Constraints on unparticles from $B_s \to \mu^+ \mu^-$

Jong-Phil Lee[*](#page-0-0)

Division of Quantum Phases Devices, School of Physics, Konkuk University, Seoul 143-701, Korea (Received 26 March 2013; published 2 December 2013)

Unparticle contributions to the recently measured decay mode $B_s \to \mu^+ \mu^-$ are analyzed. We consider only the scalar unparticles because vector unparticles are expected to provide negligible contributions. Assuming that the relevant coupling constants are real, we present allowed regions of coupling constants and the scaling dimension of the scalar unparticle. While the measured value of the branching ratio is very close to the standard model predictions, one cannot exclude the possible contributions from unparticles.

DOI: [10.1103/PhysRevD.88.116003](http://dx.doi.org/10.1103/PhysRevD.88.116003) PACS numbers: 12.90.+b, 13.20.-v, 13.20.He

Recently the LHCb Collaboration reported the first evidence for the decay $B_s \to \mu^+ \mu^-$ and an upper limit on $B_d \rightarrow \mu^+ \mu^-$ as [[1\]](#page-4-0),

$$
Br(Bs \to \mu^+ \mu^-) = (3.2^{+1.5}_{-1.2}) \times 10^{-9}, \tag{1}
$$

$$
Br(B_d \to \mu^+ \mu^-) < 9.4 \times 10^{-10}.\tag{2}
$$

The result is quite consistent with the standard model (SM) predictions [\[2](#page-4-1)]

$$
Br(B_s \to \mu^+ \mu^-)_{SM} = (3.23 \pm 0.27) \times 10^{-9}, \quad (3)
$$

$$
Br(B_d \to \mu^+ \mu^-)_{SM} = (1.07 \pm 0.10) \times 10^{-10}.
$$
 (4)

The decay of $B_s \to \mu^+ \mu^-$ is very sensitive to new physics because in the SM the process occurs only through the loop contributions. However, it would be too early to declare that there are no new physics at all. Implications of the new observation in view of new physics can be found in [\[3–](#page-4-2)[5\]](#page-4-3). In this paper, we examine the unparticle effects on $B_s \rightarrow$ $\mu^+ \mu^-$ decay.

An unparticle is a hypothetical concept associated with the scale invariance at high-energy scales [[6](#page-4-4)]. According to the unparticle scenario there is a scale-invariant hidden sector, and it couples to the SM particles very weakly at high-energy scale Λ _U. When seen at low energy, the hidden sector behaves in different ways from ordinary particles, which is why it is called the unparticle scenario. In other words, unparticles behave like a fractional number of particles.

Consider an ultraviolet (UV) theory in the hidden sector at some high energy $\sim M_{\mathcal{U}}$ with the infrared (IR)-stable fixed point. It is quite convenient to describe the interaction between the UV theory and the SM sector in an effective theory formalism. Below the scale of $M_{\mathcal{U}}$, a UV operator \mathcal{O}_{UV} interacts with an SM operator \mathcal{O}_{SM} through $\overline{\mathcal{O}}_{\text{SM}}\mathcal{O}_{\text{UV}}/M_{\mathcal{U}}^{d_{\text{SM}}+d_{\text{UV}}-4}$, where $d_{\text{UV(SM)}}$ is the scaling dimension of $\mathcal{O}_{UV(SM)}$. Through the renormalization flow, one can go down to a new scale Λ _U. It appears through the dimensional transmutation, where the scale invariance emerges. Below Λ _U the theory is matched onto the above interaction with the new unparticle operator \mathcal{O}_U as

$$
C_{\mathcal{U}} \frac{\Lambda_{\mathcal{U}}^{d_{\mathrm{UV}} - d_{\mathcal{U}}}}{M_{\mathcal{U}}^{d_{\mathrm{SM}} + d_{\mathrm{UV}} - 4}} \mathcal{O}_{\mathrm{SM}} \mathcal{O}_{\mathcal{U}},\tag{5}
$$

