\dagger H) - \lambda_4 (\phi_i^\dagger \phi_i)^2, \quad (17)$$

where  $V_{\text{SM}}$  is the SM Higgs potential. For a real scalar,

$$V_{\text{real}} = V_{\text{SM}} + \frac{m_i^2}{2} (\phi_i)^2 + \frac{C_h}{2v} (\phi_i)^2 (H^\dagger H) - \lambda_4 (\phi_i)^4. \quad (18)$$

In unitary gauge,  $H \rightarrow (0, (h+v)/\sqrt{2})$ .

#### B. Top partner model

Many BSM contain a charge- $\frac{2}{3}$  partner of the top quark. We consider a general case with a vectorlike  $SU(2)_L$  singlet fermion which is allowed to mix with the Standard Model-like top quark [46–50]. The mass eigenstates are defined to be  $t$  and  $T$  with masses  $m_t$  and  $M_T$  and are derived from the gauge eigenstates using bi-unitary transformations involving two mixing angles  $\theta_L$  and  $\theta_R$ . Without loss of generality,  $\theta_R$  can be removed by a redefinition of the top partner gauge eigenstate and the Higgs couplings are then modified from those of the SM [51]:

$$\begin{aligned} L_h^{\text{top partner}} = & - \left\{ \cos^2 \theta_L \frac{m_t}{v} \bar{t}_L t_R h + \sin^2 \theta_L \frac{M_T}{v} \bar{T}_L T_R h \right. \\ & + \frac{M_T}{2v} \sin(2\theta_L) \bar{t}_L T_R h + \frac{m_t}{2v} \sin(2\theta_L) \bar{T}_L t_R h \\ & \left. + \text{H.c.} \right\}. \end{aligned} \quad (19)$$

Precision electroweak fits to the oblique parameters, as well as  $M_W$ , place stringent restrictions on the product  $\sin^2 \theta_L M_T^2$  and for  $M_T \sim 1$  TeV,  $\sin \theta_L < .17$  [48,50]. Higgs production has been investigated at NNLO for top partner models in Ref. [50] and the rate determined to be within a few % of the SM rate for allowed values of  $\theta_L$ . Large effects in this channel require values of  $\sin \theta_L$  that are excluded by precision measurements. ATLAS [52] and CMS [53] have searched for top singlet partners and excluded  $M_T$  below 655 GeV and 687 GeV, respectively. Similar limits on top partner masses and mixing can be obtained for different choices of top partner  $SU(2)_L$  properties [48].

#### C. Predictions for coefficients

The exact results for the contributions from high-scale fermion [36,37] and scalar loops [41,42] to the rates for  $q\bar{q} \rightarrow gh$  and  $gg \rightarrow gh$  are well known. Matching to the EFT expressions, the coefficient functions can be extracted. The EFT amplitude for  $q\bar{q} \rightarrow gh$  from virtual heavy particles with mass,  $m$ , is

$$\begin{aligned} |A(q\bar{q} \rightarrow gh)|^2 &= 64g_s^2 \left( \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}} \right) \left[ C_1^2 + \frac{\hat{s} C_1 C_5}{2} \right] \\ &= \lim_{m \rightarrow \infty} \left( \frac{4\alpha_s^3}{\pi} \right) \left( \frac{\hat{u}^2 + \hat{t}^2}{\hat{s}v^2} \right) |\mathcal{A}_5(\hat{s}, \hat{t}, \hat{u}, m^2)|^2, \end{aligned} \quad (20)$$

while the EFT amplitude for  $gg \rightarrow gh$  from virtual heavy particles with mass,  $m$ , is

$$\begin{aligned}
|A(gg \rightarrow gh)|^2 &= g_s^2 \left[ 384 C_1^2 \left[ \frac{m_h^8 + \hat{s}^4 + \hat{t}^4 + \hat{u}^4}{\hat{s} \hat{t} \hat{u}} \right] \right. \\
&\quad \left. + 1152 C_1 C_3 m_h^4 \right] \\
&= \lim_{m \rightarrow \infty} \left( \frac{96 \alpha_s^3}{\pi} \frac{m_h^8}{\hat{s} \hat{t} \hat{u} v^2} \right) \left\{ |\mathcal{A}_2(\hat{s}, \hat{t}, \hat{u}, m^2)|^2 \right. \\
&\quad \left. + |\mathcal{A}_2(\hat{u}, \hat{s}, \hat{t}, m^2)|^2 + |\mathcal{A}_2(\hat{t}, \hat{u}, \hat{s}, m^2)|^2 \right. \\
&\quad \left. + |\mathcal{A}_4(\hat{s}, \hat{t}, \hat{u}, m^2)|^2 \right\}, \quad (21)
\end{aligned}$$

where  $\hat{s}$ ,  $\hat{t}$ , and  $\hat{u}$  are the usual Mandelstam variables. The coefficient functions  $\mathcal{A}_2(\hat{s}, \hat{t}, \hat{u}, m^2)$ ,  $\mathcal{A}_4(\hat{s}, \hat{t}, \hat{u}, m^2)$  and  $\mathcal{A}_5(\hat{s}, \hat{t}, \hat{u}, m^2)$  are given in Ref. [37] for fermion loops and in Ref. [41] for scalar loops. The  $C_1$ ,  $C_3$  and  $C_5$  coefficients of Eqs. (20) and (21) depend in general on the parameters of the underlying UV completion of the model. By matching the EFT predictions with the heavy fermion expansions, we obtain the EFT coefficients given in Table I. At LO, the dimension-seven term contributing to the  $gg \rightarrow gh$  amplitude does not contain any dependence on the kinematic variables. For TeV scale masses, it is clear that the coefficients are quite small. For the top partner model, the coefficient functions for the heavier Dirac fermion contributions need to be multiplied by the factor  $\sin^2 \theta_L$  appearing in Eq. (19), while the SM top quark contribution is included exactly without using the EFT.

