

# Renormalizable model for the Galactic Center gamma-ray excess from dark matter annihilation

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Evidence for an excess of gamma rays with  $\mathcal{O}(\text{GeV})$  energy coming from the center of our galaxy has been steadily accumulating over the past several years. Recent studies of the excess in data from the Fermi telescope have cast doubt on an explanation for the excess arising from unknown astrophysical sources. A potential source of the excess is the annihilation of dark matter into standard model final states, giving rise to gamma ray production. The spectrum of the excess is well fit by 30 GeV dark matter annihilating into a pair of  $b$  quarks with a cross section of the same order of magnitude as expected for a thermal relic. Simple models that can lead to this annihilation channel for dark matter are in strong tension with null results from direct detection experiments. We construct a renormalizable model where dark matter-standard model interactions are mediated by a pseudoscalar that mixes with the  $CP$ -odd component of a pair of Higgs doublets, allowing for the gamma ray excess to be explained while suppressing the direct detection signal. We consider implications for this scenario from Higgs decays, rare  $B$  meson decays and monojet searches and also comment on some difficulties that any dark matter model explaining the gamma ray excess via direct annihilation into quarks will encounter.

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## I. INTRODUCTION

One of the prime unanswered questions about our Universe is the nature of dark matter (DM). Evidence for DM is overwhelming, coming from a diverse set of observations, among them galactic rotation curves, cluster merging, and the cosmic microwave background (see, e.g. [1] and references therein). So far, dark matter has not been observed nongravitationally, yet the fact that a thermal relic with weak-scale annihilation cross section into standard model (SM) final states would have an energy density today that is compatible with dark matter measurements offers hope that this will be possible. The nongravitational interactions of DM are being searched for at particle colliders, in direct detection experiments, and in so-called indirect detection experiments, where the products of DM annihilation or decay are sought.

One final state in particular that is searched for in indirect detection experiments is gamma rays which can be produced by DM annihilating, either (i) directly to photons, which would result in an unambiguous line in the case of two body decays, or (ii) into other SM particles that then decay and produce photons in the cascade. The Fermi collaboration has published limits on DM annihilation [2] into final states containing photons.

Recently, evidence for such a signal has been mounting, with several groups [3–7] analyzing data from the Fermi Gamma Ray Space Telescope and finding an excess of gamma rays of energy  $\sim 1\text{--}3$  GeV in the region of the Galactic Center. This excess has a spectrum and spatial morphology compatible with DM annihilation. The potential for astrophysical backgrounds, in particular millisecond

pulsars in this case, to fake a signal is always a worry in indirect detection experiments. However, the observation that this gamma ray excess extends quite far beyond the Galactic Center lessens the possibility of astrophysical fakes [4], with recent studies finding the excess to extend to at least  $10^\circ$  from the Galactic Center [3,8].

The excess's spectrum has been fit by DM annihilating to a number of final states, depending on its mass, notably 10 GeV DM annihilating to  $\tau^+\tau^-$  (and possibly other leptons) [5,7,9,10] and 30 GeV DM to  $b\bar{b}$  [6,7,9,11]. The size of the excess is compatible with an annihilation cross section roughly equal to that expected for a thermal relic,  $\langle\sigma v_{\text{rel}}\rangle = 3 \times 10^{-26} \text{ cm}^3/\text{s}$ , suggesting that it is actually the result of DM annihilation.

30 GeV DM that annihilates to  $b$  quarks is particularly interesting, primarily because direct detection experiments have their maximal sensitivity to spin-independent interactions between nuclei and DM at that mass. Reconciling the extremely strong limit from direct detection in this mass range, presently  $8 \times 10^{-46} \text{ cm}^2$  [12], with a potential indirect detection signal poses a challenge, possibly offering a clue about the structure of the SM-DM interactions. We will focus on this DM mass and final state in this paper.

In the case of DM annihilation to SM fermions through an  $s$ -channel mediator, we can roughly distinguish the distribution of final states by the spin of the mediator. Spin-0 mediators tend to couple with strength proportional to mass—either due to inheriting their couplings from the Higgs or because of general considerations of minimal flavor violation—which results in decays primarily to the heaviest fermion pair kinematically allowed. On the other

hand, spin-1 mediators generally couple more democratically, leading to a more uniform mixture of final states. For this reason, the fact that the excess is well fit by 30 GeV DM annihilating dominantly to  $b\bar{b}$  suggests annihilation through a scalar. However, this is problematic: to get an appreciable indirect detection signal today requires scalar DM (fermionic DM annihilating through a scalar is  $p$ -wave suppressed) but this leads to a spin-independent direct detection cross section that is in conflict with experimental bounds, as mentioned above. Therefore, we are led to consider a pseudoscalar mediator, instead of a scalar, between the (fermionic) DM and the SM, leading to an effective dimension-six operator of the form

$$\mathcal{L}_{\text{eff}} = \frac{m_b}{\Lambda^3} \bar{\chi} i \gamma^5 \chi \bar{b} i \gamma^5 b, \quad (1)$$

where  $\chi$  is the DM. This operator has been singled out previously as a good candidate to describe the effective interaction between the SM and the dark sector [13,14]. It implies  $s$ -wave DM annihilation, which allows the gamma ray excess to be fit while having a large enough suppression scale  $\Lambda$  that it is not immediately ruled out by collider measurements of monojets/photons. The direct detection signal from this operator is spin-dependent and velocity-suppressed, rendering it safe from current constraints.

To move beyond the effective, higher dimensional operator in Eq. (1) requires confronting electroweak symmetry breaking because the SM portion of  $\mathcal{L}_{\text{eff}}$  is not an electroweak singlet:

$$\bar{b} i \gamma^5 b = i(\bar{b}_L b_R - \bar{b}_R b_L). \quad (2)$$

Therefore,  $\mathcal{L}_{\text{eff}}$  has to include the Higgs field (which would make it a singlet) which then gets a vacuum expectation value (VEV), implying a mediator which can couple to the Higgs.

