Comprehensive analysis on lepton flavor violating Higgs boson to $\mu^{\mp}\tau^{\pm}$ decay in supersymmetry without *R* parity

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In this paper we examine thoroughly the Higgs boson to $\mu^{\pm}\tau^{\pm}$ decay via processes involving *R* parity violating couplings. By means of full one-loop diagrammatic calculations, we found that even if known experimental constraints, particularly including the stringent sub-eV neutrino mass bounds, give strong restrictions on some of the *R* parity violating parameters, the branching ratio could still achieve notable value in the admissible parameter space. Hence, the flavor violating leptonic decay is of interest to future experiments. We present here key results of our analysis. Based on the analysis, we give some comments on $h^0 \rightarrow e^{\mp}\mu^{\pm}$ and $h^0 \rightarrow e^{\mp}\tau^{\pm}$ also.

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I. INTRODUCTION

As we know, in the standard model (SM) the lepton number of each flavor is separately conserved. Thus lepton flavor violating (LFV) decays such as the Higgs boson to $\mu^{\mp}\tau^{\pm}$ are forbidden. However, neutrino oscillation experiments provide strong evidence that the lepton flavor conservation should be violated [1–4]. If lepton flavor violation can be observed in processes involving only SM particles, this would contribute an important probe to physics beyond the SM. Such processes, in particular the Higgs boson to $\mu^{\mp}\tau^{\pm}$ decay, deserve attention.

Looking into the literature, various sources or scenarios to accommodate LFV interactions have been introduced and analyzed. For example, adding heavy right-handed neutrinos can give neutrinos mixings and hence lepton flavor violation [5]. Also, a general two Higgs doublet model has LFV interactions due to Yukawa coupling matrices which cannot be diagonalized simultaneously [6,7]. Under the framework of supersymmetry (SUSY), it is well known that nonzero off-diagonal elements of soft SUSY breaking terms in the leptonic sector (A^E , \tilde{m}_L^2 and \tilde{m}_E^2 , to be precisely defined below) generate LFV couplings. Moreover, the (total) lepton number itself may not be conserved. For the SUSY case, such *R* parity violating (RPV) couplings also give interesting contributions to processes like the Higgs boson to $\mu^{\mp} \tau^{\pm}$ decay.

While SUSY is undoubtedly a popular candidate theory for new physics, its existence so far lacks experimental evidence [8]. Thus, some simple versions of the supersymmetric model, such as the constrained minimal supersymmetric standard model, have faced stringent challenges [9]. However, it has been pointed out that there is still room for the (minimal) supersymmetric standard model to accommodate existing experimental constraints [10–13]. For instance, the large mass spectrum for the majority of supersymmetric particles around or beyond 1 TeV has yet to be probed [13]. The heavy spectrum is in accordance with the newly discovered boson mass \approx 125 to 126 GeV [14–16]. A large portion of the parameter space remains uncovered in versions of the minimal supersymmetric standard model (MSSM) with more free parameters [11]. Nonuniversality of soft SUSY breaking masses is also a possible explanation for the nonobservation of supersymmetric signals [12].

Under the scheme of the MSSM, various LFV decays such as $\tau \to \mu \gamma, \tau \to \mu X, \tau \to \mu \eta, \tau \to \mu \mu \mu$, and so on [17], as well as the Higgs boson to $\mu^{\pm}\tau^{\pm}$ decay [7,18] which we put our focus on in this paper, have been discussed. However, in many studies of the MSSM, R parity is often imposed by hand to prevent proton decay and make the lightest supersymmetric particle a possible dark matter candidate. From the theoretical point of view, R parity is ad hoc and not well motivated so long as the phenomenological (minimal) supersymmetric standard model is concerned [19]. A generic supersymmetric standard model (without R parity imposed), on the contrary, not only provides a convenient way to lepton flavor violation, but also has the advantage of a richer phenomenology including neutrino masses and mixings without introducing any extra superfield. Under the framework of SUSY with Rparity violation, there have been some studies [20,21] on the issue of lepton flavor violation. Nevertheless, such studies were either limited to particular types of R parity violation or did not take $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ into consideration. While recently both ATLAS and CMS [14,15] reported discovery of a boson state which is essentially compatible with a SM-like Higgs, more data are needed to pin down its nature, and the flavor violating Higgs decay