where $d_{\mathcal{U}}$ is the scaling dimension of $\mathcal{O}_{\mathcal{U}}$, and $C_{\mathcal{U}}$ is the matching coefficient. The value of $d_{\mathcal{U}}$ is not constrained to be integers because of the scale invariance. This unusual behavior of unparticles is reflected on the phase space of $\mathcal{O}_{\mathcal{U}}$. The spectral function of the unparticle is given by the two-point function of \mathcal{O}_U as

$$
\rho_{\mathcal{U}}(P^2) = \int d^4x e^{iP \cdot x} \langle 0 | \mathcal{O}_{\mathcal{U}}(x) \mathcal{O}_{\mathcal{U}}^{\dagger}(0) | 0 \rangle
$$

= $A_{d_{\mathcal{U}}} \theta(P^0) \theta(P^2) (P^2)^{d_{\mathcal{U}} - 2}$, (6)

where

$$
A_{d_{u}} = \frac{16\pi^{2}\sqrt{\pi}}{(2\pi)^{2d_{u}}} \frac{\Gamma(d_{u} + \frac{1}{2})}{\Gamma(d_{u} - 1)\Gamma(2d_{u})}
$$
(7)

is the normalization factor. The corresponding phase space is

$$
d\Phi_{\mathcal{U}}(P) = \rho_{\mathcal{U}}(P^2) \frac{d^4 P}{(2\pi)^4}
$$

= $A_{d_{\mathcal{U}}} \theta(P^0) \theta(P^2)(P^2)^{d_{\mathcal{U}}-2} \frac{d^4 P}{(2\pi)^4}$, (8)

and the propagator is given by

$$
\int d^4x e^{iP\cdot x} \langle 0|T\mathcal{O}_U(x)\mathcal{O}_U^{\dagger}(0)|0\rangle = \frac{iA_{d_u}}{2\sin d_u\pi} \frac{e^{-i\phi_{d_u}}}{(P^2 + i\epsilon)^{2-d_u}},\tag{9}
$$

where $\phi_{d_u} = (d_u - 2)\pi$.

B physics is a good test bed for the unparticle effects [\[7,](#page-4-5)[8](#page-4-6)], including $B_s - \bar{B}_s$ mixing [\[9](#page-4-7)[–12\]](#page-4-8) (see also [\[13,](#page-4-9)[14\]](#page-4-10) for meson mixing). One reason is that unparticles can contribute to the flavor-changing neutral current at tree level. For decays of $B_s \to \ell^+ \ell^-$, the scalar unparticle [*j](#page-0-1)ongphil7@gmail.com can contribute generally through

$$
\mathcal{L} = \sum_{i} [C_q^i \mathcal{O}_q^i \mathcal{O}_u + D_q^i (\mathcal{O}_q^i)_\mu \partial^\mu \mathcal{O}_u + C_\ell^i \mathcal{O}_\ell \mathcal{O}_u + D_\ell^i (\mathcal{O}_\ell^i)_\mu \partial^\mu \mathcal{O}_u],
$$
\n(10)

where $C_{a,\ell}^i$ and $D_{a,\ell}^i$ are coefficients. The quark operators are $\mathcal{O}_q^i = \bar{q}q$, $\bar{q}\gamma_5q$, and $(\mathcal{O}_q^i)_{\mu} = \bar{q}\gamma_{\mu}q$, $\bar{q}\gamma_{\mu}\gamma_5q$, while the leptonic operators are $\hat{\mathcal{O}}_{\ell}^{i} = \bar{\ell} \ell$, $\bar{\ell} \gamma_5 \ell$ and $(\hat{\mathcal{O}}_{\ell}^{i})_{\mu} =$ $\bar{\ell}\gamma_\mu \ell$, $\bar{\ell}\gamma_\mu \gamma_5 \ell$.

