

Coupling-mass mapping of dijet peak searches

Bogdan A. Dobrescu* and Felix Yu†

Theoretical Physics Department, Fermilab, Batavia, Illinois 60510, USA

(Received 18 June 2013; published 26 August 2013)

We study hypothetical gauge bosons that may produce dijet resonances at the LHC. Simple renormalizable models include leptophobic Z' bosons or colorons that have flavor-independent couplings and decay into a color-singlet or -octet quark-antiquark pair, respectively. We present the experimental results on dijet resonances at hadron colliders as limits in the coupling-versus-mass plane of a gauge boson associated with baryon number. This theoretical framework facilitates a direct comparison of dijet resonance searches performed at different center-of-mass energies or at different colliders.

DOI: [10.1103/PhysRevD.88.035021](https://doi.org/10.1103/PhysRevD.88.035021)

PACS numbers: 12.60.-i, 13.85.Rm, 14.70.Pw

I. INTRODUCTION

If a new particle is produced in the s channel at hadron colliders, then it can decay into a pair of hadronic jets (“dijet”). The invariant mass distribution of the dijet exhibits a peak at (or slightly below) the mass of the new particle [1,2]. In many models, particles produced in the s channel can decay into leptons or other final states with low backgrounds. If the branching fractions of those final states are small enough, however, the dijet resonance searches may provide the simplest way of discovering the new particles.

Searches for narrow dijet resonances at hadron colliders have been performed over the last three decades by the UA2 [3,4] and UA1 [5] experiments at the SPS collider, the CDF [6–10] and D0 [11] experiments at the Tevatron, and the ATLAS [12–19] and CMS [20–25] experiments at the LHC. The results are traditionally presented as limits on an effective rate (defined as cross section times branching fraction times acceptance) to produce a resonance as a function of its mass. While this procedure has the advantage of being rather model independent, it complicates the comparison of experimental results with theoretical models.

The acceptance, in particular, requires the computation of the probability for the two jets to be observed in a certain geometric region of the detector. This can be done analytically given the differential cross section of the signal and the kinematic cuts, as long as effects arising from showering, from an assumed Gaussian signal (in the case of ATLAS [16]), or from a mismatch between partons and analysis-level wide jets are negligible. Otherwise, it is necessary to perform a simulation based on the jet selection criteria used by the experimental analyses.

The effective rate procedure also precludes a comparison of the limits set in $p\bar{p}$ collisions (at the SPS and the Tevatron) with those from pp collisions (at the LHC). Even for a particular collider, it is hard to compare the limits set during runs of different energies because the cross section grows

with the center-of-mass energy (\sqrt{s}) for a fixed resonance mass. A naive hope is that limits set at the larger \sqrt{s} and with larger integrated luminosity would supersede previous limits. The situation is not so straightforward because the backgrounds also increase so that the trigger thresholds for a jet-only final state need to be increased. As a result, the sensitivity to lighter resonances can be better in the runs using lower luminosity or lower energy. For example, the ATLAS dijet limits from $\sqrt{s} = 7$ TeV start at a resonance mass that has increased with luminosity from 0.3 TeV [12] to 0.6 TeV [13] to 0.9 TeV [16] to 1 TeV [17], and those from $\sqrt{s} = 8$ TeV start at a mass 1.5 TeV [18,19].

In this article we explore a unified presentation of the dijet limits in a coupling-versus-mass plot. The mass and coupling refer to a certain hypothetical particle of a given spin and $SU(3)_c \times SU(2)_W \times U(1)_Y$ charges, which is produced in the s channel at hadron colliders and decays into a pair of jets. This is by no means a substitute for the effective rate plots, as it is more model dependent. The coupling-versus-mass plot, however, has the advantage of allowing simple comparisons of searches performed at different luminosities, experiments, \sqrt{s} or colliders. Furthermore, it provides a measure of how stringent the limits are, given some natural ranges for the physical parameters.

Specifically, we consider an electrically neutral spin-1 particle that couples in a flavor-universal way to the standard model (SM) quark-antiquark pairs and is leptophobic, i.e., its tree-level couplings to SM leptons vanish. This is well motivated by the following arguments. In many theories beyond the SM, there are particles that can be produced from a quark-antiquark initial state and lead to a dijet resonance with large rates. By contrast, both the gluon-gluon (as in the case of the Higgs boson) and quark-gluon initial states require a loop to produce an s -channel resonance, so that the signal is typically too small (at least in perturbative theories) to compete with the dijet background. The quark-quark initial state could lead to an s -channel resonance if there is a diquark scalar, but in that case flavor-changing processes typically impose strong constraints on its mass and couplings (these are relaxed in the case of the color-sextet, hypercharge-4/3 diquark [26]).

*bdob@fnal.gov

†Corresponding author.
felixyu@fnal.gov

Electroweak symmetry suppresses the coupling of spin-0 particles to first generation $q\bar{q}$ pairs (an exception is the color-octet weak-doublet scalar [27], but in that case there are strong flavor constraints). Leptophobic spin-2 particles, although possible, require much more complicated UV completions.

Including a spin-1 particle coupled to first generation quarks is more straightforward. Large flavor effects are avoided if its quark couplings are generation independent. Moreover, the spin-1 particle should be associated with a spontaneously broken gauge symmetry (unless the particle is a bound state whose compositeness scale is near its mass), and the cancellation of various gauge anomalies is more easily achieved for equal couplings to up- and down-type quarks. Although some of the above arguments can be evaded (for example, with a more complicated fermion sector that is anomaly free), a flavor-universal gauge boson appears to be the simplest origin of a dijet peak. In order to couple to the SM quarks, the heavy gauge boson must be either a singlet or an octet under the $SU(3)_c$ color group.

In the case of the color singlet (a Z' boson), the dijet channel can be the discovery mode only if the Z' is nearly leptophobic (for an early model, see [28]) and its decays into Higgs states [29] or vectorlike leptons [30] are suppressed. We consider Z' bosons whose tree-level leptonic and Higgs couplings vanish, implying that the gauge charges are proportional to the baryon number. The corresponding $U(1)_B$ symmetry is anomalous in the SM, but we will show that it is anomaly free in the presence of a few vectorlike quarks (the simplest charge assignment has been discussed in [31]).

A color-octet gauge boson referred to as the coloron [32] is associated with an $SU(3)_1 \times SU(3)_2$ extension of QCD, and is automatically leptophobic. The coloron, in the case of flavor-universal couplings [33], can arise from a simple renormalizable extension of the SM [34]. Although its low-energy effects are usually negligible (in contrast to the case of flavor-dependent couplings [35]), the coloron can modify Higgs production via gluon fusion [36].