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such as $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ is especially interesting at this moment. In this paper, we will investigate thoroughly the LFV Higgs boson to $\mu^{\mp} \tau^{\pm}$ decay from SUSY without *R* parity via full diagrammatic calculations up to one-loop level. Under a reasonable choice of the experimentally viable parameter space, the most significant branching ratios of various RPV parameter combinations will be reported. Note that part of the key results has been reported, with limited presentation of analytical expressions and discussions, in a short letter [22].

In following section, we summarize our basic formulation and parametrization of the generic supersymmetric standard model (without R parity). Particularly, the neutral and charged Higgs mass terms, including loop corrections (up to two-loop for the neutral Higgs case), would be discussed. Then we give a sketch of our calculations and show numerical results from all possible RPV parameter combinations in Sec. III. Note that during our analysis we made no assumptions on the RPV parameters. The mass spectrum of all SUSY particles as well as the Higgs boson are kept within experimental constraints. Finally, we conclude this paper with some remarks in Sec. IV. Lists of all one-loop diagrams and useful effective couplings will be given in the Appendices. We may be including more details than necessary, particularly in the sense of showing some experimentally uninteresting results. We include those to give a full picture about the physics involved, so that readers can appreciate the key features leading to the interesting or uninteresting results. Some of the lessons one can learn from the analysis would be useful for future studies of other related aspects of the model. Under the same consideration, we give detailed expressions of the couplings involved and the Feynman diagrams in the Appendices.

II. SUPERSYMMETRIC STANDARD MODEL WITHOUT *R* PARITY AND SCALAR MASS MATRICES

A. Formulation and parametrization

With the content of the minimal superfields spectrum, the most general renormalizable superpotential without R parity can be written as

$$W = \epsilon_{ab} \left[\mu_{\alpha} \hat{H}^{a}_{u} \hat{L}^{b}_{\alpha} + h^{u}_{ik} \hat{Q}^{a}_{i} \hat{H}^{b}_{u} \hat{U}^{C}_{k} + \lambda'_{\alpha j k} \hat{L}^{a}_{\alpha} \hat{Q}^{b}_{j} \hat{D}^{C}_{k} \right. \\ \left. + \frac{1}{2} \lambda_{\alpha \beta k} \hat{L}^{a}_{\alpha} \hat{L}^{b}_{\beta} \hat{E}^{C}_{k} \right] + \frac{1}{2} \lambda''_{i j k} \hat{U}^{C}_{i} \hat{D}^{C}_{j} \hat{D}^{C}_{k}, \tag{1}$$

where (a, b) are SU(2) indices with $\epsilon_{12} = -\epsilon_{21} = 1$, (i, j, k) are the usual family (flavor) indices, and (α, β) are extended flavor indices going from 0 to 3. Note that λ is antisymmetric in the first two indices as required by SU(2) product rules while λ'' is antisymmetric in the last two indices by SU(3)_C. The soft SUSY breaking terms can be written as follows:

$$V_{\text{soft}} = \epsilon_{ab} B_{\alpha} H^{a}_{u} \tilde{L}^{b}_{\alpha} + \epsilon_{ab} [A^{U}_{ij} \tilde{Q}^{a}_{i} H^{b}_{u} \tilde{U}^{\dagger}_{j} + A^{D}_{ij} H^{a}_{d} \tilde{Q}^{b}_{i} \tilde{D}^{\dagger}_{j} + A^{E}_{ij} H^{a}_{d} \tilde{L}^{b}_{i} \tilde{E}^{\dagger}_{j}] + \text{H.c.}$$

$$+ \epsilon_{ab} \left[A^{\lambda'}_{ijk} \tilde{L}^{a}_{i} \tilde{Q}^{b}_{j} \tilde{D}^{\dagger}_{k} + \frac{1}{2} A^{\lambda}_{ijk} \tilde{L}^{a}_{i} \tilde{L}^{b}_{j} \tilde{E}^{\dagger}_{k} \right] + \frac{1}{2} A^{\lambda''}_{ijk} \tilde{U}^{\dagger}_{i} \tilde{D}^{\dagger}_{j} \tilde{D}^{\dagger}_{k} + \text{H.c.}$$