For simplicity we only consider the left-handed currents coupled to scalar unparticles by the following Lagrangian,

$$
\mathcal{L}_{\mathcal{U}} = \frac{c_q}{\Lambda_{\mathcal{U}}^{d_u}} \bar{q}' \gamma_\mu (1 - \gamma_5) q \partial^\mu \mathcal{O}_{\mathcal{U}} + \frac{c_\ell}{\Lambda_{\mathcal{U}}^{d_u}} \bar{\ell}' \gamma_\mu (1 - \gamma_5) \ell \partial^\mu \mathcal{O}_{\mathcal{U}},
$$
(11)

where $c_{q,\ell}$ are dimensionless couplings. We assume that $c_{a,\ell}$ are real numbers. Recent studies on the τ lepton and lepton electric/magnetic dipole moments provide bounds on the various leptonic couplings [[15](#page-4-11),[16](#page-4-12)]. For example, for Λ _U = 1 TeV and d _U = 1.9, the relevant couplings can be large as $\geq \mathcal{O}(1)$. In this analysis we concentrate on the range $0 \le c_i \le 1$. As will be clear later, the unparticle contributes in the form of $(c_q \cdot c_\ell) (m_{B_s}^2 / \Lambda_u^2)^{du}$, thus larger values of $c_{q,\ell}$ could be compensated by larger $d_{\mathcal{U}}$.

We do not consider vector unparticle contributions because they are expected to be highly suppressed. One can infer from Eq. ([11\)](#page-1-0) that the scalar unparticle contribution is proportional to $\sim (1/\Lambda_{\mathcal{U}}^2)^{d_u}$, or more exactly (as will be shown later), $\sim (m_{B_s}^2 / \Lambda_{\tau}^2)^{d_u}$. On the other hand, the vector unparticle $\mathcal{O}_{\mathcal{U}}^{\mu}$ couples to the SM current as

$$
\frac{c_V}{\Lambda_U^{d_V - 1}} \bar{q}' \gamma_\mu (1 - \gamma_5) q \mathcal{O}_U^\mu, \tag{12}
$$

where d_V is the scaling dimension of $\mathcal{O}_{\mathcal{U}}^{\mu}$, and its contribution is $\sim (m_{B_s}^2 / \Lambda_u^2)^{d_V - 1}$. But the unitarity constraints require that $d_{\mathcal{U}} \ge 1$ and $d_{\mathcal{V}} \ge 3$ [\[17\]](#page-4-13), resulting in much more suppression of the vector contribution [\[12\]](#page-4-8).

The total decay rate of $B_s \to \mu^+ \mu^-$ is now given by

$$
\Gamma = \frac{1}{16\pi M_{B_s}} \sqrt{1 - \frac{4m_\mu^2}{m_{B_s}^2}} |\langle \mu \mu | (\mathcal{H}_{\text{eff}}^{\text{SM}} + \mathcal{H}_{\text{eff}}^{\text{U}}) | B_s \rangle|^2, \quad (13)
$$

where $\mathcal{H}_{\text{eff}}^{\text{SM}}$ is the SM effective Hamiltonian, while the unparticle effective Hamiltonian $\mathcal{H}_{\text{eff}}^{\text{U}}$ is

$$
\mathcal{H}_{\text{eff}}^{U} = \frac{A_{d_{U}}e^{-i\phi_{U}}}{\sin d_{U}\pi} \left(\frac{m_{B_{s}}}{\Lambda_{U}}\right)^{2d_{U}} \left(\frac{m_{\mu}m_{b}}{m_{B_{s}}^{4}}\right) (c_{q} \cdot c_{\ell})
$$

$$
\times \left[\bar{b}(1-\gamma_{5})s\right] \left[\bar{\ell}\gamma_{5}\ell\right]. \tag{14}
$$

Now the branching ratio can be written as

$$
Br(B_s \to \mu \mu) = Br_{SM} \cdot |P|^2. \tag{15}
$$

Here Br_{SM} is the SM prediction and

$$
P = 1 + \frac{m_{B_s}^2}{2m_\mu} \frac{m_b}{m_b + m_s} \frac{C_P}{C_{10}^{\text{SM}}}.
$$
 (16)