It is easy to construct a scalar-scalar interaction between DM and the SM using the ‘‘Higgs portal’’ operator  $H^\dagger H$ , where  $H$  is the SM Higgs doublet, since it is a SM gauge singlet. This portal has been well explored in the literature, particularly in its connection to DM [15]. In this paper, however, we expand the Higgs sector of the SM to include a second doublet, which has enough degrees of freedom to allow for a pseudoscalar to mix with the dark matter mediator. In the presence of  $CP$  violation one could also induce a pseudoscalar-scalar coupling via this portal, however it is puzzling why a new boson with  $CP$  violating couplings would not also have a scalar coupling to the dark fermion. Including two Higgs doublets allows  $CP$  to be an approximate symmetry of the theory, broken by the SM fermion Yukawa coupling matrices. Tiny  $CP$  violating couplings will need to be included in order to renormalize the theory at high orders in perturbation theory, but we simply assume that all flavor and  $CP$  violation is derived from spurions proportional to the Yukawa coupling

matrices, and so has minimal effect on the Higgs potential and dark sector.

The outline of this paper is as follows. In Sec. II we introduce the two Higgs doublet model (2HDM) and the pseudoscalar mediator which mixes with the Higgs sector. We also discuss  $CP$  violation in the dark sector and in interactions between DM and SM fermions. We briefly discuss the annihilation cross section for our DM model in Sec. III. In Sec. IV, we catalog constraints on this model, such as direct detection, Higgs and  $B$  meson decays, and monojets. Section V contains our conclusions.

## II. THE MODEL

### A. $CP$ -conserving extended Higgs sector

As mentioned above, a straightforward way to couple dark matter to the SM through pseudoscalar exchange is by mixing the mediator with the pseudoscalar Higgs in a 2HDM.

For concreteness, we take the DM to be a Dirac fermion,  $\chi$ , with mass  $m_\chi$ , coupled to a real, gauge singlet, pseudoscalar mediator,  $a_0$ , through

$$\mathcal{L}_{\text{dark}} = y_\chi a_0 \bar{\chi} i \gamma^5 \chi. \quad (3)$$

The mediator couples to the SM via the Higgs portal in the scalar potential which is

$$V = V_{\text{2HDM}} + \frac{1}{2} m_{a_0}^2 a_0^2 + \frac{\lambda_a}{4} a_0^4 + V_{\text{port}}, \quad (4)$$

$$V_{\text{port}} = i B a_0 H_1^\dagger H_2 + \text{H.c.} \quad (5)$$

with  $H_{1,2}$  the two Higgs doublets.  $B$  is a parameter with dimensions of mass. We assume that  $\mathcal{L}_{\text{dark}}$  and  $V$  are  $CP$ -conserving (i.e.  $B$  and  $y_\chi$  are both real, and there is no  $CP$  violation in  $V_{\text{2HDM}}$ ) and we will comment on relaxing this assumption in Sec. II B. In this case,  $a_0$  does not develop a VEV. We write the most general  $CP$ -conserving 2HDM potential as

$$\begin{aligned} V_{\text{2HDM}} = & \lambda_1 \left( H_1^\dagger H_1 - \frac{v_1^2}{2} \right)^2 + \lambda_2 \left( H_2^\dagger H_2 - \frac{v_2^2}{2} \right)^2 \\ & + \lambda_3 \left[ \left( H_1^\dagger H_1 - \frac{v_1^2}{2} \right) + \left( H_2^\dagger H_2 - \frac{v_2^2}{2} \right) \right]^2 \\ & + \lambda_4 [(H_1^\dagger H_1)(H_2^\dagger H_2) - (H_1^\dagger H_2)(H_2^\dagger H_1)] \\ & + \lambda_5 \left[ \text{Re}(H_1^\dagger H_2) - \frac{v_1 v_2}{2} \right]^2 + \lambda_6 [\text{Im}(H_1^\dagger H_2)]^2, \end{aligned} \quad (6)$$

with all  $\lambda_i$  real. We have also imposed a  $\mathbb{Z}_2$  symmetry under which  $H_1 \rightarrow H_1$  and  $H_2 \rightarrow -H_2$  to suppress flavor-changing neutral currents, which is only softly broken by

$V_{2\text{HDM}}$  and  $V_{\text{port}}$ . The potential is minimized at  $\langle H_i \rangle = v_i/\sqrt{2}$ ,  $i = 1, 2$ , and the  $W$  and  $Z$  masses fix  $v_1^2 + v_2^2 = v^2 = (246 \text{ GeV})^2$ . The angle  $\beta$  is defined by  $\tan \beta = v_2/v_1$ . In unitary gauge we can decompose the doublets as

$$H_i = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}\phi_i^+ \\ v_i + \rho_i + i\eta_i \end{pmatrix}. \quad (7)$$

The spectrum contains a charged Higgs,

$$H^\pm = \sin \beta \phi_1^\pm - \cos \beta \phi_2^\pm, \quad (8)$$

with mass  $m_{H^\pm}^2 = \lambda_4 v^2/2$ .

