PHYSICAL REVIEW D 90, 014007 (2014)

Stabilizing electroweak vacuum in a vectorlike fermion model

Ming-Lei Xiao^{1,*} and Jiang-Hao Yu^{1,2,†}

¹Theory Group, Department of Physics, The University of Texas at Austin, Austin, Texas 78712, USA

²Texas Cosmology Center, The University of Texas at Austin, Austin, Texas 78712, USA

(Received 14 April 2014; published 3 July 2014; publisher error corrected 7 July 2014)

To avoid possible electroweak vacuum instability in the vectorlike fermion model, we introduce a new singlet scalar to the model, which couples to the vectorlike fermion and also mixes with the Higgs boson after spontaneous symmetry breaking. We investigate the vectorlike fermion predominantly coupled to the third-generation quarks, and its mass is generated from the vacuum expectation value of the new scalar field in the model. In this setup, as running towards high energies, the new scalar provides a positive contribution to the running of the Higgs quartic coupling, and the matching on the scale of the scalar mass gives rise to a threshold effect that lifts up the Higgs quartic coupling strength. The two effects help stabilize the electroweak vacuum of the Higgs potential. Therefore, this setup could evade possible vacuum instability in the vectorlike fermion model. We show that a large range of parameter space is allowed to have both stable Higgs vacuum and perturbativity of all the running couplings, up to the Planck scale. We also examine the experimental constraints from the electroweak precision observables such as oblique corrections S,T and nonoblique corrections to the $Zb_L\bar{b}_L$ coupling, the Higgs coupling precision measurements, and the current LHC direct searches.

DOI: 10.1103/PhysRevD.90.014007 PACS numbers: 14.65.Jk, 12.60.-i, 11.10.Hi

I. INTRODUCTION

The discovery of the Higgs-like scalar boson at the Large Hadron Collider (LHC) is the great triumph of the standard model (SM) of particle physics. The Higgs boson mass was measured at the ATLAS and CMS with reasonable accuracy: $m_h = 125.9 \pm 0.4$ GeV [1]. Now that all the parameters of the SM are determined by experimental data, the completion of the SM evoked our interest in its high energy behavior such as Higgs vacuum stability. The measured value of the Higgs boson mass leads to a very intriguing situation. The most accurate analysis of the electroweak vacuum stability in the SM was performed in Refs. [2,3], showing that the theory sits near the boundary between a stable phase and an instable phase of the vacuum structure if there is no new physics (NP) beyond the SM. Therefore, NP should be introduced to stabilize the electroweak vacuum of the Higgs potential.

There are already many kinds of NP models available to address the TeV scale physics. These models involve various extensions of the scalar sector, fermion sector, and/or gauge boson sector of the SM. The Higgs vacuum stability serves as a criterion to justify the high energy behavior of these NP models [4]. Among these, the models with an extended fermion sector would worsen the potential instability [5–8]. We will focus on a vectorlike fermion model predominantly coupled to the third-generation quarks [9–13] and manage to improve the stability of the electroweak vacuum by modifying its particle content.

The vectorlike fermion model is less constrained by the experimental data than the models with extra chiral fermions. Because of nondecoupling behavior of the chiral fermion, the electroweak data from the precision measurements, the Higgs coupling measurements, and the LHC direct searches put very strong limits on its parameter space [14,15]. Moreover, due to the tight constraints on the light quarks from flavor physics, the heavy vectorlike fermion cannot significantly couple to the first two generations.

In order to find out the true vacuum state and analyze its stability, we need to investigate the Higgs effective potential. Since the instability occurs at energies much higher than the electroweak scale, the effective potential is well approximated by the renormalization group (RG) improved tree-level expression for the large field values $h \gg v = 246 \text{ GeV}$ [3]:

$$V_{\rm eff}(h) = \frac{\lambda(\mu)}{4} h^4,\tag{1}$$

where the Higgs quartic coupling $\lambda(\mu)$ runs with the renormalization scale μ . Generally speaking, if the Higgs quartic coupling $\lambda(\mu)$ becomes negative, the effective potential becomes instable through developing a minimum much deeper than the realistic minimum. As we know, in the SM the Higgs quartic coupling becomes negative at around 10^{10} GeV according to complete next-to-next-to-leading order calculation of the running Higgs quartic coupling [2]. As shown in Fig. 3 of Ref. [3], in which the measured uncertainties of the top quark and the Higgs masses are taken into account, the SM Higgs vacuum state lies in a narrow region of the metastable phase. In the

^{*}mingleix@utexas.edu

jhyu@utexas.edu

vectorlike fermion model, the new vectorlike fermion has negative contributions to the β function of the running Higgs quartic coupling, which drives the Higgs potential towards the absolute instable phase.

To cure the potential instability in the vectorlike fermion model, we would like to modify the particle content and interactions in the model. In the RG running, new bosonic particles provide positive contributions to the running of the Higgs quartic coupling, while new fermionic particles contribute negatively. Although there may be many possible ways to extend the model, here we suggest a very simple and economical extension by adding a new scalar singlet to the vectorlike fermion model. This new singlet scalar couples to the Higgs boson and thus provides a positive contribution to the running of the Higgs quartic coupling. However, if the new scalar couples only to the Higgs boson but not to others, the quartic coupling of the new scalar will increase as the energy goes higher and higher. Thus it is likely that the scalar quartic coupling by itself runs into a nonperturbativity region at or below the Planck scale. To avoid this possible problem, we require that the new scalar couples to the vectorlike fermion, which provides a negative contribution to the running of the scalar quartic coupling and thus controls the growth of the scalar quartic coupling strength at high energies. We assume that the new scalar singlet has a nonzero vacuum expectation value (VEV). To make the model more predictive, this VEV also generates the mass term for the vectorlike fermion. In this setup, there are two effects to lift up the running Higgs quartic coupling strength. First, the new scalar provides a positive contribution to the β function of the running Higgs quartic coupling. Second, in the matching on the scale of the scalar mass, the Higgs quartic coupling obtains a positive threshold shift [4,16]. Therefore, the new scalar could stabilize the electroweak vacuum of the Higgs potential, and this setup could evade possible vacuum instability in the vectorlike fermion model.

The paper is organized as follows. In the next section, we set up the Lagrangian of the model and obtain the mass spectrum in the model. In Sec. 3, we present a study of vacuum stability through the one-loop renormalization group running. The matchings between different energy scales are carefully treated. We consider the theoretical bounds on the masses of the heavy particles from perturbative unitarity in Sec. 4. In Sec. 5, the precision electroweak observables, including the oblique corrections S, T and nonoblique corrections to the $Zb_L\bar{b}_L$ couplings, are examined. In Sec. 6, we perform a global fit on the Higgs coupling precision measurements and put constraints on the parameter space. Then we discuss the direct searches on the heavy scalar and the vectorlike fermion. Finally, we summarize the constraints on the parameter spaces in the conclusion section. In Appendix A, we provide details of the relevant electroweak Lagrangian in the model. In

Appendix B, we list the one-loop renormalization group equations. Appendix C presents the detailed calculations on the oblique corrections. In Appendix D, we list the partial decay widths of the heavy particles.

II. THE MODEL

We consider an extension of the SM, by adding a vectorlike fermion singlet ψ with charge +2/3, and a real neutral singlet scalar χ . Since the vectorlike fermion has the same quantum number as the right-handed up-type quarks, they will mix together. Because of the tight constraints on the up and charm quarks from flavor physics, we assume the vectorlike fermion mixes only with the top quark as a fermionic top partner. The new scalar interacts with the Higgs doublet in the potential, which induces mixing between the scalar and the SM Higgs boson after spontaneous symmetry breaking.

The scalar potential reads

$$V(\Phi,\chi) = -\mu_H^2 \Phi^{\dagger} \Phi + \lambda_H (\Phi^{\dagger} \Phi)^2$$
$$-\frac{\mu_S^2}{2} \chi^2 + \frac{\lambda_S}{4} \chi^4 + \frac{\lambda_{SH}}{2} (\Phi^{\dagger} \Phi) \chi^2, \qquad (2)$$

where Φ is the SM Higgs doublet

$$\Phi = \begin{pmatrix} \pi^+ \\ \frac{1}{\sqrt{2}} (\phi + i\pi^0) \end{pmatrix}. \tag{3}$$

Requiring the scalar potential to be positive for asymptotically large values of the fields, we obtain the following conditions:

$$4\lambda_S\lambda_H > \lambda_{SH}^2, \qquad \lambda_H > 0, \qquad \lambda_S > 0.$$
 (4)

In general, the scalar potential develops nonzero vacuum expectation values for both the Higgs and the singlet:

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}, \qquad \langle \chi \rangle = u,$$
 (5)

with the following relations from tadpole conditions:

$$\mu_H^2 = \lambda_H v^2 + \frac{\lambda_{SH} u^2}{2},\tag{6}$$

$$\mu_S^2 = \lambda_S u^2 + \frac{\lambda_{SH} v^2}{2}.\tag{7}$$

If we assume the new physics is at the TeV scale, the new scale u is larger than the electroweak scale v. After symmetry breaking, there are mass mixings between the SM Higgs ϕ and the scalar χ . The mixing matrix is

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$$\mathcal{M}_{S}^{2} = \begin{pmatrix} 2\lambda_{H}v^{2} & \lambda_{SH}vu\\ \lambda_{SH}vu & 2\lambda_{S}u^{2} \end{pmatrix}. \tag{8}$$

Diagonalizing the above matrix, we obtain the mass squared eigenvalues

$$m_{h,S}^2 = \lambda_H v^2 + \lambda_S u^2 \mp \sqrt{(\lambda_S u^2 - \lambda_H v^2)^2 + \lambda_{SH}^2 u^2 v^2}$$
 (9)

and the eigenvectors

$$\binom{h}{S} = \begin{pmatrix} \cos \varphi & -\sin \varphi \\ \sin \varphi & \cos \varphi \end{pmatrix} \binom{\phi}{\chi},$$
 (10)

where the mixing angle φ is given by

$$\tan 2\varphi = \frac{\lambda_{SH}uv}{\lambda_S u^2 - \lambda_H v^2}.$$
 (11)

Equations (9) and (11) can be inverted to express the parameters λ_H , λ_S , and λ_{SH} in terms of the physical quantities $m_{h,S}$ and the mixing angle φ :

$$\lambda_H = \frac{m_h^2 \cos^2 \varphi + m_S^2 \sin^2 \varphi}{2v^2},$$

$$\lambda_S = \frac{m_S^2 \cos^2 \varphi + m_h^2 \sin^2 \varphi}{2u^2},$$

$$\lambda_{SH} = \frac{m_S^2 - m_h^2}{2uv} \sin 2\varphi.$$
(12)

The general Yukawa couplings involved in the vectorlike fermion ψ and the top quark u_3 read

$$-\mathcal{L}_{\text{Yukawa}} = \frac{y_M}{\sqrt{2}} \chi \bar{\psi}_L \psi_R + \frac{\lambda_T}{\sqrt{2}} \chi \bar{\psi}_L u_{3R} + y_t \bar{Q}_L \tilde{H} u_{3R} + y_T \bar{Q}_L \tilde{H} \psi_R + \text{H.c.}, \quad (13)$$

where $\tilde{H}=i\sigma_2H^{\star}$ and Q_L is the left-handed third-generation quark doublet $Q_L=(\begin{array}{c}u_{3L}\\b_L\end{array})$. We can also write down a Dirac mass term of the vectorlike fermion:

$$-\mathcal{L}_{\text{mass}} = m_D \bar{\psi}_L \psi_R + \text{H.c.}$$
 (14)

After spontaneous symmetry breaking, the vectorlike fermion and the top quark mix together. The mass mixing matrix between (u_{3L}, ψ_L) and (u_{3R}, ψ_R) is written as

$$\mathcal{M}_F = \begin{pmatrix} \frac{y_t v}{\sqrt{2}} & \frac{y_T v}{\sqrt{2}} \\ \frac{\lambda_T u}{\sqrt{2}} & m_D + \frac{y_M u}{\sqrt{2}} \end{pmatrix}. \tag{15}$$

To make the model more predictive, we assume that the masses of the vectorlike fermion are purely generated from the spontaneous symmetry breaking, such that $m_D = 0$. Through a redefinition of the fields (t_R, T_R) , one can

always rotate away one off-diagonal element of the mass matrix, such that $y_T = 0$ or $\lambda_T = 0$. As is in the literature [9], we choose to rotate (t_R, T_R) by an angle $\tan^{-1}(\lambda_T/(y_M))$ to have $\lambda_T = 0$. So after the rotation, the mass matrix becomes

$$\mathcal{M}_F = \begin{pmatrix} \frac{y_t v}{\sqrt{2}} & \frac{y_T v}{\sqrt{2}} \\ 0 & \frac{y_M u}{\sqrt{2}} \end{pmatrix}. \tag{16}$$