The coefficients C_{10}^{SM} and C_P are given by

$$
C_{10}^{\rm SM} = -\frac{1}{\sin^2 \theta_W} \eta_Y Y_0(x_t), \tag{17}
$$

$$
C_P = \frac{\sqrt{2}\pi}{G_F\alpha(V_{tb}V_{ts}^*)} \frac{A_{d_{\mathcal{U}}}e^{i\phi_{\mathcal{U}}}}{\sin d_{\mathcal{U}}\pi} \left(\frac{m_{B_s}}{\Lambda_{\mathcal{U}}}\right)^{2d_{\mathcal{U}}} \left(\frac{2m_{\mu}}{m_{B_s}^4}\right) (c_q \cdot c_\ell)^*,\tag{18}
$$

where $x_t = m_t^2/m_W^2$, $Y(x) = \eta_Y Y_0(x)$, and

$$
Y_0(x) = \frac{x}{8} \left[\frac{x-4}{x-1} + \frac{3x}{(x-1)^2} \ln x \right], \quad \eta_Y = 1.0113. \tag{19}
$$

Some remarks are in order. Our effective Lagrangian \mathcal{L}_U in Eq. [\(11\)](#page-1-0) contains minimal couplings, so the effective Hamiltonian $\mathcal{H}_{\text{eff}}^{U}$ in Eq. ([14](#page-1-1)) is just proportional to the leptonic pseudoscalar operator with left-handed quark sector. If we added right-handed quark current in \mathcal{L}_u , we would have a leptonic pseudoscalar operator with right-handed quarks. The corresponding coefficient is usually C_p in the literature, which is a counterpart of C_p in Eq. ([18\)](#page-1-2). As shown in [[18\]](#page-4-14), C_P and C_P' appear with different combinations in $B_s \to \ell^+ \ell^-$ and $B \to K \ell^+ \ell^-$ decays. In $B_s \rightarrow \mu^+ \mu^-$, the new physics contributes with $C_P - C_P^{\prime}$, while in $B \to K \ell^+ \ell^-$ with $C_P + C_P'$; thus, the two decay modes are complementary. Numerically, one can estimate from Eqs. (1) (1) , (15) (15) (15) , and (16) that (neglecting the nonzero $\Delta\Gamma_s$ effects discussed later)

$$
|(C_P - C'_P)m_b - 0.16| = 0.15, \tag{20}
$$

while $|(C_P + C'_P)m_b - 0.33| \le 1.3$ from $B \to K\ell^+\ell^-$ [\[18\]](#page-4-14). Thus the new measurement of $B_s \to \mu^+ \mu^-$ is very impressive for pinning down the Wilson coefficients.

On the other hand in $B \to K^* \ell^+ \ell^-$, new physics enters in $C_P - C'_P$ combination and the pseudoscalar operators are numerically irrelevant $[19]$. Estimation of Eq. (20) is much smaller than the values considered in [\[19\]](#page-4-15), $-0.38 \le$ $(C_P - C'_P) m_b \le 0.63$, so we expect that numerically $C_P^{(0)}$ would be much more irrelevant to $B \to K^* \ell^+ \ell^-$. In the inclusive decay $B \to X_s \mu^+ \mu^-$, the coefficients contribute as $|C_P|^2 + |C_P^{\prime}|^2$, which can be complementary to $B_s \rightarrow$ $\mu^+ \mu^-$ decay. The constraint is rather weak, however, since $m_b^2(|C_P|^2 + |C_P'|^2) < 45$ from $B \to X_s \mu^+ \mu^-$ [\[20\]](#page-4-16).

In Table [I,](#page-2-0) we summarize the input values used in this analysis. With the values of Table [I](#page-2-0), one gets Br_{SM} = 3.54×10^{-9} , which is consistent with the other literature. To compare the theoretical prediction with the experimental result, one should consider the nonzero decay width effect of B_s meson [[21](#page-4-17)–[23](#page-4-18)]. According to [\[22\]](#page-4-19),

TABLE I. Input parameters used in this paper. Here $\alpha^{-1} =$ $\alpha(m_Z)^{-1}$, $m_t = m_t(m_t)$ in the $\overline{\text{MS}}$ scheme, and ϕ_{ts} is the phase of V_{ts} .