$$+ \tilde{Q}^{\dagger} \tilde{m}^{2}_{Q} \tilde{Q} + \tilde{U}^{\dagger} \tilde{m}^{2}_{U} \tilde{U} + \tilde{D}^{\dagger} \tilde{m}^{2}_{D} \tilde{D} + \tilde{L}^{\dagger} \tilde{m}^{2}_{L} \tilde{L} + \tilde{E}^{\dagger} \tilde{m}^{2}_{E} \tilde{E} + \tilde{m}^{2}_{H_{u}} |H_{u}|^{2}$$

$$+ \frac{M_{1}}{2} \tilde{B} \tilde{B} + \frac{M_{2}}{2} \tilde{W} \tilde{W} + \frac{M_{3}}{2} \tilde{g} \tilde{g} + \text{H.c.}, \qquad (2)$$

where $\tilde{L}^{\dagger}\tilde{m}_{\tilde{L}}^{2}\tilde{L}$ is given by a 4 × 4 matrix. $\tilde{m}_{L_{00}}^{2}$ corresponds to $\tilde{m}_{H_{d}}^{2}$ in MSSM, while $\tilde{m}_{L_{0k}}^{2}$'s give new mass mixings. Note that $\tilde{U}^{\dagger}, \tilde{D}^{\dagger}$, and \tilde{E}^{\dagger} are the scalar components of the superfields \hat{U}^{C}, \hat{D}^{C} , and \hat{E}^{C} , respectively.

The above, together with the standard (gauged) kinetic terms, describe the full Lagrangian of the model. We have four \hat{L} superfields, which contain the components of the fermion doublet as l^0 and l^- , while their scalar partners are \tilde{l}^0 and \tilde{l}^- . In principle, the neutral scalar part \tilde{l}^0_{α} of all four \hat{L} superfields can bear vacuum expectation values (VEVs). To make the analysis simple and the physics more transparent, we use a parametrization which picks a basis such that the direction of the VEV is singled out, i.e., only \hat{L}_0 bears a nonzero VEV among four \hat{L} 's. This procedure guarantees \hat{L}_0 can be always identified as \hat{H}_d in MSSM. The two superfields have the same quantum number as the symmetry of the lepton number which makes the distinction between \hat{L} and \hat{H}_d by definition not part of the model.

However, one should keep in mind that \hat{H}_d may contain partly the charged lepton states. It is also worth mentioning here that the down quark and charged lepton Yukawa coupling matrices are both diagonal under our parametrization while the up quark Yukawa coupling is the product of Cabibbo-Kobayashi-Maskawa (CKM) factors and diagonal quark masses. The parametrization has the advantage that tree level RPV contributions to the neutral scalar mass matrix are described completely by the μ_i , B_i , and $\tilde{m}_{L_{0i}}^2$ parameters, which are well constrained to be small even with just very conservative neutrino mass bounds imposed [23,24].

Now we turn to the issue about mass matrices of matter fields. In our framework, the three known charged leptons, together with two charginos, correspond to the mass eigenstates of a 5 × 5 charged fermion matrix \mathcal{M}_C , which can be diagonalized by two unitary matrices as $V^{\dagger}\mathcal{M}_C U =$ diag $\{M_{\chi_n^-}\} \equiv$ diag $\{M_{c1}, M_{c2}, m_e, m_\mu, m_\tau\}$. For neutral fermions, we take four heavy neutralinos and three very light neutrinos as mass eigenstates under the scheme of a 7×7 neutral fermion mass matrix $\mathcal{M}_{\mathcal{N}}$. By using a unitary matrix X, the diagonalization can be done as $X^T \mathcal{M}_{\mathcal{N}} X = \text{diag}\{M_{\chi_n^0}\} \equiv \text{diag}\{M_{n_{i=1,4}}, m_{\nu_1}, m_{\nu_2}, m_{\nu_3}\}$. On considering the squark sectors, the up squark mass-squared matrix looks exactly the same as the one in MSSM, while the down squark one contains a new contribution from RPV terms. They can be diagonalized separately as $\mathcal{D}^u^\dagger \mathcal{M}_U^2 \mathcal{D}^u = \text{diag}\{\mathcal{M}_U^2\}$ and $\mathcal{D}^d^\dagger \mathcal{M}_D^2 \mathcal{D}^d = \text{diag}\{\mathcal{M}_D^2\}$. All the mass matrices mentioned above can be found in Ref. [23].

