# Initial data for neutron star binaries with arbitrary spins

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The starting point of any general relativistic numerical simulation is a solution of the Hamiltonian and momentum constraints that (ideally) represents an astrophysically realistic scenario. We present a new method to produce initial data sets for binary neutron stars with arbitrary spins and orbital eccentricities. The method only provides approximate solutions to the constraints. However, we show that the corresponding constraint violations subside after a few orbits, becoming comparable to those found in evolutions of standard conformally flat, helically symmetric binary initial data. We evolve in time data sets corresponding to binaries with spins aligned, zero, and antialigned with the orbital angular momentum. These simulations show the orbital "hang-up" effect previously seen in binary black holes. Additionally, they show orbital eccentricities that can be up to 1 order of magnitude smaller than those found in helically symmetric initial sets evolutions.

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# I. INTRODUCTION

Binary neutron stars (BNS) are currently some of the most studied objects in astrophysics due to their potential as engines for short gamma-ray bursts [1,2] and as generators of detectable gravitational waves (GW) [3]. Recent detection rate estimations for the advanced interferometric detectors are in the range of 0.4–400 BNS events per year [4], making the observation of GW from BNS very likely in the next few years. However, given the complex nature of neutron stars (NS), a numerical modeling of the last few orbits and the merger of such binaries is essential for the interpretation of the corresponding GW signatures.

Every numerical simulation has a starting point that is, essentially, a snapshot of all the fields (gravitational, hydrodynamical, electromagnetic, etc.) at a given time. Depending on the characteristics of the modeling formalism, these fields can either be freely specified or constrained by a set of conditions. Numerical simulations in general relativity that are based on "3 + 1"-type formalisms are of the latter kind: the fields have to be solutions of the Hamiltonian and momentum constraints to be consistent with the full set of the Einstein field equations [5]. The Hamiltonian and momentum constraints are four coupled second-order elliptic PDEs that are solved numerically through some iterative procedure that starts with an initial guess and loops around the equations, correcting the fields until some predetermined convergence criteria are reached. Since these four equations are not enough to determine the ten independent components of the spacetime metric, the modeler has the freedom to choose additional constraints/ conditions. When it comes to finding initial states for BNS in circular orbits, the most popular approach is the Wilson-Mathews conformal "thin-sandwich" scheme [6,7], which consists of restricting the solutions with three extra conditions: that the spatial 3-metric  $\gamma_{ii}$  be conformally flat,

that the slicing be maximal  $[tr(K_{ij}) = 0$ , where  $K_{ij}$  is extrinsic curvature], and that the spacetime be helically symmetric (simply put, that the fields be time independent in the frame that corotates with the binary). The first two conditions reduce the number of unknowns from ten to five (the conformal factor, the lapse function, and the three components of the shift vector). The third, however, is related to another concern of the initial data (ID): the need for it to represent "astrophysically realistic" scenarios.

A great deal could be discussed about what constitutes an astrophysically realistic BNS, particularly since we are largely ignorant of the state of matter inside a neutron star. However, there are two aspects of these systems that most researchers agree on. One is related to the circularity of the orbits of a BNS system that has evolved in isolation. In cases like these, it is expected that any initial eccentricity the binary may have acquired at birth will be minimized by emission of gravitational radiation [8] (for instance, the BNS known as PSR 1913 + 16 is supposed to end its life with eccentricities of about  $10^{-6}$  [9]). Recent estimates of Advanced LIGO event rates indicate that the fraction of BNS formed by stellar evolution of binary systems with eccentricities larger than 0.01 is, for the most optimistic scenario, below 2% [10]. BNS formed by dynamical capture are expected to have higher eccentricities by the time they merge. However, their detection event rate is uncertain and likely to be much smaller than the one corresponding to the binary evolution channel (see Ref. [11] and references therein). While the helical symmetry condition demands exact circular orbits, it actually produces nonnegligible eccentricities that, as it is shown below, surpass 0.01 by a factor of several (see also Ref. [12]).

The other aspect of astrophysically realistic ID sets is that they should, in principle, be able to describe spinning stars. Finding ways to construct ID for binaries with spinning NS has been a problem more difficult to address. Neutron stars obey hydrodynamical equations such as the general relativistic versions of the continuity and Euler equations, and any description of fluids in rotation should be consistent with them. The original work of Wilson and collaborators handled the hydrodynamics through a lengthy evolution process that, while not practical for the production of ID sets, permitted the imposition of arbitrary NS spins by the way of angular momentum drivers that forced the stars to adopt the desired rotations. The impractical nature of this method gave rise to a search for simpler techniques. One of the first to be considered was the special case in which the two stars are tidally locked or "corotating" [13,14]. Under corotation, the fluid is static in the frame that rotates with the BNS, and the continuity equation is trivially satisfied. These cases are unlikely to exist in nature since they would require fluid viscosities unrealistically high [15,16], but they are still useful to test new algorithms and numerical codes. Corotating solutions were followed by solutions with null fluid vorticity ("irrotational"). This formalism was developed to find solutions for BNS with (nearly) zero spin by the way of specifying the fluid velocity as the gradient of a potential [17-20]. This potential is obtained from an additional elliptic equation derived from imposing zero vorticity. Since its introduction, this formalism has become the preferred method for BNS ID production, and several groups have developed codes and techniques for its implementation [17,21-29]. All simulations of BNS in circular orbits performed to date are either based on corotating or irrotational ID sets [30]. In recent times, several groups have experimented with nonconformally flat techniques [31-33]. Among these, the works by Anderson et al. [34], Gold et al. [11], East et al. [35], and Kastaun et al. [36] are of relevance to this paper, and more about them is said in Sec. II.