$G_F = 1.16638 \times 10^{-5}$ GeV ⁻²	$\sin^2 \theta_W = 0.23116$
$\alpha^{-1} = 127.937$	$V_{th} = 0.999$
$ V_{ts} = 0.0407$	$\phi_{ts} = -3.123$
$m_{\mu} = 105.658$ MeV	$m_t = 163.2 \text{ GeV}$
$m_{B_c} = 5.3667 \text{ GeV}$	$\tau_{B_s} = 1.497$ ps
$f_{B_0} = 234$ MeV	$\Lambda_{11} = 1000$ GeV

$$
Br(Bs \to \mu^+ \mu^-)_{\text{theo}}
$$

= $\left[\frac{1 - y_s^2}{1 + y_s \mathcal{A}_{\Delta \Gamma}}\right] Br(B_s \to \mu^+ \mu^-)_{\text{exp}},$ (21)

where

$$
y_s \equiv \tau_{B_s} \frac{\Delta \Gamma_s}{2} = 0.088 \pm 0.014. \tag{22}
$$

Here,

$$
\mathcal{A}_{\Delta\Gamma} = \frac{R_H - R_L}{R_H + R_L},\tag{23}
$$

where $R_{H(L)} \exp \left[-\Gamma_H^{(s)}\right]$ $H(L)$ ^(s) is the decay rate of the heavy (light) mass eigenstate. In our case of Eq. ([14](#page-1-1)) (pseudoscalar leptonic operator), one can easily find that

$$
\mathcal{A}_{\Delta\Gamma} = \cos\left(2\phi_P - \phi_s^{\rm NP}\right),\tag{24}
$$

where ϕ_P is the phase of P in Eq. ([16](#page-1-4)), and ϕ_s^{NP} is the phase of new physics (in this case unparticles) in $B_s - \bar{B}_s$ mixing. From the analysis of [[12](#page-4-8)], $\Delta = |\Delta| \cdot \exp(i \phi_s^{NP})$ and

$$
\Delta = 1 + \frac{1}{M_{12}^{\text{SM}}} \frac{A_{d_{\mathcal{U}}} e^{-i\phi_{\mathcal{U}}}}{8 \sin d_{\mathcal{U}} \pi} \left(\frac{f_{B_s}^2 m_b^2}{m_{B_s}^3}\right) \left(\frac{m_{B_s}}{\Lambda_{\mathcal{U}}}\right)^{2d_{\mathcal{U}}} \frac{5c_q^2}{3},\tag{25}
$$

where M_{12}^{SM} is the standard model contribution.

And the time-dependent CP asymmetric observable $S_{\mu\mu}$ is [\[22,](#page-4-19)[24\]](#page-4-20)

$$
S_{\mu\mu} = \sin(2\phi_P - \phi_s^{\rm NP}),\tag{26}
$$

which is proportional to the helicity-summed timedependent rate asymmetry, $S_{\mu\mu} \sim \Gamma(B_s(t) \rightarrow \mu^+ \mu^-)$ – $\Gamma(\bar{B}_s(t) \rightarrow \mu^+ \mu^-).$

