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Can the supermassive objects at the centers of galaxies be traversable wormholes? The first test of strong gravity for mm/sub-mm very long baseline interferometry facilities

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The near future mm/sub-mm very long baseline interferometry experiments are ambitious projects aiming at imaging the "shadow" of the supermassive black hole candidate at the center of the Milky Way and of the ones in nearby galaxies. An accurate observation of the shape of the shadow can potentially test the nature of these objects and verify if they are Kerr black holes, as predicted by general relativity. However, previous work on the subject has shown that the shadows produced in other spacetimes are very similar to the one of the Kerr background, suggesting that tests of strong gravity are not really possible with these facilities in the near future. In this work, I instead point out that it will be relatively easy to distinguish black holes from wormholes, topologically nontrivial structures of the spacetime that might have been formed in the early Universe and might connect our Universe with other universes.

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It is thought that the center of every normal galaxy harbors a supermassive black hole (BH) of $\sim 10^5 - 10^9 M_{\odot}$ [1]. Studies of the orbital motion of gas and of individual stars point out the existence of dark concentrations of mass too heavy, compact, and old to be clusters of nonluminous bodies, as the cluster lifetime due to evaporation and physical collisions would be shorter that the age of these systems [2]. The nonobservation of thermal radiation emitted by the putative surface of these objects may be seen as an indication for the absence of a normal surface and the presence of an event horizon [3] (see however [4]). The widely accepted interpretation is that all these supermassive objects are the Kerr BHs predicted by general relativity, even if we do not yet have evidence that the geometry of the spacetime around them is really described by the Kerr solution [5,6].

SgrA* is a bright and very compact radio source at the center of the Milky Way. Its position coincides with the one of the supermassive BH candidate of the Galaxy. At cm wavelengths, the structure of SgrA* is completely washed out by interstellar scattering. Observations of SgrA* at mm wavelengths suggest that in the near future it will be possible to image the emission region around the supermassive BH candidate with very long baseline interferometry (VLBI) techniques at sub-mm wavelengths [7]. This can be possible for three favorable conditions. First, the interstellar scattering reduces significantly at shorter wavelengths. Second, at sub-mm wavelengths, VLBI experiments can reach a resolution $\lambda/D \sim 10 \mu as$, where λ is the wavelength of the radiation and D is the distance between different stations; such a resolution is of the order of the angular size of the gravitational radius of SgrA*. Third, the compact synchrotron emitting region of SgrA* is expected to become optically thin at sub-mm wavelengths, thus allowing one to see the region around the

supermassive object. Another good candidate for the observation of its emission region is the supermassive object at the center of the galaxy M87 [8].

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General relativity makes clear predictions of the image of an optically thin emitting region around a BH. In particular, the image has a "shadow," a dark region over a brighter background [9,10]. While the intensity map of the image depends on the details of the accretion process and of the emission mechanisms, the boundary of the shadow is only determined by the metric of the spacetime, since it corresponds to the apparent image of the photon capture sphere as seen by a distant observer. The Event Horizon Telescope is an ambitious project with the main goal to observe the shadow of SgrA* [11,12]. The idea is to combine existing and planned mm/sub-mm facilities into a high resolution observatory. Similar experiments include the Japanese VLBI Network [13], the Chinese VLBI Network [14], the Korean VLBI Network [15], the Chinese Space VLBI project, and the effort of joining these East Asia facilities together.

The possibility of testing the nature of supermassive BH candidates by observing the shape of their shadow has been already discussed in the literature. The idea was first explored in [16], where the authors showed that the shadow of a Kerr BH and of a Kerr superspinning object (a very compact object described by the Kerr solution with spin parameter $|a_*| > 1$) are dramatically different, and that it would thus be relatively easy to distinguish the two cases with near future observations. However, superspinning compact objects seem to be ruled out on general theoretical reasons, because they are impossible to create and, in any case, strongly unstable [17]. If we consider physically acceptable non-Kerr exotic compact objects or non-Kerr BHs in putative alternative theories of gravity, their shadow is not so different with respect to the one of a Kerr BH and only high precision observations can detect deviations from the Kerr predictions [18]. This is not a surprise.