However, in general, neutron stars in binaries are expected to be spinning. A good example of this is the double pulsar PSR J0737-3039 [37] that could have one of the stars spinning at a rate of about  $\sim 27$  ms at the time of the merger [38]. Numerical schemes to produce ID for spinning BNS have been presented by Marronetti and Shapiro [39], Baumgarte and Shapiro [40], and Tichy [38,41]. All of these are based on the Wilson–Mathews helically symmetric, conformally flat approximation. Like in the case of irrotational BNS, these methods also rely on advanced computationally intensive iterative algorithms.

We present here a method for producing ID corresponding to spinning BNS that also allows for arbitrary orbital and radial velocities. This freedom gives more control over the orbital eccentricity than in the case of helically symmetric methods. Our method does not look for solutions of the Hamiltonian and momentum constraints: their satisfaction is only asymptotic with binary separation. This has the advantage of not requiring the numerical solution of elliptic equations, thus greatly simplifying its implementation. To find out the impact of the resulting constraint violations, we produced nonspinning BNS ID sets, evolved them in time, and compared the results with those of simulations starting with irrotational ID generated with the LORENE library [26,42]. To facilitate the simulations, we implemented our method as a module ("thorn") of the Einstein Toolkit (ET) [43,44]. We evolved these BNS for up to seven orbits before merger and show that, for the grid resolutions and binary separations studied here, the constraint violations in both simulations become comparable before the merger [45]. Additionally, we show that our ID sets can lead to orbits that exhibit eccentricities smaller than those resulting from evolving helically symmetric ID sets. Finally, we present the evolution of ID sets with spinning NS (spins aligned and counteraligned to the orbital angular momentum) that showcase the ability of our method to handle rotating stars. These simulations present the orbit hang-up effect [47] in BNS that is also seen in Ref. [36].

This article is organized as follows. Sections II and III introduce our method and present some tests, respectively. In Sec. IV we use our approach to construct ID for non-spinning and spinning binaries and show the results of their evolution in full general relativistic hydrodynamics using the Einstein Toolkit [43]. Finally, we will briefly summarize our findings in Sec. V. Several of the figures presented below contain temporal and spatial coordinates, which are displayed both in Systeme International (SI) units and normalized by a nominal constant  $M_3 \equiv 3M_{\odot}$ .

### **II. CONSTRUCTION OF INITIAL DATA SETS**

#### A. Single rotating neutron stars

Our approximation to ID for BNS starts with the solution of an isolated rotating NS in equilibrium. The study of stationary rotating NS has been undertaken by a number of groups in the past (see Ref. [48] and references therein). These studies have led to the creation of publicly available codes specially designed to find numerical solutions in the framework of the theory of general relativity. One such code is RNS, developed by Stergioulas and Friedman [49,50] and based on the Komatsu–Eriguchi–Hachisu method [51,52], which describes the geometry of stationary and axisymmetric rotating NS with a metric of the form

$$ds^{2} = -e^{A+B}dt^{2} + e^{2C}(dr^{2} + r^{2}d\theta^{2}) + e^{A-B}r^{2}\sin^{2}\theta(d\phi - Ddt)^{2},$$
(1)

where the metric functions A, B, C, and D depend on r and  $\theta$ . The equations for the gravitational and matter fields are then solved using a combination of integral and finite-differencing techniques [52].

## B. Our initial data

Our ID is produced following these three steps:

- (i) Calculate the fields corresponding to two isolated rotating neutron stars using RNS.
- (ii) Rotate (if needed) and boost independently each solution, and map them into a single inertial frame, making sure that the BNS total linear momentum is zero.
- (iii) Superpose the fields as indicated below.

Step i is straightforward and generates two stationary solutions for rotating NS. Each one is originally given in the reference frame of the RNS code:  $x'^{\mu}$ . RNS provides solutions in polar coordinates with the NS rotating around the z' axis. Since we are interested in NS with spins arbitrarily aligned, a rotation of the solutions may be required in combination with the boost. To simplify the notation, we will ignore here the rotation (i.e., we will consider BNS with the spins in the direction of the orbital angular momentum).

Step ii is inspired by standard binary black hole (BBH) superposition methods [53,54] and starts with the Lorentz boost of the RNS coordinates into the Cartesian inertial frame coordinates  $x^{\mu}$ ,

$$x^{\nu} = {}_a \Lambda^{\nu}_{\mu} x^{\prime \mu}, \qquad (2)$$

where the Lorentz transformation  $_{a}\Lambda^{\nu}_{\mu}$  is a function of the corresponding boost velocity  $\mathbf{v}_{a}$ , with the index *a* labeling each star (*a* = 1, 2). We now map the metric functions to the new coordinate system using Eq. (2):

$${}_{a}A'(x'^{\mu}) \to {}_{a}A'(x^{\nu}) \qquad {}_{a}B'(x'^{\mu}) \to {}_{a}B'(x^{\nu})$$
$${}_{a}C'(x'^{\mu}) \to {}_{a}C'(x^{\nu}) \qquad {}_{a}D'(x'^{\mu}) \to {}_{a}D'(x^{\nu}).$$

This allows us to write the spacetime metric  $g_{\tau\lambda}^{\prime a}$  as a function of the new coordinates  $x^{\nu}$  and Lorentz transform it to the inertial frame

$$_{a}g_{\tau\lambda}(x^{\nu}) = _{a}\Lambda^{\delta}_{\tau a}\Lambda^{\eta}_{\lambda a}g'_{\delta\eta}(x^{\nu}), \qquad (3)$$

where there is no summation over *a*. Since we are interested in solutions in terms of a 3 + 1 decomposition of the metric, we extract from  ${}_{a}g_{\tau\lambda}(x^{\nu})$  the corresponding lapse function  ${}_{a}\alpha$ , shift vector  ${}_{a}\beta^{i}$ , and spatial metric  ${}_{a}\gamma_{ij}$ . Similarly, a mapping/transformation is applied to the rest mass and fluid velocity  ${}_{a}\rho'$  and  ${}_{a}\nu'^{i}$  to obtain the fields  ${}_{a}\rho$ and  ${}_{a}\nu^{i}$ . The latter is defined as  $\nu^{i} = (u^{i}/u^{0} + \beta^{i})/\alpha$ , where  $u^{\mu}$  is the 4-velocity of the fluid.