In Sec. II we present some simple renormalizable models that include a Z' boson coupled to baryon number (Z'_B) or a coloron (G'). In Sec. III we use the existing experimental limits on the effective rate to derive the limits in the coupling-mass plane for Z'_B , and also for G' . Section IV includes our conclusions.

II. MODELS OF DIJET RESONANCES

In this section we present some renormalizable models of spin-1 particles that are either color singlets (Z') or octets (coloron) and couple to quark-antiquark pairs.

A. Z' coupled to baryon number

Each coupling of a Z' boson to a quark or a lepton is in principle a free parameter. In practice, though, there are various theoretical and phenomenological constraints on

these couplings. Massive spin-1 particles, such as Z' bosons, must be either bound states or else be associated with a spontaneously broken gauge symmetry, the simplest case being a new $U(1)$ group. At hadron colliders, in order to discover a dijet resonance before a dilepton resonance, some of the Z' couplings to quarks must be more than an order of magnitude larger than all Z' couplings to leptons.

In the limit where the tree-level couplings to leptons vanish, the case of a leptophobic Z' , there are severe constraints from the requirement of anomaly cancellations. These form a set of linear, quadratic, and cubic equations in the $U(1)$ charges, which must have as a solution a set of commensurate numbers (i.e., a set of integers upon a rescaling of the gauge coupling). Despite the intricacies of cubic equations for integers, it can be proven that there is always a solution in the presence of a certain set of fermions which are vectorlike with respect to the SM gauge group and chiral under $U(1)$ [37]. To have a viable model, however, the number of new fermions cannot be too large, and their properties must avoid various phenomenological constraints.

Let us construct some viable models where the $U(1)_B$ symmetry associated with baryon number is gauged; i.e., all SM quarks have $U(1)_B$ charge $1/3$, while all SM leptons and bosons have charge 0. This choice is convenient because the SM mechanism for generating quark masses is not affected by the additional gauge symmetry, and furthermore the Z' couplings to quarks are flavor blind.

We construct a class of explicit models of this type that include n sets of vectorlike quarks (color triplets) transforming under $SU(2)_W$ as doublets, Q^k , or singlets, U^k, D^k ; here $k = 1, \dots, n$ labels their flavor. Although these new fermions do not introduce anomalies involving only SM gauge groups, the $U(1)_B$ charges of the vectorlike quarks are restricted by anomaly cancellation. The $[SU(2)_W]^2 U(1)_B$, $[SU(3)_c]^2 U(1)_B$, and $[U(1)_Y]^2 U(1)_B$ anomalies cancel only if

$$z_{U_L} - z_{U_R} = z_{D_L} - z_{D_R} = -z_{Q_L} + z_{Q_R} = \frac{1}{n}, \quad (1)$$

where z_{Q_R} is the $U(1)_B$ charge of Q_R , etc. The $U(1)_Y \times [U(1)_B]^2$ anomaly then cancels only if

$$z_{Q_L} = 2z_{U_R} - z_{D_R}. \quad (2)$$

It follows that there is no $U(1)_B$ gauge-gravitational anomaly, and finally, the $[U(1)_B]^3$ anomaly cancels only if

$$(z_{U_R} - z_{D_R})(7z_{U_R} - z_{D_R} + 3) = 0. \quad (3)$$

We will refer to the $z_{D_R} = z_{U_R}$ solution as the $D = U$ model, and to the $z_{D_R} = 7z_{U_R} + 3$ solution as the $D = 7U + 3$ model. Both these models are in fact families of $U(1)_B$ charges for the vectorlike quarks described by a rational parameter ($z_{U_R} \equiv z$) and an integer n (the number of vectorlike flavors).

TABLE I. Fields carrying $U(1)_B$ charge. With the exception of ϕ (a color-singlet scalar), all fields shown here are color-triplet fermions. The charge assignments labeled by $D = U$ and $D = 7U + 3$ correspond to the two solutions of the $[U(1)_B]^3$ anomaly cancellation condition. The SM quarks have a generation index, $j = 1, 2, 3$, and the vectorlike quarks have a flavor index $k = 1, \dots, n$.

Field	$SU(2)_W$	$U(1)_Y$	$U(1)_B$	
			$D = U$ model	$D = 7U + 3$ model
u_R^j	1	+2/3		+1/3
d_R^j	1	-1/3		+1/3
q_L^j	2	+1/6		+1/3
U_L^k	1	+2/3		$z + 1/n$
U_R^k				z
D_L^k	1	-1/3	$z + 1/n$	$7z + 3 + 1/n$
D_R^k			z	$7z + 3$
Q_L^k	2	+1/6	z	$-5z - 3$
Q_R^k			$z + 1/n$	$-5z - 3 + 1/n$
ϕ	1	0		+1/n

There is need for at least one scalar field, ϕ , to carry $U(1)_B$ charge and to have a vacuum expectation value (VEV). The ‘‘vectorlike’’ quarks are chiral with respect to $U(1)_B$, so that they can acquire mass only by coupling to the VEVs that break $U(1)_B$. In renormalizable models with only one ϕ scalar, Eq. (1), then requires that the charge of ϕ is $+1/n$ (charge $-1/n$ is the same modulo the interchange of ϕ and ϕ^\dagger) so that operators of the type $\bar{Q}_L Q_R \phi^\dagger$ are gauge invariant. The fields charged under $U(1)_B$ are listed in Table I.

If the vectorlike quarks are stable, then they form QCD bound states. The lightest of these is a heavy-light meson involving a vectorlike quark and a u or d quark. If this heavy-light meson is electrically neutral, then it can be a component of dark matter. The heavy-light meson, however, interacts with nucleons (e.g., via meson exchange) and also has a magnetic dipole moment, so that there are stringent limits on the mass of the vectorlike quark from direct searches for dark matter.

A simpler alternative is that all vectorlike quarks decay into SM particles. For that to happen, the charge z must take certain values, or else there must be additional scalars with VEVs carrying $U(1)_B$ charge.

In the simplest case, the $D = U$ model with $n = 1$ [31], we find that $z = 1/3$ would allow decays into a SM quark and h^0 (the SM Higgs boson) through the Yukawa interactions

$$\bar{q}_L U_R H, \quad \bar{q}_L D_R H^\dagger, \quad \bar{u}_R Q_L H^\dagger, \quad \bar{d}_R Q_L H, \quad (4)$$

where H is the SM Higgs doublet. In addition, decays into a SM quark and ϕ may proceed through the following Yukawa terms:

$$\bar{q}_L Q_R \phi^\dagger, \quad \bar{u}_R U_L \phi^\dagger, \quad \bar{d}_R D_L \phi^\dagger. \quad (5)$$

Even when the two particles described by the complex scalar ϕ are heavier than the vectorlike quarks, the above Yukawa terms in conjunction with the Higgs portal coupling $H^\dagger H \phi^\dagger \phi$ induce Q , U , and D decays of the type $Q \rightarrow q h^0 h^0$ (or $Q \rightarrow q b \bar{b} h^0$ for masses below $2M_h$). For $z = -5/3$, the vectorlike quarks decay through Yukawa couplings of the type $\bar{q}_L Q_R \phi$.

