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Helical phase inflation

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We show that the quadratic inflation can be realized by the phase of a complex field with helicoid potential. Remarkably, this helicoid potential can be simply realized in minimal supergravity. The global $U(1)$ symmetry of the Kähler potential introduces a flat direction and evades the η problem automatically. So such inflation is technically natural. The phase excursion is super-Planckian as required by the Lyth bound, while the norm of the complex field can be suppressed in the sub-Planckian region. This model resolves the ultraviolet sensitive problem of the large field inflation; besides, it also provides a new type of monodromy inflation in supersymmetric field theory with consistent field stabilization.

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I. INTRODUCTION

Inflation [\[1\]](#page-4-0) as a model of the early Universe plays a crucial role in modern cosmology. It beautifully solves the horizon, flatness, and monopole problems, as well as explains the density fluctuation observed in the cosmic microwave background. Some details on the inflationary process are obtained from recent observations of the Planck [\[2\]](#page-4-1) and BICEP2 [\[3\]](#page-4-2) experiments. It shows the inflation scale is about 10^{16} GeV, close to the scale for grand unified theory (GUT). To generate slow-roll inflation, the scalar field ϕ should have sufficiently flat potential $V(\phi)$ so that its mass is hierarchically smaller than the Hubble constant

$$
\eta \equiv M_P^2 \frac{V''}{V} \simeq \frac{m_\phi^2}{3H^2} \ll 1,
$$
\n(1)

where M_P is the reduced Planck scale. At the classical level, the potential can be set sufficiently flat by hand. However, the inflaton as a scalar field receives dangerous quantum corrections and even serious quantum gravity corrections if there is super-Planckian field excursion. The crucial challenge for a sensible inflation model is to protect the flat condition against these dangerous corrections.

At the GUT scale physics is considered to be supersymmetrical and the quantum corrections on the inflaton potential are effectively suppressed by supersymmetry [\[4\]](#page-4-3). However, the flatness of the potential is significantly changed in supergravity. The F-term scalar potential is proportional to a factor e^{K} ; K is the Kähler potential and contains a term $\Phi\bar{\Phi}$ in minimal supergravity. The factor $e^{\Phi\bar{\Phi}}$ generates an inflaton mass close to the Hubble scale and hence breaks the slow-roll condition [\(1\).](#page-0-3) The η problem is absent in no-scale supergravity [\[5\]](#page-4-4), in which the Kähler potential is initially designed to solve the cosmological flatness problem [\[6\]](#page-4-5). Alternatively, one can introduce a shift symmetry $\Phi \to \Phi + iC$ [\[7\]](#page-4-6) in the Kähler potential so that e^{K} is flat along the shift direction.¹

For single field slow-roll inflation, the Lyth bound [\[9\]](#page-4-7) indicates a super-Planckian inflaton excursion $\Delta \phi \sim 10 M_P$ for large tensor modes, which makes the effective theory description of inflation problematic. In the Wilsonian sense, there are higher dimensional operators from quantum gravity effects that are suppressed by the Planck mass M_P and irrelevant in the sub-Planckian region. However, once the inflaton becomes super-Planckian, inflation is sensitive to the higher dimensional operators and the theory is not reliable unless it is ultraviolet (UV) completed [\[10\]](#page-4-8).

Problems from quantum gravity corrections can be avoided if the super-Planckian field excursion is effectively realized in the sub-Planckian region. Considering the phase of a complex scalar field, or the pseudo–Nambu-Goldstone boson (PNGB) in gauge symmetry breaking scenario $[11-14]$, the phase can have super-Planckian displacement while the magnitude of complex field remains sub-Planckian. Besides, the combination of multi-sub-Planckian fields may lead to effective super-Planckian excursion [\[15,16\].](#page-4-10) Another attractive and

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¹The shift symmetry can be slightly broken to get inflationary models with a broad range of tensor-to-scalar ratio r [\[8\].](#page-4-11)

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widely studied model is the monodromy inflation [\[17,18\]](#page-5-0), in which the inflaton is an axion obtained from string compactification and evolves periodically while all the factors except the potential remain the same.