Step iii constructs a single global set of gravitational fields by a superposition of these two solutions:

$$\alpha = {}_{1}\alpha + {}_{2}\alpha - 1 \qquad \beta^{i} = {}_{1}\beta^{i} + {}_{2}\beta^{i}$$
  
$$\gamma_{ij} = {}_{1}\gamma_{ij} + {}_{2}\gamma_{ij} - \delta_{ij}.$$
(4)

Since there is no overlap between the stars, the superposition of the hydrodynamics fields is simply

$$\rho = {}_{1}\rho + {}_{2}\rho \qquad v^{i} = {}_{1}v^{i} + {}_{2}v^{i}.$$
 (5)

In addition to the stellar matter, a pervasive atmosphere is added outside the stars with a relatively low density  $\rho_{\text{atm}} = 10^{-7} \rho_{\text{max}} (t = 0)$  and zero velocity. The remaining hydrodynamical fields (pressure and internal energy) are set by the equation of state (EOS). Finally, the extrinsic curvature is calculated using

$$K_{ij} = -\frac{1}{2\alpha} (\partial_t \gamma_{ij} - \mathcal{L}_\beta \gamma_{ij}), \qquad (6)$$

where  $\mathcal{L}_{\beta}$  is the Lie derivative along the direction of the shift vector.

Superpositions such as this have been used for BNS simulations in the past. We will refer to them as "simple superposition." In particular, Anderson et al. [34], Gold et al. [11], and, more recently, East et al. [35] and Kastaun et al. [36] have generated and evolved BNS ID sets using either a superposition similar to the one described above or even adding the extra step of actually solving the Hamiltonian and momentum constraints [55]. However, ID sets constructed in this way present two undesirable features which are evident during their time evolution: relatively large oscillations of the stellar shape and orbital eccentricities. Below, we describe two modifications to simple superposition that reduce spurious effects. Both of them play a role in controlling shape oscillations and eccentricities, even when each modification plays a dominant role in controlling a particular problem.

The oscillations of the stellar shape can be observed by monitoring the central rest mass density, as shown in Fig. 1.



FIG. 1 (color online). Maximum rest mass density for simulations of nonspinning binaries starting at a coordinate separation of 60 km. The evolution of a reference ID set (LORENE60 in Table I) is compared with four ID sets constructed using superposition (BNS60-xxx-yyy). The latter cover cases with (oc) and without (noc) "overcontraction" [Eq. (7) with *n* equal to 4 or 1, respectively] and with (rs) and without (nrs) rescaling [Eq. (9)]. The value  $M_3$  used for normalization in the upper *x* axis is defined as  $3M_{\odot}$ .

The solid line corresponds to the evolution of a reference ID with initial separation of 60 km generated by the LORENE library (LORENE60 in Table I, also known as G2\_I12VS12\_D5R33\_60KM). Details of the time evolution are given in Sec. III. The curve labeled BNS60-noc-nrs corresponds to a comparable ID set generated using the steps mentioned above. This curve presents large oscillations that contrast with the flatness of the evolution of LORENE60. While the amplitude of the oscillations is partially due to the grid sparseness, the difference between both runs indicates that there are additional causes at play. One of them is the fact that simple superposition does not make any attempt at coupling the hydrodynamical fields (obtained from single NS solutions) with the metric fields calculated in Eq. (4). These oscillations will diminish with increasing binary separation (see Table I in Ref. [35]) and could, to some extent, be controlled by introducing fluid viscosity terms in the Euler equations. However, we explored alternative ways of minimizing this effect that could be easily implemented in the ID generation code. Visual inspection of the stellar cross section on the orbital plane showed that the stars corresponding to the LORENE ID set are approximately oval in shape, with the diameter along the direction between stellar centers larger than the one in the direction of the orbital velocity. While our ID also presents this feature (a result of the Lorenz contraction in the boost direction), it does so at a lesser degree. As an experiment, we tried increasing the deformation of the stars in our ID by replacing the coordinate transformation (2) with

$$x^{\nu} = (_a \Lambda^{\nu}_{\mu})^n x'^{\mu}, \tag{7}$$

where the exponent indicates that the transformation matrix was applied n times. The result of this experiment corresponding to n = 4 is shown as the evolution of the ID set BNS60-oc-nrs in Fig. 1. One problem of this method is that the free parameter n is confined to integer values, limiting the method's fine-tuning capabilities. To compensate for this, we devised an alternative that achieves this overcontraction by using a single Lorentz transformation,

$$x^{\nu} = {}_{fa}\Lambda^{\nu}_{\mu}x^{\prime\mu},\tag{8}$$

where  ${}_{fa}\Lambda^{\nu}_{\mu}$  is now a function of a velocity  $\mathbf{v}_{fa} = f \times \mathbf{v}_a$ with f a real positive number. A comparison of the results obtained with these two techniques is given in Fig. 18, which is discussed in Sec. IVA 2. Note that the overcontraction is applied only in the coordinate transformation (7) or the one in Eq. (8) and *not* in the transformation of the components of the metric (3) or the hydrodynamical fields.

TABLE I. Parameters of the ID sets used in the binary simulations. The coordinate separation is given by d, while  $M_0$ ,  $M_{ADM}$ , and  $J_{ADM}$  are the total rest mass, ADM mass, and ADM angular momentum, respectively.  $M^*$  is the ADM mass of the corresponding LORENE set. a is the dimensionless spin parameter for each NS, and  $v^{\phi}$  and  $v^r$  are the tangential and radial components of the boost velocity. n/f is the overcontraction parameter: integers correspond to values of n in Eq. (7), while real numbers correspond to values of the f in Eq. (8). Set refers to the parameters  $\alpha_d$ ,  $\beta_d$ , and  $\epsilon_{diss}$  used in the evolution, and Resolution is the maximum spatial resolution. The numerals in the labels indicate the initial coordinate separation in kilometers. The suffixes of the top part of the table indicate whether overcorrection was applied or not and whether rescaling was applied or not. The suffixes of the bottom part of the table indicate if the stellar spins are up (u), down (d), or null (n) and if the simulation was performed in low (lr), medium (mr), or high resolution (hr).