B. Scalar mass matrices and loop corrections

For the neutral scalar mass matrix, we have now five neutral complex scalar fields from \hat{H}_u and four \hat{L}_{α} 's. Explicitly, we write the (1 + 4) complex fields in terms of their scalar and pseudoscalar parts, in the order $\{h_u^{0\dagger}, \tilde{l}_0^0, \tilde{l}_1^0, \tilde{l}_2^0, \tilde{l}_3^0\}$ to form a full 10×10 (real and symmetric) mass-squared matrix, which (in tree level) can be written as

$$\mathcal{M}_{S}^{2} = \begin{pmatrix} \mathcal{M}_{SS}^{2} & \mathcal{M}_{SP}^{2} \\ (\mathcal{M}_{SP}^{2})^{T} & \mathcal{M}_{PP}^{2} \end{pmatrix},$$
(3)

where the scalar, pseudoscalar, and mixing parts are

$$\mathcal{M}_{SS}^2 = \operatorname{Re}(\mathcal{M}_{\phi}^2) + 2\mathcal{M}_{\phi\phi}^2, \qquad \mathcal{M}_{PP}^2 = \operatorname{Re}(\mathcal{M}_{\phi}^2), \qquad (4)$$
$$\mathcal{M}_{SP}^2 = -\operatorname{Im}(\mathcal{M}_{\phi}^2),$$

respectively, with

$$\mathcal{M}_{\phi\phi}^{2} = \frac{1}{2} M_{Z}^{2} \begin{pmatrix} \sin^{2}\beta & -\cos\beta\sin\beta & 0_{1\times3} \\ -\cos\beta\sin\beta & \cos^{2}\beta & 0_{1\times3} \\ 0_{3\times1} & 0_{3\times1} & 0_{3\times3} \end{pmatrix}, \quad (5)$$

and

$$\mathcal{M}_{\phi}^{2} = \begin{pmatrix} \tilde{m}_{H_{u}}^{2} + \mu_{\alpha}^{*} \mu_{\alpha} + M_{Z}^{2} \cos 2\beta \left[-\frac{1}{2} \right] & -(B_{\alpha}) \\ -(B_{\alpha}^{*}) & \tilde{m}_{L}^{2} + (\mu_{\alpha}^{*} \mu_{\beta}) + M_{Z}^{2} \cos 2\beta \left[\frac{1}{2} \right] I_{4 \times 4} \end{pmatrix}.$$
(6)

As for charged (colorless) scalars, we should treat charged Higgs and sleptons on an equal footing. The basis $\{h_u^{+\dagger}, \tilde{l}_0^-, \tilde{l}_1^-, \tilde{l}_2^-, \tilde{l}_3^-, \tilde{l}_1^{+\dagger}, \tilde{l}_2^{+\dagger}, \tilde{l}_3^{+\dagger}\}$ as 1 + 4 + 3 form from \hat{H}_u , four \hat{L}_{α} 's and three \hat{E}_i^C 's is used to write the 8×8 charged scalar mass-squared matrix, which can be written as

$$\mathcal{M}_{E}^{2} = \begin{pmatrix} \tilde{\mathcal{M}}_{H_{u}}^{2} & \tilde{\mathcal{M}}_{LH}^{2\dagger} & \tilde{\mathcal{M}}_{RH}^{2\dagger} \\ \tilde{\mathcal{M}}_{LH}^{2} & \tilde{\mathcal{M}}_{LL}^{2} & \tilde{\mathcal{M}}_{RL}^{2\dagger} \\ \tilde{\mathcal{M}}_{RH}^{2} & \tilde{\mathcal{M}}_{RL}^{2} & \tilde{\mathcal{M}}_{RR}^{2} \end{pmatrix},$$
(7)