In this article, we present a new inflation model with helicoid potential. This potential is designed to realize super-Planckian inflaton excursion with sub-Planckian fields and the inflation is driven by the phase of a complex field, so that we can keep away from dangerous quantum gravity corrections. Remarkably, the helicoid scalar potential can be simply obtained in minimal supergravity, and the well-known η problem is automatically solved without any extra symmetry. The phase inflation also leads to a new type of monodromy in supersymmetric field theory with strong field stabilization.

II. HELICOID POTENTIAL

Now we give the supergravity realization of the helicoid potential in the simplest case. We consider two chiral superfields Φ and X in minimal supergravity; the Kähler potential is

$$
K = \Phi \bar{\Phi} + X\bar{X} - g(X\bar{X})^2, \qquad (2)
$$

where the higher order term $g(X\bar{X})^2$ is introduced to stabilize the field X at $X = 0$ [\[19,20\].](#page-5-1) Besides, we use the following superpotential:

$$
W = a \frac{X}{\Phi} \ln \Phi.
$$
 (3)

The superpotential is singular at $\Phi = 0$ with monodromy²

$$
\Phi \to \Phi e^{2\pi i}, \qquad W \to W + 2\pi a i \frac{X}{\Phi}.
$$
 (4)

In field theory, singularity appears when a massless field is integrated out. An explicit realization of this monodromy will be provided based on supersymmetric field theory in the next section.

It is obvious that the Kähler potential preserves the global $U(1)$ symmetry for Φ , which is broken by the superpotential. Thus, our model is technically natural since there is a global $U(1)$ symmetry in the $a = 0$ limit [\[22\].](#page-5-2)

The F-term scalar potential is determined by the Kähler potential and superpotential as follows:

$$
V = e^K (K^{i\bar{j}} D_i W D_{\bar{j}} \bar{W} - 3W \bar{W}). \tag{5}
$$

As the field X is stabilized at $X = 0$, the above potential is significantly simplified as below,

FIG. 1 (color online). The helicoid potential with unit $10^{-8}M_p^4$.
Along radial direction, the minimum of the potential locates at Along radial direction, the minimum of the potential locates at $|\Phi| \equiv r = 1$, while the phase θ provides a flat direction along the helix line, from which it is easy to get super-Planckian field excursion.

$$
V = e^{\Phi \bar{\Phi}} W_X \bar{W}_{\bar{X}}
$$

= $a^2 e^{r^2} \frac{1}{r^2} ((\ln r)^2 + \theta^2),$ (6)

where $\Phi \equiv re^{i\theta}$. The quadratic term θ^2 appears in the potential because of the monodromy [\(4\)](#page-1-0) with respect to the origin.

The potential [\(6\)](#page-1-1) is simple but actually has fancy helicoid structure, as shown in Fig. [1](#page-1-2). The exponential factor e^{r^2} does not depend on the phase θ resulting from the global $U(1)$ symmetry of Kähler potential [\(2\)](#page-1-3); consequently there is no η problem for this phase inflation. The complex field magnitude $|\Phi| \equiv r$ obtains vacuum expectation value at $\langle r \rangle = 1$ as both $e^{r^2} \frac{1}{r^2}$ and $(\ln r)^2$ reach minimums at $r = 1$.
The mass along the radial direction is The mass along the radial direction is

$$
m_r^2 = \frac{1}{2} \frac{\partial^2 V}{\partial r^2}\bigg|_{r=1} = \left(2 + \frac{1}{\theta^2}\right) V_I,\tag{7}
$$

where the factor $\frac{1}{2}$ is from the normalization of r, and $V = e\sigma^2\theta^2$ is the notential for inflation Equation (7) $V_I = ea^2\theta^2$ is the potential for inflation. Equation [\(7\)](#page-1-4) shows that the mass of r is larger than the Hubble constant; therefore the radial component is frozen out during inflation, and we realize the quadratic inflation dominated by V_I . The helical inflation path is shown in Fig. [2](#page-2-0). The inflaton θ has physical mass $m_{\theta} = \sqrt{e}a$ at scale 10¹³ GeV from observations [2,31]. It predicts the spectral index from observations [\[2,3\].](#page-4-1) It predicts the spectral index