To diagonalize the fermion mass matrix, we rotate the gauge eigenstates (u_3, ψ) into the mass eigenstates (t, T) by using two 2×2 unitary transformations

$$\begin{pmatrix} t_{L,R} \\ T_{L,R} \end{pmatrix} = \mathcal{U}_{L,R} \begin{pmatrix} u_{3L,R} \\ \psi_{L,R} \end{pmatrix},$$
 (17)

where the unitary matrices are

$$\mathcal{U}_{L,R} = \begin{pmatrix} \cos \theta_{L,R} & -\sin \theta_{L,R} \\ \sin \theta_{L,R} & \cos \theta_{L,R} \end{pmatrix}. \tag{18}$$

Thus, the mass matrix \mathcal{M}_F transforms as

$$\mathcal{U}_L \mathcal{M} \mathcal{U}_R^{\dagger} = \mathcal{M}_{\text{diag}} = \begin{pmatrix} m_t & 0 \\ 0 & m_T \end{pmatrix}.$$
 (19)

The masses squared of the top quark t and its partner T are

$$m_{t,T}^{2} = \frac{1}{4} (y_{t}^{2} v^{2} + y_{T}^{2} v^{2} + y_{M}^{2} u^{2}) \times \left[1 \mp \sqrt{1 - \left(\frac{2y_{t} y_{M} v u}{y_{t}^{2} v^{2} + y_{T}^{2} v^{2} + y_{M}^{2} u^{2}} \right)^{2}} \right], \quad (20)$$

and the mixing angles are

$$\tan 2\theta_L = \frac{2y_T y_M v u}{y_M^2 u^2 - y_T^2 v^2 - y_t^2 v^2},$$

$$\tan 2\theta_R = \frac{2y_t y_T v^2}{y_M^2 u^2 + y_T^2 v^2 - y_t^2 v^2}.$$
(21)

Note that the two mixing angles are not independent parameters, with the relation

$$\tan \theta_R = \frac{m_t}{m_T} \tan \theta_L. \tag{22}$$

It is also useful to invert Eqs. (20) and (21) to express the model parameters (y_t, y_T, y_M) in terms of physical parameters (m_t, m_T, θ_L) :

$$y_{M} = \frac{\sqrt{2}m_{T}}{u} \sqrt{\cos^{2}\theta_{L} + x_{t}^{2}\sin^{2}\theta_{L}},$$

$$y_{T} = \frac{\sqrt{2}m_{T}}{v} \frac{\sin\theta_{L}\cos\theta_{L}(1 - x_{t}^{2})}{\sqrt{\cos^{2}\theta_{L} + x_{t}^{2}\sin^{2}\theta_{L}}},$$

$$y_{t} = \frac{\sqrt{2}m_{t}}{v} \frac{1}{\sqrt{\cos^{2}\theta_{L} + x_{t}^{2}\sin^{2}\theta_{L}}},$$
(23)

where $x_t = m_t/m_T$.

In this model, the singlet scalar interacts with the SM particles in two ways: mixing with the SM Higgs boson and interacting with the top quark through Yukawa coupling. In the top quark sector, the vectorlike fermion mixes with the top quark. The mass of the vectorlike fermion is generated from the VEVs of the symmetry breaking. This forces the masses of the two heavy fields S and T at the order of the scale u, which is assumed to be TeV scale. Let us summarize the new parameters in the model. There are five independent parameters, which are chosen to be two heavy masses m_S and m_T , two mixing angles φ and θ_L , and the TeV symmetry breaking scale u. In the following sections, we will use the shorthand notation for the mixing angles

$$s_{\varphi} \equiv \sin \varphi,$$
 $c_{\varphi} \equiv \cos \varphi,$ $s_L \equiv \sin \theta_L,$ $c_L \equiv \cos \theta_L.$ (24)

III. VACUUM STABILITY AND RENORMALIZATION GROUP EQUATIONS

In order to find out the true vacuum and investigate its stability, we should study the effective scalar potential which includes the radiative loop corrections and RG-improved parameters. At the one-loop order, the effective scalar potential is [17], in the Landau gauge,

$$V_{\text{eff}}(\Phi, \chi) = V(\Phi, \chi) + \frac{1}{64\pi^2} \sum_{i} (-1)^{2s_i} (2s_i + 1)$$

$$\times M_i^4(\Phi^2, \chi^2) \left[\ln \frac{M_i^2(\Phi^2, \chi^2)}{\mu^2} - c_i \right], \qquad (25)$$

where $M_i^2(\Phi^2,\chi^2)$ are the field-dependent mass squared and the index i runs over all the fields in the model. Here c_i are constants that depend on the renormalization scheme. We choose the $\overline{\rm MS}$ scheme, with $c_i=3/2$ for scalars and fermions and $c_i=5/6$ for vector bosons. The effective scalar potential $V_{\rm eff}$ must develop a realistic minimum at the electroweak scale v, corresponding to the SM VEV. The stability condition on the Higgs vacuum is dependent on the behavior of $V_{\rm eff}$ in the large-field limit $h\gg v=246$ GeV. This condition is essentially equivalent to the requirement [2] that the Higgs quartic coupling $\lambda(\mu)$ never becomes negative below the Planck scale. We will study the renormalization group equation (RGE) running behavior of the Higgs quartic coupling $\lambda(\mu)$ in the $\overline{\rm MS}$ scheme.

This requires us to work in the effective field theory framework, by integrating heavy particles out at their mass thresholds and matching all the running couplings between effective theories at different scales. At the scale of the scalar pole mass M_S , we can integrate out the scalar singlet in the tree-level potential $V(\Phi,\chi)$ by using its equation of motion:

$$\chi^2 = u^2 - \frac{\lambda_{SH}}{\lambda_S} (\Phi^{\dagger} \Phi - v^2 / 2).$$
 (26)

Inserting the above equation back to $V(\Phi, \chi)$, we obtain the tree-level effective Higgs potential below the heavy mass threshold:

$$V(\Phi) = \lambda^{\text{SM}} (\Phi^{\dagger} \Phi - v^2/2)^2, \tag{27}$$

where

$$\lambda^{\rm SM} = \lambda_H - \frac{\lambda_{SH}^2}{4\lambda_S}.\tag{28}$$

This shows that there is a tree-level shift when we match the Higgs quartic coupling λ_H in the model to the Higgs quartic coupling $\lambda^{\rm SM}$ in the low energy effective theory. This is consistent with the expression of the Higgs boson mass in the limit of $v \ll u$:

$$m_h^2 = 2v^2 \left(\lambda_H - \frac{\lambda_{SH}^2}{4\lambda_S} + \mathcal{O}(v^2/u^2) \right).$$
 (29)

At the scale of the heavy fermion pole mass M_T , we also integrate out the heavy fermion by using its equation of motion. The tree-level matching between the model and the low energy effective theory in the Yukawa sector tells us

$$y_t^{\text{SM}} = y_t - \frac{\lambda_T y_T}{y_M}. (30)$$

Since we already take $\lambda_T = 0$ after the redefinition of the Yukawa couplings, no matching is needed for y_t .

Depending on different particle content in effective theories, there are different RGE running behaviors in different energy regions.

Region I: Scale $\mu < M_T, M_S$.—In this region, after integrating out all the heavy particles, we recover the SM as the low energy theory. The SM one-loop RGE for the Higgs quartic coupling is

$$\frac{d\lambda}{d\ln\mu^2} = \beta_{\lambda}^{\text{SM}} = \frac{\lambda}{(4\pi)^2} \left[12\lambda + 6y_t^2 - \frac{9g_1^2}{10} - \frac{9g_2^2}{2} \right] + \frac{1}{(4\pi)^2} \left[-3y_t^4 + \frac{9g_2^4}{16} + \frac{27g_1^4}{400} + \frac{9g_2^2g_1^2}{40} \right], \quad (31)$$

where $g_1 = \sqrt{5/3}g_Y$ is the hypercharge gauge coupling in grand unified theory (GUT) normalization and g_2 the weak $SU(2)_L$ gauge coupling. Note that, for a light Higgs, the running behavior is mainly controlled by the top quark Yukawa coupling, which drives λ towards more negative values. If there is no new particle running in the loop, λ would eventually become negative at a high energy scale around 10^{10} GeV.

In order to determine the boundary condition for $\lambda(\mu)$ at the renormalization scale μ , one needs to know how the $\overline{\rm MS}$ renormalized Higgs quartic coupling $\lambda(\mu)$ relates to the SM input parameters. Here the SM input parameters are taken to be the SM pole masses M_h , M_t , M_W , and M_Z and Fermi constant G_F , $\alpha_s(M_Z)$. The relation that connects $\lambda(\mu)$ to the SM input parameters can be written as

$$\lambda^{\text{SM}}(\mu) = \frac{G_F M_h^2}{\sqrt{2}} [1 + \Delta_h(\mu)],$$
 (32)

where $\Delta_h(\mu)$ represents electroweak one-loop radiative corrections at the scale μ [18]. Similarly, the boundary condition for y_t can be determined from the relation between the pole mass and its running mass:

$$y_t^{\text{SM}}(\mu) = (\sqrt{2}G_F)^{\frac{1}{2}}M_t[1 + \Delta_t(\mu)],$$
 (33)

where $\Delta_t(\mu)$ denotes the electroweak radiative corrections [19]. In the RGE running, we start from the scale of the top pole mass M_t . The boundary conditions of the couplings at the M_t scale are taken from the two-loop matched values presented in Ref. [3].

Region II (a): Scale $\mu \ge M_T$ and $\mu < M_S$.—There are two cases in the intermediate region, since the model could have either $M_T < M_S$ or $M_T > M_S$. Let us first discuss case (a): $M_T < M_S$. Because of $\lambda_T = 0$, there is no matching condition on the top-Yukawa coupling at the scale of the heavy fermion mass M_T . Above this scale, the heavy fermion contributes to the one-loop running of the gauge couplings, Yukawa couplings, and Higgs quartic coupling λ . The RGE for the Higgs quartic coupling becomes

$$\frac{d\lambda}{d\ln\mu^2} = \beta_{\lambda}^{SM} + \frac{1}{(4\pi)^2} [6\lambda y_T^2 - 3y_T^4 - 6y_T^2 y_t^2]. \quad (34)$$

Because of the negative contributions from the additional terms in the above RGE, we expect the scale, at which the Higgs quartic coupling becomes negative, to be lower than that in the SM. Therefore, in the pure vectorlike fermion model, the Higgs vacuum instability problem is worse than that in the SM.

Region II (b): Scale $\mu \ge M_S$ and $\mu < M_T$.—This is the case $M_T > M_S$. According to Eq. (28), the Higgs quartic coupling receives a positive shift at the M_S threshold

$$\lambda_H = \lambda^{\text{SM}} + \frac{\lambda_{SH}^2}{4\lambda_S},\tag{35}$$

which is the matching condition on the Higgs quartic coupling. The heavy scalar also changes the RGE running behavior of the Higgs quartic coupling, which becomes

$$\frac{d\lambda_H}{d\ln \mu^2} = \beta_{\lambda}^{SM} + \frac{1}{(4\pi)^2} \frac{1}{4} \lambda_{SH}^2.$$
 (36)

The positive contribution from the last term in Eq. (36) delays the occurrence of the vacuum instability at high energies. Therefore, the above two effects on the RGE running could avoid the possible vacuum instability.

However, we have to worry about the perturbativity bounds on the scalar quartic coupling λ_S . The RGE running of the scalar coupling is

$$\frac{d\lambda_S}{d\ln\mu^2} = \frac{1}{(4\pi)^2} [9\lambda_S^2 + \lambda_{SH}^2]. \tag{37}$$

If there is no new heavy fermion coupled to the heavy scalar, it is very likely that the scalar coupling λ_S blows up at some energy scale and thus violates the perturbativity bounds. Although adding a heavy scalar could solve the instability problem, there is another problem from the perturbativity bounds on the scalar coupling in the model with only scalar sector extension.

Region III: Scale $\mu \ge M_T, M_S$.—In this region, both the heavy fermion and the heavy scalar are involved in the RGE running. If $M_T < M_S$, the quartic Higgs coupling would receive the same tree-level threshold correction as Eq. (35) at the boundary of region III. The full RGE running of the Higgs quartic coupling is

$$\frac{d\lambda_H}{d\ln\mu^2} = \beta_{\lambda}^{SM} + \frac{1}{(4\pi)^2} \left[6\lambda_H y_T^2 + \frac{1}{4} \lambda_{SH}^2 - 3y_T^4 - 6y_t^2 y_T^2 \right]. \tag{38}$$

We notice that in the above RGE the negative contribution to the β function of the Higgs quartic coupling from y_T is vastly softened by the positive contribution from λ_{SH} , especially at high energies. By including the positive threshold shift, the vacuum instability problem could be evaded. On the other hand, we need to take care of the perturbativity bounds on the scalar coupling. The RGE running of the scalar coupling λ_S is

$$\frac{d\lambda_S}{d\ln u^2} = \frac{1}{(4\pi)^2} [9\lambda_S^2 + \lambda_{SH}^2 + 6y_M^2 \lambda_S - 3y_M^4], \quad (39)$$

where y_M is the Yukawa coupling of the scalar to the heavy fermion. Without the y_M^4 term in the above equation, λ_S could blow up and reach the Landau pole at some scale.