The $D = 7U + 3$ model with $n = 1$ has different decay patterns. For example, $z = -2/3$ implies that the decays $Q_R \rightarrow q_L \phi$ and $D_L \rightarrow d_R \phi^\dagger$ are allowed, but U can decay via renormalizable interactions only if there is at least one additional field [e.g., a scalar S which is a SM gauge singlet, has $U(1)_B$ charge 0, and interacts through $\bar{u}_R U_L S$].

The $D = U$ and $D = 7U + 3$ models are identical for $z = -1/2$. In the $n = 1$ case, a second scalar ϕ' of $U(1)_B$ charge $-1/6$ is necessary to allow Q , U , and D decays through $\bar{q}_L Q_R \phi'$, $\bar{u}_R U_L \phi'$, and $\bar{d}_R D_L \phi'$, respectively. In the $n = 2$ case, there is no need for ϕ' or other fields because Q_R , U_L , and D_L have $U(1)_B$ charge 0, allowing the mass mixing terms $\bar{q}_L Q_R$, $\bar{u}_R U_L$, and $\bar{d}_R D_L$.

The choice of vectorlike fermions shown in Table I is simple but not unique. For example, anomaly cancellation in the presence of vectorlike leptons instead of quarks is also possible [38]. A fourth generation of chiral quarks and leptons can also lead to the cancellation of the $U(1)_B$ anomalies [39], but this possibility is nearly ruled out [36] now by the measurements of Higgs production through gluon fusion [40] and by direct searches for t' [41] and b' [42] quarks at the LHC.

The couplings of the Z'_B to SM quarks are given by

$$\frac{g_B}{6} Z'_{B\mu} \bar{q} \gamma^\mu q, \quad (6)$$

where g_B is the $U(1)_B$ gauge coupling (using the normalization where the group generator is $1/2$), and is related to the coupling constant, as usual, by $\alpha_B = g_B^2/(4\pi)$. The Z'_B can decay into a pair of jets (including b jets) or into a $t\bar{t}$ pair (for a Z'_B mass $M_{Z'_B} > 2m_t$), with partial decay widths given by

$$\Gamma(Z'_B \rightarrow jj) = \frac{5\alpha_B}{36} M_{Z'_B} \left(1 + \frac{\alpha_s}{\pi}\right), \quad (7)$$

$$\frac{\Gamma(Z'_B \rightarrow t\bar{t})}{\Gamma(Z'_B \rightarrow jj)} = \frac{1}{5} \left[1 - \frac{4m_t^2}{(M_{Z'_B})^2}\right]^{1/2} \left[1 + O\left(\frac{\alpha_s m_t}{M_{Z'_B}}\right)\right].$$

Here we have included the next-to-leading order (NLO) QCD corrections and no electroweak corrections. If the decays into vectorlike quarks are kinematically closed, then the total width of Z'_B is

$$\Gamma_{Z'_B} = \Gamma(Z'_B \rightarrow jj) + \Gamma(Z'_B \rightarrow t\bar{t}). \quad (8)$$

B. Coloron

Another hypothetical particle that can easily produce dijet resonances with large cross section at the LHC is the coloron [32], a spin-1 color-octet gauge boson. The coloron, in the case of flavor-universal couplings [33], is not significantly constrained by flavor processes nor by other low-energy data. Furthermore, the coloron is automatically leptophobic.

The simplest gauge symmetry that can be associated with a heavy color-octet vector boson is $SU(3)_1 \times SU(3)_2$ [43]. This is spontaneously broken down to the diagonal $SU(3)_c$ gauge group, which is identified with the QCD one. A minimal renormalizable extension of the SM which includes a coloron dubbed ReCoM is analyzed in Ref. [34]. Assuming that all the SM quarks transform as (3,1) under $SU(3)_1 \times SU(3)_2$, the couplings of the coloron to SM quarks are given by the Lagrangian term

$$g_s \tan \theta \bar{q} \gamma^\mu T^a G'_\mu q, \quad (9)$$

where $g_s = \sqrt{4\pi\alpha_s}$ is the QCD gauge coupling and $\tan \theta > 0$ is a dimensionless parameter.

If there are no new quarks mixing with the SM ones, and no additional color-octet spin-1 particles, then $\tan \theta$ is the ratio of the $SU(3)_2$ and $SU(3)_1$ gauge couplings. These gauge couplings can vary between g_s and some upper limit of about $4\pi/\sqrt{3}$ corresponding to the nonperturbative regime. Consequently, there are both upper and lower limits on $\tan \theta$ [44]: $0.15 \lesssim \tan \theta \lesssim 6.7$. Unlike the Z'_B , whose UV behavior requires some new fermions, the flavor-universal coloron is anomaly free. Nevertheless, vectorlike quarks may be present, and if they mix with the SM quarks, then the lower limit on $\tan \theta$ no longer applies [45]. Similarly, a second heavy spin-1 color-octet particle can mix with the coloron and dilute its couplings to quarks.

The partial decay widths of the coloron of mass $M_{G'}$ into jj (including $b\bar{b}$) and into $t\bar{t}$ are given by

$$\begin{aligned} \Gamma(G' \rightarrow jj) &= \frac{5\alpha_s}{6} \tan^2 \theta M_{G'} \left[1 + O\left(\frac{\alpha_s}{\pi}\right) \right], \\ \frac{\Gamma(G' \rightarrow t\bar{t})}{\Gamma(G' \rightarrow jj)} &= \frac{1}{5} \left[1 - \frac{4m_t^2}{(M_{G'})^2} \right]^{1/2} \left[1 + O\left(\frac{\alpha_s m_t}{M_{G'}}\right) \right], \end{aligned} \quad (10)$$

where only NLO QCD corrections are included.

The minimal scalar sector responsible for breaking the $SU(3)_1 \times SU(3)_2$ symmetry (which is part of ReCoM) includes a color octet and two color singlets. If these are light enough, then the coloron can decay into two octet scalars or into an octet scalar and a singlet scalar, with partial decay widths that are especially large for $\tan \theta \ll 1$ [34]. In what follows, we will assume that the scalars are heavier than $M_{G'}/2$, so that the total width of the coloron is simply the sum of the jj and $t\bar{t}$ partial widths shown in Eq. (10).

III. COLLIDER SEARCHES OF DIJET RESONANCES

We now detail our procedure and results for mapping the existing dijet resonance searches to the coupling-mass plane.