	$d/M^*$	$M_0[M_{\odot}]$	$M_{\rm ADM}[M_{\odot}]$	$J_{\rm ADM}[M_{\odot}^2]$	а	$v^{\phi}/c$	$v^r/c$	n/f	rl	Set	Resolution
BNS60_noc_nrs	13.45	3.566	3.311	9.377	0	0.1450	0	1	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
BNS60_oc_nrs	13.45	3.454	3.207	9.081	0	0.1450	0	4	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
BNS60_noc_rs	13.45	3.385	3.138	9.849	0	0.1450	0	1	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
BNS60_oc_rs	13.45	3.279	3.039	9.537	0	0.1450	0	4	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
LORENE60	13.45	3.250	3.005	9.716	0	0.1238	0.0	•••	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
LORENE80	18.02	3.250	3.011	10.825	0	0.1098	0.0	•••	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
BNS50n	11.30	3.250	3.006	8.985	0	0.1615	-0.0010	4	5	(0.0, 1.0, 0.01)	$0.50 M_{\odot}$
BNS60n	13.45	3.250	3.020	9.718	0	0.1450	-0.0040	4	5	(0.0, 1.0, 0.01)	$0.50 M_{\odot}$
BNS70n	15.82	3.250	3.018	10.060	0	0.1360	-0.0045	4	5	(0.0, 1.0, 0.01)	$0.50 M_{\odot}$
BNS80n	18.02	3.250	3.020	10.497	0	0.1265	-0.0050	4	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
LORENE60_lr	13.45	3.250	3.004	9.716	0	0.1238	0.0	•••	5	(1.0,0.5,0.10)	$0.50 M_{\odot}$
LORENE60_mr	13.45	3.250	3.005	9.716	0	0.1238	0.0	•••	6	(1.0,0.5,0.10)	$0.25 M_{\odot}$
LORENE60_hr	13.45	3.250	3.005	9.716	0	0.1238	0.0	•••	6	(1.0,0.5,0.10)	$0.1875 M_{\odot}$
BNS60n_lr	13.45	3.252	3.018	9.718	0	0.1490	-0.0020	2.1	5	(1.0,0.5,0.10)	$0.50 M_{\odot}$
BNS60n_mr	13.45	3.252	3.018	9.718	0	0.1490	-0.0010	2.1	6	(1.0,0.5,0.10)	$0.25 M_{\odot}$
BNS60n_hr	13.45	3.252	3.018	9.718	0	0.1490	-0.0010	2.1	6	(1.0,0.5,0.10)	$0.1875 M_{\odot}$
BNS80u	18.02	3.250	3.034	12.142	0.327	0.1250	-0.0050	4	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$
BNS80d	18.02	3.250	3.032	8.984	-0.327	0.1265	-0.0050	4	5	(0.0,1.0,0.01)	$0.50 M_{\odot}$

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The second problem of the ID recipe as given at the beginning of the section is related to the orbital eccentricity: using the superposition outlined in Eqs. (4) and (5)leads to binaries that exhibit noncircular orbits. As expected, this problem also diminishes with increasing binary separation. We believe this is primarily due to the fact that the hydrodynamical fields are not "adjusted" to reflect the change in the gravitational fields caused by superposition. For instance, the gravitational field resulting from superposition is stronger than that of a single star, leading to a more compact stellar structure. Again we experimented with alternatives to the simple recipe given in Eqs. (5). One way to compensate for the increase in stellar density is to modify the RNS profiles  $_a\rho$  and  $_av^i$ with factors dependent on some of the gravitational fields. A simple choice, albeit not the only one, is to use  $(\alpha/_{a}\alpha)^{nr}$ for  $\rho$  and  $(a\alpha/\alpha)^{n\nu}$  for  $\nu^i$ , where the integer exponents nrand nv are free parameters:

$$\rho = \left(\frac{\alpha}{1\alpha}\right)^{nr}{}_{1}\rho + \left(\frac{\alpha}{2\alpha}\right)^{nr}{}_{2}\rho$$

$$v^{i} = \left(\frac{1\alpha}{\alpha}\right)^{nv}{}_{1}v^{i} + \left(\frac{2\alpha}{\alpha}\right)^{nv}{}_{2}v^{i}.$$
(9)

This rescaling could be interpreted as a weighted average of the hydrodynamics fields by a measure of the spacetime curvature. We tested this formula for different values of the exponents ranging from 0 to 3, and the results are presented in Fig. 2 [56]. The simulation that exhibits the smaller orbital eccentricity corresponds to the case nr = 1 and nv = 2, and, based on these tests, we decided to adopt those values of all the runs in this article that employ rescaling.



FIG. 2 (color online). Coordinate separation for simulations of nonspinning binaries starting at a distance of 60 km. The effect of the rescaling of hydrodynamical fields is shown for all the integer values of the exponents nr and nv in Eq. (9) from 0 to 3. The lowest eccentricity is achieved by the combination (nr = 1, nv = 2), depicted with a solid curve. All these runs employed the overcontraction of Eq. (7) with n = 4.

Each one of the modifications to superposition introduced here (overcontraction and rescaling) affect both shape oscillations and orbital eccentricity. Figures 1 and 3 show this by comparing runs with sets with (oc) and without (noc) overcontraction and with (rs) and without (nrs) rescaling. It is clear that optimal results are obtained when both modifications are applied (curves labeled BNS60-oc-rs).