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The presence of new Yukawa coupling plays a role to avoid this trouble.

In our numerical scan, we requires that at all the running scales below Planck scale,

$$\lambda_H(\mu) > 0, \qquad 0 < \lambda_S(\mu) < 4\pi. \tag{40}$$

The evolution of λ_{SH} is written as

$$\frac{d\lambda_{SH}}{d\ln\mu^2} = \frac{1}{(4\pi)^2} \left[\lambda_{SH} \left(2\lambda_{SH} + 6\lambda_H + 3\lambda_S + 3y_t^2 + 3y_T^2 + 3y_M^2 - \frac{9g_1^2}{20} - \frac{9g_2^2}{4} \right) - 6y_T^2 y_M^2 \right].$$
(41)

Since λ_{SH} could be either positive or negative, we require only

$$|\lambda_{SH}(\mu)| < 4\pi. \tag{42}$$

The RGE runnings of the new Yukawa couplings are

$$\frac{dy_T^2}{d\ln\mu^2} = \frac{y_T^2}{(4\pi)^2} \left[\frac{9}{2} y_T^2 + \frac{9}{2} y_t^2 + \frac{1}{4} y_M^2 - \frac{17}{20} g_1^2 - \frac{9}{4} g_2^2 - 8g_3^2 \right],\tag{43}$$

$$\frac{dy_M^2}{d\ln\mu^2} = \frac{y_M^2}{(4\pi)^2} \left[y_T^2 + \frac{9}{2} y_M^2 - \frac{8}{5} g_1^2 - 8g_3^2 \right]. \tag{44}$$

We require all the Yukawa couplings to be in the perturbative region at all energies below the Planck scale.

The complete RGEs in three regions are listed in Appendix B. To illustrate, we show the RGE running of the Yukawa and scalar couplings in Fig. 1 for a typical parameter point: $m_S = 1 \text{ TeV}$, $m_T = 800 \text{ GeV}$, $\sin \varphi = 0.1$, $\sin \theta_L = 0.08$, and u = 2 TeV. Using Eqs. (40) and (42), we could put constraints on the parameter space in the model. So we perform a numerical scan over a large range of the parameter space for all parameters: the masses m_S and m_T , the mixing angles s_{ω} and s_L , and the scale u. Figures 2 and 3 show the allowed parameter space satisfying the stability and the perturbativity conditions. As expected, if the mixing angle s_{ω} is too small, and the scalar mass is light, the scalar cannot give enough lift on the Higgs quartic coupling. In this small parameter region, the Higgs quartic coupling will become negative below the Planck scale. So in Fig. 2 we notice there is a small region where the Higgs vacuum is instable. Figure 2 also shows the zero s_{ω} is always excluded. This indicates that it is not allowed to take the decoupling limit in the scalar sector. On the other hand, the parameter region where the scalar and the Higgs have a large mixing is disfavored, especially when the scalar is heavy. The reason for this is that the scalar quartic couplings will increase as evolving to the high energy

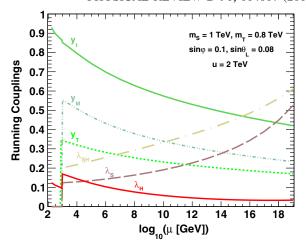


FIG. 1 (color online). The RGE running of the Yukawa and scalar couplings in the model. All parameters are defined in the $\overline{\rm MS}$ scheme. The starting point of the running is $m_t(M_t)$. The benchmark point $m_S=1~{\rm TeV},~m_T=800~{\rm GeV},~\sin\varphi=0.1,$ $\sin\theta_L=0.08,$ and $u=2~{\rm TeV}$ is taken.

scale and eventually become nonperturbative. Indeed, Fig. 2 shows the region with large mixing angle s_{φ} is excluded. If we fix the scale u (dashed contours in Fig. 2), there is a strict bound on the mass of the scalar from the perturbativity limit on the scalar coupling strength λ_S . Regarding the parameter space for the heavy fermion, we expect that small s_L is favored, since the small mixing angle usually gives rise to small Yukawa

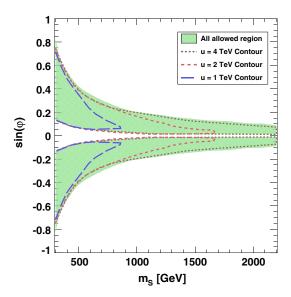


FIG. 2 (color online). The allowed parameter region of the scalar mass and mixing angle (m_S, s_{φ}) when all other parameters are scanned over. The colored region satisfies the vacuum stability of the Higgs potential and perturbativity of all the running couplings. The interiors of the dashed lines are the allowed contours (m_S, s_{φ}) for different fixed scales u.

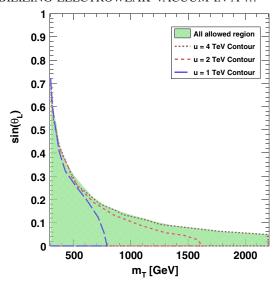


FIG. 3 (color online). The allowed parameter region of the vectorlike fermion mass and mixing angle (m_T, s_L) when all other parameters are scanned over. The colored region satisfies the vacuum stability of the Higgs potential and perturbativity of all the running couplings. The interiors of the dashed lines are the allowed contours (m_T, s_L) for different fixed scales u.

couplings y_T . Small s_L could keep the Higgs quartic coupling positive up to the Planck scale. Figure 3 exhibits this feature. As also shown in Fig. 3, if we fix the scale u (dashed contours), the mass of the vectorlike fermion also has an upper bound, since small Yukawa coupling y_M is favored. Finally, we notice that Fig. 2 is symmetric for the positive and negative value

of the s_{φ} . From now on, we will present the parameter space with only the positive half of the whole range of s_{φ} .

IV. PERTURBATIVE UNITARITY

Although there is no bad s-dependent high energy behavior in the model, the tree-level perturbative unitarity could put constraints on the masses and couplings of the heavy particles. In the partial wave treatment [20], given the tree-level scattering amplitude $\mathcal{M}(s,\theta)$ of all possible $2 \to 2$ scattering processes, the partial wave amplitude with angular momentum J is written as

$$a_J = \frac{1}{32\pi} \int_{-1}^1 d\cos\theta P_J(\cos\theta) \mathcal{M}(s,\theta), \qquad (45)$$

where s and θ are the total energy squared and the scattering polar angle in the center of mass frame, respectively. $P_J(\cos \theta)$ is the Legendre polynomial. The unitarity requires the following condition [20–22]:

$$|\operatorname{Re}(a_J)| \le \frac{1}{2}.\tag{46}$$

In the high energy limit, following the equivalence theorem [23–26], the unitarity condition could be obtained by calculating the partial wave amplitudes of the coupled channels in the scalar sector. It has been shown [27] that the dominant contribution in the coupled channels is the process $SS \rightarrow SS$. In the high energy limit, the tree-level amplitude of the $SS \rightarrow SS$ is

$$\mathcal{M}\left(\frac{1}{\sqrt{2}}SS \to \frac{1}{\sqrt{2}}SS\right) = \frac{1}{64v^2u^2} \left[6(m_H^2 + 5m_S^2)(v^2 + u^2) + 3(m_H^2 + 15m_S^2)(v^2 - u^2)\cos(2\varphi) - 6(m_H^2 - 3m_S^2)(v^2 + u^2)\cos(4\varphi) - 3(m_H^2 - m_S^2)(v^2 - u^2)\cos(6\varphi) - 12(m_H^2 - m_S^2)2vu\sin^3(2\varphi)\right]. \tag{47}$$

If we put it back to the unitarity condition Eq. (46), we obtain the constraints on the parameter space. In the limit of no mixing between the Higgs and the scalar, it gives a constraint on m_S against u:

$$m_S < \sqrt{\frac{4\pi}{3}}u. \tag{48}$$

On the other hand, the heavy fermion also has an upper bound on its mass and coupling s_L from the requirement of the perturbative unitarity through the fermion antifermion scattering process. At high energy $\sqrt{s} \gg m_T$, the tree-level amplitude of the process $T\bar{T} \to T\bar{T}$ is

$$\mathcal{M}(T\bar{T} \to T\bar{T})_{\lambda_i \lambda_f} = m_T^2 (u^{-2} c_L^4 + v^{-2} s_L^4) \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \quad (49)$$

where λ_i and λ_f are the helicity states of the initial and final states, respectively. λ_i and λ_f are taken to be one of the following helicity states: $\{++,+-,-+,--\}$. Diagonalizing it and taking the largest *s*-wave component, we have the unitarity condition

$$a_0^{\text{max}} = \frac{1}{16\pi} [m_T^2 (u^{-2} c_L^4 + v^{-2} s_L^4)] < \frac{1}{2}.$$
 (50)

Similarly, if there is no mixing between the vectorlike fermion and the top quark, it gives a constraint on m_T against u:

$$m_T < \sqrt{8\pi}u. \tag{51}$$

V. PRECISION ELECTROWEAK MEASUREMENTS

The presence of the new scalar *S* and the vectorlike fermion *T* renders both modified SM couplings and new electroweak couplings. We summarize the relevant Lagrangian involving gauge couplings and the Higgs couplings in Appendix A. These electroweak couplings have impact on the electroweak observables, precisely measured at the LEP and SLC.

The dominant NP effects on the electroweak observables appear in the gauge boson vacuum polarization correlations, named oblique corrections [28], parametrized by three independent parameters S, T, and U:

$$\alpha S \equiv 4e^2 [\Pi'_{33}(0) - \Pi'_{3O}(0)], \tag{52}$$

$$\alpha T \equiv \frac{e^2}{s_W^2 c_W^2 m_Z^2} [\Pi_{11}(0) - \Pi_{33}(0)], \tag{53}$$

$$\alpha U \equiv 4e^2 [\Pi'_{11}(0) - \Pi'_{33}(0)], \tag{54}$$

where the notation Π_{XY} with X,Y=1,3,Q denotes the vacuum polarization amplitudes and $\Pi'_{XY}(q^2)=\frac{d}{dq^2}\Pi_{XY}(q^2)$. From the global fit of the electroweak precision data, the constraints on the S,T, and U parameters can be obtained. The following fit results are determined from the GFITTER fit [29] for the reference SM parameters $m_t=173$ GeV and $m_h=126$ GeV. In the NP model, the contribution of the U parameter is usually very small and can be neglected. By fixing U=0, the GFITTER global fit results in

$$\Delta S = S^{\text{NP}} - S^{\text{SM}} = 0.05 \pm 0.09,$$
 (55)

$$\Delta T = T^{\text{NP}} - T^{\text{SM}} = 0.08 \pm 0.07,\tag{56}$$

and the correlation coefficient is taken to be 0.91.

We split the calculation on the oblique parameters into boson-loop contributions T_S , S_S and fermion-loop contributions T_F , S_F and consider them separately. For the boson-loop contributions, the NP effect is involved only in the vacuum polarization amplitudes where the Higgs or the heavy scalar are in the loop. This is shown by Feynman diagrams in Fig. 4. Using the vector boson self-energy Π_{VV} defined in Appendix C, we obtain

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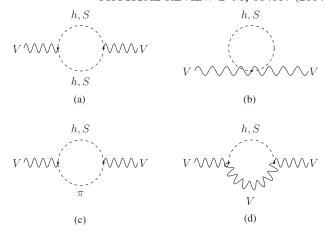


FIG. 4. The one-loop Feynman diagrams (a–d) of the vector boson self-energy Π_{VV} due to the scalars in the loop.

$$\Delta T_S = s_{\varphi}^2 [T_s(m_S^2) - T_s(m_h^2)], \tag{57}$$

$$\Delta S_S = s_{\varphi}^2 [S_s(m_S^2) - S_s(m_h^2)], \tag{58}$$

where the functions are defined as

$$T_s(m) = -\frac{3}{16\pi c_W^2} \left[\frac{1}{(m^2 - m_Z^2)(m^2 - m_W^2)} \times (m^4 \ln m^2 - s_W^{-2}(m^2 - m_W^2)m_Z^2 \ln m_Z^2 + s_W^{-2} c_W^2(m^2 - m_Z^2)m_W^2 \ln m_W^2) - \frac{5}{6} \right],$$
 (59)

$$S_s(m) = \frac{1}{12\pi} \left[\ln m^2 - \frac{(4m^2 + 6m_Z^2)m_Z^2}{(m^2 - m_Z^2)^2} + \frac{(9m^2 + m_Z^2)m_Z^4}{(m^2 - m_Z^2)^3} \ln \frac{m^2}{m_Z^2} - \frac{5}{6} \right].$$
 (60)

Similarly, it is straightforward to calculate the oblique corrections due to the top quark and the vectorlike fermion shown in Fig. 5. Subtracting the SM contributions due to the third-generation quarks

$$T_F^{\rm SM} = \frac{3m_t^2}{4\pi e^2 v^2},\tag{61}$$



FIG. 5. The one-loop Feynman diagrams of (a) W boson self-energy and (b) Z boson self-energy, due to heavy fermions in the loop.