A. Mapping procedure and experimental limits

As discussed in Sec. I, the partons responsible for s -channel production at hadron colliders are also a decay mode, and so the new particle must decay back to pairs of jets at some rate. Models that give rise to a spin-1 dijet resonance are the most straightforward to construct. For the representative spin-1 particles discussed in Sec. II, the Z'_B boson and the coloron, there are two parameters that characterize the dijet signal: mass and coupling.

Even with only two parameters, the extraction of limits from experimental searches for dijet resonances remains challenging. For example, varying the resonance mass while keeping the coupling fixed introduces varying levels of final state radiation, cut-dependent effects from parton distribution function (PDF) sampling at high masses relative to the total \sqrt{s} (the mass dependence of PDFs is shown in [46]), and trigger-dependent efficiencies at low masses.

Dijet resonance searches probe the existence of narrow peaks in the dijet invariant mass (m_{jj}) spectrum. The QCD background is expected to be a smoothly falling exponential. Other backgrounds, such as hadronic $t\bar{t}$ decays, are expected to give broad features at their respective mass scales.

Although a bumplike feature on top of a smoothly falling background is seemingly easy to observe, the experimental resolution in the dijet channel is rather poor ($\sim 5\%$ – 10% depending on mass [2] as well as experiment), and the QCD background at energies much smaller than the total \sqrt{s} become overwhelming. Higher \sqrt{s} colliders rapidly lose sensitivity to low mass resonances in dijet searches because of the minimum p_T , E_T , and m_{jj} trigger requirements. Prescaled triggers (and so-called “data-parking” techniques [23]), however, can help augment the trigger bandwidth to extend the searches down to lower masses.

For our mapping, we start by running a Monte Carlo (MC) simulation for a given choice of coupling and mass. In the narrow width approximation, the s -channel production factorizes from the decay, hence the acceptance and efficiency do not depend on the coupling at leading order. Some dependence on the coupling arises from loops involving the new spin-1 particle, as shown in the case of NLO coloron production [47]; however, this effect is relatively small, and for simplicity we ignore it in what follows. For a given set of experimental cuts we obtain a simulated effective rate. The ratio of the experimental limit to the simulated effective rate is the square of a coupling rescaling factor. Multiplying the initial coupling by this

TABLE II. Mass ranges for existing dijet resonance searches at hadron colliders.

Collisions, \sqrt{s} (TeV)	Experiment	References	Luminosity (fb^{-1})	Mass range (TeV)
$p\bar{p}$, 0.63	UA2	[3]	4.7×10^{-3}	0.08–0.32
		[4]	1.1×10^{-2}	0.14–0.3
	UA1	[5]	4.9×10^{-4}	0.15–0.4
$p\bar{p}$, 1.8	CDF	[6]	2.6×10^{-6}	0.06–0.5
		[7]	4.2×10^{-3}	0.2–0.9
		[8]	1.9×10^{-2}	0.2–1.15
		[9]	0.11	0.2–1.15
	D0	[11]	0.11	0.2–0.9
$p\bar{p}$, 1.96	CDF	[10]	1.1	0.26–1.4
pp , 7	ATLAS	[12]	3.2×10^{-4}	0.3–1.7
		[13]	3.6×10^{-2}	0.6–4
		[14]	0.16	0.9–4
		[15]	0.81	0.9–4
		[16]	1.0	0.9–4
		[17]	4.8	1–4
	CMS	[20]	2.9×10^{-3}	0.5–2.6
		[21]	1.0	1–4.1
		[22]	5.0	1–4.3
		[23]	0.13	0.6–1
pp , 8	ATLAS	[18]	5.8	1.5–4
		[19]	13	1.5–4.8
	CMS	[24]	4.0	1–4.8
		[25]	20	1.2–5.3

rescaling factor gives the experimental upper limit on the coupling for the chosen mass. Repeating this procedure for all experimental searches, we determine the excluded region in the coupling-mass plane.

There has been a host of resonance searches from every experiment at hadron colliders in the dijet channel. We summarize all of them in Table II.

For each mass point and collider, we simulate an event sample of on-shell s -channel Z'_B as well as coloron production (at leading order) with subsequent decay to light-flavor and b jets using MadGraph 5 v1.5.7 [48] with the CTEQ6L1 PDFs [49]. Each event is passed through PYTHIA v6.4.20 [50] for showering and hadronization, and then through PGS v4 [51] for basic detector simulation and jet clustering.

Choosing $g_B = 0.2$ for the Z'_B or $\tan \theta = 0.2$ for the coloron, we obtain the cross section times branching fraction from MadGraph 5, denoted $\sigma_{0.2} \cdot B$, as a function of mass for each collider. We then implement the various triggers and cuts as described in each analysis listed in Table II to obtain an acceptance A . The ratio of the resulting simulated effective rate, $\sigma_{0.2} \cdot B \cdot A$, to the limit from each relevant analysis in Table II allows us to extract the upper limit on the coupling as a function of mass:

$$(g_B)_{\max} = 0.2 \left(\frac{(\sigma \cdot B \cdot A)_{\text{limit}}}{\sigma_{0.2} \cdot B \cdot A} \right)^{1/2}, \quad (11)$$

and similarly for $(\tan \theta)_{\max}$.

We now discuss the most relevant searches grouped according to the mass range probed.

I. Searches for $m_{jj} < 200$ GeV

Although a couple of searches (from UA2 and CDF, see Table II) extend to masses below 140 GeV, we do not use them because those results were based on a subtraction of the expected W and Z dijet distribution calculated at $O(\alpha_s)$; modern precision of W and Z two-dijet distributions far exceeds the interpretative power of the effective rate limit in the 60–140 GeV mass window. For studies of theoretical constraints on colorons in that mass range, see Ref. [52].

In the 140–200 GeV mass range, by far the largest data sample (10.9 pb^{-1}) has been analyzed [4] by the UA2 experiment at the CERN SPS collider, which operated mainly at $\sqrt{s} = 630$ GeV. Mapping the UA2 limit to the coupling-mass plane is simpler than the procedure required for later analyses because the UA2 analysis includes a table of efficiencies for selecting the signal events from

background as well as for isolating the peak feature in the signal events (cf. Tables 1 and 2 of Ref. [4]). We linearly interpolate this overall efficiency to obtain a combined acceptance times efficiency factor. Finally, since the UA2 constraint is presented as a branching fraction limit on a sequential SM Z' , we unfold the Z' cross section to obtain an estimated $\sigma \cdot B$ limit, as discussed in Ref. [53]. After applying the overall efficiency, we obtain an effective rate limit from UA2, which we then map into the upper limit on the Z'_B coupling shown on the left-hand side of Fig. 1.