To summarize, our recipe for BNS ID consists of following steps i–iii, employing either the coordinate transformation given in Eq. (7) or the one in Eq. (8) and the calculation of the fields given in Eqs. (4), (6), and (9).

We conclude this section with some thoughts about the motivation behind the overcontraction and rescaling techniques. We do not offer here any rigorous justification for them beyond their empirical success. While we believe that proper mathematical studies could provide strong reasons for the choices we made and suggest improvements, the process by which we constructed these methods was a combination of intuition and trial and error. As we already mentioned, we believe that the uncoupling of the matter and gravitational fields caused by simple superposition is the root of the problem, and overcontraction and rescaling constitute a rather simple attempt at adjusting the matter fields to the new gravitational background. It has been suggested to us that other alternatives could be used to attain similar goals. One, for instance, is the use of different coordinate systems including variations of the lapse and shift that, if properly chosen, would have the additional advantage of not exacerbating the constraints' violations. We have not tried this here since coordinate transformations would not affect the relation between gravitational and hydrodynamical fields, and, in our opinion, they do not address directly the problem. However, we do believe that our methods can be improved, and we will dedicate future studies to that effect.



FIG. 3 (color online). Coordinate separation for the runs of Fig. 1.

# **III. NUMERICAL TESTS**

The algorithms described in the previous section have been implemented in a numerical module (thorn) for the ET framework [43,44]. This thorn will be made publicly available in the near future. The code accepts the selection of one or two NS with arbitrary boost velocities, spin directions, and initial positions. The characteristics of the NS (mass, spin, and EOS) are selected through free parameters in RNS which provides the stellar profiles to be mapped into the ET grid. To test our code, we generated ID for single and binary NS and evolved them using ET. Almost all the simulations have the same grid domain: 5 levels of mesh refinement, provided by CARPET thorn [57], with box sizes  $320M_{\odot}$  (outer boundary),  $120M_{\odot}$ ,  $60M_{\odot}$ ,  $30M_{\odot}$ , and  $15M_{\odot}$ , resulting in a resolution of approximately 36 points across the stellar diameter. Since it is not our intention to produce high quality BNS models but to test the viability of our ID, we opted for a computationally affordable and expedient numerical setup. The only exceptions are the medium- and high-resolution cases presented in the third block of Table I that have extra levels of mesh refinement, increasing the number of grid points across the star to 72 and 96, respectively.

The BNS simulations for this article make use of xy-plane reflection and  $\pi$ -rotation symmetries since they pertain to systems with identical NS with nonprecessing orbits. We employ a polytropic EOS  $(p = K\rho^{\Gamma})$  with K =123.6 and  $\Gamma = 2.0$  for both the ID sets and the evolution. Spacetime evolution is obtained through the Baumgarte-Shapiro-Shibata-Nakamura-Oohara-Kojima formalism (BSSNOK) [58–60], provided by the MCLACHLAN/ ML\_BSSN thorn [61]. The general relativistic hydrodynamic equations are evolved by the GRHYDRO thorn [62]. We use a Marquina Riemann solver with piecewise parabolic method (PPM) reconstruction of the primitive variables. Kreiss-Oliger dissipation is added to the right-hand sides of the BSSNOK evolution equations, modulated by the dissipation strength parameter  $\epsilon_{diss}$ . Finally, the lapse function and shift vector are evolved in time using

$$\partial_t \alpha - \beta^j \partial_j \alpha = -2\alpha (\operatorname{tr}(K_{ij}) + \alpha_d(\alpha - 1)),$$
  

$$\partial_t \beta^i - \beta^j \partial_j \beta^i = 0.75 (\tilde{\Gamma}^i - \beta_d \beta^i).$$
(10)

The parameters  $\alpha_d$  ("alpha driver"),  $\beta_d$  ("beta driver"), and  $\epsilon_{\text{diss}}$  adopted the values detailed in Table I.

The runs presented here were performed on the Cray XT5 system "Kraken" of The National Institute for Computational Sciences. The computational resources needed for a given simulation are a function of the separation distance and the grid structure, as well as the physical characteristics of the BNS (masses, spins, etc.). The low resolution ( $\Delta x = 0.50M_{\odot}$ ) runs for nonspinning BNS starting at a separation of 60 (80) km required close to 2 (3.5) KSUs (thousands of Service Units). However,

we need to add to this amount the computer time spent determining the optimal boost velocity. This typically involved ten iterations of about three orbits each, increasing the number of KSUs from 2 (3.5) to 11 (20)for 60 (80) km separation runs. BNS with nonzero spins such as those described in the last block of Table I will have inspirals of different lengths, requiring computer times that in our cases ranged from 19 (BNS80d) to 23 (BNS80u) KSUs. The nonspinning BNS simulations with medium and high resolutions described in the third block of Table I take as much as 105 and 570 KSUs, respectively (these figures include the determination of the boost velocity). The total amount of computer time spent on the runs presented in this article was close to 1,000 KSUs. The low-resolution runs were executed using either 12 or 24 cores. For the medium- and high-resolution runs, we found that the optimal number of cores was 64 and 240, correspondingly.

#### A. Isolated stars

We start our tests with four single NS cases: with and without spin and stationary and boosted. While these seem rather trivial since they only involve mapped solutions of the RNS code into the ET grid, they fulfill two purposes: to test the mapping/boost algorithms and to provide an apt reference in terms of the constraint violations that will be useful when analyzing the simulations of Sec. IV. The NS rest masses are  $M_0 = 1.625 M_{\odot}$  (compaction ratio = 0.14). The dimensionless spin parameter  $a (J/M^2)$  is either zero or 0.33, and the boost velocity v is either zero or 0.2c. Figure 4 shows the evolution of the maximum rest mass density. We observe a stable evolution for all four cases, with central density oscillations consistent with our grid resolution. Figure 5 shows the Hamiltonian and momentum constraint violations for the four cases under consideration.



FIG. 4 (color online). Normalized maximum rest mass density for four single NS test cases that include stationary, spinning and boosted stars.