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$$S_F^{\text{SM}} = \frac{1}{2\pi} \left(1 - \frac{1}{3} \log \frac{m_t^2}{m_b^2} \right),\tag{62}$$

we arrive at the final expressions

$$\Delta T_F = T^{\text{SM}} s_L^2 \left[-(1 + c_L^2) + s_L^2 \frac{m_T^2}{m_t^2} + c_L^2 \frac{2m_T^2}{m_T^2 - m_t^2} \ln \frac{m_T^2}{m_t^2} \right], \tag{63}$$

$$\begin{split} \Delta S_F &= -\frac{s_L^2}{6\pi} \left[(1-3c_L^2) \ln \frac{m_T^2}{m_t^2} + 5c_L^2 \right. \\ &\left. - \frac{6c_L^2 m_t^4}{(m_T^2 - m_t^2)^2} \left(\frac{2m_T^2}{m_t^2} - \frac{3m_T^2 - m_t^2}{m_T^2 - m_t^2} \ln \frac{m_T^2}{m_t^2} \right) \right], \quad (64) \end{split}$$

which agree with the results in Ref. [9]. We expect that both $\Delta S_F \to 0$ and $\Delta T_F \to 0$ would occur in the heavy mass limit $m_T \to \infty$ due to decoupling of the vectorlike fermion. However, it is hard to observe such a decoupling feature from Eqs. (63) and (64). As we know, decoupling happens when mass goes to infinity but couplings are fixed. If one uses the mixing angle instead of the couplings, the decoupling behavior becomes opaque. The expression of the mixing angle

$$s_L \simeq \frac{y_T v}{\sqrt{2}m_T} \tag{65}$$

shows that s_L goes to zero when m_T goes to infinity and y_T is fixed. Therefore, as s_L goes to zero, the ΔS_F and ΔT_F vanish. On the other hand, if one expresses Eqs. (63) and (64) by using the parameters (y_T, m_T) instead of (s_L, m_T) , it is easy to see that both ΔS_F and ΔT_F are proportional to $\frac{y_T^2 v^2}{m_T^2}$, which clearly exhibit the decoupling behavior.

The only important nonoblique correction comes from the vertex correction of the $Zb\bar{b}$ coupling. In general, the effective $Zb\bar{b}$ vertex can be parametrized as

$$\frac{g_2}{c_W} \bar{b} \gamma^{\mu} \left[g_L \frac{1 - \gamma_5}{2} + g_R \frac{1 + \gamma_5}{2} \right] b Z_{\mu}, \tag{66}$$

where

$$g_L = g_L^{\rm SM} + \delta g_L^{\rm NP}, \tag{67}$$

$$g_R = g_R^{\text{SM}} + \delta g_R^{\text{NP}}.$$
 (68)

Here $g^{\rm SM}$ denotes the SM coupling with a radiative correction included, and $\delta g^{\rm NP}$ represents the correction purely from the NP model. In the SM, by taking the leading m_t -dependent radiative corrections into account, the SM couplings are

$$g_L^{\text{SM}} = -\frac{1}{2} + \frac{1}{3}s_W^2 + \frac{m_t^2}{16\pi^2 v^2},\tag{69}$$

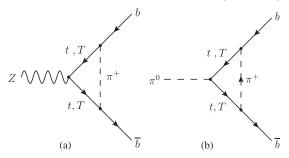


FIG. 6. (a) The dominant one-loop Feynman diagrams in the t' Hooft–Feynman gauge; (b) the only Feynman diagrams after the gaugeless limit is taken in the model.

$$g_R^{\rm SM} = \frac{1}{3} s_W^2. \tag{70}$$

In our model, there is no tree-level correction to the $Zb\bar{b}$ coupling. However, at one loop, flavor-dependent vertex corrections arise and contribute to the $Zb_L\bar{b}_L$ coupling. Figure 6(a) shows the dominant one-loop Feynman diagram in the t' Hooft–Feynman gauge, in which the vectorlike fermion and the top quark appear in the loop. The presence of vertex corrections gives rise to nonzero δg_I^{NP} . To extract out the leading m_T -dependent terms explicitly, we perform the loop calculation in the "gaugeless" limit [30–33], in which the Z boson is treated as a nonpropagating external field coupled to the current $J^{\mu} = \bar{b}_L \gamma^{\mu} b_L$. By using the Ward identity [30,31], the leading contribution to the $Zb_L\bar{b}_L$ coupling can be obtained via the calculation of the higher dimensional operator $\frac{\partial_{\mu}\pi^{0}}{m_{Z}}\bar{b}_{L}\gamma^{\mu}b_{L}$, where π^{0} is the Goldstone boson eaten by the Z boson. The relevant Feynman diagram is shown in Fig. 6(b). The one-loop effective Lagrangian that is generated by the Feynman diagram is

$$\mathcal{L}_{\pi b\bar{b}} = \epsilon_b \frac{2}{v} \bar{b}_L \gamma^\mu b_L \partial_\mu \pi^0, \tag{71}$$

where

$$\epsilon_b = -\frac{1}{16\pi^2 v^2} [m_t^4 c_L^4 C_0(m_t^2, m_t^2, 0) + m_T^4 s_L^4 C_0(m_T^2, m_T^2, 0) + 2m_t^2 m_T^2 c_1^2 s_I^2 C_0(m_t^2, m_T^2, 0)]. \tag{72}$$

Here $C_0(m_1^2, m_2^2, m_3^2)$ is the three-point Passarino-Veltman (PV) function [34] in the zero external momentum limit, where m_i are the masses of the particles in the triangle loop. In the limit of the Goldstone boson, the three-point PV function reduces to

$$C_0(m_1^2, m_2^2, 0) = \begin{cases} -\frac{1}{m_1^2 - m_2^2} \ln \frac{m_1^2}{m_2^2} & \text{if } m_1 \neq m_2, \\ -\frac{1}{m_1^2} & \text{if } m_1 = m_2. \end{cases}$$
(73)

In the decoupling limit, taking $s_L \to 0$ in Eq. (72), one recovers the leading m_t -dependent contribution in the SM:

$$\epsilon_b^{\rm SM} = \frac{m_t^2}{16\pi^2 v^2}.\tag{74}$$

Based on the Ward identity in Refs. [30,31], we recognize the coefficient ϵ_b in Eq. (71) is proportional to the quantity we are interested in:

$$\delta g_L^{\rm NP} = \epsilon_b - \epsilon_b^{\rm SM}. \tag{75}$$

So we obtain the expression for the NP correction $\delta g_L^{\rm NP}$:

$$\delta g_L^{\text{NP}} = \frac{m_t^2 s_L^2}{16\pi^2 v^2} \left[-(1+c_L^2) + s_L^2 \frac{m_T^2}{m_t^2} + c_L^2 \frac{2m_T^2}{m_T^2 - m_t^2} \ln \frac{m_T^2}{m_t^2} \right]. \tag{76}$$

Note that the terms inside the bracket are the same as in Eq. (63).

Among all electroweak observables, three of them are related to the $Z\bar{b}b$ couplings: \mathcal{A}_b , $\mathcal{A}_{FB}^{0,b}$, and R_b . It is known that the asymmetries \mathcal{A}_b and $\mathcal{A}_{FB}^{0,b}$ are mainly sensitive to δg_R^{NP} , while the R_b mainly sets constraints on δg_L^{NP} . Because of the dominant corrections on the δg_L^{NP} , we will make use of the observable R_b to constrain the parameter space. The shift in R_b due to new physics is

$$\delta R_b = 2R_b (1 - R_b) \frac{g_L \delta g_L^{\text{NP}} + g_R \delta g_R^{\text{NP}}}{g_L^2 + g_R^2}.$$
 (77)

The experimental value and SM theoretical value (including two-loop corrections) [1] is

$$R_h^{\text{exp}} = 0.21629 \pm 0.00066,$$
 (78)

$$R_h^{\text{th}} = 0.21575 \pm 0.00003.$$
 (79)

Following Ref. [35], $\delta g_L^{\rm NP}$ is determined to be $\delta g_L = 0.0028 \pm 0.0014$.

The experimental constraints on the oblique parameters and the $Z\bar{b}b$ couplings set limits on the parameter space in the model. We scan over a large range of the parameter space and obtain the allowed parameter region at the 95% confidence level (C.L.). We find that all the parameter spaces on the (m_S, s_{φ}) in the scalar sector are allowed. This means the constraint from the electroweak precision data on the scalar sector is quite weak. However, only part of the parameter space on the (m_T, s_L) in the top sector is allowed, as is shown in Fig. 7. Since all the NP corrections are proportional to s_L^2 , there is an upper limit on the s_L . Figure 7 shows the decoupling nature of the vectorlike fermion: as the fermion becomes heavier, there are less allowed regions of the mixing angle due to the implicit $1/m_T$ dependence of the mixing angle. The constraint from

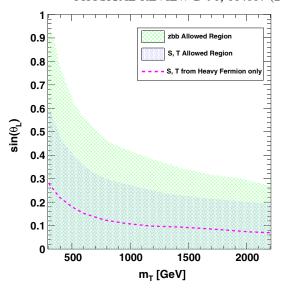


FIG. 7 (color online). The allowed region from the oblique corrections S, T, and $Z\bar{b}_Lb_L$ at the 95% confidence level. Below the pink dashed line is the allowed region from the S, T parameters in the pure vectorlike fermion model.

the nonuniversal correction to the $Zb\bar{b}$ coupling is weaker than the one from the universal oblique corrections. The tightest constraint comes from the T parameter, since the vectorlike fermion is in the singlet representation of the electroweak group, which contributes to the custodial symmetry breaking in the model at the loop level. The dashed line in Fig. 7 shows tighter constraints in the pure vectorlike fermion model than in our model. The relaxed constraint on the T parameter in our model is due to the opposite correction from the boson loops with respect to the fermion contribution. Therefore, the existence of the heavy scalar leads to a larger allowed parameter space.

VI. HIGGS COUPLING MEASUREMENTS

Current data on the measurements of the coupling properties of the Higgs boson at the LHC show that there is no significant deviation from the SM expectation. This put constraints on the NP models in which the Higgs couplings to the SM particles are modified. The deviations in the Higgs couplings can occur in two ways: new fermions or charged bosons contribute to the loop-induced $h\gamma\gamma$ and/or hgg couplings, or new scalars mixed with the Higgs boson give rise to the deviation in the tree-level hVVand/or $hf\bar{f}$ couplings. In our model, the heavy scalar mixed with the Higgs boson induces tree-level correction to the couplings of the Higgs to the SM particles. The vectorlike fermion also contribute to the loop-induced hgg coupling and $h\gamma\gamma$ coupling. These effects will modify both the production cross section and the decay branching ratio of the Higgs boson. In the narrow-width approximation, the signal cross section can be decomposed in the following way for all channels:

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$$(\sigma \cdot BR)(ii \to h \to ff) \equiv \sigma_{ii} \cdot BR_{ff} = \frac{\sigma_{ii} \cdot \Gamma_{ff}}{\Gamma_h},$$
 (80)

where σ_{ii} is the production cross section through the initial state ii, Γ_{ff} the partial decay width into the final state ff, Γ_h the total width of the Higgs boson, and BR_{ff} the branching ratio.