2. Searches in the 200–900 GeV mass range

The CDF [9] and D0 [11] searches using the full data samples ($\approx 110 \text{ pb}^{-1}$) of the Run I at the Tevatron compete for the best limit in the 200–260 GeV mass window. We choose to extract a limit from the CDF analysis because it applies to a larger mass range.

Above 260 GeV, the CDF analysis using 1.1 fb^{-1} of Run II data [10] supersedes the Run I results. For the 260–900 GeV window, the only ATLAS [12,13] and CMS [20,23] searches use very small $\sqrt{s} = 7 \text{ TeV}$ data sets. The most competitive of these is the 0.13 fb^{-1} CMS [23] analysis of the so-called “parked data” obtained via a special low-threshold trigger which retains sensitivity at low masses even during high instantaneous luminosity conditions. We implement the appropriate trigger and analysis requirements for each mass point probed by these CDF and CMS analyses to calculate their respective acceptances needed for the coupling-mass mapping. For all CMS limits, we adopt their qq resonance constraint, since our spin-1 resonances only couple (at leading order) to $q\bar{q}$ (note that the radiation patterns from qq and $q\bar{q}$ final states are indistinguishable). As can be seen from Fig. 1, the CDF limits on spin-1 resonances are the most stringent ones, even though they are based on only a tenth of the Run II data.

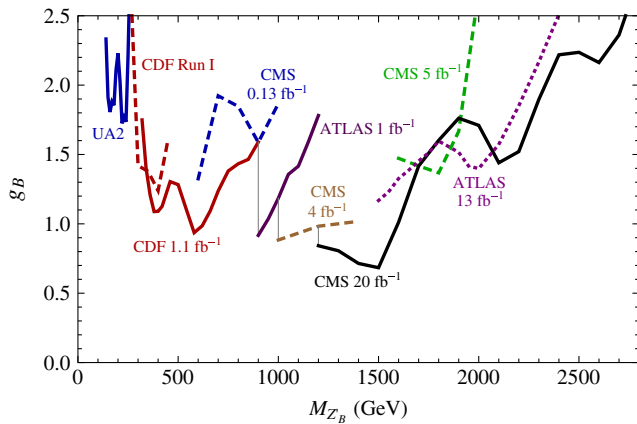


FIG. 1 (color online). Leading experimental limits in the coupling g_B versus mass $M_{Z'_B}$ plane for Z'_B resonances. Values of g_B above each line are excluded at the 95% C.L.

3. Searches for resonance masses above 900 GeV

Most ATLAS and CMS searches begin at about 900 GeV. For the 900–1000 GeV range, the ATLAS 1 fb^{-1} search [16] is expected to be the most sensitive, as it has higher energy than CDF 1.1 fb^{-1} [10], and a larger data sample than the other ATLAS [12–15] and CMS studies [20,23].

From 1–1.2 TeV, the CMS 4.0 fb^{-1} search using 8 TeV data [24] is expected to be competitive with the earlier 7 TeV ATLAS 4.8 fb^{-1} [17] and CMS 5.0 fb^{-1} analyses [22], superseding the ATLAS and CMS 1 fb^{-1} analyses [16,21]. The slightly smaller amount of integrated luminosity analyzed in Ref. [24] compared to Refs. [17,22] is counterbalanced by the slight increase in collider energy, giving comparable coupling sensitivities.

Above 1.2 TeV, the CMS analysis [25] using 19.6 fb^{-1} of $\sqrt{s} = 8 \text{ TeV}$ data is expected to be the most sensitive (we will refer to this search as CMS 20 fb^{-1}). This analysis is the most recent dijet resonance search and has sensitivity to resonances as heavy as 5 TeV. Nevertheless, upward fluctuations in the CMS 20 fb^{-1} limit actually leave some small gaps where the ATLAS [19] 13.0 fb^{-1} limit and the CMS 5.0 fb^{-1} limits are more stringent (see Figs. 1 and 2).

For the various CMS analyses, we implement the respective trigger and analysis cuts to tabulate the acceptance for each mass point and obtain an effective rate limit from the qq resonance constraint. For the 8 TeV analyses we find that the acceptance grows from 38% to 50% for the Z'_B signal (and from 33% to 44% for the coloron) when the mass grows from 1 to 2.5 TeV and is constant at larger masses.

The ATLAS results, on the other hand, are presented as limits on Gaussian resonances in the m_{jj} spectrum after trigger requirements, detector effects, and analysis cuts are implemented. This poses additional problems because the m_{jj} distribution produced by any particle decaying to a pair

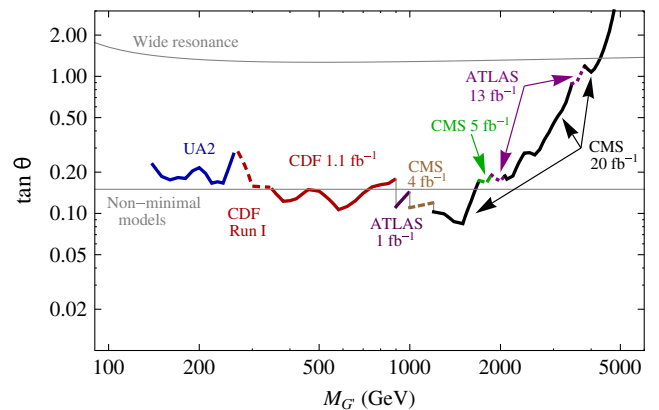


FIG. 2 (color online). Envelope of experimental limits for colorons of coupling $\tan \theta$ and mass M_G . Values of $\tan \theta$ above each limit are excluded at the 95% C.L. The region above the line labeled “Wide resonance” corresponds to a coloron width-to-mass ratio larger than 15%. The region below the line labeled “Nonminimal models” (at $\tan \theta = 0.15$) requires additional particles, such as vectorlike quarks or a second coloron.

of jets would be quite different from a Gaussian: a long tail at low invariant mass is induced by imperfect recapturing of final state radiation. To overcome this mismatch, we form the m_{jj} spectrum after cuts and then model and apply a Gaussian core efficiency (ϵ_G) for our signal, which is an additional factor beyond the canonical acceptance. Our procedure of determining ϵ_G is described in the Appendix.

The ATLAS limits are given for a variety of Gaussian widths: for each ATLAS limit, we adopt the smallest Gaussian width constraint in performing our mapping, since our resonances typically have intrinsic widths at the percent and subpercent level.

B. Results and discussion

Following the procedure described in Sec. III A for the leading experimental dijet limits, we obtain the coupling-mass mapping shown in Fig. 1 for a spin-1 resonance Z'_B . We use the leading order production computed with MadGraph 5.