²An interesting proposal based on multivalueness of the complex function with fractional power is studied in [\[21\].](#page-5-3)

FIG. 2 (color online). Helix trajectory with $r = 1$. The red part indicates the phase excursion for quadratic inflation with $N_e = 55$.

 $n_s \approx 1 - \frac{2}{N_e}$ and the tensor-to-scalar ratio $r \approx \frac{8}{N_e}$, where N_e is the e-folding number.

In the PNGB inflation, the phase of the Higgs field also plays the role of the inflaton [\[11\].](#page-4-9) However, the potential is periodic and a super-Planckian decay constant is needed. In our model, the inflation path is helical; there is no limit on the field displacement during inflation. Actually this is a new realization of the monodromy, which is proposed as stringy axion inflation in a rather different way [\[17\].](#page-5-0)

The norm can be stabilized in the sub-Planckian scale by taking the following superpotential:

$$
W = aX\Phi^{-\frac{1}{n}}\ln\frac{\Phi}{\Lambda}.
$$
 (8)

The scalar potential becomes

$$
V = a^2 e^{r^2} r^{-\frac{2}{n}} ((\ln r - \ln \Lambda)^2 + \theta^2).
$$
 (9)

The minimum of the factor $e^{r^2} r^{-\frac{2}{n}}$ locates at $r_0 = \frac{1}{\sqrt{n}} (= \Lambda)$.
The mass along the radial direction at r_0 is The mass along the radial direction at r_0 is

$$
m_r^2 = \left(2 + \frac{n}{\theta^2}\right) V_I > H^2,\tag{10}
$$

where $V_I = (en)^{1/n} a^2 \theta^2$, providing a strong stabilization even though r is very small. Giving $n \geq 10$ the norm can be stabilized at $r_0 \sim O(10^{-1})(M_P)$.

III. MONODROMY FROM SUPERSYMMETRIC FIELD THEORY

To realize helical phase inflation, the monodromy [\(4\)](#page-1-0) of superpotential [\(3\)](#page-1-5) is crucial. The monodromy is from the superpotential

$$
W_0 = \sigma X \Psi (T - \delta) + Y(e^{-\alpha T} - \beta \Psi) + Z(\Psi \Phi - \lambda), \quad (11)
$$

in which the coupling constants of the last two terms are absorbed in the chiral superfields Y and Z, and $\sigma \ll 1$ to provide inflation potential at a scale much lower than that of the last two terms. The couplings in [\(11\)](#page-2-1) consist of renormalizable perturbative terms and $Ye^{-\alpha T}$, which is considered to be an effective description of a certain nonperturbative effect. A reasonable decay constant f is much smaller than Planck mass, so $\alpha \propto \frac{1}{f} \gg 1$. In type II string theory similar nonperturbative terms can be obtained from the D-brane instanton effect [\[23\].](#page-5-4)

The supergravity vacuum is given by the vanishing F-term conditions

$$
F_z = D_z W_0 = \partial_z W_0 + K_z W_0 = 0, \qquad (12)
$$

where $z \in \{X, Y, Z, T, \Psi, \Phi\}$. Combing with Minkowski vacuum condition $W_0 = 0$, the preferred vacuum is given by $\partial_z W_0 = 0$, and it locates at

$$
\langle X \rangle = \langle Y \rangle = \langle Z \rangle = 0, \qquad \langle T \rangle = \delta,
$$

$$
\langle \Psi \rangle = \frac{1}{\beta} e^{-a\delta}, \qquad \langle \Phi \rangle = \lambda \beta e^{a\delta}.
$$
 (13)