Let us parametrize the deviations on the Higgs couplings in terms of the Higgs coupling scale factors κ , defined as $g^{\rm NP}/g^{\rm SM}$. The general effective Higgs couplings could be rewritten as

$$\mathcal{L}_{\text{Higgs}} = \kappa_W g_{\text{hWW}}^{\text{SM}} h W^{+\mu} W_{\mu}^{-} + \kappa_Z g_{\text{hZZ}}^{\text{SM}} h Z^{\mu} Z_{\mu}$$

$$- \kappa_t g_{htt}^{\text{SM}} h \bar{t} t - \kappa_b g_{hbb}^{\text{SM}} h \bar{b} b - \kappa_\tau g_{h\tau\tau}^{\text{SM}} h \bar{\tau} \tau$$

$$+ \kappa_g g_{hqq}^{\text{SM}} h G^{\mu\nu} G_{\mu\nu} + \kappa_\gamma g_{h\gamma\gamma}^{\text{SM}} h A^{\mu\nu} A_{\mu\nu}, \tag{81}$$

where $g^{\rm SM}$ are the SM Higgs couplings. At the tree level, $g_{hWW}^{\rm SM} = \frac{2m_W^2}{v}, g_{hZZ}^{\rm SM} = \frac{m_Z^2}{v}$, and $g_{hff}^{\rm SM} = \frac{m_f}{v}$. On the other hand, the couplings $g_{h\gamma\gamma}^{\rm SM}$ and $g_{hgg}^{\rm SM}$ only receive loop corrections and thus are suppressed by the loop factor. Up to one-loop level, the SM couplings to the photon and the gluon are

$$g_{hgg}^{SM} = \frac{g_s^2}{16\pi^2} \sum_f \frac{g_{hff}^{SM}}{m_f} A_{1/2}(\tau_f), \tag{82}$$

$$g_{h\gamma\gamma}^{\text{SM}} = \frac{e^2}{16\pi^2} \left[\frac{g_{\text{hWW}}^{\text{SM}}}{m_W^2} A_1(\tau_W) + \sum_f 2N_c^f Q_f^2 \frac{g_{hff}^{\text{SM}}}{m_f} A_{1/2}(\tau_f) \right], \tag{83}$$

where the sum over f runs over t,b,s,c quarks and $\tau_i=\frac{4m_i^2}{m_h^2}$. Here the loop functions $A_1(\tau)$ and $A_{1/2}(\tau)$ are

$$A_{1/2}(\tau) = 2\tau [1 + (1 - \tau)f(\tau)], \tag{84}$$

$$A_1(\tau) = -2 - 3\tau[1 + (2 - \tau)f(\tau)]. \tag{85}$$

with

$$f(x) = \begin{cases} \arcsin^2[1/\sqrt{x}], & \text{for } x \ge 1, \\ -\frac{1}{4} \left[\ln \frac{1+\sqrt{1-x}}{1-\sqrt{1-x}} - i\pi \right]^2, & \text{for } x < 1. \end{cases}$$
(86)

In our model, due to mixing between the Higgs boson and the heavy scalar, all the tree-level Higgs couplings are modified as

$$g_{hff}^{\rm NP}=c_{\varphi}g_{hff}^{\rm SM}, \qquad g_{hVV}^{\rm NP}=c_{\varphi}g_{hVV}^{\rm SM}. \tag{87} \label{eq:87}$$

The loop-induced Higgs couplings to the photon and the gluon are also modified by the new contribution from the vectorlike fermion loop, as shown in Fig. 8. So the Higgs couplings to the photon and the gluon are

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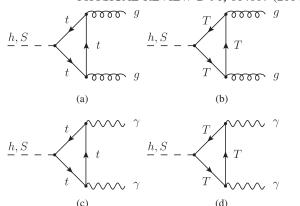


FIG. 8. The loop-induced $h \to gg$ Feynman diagrams due to the top quark (a) and the vectorlike fermion (b), and the loop-induced $h \to \gamma \gamma$ Feynman diagrams due to the top quark (c) and the vectorlike fermion (d).

$$g_{hgg}^{NP} = \frac{g_s^2}{16\pi^2} \left(\sum_f \frac{g_{hff}}{m_f} A_{1/2}(\tau_f) + \frac{g_{hTT}}{m_T} A_{1/2}(\tau_T) \right), \quad (88)$$

$$g_{h\gamma\gamma}^{\text{NP}} = \frac{e^2}{16\pi^2} \left[\frac{g_{\text{hWW}}}{m_W^2} A_1(\tau_W) + \sum_f 2N_c^f Q_f^2 \frac{g_{hff}}{m_f} A_{1/2}(\tau_f) + \frac{8}{3} \frac{g_{hTT}}{m_T} A_{1/2}(\tau_T) \right], \tag{89}$$

where $\tau_T = \frac{4m_T^2}{m_h^2}$ and g_{htt}, g_{hTT} couplings are given in Appendix A. Note that in the above equations there is no scalar mass m_S dependence. From these couplings, we obtain the Higgs coupling scale factors κ in the model:

$$\kappa_V = \kappa_f = c_{\varphi}, \qquad \kappa_g = \frac{g_{hgg}^{\text{NP}}}{g_{hgg}^{\text{SM}}}, \qquad \kappa_{\gamma} = \frac{g_{h\gamma\gamma}^{\text{NP}}}{g_{h\gamma\gamma}^{\text{SM}}}.$$
(90)

The above parameters are not independent. κ_{γ} can be expressed in terms of κ_{g} , because the loop contributions from the vectorlike fermion to the $h \to \gamma \gamma$ and $h \to gg$ couplings are the same. Therefore, there are only two independent parameters (κ_{V}, κ_{g}) in our general parametrization of the Higgs couplings in the model.

In the Higgs measurement at the LHC, the signal strength modifier [36] for each individual channel is defined as

$$R_{ii \to h \to ff} = \frac{\sigma_{ii}^{\text{NP}} \cdot \text{BR}_{ff}^{\text{NP}}}{\sigma_{ii}^{\text{SM}} \cdot \text{BR}_{ff}^{\text{SM}}}.$$
 (91)

The main channels for the Higgs production are the gluon fusion process $gg \rightarrow h$, the vector-boson fusion (VBF) process $qq \rightarrow hqq$, and the associated production $qq \rightarrow Vh$. To distinguish them, we denote the initial state ii as (gg, HV, VBF). So the production cross section in the parton level could be written as

$$\sigma_{gg}^{NP} = \kappa_g^2 \sigma_{gg}^{SM}, \qquad \sigma_{HV}^{NP} = \kappa_V^2 \sigma_{HV}^{SM}, \qquad \sigma_{VBF}^{NP} = \kappa_V^2 \sigma_{VBF}^{SM}.$$
(92)

In practice, it is hard to separate contributions from different production channels. So the production cross section in the hadron level should be

$$\sigma_{pp} = \sum_{i} c_i \sigma_{ii}^{\text{NP}}, \tag{93}$$

where c_i is the relative contribution from the production channel ii, which depends on experimental cuts and detector efficiencies. At the current LHC running, the following decay channels: $h \to WW/ZZ$, $h \to \gamma\gamma$, and $h \to bb/\tau\tau$ are observed. Among these channels, the measurements in the $h \to bb/\tau\tau$ channels still have large uncertainties on the coupling measurements as well as poor mass resolution. Therefore, the precise determination of the Higgs coupling mainly comes from the $h \to WW/ZZ$, $h \to \gamma\gamma$ channels. The decay branching ratio in the model is

$$\begin{split} \mathrm{BR}_{\gamma\gamma} &= r_\Gamma \kappa_\gamma^2 \mathrm{BR}_{\gamma\gamma}^{\mathrm{SM}}, \qquad \mathrm{BR}_{VV} = r_\Gamma \kappa_V^2 \mathrm{BR}_{VV}^{\mathrm{SM}}, \\ \mathrm{BR}_{ff} &= r_\Gamma \kappa_f^2 \mathrm{BR}_{ff}^{\mathrm{SM}}, \end{split} \tag{94}$$

where $r_{\Gamma} = \frac{\Gamma_h^{\rm SM}}{\Gamma_h^{\rm NP}}$ is the ratio of the total width in the SM against that in our model. In terms of the scale factors in the model, the total decay width is parametrized as

$$\Gamma_h^{\text{NP}} \simeq (0.917\kappa_V^2 + 0.003\kappa_\gamma^2 + 0.08\kappa_g^2)\Gamma_h^{\text{SM}},$$
 (95)

where the coefficients come from the numerical values of the SM contributions.

Given the total production cross section and the decay branching ratios in terms of the two independent parameters (κ_V, κ_g) , we are ready to compare our theoretical predictions with the experimental data. We will use all the available data from Tables 10 and 11 in Ref. [37], which collect both the ATLAS and CMS experimental results with full integrated luminosity at 7 and 8 TeV. Then we perform a global fit based on the χ^2 analysis:

$$\chi^2 = \sum_{i} \left(\frac{R_i^{\text{exp}} - R_i^{\text{th}}}{\sigma_i^{\text{exp}}} \right)^2, \tag{96}$$

where we sum over all the available channels in the measurements. Here $R^{\rm exp}$ is the Higgs signal modifier obtained from the experimental data, and $\sigma^{\rm exp}$ is its experimental error. Figure 9 shows the allowed parameter region for the scale factors (κ_V, κ_g) at the 68.27%, 95%, and 99.7% C.L., respectively. The best fit of the scale factors (κ_V, κ_g) is found to be

$$\kappa_V = 1.0096 \pm 0.297, \qquad \kappa_g = 0.941 \pm 0.176,$$

with $\chi^2/\text{ndf} = 61.022/54.$ (97)

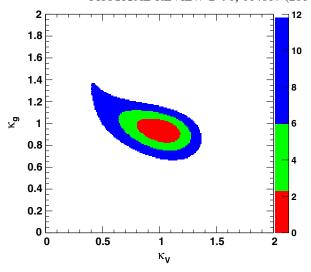


FIG. 9 (color online). The allowed parameter region for the general parametrization (κ_V, κ_g) at the 68.27% (red), 95% (green), and 99.7% (blue) confidence levels. The color palette in the right side shows the value of the $\Delta\chi^2$ for the allowed parameter.

From Eq. (97) and Fig. 9, we find that the central value of the best fit is close to the SM value, and the 95% C.L. contour shows a moderate accuracy. In Fig. 9, there is a small tail in the 99.7% C.L. contour. This tail tells us the parameter space with larger κ_g and smaller κ_V is still allowed by the current data. In the $h \to \gamma \gamma$ channel, due to the enhanced total cross section, κ_g could be larger. While in the $h \to VV$ channel, since the total cross section $\sigma_{gg \to h \to VV} \sim \kappa_g^2 \kappa_V^2$, a larger κ_g implies a smaller κ_V . We could convert our constraints on the scale factors (κ_V, κ_g) into a limit on the model parameters, as shown in Fig. 10. From Fig. 10, we read that the large mixing angles (s_{ω}, s_L)

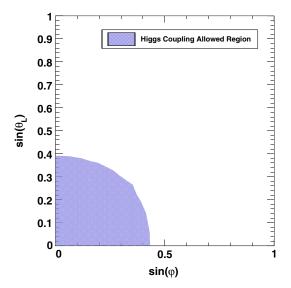


FIG. 10 (color online). The allowed parameter region for the parameters (s_{φ}, s_L) in the model at 95% C.L.

are not allowed. The constraint on s_{φ} is expected, since all the NP corrections in the total cross section are proportional to s_{φ}^2 . The constraint on s_L mainly comes from the gluon fusion production cross section and the $h \to \gamma \gamma$ decay branching ratio. The constraints on the parameters (u, m_T) are quite weak, and there is no constraint on m_S at all. For the scale u, it appears only in the combination $\frac{s_{\varphi}}{u}$, inside the $gg \to h$ and $h \to \gamma \gamma$ loops. Since s_{φ} cannot be large, there is no constraint for a TeV scale u. Because of the saturated behavior of the function $A_{1/2}(\tau_T)$ for a heavy m_T , the constraint on the m_T is weak.

VII. HADRON COLLIDER SEARCHES

There are many direct searches on the vectorlike quarks which couple predominantly to the third-generation quarks at the Tevatron and the LHC. At the LHC, the vectorlike quark could be produced in a pair through QCD production $pp \to T\bar{T}$ or be singly produced via electroweak process $pp \to T\bar{b}$. For a light vectorlike fermion, the pair production cross section is larger than the one in the single production, while for a heavy vectorlike fermion the single production is more efficient. The main decay channels of the heavy vectorlike fermion are

$$T \to tZ$$
, $T \to bW$, $T \to th$, (98)

and $T \rightarrow tS$ only if the scalar is much lighter than the vectorlike fermion. In the model, the tree-level partial decay widths are given by

$$\Gamma_{T \to bW} = \frac{s_L^2 m_T^3}{32\pi v^2} \left(1 + \mathcal{O}\left(\frac{m_W^2}{m_T^2}\right) \right), \tag{99}$$

$$\Gamma_{T \to tZ} = \frac{s_L^2 m_T^3}{64\pi v^2} \left(\left(1 - \frac{m_t^2}{m_T^2} \right)^3 + \mathcal{O}\left(\frac{m_Z^2}{m_T^2} \right) \right), \quad (100)$$

$$\Gamma_{T \to th} = \frac{s_L^2 c_L^2 c_\varphi^2 m_T^3}{64\pi v^2} \left(1 + \frac{5m_t^2}{m_T^2} + \mathcal{O}\left(\frac{m_h^2}{m_T^2}, \frac{m_t^4}{m_T^4}, \frac{v^2}{u^2}\right) \right). \tag{101}$$

By taking the limit $m_T \gg m_t, m_h$, the partial decay widths have the following pattern:

$$\Gamma_{T \to bW} : \Gamma_{T \to tZ} : \Gamma_{T \to th} \simeq 2:1:1.$$
 (102)

This can be understood in the following way. By using the Goldstone equivalence theorem [24–26], the partial decay widths can be estimated by calculating the corresponding Goldstone boson final state instead:

$$\Gamma_{T \to bW} \simeq \Gamma_{T \to b\pi^{\pm}}, \qquad \Gamma_{T \to tZ} \simeq \Gamma_{T \to t\pi^{0}}.$$

Because of the custodial symmetry in the scalar sector, the partial decay widths have

$$\Gamma_{T \to h\pi^{\pm}} : \Gamma_{T \to t\pi^{0}} : \Gamma_{T \to th} \simeq 2:1:1. \tag{103}$$

In a recent CMS analysis [38], using the 8 TeV data collected up to integrated luminosity of 19.5 fb⁻¹, the upto-date lower limits on the mass of the heavy fermion are set to be around 687–782 GeV depending on different patterns of the vectorlike quark decay branching ratios. Setting the pattern of the branching ratio as 2:1:1, we could put a limit on the vectorlike fermion mass: 696 GeV.