If the NLO corrections to the process $pp \rightarrow Z'_B X \rightarrow jjX$ are included in an event generator, then the mapping can be performed more precisely. We do not expect that they would change the values of g_B by more than $O(10\%)$.

We emphasize that, unlike the usual $\sigma \cdot B \cdot A$ limit plots, Fig. 1 readily shows the exclusion in coupling as well as mass. This mapping also demonstrates the complicated interplay between different experimental analyses using different colliders and luminosities.

From Fig. 1, we conclude that Z'_B bosons are unconstrained for a gauge coupling $g_B \lesssim 0.6$, leaving a large area of parameter space unexplored by dijet resonance searches so far. Moreover, for the entire sub-TeV region, the experimental limits allow for g_B couplings as large as 0.9, while locally, g_B couplings can reach ≈ 1.5 . Importantly, an update from CDF or an analysis by D0 with their full $\approx 10 \text{ fb}^{-1}$ Run II data sets could offer evidence for or provide interesting limits on new sub-TeV dijet resonances. We also note that an update of the “parked data” analysis [23] with more luminosity by CMS (and ATLAS) would also push sensitivity to lower couplings in the several hundred GeV mass range.

The plot is not extended above $g_B = 2.5$ because the $U(1)_B$ coupling constant is already large, $\alpha_B = g_B^2/(4\pi) \approx 0.5$, so that it is difficult to avoid a Landau pole. For that large coupling, the current mass reach is around 2.8 TeV. The 14 TeV LHC will extend significantly the mass reach and can probe smaller couplings once enough data are analyzed. Note that couplings of $g_B \approx 0.1$ can be viewed as typical (the analogous coupling of the photon is approximately 0.3), and even g_B as small as 0.01 would not be very surprising.

We also present the coupling-mass mapping for colorons in Fig. 2. For clarity, we only show the envelope of the strongest $\tan\theta$ upper limits from all available analyses at each coloron mass. This mapping is performed again using leading order production. The NLO corrections to coloron

production have been computed recently [47] and can vary between roughly -30% and $+20\%$. We do not take the NLO corrections into account as we do not have an event generator that includes them; furthermore, there is some model dependence in the NLO corrections at small $\tan\theta$ (for example, they are sensitive to the color-octet scalar present in ReCoM [34]).

As mentioned in Sec. II B, in the minimal coloron model there is a theoretical lower limit imposed by perturbativity, $\tan\theta \gtrsim 0.15$. The experimental upper limit dips below that value only in the 350–700 GeV and 0.9–1.6 TeV mass ranges. In nonminimal models, where there are vectorlike quarks or a second coloron, $\tan\theta$ can be substantially smaller than 0.15. Thus, searches for colorons should continue even after they rule out $\tan\theta \gtrsim 0.15$ in some mass windows. On the contrary, the discovery of a coloron with $\tan\theta < 0.15$ would imply the existence of additional colored particles that can be probed in hadron collisions.

Unlike the $U(1)$ gauge bosons, the coloron can be rather strongly coupled before reaching the perturbative upper limit, $\tan\theta \lesssim 6.7$, because it is associated with a non-Abelian gauge interaction that is asymptotically free.

There is, however, a tighter upper limit on $\tan\theta$ if the total width $\Gamma(G' \rightarrow jj) + \Gamma(G' \rightarrow t\bar{t})$ [see Eq. (10)] is required to be smaller than the dijet resolution. A ratio of the total width to $M_{G'}$ of 15% (as used in [16]) corresponds to $\tan\theta \approx 1.3$ for $M_{G'} \gg 2m_t$ (with a mild dependence on $M_{G'}$ due to the running of α_s), and to slightly larger $\tan\theta$ for smaller masses, as shown in Fig. 2. Limits above the line marked there by “Wide resonance” are not reliable if set by narrow resonance searches [54]. Clearly, resonances that have a much broader intrinsic width than the experimental m_{jj} resolution will fade more easily into the exponentially falling QCD background. Separately, for large enough coupling, the t -channel exchange of a coloron starts contributing significantly to the dijet signal, further diluting the m_{jj} peak. Note also that at resonance masses approaching the total \sqrt{s} of the collider, PDF uncertainties increase.

IV. CONCLUSIONS

We urge the experimental collaborations to present limits (or contours if a signal is observed) on dijet resonances in the coupling-versus-mass plane of a “baryonic” Z'_B , as in Fig. 1 (or a coloron as in Fig. 2, if the search is sensitive primarily to large signals arising from heavy resonances). This coupling-mass mapping, while being somewhat model dependent (and thus a complement to—not a replacement for—the cross-section limit plots), has multiple advantages. First, it allows a comparison of limits set by experiments performed at different colliders and at different center-of-mass energies. Second, it allows an assessment of how stringent the experimental limits are by comparing them with the expected range of the physical coupling. Third, it provides a direct interpretation without

the need for MC simulations to compute the acceptance or to convert limits on a Gaussian into limits on a realistic particle (in the case of the existing ATLAS results).

The coupling-mass mapping also highlights gaps in the combined sensitivity of all existing searches. Figure 1 shows that the coupling reach is rather poor in the mass range of 700–900 GeV, and it is even worse for masses below about 300 GeV. A new analysis by CDF or D0 with the full Run II data set could have great impact there. Nonconventional methods, such as analyzing parked data [23], are also important for extending the sensitivity of LHC experiments in the sub-TeV mass range. More generally, the traditional trend for each new dijet search to attain ever higher mass reach does not need to leave the (equally important) small-coupling region unexplored.

We argue that the simplest origin of narrow dijet resonances is a spin-1 particle with flavor-independent couplings. Our mapping focuses on the Z'_B and G' . The same procedure can also be applied to other spins or color representations [1], but the results would be different because of PDF dependencies and radiation patterns of the decay products.

The overview of theoretical and experimental status of dijet resonances in this paper is not exhaustive. For example, we do not discuss angular correlations, which complement the information contained in the m_{jj} distribution. We also note that any particle that produces a dijet resonance can also be produced in association with a W , a Z , or a photon. Even though the cross sections for these associated productions are much smaller [34,55], the searches for $W + jj$, $Z + jj$, and $\gamma + jj$ benefit from better triggers that extend sensitivity to lower resonance masses compared to the pure dijet resonance searches.

The coupling-mass plane can and should be used for any resonance search (as it has been done in some cases, e.g., [8,9,56]). In particular, the $t\bar{t}$ resonance searches can be interpreted in terms of the same Z'_B or coloron. For these flavor-blind particles, it would also be interesting to investigate the complementarity between $t\bar{t}$ and dijet resonance searches.