The  $CP$ -even Higgs mass matrix in the  $(\rho_1, \rho_2)$  basis is  $\mathcal{M}_h^2$ , with

$$\begin{aligned} \mathcal{M}_{h11}^2 &= \frac{v^2}{2} [\lambda_5 s_\beta^2 + 4(\lambda_1 + \lambda_3) c_\beta^2], \\ \mathcal{M}_{h22}^2 &= \frac{v^2}{2} [\lambda_5 c_\beta^2 + 4(\lambda_2 + \lambda_3) s_\beta^2], \\ \mathcal{M}_{h12}^2 &= \mathcal{M}_{h21}^2 = \frac{v^2}{2} (\lambda_5 + 4\lambda_3) s_\beta c_\beta. \end{aligned} \quad (9)$$

We use  $s$  and  $c$  to denote sine and cosine here (and will do so intermittently throughout this paper along with  $t$  for tangent). The physical  $CP$ -even states are  $h$  and  $H$  ( $m_h \leq m_H$ ), related to  $\rho_{1,2}$  by

$$\begin{aligned} \begin{pmatrix} \rho_1 \\ \rho_2 \end{pmatrix} &= \begin{pmatrix} -\sin \alpha & \cos \alpha \\ \cos \alpha & \sin \alpha \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}, \\ \tan 2\alpha &= \frac{2\mathcal{M}_{h12}^2}{\mathcal{M}_{h11}^2 - \mathcal{M}_{h22}^2}, \end{aligned} \quad (10)$$

with masses

$$m_{h,H}^2 = \frac{1}{2} \left[ \mathcal{M}_{h11}^2 + \mathcal{M}_{h22}^2 \mp \sqrt{(\mathcal{M}_{h11}^2 - \mathcal{M}_{h22}^2)^2 + 4(\mathcal{M}_{h12}^2)^2} \right]. \quad (11)$$

We will use  $\xi_\psi^\phi$  to denote the strength of the coupling of the scalar  $\phi$  to  $\psi$  pairs (weak gauge bosons, quarks, and leptons) in units of SM Higgs coupling to those particles. The  $CP$ -even Higgs couplings to weak gauge bosons  $V = W, Z$  are rescaled by

$$\xi_V^h = \sin(\beta - \alpha), \quad \xi_V^H = \cos(\beta - \alpha). \quad (12)$$

The neutral, imaginary components of  $H_{1,2}$  combine to form a pseudoscalar,

$$A_0 = \sin \beta \eta_1 - \cos \beta \eta_2. \quad (13)$$

that mixes with  $a_0$  due to the portal coupling,

$$V_{\text{port}} = B a_0 A_0 [v + \sin(\beta - \alpha)h + \cos(\beta - \alpha)H]. \quad (14)$$

The  $CP$ -odd mass matrix in the  $(A_0, a_0)$  basis is

$$\mathcal{M}_A^2 = \begin{pmatrix} m_{A_0}^2 & Bv \\ Bv & m_{a_0}^2 \end{pmatrix}, \quad m_{A_0}^2 = \frac{\lambda_6 v^2}{2}. \quad (15)$$

Thus, the mass eigenstates,  $A$  and  $a$  are

$$\begin{aligned} \begin{pmatrix} A_0 \\ a_0 \end{pmatrix} &= \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} A \\ a \end{pmatrix}, \\ \tan 2\theta &= \frac{2Bv}{m_{A_0}^2 - m_{a_0}^2}, \\ m_{a,A}^2 &= \frac{1}{2} \left[ m_{A_0}^2 + m_{a_0}^2 \pm \sqrt{(m_{A_0}^2 - m_{a_0}^2)^2 + 4B^2 v^2} \right]. \end{aligned} \quad (16)$$

We can express  $B$  in terms of  $m_{a,A}$  and the mixing angle  $\theta$ ,

$$B = \frac{1}{2v} (m_A^2 - m_a^2) \sin 2\theta. \quad (17)$$

Written in terms of mass eigenstates and mixing angles,  $V_{\text{port}}$  becomes

$$\begin{aligned} V_{\text{port}} &= \frac{1}{2v} (m_A^2 - m_a^2) [s_{4\theta} a A + s_{2\theta}^2 (A^2 - a^2)] \\ &\quad \times [\sin(\beta - \alpha)h + \cos(\beta - \alpha)H]. \end{aligned} \quad (18)$$

The DM coupling to the mediator in Eq. (3) is simply expressed in terms of  $CP$ -odd mass eigenstates,

$$\mathcal{L}_{\text{dark}} = y_\chi (\cos \theta a + \sin \theta A) \bar{\chi} i \gamma^5 \chi. \quad (19)$$

We will work in a Type II 2HDM, where the Yukawa couplings of the SM fermions are

$$\mathcal{L}_{\text{Yuk}} = -\bar{L} Y_e H_1 e_R - \bar{Q} Y_d H_1 d_R - \bar{Q} Y_u \tilde{H}_2 u_R + \text{H.c.}$$

$Y_{e,d,u}$  are Yukawa matrices acting on the three generations (we employ first generation notation).  $L$  and  $Q$  are the left-handed lepton and quark doublets and  $e_R$ ,  $d_R$ , and  $u_R$  are the right-handed singlets. These couplings respect the  $\mathbb{Z}_2$  symmetry  $H_2 \rightarrow -H_2$  provided  $u_R \rightarrow -u_R$ . We can forbid the operator

$$\mathcal{L}_{\text{Yuk}} = -\bar{L} Y_\chi \tilde{H}_1 \chi_R + \text{H.c.}$$

by taking  $\chi \rightarrow -\chi$  under a separate  $\mathbb{Z}_2$ . Note  $\tilde{H}_i$  stands for  $i\sigma_2 H_i^*$ . Given these Yukawa interactions the couplings of the neutral scalar mass eigenstates are then rescaled from the SM Higgs values by

$$\xi_e^h = \xi_d^h = -\frac{\sin \alpha}{\cos \beta}, \quad \xi_u^h = \frac{\cos \alpha}{\sin \beta}, \quad (20)$$

$$\xi_e^H = \xi_d^H = \frac{\cos \alpha}{\cos \beta}, \quad \xi_u^H = \frac{\sin \alpha}{\sin \beta}, \quad (21)$$

$$\xi_e^A = \xi_d^A = \tan \beta \cos \theta, \quad \xi_u^A = \cot \beta \cos \theta, \quad (22)$$

$$\xi_e^a = \xi_d^a = -\tan \beta \sin \theta, \quad \xi_u^a = -\cot \beta \sin \theta. \quad (23)$$