In the model, the heavy scalar is CP even, the same as the SM Higgs boson. The search limits on the high mass Higgs boson at the Tevatron and the LHC could be used to set constraints on the mass and couplings of the heavy scalar. The production mechanism is similar to the Higgs boson, dominated by the gluon fusion with the production cross section $\sigma_{gg \to S}$. The decay channels of the heavy scalar are

$$S \to WW$$
, $S \to ZZ$, $S \to hh$, $S \to t\bar{t}$, (104)

and $S \to tT$ only if the vectorlike fermion is much lighter than the scalar. Other decay channels, such as $S \to \gamma \gamma/gg$, $S \to f\bar{f}$, where f is the fermion other than the top quark, are negligible. The explicit formulas of the partial decay widths are listed in Appendix D. Similar to the vectorlike fermion case, in the limit $m_S \gg m_h, m_t$, one could estimate the partial widths by calculating the decays to the corresponding Goldstone bosons instead:

$$\Gamma_{S \to WW} \simeq \Gamma_{S \to \pi^+ \pi^-} = \frac{s_{\varphi}^2 m_S^3}{32\pi v^2} \left(1 + \mathcal{O}\left(\frac{m_Z^2}{m_S^2}\right) \right), \quad (105)$$

$$\Gamma_{S \to ZZ} \simeq \Gamma_{S \to \pi^0 \pi^0} = \frac{s_{\varphi}^2 m_S^3}{64\pi v^2} \left(1 + \mathcal{O}\left(\frac{m_Z^2}{m_\sigma^2}\right) \right), \quad (106)$$

$$\Gamma_{S \to hh} = \frac{s_{\varphi}^2 c_{\varphi}^4 m_S^3}{64\pi v^2} \left(1 + \mathcal{O}\left(\frac{m_h^2}{m_S^2}, \frac{v^2}{u^2}\right) \right). \tag{107}$$

A similar decay pattern holds here: $\Gamma_{S \to WW}$: $\Gamma_{S \to ZZ}$: $\Gamma_{S \to hh} \simeq 2:1:1$. In an up-to-date analysis from the CMS [39], the searches in $S \to WW$ and $S \to ZZ$ decay channels are studied in the mass range between 145 and 1000 GeV. If the high mass Higgs boson has the same coupling as the SM, the mass range between 145 and 710 GeV is excluded at the 95% C.L. We convert this constraint into the limit on the heavy scalar in the model. After calculating the production cross section and the decay branching ratios of the heavy scalar, we perform a scan over the whole range of the parameter space, which is shown in Fig. 12. It is shown that a range of the parameter space with light scalar mass and moderate mixing angle is ruled out.

VIII. CONCLUSIONS

We investigated a vectorlike fermion coupled to a new singlet scalar and the third-generation quarks. The singlet scalar extended the Higgs sector, through the mixing with the Higgs boson. In our setup, the mass of the vectorlike fermion is purely generated from symmetry breaking of the singlet scalar. We carefully examined the electroweak vacuum stability and scalar perturbativity via the renormalization group evolution of the Higgs quartic coupling and the scalar quartic couplings. The matching condition when integrating out heavy particles and the relation between the running and physical parameters were considered. Although the vectorlike fermion provides negative contributions to the running of the Higgs quartic coupling, the new scalar contributes positively. In the matching of the renormalization group, the Higgs quartic coupling obtains a positive threshold shift at the scale of the scalar mass. By taking the above two effects into account, it is likely that the Higgs quartic coupling could stay positive up to the Planck scale. We performed a scan over the parameter space and found that a large range of the parameter space is allowed. In this model, we also examined the constraints from the precision electroweak observables, Higgs coupling precision measurements, and the LHC direct searches. In Figs. 11 and 12, we summarized current constraints on the parameter space of the top sector $(m_T, \sin \theta_L)$ and the scalar sector $(m_S, \sin \varphi)$. It is interesting to see that the tightest constraints always come from the Higgs vacuum stability and perturbativity in the $(m_T, \sin \theta_L)$ and $(m_S, \sin \varphi)$ spaces. However, the constraints from the perturbative unitarity are very weak. Concerning the

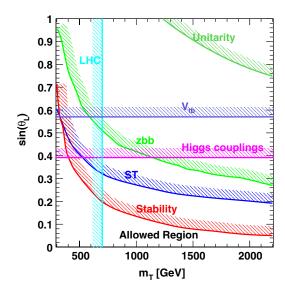


FIG. 11 (color online). Exclusion plot on the parameters $m_T - \sin \theta_L$ with all current constraints included. The exclusion zones are on the shadow side of each line. The allowed region is shown as the zone delimited by the tightest constraints from the stability and the LHC.

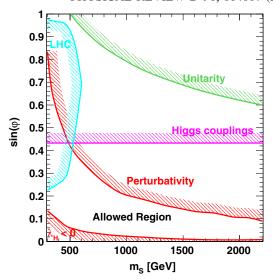


FIG. 12 (color online). Exclusion plot on the parameters m_S – $\sin \varphi$ with all current constraints included. The exclusion zones are on the shadow side of each line. The allowed region is shown as the zone delimited by the tightest constraints from the perturbativity, the stability ($\lambda_H < 0$), and the LHC.

 $(m_T, \sin \theta_L)$ parameter space, the oblique parameters S, T put a tight constraint on the parameter space, while the constraints from the $Zb_L\bar{b}_L$ coupling and the Higgs coupling measurements are weaker. The direct LHC searches set the lower limits on the mass of the vectorlike fermion at around 700 GeV. On the other hand, there is no constraint on the $(m_S, \sin \varphi)$ parameter space from the oblique parameters S, T and $Zb_L\bar{b}_L$ coupling measurements. The Higgs coupling measurements give rise to an upper bound on the mixing angle s_φ . Regarding to the LHC direct searches, only a small range of the parameter space with a moderate mixing angle and light mass is ruled out. As shown in Figs. 11 and 12, a large region of the parameter space is still unexplored.

ACKNOWLEDGMENTS

We thank Can Kilic, Duane Dicus, Jacques Distler, and Willy Fischler for helpful discussion and valuable comments. The research of J.-H. Y. was supported by the National Science Foundation under Grants No. PHY-1315983 and No. PHY-1316033.

APPENDIX A: RELEVANT ELECTROWEAK LAGRANGIAN IN THE MODEL

Let us summarize the relevant Lagrangian as follows. The interactions of the SM quarks (t, b) reads

$$\mathcal{L}_W = -\frac{g_2}{\sqrt{2}}\bar{t}\gamma^{\mu}(c_L P_L)bW^+_{\mu} + \text{H.c.}, \tag{A1}$$

$$\mathcal{L}_{Z} = -\frac{g_{2}}{c_{W}} \bar{t} \gamma^{\mu} (c_{L}^{2} T_{u}^{3} P_{L} - Q s_{W}^{2}) t Z_{\mu}, \tag{A2}$$

$$\mathcal{L}_{H} = -\frac{\sqrt{2}\pi^{+}}{v}\bar{t}(m_{b}c_{L}P_{R} - m_{t}c_{L}P_{L})b + \text{H.c.} - \left(\frac{m_{t}c_{L}^{2}}{v}(\phi - i\pi^{0}) + \frac{m_{t}s_{L}^{2}}{u}\chi\right)\bar{t}t, \tag{A3}$$

where $\phi = c_{\varphi}h + s_{\varphi}S$ and $\chi = -s_{\varphi}h + c_{\varphi}S$. The interactions with the gluon and the photon are the same as in the SM. The interactions of the heavy quark T are

$$\mathcal{L}_{Z} = -\frac{g_{2}}{c_{W}} \bar{T} \gamma^{\mu} (s_{L}^{2} T_{u}^{3} P_{L} - Q s_{W}^{2}) T Z_{\mu}, \tag{A4}$$

$$\mathcal{L}_{H} = -\left(\frac{m_{T}s_{L}^{2}}{v}(\phi - i\pi^{0}) + \frac{m_{T}c_{L}^{2}}{u}\chi\right)\bar{T}T. \tag{A5}$$

Finally, the terms involved in a T and a (t, b) are

$$\mathcal{L}_W = -\frac{g_2}{\sqrt{2}}\bar{T}\gamma^{\mu}(s_L P_L)bW_{\mu}^+ + \text{H.c.}, \tag{A6}$$

$$\mathcal{L}_Z = -\frac{g_2}{c_W} \bar{t} \gamma^\mu (s_L c_L T_u^3 P_L) T Z_\mu + \text{H.c.}, \tag{A7}$$

$$\mathcal{L}_{H} = -\frac{\sqrt{2}\pi^{+}}{v}\bar{T}(m_{b}s_{L}P_{R} - m_{T}s_{L}P_{L})b - \left(\frac{\phi - i\pi^{0}}{v} - \frac{\chi}{u}\right)\bar{t}(m_{t}s_{L}c_{L}P_{L} + m_{T}s_{L}c_{L}P_{R})T + \text{H.c.}$$
(A8)

APPENDIX B: RENORMALIZATION GROUP EQUATIONS

In this section, we listed the one-loop RGEs in different effective field theories.

1. Renormalization group equations in our model

At the scale $\mu > M_S, M_T$, both the heavy scalar and the vectorlike fermion are involved in the RGE running. The gauge coupling RGEs are

$$\frac{dg_1^2}{d\ln\mu^2} = \frac{g_1^4}{(4\pi)^2} \left[\frac{41}{10} + \frac{16}{15} \right],\tag{B1}$$

$$\frac{dg_2^2}{d\ln\mu^2} = \frac{g_2^4}{(4\pi)^2} \left[-\frac{19}{6} \right],\tag{B2}$$

$$\frac{dg_3^2}{d\ln \mu^2} = \frac{g_3^4}{(4\pi)^2} \left[-7 + \frac{2}{3} \right],\tag{B3}$$

where $g_1^2 = 5g_Y^2/3$ is the hypercharge gauge coupling in GUT normalization. The Yukawa coupling RGEs are

$$\frac{dy_t^2}{d\ln\mu^2} = \frac{y_t^2}{(4\pi)^2} \left[\frac{9y_T^2}{2} + \frac{9y_t^2}{2} + \frac{3y_b^2}{2} + y_\tau^2 - \frac{17g_1^2}{20} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B4}$$

$$\frac{dy_b^2}{d\ln\mu^2} = \frac{y_S^2}{(4\pi)^2} \left[\frac{3y_t^2}{2} + \frac{9y_b^2}{2} + \frac{3y_T^2}{2} + y_\tau^2 - \frac{g_1^2}{4} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B5}$$

$$\frac{dy_{\tau}^{2}}{d\ln\mu^{2}} = \frac{y_{\tau}^{2}}{(4\pi)^{2}} \left[3y_{t}^{2} + 3y_{b}^{2} + 3y_{T}^{2} + \frac{5y_{\tau}^{2}}{2} - \frac{9g_{1}^{2}}{4} - \frac{9g_{2}^{2}}{4} \right], \tag{B6}$$

$$\frac{dy_T^2}{d\ln\mu^2} = \frac{y_T^2}{(4\pi)^2} \left[\frac{9}{2} y_T^2 + \frac{9}{2} y_t^2 + \frac{3}{2} y_b^2 + y_\tau^2 + \frac{1}{4} y_M^2 - \frac{17}{20} g_1^2 - \frac{9}{4} g_2^2 - 8g_3^2) \right],\tag{B7}$$

$$\frac{dy_M^2}{d\ln\mu^2} = \frac{y_M^2}{(4\pi)^2} \left[y_T^2 + \frac{9}{2} y_M^2 - \frac{8}{5} g_1^2 - 8g_3^2 \right].$$
 (B8)