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FIG. 5 (color online). Hamiltonian and momentum constraint violation ( $L_2$  norm) for the runs of Fig. 4.

#### **B.** Binaries

Figure 6 presents a comparison of several metric fields between a LORENE-generated irrotational ID (LORENE80 in Table I, also known as G2\_I12VS12\_D5R33\_80KM) and a nonspinning binary ID set with coordinate separation of 80 km produced with our method (BNS80n in Table I). These plots show that even the simple superposition of Eq. (4) gives good agreement. We experimented with higher-order alternatives that, while reducing the separation between curves, did not improve noticeably the results of the time evolution. The agreement in the fluid velocity can be further improved by adding small positive spins to the NS. We decided to neglect this higher-order correction in this paper. Figure 7 shows a point-by-point convergence of the BNS80n ID set along the line connecting the stars that is consistent with the fourth order of the finite-difference stencils used for spatial derivatives. For this convergence plot, we set the initial data on an extended unigrid for the resolutions  $\Delta x = (0.50M_{\odot}, 0.25M_{\odot}, 0.125M_{\odot})$ , which correspond to (0.738, 0.369, 0.184) in kilometers. Almost all our simulations have a central resolution equal to the lowest of the ones shown in Fig. 7 ( $\Delta x = 0.50 M_{\odot}$ ). The exceptions are the medium- and high-resolution runs presented in the third block of Table I.

### **IV. BINARY EVOLUTIONS**

#### A. Comparison with known initial data

One of the most important tests of any ID set is provided by its evolution. Qualitatively good agreement between the fields such as the one presented in Fig. 6 could lead to large behavior differences after several orbits. In this section we study the evolution of nonspinning ID sets produced by our method and compare them with those produced with the LORENE library. As previously mentioned, the goal of these simulations is not to provide highly accurate models of the mergers but simply



FIG. 6 (color online). Comparison of several fields from the reference ID set LORENE80 (red solid line) and our nonspinning ID set BNS80n (blue dashed line). The fields are plotted along the line connecting the two NS centers.

to test the ID sets; the simulations track the BNS evolution until the code crashes due to the formation of singularities, and no attempt is made to study in detail the formation/evolution of the newly created compact object and/or detect horizons.

### 1. Varying binary separation

We start our tests by evolving sets with coordinate separations of 60 km (BNS60n) and 80 km (BNS80n) and comparing them with their LORENE counterparts. These simulations' parameters are given in the second block of Table I.

While some of the design parameters of the BNS sets were chosen to produce a meaningful comparison with the corresponding LORENE sets (coordinate separation, total rest mass, and zero spins), the boost velocities were finetuned to minimize eccentricity. The purpose was to find ID sets less eccentric than those based on helical symmetry. This idea was inspired by the work of Miller [12], PETR TSATSIN AND PEDRO MARRONETTI



FIG. 7 (color online). Hamiltonian constraint convergence of nonspinning BNS ID sets with a separation of 80 km. The plot shows the difference between medium  $(0.25M_{\odot})$  and low  $(0.5M_{\odot})$  resolution (solid line) and the difference (scaled for fourth-order convergence) between the high  $(0.125M_{\odot})$  and medium resolution (dashed line).

who showed that zeroing the radial velocity could lead to non-negligible orbital eccentricities. More recent work done on BBH [63-67] and BNS [29] ID sets show that this eccentricity can be controlled to some extent by a careful choice of tangential and transverse velocities. The determination of these velocity components was done by a corrective iteration that started with a null radial velocity  $v^r$  and a post-Newtonian estimation [68] for the tangential velocity  $v^{\phi}$  [69]. The iteration alternates adjustments for both components using a bisectionlike algorithm that, in average, bracketed the velocity components after ten iterations. The boost velocity determination could be sped up by adopting more efficient techniques such as the methods developed for BBH ID sets [65,70], and this will be explored in future work. The optimal boost velocity for each BNS set evolved for this article is given in Table I.

Figure 8 shows three snapshots of the rest mass density for the BNS80n and the LORENE80 simulations, while Fig. 9 plots the trajectory of one of the NS for each simulation. Figure 10 compares the evolution of half of the coordinate separation between NS centers for the BNS60n and BNS80n runs and the respective LORENE counterparts. We see that the orbital eccentricities of the BNS runs are smaller than those of the LORENE runs, a difference that can be quantitatively appreciated in the eccentricity plot of Fig. 11 (the eccentricity was calculated using the formula (1) from Ref. [70]). By the time of the last orbits, the BNS runs' eccentricities are close to 1 order of magnitude smaller than those of the LORENE simulations. Note that the method of adjusting the orbital velocity to reduce eccentricity can also be applied to LORENE-like ID sets, as it has been shown by Kiuchi et al. [29]. Note that in these cases, the Hamiltonian and momentum constraint





FIG. 8 (color online). Rest mass density for the LORENE80 (top) and the BNS80n (bottom) simulations.

equations have to be solved again after the modification is applied.

The coordinate systems used in the LORENE and BNS ID sets are essentially different since they depend on the choice of lapse and shift; while  $\alpha$  and  $\beta^i$  are freely



FIG. 9 (color online). Trajectory of one NS for the runs of Fig. 8.

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FIG. 10 (color online). Half of the coordinate separation between NS centers for equal-mass nonspinning binaries. The runs correspond to initial coordinate separations of 60 and 80 km.

specifiable when using superposition, they are obtained by numerically solving coupled elliptic equations in the LORENE ID sets. In order to confirm that the eccentricity reduction is not a coordinate effect, we computed the gravitational waves resulting from the binary evolution at an extraction coordinate radius of  $200M_{\odot}$ . Figure 12 shows the corresponding GW where, for clarity, the signals were shifted in time to make the maxima in amplitude coincide. The eccentricity reduction is appreciated in the amplitude inset in the bottom panel of the figure. Additionally, our ID sets seem to possess less "junk" radiation. Whether this effect persists in the case of BNS with generic spins will be studied in future work.