where

$$\tilde{\mathcal{M}}_{H_{u}}^{2} = \tilde{m}_{H_{u}}^{2} + \mu_{\alpha}^{*} \mu_{\alpha} + M_{Z}^{2} \cos 2\beta \left[\frac{1}{2} - \sin^{2} \theta_{W} \right] + M_{Z}^{2} \sin^{2} \beta [1 - \sin^{2} \theta_{W}],$$

$$\tilde{\mathcal{M}}_{LL}^{2} = \tilde{m}_{L}^{2} + m_{L}^{\dagger} m_{L} + (\mu_{\alpha}^{*} \mu_{\beta}) + M_{Z}^{2} \cos 2\beta \left[-\frac{1}{2} + \sin^{2} \theta_{W} \right] I_{4 \times 4} + \begin{pmatrix} M_{Z}^{2} \cos^{2} \beta [1 - \sin^{2} \theta_{W}] & 0_{1 \times 3} \\ 0_{3 \times 1} & 0_{3 \times 3} \end{pmatrix},$$

$$\tilde{\mathcal{M}}_{RR}^{2} = \tilde{m}_{E}^{2} + m_{E} m_{E}^{\dagger} + M_{Z}^{2} \cos 2\beta [-\sin^{2} \theta_{W}] I_{3 \times 3},$$
(8)

and

$$\begin{split} \tilde{\mathcal{M}}_{LH}^2 &= (B_{\alpha}^*) + \begin{pmatrix} \frac{1}{2}M_Z^2 \sin 2\beta [1 - \sin^2 \theta_W] \\ 0_{3\times 1} \end{pmatrix}, \\ \tilde{\mathcal{M}}_{RH}^2 &= -(\mu_i^* \lambda_{i0k}) \frac{\nu_0}{\sqrt{2}} = (\mu_k^* m_k) \quad \text{(no sum over } k), \end{split}$$

$$(\tilde{\mathcal{M}}_{RL}^2)^T = \begin{pmatrix} 0\\ A^E \end{pmatrix} \frac{v_0}{\sqrt{2}} - (\mu_{\alpha}^* \lambda_{\alpha\beta k}) \frac{v_u}{\sqrt{2}},\tag{9}$$

with $m_L = \text{diag}\{0, m_E\} = \text{diag}\{0, m_1, m_2, m_3\}$. m_i 's ($\approx m_{e_i}$ under the small- μ_i scenario) are mass parameters in the charged fermion mass matrix [23]. Furthermore, the two scalar mass-squared matrices can be diagonalized

as $\mathcal{D}^{sT}\mathcal{M}_{S}^{2}\mathcal{D}^{s} = \text{diag}\{M_{Sm=1,10}^{2}\}$ and $\mathcal{D}^{l\dagger}\mathcal{M}_{E}^{2}\mathcal{D}^{l} = \text{diag}\{M_{\tilde{\ell}n=1,8}^{2}\}$, which will become useful later.

Different from MSSM, the physical scalar states are now a mixture of Higgs bosons and sleptons. The RPV terms provide new contributions to the scalar mass matrices and hence the Higgs masses. In addition, radiative corrections, especially those from third generation quarks and squarks, could play important roles in the Higgs mass. Accordingly, we implement complete oneloop corrections [25] to matrix elements directly relating to Higgs bosons (*CP*-even, *CP*-odd and charged ones as well) during our computation. Moreover, the light Higgs mass should be treated delicately because of the newly discovered boson mass \cong 125 to 126 GeV by the Large Hadron Collider (LHC) [14,15]. Therefore we include further an estimation [26] of key two-loop corrections in light Higgs related elements.¹ Note that radiative RPV corrections are typically too small to be taken into account; thus we study tree level RPV effects only.