The RGEs in the Higgs sector are

$$\frac{d\lambda_H}{d\ln\mu^2} = \frac{1}{(4\pi)^2} \left[\lambda_H \left(12\lambda_H + 6y_t^2 + 6y_b^2 + 2y_\tau^2 + 6y_T^2 - \frac{9g_1^2}{10} - \frac{9g_2^2}{2} \right) + \left(\frac{1}{4} \lambda_{SH}^2 - 3y_t^4 - 3y_b^4 - y_\tau^4 - 3y_T^4 - 6y_t^2 y_T^2 + \frac{27g_1^4}{400} + \frac{9g_2^4}{16} + \frac{9g_2^2 g_1^2}{40} \right) \right],$$
(B9)

$$\frac{d\lambda_{SH}}{d\ln\mu^2} = \frac{1}{(4\pi)^2} \left[\lambda_{SH} \left(2\lambda_{SH} + 6\lambda_H + 3\lambda_S + 3y_t^2 + 3y_b^2 + y_\tau^2 + 3y_T^2 + 3y_M^2 - \frac{9g_1^2}{20} - \frac{9g_2^2}{4} \right) - 6y_T^2 y_M^2 \right], \tag{B10}$$

$$\frac{d\lambda_S}{d\ln\mu^2} = \frac{1}{(4\pi)^2} [9\lambda_S^2 + 6y_M^2 \lambda_S + \lambda_{SH}^2 - 3y_M^4].$$
 (B11)

2. The standard model + vectorlike fermion singlet

At the scale $\mu < M_S$, and $\mu > M_T$, only the vectorlike fermion is involved in the RGE running. The gauge coupling RGEs are

$$\frac{dg_1^2}{d\ln\mu^2} = \frac{g_1^4}{(4\pi)^2} \left[\frac{41}{10} + \frac{16}{15} \right],\tag{B12}$$

$$\frac{dg_2^2}{d\ln\mu^2} = \frac{g_2^4}{(4\pi)^2} \left[-\frac{19}{6} + 0 \right],\tag{B13}$$

$$\frac{dg_3^2}{d\ln\mu^2} = \frac{g_3^4}{(4\pi)^2} \left[-7 + \frac{2}{3} \right]. \tag{B14}$$

The Yukawa coupling RGEs are

$$\frac{dy_t^2}{d\ln\mu^2} = \frac{y_t^2}{(4\pi)^2} \left[\frac{9y_T^2}{2} + \frac{9y_t^2}{2} + \frac{3y_b^2}{2} + y_\tau^2 - \frac{17g_1^2}{20} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B15}$$

$$\frac{dy_b^2}{d\ln\mu^2} = \frac{y_b^2}{(4\pi)^2} \left[\frac{3y_t^2}{2} + \frac{3}{2}y_T^2 + \frac{9y_b^2}{2} + y_\tau^2 - \frac{g_1^2}{4} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B16}$$

$$\frac{dy_{\tau}^{2}}{d\ln\mu^{2}} = \frac{y_{\tau}^{2}}{(4\pi)^{2}} \left[3y_{t}^{2} + 3y_{T}^{2} + 3y_{b}^{2} + \frac{5y_{\tau}^{2}}{2} - \frac{9g_{1}^{2}}{4} - \frac{9g_{2}^{2}}{4} \right], \tag{B17}$$

$$\frac{dy_T^2}{d\ln \mu^2} = \frac{y_T^2}{(4\pi)^2} \left[\frac{9}{2} y_T^2 + \frac{9}{2} y_t^2 + \frac{3}{2} y_b^2 + y_\tau^2 - \frac{17}{20} g_1^2 - \frac{9}{4} g_2^2 - 8g_3^2 \right],\tag{B18}$$

and the RGE in the Higgs sector is

$$\frac{d\lambda}{d\ln\mu^2} = \frac{\lambda}{(4\pi)^2} \left[12\lambda + 6y_T^2 + 6y_t^2 + 6y_b^2 + 2y_\tau^2 - \frac{9g_1^2}{10} - \frac{9g_2^2}{2} \right] + \frac{1}{(4\pi)^2} \left[-3y_T^4 - 6y_T^2y_t^2 - 3y_t^4 - 3y_b^4 - y_\tau^4 + \frac{27g_1^4}{400} + \frac{9g_2^4}{16} + \frac{9g_1^2g_2^2}{40} \right].$$
(B19)

3. The standard model + real scalar singlet

At the scale $\mu > M_S$, and $\mu < M_T$, only the vectorlike fermion is involved in the RGE running. The gauge coupling RGEs are

$$\frac{dg_1^2}{d\ln\mu^2} = \frac{g_1^4}{(4\pi)^2} \left[\frac{41}{10} \right],\tag{B20}$$

$$\frac{dg_2^2}{d\ln\mu^2} = \frac{g_2^4}{(4\pi)^2} \left[-\frac{19}{6} \right],\tag{B21}$$

$$\frac{dg_3^2}{d\ln\mu^2} = \frac{g_3^4}{(4\pi)^2} [-7]. \tag{B22}$$

The Yukawa coupling RGEs are

$$\frac{dy_t^2}{d\ln\mu^2} = \frac{y_t^2}{(4\pi)^2} \left[\frac{9y_t^2}{2} + \frac{3y_b^2}{2} + y_\tau^2 - \frac{17g_1^2}{20} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B23}$$

$$\frac{dy_b^2}{d\ln\mu^2} = \frac{y_b^2}{(4\pi)^2} \left[\frac{3y_t^2}{2} + \frac{9y_b^2}{2} + y_\tau^2 - \frac{g_1^2}{4} - \frac{9g_2^2}{4} - 8g_3^2 \right],\tag{B24}$$

$$\frac{dy_{\tau}^{2}}{d\ln\mu^{2}} = \frac{y_{\tau}^{2}}{(4\pi)^{2}} \left[3y_{t}^{2} + 3y_{b}^{2} + \frac{5y_{\tau}^{2}}{2} - \frac{9g_{1}^{2}}{4} - \frac{9g_{2}^{2}}{4} \right], \tag{B25}$$

and the RGEs in the Higgs sector are

$$\frac{d\lambda_H}{d\ln\mu^2} = \frac{\lambda_H}{(4\pi)^2} \left[12\lambda_H + 6y_t^2 + 6y_b^2 + 2y_\tau^2 - \frac{9g_1^2}{10} - \frac{9g_2^2}{2} \right] + \frac{1}{(4\pi)^2} \left[\frac{1}{4}\lambda_{SH}^2 - 3y_t^4 - 3y_b^4 - y_\tau^4 + \frac{9g_2^4}{16} + \frac{27g_1^4}{400} + \frac{9g_2^2g_1^2}{40} \right],$$
(B26)

$$\frac{d\lambda_{SH}}{d\ln\mu^2} = \frac{\lambda_{SH}}{(4\pi)^2} \left[2\lambda_{SH} + 6\lambda_H + 3\lambda_S + 3y_t^2 + 3y_b^2 + y_\tau^2 - \frac{9g_1^2}{20} - \frac{9g_2^2}{4} \right],\tag{B27}$$

$$\frac{d\lambda_S}{d\ln u^2} = \frac{1}{(4\pi)^2} [9\lambda_S^2 + \lambda_{SH}^2].$$
 (B28)

APPENDIX C: CALCULATION OF THE OBLIQUE PARAMETERS S.T

In this section, we present the computation of the S, T parameters with Passarino-Veltman functions [34].

1. General formulas for gauge boson self-energy

We list the general formulas for the gauge boson self-energy functions Π_{ij} , where i,j denote the gauge boson species. In the formulas, only the one-point PV function $A_0(m^2)$ and the two-point PV functions $B_0(p^2, m_1^2, m_2^2)$ and $B_{00}(p^2, m_1^2, m_2^2)$ are involved. In the calculation of the oblique parameters, all the self-energy functions Π_{ij} and their derivatives $\Pi'_{ij} = \frac{d\Pi}{dp^2}$ are computed at $p^2 = 0$. Various contributions from fermion and scalar loops are summarized as follows.

(i) Fermion loop contribution:

$$\Pi_{ij}^{ff} = -\frac{N_c}{16\pi^2} [(g_{iL}g_{jL} + g_{iR}g_{jR})(4B_{00}(0, m_{f1}^2, m_{f2}^2) - (m_{f1}^2 + m_{f2}^2)B_0(0, m_{f1}^2, m_{f2}^2) - A_0(m_{f1}^2) - A_0(m_{f2}^2)) + 2m_{f1}m_{f2}(g_{iL}g_{jR} + g_{iR}g_{jL})B_0(0, m_{f1}^2, m_{f2}^2)], \tag{C1}$$

$$\Pi_{ij}^{\prime ff} = -\frac{N_c}{16\pi^2} [(g_{iL}g_{jL} + g_{iR}g_{jR})(4B_{00}^{\prime}(0, m_{f1}^2, m_{f2}^2) - (m_{f1}^2 + m_{f2}^2)B_0^{\prime}(m_{f1}^2, m_{f2}^2) + B_0(0, m_{f1}^2, m_{f2}^2))
+ 2m_{f1}m_{f2}(g_{iL}g_{jR} + g_{iR}g_{jL})B_0^{\prime}(0, m_{f1}^2, m_{f2}^2)],$$
(C2)

where g_{iL} and g_{iR} are the left-handed and right-handed couplings, respectively, of the gauge boson labeled i to the fermions running in the loop, from the vertex

$$\bar{f}_1 \gamma^\mu (g_{iL} P_L + g_{iR} P_R) f_2 A_\mu. \tag{C3}$$

(ii) Scalar tadpole contribution:

$$\Pi_{ij}^s = -gA_0(m_s^2),\tag{C4}$$

$$\Pi_{ii}^{\prime s} = 0, \tag{C5}$$

where g is the coupling strength of the s - s - V - V four-point coupling.

(iii) Scalar loop contribution:

$$\Pi_{ij}^{ss} = 4g_i g_i B_{00}(0, m_{s1}^2, m_{s2}^2),$$
 (C6)

$$\Pi_{ij}^{\prime ss} = 4g_i g_j B_{00}^{\prime}(0, m_{s1}^2, m_{s2}^2),$$
 (C7)

where g_i is the coupling strength of the s-s-V three-point coupling involving the gauge boson labeled i.

(iv) Scalar-vector loop contribution:

$$\Pi_{ij}^{vs} = -g_i g_j B_0(0, m_v^2, m_s^2),$$
 (C8)

$$\Pi_{ii}^{\prime vs} = -g_i g_i B_0^{\prime}(0, m_v^2, m_s^2),$$
 (C9)

where g_i is the coupling strength of the s-V-V three-point coupling involving the gauge boson labeled i.

2. The oblique parameters S,T

We present the contributions to the *S*, *T* from the fermion loops and the boson loops, separately.

a. The fermion loops

The T parameter is computed as

$$\alpha T \equiv \frac{e^2}{s_W^2 c_W^2 m_Z^2} [\Pi_{11}(0) - \Pi_{33}(0)] = \frac{\Pi_{WW}}{m_W^2} - \frac{\Pi_{ZZ}}{m_Z^2} - \frac{2s_W}{c_W} \frac{\Pi_{Z\gamma}}{m_Z^2},$$
(C10)

where for fermion loops the last term on the right-hand side does not contribute. In the SM, the fermion contributions mainly come from the third-generation quarks:

$$\Pi_{WW}^{SM} = \Pi_{WW}^{tb,SM},\tag{C11}$$

$$\Pi_{ZZ}^{SM} = \Pi_{ZZ}^{tt,SM} + \Pi_{ZZ}^{bb,SM}.$$
 (C12)

In our model, there are new contributions from the vector-like fermion T:

$$\Pi_{WW} = \Pi_{WW}^{tb} + \Pi_{WW}^{Tb}, \tag{C13}$$

$$\Pi_{ZZ} = \Pi_{ZZ}^{tt} + 2\Pi_{ZZ}^{tT} + \Pi_{ZZ}^{TT} + \Pi_{ZZ}^{bb,SM}.$$
 (C14)

By subtracting the SM contribution, the NP correction on the parameter T from the fermion loops can be obtained:

$$\Delta T_{F} = \frac{1}{\alpha} \left[\frac{1}{m_{W}^{2}} (\Pi_{WW}^{tb} + \Pi_{WW}^{Tb} - \Pi_{WW}^{tb,SM}) - \frac{1}{m_{Z}^{2}} (\Pi_{ZZ}^{tt} + 2\Pi_{ZZ}^{tT} + \Pi_{ZZ}^{TT} - \Pi_{ZZ}^{tt,SM}) \right]. \quad (C15)$$