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At first approximation, the boundary of the shadow is a circle, whose radius is determined by the distance and by the mass of the compact object. The first order correction comes from the spin of the compact object, i.e., the current-dipole term in a multipole moment expansion of the gravitational field. Deviations from the Kerr shadow correspond to second order deformations, as they are associated with higher order multipole moment terms. As the measurement of the spin parameter of SgrA* and of the supermassive BH candidate at the center of M87 with the observation of their shadow is already out of reach for the Event Horizon Telescope and the East Asia projects, the possibility of testing the Kerr nature of these objects seems to be even more unlikely.

The aim of this short paper is to show that this conclusion is not completely true. While the near future mm/sub-mm VLBI experiments will not be able to distinguish Kerr BHs from non-Kerr exotic compact objects or non-Kerr BHs, meaningful tests of the nature of SgrA* are possible. In particular, it should be relatively easy to check if SgrA* is actually a wormhole (WH) [19]. WHs are topological structures of the spacetime connecting either two different regions of our Universe or two different universes in Multiverse models. The nonobservation of thermal radiation from SgrA* may be explained in the WH scenario, as WHs have no surface. WHs at the center of galaxies may also bypass the puzzle of the existence of BH candidates with $M \sim 10^9 M_{\odot}$ already at redshift $z \gtrsim 6$, as they would be relics of the very early Universe. Studies to observationally distinguish BHs from WHs are already present in the literature [20–22] and they may represent the only way to test Multiverse models.

Before discussing specific cases, let us consider a generic static, spherically symmetric, and asymptotically flat spacetime. Without loss of generality, its line element can be written as

$$ds^{2} = A(r)dt^{2} - B(r)dr^{2} - r^{2}d\theta^{2} - r^{2}\sin^{2}\theta d\phi^{2}, \quad (1)$$

where A(r) and B(r) must reduce to 1 for $r \to \infty$. Now we want to determine the apparent size of the central object as seen by a distant observer; that is, the photon impact parameter separating those photons falling onto the object from the ones reaching a minimum distance and coming back to infinity. Thanks to the spherical symmetry of the problem, we can restrict our discussion to the equatorial plane $\theta = \pi/2$. As the metric coefficients in Eq. (1) do not depend on the t and ϕ coordinates, there are two constants of motion, the energy E and the angular momentum L. From the Euler-Lagrangian equations we find

$$\dot{t} = \frac{E}{A(r)}, \qquad \dot{\phi} = \frac{L}{r^2}.$$
 (2)

 \dot{t} and $\dot{\phi}$ can then be plugged into $g_{\mu\nu}\dot{x}^{\mu}\dot{x}^{\nu}=0$ to get

$$\dot{r}^2 = \frac{1}{B(r)} \left[\frac{E^2}{A(r)} - \frac{L^2}{r^2} \right]. \tag{3}$$

If \dot{r}^2 vanishes before hitting the object, the photon reaches a turning point at $\dot{r}^2 = 0$ and then comes back to infinity. In the opposite case, the photon falls onto the object. The impact parameter is b = L/E and the critical one separating captured and uncaptured photons is given by the solution of the system $\dot{r}^2 = 0$ and $\partial_r \dot{r}^2 = 0$, that is:

$$r^2 - b_{\text{crit}}^2 A(r) = 0,$$
 $2b_{\text{crit}}^2 A^2(r) - r^3 A'(r) = 0.$ (4)

 $b_{\rm crit}$ corresponds to the value of the radius of the shadow as seen by a distant observer. Let us note that $b_{\rm crit}$ depends only on A(r), not on B(r).

In the Schwarzschild background, A(r) = 1 - 2M/r, and the solution of the system (4) is

$$b_{\text{Schwarzschild}}/M = 3\sqrt{3} \approx 5.196.$$
 (5)