The matching of the EFT and the underlying UV theory are done at the high-scale  $\Lambda$ . Using the anomalous dimensions found in Ref. [13,54], the coefficients can be evolved to a low scale,  $\mu_R \sim m_h$ ,

$$\frac{d}{d \ln \mu_R} \ln \left( \frac{C_1(\mu_R)}{g_s^2(\mu_R)} \right) = \mathcal{O}(\alpha_s^2(\mu_R)), \quad (22)$$

$$\frac{d}{d \ln \mu_R} \ln \left( \frac{C_3(\mu_R)}{g_s^3(\mu_R)} \right) = \frac{\alpha_s(\mu_R)}{\pi} 3C_A, \quad (23)$$

$$\frac{d}{d \ln \mu_R} \ln \left( \frac{C_5(\mu_R)}{g_s^2(\mu_R)} \right) = \frac{\alpha_s(\mu_R)}{\pi} \left( \frac{11}{6} C_A + \frac{4}{3} C_F \right), \quad (24)$$

TABLE I. The effective Lagrangian coefficient functions for heavy Dirac fermions and heavy scalars with mass,  $m_F$  and  $M_S$ , respectively. The coefficient functions, along with  $g_s$  and  $\alpha_s$ , are evaluated at the scale  $\Lambda = m_F, M_S$ .

	Dirac fermion	$SU(3)$ triplet scalar	$SU(3)$ octet scalar
$C_1(\Lambda)$	$\frac{\alpha_s \kappa_F}{12\pi v} \left[ 1 + \frac{7m_F^2}{120m_F^2} \right]$	$-\frac{\alpha_s}{96\pi M_S^2} C_h \left[ 1 + \frac{2m_h^2}{15M_S^2} \right]$	$-\frac{\alpha_s}{16\pi M_S^2} C_h \left[ 1 + \frac{2m_h^2}{15M_S^2} \right]$
$C_3(\Lambda)$	$-\frac{g_s \alpha_s \kappa_F}{360\pi v m_F^2}$	$-\frac{g_s \alpha_s}{1440M_S^4} C_h$	$-\frac{g_s \alpha_s}{240M_S^4} C_h$
$C_5(\Lambda)$	$\frac{11\kappa_F \alpha_s}{360\pi v m_F^2}$	$-\frac{\alpha_s}{360\pi M_S^4} C_h$	$-\frac{\alpha_s}{60\pi M_S^4} C_h$

RGE Scaling of EFT Coefficients

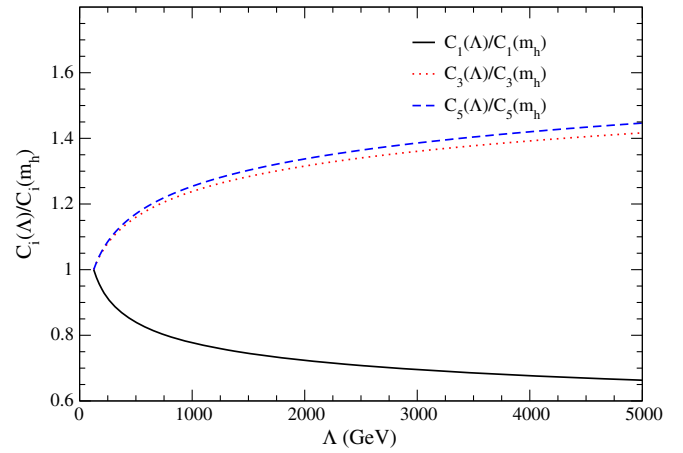


FIG. 2 (color online). The evolution of the dimension-five and dimension-seven EFT coefficients from the scale of new physics,  $\sim \Lambda$ , to the electroweak scale.

where  $C_A = 3$  and  $C_F = \frac{4}{3}$ . The one-loop electroweak RG running of  $C_1/g_s^2$  [55] is nonzero, and its effect on the Higgs  $p_T$  distribution in the TeV range is found to be at the percent level [56].