To further assess the quality of the BNS simulations, we plotted the maximum rest mass density as a function of



FIG. 12 (color online). Gravitational wave amplitude (bottom) and real part (top) of the (2, 2) mode of  $\Psi_4$  for the runs of Fig. 8. Signals were shifted to coincide at the amplitude maximum (top and bottom) and at the junk radiation (lower left inset).

time (Fig. 13). Our ID runs show oscillations with larger amplitudes than those of LORENE during the first orbits, a behavior already discussed in Fig. 1. However, the amplitude diminishes with time, and, after a couple of orbits, all the runs show comparable oscillations. The most important question for the assessment of the quality of our ID sets is, however, how large the violations of the constraints are. Figure 14 presents a qualitative view of the Hamiltonian constraint violation through snapshots that compare LORENE80 vs BNS80n. A quantitative comparison is given by the  $L_2$  norm of the Hamiltonian and the y component of the momentum constraint violations as a function of time (Fig. 15). As expected, at t = 0 the constraint violations in the BNS runs are larger than those of the LORENE counterparts. However, after a couple of orbits,



FIG. 11 (color online). Eccentricity estimation for the runs of Fig. 10. The eccentricity was calculated using formula (1) from Ref. [70].



FIG. 13 (color online). Maximum rest mass density normalized to the initial values for the runs of Fig. 10.

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FIG. 14 (color online). Absolute value of the Hamiltonian constraint violation for the Lorene80 (top) and the BNS80n (bottom) simulations. The time of the snapshots match those of Fig. 8. The color logarithmic ruler is shown at the bottom.



FIG. 15 (color online). The  $L_2$  norm of the Hamiltonian (top) and the y component of the momentum (bottom) constraint violations for the runs of Fig. 10.



FIG. 16 (color online). Comparison of BNS ID evolutions starting at different coordinate separations. These runs are described in the second block of Table I.

the difference diminishes, and the scale of the violations for all the runs become comparable. Other quantitative indicators such as the  $L_1$  and  $L_{\infty}$  norms show similar behavior. This damping is attributable to the well-known constraint violation propagation properties of the BSSNOK formulation and seems to indicate that this violation reduction could possibly be hastened with the use of formulations with superior constraint damping characteristics such as CCZ4 [71,72] and Z4c [73] (Kastaun *et al.* [36] and Alic *et al.* [46] show CCZ4 simulations where the constraint violations fall well below BSSNOK levels after only 1 ms).

Finally, we added to this section a series of evolutions of BNS ID sets corresponding to nonspinning NS starting at separation distances between 50 and 80 km. Figures 16 and 17 show the coordinate separation and eccentricity as a function of time. Details of these runs are provided in the



FIG. 17 (color online). Eccentricity estimation for the runs of Fig. 16.

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second block of Table I. The evolution of the run starting at a coordinate separation of 50 km is too short to provide a meaningful measure of the eccentricity. Note that, against expectations, the absolute value of the boost velocity radial component seems to increase with the separation. We attribute this to the dominance of grid structure effects, in particular resolution, for the setups employed here.

# 2. Varying grid resolution

A complete study of how these quality control markers depend on the grid resolution is important and, due to the corresponding large computational cost, outside the scope of this work. However, to gain insights on the behavior of simulations based on our data at resolutions similar to those of the current state-of-the-art simulations, we have performed a set of runs corresponding to equal mass nonspinning binaries that start at a separation of 60 km. These runs are listed in the third block of Table I, where the "lr," "mr," and "hr" suffixes indicate low ( $\Delta x = 0.50M_{\odot}$ ), medium ( $\Delta x = 0.25M_{\odot}$ ), and high ( $\Delta x = 0.1875M_{\odot}$ ) maximum spatial resolution. The grid structure is similar in these cases with the addition of an extra level of refinement at the center of the medium- and high-resolution runs.

There is an additional difference between the runs in this section and the previous ones: these ID sets are based on the alternative scheme of Eq. (8) instead of that of Eq. (7). The advantage of using Eq. (8) over Eq. (7) can be better appreciated in the medium-resolution runs displayed in Fig. 18. There we see that the oscillations of the central density observed when using n = 4 (n = 5) in Eq. (7) are similar to those obtained when using f = 2.0 (f = 2.2) in Eq. (8). A value of f = 2.1 provides intermediate amplitude variations of the order of 1% and is the value



FIG. 18 (color online). Comparison between the overcontraction method of Eq. (7), represented by the curves with the parameter n, and that of Eq. (8), represented by the curves with the parameter f. All the BNS simulations were performed with the same parameters used for BNS60n\_mr, with the obvious exception of the values of n and f.



FIG. 19 (color online). Half of the coordinate separation between NS centers for equal-mass nonspinning binaries. The runs correspond to binaries with initial separation of 60 km and compare low-, medium-, and high-resolution results.

selected for the BNS60n\_lr, BNS60n\_mr, and BNS60n\_hr runs.

Figures 19 and 20 show the evolution of the coordinate separation and eccentricity for the runs described in the third block of Table I. These six simulations were run using gauge ( $\alpha_d$ ,  $\beta_d$ ) and dissipation ( $\epsilon_{diss}$ ) parameters that resemble more closely those employed in the most current binary modeling performed with ET. One clear effect of this set of parameters is the reduction of eccentricity in the LORENE60 runs. Our choice for the boost velocity used for the corresponding BNS60n runs manages to reduce the orbital eccentricity even further, but this reduction is not as large as the one presented in the previous section. It can be seen, however, that increasing the spatial resolution diminishes the orbital eccentricity for both types of ID. In the BNS60n ID cases, smaller eccentricities could potentially



FIG. 20 (color online). Eccentricity estimation for the runs of Fig. 19.