If a dijet resonance will be discovered in the absence of a dilepton resonance at the same mass, it is likely that additional colored particles will remain to be discovered. To see this, recall (from Sec. II) that the Z'_B requires some vectorlike fermions to cancel the gauge anomalies, while the coloron requires at least some scalars from the gauge symmetry breaking sector.

ACKNOWLEDGMENTS

We would like to thank Sekhar Chivukula, Arsham Farzinnia, Robert Harris, Olivier Mattelaer, Elizabeth Simmons, and Ciaran Williams for useful communications. Fermilab is operated by the Fermi Research Alliance, LLC under Contract No. De-AC02-07CH11359 with the United States Department of Energy.

APPENDIX: FROM GAUSSIANS TO PARTICLES

As explained in Sec. III A, the effective rate in the case of ATLAS analyses is given by $\sigma \cdot B \cdot A \cdot \epsilon_G$, where ϵ_G is the efficiency of converting the limits on a realistic particle (whose m_{jj} distribution has a long tail due to final state radiation) into limits on a Gaussian. As noted in the Appendix of Ref. [16], the low- m_{jj} tail should be removed as it does not contribute to the assumed Gaussian signal. In this appendix we present a more precise procedure for estimating ϵ_G .

We fit the m_{jj} signal spectrum with a Crystal Ball function [57],

$$f(x; \alpha, n, \bar{x}, \sigma) = N \begin{cases} \exp\left(-\frac{(x-\bar{x})^2}{2\sigma^2}\right), & \text{for } \frac{x-\bar{x}}{\sigma} > -\alpha, \\ A\left(\frac{n}{|\alpha|} - |\alpha| - \frac{x-\bar{x}}{\sigma}\right)^{-n}, & \text{for } \frac{x-\bar{x}}{\sigma} \leq -\alpha, \end{cases} \quad (\text{A1})$$

which is a combination of a truncated Gaussian and a power-law tail; here

$$A = \left(\frac{n}{|\alpha|}\right)^n e^{-|\alpha|^2/2}, \quad (\text{A2})$$

and N is an overall normalization factor. The fit parameters α , n , \bar{x} , and σ correspond to the location of the power-law Gaussian crossover in units of σ , the power-law exponent, and the mean and width of the Gaussian, respectively. Performing this fit allows us to use the Gaussian fit parameters to calculate the Gaussian core efficiency.

We have checked that this fitting function accurately reproduces the expected signal shape for our on-shell s -channel resonance production in the m_{jj} spectrum, as shown in Fig. 3, which is in reasonable agreement with

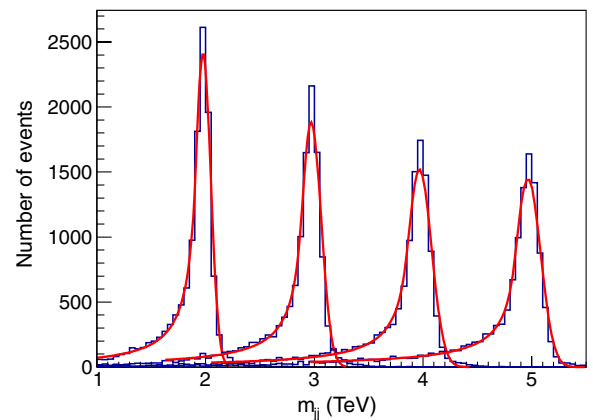


FIG. 3 (color online). Simulated m_{jj} distributions (blue histograms) and Crystal Ball fits (red curves) performed on 25 000 Z' signal events for $M_{Z'_B} = 2, 3, 4,$ and 5 TeV, after implementing the CMS 20 fb^{-1} search [25].

Fig. 2 of Ref. [25].¹ The fit parameters are varied within a large range of values: α floats within 0.05 to 3.5, n within 0.5 to 5.0, \bar{x} within (70–105)% of the truth boson mass, σ within (0.5–30)% of the truth boson mass, and the overall normalization N floats within (50–300)% of the $N_{\text{events}}^{\text{total}}$ in the histogram. Moreover, the beginning and end of the fit range is adjusted from (50–70)% and (110–115)% of the m_{jj} peak, respectively. The fit range with the smallest χ^2

¹Even though we only use the Gaussian fit procedure on ATLAS limits, we show the fit results from our implementation of the CMS 20 fb⁻¹ study to facilitate comparison with Fig. 2 of Ref. [25]. The corresponding m_{jj} spectrum and Crystal Ball fits for ATLAS analyses are qualitatively similar.

per number of degrees of freedom dictates the fit parameters \bar{x} and σ used in the estimation of the Gaussian core component of the m_{jj} shape.

From the fit parameters, we count the number of events in the m_{jj} distribution within $\bar{x} \pm 3\sigma$ to give the efficiency ϵ_G for extracting the Gaussian peak appropriate for the Gaussian template limits set by ATLAS,

$$\epsilon_G = \frac{N_{\text{events}}^{\bar{x} \pm 3\sigma}}{N_{\text{events}}^{\text{total}}}. \quad (\text{A3})$$

From our simulated ATLAS m_{jj} distributions, we get ϵ_G values for both the Z'_B and the coloron between 55% and 65%.