Traversable WHs may have a quite different A(r). There are many kinds of WHs proposed in the literature, but a common WH geometry is the one with line element (see, e.g., [21,22])

$$ds^{2} = e^{2\Phi(r)}dt^{2} - \frac{dr^{2}}{1 - \Psi(r)} - r^{2}d\theta^{2} - r^{2}\sin^{2}\theta d\phi^{2}, \quad (6)$$

where Φ and Ψ are, respectively, the redshift and the shape function. A common choice is $\Phi = -r_0/r$, where r_0 is the WH throat radius and sets the scales of the system. r_0 is interpreted as the mass of the object in the Newtonian limit. With this choice of the redshift factor, Eq. (4) gives

$$b_{\text{Wormhole}}/r_0 = e \approx 2.718,\tag{7}$$

which is significantly smaller than the Schwarzschild prediction. If SgrA* is a Schwarzschild BH, the diameter of the shadow should be

$$\theta_{\text{Schwarzschild}} = (56 \pm 8) \ \mu \text{as},$$
 (8)

where the 14% uncertainty comes from the uncertainty of the measurements of its mass and its distance from us [23,24]:

$$M = (4.31 \pm 0.38)10^6 M_{\odot}, \qquad d = 7.94 \pm 0.42 \text{ kpc.}$$
 (9)

For a WH, we have

$$\theta_{\text{Wormhole}} = (29 \pm 4) \ \mu \text{as.} \tag{10}$$

The possibility that SgrA* is an extremal Kerr BH (which is unlikely) slightly reduces this gap, as the expected angular size orthogonal to the direction of the spin would be (see, e.g., [10])

$$\theta_{\text{Kerr. } a_n=1} = (48 \pm 7) \ \mu \text{as.}$$
 (11)

¹The reader should note that the shape function is usually defined in a different way in the literature of WHs.

While the current uncertainty in the measurements of Mand d are significant, thus forbidding in general the possibility of measuring the spin parameter (assuming the Kerr metric) or of distinguishing a Schwarzschild/Kerr BH from another object, in the case of WHs the difference in the expected apparent size is large enough to overcome these uncertainties. Spin parameter and deviations from Kerr can be measured/constrained without significant improvements of the measurements of M and d only with high precision observations, as they can be inferred from the exact shape (rather than the size) of the shadow. This is out of reach for near future experiments. Let us also note that the shadows of non-Kerr objects discussed so far in the literature differ from the Schwarzschild/Kerr one by a few percent [18]; that is, less than the uncertainty due to the measurements of M and d.

The calculation of the intensity map of the image of the emitting region requires instead some assumptions about the accretion process and the emission mechanisms. The observed specific intensity at the observed photon frequency $\nu_{\rm obs}$ at the point (X,Y) of the observer's image (usually measured in erg s⁻¹ cm⁻² str⁻¹ Hz⁻¹) can be found integrating the specific emissivity along the photon path (see, e.g., [25])

$$I_{\text{obs}}(\nu_{\text{obs}}, X, Y) = \int_{\gamma} g^3 j(\nu_{\text{e}}) dl_{\text{prop}}, \tag{12}$$

where $g = \nu_{\rm obs}/\nu_{\rm e}$ is the redshift factor, $\nu_{\rm e}$ is the photon frequency as measured in the rest frame of the emitter, $j(\nu_{\rm e})$ is the emissivity per unit volume in the rest frame of the emitter, and $dl_{\rm prop}$ is the infinitesimal proper length as measured in the rest frame of the emitter. The redshift factor can be evaluated from

$$g = \frac{k_{\alpha} u_{\text{obs}}^{\alpha}}{k_{\beta} u_{\text{e}}^{\beta}},\tag{13}$$

where k^{μ} is the 4-momentum of the photon, $u_{\text{obs}}^{\mu} = (1, 0, 0, 0)$ is the 4-velocity of the distant observer, while u_{e}^{μ} is the 4-velocity of the accreting gas emitting the

radiation. Here, I consider the simple case of gas in free fall, which, in a static and spherically symmetric spacetime, reduces to

$$u_{e}^{t} = \frac{1}{A(r)}, \qquad u_{e}^{r} = -\sqrt{\frac{1 - A(r)}{A(r)B(r)}}, \qquad u_{e}^{\theta} = u_{e}^{\phi} = 0.$$
 (14)

For the photons, k_t is a constant of motion and k_r can be inferred from $k_{\alpha}k^{\alpha}=0$, that is:

$$k_r = \pm k_t \sqrt{B(r) \left(\frac{1}{A(r)} - \frac{b^2}{r^2}\right)},$$
 (15)

where the sign +(-) is when the photon approaches (goes away from) the massive object. g is thus a function of r and b. Unlike the calculation of $b_{\rm crit}$, which is determined only by A(r), the intensity map depends also on B(r). Concerning the specific emissivity, we can assume a very simple model in which the emission is monochromatic with rest-frame frequency ν_{\star} and a $1/r^2$ radial profile:

$$j(\nu_{\rm e}) \propto \frac{\delta(\nu_{\rm e} - \nu_{\star})}{r^2},$$
 (16)