Figure [1](#page-2-1) shows the allowed values of c_q and c_ℓ versus $d_{\mathcal{U}}$ constrained by the measured branching ratio, Eq. ([1\)](#page-0-2). The behavior of Fig. [1](#page-2-1) can be inferred from Eqs. [\(15](#page-1-3)) and [\(18\)](#page-1-2). Note that C_P is proportional to $(m_{B_s}/\Lambda_u)^{2d_u} \approx$ (2.88×10^{-5}) ^du, which suppresses the unparticle contribution to the total branching ratio significantly for $1 <$ $d_{\mathcal{U}}$ < 2. Thus for larger values of $d_{\mathcal{U}}$, the value of $c_a \cdot c_\ell$ can be large to fit the experimental result. For some combinations of c_q and c_ℓ , $\mathcal{A}_{\Delta \Gamma}$ can be negative in Eq. ([24\)](#page-2-2), allowing rather smaller values of $d_{\mathcal{U}}$. As shown in Fig. [1](#page-2-1), for $d_{\mathcal{U}} \ge 1.4$, almost all the region of $0 \le c_q \le 1$ or $0 \le$ $c_{\ell} \leq 1$ is allowed. Figure [2](#page-3-0) shows the allowed region of (c_q, c_ℓ) for different values of $d_U \le 1.5$. Note that the red points corresponding to $1.4 \le d_U \le 1.5$ cover almost all the space of $0 \leq c_{q,\ell} \leq 1.0$. That is the reason why we do not consider the region $d_U > 2$ in this analysis. It was pointed out in [\[25\]](#page-4-21) that the best candidate for the scalar operator is the fermion bilinear $\mathcal{O} = \bar{\psi} \psi$, and current lattice simulation indicates that the scaling dimension of this operator is larger than 2. If that was the case, the scalar unparticle contribution gets very suppressed and the vector unparticle contributions might be comparable to the scalar ones. In this analysis we are considering the general scalar operator with scaling dimension $d_u \ge 1$.

In Fig. [3](#page-3-1) we show the time-dependent CP asymmetry parameter $S_{\mu\mu}$ as a function of $d_{\mathcal{U}}$. The figure shows that unconstrained $S_{\mu\mu}$ (red points) is mostly negative. But if

FIG. 1 (color online). Allowed region in $d_U - c_{\ell}$ (a) and $d_U - c_q$ (b) plane.

FIG. 2 (color online). Allowed values of c_q and c_ℓ for $1.0 \leq$ d_U < 1.1 (cyan, light gray), $1.1 \leq d_U$ < 1.2 (pink, dim gray), $1.2 \le d_U < 1.3$ (blue, black), $1.3 \le d_U < 1.4$ (green, silver), and $1.4 \le d_U < 1.5$ (red, gray). For $d_U \ge 1.5$, almost all the values of $0 \leq c_{q,\ell} \leq 1.0$ are allowed.

FIG. 3 (color online). Time-dependent CP asymmetry parameter $S_{\mu\mu}$ versus $d\mu$. Green (silver) points are from the constraints of $B_s \to \psi \phi$, while red (gray) ones are unconstrained.

we impose the constraints from $B_s \to \psi \phi$ where $-0.20 \le$ $S_{\psi\phi} \equiv \sin(2|\beta_s| - \phi_s^{\rm NP}) \le 0.20 \ (\beta_s \text{ is the phase of } V_{ts})$ [\[26\]](#page-4-22), then $-0.25 \leq S_{\mu\mu} \leq 0.2$ (green points). Note that the $S_{\psi\phi}$ constraint is very strong. If $S_{\mu\mu}$ turned out to be $|\mathcal{S}_{uu}| \ge 0.25$, it could not be explained by unparticles. Figure [3](#page-3-1) can be used to distinguish scalar unparticles from ordinary scalar particles. It was shown in [[26\]](#page-4-22) that $|S_{\mu\mu}| \lesssim$ 0.5 for C_P contributions from new scalar particles. In [\[26\]](#page-4-22) the nonzero phase of $S_{\mu\mu}$ comes from the complex couplings, but in this work the source of the phase is $\phi_{d_{\eta}}$ with real couplings. If $d_{\mathcal{U}} \rightarrow 1$ and the unparticle couplings are complex, then contributions of the scalar unparticle become those of ordinary scalar particles, since in this limit $C_P \rightarrow \frac{c_q c_\ell}{\Lambda_U^2}$, which is equivalent to the C_P of [\[26\]](#page-4-22).

It should be noticed that only a replacement of $(m_{B_s}/\Lambda_u)^{2d_u}(1/\Lambda_u^2)$ with $1/M_0^2$, where M_0 is a mass of some new scalar particle, is not enough to reduce the unparticle to an ordinary scalar particle, because there is a nontrivial phase associated with $d_{\mathcal{U}}$.