The leading-logarithmic solutions to the renormalization group running equations Eqs. (22)–(24) are

$$C_1(\mu_R)/g_s^2(\mu_R) = C_1(\mu_0)/g_s^2(\mu_0), \quad (25)$$

$$C_3(\mu_R)/g_s^3(\mu_R) = \left( \frac{\alpha_s(\mu_R)}{\alpha_s(\mu_0)} \right)^{\frac{3C_A}{2b_0}} \cdot C_3(\mu_0)/g_s^3(\mu_0), \quad (26)$$

$$C_5(\mu_R)/g_s^2(\mu_R) = \left( \frac{\alpha_s(\mu_R)}{\alpha_s(\mu_0)} \right)^{-\frac{1}{2b_0}(\frac{11}{6}C_A + \frac{4}{3}C_F)} \cdot C_5(\mu_0)/g_s^2(\mu_0), \quad (27)$$

where  $b_0 = \frac{1}{12}(11C_A - 2n_{lf})$  and  $\mu_0 \sim \Lambda$ . The evolution of the coefficient functions is shown in Fig. 2.  $C_1$  is increased by  $\sim$  a factor of 2 when evolving from  $\Lambda \sim 5$  TeV to the weak scale, while  $C_3$  and  $C_5$  are reduced by a similar factor.

## IV. PHENOMENOLOGY

We will eventually be interested in whether measurements of the  $p_T$  spectrum can distinguish between the effects of the dimension-five and dimension-seven operators resulting from scalars and from fermions; that is, “*Is the EFT a useful tool for disentangling the source of high-scale physics?*”

Throughout this paper, diagrams involving the SM top quark are evaluated with exact  $m_t$  dependence without using the Higgs-gluon EFT, while the contributions from heavy BSM particles, such as a color triplet scalar or a fermionic top partner, are considered both exactly and in the EFT approximation.

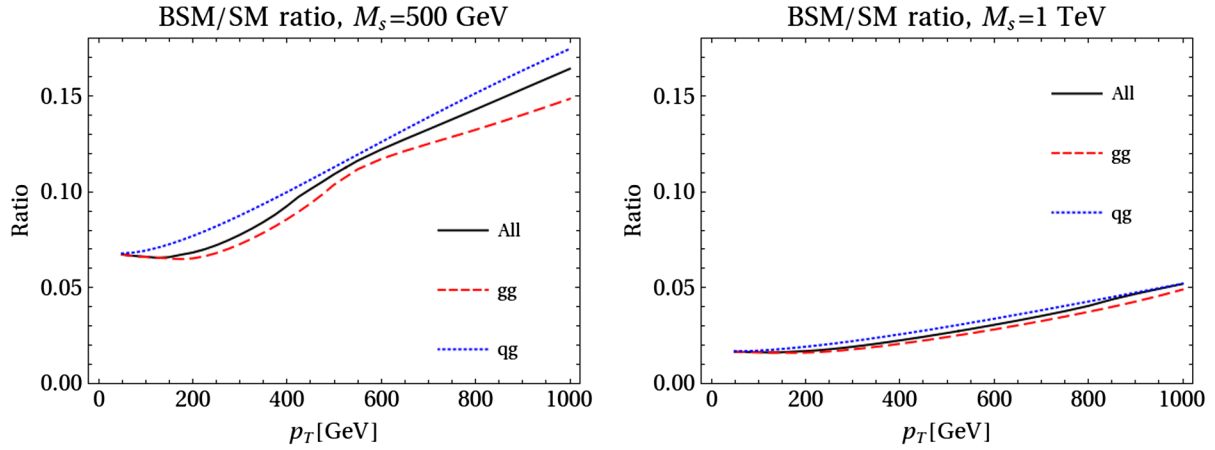


FIG. 3 (color online). Contribution of a 500 GeV color triplet scalar (lhs) and a 1 TeV scalar (rhs), relative to the SM Higgs  $p_T$  distribution. The  $gg$  and  $qg$  partonic channels, and the sum of all partonic channels (which also includes  $q\bar{q}$ ), are shown separately. Both the SM top and the scalar contributions are included exactly at LO.

### A. Heavy colored scalars

We begin by considering the effect of heavy color triplet scalars on Higgs + jet production. (The case of a light colored scalar has been considered in [42].) We use CJ12 NLO PDFs [57] and  $\mu_R = \mu_F = \sqrt{m_h^2 + p_T^2}$  for all curves, with  $m_h = 125$  GeV,  $m_t = 173$  GeV, and  $m_b = 4.5$  GeV. All plots refer to Higgs + jet production at lowest order and with  $\sqrt{s} = 14$  TeV. When using the EFT, the effects of heavy scalars are included using the coefficients of Table I. Since the effects are suppressed by  $1/M_S^2$  in  $C_1$  and  $1/M_S^4$  in the other  $C_i$ , we expect relatively small effects unless the coefficient function  $C_h$  is large. We expect  $C_h$  to be of order the electroweak scale in a realistic model, and in our plots, we take  $C_h = 3M_Z$ .<sup>1</sup> Numerically, the effects are linear in  $C_h$  for modest values of  $C_h/M_Z$ , and our results can be trivially rescaled.