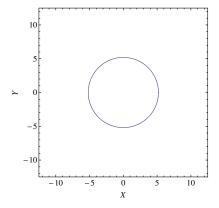
where δ is the delta function. Lastly, $dl_{\text{prop}} = k_{\alpha} u_{\text{e}}^{\alpha} d\lambda$ and, in our case, it reduces to

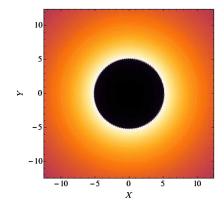
$$dl_{\text{prop}} = \frac{k_t}{g|k_r|} dr. \tag{17}$$

Integrating Eq. (12) over all the observed frequencies, we get the observed photon flux

$$F_{\text{obs}}(X, Y) \propto \int_{\gamma} \frac{g^3 k_t dr}{r^2 |k_r|}.$$
 (18)

The intensity map of the images for a Schwarzschild BH and a traversable WH are shown in the central panels of, respectively, Figs. 1 and 2. In the same figures, the right panels show the intensity along the *X* axis. In the case of





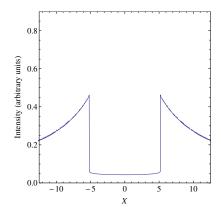
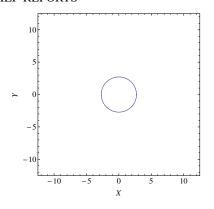
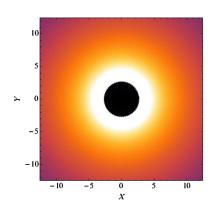


FIG. 1 (color online). Schwarzschild black hole: Contour of the black hole shadow (left panel), image of an optically thin emission region surrounding the black hole (central panel), and its intensity variation along the *X* axis (right panel). See the text for details.





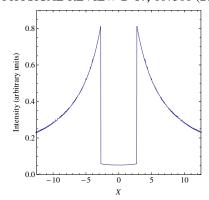


FIG. 2 (color online). Traversable wormhole: Contour of the wormhole shadow (left panel), image of an optically thin emission region surrounding the wormhole (central panel), and its intensity variation along the *X* axis (right panel). See the text for details.

the traversable WH, the calculations have used the shape function $\Psi = r_0/r$. It is also assumed that there is no or negligible emission of radiation coming from the other side of the WH.

Conclusions.—The "shadow" of the supermassive BH candidate at the center of the Milky Way and of the one in the galactic nucleus of M87 will be hopefully observed in the near future with mm/sub-mm VLBI facilities. As the shape of the shadow is only determined by the background metric around the compact object, these observations can potentially test the nature of these objects and verify if they are Kerr BHs, as predicted by general relativity. However, the uncertainties in the measurements of their mass and distance is quite large. In the case of SgrA*, the expected size of the apparent image has an uncertainty of about 14%, while the deformations considered in the recent literature due to deviations from the Kerr geometry are around a few percent. For the supermassive object at the center of M87, the predictions are even less clear. So, near future observations may not be able to distinguish Kerr BHs from other candidates. In this short work, I noted that the difference between the apparent image of Schwarzschild/Kerr BHs and WHs is instead quite significant, larger than the

uncertainty coming from the measurements of M and d, and thus relatively easy to test.

As a final remark, let us comment on possible wormholes with different geometries or the case of wormholes with nonvanishing spin. For a static and spherically symmetric spacetime, the size of the shadow is determined by g_{tt} , in the case of the wormholes discussed in this paper $g_{tt} = e^{-2r_0/r}$. While this form of g_{tt} is a quite common choice in the literature, it is not unique. For instance, the one-way traversable wormholes discussed in [26] have the exterior spacetime equivalent to the Schwarzschild/Kerr solution, and they are thus indistinguishable from the BHs of general relativity. The possibility of rotating wormholes should instead not change at all the conclusions of this work. The angular size would decrease for spinning solutions, so that the shadow of the Kerr family can always be distinguished from that of a spinning wormhole family. Moreover, rotating wormholes seem already to be ruled out by current x-ray data [22].

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