To simplify the analysis, we work close to the decoupling limit of the 2HDM where

$$\lambda_1 \simeq \lambda_2 \simeq -\lambda_3 \simeq \frac{\lambda_4}{2} \simeq \frac{\lambda_5}{2} \simeq \frac{\lambda_6}{2} \equiv \lambda \gg 1. \quad (24)$$

Then,  $\alpha \simeq \beta - \pi/2$  and  $m_h \ll m_H \simeq m_{H^\pm} \simeq m_{A_0}$ . Since  $h$  has SM-like couplings in this limit, we identify it with the boson with mass 125 GeV recently discovered at the LHC. The degeneracy of  $H$  and  $H^\pm$  (and possibly  $A$ , given that we expect  $B$  to be somewhat small compared to  $m_{A_0}$ ) allows for precision electroweak constraints to be satisfied.

### B. Dark matter $CP$ problem

We now briefly discuss relaxing the assumption of  $CP$  conservation in the DM Yukawa interaction or in the scalar potential. If we write a general, possibly  $CP$ -violating, 4-Fermi interaction between quarks and DM that results after integrating out a spin-0 mediator as

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda^2} \frac{m_q}{v} \bar{\chi}(a_\chi + ib_\chi \gamma^5) \chi \bar{q}(a_q + ib_q \gamma^5) q, \quad (25)$$

we find an annihilation cross section for  $\chi\bar{\chi} \rightarrow b\bar{b}$  in the nonrelativistic limit, relevant for thermal freeze-out and indirect detection, of

$$\begin{aligned} \sigma v_{\text{rel}} &= \frac{1}{2\pi} \left( \frac{m_\chi m_b}{\Lambda^2 v} \right)^2 (b_\chi^2 + a_\chi^2 v_{\text{rel}}^2) (b_b^2 + a_b^2) \\ &\simeq 3 \times 10^{-26} \frac{\text{cm}^3}{\text{s}} \left( \frac{m_\chi}{30 \text{ GeV}} \right)^2 \left( \frac{54 \text{ GeV}}{\Lambda} \right)^4 \\ &\quad \times (b_\chi^2 + a_\chi^2 v_{\text{rel}}^2) (b_b^2 + a_b^2), \end{aligned} \quad (26)$$

with  $v_{\text{rel}}$  the relative velocity between  $\chi$  and  $\bar{\chi}$ . We have taken  $m_b \ll m_\chi$  and normalized on parameters that give the appropriate annihilation cross section for a thermal relic as well as the gamma ray excess. This operator also leads to a spin-independent cross section for DM scattering on a nucleon of

$$\begin{aligned} \sigma_{\text{SI}} &= \frac{\mu^2}{\pi} \left( \frac{\langle N | \sum_q a_q m_q \bar{q} q | N \rangle}{\Lambda^2 v} \right)^2 a_\chi^2 \\ &\simeq 2.6 \times 10^{-41} \text{ cm}^2 \left( \frac{54 \text{ GeV}}{\Lambda} \right)^4 \\ &\quad \times \left( \frac{\langle N | \sum_q a_q m_q \bar{q} q | N \rangle}{330 \text{ MeV}} \right)^2 a_\chi^2, \end{aligned} \quad (27)$$

where  $\mu$  is the reduced mass of the nucleon-DM system. The LUX experiment has set a limit of  $\sigma_{\text{SI}} < 8 \times 10^{-46} \text{ cm}^2$  [12] at a dark matter mass of 30 GeV, which highlights a problem for the general dimension-six operator in Eq. (25). The scalar-scalar coupling needs to be suppressed by about five orders of magnitude relative to the pseudoscalar-pseudoscalar coupling (which is why the latter has been focused on in the literature) without any good reason. If not, the stringent limits from direct detection preclude the possibility of an annihilation cross section large enough for an observable indirect detection signal or even to obtain the observed relic density and not overclose the Universe.

A scalar coupling of  $a$  to  $\chi$  is obtained if  $y_\chi$  in Eq. (3) has a nonzero imaginary component.  $a$  will also develop a scalar coupling to quarks if  $B$  in Eq. (5) is not real or if there is  $CP$  violation in the rest of the scalar potential. As highlighted above in the discussion of a general dimension-six interaction, (the product of) these  $CP$ -violating phases in  $y_\chi$  and  $V$  must be limited to less than about  $10^{-4}$  to  $10^{-5}$  (ignoring possible suppressions or enhancements at large  $\tan \beta$ ). That is, in addition to the usual EDM constraints on  $CP$ -violating phases in the scalar potential (see, e.g. [16]), these models face tests from direct detection experiments (which become probes of  $CP$  violation).

$CP$  is not an exact symmetry of the SM; indeed, we expect to see even larger violations of  $CP$  in physics beyond the SM because of baryogenesis. In this light, simply asserting that these new interactions respect  $CP$  seems a little peculiar. It is however technically natural to assume that spurions proportional to the SM Yukawa coupling matrices are the only source of  $CP$  and flavor violation, with the consequence that  $CP$ -violating couplings outside of the CKM are tiny.

Should the evidence for this gamma ray signal remain or increase, understanding the smallness of these  $CP$ -violating couplings will pose a model-building challenge and hint about the structure of the new physics, much like the  $CP$  problems encountered in other models of physics beyond the SM.