The exact one-loop contribution of the heavy scalars relative to the SM rate are shown in Fig. 3 and as expected, they cause only a few percent deviation from the SM rate at low  $p_T$ . We define the ratio BSM/SM to be the differential (or integrated) rate in the theory with the SM top quark and scalar included exactly normalized to the SM rate minus 1; i.e., it is the incremental contribution from the addition of a scalar. At large  $p_T$ , the deviation becomes significant, approaching  $\sim 15\%$  for  $p_T \sim 1$  TeV for a 500 GeV scalar and  $\sim 5\%$  for a 1 TeV scalar. We note that the effects of a color octet scalar are a factor of  $C_A/T_F = 6$  larger than those of a color triplet scalar. The integrated cross sections with a  $p_{T,\text{cut}}$  are shown in Fig. 4, and a significant contribution from the scalars to the boosted Higgs signal is apparent for  $p_{T,\text{cut}} \sim M_S$  for  $M_S = 500$  GeV. For the

<sup>1</sup>If  $\phi_i$  corresponds to the left-handed top squark of the MSSM, then in the alignment limit ( $\sin\beta = \cos\alpha$ ),  $C_h \sim 3M_Z$ , which motivates our choice. This numerical value is not important for our conclusions, as long as  $C_h/M_Z$  is not a large number.

heavier scalar,  $M_S \sim \text{TeV}$ , the effects are only a few % even for very large  $p_{T,\text{cut}}$ .

Since the lowest-order contribution from scalars is known exactly, we can explore the range of validity of the EFT. Figure 5 shows the deviation of the EFT calculation from the exact one-loop result when color triplet scalars are included. For a 500 GeV scalar, the EFT is accurate to within a few % below  $M_S$  and has large deviations above 500 GeV when only the dimension-five ( $\sim 1/M_S^2$ ) contributions are included. Including the dimension-seven contributions improves the accuracy of the EFT. Interestingly, for  $M_S = 1$  TeV, the EFT becomes less accurate at large  $p_T$  when the dimension-seven effects are included. The EFT expansion clearly breaks down at a scale  $p_T \sim M_S$ . Figure 6 demonstrates the accuracy of the EFT in the  $p_T$  integrated cross section, and we observe the same behavior. (The cross section is integrated to  $p_T = 1$  TeV, where the EFT is breaking down. Since the partonic results are integrated with a falling PDF spectrum, we expect the results to be reasonably reliable.) The contributions from the  $gg$  and  $qg$  initial states are shown separately in Figs. 7 and 8.

### B. Heavy fermion top partners

In this section we consider the effect of a top partner model on the shape of the Higgs  $p_T$  distribution. We take the top partner mass  $M_T = 500$  GeV and the mixing angle  $\cos\theta_L = 0.966$ . Figure 9 shows the ratio of the inclusive cross section in the top partner model to that in the SM, minus 1, evaluated with the exact dependence on the masses  $m_t$  and  $M_T$ , along with the same quantity integrated with a  $P_{T,\text{cut}}$ . We note that the results of Ref. [22] demonstrate large effects at high  $p_T \sim 1$  TeV when  $\sin\theta_L = 0.4$ . Regrettably, such large mixing angles are excluded by precision electroweak data. (We agree with the results of Ref. [22] for small  $\sin\theta_L$ .) Figure 10 shows the accuracy of

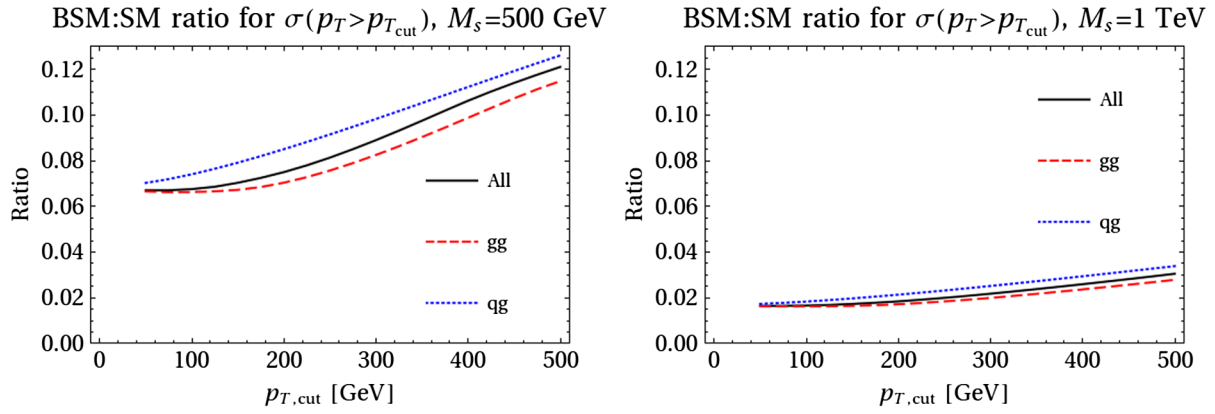


FIG. 4 (color online). Contribution of a 500 GeV color triplet scalar and a 1 TeV scalar, relative to the SM cross section, with a cut  $p_{T,\text{cut}}$ . The  $gg$  and  $qg$  partonic channels, and the sum of all partonic channels (which also include  $q\bar{q}$ ), are shown separately. Both the SM top and the scalar contributions are included exactly at LO.