-
- [1] T. Han, I. Lewis, and Z. Liu, *J. High Energy Phys.* **12** (2010) 085.
 - [2] R. M. Harris and K. Kousouris, *Int. J. Mod. Phys. A* **26**, 5005 (2011).
 - [3] J. Alitti *et al.* (UA2 Collaboration), *Z. Phys. C* **49**, 17 (1991).
 - [4] J. Alitti *et al.* (UA2 Collaboration), *Nucl. Phys.* **B400**, 3 (1993).
 - [5] C. Albajar *et al.* (UA1 Collaboration), *Phys. Lett. B* **209**, 127 (1988).
 - [6] F. Abe *et al.* (CDF Collaboration), *Phys. Rev. D* **41**, 1722 (1990).
 - [7] F. Abe *et al.* (CDF Collaboration), *Phys. Rev. Lett.* **71**, 2542 (1993).
 - [8] F. Abe *et al.* (CDF Collaboration), *Phys. Rev. Lett.* **74**, 3538 (1995).
 - [9] F. Abe *et al.* (CDF Collaboration), *Phys. Rev. D* **55**, R5263 (1997).
 - [10] T. Aaltonen *et al.* (CDF Collaboration), *Phys. Rev. D* **79**, 112002 (2009).
 - [11] V. M. Abazov *et al.* (D0 Collaboration), *Phys. Rev. D* **69**, 111101 (2004).
 - [12] G. Aad *et al.* (ATLAS Collaboration), *Phys. Rev. Lett.* **105**, 161801 (2010).
 - [13] G. Aad *et al.* (ATLAS Collaboration), *New J. Phys.* **13**, 053044 (2011).
 - [14] ATLAS Collaboration, Report No. ATLAS-CONF-2011-081 (2011).
 - [15] ATLAS Collaboration, Report No. ATLAS-CONF-2011-095 (2011).
 - [16] G. Aad *et al.* (ATLAS Collaboration), *Phys. Lett. B* **708**, 37 (2012).
 - [17] G. Aad *et al.* (ATLAS Collaboration), *J. High Energy Phys.* **01** (2013) 029.
 - [18] ATLAS Collaboration, Report No. ATLAS-CONF-2012-088 (2012).
 - [19] ATLAS Collaboration, Report No. ATLAS-CONF-2012-148 (2012).
 - [20] V. Khachatryan *et al.* (CMS Collaboration), *Phys. Rev. Lett.* **105**, 211801 (2010).
 - [21] S. Chatrchyan *et al.* (CMS Collaboration), *Phys. Lett. B* **704**, 123 (2011).
 - [22] S. Chatrchyan *et al.* (CMS Collaboration), *J. High Energy Phys.* **01** (2013) 013.
 - [23] CMS Collaboration, Report No. CMS-PAS-EXO-11-094 (2012).
 - [24] S. Chatrchyan *et al.* (CMS Collaboration), [arXiv:1302.4794](https://arxiv.org/abs/1302.4794).
 - [25] CMS Collaboration, Report No. CMS-PAS-EXO-12-059 (2013).
 - [26] C. W. Bauer, Z. Ligeti, M. Schmaltz, J. Thaler, and D. G. E. Walker, *Phys. Lett. B* **690**, 280 (2010).
 - [27] A. V. Manohar and M. B. Wise, *Phys. Rev. D* **74**, 035009 (2006).
 - [28] K. S. Babu, C. F. Kolda, and J. March-Russell, *Phys. Rev. D* **54**, 4635 (1996).
 - [29] H. Georgi and S. L. Glashow, *Phys. Lett. B* **387**, 341 (1996).
 - [30] J. L. Rosner, *Phys. Lett. B* **387**, 113 (1996).
 - [31] P. Fileviez Perez and M. B. Wise, *J. High Energy Phys.* **08** (2011) 068.
 - [32] C. T. Hill, *Phys. Lett. B* **266**, 419 (1991); C. T. Hill and S. J. Parke, *Phys. Rev. D* **49**, 4454 (1994).
 - [33] R. S. Chivukula, A. G. Cohen, and E. H. Simmons, *Phys. Lett. B* **380**, 92 (1996); E. H. Simmons, *Phys. Rev. D* **55**, 1678 (1997).
 - [34] Y. Bai and B. A. Dobrescu, *J. High Energy Phys.* **07** (2011) 100.
 - [35] R. S. Chivukula, E. H. Simmons, and N. Vignaroli, *Phys. Rev. D* **87**, 075002 (2013); [arXiv:1306.2248](https://arxiv.org/abs/1306.2248).
 - [36] K. Kumar, R. Vega-Morales, and F. Yu, *Phys. Rev. D* **86**, 113002 (2012).
 - [37] P. Batra, B. A. Dobrescu, and D. Spivak, *J. Math. Phys. (N.Y.)* **47**, 082301 (2006).
 - [38] M. S. Carena, A. Daleo, B. A. Dobrescu, and T. M. P. Tait, *Phys. Rev. D* **70**, 093009 (2004); M. Duerr, P. Fileviez Perez, and M. B. Wise, *Phys. Rev. Lett.* **110**, 231801 (2013).
 - [39] C. D. Carone and H. Murayama, *Phys. Rev. Lett.* **74**, 3122 (1995); *Phys. Rev. D* **52**, 484 (1995); P. Fileviez Perez and

- M. B. Wise, *Phys. Rev. D* **82**, 011901 (2010); **82**, 079901 (E) (2010).
- [40] S. Chatrchyan *et al.* (CMS Collaboration), *Phys. Lett. B* **725**, 36 (2013); Report No. ATLAS-CONF-2011-135 (2011).
- [41] G. Aad *et al.* (ATLAS Collaboration), *Phys. Lett. B* **718**, 1284 (2013); S. Chatrchyan *et al.* (CMS Collaboration), *Phys. Lett. B* **716**, 103 (2012); **718**, 307 (2012).
- [42] S. Chatrchyan *et al.* (CMS Collaboration), *J. High Energy Phys.* **05** (2012) 123; **01** (2013) 154; *Phys. Rev. D* **86**, 112003 (2012).
- [43] L. J. Hall and A. E. Nelson, *Phys. Lett.* **153B**, 430 (1985); P. H. Frampton and S. L. Glashow, *Phys. Lett. B* **190**, 157 (1987).
- [44] B. A. Dobrescu, K. Kong, and R. Mahbubani, *J. High Energy Phys.* **06** (2009) 001.
- [45] B. A. Dobrescu, K. Kong, and R. Mahbubani, *Phys. Lett. B* **670**, 119 (2008).
- [46] C. Quigg, [arXiv:0908.3660](https://arxiv.org/abs/0908.3660).
- [47] R. S. Chivukula, A. Farzinnia, E. H. Simmons, and R. Foadi, *Phys. Rev. D* **85**, 054005 (2012); R. S. Chivukula, A. Farzinnia, J. Ren, and E. H. Simmons, *Phys. Rev. D* **87**, 094011 (2013).
- [48] J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer, and T. Stelzer, *J. High Energy Phys.* **06** (2011) 128.
- [49] J. Pumplin, D. R. Stump, J. Huston, H.-L. Lai, P. Nadolsky, and W.-K. Tung, *J. High Energy Phys.* **07** (2002) 012.
- [50] T. Sjostrand, S. Mrenna, and P. Z. Skands, *J. High Energy Phys.* **05** (2006) 026.
- [51] J. Conway *et al.*, “Pretty Good Simulation of High Energy Collisions,” <http://physics.ucdavis.edu/~conway/research/software/pgs/pgs4-general.htm>.
- [52] G. Z. Krnjaic, *Phys. Rev. D* **85**, 014030 (2012); M. Gresham, J. Shelton, and K. M. Zurek, *J. High Energy Phys.* **03** (2013) 008.
- [53] F. Yu, *Phys. Rev. D* **83**, 094028 (2011).
- [54] D. Choudhury, R. M. Godbole, and P. Saha, *J. High Energy Phys.* **01** (2012) 155.
- [55] A. Atre, R. S. Chivukula, P. Ittisamai, E. H. Simmons, and J.-H. Yu, *Phys. Rev. D* **86**, 054003 (2012).
- [56] T. Aaltonen *et al.* (CDF Collaboration), *Phys. Rev. Lett.* **103**, 041801 (2009).
- [57] J. Gaiser, Report No. SLAC-255 (1983), see Appendix F.1.