### III. DARK MATTER ANNIHILATION

For  $m_a \ll m_A$ , the dark matter annihilates to SM particles primarily through  $s$ -channel  $a$  exchange. The velocity averaged annihilation cross section for  $\chi\bar{\chi} \rightarrow \text{SM}$  in the nonrelativistic limit is

$$\langle\sigma v_{\text{rel}}\rangle = \frac{y_\chi^2 m_\chi^2}{8\pi m_a^4} s_{2\theta}^2 \tan^2\beta \left[ \left(1 - \frac{4m_\chi^2}{m_a^2}\right)^2 + \frac{\Gamma_a^2}{m_a^2} \right]^{-1} \times \sum_{f=b,\tau,\dots} N_C \frac{m_f^2}{v^2} \sqrt{1 - \frac{m_f^2}{m_a^2}}. \quad (28)$$

The sum is over down-type quarks ( $N_C = 3$ ) and charged leptons ( $N_C = 1$ ) since  $a$ 's coupling to up-type quarks is suppressed by  $1/\tan\beta$ . Evaluating this at the experimentally favored DM mass of 30 GeV, taking  $m_a = 100$  GeV (and ignoring  $\Gamma_a$ ) gives

$$\langle\sigma v_{\text{rel}}\rangle = 3 \times 10^{-26} \frac{\text{cm}^3}{\text{s}} \left( \frac{y_\chi \sin 2\theta \tan\beta}{2.4} \right)^2. \quad (29)$$

We see that it is possible to achieve values of the annihilation cross section compatible with the gamma ray excess and relic density constraints with modest values of the mixing angle  $\theta$ , provided  $\tan\beta$  is somewhat large. At this value of  $m_\chi$  and for  $\tan\beta$  larger than a few, the  $b\bar{b}$  final state accounts for about 90% of the annihilation cross section with  $\tau^+\tau^-$  making up nearly all the rest. This is in line with what is suggested by fits to the gamma ray excess.

The general requirement that  $\tan\beta$  is large will help focus the mass scale of the heavy Higgs bosons. CMS's search for heavy neutral minimal supersymmetric standard model (MSSM) Higgses decaying to  $\tau^+\tau^-$  [17] applies straightforwardly in this case, since the Higgs sector is the same as in the MSSM. The production cross section for  $pp \rightarrow (H/A) + X$  is enhanced at large  $\tan\beta$  so the lack of a signal sets an upper limit on  $\tan\beta$  as a function of  $m_{A,H}$ . This limit is roughly  $\tan\beta < 10$  at  $m_{A,H} = 300$  GeV, and weakens to  $\tan\beta < 60$  at  $m_{A,H} = 900$  GeV.

#### IV. CONSTRAINTS ON THE DARK SECTOR

In this section we investigate the limits on the mediator mass and the mixing angle between the mediator and the pseudoscalar of the 2HDM. Taking the heavy Higgs search described above into account, we fix the other parameters to the benchmark values  $m_H = m_{H^\pm} \approx m_A = 800$  GeV,  $\tan\beta = 40$ ,  $\alpha = \beta - \pi/2$ , and  $y_\chi = 0.5$  and comment on changing these later. We first consider the spin-independent direct detection cross section induced at one-loop. Current limits from direct detection experiments do not constrain this model, but future searches can possibly probe interesting regions of parameter space. We next consider Higgs decays to the pseudoscalar mediator. Searches for  $h \rightarrow b\bar{b}$  can be used to put bounds to  $h \rightarrow aa \rightarrow 4b$  decays for  $m_h > 2m_a$  and future  $h \rightarrow 2b2\mu$  searches could probe much more of the  $m_a$ - $\theta$  parameter space. Indirect limits on the branching for  $h \rightarrow aa$  from global Higgs property fits are also quite constraining. We then consider changes to the  $B_s \rightarrow \mu^+\mu^-$  branching ratio. Since this has been measured to be very close to its SM value, it is particularly

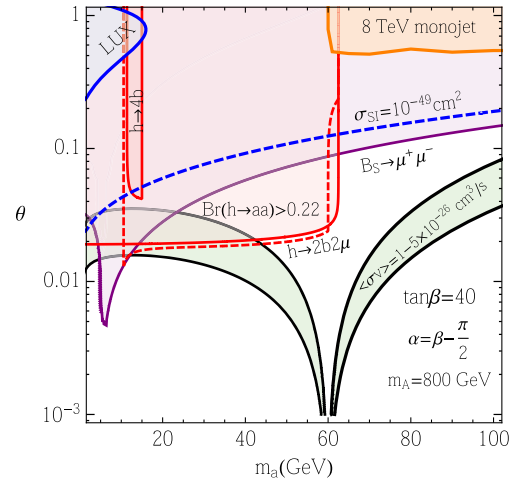


FIG. 1 (color online). Regions of mixing angle  $\theta$  vs  $m_a$  that are ruled out or suggested by various measurements. We have fixed  $m_{H,H^\pm} \approx m_A = 800$  GeV,  $\tan\beta = 40$ ,  $\alpha = \beta - \pi/2$ , and  $y_\chi = 0.5$ . The area that gives an annihilation cross section of  $\langle\sigma v_{\text{rel}}\rangle = 1-5 \times 10^{-26}$   $\text{cm}^3/\text{s}$  as indicated by fits to the gamma ray excess is between the solid black lines (shaded in green). The shaded purple region above the solid purple line is in  $2\sigma$  conflict with the LHCb measurement of  $B_s \rightarrow \mu^+\mu^-$ . The darker red region with the solid outline is ruled out by  $h \rightarrow b\bar{b}$  constraints on the  $h \rightarrow 4b$  signal. The larger, lighter red region with a solid outline is ruled out from the indirect limit  $\text{Br}(h \rightarrow aa) < 0.22$  coming from fits to Higgs properties, assuming SM Higgs production. The dashed red line shows the area that could be probed by limiting  $\text{Br}(h \rightarrow aa \rightarrow 2b2\mu) \lesssim 10^{-4}$ . The blue region labeled LUX is in conflict with the limit  $\sigma_{\text{SI}} < 8 \times 10^{-46}$   $\text{cm}^2$  while the area above the blue dashed line leads to  $\sigma_{\text{SI}} > 10^{-49}$   $\text{cm}^2$ , potentially accessible at the next generation of direct detection experiments. The orange region shows the area ruled out by a mono- $b$ -jet search at 8 TeV with  $20 \text{ fb}^{-1}$  of data. See text for details.

constraining for a light mediator. Finally, we consider monojet searches. Our main results are summarized in Fig. 1.