Under the scheme of MSSM without R parity, the one-loop effective Higgs potential is (recall that $\hat{H}_d \equiv \hat{L}_0$ after our parametrization is chosen)

$$V_{\text{eff}} = (\tilde{m}_{H_u}^2 + |\mu_{\alpha}|^2)|H_u|^2 + (\tilde{m}_{L_{00}}^2 + |\mu_0|^2)|H_d|^2 + (\epsilon_{ab}B_0H_u^aH_d^b + \text{H.c.}) + \frac{1}{8}(g_2^2 + g'^2)|H_u|^4 + \frac{1}{8}(g_2^2 + g'^2)|H_d|^4 + \frac{1}{4}(g_2^2 - g'^2)|H_u|^2 + \frac{1}{2}g_2^2|\epsilon_{ab}H_u^aH_d^b|^2 + \frac{3}{32\pi^2}\sum_{q=t,b}\left[\sum_{i=1,2}\tilde{m}_{q_i}^4\left(\ln\frac{\tilde{m}_{q_i}^2}{Q^2} - \frac{3}{2}\right) - 2\bar{m}_q^4\left(\ln\frac{\tilde{m}_q^2}{Q^2} - \frac{3}{2}\right)\right],$$
(10)

where Q is the renormalization scale which should be around the weak scale (10² to 10³ GeV). $\tilde{m}_{q_i}^2$ and \bar{m}_q^2 denote (Higgs background fields dependent) eigenvalues of the squark and quark mass matrices respectively.

By using the following linear expansion of Higgs bosons (with a relative complex phase for generality,²)

$$H_{u} = \begin{pmatrix} h_{u}^{+} \\ \frac{1}{\sqrt{2}}(v_{u} + h_{u}^{s} - ih_{u}^{a}) \end{pmatrix}, \qquad H_{d} = e^{i\theta_{v}} \begin{pmatrix} \frac{1}{\sqrt{2}}(v_{d} + h_{d}^{s} + ih_{d}^{a}) \\ h_{d}^{-} \end{pmatrix},$$
(11)

tadpole equations can be written as

$$\boldsymbol{v}_{d} \operatorname{Re}(B_{0}e^{i\theta_{v}}) = (\tilde{m}_{H_{u}}^{2} + |\boldsymbol{\mu}_{\alpha}|^{2})\boldsymbol{v}_{u} + \frac{1}{8}(g_{2}^{2} + g^{\prime 2})\boldsymbol{v}_{u}(\boldsymbol{v}_{u}^{2} - \boldsymbol{v}_{d}^{2}) \\
+ \frac{3}{16\pi^{2}} \bigg[\sum_{q=t,b} \sum_{i=1,2} m_{\tilde{q}_{i}}^{2} \Big\langle \frac{\partial \tilde{m}_{q_{i}}^{2}}{\partial h_{u}^{s}} \Big\rangle \Big(\ln \frac{m_{\tilde{q}_{i}}^{2}}{Q^{2}} - 1 \Big) - 2m_{t}^{2} \Big\langle \frac{\partial \bar{m}_{t}^{2}}{\partial h_{u}^{s}} \Big\rangle \Big(\ln \frac{m_{t}^{2}}{Q^{2}} - 1 \Big) \bigg] \\
\boldsymbol{v}_{u} \operatorname{Re}(B_{0}e^{i\theta_{v}}) = (\tilde{m}_{L_{00}}^{2} + |\boldsymbol{\mu}_{0}|^{2})\boldsymbol{v}_{d} + \frac{1}{8}(g_{2}^{2} + g^{\prime 2})\boldsymbol{v}_{d}(\boldsymbol{v}_{d}^{2} - \boldsymbol{v}_{u}^{2}) \\
+ \frac{3}{16\pi^{2}} \bigg[\sum_{q=t,b} \sum_{i=1,2} m_{\tilde{q}_{i}}^{2} \Big\langle \frac{\partial \tilde{m}_{q_{i}}^{2}}{\partial h_{d}^{s}} \Big\rangle \Big(\ln \frac{m_{\tilde{q}_{i}}^{2}}{Q^{2}} - 1 \Big) - 2m_{b}^{2} \Big\langle \frac{\partial \bar{m}_{b}^{2}}{\partial h_{d}^{s}} \Big\rangle \Big(\ln \frac{m_{b}^{2}}{Q^{2}} - 1 \Big) \bigg] \\
\boldsymbol{v}_{d(u)} \operatorname{Im}(B_{0}e^{i\theta_{v}}) = + (-) \frac{3}{16\pi^{2}} \sum_{q=t,b} \sum_{i=1,2} m_{\tilde{q}_{i}}^{2} \Big\langle \frac{\partial \tilde{m}_{q_{i}}^{2}}{\partial h_{u(d}^{s}}} \Big\rangle \Big(\ln \frac{m_{\tilde{q}_{i}}^{2}}{Q^{2}} - 1 \Big), \tag{12}$$