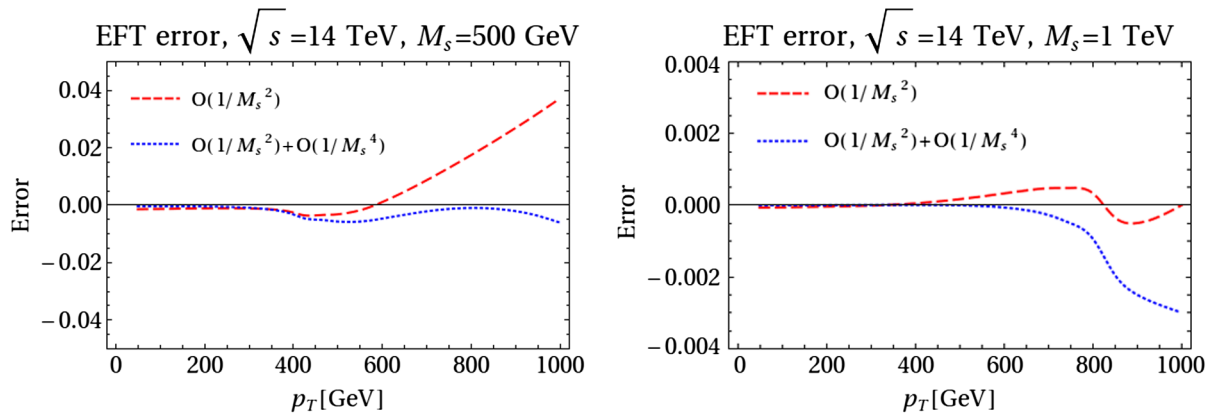


FIG. 5 (color online). Accuracy of the effective field theory calculation of  $d\sigma/dp_T$  relative to the exact calculation when including 500 GeV (lhs) and 1 TeV (rhs) color triplet scalars including all partonic initial states. The dashed lines contain only the dimension-five contributions, while the dotted lines contain both the dimension-five and dimension-seven contributions. The SM top quark contribution is always included exactly.

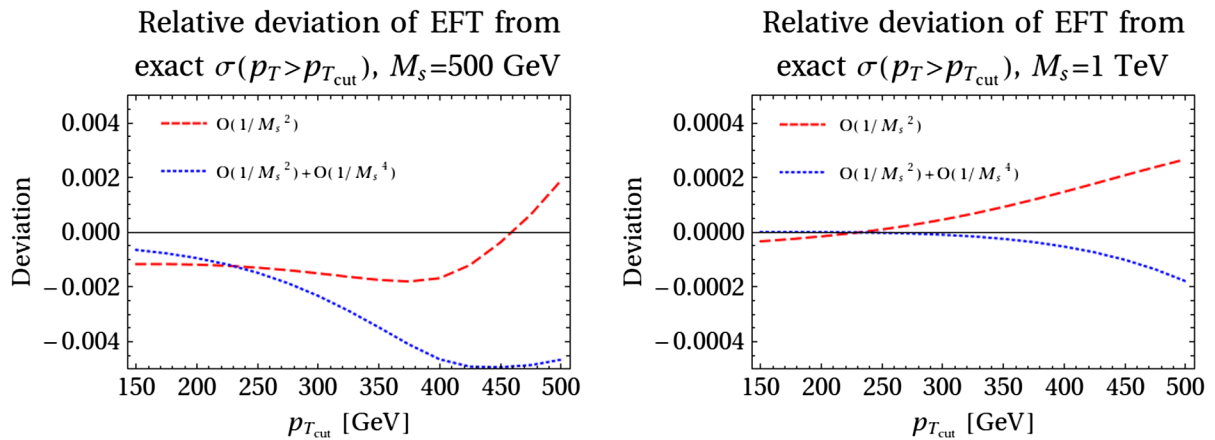


FIG. 6 (color online). Accuracy of the effective field theory calculation of the total cross section subject to a  $p_{T,\text{cut}}$ , relative to the exact calculation when including 500 GeV (LHS) and 1 TeV (RHS) color triplet scalars including all partonic initial states. The dashed lines contain only the dimension-five contributions, while the dotted lines contain both the dimension-five and dimension-seven contributions. The SM top quark contribution is included exactly.

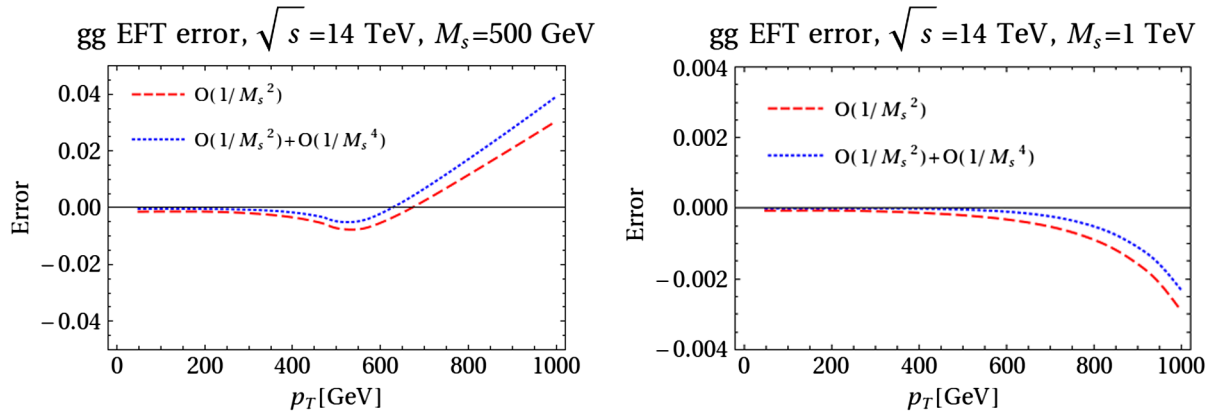


FIG. 7 (color online). Accuracy of the effective field theory calculation of  $d\sigma/dp_T$  relative to the exact calculation when including 500 GeV (lhs) 1 TeV (rhs) color triplet scalars and including only the  $gg$  initial state. The dashed lines contain only the dimension-five contributions, while the dotted lines contain both the dimension-five and dimension-seven contributions. The SM top quark contribution is included exactly.