#### A. Direct detection

One of the virtues of this model is that single pseudo-scalar exchange between  $\chi$  and quarks leads to (highly suppressed) spin-dependent scattering of the DM on nuclei [13,14]. At one-loop, however, spin-independent interactions are generated through the diagrams shown in Fig. 2. The top diagram (plus its crossed version) leads to an effective interaction between  $\chi$  and  $b$  quarks at zero momentum transfer given by

$$\mathcal{L}_{\text{box}} = \sum_{q=d,s,b} \frac{m_q^2 y_\chi^2 \tan^2\beta \sin^2 2\theta}{128\pi^2 m_a^2 (m_\chi^2 - m_q^2)} \times \left[ F\left(\frac{m_\chi^2}{m_a^2}\right) - F\left(\frac{m_q^2}{m_a^2}\right) \right] \frac{m_\chi m_q}{v^2} \bar{\chi}\chi \bar{q}q. \quad (30)$$

The function  $F$  is given in the Appendix in Eq. (A1).

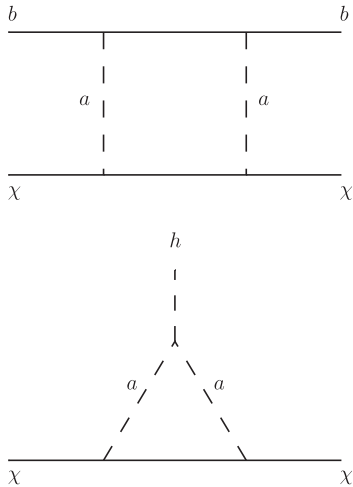


FIG. 2. Diagrams that (with the crossed top diagram) lead to spin-independent DM-nucleon scattering. The  $b$  quarks in the top diagram can also be replaced by  $d$  and  $s$  quarks.

The bottom diagram of Fig. 2 leads to a DM-Higgs coupling of

$$\mathcal{L}_{h\chi\chi} = -\frac{(m_A^2 - m_a^2) \sin^2 2\theta y_\chi^2}{64\pi^2 m_a^2} G(x_\chi, x_q) \frac{m_\chi}{v} h \bar{\chi}\chi, \quad (31)$$

where  $x_\chi = m_\chi^2/m_a^2$ ,  $x_q = q^2/m_a^2$ , and  $q$  is the momentum transfer between  $\chi$  and  $\bar{\chi}$ .  $G$  is given in Eq. (A3). This leads to an effective 4-fermion interaction relevant for spin-independent nucleon scattering,

$$\mathcal{L}_h = \frac{(m_A^2 - m_a^2) s_{2\theta}^2 y_\chi^2}{64\pi^2 m_h^2 m_a^2} G(x_\chi, 0) \frac{m_\chi m_q}{v^2} \bar{\chi}\chi \bar{q}q. \quad (32)$$

We have assumed  $\alpha = \beta - \pi/2$  which results in SM-like couplings of  $h$  to quarks,  $-s_\alpha/c_\beta = c_\alpha/s_\beta = 1$ . For

$$\tan \beta \lesssim 100 \left( \frac{m_A}{800 \text{ GeV}} \right), \quad (33)$$

the Higgs exchange contribution to direct detection dominates over the box diagram, leading to a spin-independent cross section for scattering on a nucleon of

$$\begin{aligned} \sigma_{\text{SI}} \approx & 2.2 \times 10^{-49} \text{ cm}^2 \left( \frac{m_A}{800 \text{ GeV}} \right)^4 \left( \frac{50 \text{ GeV}}{m_a} \right)^4 \\ & \times \left( \frac{m_\chi}{30 \text{ GeV}} \right)^2 \left( \frac{\theta}{0.1} \right)^4 \left( \frac{y_\chi}{0.5} \right)^4 \left( \frac{\langle N | \sum_q m_q \bar{q}q | N \rangle}{330 \text{ MeV}} \right)^2, \end{aligned} \quad (34)$$

using a value of the  $\bar{q}q$  matrix element from Ref. [18]. Cross sections at the  $10^{-48}$  to  $10^{-49}$   $\text{cm}^2$  level are potentially observable at the next generation of direct detection experiments [19]. The loop suppression of the

spin-independent cross section, however, is sufficient for this model to remain safe from direct detection experiments for the near future.

In Fig. 1, we show the area of parameter space ruled out by the LUX limit of  $8 \times 10^{-46}$   $\text{cm}^2$  on a spin-independent cross section that arises from the loop diagrams above. Only areas of very large mixing angle  $\theta$  and small  $m_a$  are impacted. We also show the area that can be probed by a future cross section limit of  $10^{-49}$   $\text{cm}^2$  which covers a much larger region.