where $m_{\tilde{q}_i}^2 = \langle \tilde{m}_{q_i}^2 \rangle$ is the squark mass squared, while expressions for the derivatives with respect to the scalar fields in the bracket (including second derivatives used later) are complicated so we do not list them here. One can see Ref. [25] for example, for details.³

Tadpole equations along the direction of other scalars/sleptons can be obtained easily from scalar potential terms which are related to neutral sleptons:⁴

$$V = \sum_{i,j=1,3} \left[(\tilde{m}_{L_{ij}}^2 + \mu_i^* \mu_j) \tilde{l}_i^{0*} \tilde{l}_j^0 + (\tilde{m}_{L_{i0}}^2 + \mu_0 \mu_i^*) h_d^0 \tilde{l}_i^{0*} + (\tilde{m}_{L_{0i}}^2 + \mu_0^* \mu_i) h_d^0 \tilde{l}_i^0 + \frac{1}{8} (g_2^2 + g'^2) (|\tilde{l}_i^0|^2 |\tilde{l}_j^0|^2 - 2|\tilde{l}_i^0|^2 |h_u^0|^2 + 2|\tilde{l}_i^0|^2 |h_d^0|^2) - (B_i h_u^0 \tilde{l}_i^0 + \text{H.c.}) \right],$$
(13)

while vanishing derivatives of V give

$$B_i \tan\beta = \tilde{m}_{L_{0i}}^2 + \mu_0^* \mu_i.$$
(14)

¹Though the Higgs bosons mix with the sleptons via RPV terms, we can still identify the Higgs bosons among other sleptons due to the foreseeable smallness of RPV parameters.

²It is basically a *CP* phase. In this study, the phase is set to be zero for simplicity. ³There may be a sign difference between the expression for derivatives in the reference and ours due to the definition of linear expansion of scalars.

⁴Conceptually, \tilde{l} is not the usual $\tilde{\nu}_i$ since l_i^0 deviates from ν_i slightly, with parameter μ_i characterizing the deviation between them. See Ref. [23] for details.

Free parameters	Range		
$ \mu_0 , M_2, A_{\mu} , A_d $ and $ A^{\lambda} $	≤ 2500 GeV		
A_e	0, since its influence is negligible		
tanβ	3 to 60		
$\tilde{m}_E^2 = \tilde{m}_L^2$ (without zeroth component)	$\leq (2500 \text{ GeV})^2$ with off-diagonal elements 0		
$\tilde{m}_E^2 = \tilde{m}_L^2$ (without zeroth component) $\tilde{m}_{L_{00}}^2$	Constrained only by mass eigenvalues below		
Mass eigenvalues output	Range		
Light Higgs mass	123 to 127 GeV		
Heavy Higgs/sneutrino masses	200 GeV to 3 TeV		
Charged Higgs/slepton masses	200 GeV to 3 TeV		

TABLE I. List of the parameter ranges and conditions we adopted.