The S parameter is defined as

$$S = 16\pi(\Pi'_{33} - \Pi'_{3\gamma}). \tag{C16}$$

In the SM, the fermion contributions are

$$\Pi_{33}^{\prime SM} = \Pi_{33}^{\prime tt,SM} + \Pi_{33}^{\prime bb,SM},$$
 (C17)

$$\Pi_{3\gamma}^{\prime SM} = \Pi_{3\gamma}^{\prime tt,SM} + \Pi_{3\gamma}^{\prime bb,SM}, \tag{C18}$$

while the new model gives

$$\Pi_{33}^{\prime SM} = \Pi_{33}^{\prime\prime\prime} + 2\Pi_{33}^{\prime\prime T} + \Pi_{33}^{\prime TT} + \Pi_{33}^{\prime bb, SM},$$
 (C19)

$$\Pi_{3\gamma}^{\prime SM} = \Pi_{3\gamma}^{\prime\prime t} + 2\Pi_{3\gamma}^{\prime\prime T} + \Pi_{3\gamma}^{\prime TT} + \Pi_{3\gamma}^{\prime bb, SM}. \quad (C20)$$

Therefore the NP correction on the parameter S from the fermion loops is

$$\Delta S_F = 16\pi \left[\left(\Pi_{33}^{\prime\prime\prime} + 2\Pi_{33}^{\prime\prime\prime} + \Pi_{33}^{\prime\prime\prime} - \Pi_{33}^{\prime\prime\prime}, SM \right) - \left(\Pi_{3\gamma}^{\prime\prime\prime} + 2\Pi_{3\gamma}^{\prime\prime\prime} + \Pi_{3\gamma}^{\prime\prime} - \Pi_{3\gamma}^{\prime\prime\prime}, SM \right) \right]. \tag{C21}$$

b. The boson loops

To compute the boson contributions, it is convenient to split them into the gauge parts $(\tilde{T}_v, \tilde{S}_v)$ and the scalar parts $(\tilde{T}_s, \tilde{S}_s)$:

$$T_S = \tilde{T}_v + \tilde{T}_s, \qquad S_S = \tilde{S}_v + \tilde{S}_s,$$
 (C22)

where the tilde indicates there are divergences in each part (\tilde{T}, \tilde{S}) , while the total boson contributions to (T_S, S_S) are convergent. The gauge parts consist of the contributions from the W/Z loops, the ghost loops, and the Goldstone loops, which are not altered in our model. So the gauge parts will not contribute to ΔT_S and ΔS_S in our model. The scalar parts $(\tilde{T}_S, \tilde{S}_S)$ consist of all the loops that involve the Higgs boson, or any new real scalars that mix with the Higgs boson. In the following, we will consider only the contributions to the ΔT_S and ΔS_S from the scalar parts.

In the SM, the self-energy functions involving the Higgs boson are

$$\Pi_{WW}^{\rm SM} = \frac{1}{2} \Pi_{WW}^{h, \rm SM} + \Pi_{WW}^{hW, \rm SM} + \Pi_{WW}^{h\pi^{\pm}, \rm SM}, \quad (C23)$$

$$\Pi_{ZZ}^{SM} = \frac{1}{2}\Pi_{ZZ}^{h,SM} + \Pi_{ZZ}^{hZ,SM} + \Pi_{ZZ}^{h\pi^0,SM},$$
 (C24)

while there is no Higgs boson contribution in the two-point function $\Pi_{Z\gamma}$. Inserting the above self-energy functions back to the T parameter definition, due to the cancellation between the first terms in the W and Z self-energy functions, we obtain the scalar part $\tilde{T}_s^{\rm SM}$:

$$\tilde{T}_{s}^{\rm SM} = \frac{1}{\alpha} \left[\frac{\Pi_{WW}^{hW,\rm SM} + \Pi_{WW}^{h\pi^{\pm},\rm SM}}{m_{W}^{2}} - \frac{\Pi_{ZZ}^{hZ,\rm SM} + \Pi_{ZZ}^{h\pi^{0},\rm SM}}{m_{Z}^{2}} \right] \ \ (\rm C25)$$

$$= \frac{3}{16\pi c_W^2} \Delta + T_s(m_h), \tag{C26}$$

where Δ is the divergent term $\Delta = \frac{2}{4-d} - \gamma + \ln 4\pi \mu^2$ in the $\overline{\text{MS}}$ scheme. Here the finite part is written as a function of the scalar mass m:

$$T_s(m) = -\frac{3}{16\pi c_W^2} \left[\frac{1}{(m^2 - m_Z^2)(m^2 - m_W^2)} (m^4 \ln m^2 - s_W^{-2}(m^2 - m_W^2) m_Z^2 \ln m_Z^2 + s_W^{-2} c_W^2 (m^2 - m_Z^2) m_W^2 \ln m_W^2) - \frac{5}{6} \right]. \tag{C27}$$

The calculation is done in the \overline{MS} scheme, without loss of generality.

In our model, the self-energy functions involving the Higgs boson and the new scalar are

$$\Pi_{WW} = \frac{1}{2} (\Pi_{WW}^h + \Pi_{WW}^S) + (\Pi_{WW}^{hW} + \Pi_{WW}^{SW}) + (\Pi_{WW}^{h\pi^{\pm}} + \Pi_{WW}^{S\pi^{\pm}}), \tag{C28}$$

$$\Pi_{ZZ} = \frac{1}{2} (\Pi_{ZZ}^h + \Pi_{ZZ}^S) + (\Pi_{ZZ}^{hZ} + \Pi_{ZZ}^{SZ}) + (\Pi_{ZZ}^{h\pi^0} + \Pi_{ZZ}^{h\pi^0}). \tag{C29}$$

Note that the first terms do not contribute to the T parameter, as in the SM. Similarly, we obtain the scalar part T_s :

$$\tilde{T}_{s} = \frac{1}{\alpha} \left[\frac{\Pi_{WW}^{hW} + \Pi_{WW}^{h\pi^{\pm}}}{m_{W}^{2}} - \frac{\Pi_{ZZ}^{hZ} + \Pi_{ZZ}^{h\pi^{0}}}{m_{Z}^{2}} \right] + \frac{1}{\alpha} \left[\frac{\Pi_{WW}^{SW} + \Pi_{WW}^{S\pi^{\pm}}}{m_{W}^{2}} - \frac{\Pi_{ZZ}^{SZ} + \Pi_{ZZ}^{S\pi^{0}}}{m_{Z}^{2}} \right]$$
(C30)

$$= c_{\varphi}^{2} \left(\frac{3\Delta}{16\pi c_{W}^{2}} + T_{s}(m_{h}) \right) + s_{\varphi}^{2} \left(\frac{3\Delta}{16\pi c_{W}^{2}} + T_{s}(m_{S}) \right)$$
 (C31)

$$=\frac{3\Delta}{16\pi c_W^2} + c_\varphi^2 T_s(m_h) + s_\varphi^2 T_s(m_S),\tag{C32}$$

where the divergent part is the same as the SM as expected. As the new scalar only contributes to the part \tilde{T}_s via mixing with the SM Higgs, common factors s_{φ} and c_{φ} could be extracted, leaving a SM-like $\tilde{T}_s(m)$. Hence the function $T_s(m)$ can be used to obtain a concise form for the \tilde{T}_s in our model. Subtracting the SM contribution $\tilde{T}_s^{\rm SM}$ in Eq. (C26), we get a finite and very concise result for ΔT_s :

$$\Delta T_S = \Delta \tilde{T}_s = s_{\varphi}^2 [T_s(m_S) - T_s(m_h)]. \tag{C33}$$

The S parameter can be defined in an alternative way using the hypercharge Y:

$$S \equiv -16\pi\Pi_{3Y}',\tag{C34}$$

which reduces a lot of work for boson contributions. The Higgs-dependent part \tilde{S}_s in the SM is

$$\tilde{S}_{s}^{\text{SM}} = -16\pi (\Pi_{3y}^{\prime hZ,\text{SM}} + \Pi_{3y}^{\prime h\pi^{0},\text{SM}}) \tag{C35}$$

$$= -\frac{1}{12\pi}\Delta + S_s(m_h),\tag{C36}$$

where

$$S_s(m) = \frac{1}{12\pi} \left[\ln m^2 - \frac{5}{6} - \frac{(4m^2 + 6m_Z^2)m_Z^2}{(m^2 - m_Z^2)^2} + \frac{(9m^2 + m_Z^2)m_Z^4}{(m^2 - m_Z^2)^3} \ln \frac{m^2}{m_Z^2} \right].$$
 (C37)

For the same reason as in the T_S calculation, when we turn to the new model, it has a very concise form:

$$\tilde{S}_s = c_{\varphi}^2 \left(-\frac{\Delta}{12\pi} + S_s(m_h) \right) + s_{\varphi}^2 \left(-\frac{\Delta}{12\pi} + S_s(m_S) \right)$$
(C38)

$$= -\frac{\Delta}{12\pi} + c_{\varphi}^2 S_s(m_h) + s_{\varphi}^2 S_s(m_S), \tag{C39}$$

and similarly

$$\Delta S_S = \Delta \tilde{S}_s = s_{\omega}^2 [S_s(m_S) - S_s(m_h)]. \tag{C40}$$

APPENDIX D: THE PARTIAL DECAY WIDTHS OF THE HEAVY PARTICLES

The heavy scalar S mainly decays in the following channels with partial widths:

$$\Gamma(S \to ZZ) = \frac{G_F m_S^3}{16\sqrt{2}\pi} s_{\varphi}^2 \times \lambda(1, r_Z, r_Z)^{\frac{1}{2}} (1 - 4r_Z + 12r_Z^2), \tag{D1}$$

$$\Gamma(S \to WW) = \frac{G_F m_S^3}{8\sqrt{2}\pi} s_{\varphi}^2 \times \lambda (1, r_Z, r_Z)^{\frac{1}{2}} (1 - 4r_W + 12r_W^2), \tag{D2}$$

$$\Gamma(S \to hh) = \frac{G_F m_S^3}{16\sqrt{2}\pi} s_{\varphi}^2 c_{\varphi}^2 \left(c_{\varphi} + \frac{v}{u} s_{\varphi}\right)^2 \times \lambda(1, r_h, r_h)^{\frac{1}{2}} (1 + 2r_h)^2, \tag{D3}$$

$$\Gamma(S \to Tt) = \frac{3G_F m_S m_T^2}{8\sqrt{2}\pi} s_L^2 c_L^2 \left(s_\varphi - \frac{v}{u} c_\varphi \right)^2 \times \lambda (1, r_T, r_t)^{\frac{1}{2}} \left(1 + \frac{r_t}{r_T} \right) [1 - (r_T - r_t)^2], \tag{D4}$$

$$\Gamma(S \to tt) = \frac{3G_F m_S m_t^2}{4\sqrt{2}\pi} \left(s_{\varphi} c_L^2 + \frac{v}{u} c_{\varphi} s_L^2 \right)^2 \times \lambda (1, r_t, r_t)^{\frac{3}{2}}, \tag{D5}$$

where $r_X = m_X^2/m_S^2$ and the kinematic function λ is

$$\lambda(1, r_1, r_2) = 1 + r_1^2 + r_2^2 - 2r_1 - 2r_2 - 2r_1 r_2. \tag{D6}$$

Note that if $\tan \varphi \sim \frac{v}{u}$, the partial width in the Tt channel is suppressed, while if $\tan \varphi \sim -\frac{v}{u} \tan^2 \theta_L$, the tt channel is suppressed.

The vectorlike fermion mainly decays in the following channels with partial widths:

$$\Gamma(T \to Zt) = \frac{G_F m_T^3}{16\sqrt{2}\pi} s_L^2 c_L^2 \times \lambda(1, r_Z, r_t)^{\frac{1}{2}} (1 + r_Z - 2r_t - 2r_Z^2 + r_t r_Z + r_t^2), \tag{D7}$$

$$\Gamma(T \to Wb) = \frac{G_F m_T^3}{8\sqrt{2}\pi} s_L^2 \times \lambda (1, r_W, r_b)^{\frac{1}{2}} (1 + r_W - 2r_b - 2r_W^2 + r_b r_W + r_b^2), \tag{D8}$$

$$\Gamma(T \to ht) = \frac{G_F m_T^3}{16\sqrt{2}\pi} s_L^2 c_L^2 \left(c_{\varphi} + \frac{v}{u} s_{\varphi} \right)^2 \times \lambda(1, r_h, r_t)^{\frac{1}{2}} (1 + 6r_t - r_h - r_t r_h + r_t^2), \tag{D9}$$

$$\Gamma(T \to St) = \frac{G_F m_T^3}{16\sqrt{2}\pi} s_L^2 c_L^2 \left(s_\varphi - \frac{v}{u} c_\varphi \right)^2 \times \lambda(1, r_S, r_t)^{\frac{1}{2}} (1 + 6r_t - r_S - r_t r_S + r_t^2). \tag{D10}$$

Also note that the St channel is suppressed due to the factor $s_{\varphi} - \frac{v}{\mu} c_{\varphi}$ in its coupling.

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