For nonintegral $d_{\mathcal{U}}$, it serves as a phase of new physics but it also suppresses new physics effects through $(m_{B_s}/\Lambda_u)^{2d_u}$. That's the reason why the allowed region of $S_{\mu\mu}$ from unparticles is smaller than that from ordinary particles. This is a very unique feature of unparticles. For ordinary particles, to suppress the new physics contributions, the new couplings should be small or the mass of new particle must be large. But in the unparticle scenario, nonintegral scaling dimension $d_{\mathcal{U}}$ can do the work, and $d_{\mathcal{U}}$ itself enters as a new phase as shown in Eq. [\(9\)](#page-0-3).

Current analysis is done for Λ _U = 1 TeV. For larger values of $\Lambda_{\mathcal{U}}$, the unparticle contribution gets smaller by $(m_{B_s}/\Lambda_u)^{2d_u}$ and the allowed parameter space becomes larger.

In conclusion, we have investigated the unparticle effects on $B_s \to \mu^+ \mu^-$ decay. The experimental result is quite consistent with the SM, but it does not mean that there is no room for new physics. In this analysis only the scalar unparticles are considered because vector unparticles are expected to give negligible contributions. Assuming that scalar unparticles couple to the left-handed current, we provided the allowed regions of the couplings $c_{q,\ell}$ and the scaling dimension $d_{\mathcal{U}}$ for a fixed $\Lambda_{\mathcal{U}} = 1$ TeV. Since the unparticle contributions are proportional to $(m_{B_s}/\Lambda_u)^{2d_u}$, the allowed parameter space of $c_{q,\ell}$ gets larger for large $d_{\mathcal{U}}$. The upper bound on Br($B_d \rightarrow \mu^+ \mu^-$) of Eq. [\(2\)](#page-0-4) would not give strong constraints on the model parameters, since the SM prediction of Eq. ([4](#page-0-5)) is almost an order of magnitude smaller. But if the branching ratio $Br(B_d \to \mu^+ \mu^-)$ is measured in the near future, a combined analysis with $B_s \rightarrow$ $\mu^+\mu^-$ would give some hints on the flavor structure of unparticle interactions. And the scalar unparticle predicts mostly negative $S_{\mu\mu}$, which could be used to distinguish unparticles from ordinary particles.

The author thanks Kang Young Lee for his recollections of the subject and helpful discussions. This work is supported by the WCU program through the KOSEF, funded by the MEST (R31-2008-000-10057-0).

CONSTRAINTS ON UNPARTICLES FROM ... PHYSICAL REVIEW D 88, 116003 (2013)