Giving $\langle \Phi \rangle \gg \langle \Psi \rangle$, near the vacuum Y, Z, T, Ψ obtain heavy effective masses from the last two coupling terms while X , Φ are light. During inflation all the heavy fields are frozen out and can be integrated out; then we get an effective field theory at inflation scale. To integrate out the heavy fields, we need to solve the equations of vanishing F terms of frozen fields

$$
F_Y = e^{-\alpha T} - \beta \Psi + K_Y W_0 = 0,
$$

\n
$$
F_Z = \Psi \Phi - \lambda + K_Z W_0 = 0.
$$
 (14)

In minimal supergravity, the Kähler potential is $K = \Sigma z \overline{z}^3$, which gives $K = \overline{z}$ Besides near the vacuum which gives $K_z = \overline{z}$. Besides, near the vacuum $Y = Z \approx 0 \ll M_P$, the higher order terms K_zW_0 in [\(14\)](#page-2-2) just give small corrections and we get the approximate solutions of Eq. [\(14\),](#page-2-2)

$$
\Psi = \frac{\lambda}{\Phi}, \qquad T = \frac{1}{\alpha} \ln \frac{\Phi}{\beta \lambda}.
$$
 (15)

³Except for *T*, for the reasons shown below, Kähler potential of has to be shift invariant under $T \rightarrow T + iC$. T has to be shift invariant under $T \rightarrow T + iC$.

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Substituting the above solutions for T and Ψ in the original superpotential W_0 , we get the effective superpotential [\(3\)](#page-1-5) during inflation. The parameters should satisfy

$$
\beta e^{a\delta} = \lambda^{-1} \gg 1, \qquad a = \frac{\sigma \lambda}{\alpha} \sim 10^{-5}, \tag{16}
$$

which can be easily adjusted to fit with observations.

The singularity of superpotential W at $\Phi = 0$ is clear from this procedure. When $\Phi \to 0$, we have $\Psi \gg \Phi$ con-strained by [\(14\)](#page-2-2) and it is illegal to integrate out Ψ , the model should be studied in another effective field theory. Fortunately during inflation $|\Phi|$ is fixed at vacuum expectation value and the phase rotation cannot break the effectiveness the theory given by W. As to the monodromy, vanishing conditions of F_y and F_z fix four directions of three complex fields T , Ψ , and Φ , but allow the transformation

$$
\Psi \to \Psi e^{-u-iv}
$$

\n
$$
\Phi \to \Phi e^{u+iv}
$$

\n
$$
T \to T + u/\alpha + iv/\alpha.
$$
\n(17)

However, because of the supergravity correction on the scalar potential $V \propto e^{K}$, norms of Ψ and Φ are stabilized; $u = 0$ in [\(17\)](#page-3-0). Field stabilization does not fix the phase rotation. and for a whole circular rotation, $W_0 \rightarrow W_0 + 2\pi \sigma i X \Psi/\alpha$, which is exactly the monodromy in [\(4\).](#page-1-0)

By integrating out the heavy fields, the supergravity correction e^{K} should be replaced by the solution of Eq. [\(14\)](#page-2-2) as well, which just gives norm-dependent terms and slightly shifts the fixed norm since K is invariant under phase rotation. Specifically, for T a shift symmetry in K is needed; otherwise the factor e^{K} contains the phase of Φ and breaks the inflation. Among these phase factors, the phase of Φ, after canonical field redefinition, has the lightest physical mass and evolves as inflaton.

At quantum level, because of the nonrenormalization theorem for the superpotential, the loop corrections from integrating out heavy fields appear in Kähler potential only, and these corrections just sightly affect the field stabilization but not the phase inflation which is protected by the $U(1)$ symmetry in Kähler potential.