## B. Higgs decays

If  $m_a < m_h$ , the Higgs can decay into final states involving  $a$  and, in particular, when  $m_a < m_h/2$ , the two body mode  $h \rightarrow aa$  opens up. Using Eq. (18) with  $\sin(\beta - \alpha) = 1$ , the rate is

$$\begin{aligned} \Gamma(h \rightarrow aa) &= \frac{(m_A^2 - m_a^2)^2 \sin^4 2\theta}{32\pi m_h v^2} \sqrt{1 - \frac{4m_a^2}{m_h^2}} \\ &\approx 840 \text{ MeV} \left( \frac{m_A}{800 \text{ GeV}} \right)^4 \left( \frac{\theta}{0.1} \right)^4, \end{aligned} \quad (35)$$

having taken  $m_a \ll m_h, m_A$  in the second line. Since the width of the SM Higgs is 4 MeV, this can impact LHC measurements that broadly indicate that  $h$  is SM-like to  $\sim 10$ – $20\%$  if  $\theta \gtrsim \text{few} \times 10^{-2} (800 \text{ GeV}/m_A)$ .

This mode requires  $m_a < m_h/2 \approx 2m_\chi$ , so the pseudo-scalars will primarily go to  $b$  quarks with a small branching to  $\tau$  and  $\mu$  pairs. The  $h \rightarrow aa \rightarrow 4b$  signal will contribute to  $h \rightarrow b\bar{b}$  searches [20]. A CMS search in  $W/Z$ -associated production at 7 and 8 TeV,  $pp \rightarrow (W/Z) + (h \rightarrow b\bar{b})$  [21], sets a limit  $\text{Br}(h \rightarrow aa \rightarrow 4b) < 0.7$  for  $2m_b < m_a < 15$  GeV. This can potentially be improved to 0.2 with  $100 \text{ fb}^{-1}$  data at the 14 TeV LHC. For larger  $m_a$ , there are no current limits. Additionally, the  $h \rightarrow 2b2\mu$  final state can offer a probe comparable to  $4b$ , with its relative cleanliness compensating for its rarity. Current 7 and 8 TeV data can limit this to  $\text{Br}(h \rightarrow aa \rightarrow 2b2\mu) \lesssim 10^{-3}$  for  $m_a > 25$  GeV. The 14 TeV run with  $100 \text{ fb}^{-1}$  data can improve this limit to  $10^{-4}$  [20].

Taking the branching ratios of  $a$  into account, the limits above translate into a limit  $\text{Br}(h \rightarrow aa) \lesssim 0.9$  for  $2m_b < m_a < 15$  GeV currently, with the possibility of improving this to  $\text{Br}(h \rightarrow aa) \lesssim 0.1$ – $0.2$  in the future.

Since we are in the decoupling limit, the production cross section of the Higgs is unchanged from its SM value in this model (unless we add further states). Therefore there are strong limits on unobserved final states, such as  $aa$ , that would dilute the signal strength in the observed channels. Given current data, this limits  $\text{Br}(h \rightarrow aa) < 0.22$  [22].

The decay  $h \rightarrow \chi\bar{\chi}$  through the bottom diagram in Fig. 2 is loop-suppressed and offers no meaningful constraints. For larger  $m_a$ , the three-body decays  $h \rightarrow aa^*$ ,  $aA^*$  become the dominant exotic Higgs decay modes, but are suppressed

by the extra particle in the final state and are also not constraining.

We show the limits on the mixing angle as a function of  $m_a$  coming from the determination  $\text{Br}(h \rightarrow aa \rightarrow 4b) < 0.7$  as well as the indirect constraint  $\text{Br}(h \rightarrow aa) < 0.22$  in Fig. 1. We also show the limit that can be set by a future measurement of  $\text{Br}(h \rightarrow aa \rightarrow 2b2\mu) < 10^{-4}$ .  $h \rightarrow aa$  decays provide strong constraints when kinematically allowed, i.e.  $m_a \lesssim 60$  GeV.

### C. B physics constraints

A light  $a$  can also potentially be constrained by its contributions to the decay  $B_s \rightarrow \mu^+\mu^-$ . For  $m_a \ll m_Z$ , the correction due to s-channel  $a$  exchange can be simply written as [23]

$$\text{Br}(B_s \rightarrow \mu^+\mu^-) \simeq \text{Br}(B_s \rightarrow \mu^+\mu^-)_{\text{SM}} \times \left| 1 + \frac{m_b m_{B_s} t_\beta^2 s_\theta^2 f(x_t, y_t, r)}{m_{B_s}^2 - m_a^2 Y(x_t)} \right|^2, \quad (36)$$

with  $x_t = m_t^2/m_W^2$ ,  $y_t = m_t^2/m_{H^\pm}^2$ ,  $r = m_{H^\pm}^2/m_W^2$ ,

$$f(x, y, r) = \frac{x}{8} \left[ -\frac{r(x-1) - x}{(r-1)(x-1)} \log r + \frac{x \log x}{(x-1)} - \frac{y \log y}{(y-1)} + \frac{x \log y}{(r-x)(x-1)} \right], \quad (37)$$

and  $Y(x)$  the usual Inami-Lim function,

$$Y(x) = \frac{x}{8} \left[ \frac{x-4}{x-1} \log x + \frac{3x \log x}{(x-1)^2} \right]. \quad (38)$$

The average of the LHCb and CMS measurements of this mode is  $\text{Br}(B_s \rightarrow \mu^+\mu^-) = (2.9 \pm 0.7) \times 10^{-9}$  [24]. This should be compared against the SM prediction, which we take to be  $(3.65 \pm 0.23) \times 10^{-9}$  [25]. This offers a strong test of the model, especially for a light  $a$ , which we show in Fig. 1.

### D. Collider probes

Monojet and monophoton searches have become standard techniques to look for dark matter at hadron colliders in recent years (see, e.g. [26]).

To estimate the reach that such searches might have in this model, we make use of a recent analysis [27] designed to probe dark matter that couples preferentially to heavy quarks, taking advantage of  $b$ -tagging a jet recoiling against missing energy to cut down substantially on backgrounds.