- [1] R. Aaij et al. (LHCb Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.110.021801) 110, [021801 \(2013\)](http://dx.doi.org/10.1103/PhysRevLett.110.021801).
- [2] A. J. Buras, J. Girrbach, D. Guadagnoli, and G. Isidori, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s10052-012-2172-1) 72, 2172 (2012).
- [3] A. Arbey, M. Battaglia, F. Mahmoudi, and D. M. Santos, Phys. Rev. D 87[, 035026 \(2013\).](http://dx.doi.org/10.1103/PhysRevD.87.035026)
- [4] D. Guadagnoli and G. Isidori, [arXiv:1302.3909.](http://arXiv.org/abs/1302.3909)
- [5] A. J. Buras, R. Fleischer, J. Girrbach, and R. Knegjens, [J.](http://dx.doi.org/10.1007/JHEP07(2013)077) [High Energy Phys. 07 \(2013\) 77.](http://dx.doi.org/10.1007/JHEP07(2013)077)
- [6] H. Georgi, Phys. Rev. Lett. 98[, 221601 \(2007\)](http://dx.doi.org/10.1103/PhysRevLett.98.221601); [Phys. Lett.](http://dx.doi.org/10.1016/j.physletb.2007.05.037) B 650[, 275 \(2007\)](http://dx.doi.org/10.1016/j.physletb.2007.05.037).
- [7] C. H. Chen and C. Q. Geng, *[Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.76.115003)* **76**, 115003 [\(2007\)](http://dx.doi.org/10.1103/PhysRevD.76.115003).
- [8] R. Mohanta and A. K. Giri, [Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2008.01.009) 660, 376 (2008).
- [9] R. Mohanta and A. K. Giri, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.76.075015) 76, 075015 [\(2007\)](http://dx.doi.org/10.1103/PhysRevD.76.075015).
- [10] A. Lenz, *Phys. Rev. D* **76**[, 065006 \(2007\)](http://dx.doi.org/10.1103/PhysRevD.76.065006).
- [11] J. K. Parry, *Phys. Rev. D* **78**[, 114023 \(2008\).](http://dx.doi.org/10.1103/PhysRevD.78.114023)
- [12] J.-P. Lee, *Phys. Rev. D* **82**[, 096009 \(2010\)](http://dx.doi.org/10.1103/PhysRevD.82.096009).
- [13] X. Q. Li and Z. T. Wei, *[Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2007.06.045)* **651**, 380 (2007).
- [14] S. L. Chen, X. G. He, X. Q. Li, H. C. Tsai, and Z. T. Wei, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s10052-008-0823-z) 59, 899 (2009).
- [15] A. Moyotl, A. Rosado, and G. Tavares-Velasco, *[Phys. Rev.](http://dx.doi.org/10.1103/PhysRevD.84.073010)* D 84[, 073010 \(2011\)](http://dx.doi.org/10.1103/PhysRevD.84.073010).
- [16] A. Moyotl and G. Tavares-Velasco, *[Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.86.013014)* 86, [013014 \(2012\).](http://dx.doi.org/10.1103/PhysRevD.86.013014)
- [17] B. Grinstein, K. A. Intriligator, and I. Z. Rothstein, *[Phys.](http://dx.doi.org/10.1016/j.physletb.2008.03.020)* Lett. B **662**[, 367 \(2008\)](http://dx.doi.org/10.1016/j.physletb.2008.03.020).
- [18] D. Becirevic, N. Kosnik, F. Mescia, and E. Schneider, Phys. Rev. D 86[, 034034 \(2012\).](http://dx.doi.org/10.1103/PhysRevD.86.034034)
- [19] W. Altmannshofer, P. Ball, A. Bharucha, A. J. Buras, D. M. Straub, and M. Wick, [J. High Energy Phys. 01](http://dx.doi.org/10.1088/1126-6708/2009/01/019) [\(2009\) 019.](http://dx.doi.org/10.1088/1126-6708/2009/01/019)
- [20] A. K. Alok, A. Dighe, D. Ghosh, D. London, J. Matias, M. Nagashima, and A. Szynkman, [J. High Energy Phys. 02](http://dx.doi.org/10.1007/JHEP02(2010)053) [\(2010\) 053.](http://dx.doi.org/10.1007/JHEP02(2010)053)
- [21] S. Descotes-Genon, J. Matias, and J. Virto, *[Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.85.034010)* 85[, 034010 \(2012\)](http://dx.doi.org/10.1103/PhysRevD.85.034010).
- [22] K. De Bruyn, R. Fleischer, R. Knegjens, P. Koppenburg, M. Merk, and N. Tuning, Phys. Rev. D 86[, 014027 \(2012\).](http://dx.doi.org/10.1103/PhysRevD.86.014027)
- [23] K. De Bruyn, R. Fleischer, R. Knegjens, P. Koppenburg, M. Merk, A. Pellegrino, and N. Tuning, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.109.041801) 109[, 041801 \(2012\)](http://dx.doi.org/10.1103/PhysRevLett.109.041801).
- [24] R. Zwicky, *Phys. Rev. D 77[, 036004 \(2008\)](http://dx.doi.org/10.1103/PhysRevD.77.036004)*.
- [25] F. Sannino and R. Zwicky, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.79.015016) 79, 015016 [\(2009\)](http://dx.doi.org/10.1103/PhysRevD.79.015016).
- [26] A. J. Buras, F. De Fazio, J. Girrbach, R. Knegjens, and M. Nagai, [J. High Energy Phys. 06 \(2013\) 111.](http://dx.doi.org/10.1007/JHEP06(2013)111)