FIG. 21 (color online). Maximum rest mass density normalized to the initial values for the runs of Fig. 19.

be achieved by further fine-tuning of the boost velocity. Again we relied on comparisons of the evolution of the maximum rest mass density (Fig. 21) and the constraints violations (Fig. 22) to assess the behavior of our ID sets under time evolutions. The results are qualitatively similar to those of the previous section. The main difference is that the time needed for the Hamiltonian constraint violations of the BNS60n runs to relax to the level of the corresponding LORENE60 cases increases with decreasing resolution. This is to be expected; the use of higher grid resolution diminishes the initial constraint violation of the LORENE60 ID sets (which are, after all, numerical solutions of the constraints) while leaving mostly intact that of the BNS60n cases (only an approximation). As mentioned above, the use of formulations such as CCZ4 and Z4c has been shown to reduce this relaxation time to the point where this difference may be moot for simulations at the resolution used in the current state-of-the-art runs [36,46]. Finally, Fig. 23 shows that the evolution of



FIG. 22 (color online). The  $L_2$  norm of the Hamiltonian constraint violation for the runs of Fig. 19.



FIG. 23 (color online). Study of the convergence of the maximum rest mass density with resolution for the runs of Fig. 19. The factor multiplying the dashed curves corresponds to that of second-order convergence.

the maximum rest mass density is consistent with a secondorder convergence in resolution; while the spatial stencils used here are fourth order, hydrodynamics of compact objects usually present a degree of degradation due to stellar surface effects.

#### **B.** Spinning binaries evolution

The most salient characteristic of our method for constructing BNS ID sets is the ability to handle spinning stars. To show this, we produced two ID sets with NS with spins aligned (BNS80u) and antialigned (BNS80d) with the orbital angular momentum and evolved them from a starting coordinate separation of 80 km through their mergers. Both sets have identical NS with rest masses  $M_0 = 1.625M_{\odot}$  and dimensionless spin parameters  $a = J/M^2 \simeq 0.33$ , as detailed in last block of Table I.

Figure 24 shows the trajectories of one NS for the evolution of each set; these curves complement the nonspinning BNS (BNS80n) trajectory given in Fig. 9.



FIG. 24. Trajectory of one NS for the evolution of binary sets with spins aligned (BNS80u, left) and antialigned (BNS80d, right) with the orbital angular momentum that start at a coordinate separation of 80 km.



FIG. 25 (color online). Maximum rest mass density normalized to the initial value for simulations of binaries with spins aligned (BNS80u), zero (BNS80n) and antialigned (BNS80d) with the orbital angular momentum.



FIG. 26 (color online). Coordinate separation for the runs of Fig. 25.

One interesting feature is the presence of the orbital "hangup" [47]. This effect predicts that systems with spins aligned with the orbital angular momentum orbit longer than those with antialigned spins, allowing the shedding of excess of the angular momentum through the emission of gravitational radiation. While the antialigned binary merged and immediately collapsed to a black hole, the aligned case led to the formation of a centrifugally supported hypermassive neutron star that survived for about 20 ms before collapsing.

Figures 25 and 26 show the maximum rest mass density and the coordinate separation vs time for the three BNS80 runs. We have made an effort to find the velocities that would minimize the eccentricity but halted the fine-tuning after reaching what we deemed a reasonable precision



FIG. 27 (color online). Orbital eccentricity for the runs of Fig. 25.



FIG. 28 (color online). Gravitational wave amplitude (bottom) and real part (top) of the (2, 2) mode of  $\Psi_4$  for the runs of Fig. 25.

considering the low resolution of these simulations. More accurate evolutions with even lower eccentricities are likely to result in merger times that are quantitatively different than the values seen here. Figure 27 presents the orbital eccentricities of the three BNS80 runs and compares them with that of the LORENE80 simulation. The eccentricities achieved during the last orbits of the three BNS80 cases are lower than that of the reference LORENE80 simulation. Finally, Fig. 28 presents the GWs corresponding to these three runs.

#### **V. CONCLUSIONS**

We introduced a new way of constructing initial data for binary neutron stars with arbitrary spins and orbital eccentricities. The method only offers approximations to the Einstein field equations since, by design, the data sets do not satisfy the Hamiltonian and momentum constraints. However, by evolving our initial data using the BSSNOK formulation, we showed that these constraint violations become comparable to those seen in evolutions of standard (i.e., irrotational, conformally flat, helically symmetric, and constraint solving) initial data sets after relaxation times that increase with increasing grid resolution. Our method consists of a variant of metric superposition that addresses two common problems: large stellar shape oscillations and orbital eccentricities. It reduces the former to variations of the order of 1% and offers great control over orbital eccentricities. Additionally, we see indications that our initial data sets possess less junk radiation than that found in standard sets.

We tested our initial data by evolving in time initial data for single and binary neutron star systems. We showed that our data leads to inspirals with orbital eccentricities smaller than those seen in standard initial data simulations. However, since the method's most important characteristic is the ability to handle spinning binaries, we also evolved binaries with spins aligned and antialigned with the orbital angular momentum. The antialigned binary merges and immediately collapses into a black hole, while the aligned case leads to the formation of a centrifugally supported hypermassive neutron star that survives for several dynamical times before collapsing.

The work presented here will be followed by studies that are outside of the scope of this article due to computational demands. We plan to explore the viability of our method for binaries with generic spins and explore possible improvements aimed at reducing the constraint violations and orbital eccentricity even further. We will study more efficient ways of selecting the stars' boost velocity since the direct trial-and-error approach employed here is time and resource consuming. We will conduct a more systematical study of the content of junk radiation in our sets, to find out if the reduction in this unwanted quantity is a common feature in binaries with arbitrary spins. Another priority is the evolution of our ID sets using numerical formulations such as CCZ4 and Z4c, since they possess better constraint damping characteristics than BSSNOK. Finally, more realistic simulations (different equations of state, horizon detection and tracking, and ringdown modeling) with arbitrarily spinning stars (which would require grids without symmetries) will be pursued.

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