For our signal, we use MadGraph 5 [28] to generate matched samples of  $\chi\bar{\chi} + (0, 1, 2)j$  (with  $j$  representing both  $b$ - and light flavor/gluon-jets), shower and hadronize with PYTHIA 6 [29], and use DELPHES 2 [30] for detector simulation. We take a 50%  $b$ -tag efficiency for  $p_T > 80$  GeV, which measurements from CMS [31] and

ATLAS [32] show is conservative (a larger efficiency would lead to stronger limits).

The most useful signal region defined in Ref. [27] for this model has the following requirements: (i) missing transverse energy greater than 350 GeV, (ii) no more than two jets with  $p_T > 50$  GeV, (iii) the leading jet has  $p_T > 100$  GeV and is  $b$ -tagged, (iv) no isolated leptons, and (v) if there is a second jet, its separation in azimuthal angle with respect to the missing energy is  $\Delta\phi > 0.4$ . Using backgrounds estimated in [27] at the 8 TeV LHC (mainly  $Z + \text{jets}$  and  $t\bar{t} + \text{jets}$ ), we can identify regions of parameter space that can be expected to be probed by this search with  $20 \text{ fb}^{-1}$  of data. Monojet searches of this type are most sensitive when  $m_a > 2m_\chi$  since then  $a$  can be produced on-shell and decay to  $\chi\bar{\chi}$ . If  $m_a < 2m_\chi$  the reach substantially weakens due to the additional particle in the final state and the softness of the missing energy since the  $\chi\bar{\chi}$  pair tends to be created close to threshold.

This model is relatively less well constrained by monojet searches than the EFTs studied in Refs. [13] and [27] because of the suppressed coupling to top at large  $\tan\beta$ . The values of  $\theta$  as a function of  $m_a$  that would be ruled out by the search described above are shown in Fig. 1. Extending this search to  $100 \text{ fb}^{-1}$  of 14 TeV data could improve the reach in  $\theta$  by a factor of  $\sim 3$  [27].

## V. CONCLUSIONS AND OUTLOOK

An excess in gamma rays from the Galactic Center as measured by the Fermi Gamma Ray Space Telescope can be explained by 30 GeV DM annihilating dominantly into  $b\bar{b}$  pairs. To do so while eluding bounds on spin-independent scattering of DM on nuclei suggests that the mediator between the dark sector and the SM is a pseudoscalar. We have studied a 2HDM where the pseudoscalar mediator mixes with the  $CP$ -odd Higgs, giving rise to interactions between DM and the SM.

At one-loop, scalar-scalar interactions between DM and SM quarks arise. This leads to a spin-independent cross section for direct detection well below the current bound of  $8 \times 10^{-46} \text{ cm}^2$  at a dark matter mass of 30 GeV. Future limits at better than  $10^{-49} \text{ cm}^2$  could impact this model. We also consider decays of the 125 GeV SM-like Higgs boson involving the mediator. If the mediator is light  $h \rightarrow aa \rightarrow 4b, 2b2\mu$  can be constraining with data from the 14 TeV LHC. Additional contributions to  $B_s \rightarrow \mu^+\mu^-$  in this model eliminate some of the favored parameter space for  $m_a < 10$  GeV. This scenario is not well tested by monojet searches, including ones that rely on  $b$ -tagging to increase the sensitivity to DM coupled to heavy quarks, due to a suppressed coupling of the mediator to  $t$  quarks.

Changing the benchmark parameters that we used above does not greatly change the general results. For example, if we lower  $m_A$  to decrease the  $h \rightarrow aa$  signal coming from Eq. (18), we have to decrease  $\tan\beta$  because of the CMS heavy Higgs search [17]. Then, to obtain the correct

annihilation cross section in Eq. (28), we have to increase the mixing angle (or, equivalently,  $B$ ) which in turn increases the  $h \rightarrow aa$  rate.

One obvious piece of evidence in favor of this scenario would be finding heavy Higgses at the LHC. However, conclusively determining whether these heavy Higgses are connected to 30 GeV DM annihilating at the center of the galaxy will be a formidable challenge. Among the possible signatures to probe this scenario is  $A \rightarrow ha \rightarrow 2b + \text{inv}$ . We leave a detailed study of this search and others for future work.

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*Note added.*—While this work was in preparation Refs. [33,34] appeared, with some overlapping results.

### APPENDIX: LOOP FUNCTIONS

We provide expressions for the loop functions presented above in this appendix.

The form factor needed for the box diagrams in Eq. (30) is given by

$$F(x) = \frac{2}{3x} [4 + f_+(x) + f_-(x)], \quad (\text{A1})$$

with

$$f_{\pm}(x) \equiv \frac{1}{x} \left( 1 \pm \frac{3}{\sqrt{1-4x}} \right) \left( \frac{1 \pm \sqrt{1-4x}}{2} \right)^3 \times \log \left( \frac{1 \pm \sqrt{1-4x}}{2} \right). \quad (\text{A2})$$

$F$  vanishes when its argument is small as  $F(x \rightarrow 0) \rightarrow (4x/3) \log(1/x)$ .

The function arising in the effective  $\chi\text{-}\chi\text{-}h$  interaction in Eq. (31) is

$$G(x, y) = -4i \int_0^1 dz \frac{z}{\lambda^{1/2}(x, y, z)} \times \log \left[ \frac{\lambda^{1/2}(x, y, z) + iy(1-z)}{\lambda^{1/2}(x, y, z) - iy(1-z)} \right], \quad (\text{A3})$$

with

$$\lambda(x, y, z) \equiv y[4(1-z) + 4xz^2 - y(1-z)^2]. \quad (\text{A4})$$

For small arguments  $G$  approaches unity,  $G(0, 0) = 1$ .

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