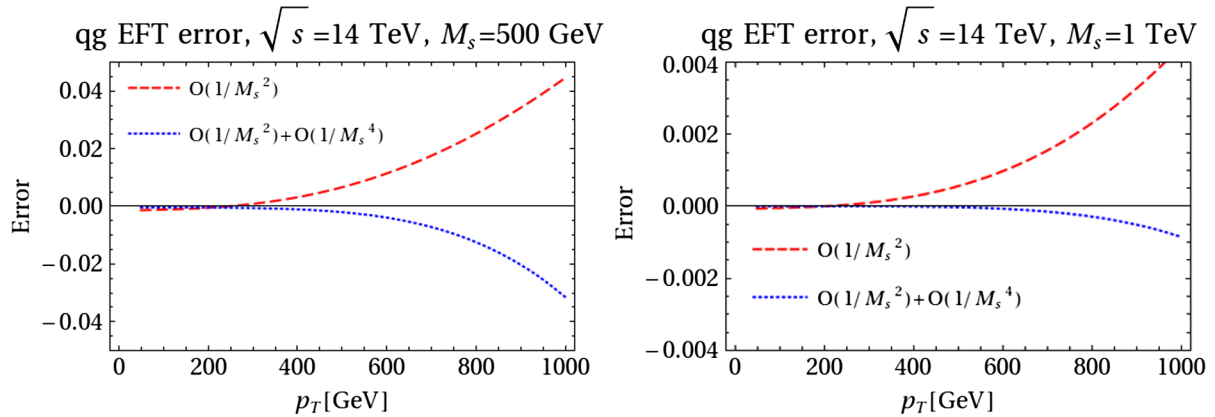


FIG. 8 (color online). Accuracy of the effective field theory calculation of  $d\sigma/dp_T$  relative to the exact calculation when including 500 GeV (lhs) and 1 TeV (rhs) color triplet scalars and including only the  $qg$  initial state. The dashed lines contain only the dimension-five contributions, while the dotted lines contain both the dimension-five and dimension-seven contributions. The SM top quark contribution is included exactly.

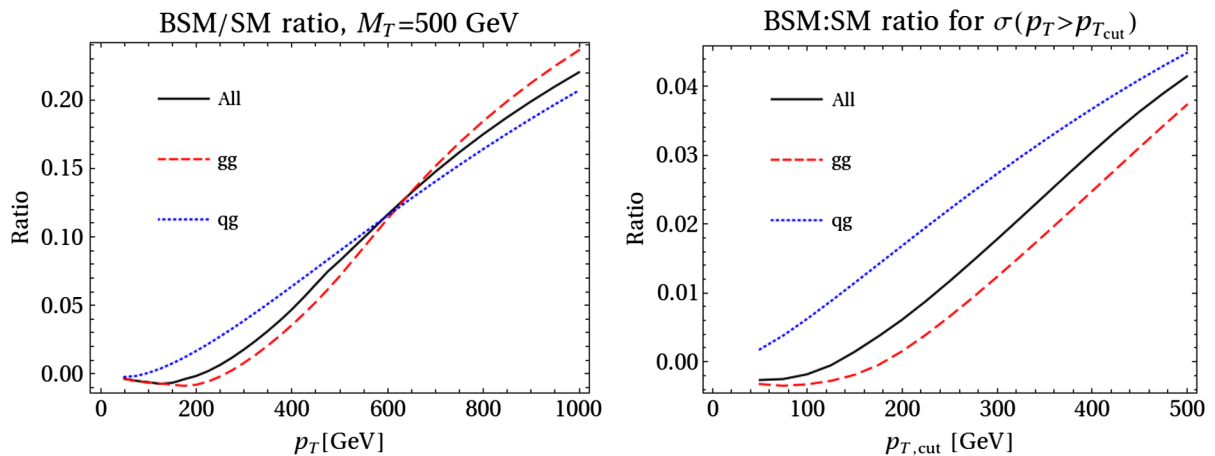


FIG. 9 (color online). The BSM contribution, relative to the SM contribution, to the differential (LHS) and integrated Higgs  $p_T$  distribution (RHS). The  $gg$  and  $qg$  partonic channels, and the sum of all partonic channels (which also include  $q\bar{q}$ ), are shown separately. Both the top partner and top quark contributions are included exactly at LO.