IV. UV SENSITIVITY OF LARGE FIELD INFLATION

The crucial challenge for large field inflation is the higher dimensional operators from quantum gravity cor-rections [\[10\].](#page-4-8) The higher order terms of the inflaton ϕ ,

$$
\Delta V = c_i V \left(\frac{\phi}{M_P}\right)^i + \cdots, \qquad (18)
$$

are unignorable at the initial stage of inflation when $\phi \sim O(10)M_P$. They can modify the predictions significantly or even destroy slow-roll conditions. In this model, the inflaton is just the phase of a complex field like PNGB and admits no polynomial correction at all; in consequence quantum gravity corrections like [\(18\)](#page-3-1) immediately disappear without any constraint from extrasymmetry. So the helical phase inflation is not sensitive to the quantum gravity effects.

In the bottom-up approach, one can apply axionic shift symmetry of the inflaton $\phi \rightarrow \phi + c$, which is broken down to discrete symmetry $\phi \rightarrow \phi + 2\pi f$ by nonperturbative effect. To fit the experimental observations it requires super-Planckian axion decay constant f_2^5 which
can be realized by aligned axions [12] (or equally a S_2 can be realized by aligned axions $[12]$ (or equally a $S₂$) symmetry between two Kähler moduli [\[25\]\)](#page-5-5) or anomalous gauged $U(1)_X$ with large gauge symmetry [\[26\].](#page-5-6) The inflation path of aligned axions has similar helical structure in axion space [\[27,28\],](#page-5-7) and it shows that the alignment mechanism is the kind of monodromy inflation realized by axions that are plentiful in string compactification. Stringy inflation is expected to solve the UV sensitivity of large field inflation but needs to address several difficult problems like moduli stabilization, Minkowski or de Sitter vacua, etc. Our model provides another type of monodromy inflation just in supersymmetric field theory, which is more simpler and controllable. The $U(1)$ symmetry is built in the Kähler potential and there is no naturalness problem in the top-down perspective. Based on the supersymmetric field realization of inflation, a unified description of the inflation and the well-known GUT is at hand. A direct test on the relationship between inflation and GUT is the reheating process. In our model, a simple guess is that the chiral superfield X is a gauge singlet in a certain grand unification model, like the scenario in [\[29\]](#page-5-8); then the inflaton decays into visible particles through couplings of X during reheating.

V. CONCLUSION

We have shown in this article that the phase inflation along a single helix trajectory can be realized in a surprisingly simple way based on minimal supergravity. The global $U(1)$ symmetry of minimal Kähler potential naturally solves the η problem which appears generically for supergravity inflation. The radial direction is strongly stabilized during inflation, and the super-Planckian phase excursion is fulfilled along a helix path.

The helical phase inflation is not sensitive to the quantum gravity effect as higher order corrections are

⁴If the Kähler potential of T is minimal, then the supergravity rection $e^{T\bar{T}}$ would fix the phase rotation as well correction $e^{T\bar{T}}$ would fix the phase rotation as well.

⁵Giving a coupling between the inflaton kinetic term and Einstein tensor, natural inflation with $f \ll M_p$ still works [\[24\].](#page-5-9)

not possible for a PNGB-like particle. The phase inflation also admits an effective description on super-Planckian field excursion within supersymmetric field theory, and it naturally leads to field monodromy, which relates to a global $U(1)$ symmetry explicitly breaking at inflation scale. It is surprising that the supergravity η problem, field stabilization, monodromy inflation and the puzzle of super-Planckian field excursion admit a simple unified solution within a helicoid structure. As will be shown in [\[30\]](#page-5-10), the monodromy in [\(11\)](#page-2-1) can be easily generalized to obtain supersymmetric field realization of aligned axions with consistent field stabilization [\[12,27,28\]](#page-4-12), so the helical phase inflation actually provides a general frame to realize supergravity inflation with several amazing features. However, because inflation is an extraordinarily unusual and unique event in the

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history of our Universe, we are not hesitant in being bold. It will be phenomenal if nature employed helix structures to promote evolution from the very early Universe to present time organisms.

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