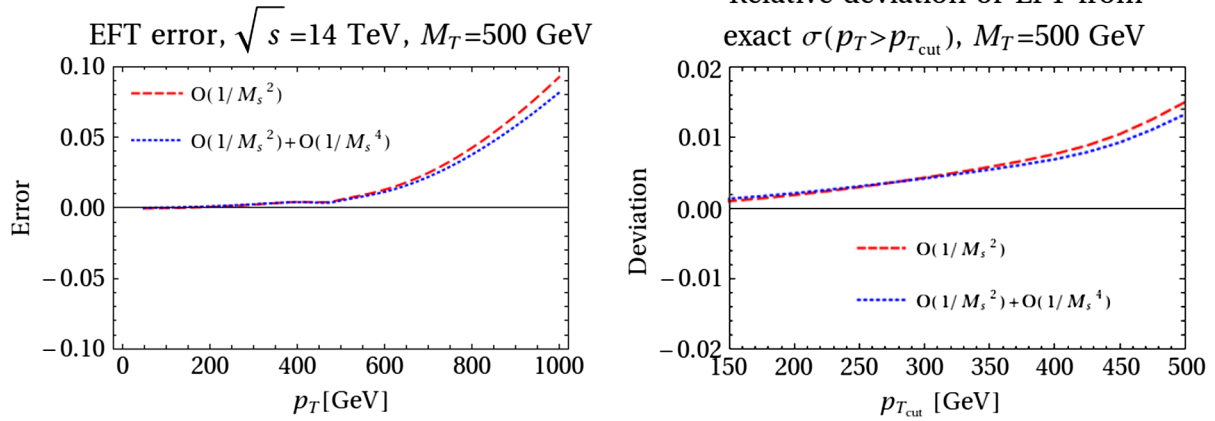


FIG. 10 (color online). Accuracy of the effective field theory calculation of the differential (lhs) and integrated (rhs)  $p_T$  distribution, relative to the exact calculation, for a 500 GeV fermionic top partner with  $\theta = \pi/12$ .

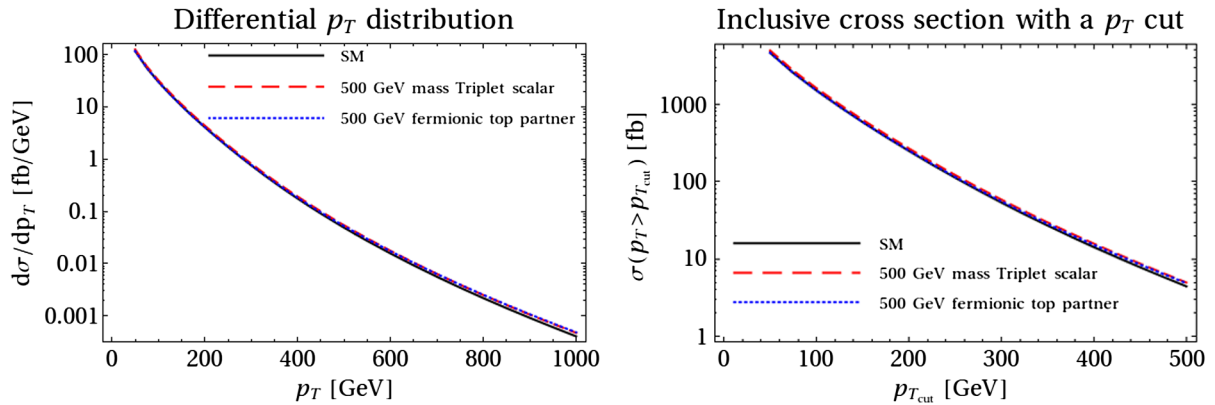


FIG. 11 (color online). Cross sections including the SM result and a 500 GeV color triplet scalar, the SM result and a 500 GeV top partner, compared with the SM predictions.

the EFT predictions for differential and integrated  $p_T$  distributions, relative to the results with exact  $m_t$  and  $M_T$  dependence.

We close this section by summarizing our results for top partners and scalars in Fig. 11, which dramatically demonstrates the difficulty of extracting information about the underlying UV physics.

### C. EFT fits

In this subsection, we consider the effects of a general rescaling of the EFT coefficients. As in Eq. (1) and Eq. (3), we consider the SM top quark contribution rescaled by  $\kappa_t$ , and the  $C_1$  coefficients rescaled by  $\kappa_g$  relative to an infinitely heavy Dirac fermion whose mass comes entirely from the Higgs, i.e.  $C_1 = \kappa_g \cdot \alpha_s / (12\pi v)$ . For the dimension-seven operators, we vary the matching coefficients  $C_i = \kappa_i C_i(M_S = 500 \text{ GeV}, C_h = 3m_Z)$  for  $i = 3, 5$ , where the reference values, scaled by  $\kappa_i$ , are  $C_3(M_S, C_h) = -g_s \alpha_s C_h / (1440 M_S^4)$  and  $C_5(M_S, C_h) = -\alpha_s C_h / (360 \pi M_S^4)$  corresponding to the EFT coefficients from Table I for a 500 GeV scalar. The total cross section for single Higgs

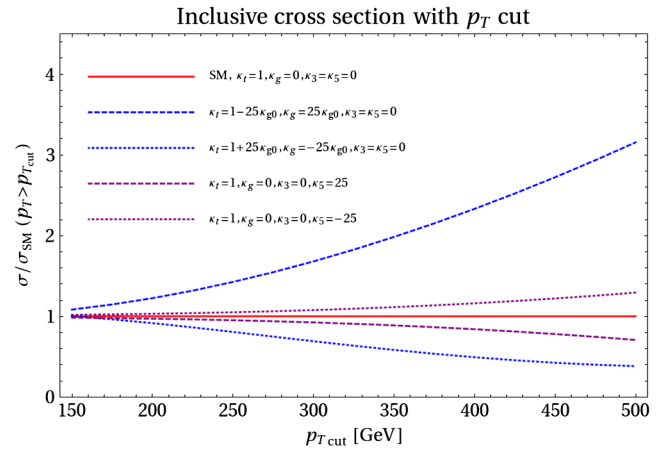


FIG. 12 (color online). Inclusive cross section with a  $p_T$  cut at  $\sqrt{s} = 14 \text{ TeV}$ , normalized to the SM rate. In our parametrization of BSM effects, the SM rate is rescaled by  $\kappa_t$ , while  $C_1$ ,  $C_3$ , and  $C_5$  are rescaled by  $\kappa_g$ ,  $\kappa_3$ , and  $\kappa_5$ , respectively, with the model in Sec. IVA corresponding to  $|\kappa_g|/\kappa_{g0} = \kappa_3 = \kappa_5 = 1$ ,  $\kappa_{g0} \approx 0.0337$ . We have fixed  $\kappa_t + \kappa_g = 1$  to approximately conserve the total cross section.  $\kappa_3$  is fixed to zero in this plot to highlight the effects of  $\kappa_g$  and  $\kappa_5$ .



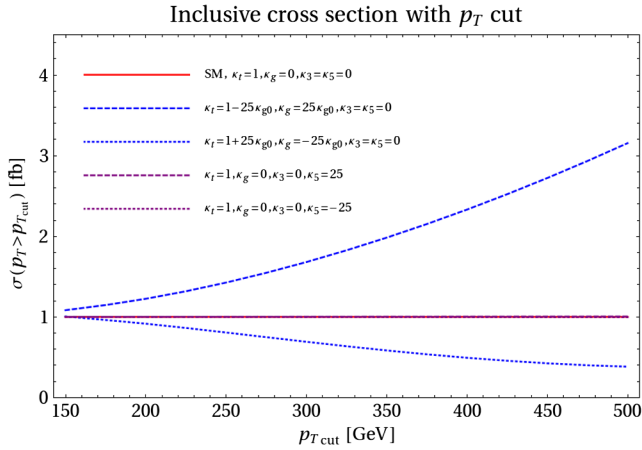


FIG. 13 (color online). Inclusive cross section with a  $p_T$  cut at  $\sqrt{s} = 14$  TeV, normalized to the SM rate. In our parametrization of BSM effects, the SM rate is rescaled by  $\kappa_t$ , while  $C_1$ ,  $C_3$ , and  $C_5$  are rescaled by  $\kappa_g$ ,  $\kappa_3$ , and  $\kappa_5$ , respectively, with the model in Sec. IV A corresponding to  $|\kappa_g|/\kappa_{g0} = \kappa_3 = \kappa_5 = 1$ ,  $\kappa_{g0} \approx 0.0337$ . We have fixed  $\kappa_t + \kappa_g = 1$  to approximately conserve the total cross section.  $\kappa_5$  is fixed to zero in this plot to highlight the effects of  $\kappa_g$  and  $\kappa_3$ . The effect of  $\kappa_3$  can be seen to be extremely small.

production is roughly unchanged from the SM, if we fix  $\kappa_t + \kappa_g$  to be 1, according to Eq. (4). Figure 12 demonstrates that excessively large values of  $\kappa_5$  are required for a large effect from  $O_5$ . Figure 13 shows that the inclusion of  $O_3$  has very little effect even for huge values of  $\kappa_3$ , as expected from the helicity arguments in [13]. On the other hand, the effect of rescaling  $\kappa_t$  and  $\kappa_g$  separately can have a relatively large effect.

## V. CONCLUSION

The process Higgs + jet has been proposed as a useful channel for studying BSM physics and for disentangling

the effects of a modification of the dimension-four  $t\bar{t}h$  Yukawa coupling from a non-SM dimension-five Higgs-gluon effective vertex. We further include dimension-seven effective Higgs-gluon operators and compute the EFT coefficient functions in two representative models with heavy colored scalars and fermions. The coefficient functions are suppressed by inverse powers of the heavy mass scales,  $m$ , and are therefore quite small.

At lowest order, the effects of colored scalars and fermions can be computed exactly and the accuracy of the EFT determined. Typically, better accuracy is obtained in the  $gg$  channel than in the  $qg$  channel, and the EFT is accurate to a few percent for  $p_T < m$ . Our results illustrate the dilemma of the EFT approach: large effects are only obtained at high  $p_T$  and the contribution from the dimension-seven operators is small for  $p_T < m$ . On the other hand, Fig. 12 demonstrates a modest sensitivity to  $C_1$ , independent of  $\kappa_t$ . If any deviation is found in the Higgs transverse momentum distribution up to 1 TeV, the deviation is unlikely to provide information about the UV physics beyond the single parameter  $C_1$ . Our results support the validity of an approach using only the dimension-five Higgs-gluon operator. Inclusion of the NLO QCD corrections is unlikely to change this conclusion, since the NLO corrections to the  $C_1^2$  contribution do not have a large  $p_T$  dependence in the region where the EFT is valid.

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