The exact form of tree level elements of scalar matrices are as mentioned above, while the one-loop corrections from third generation quarks and squarks are

$$\mathcal{M}_{jk}^{\text{Loop}} = \frac{3}{16\pi^2} \sum_{q=t,b} \left\{ \sum_{i=1,2} \left[\left\langle \frac{\partial \tilde{m}_{q_i}^2}{\partial \phi_j} \right\rangle \left\langle \frac{\partial \tilde{m}_{q_i}^2}{\partial \phi_k} \right\rangle \ln \frac{m_{\tilde{q}_i}^2}{Q^2} \right. \\ \left. + m_{\tilde{q}_i}^2 \left\langle \frac{\partial^2 \tilde{m}_{q_i}^2}{\partial \phi_j \partial \phi_k} \right\rangle \left(\ln \frac{m_{\tilde{q}_i}^2}{Q^2} - 1 \right) \right] - 2 \left[\left\langle \frac{\partial \tilde{m}_q^2}{\partial \phi_j} \right\rangle \right] \\ \left. \times \left\langle \frac{\partial \tilde{m}_q^2}{\partial \phi_k} \right\rangle \ln \frac{m_q^2}{Q^2} + m_q^2 \left\langle \frac{\partial^2 \tilde{m}_q^2}{\partial \phi_j \partial \phi_k} \right\rangle \left(\ln \frac{m_q^2}{Q^2} - 1 \right) \right] \right\}.$$

$$(15)$$

In the case of neutral scalars, *j* and *k* can be any number among 1, 2, 6, 7 which correspond to h_u^s , h_d^s , h_u^a and h_d^a respectively. As to the charged scalar case, *j* and *k* can only take the value of 1 or 2, with $\phi_j = \{h_u^+, h_d^+\}$ and $\phi_k = \{h_u^-, h_d^-\}$. By including the one-loop corrections mentioned above and the estimation of two-loop corrections [26] to the scalar mass matrices, the numerical values of the Higgs masses can be obtained with enough accuracy.

III. CALCULATIONS AND NUMERICAL RESULTS

At tree level, a neutral Higgs boson can decay into $\mu^-\tau^+$ or $\tau^-\mu^+$ directly via RPV neutral scalar-charged lepton-charged lepton coupling which is absent in MSSM. Otherwise, the neutral Higgs boson can decay through one-loop diagrams (or higher loop diagrams). We list in Appendix A all possible one-loop diagrams containing RPV couplings for a neutral scalar decaying to $\mu^-\tau^+$. The RPV effective couplings we used among all relevant mass eigenstates are listed in Appendix B. In our analysis, we diagonalize all the mass matrices numerically and deal directly with the mass eigenstates. The one-loop and two-loop corrections (as mentioned in Sec. II) to matrix elements which are most relevant to the Higgs mass are also implemented. We have fully calculated the decay amplitude of all (tree and one-loop)

diagrams that may contribute. By encoding the analytical formulas of decay amplitude into the program, and using the LoopTools [27] program for the evaluation of loop functions, the numerical value of total amplitude and hence decay rate of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ can be obtained. We include all the widths of significant decay channels in MSSM such as Higgs boson to $\bar{b}b$, $\tau^-\tau^+$, WW^* , ZZ^* , $\gamma\gamma$, and gg, plus the RPV decay rate of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$, to get the total width of Higgs decay. The branching ratio of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ can then be obtained.

Our aim is to use a concrete setting that is compatible with known constraints but not otherwise too restrictive, to illustrate what we expect to be more generic features of the RPV signature. After considering the uncertainties in the experimental Higgs mass and loop corrections to Higgs mass terms, we kept the numerical light Higgs mass to be in the range of 123 to 127 GeV. Furthermore, we adopt the relation $M_2 = \frac{1}{35}M_3 = 2M_1$ between three gaugino masses and the condition that squarks of the first two families cannot be lighter than about $0.8M_3$. Therefore we take soft SUSY breaking scalar masses $\tilde{m}_Q^2 = \tilde{m}_U^2 =$ $\tilde{m}_D^2 = (0.8M_3 \times \text{identity matrix})^2$ for simplicity in our analysis. The parameter setting is in accordance with the gravity-mediated SUSY breaking picture [28], for instance. The other restrictions and assumptions we used can be found in Table I.

There are many different sources (e.g., flavor violating charged lepton decays like $\tau^- \rightarrow \mu^- e^+ e^-$ [29], leptonic radiative decays like $\mu \rightarrow e\gamma$ [21], semileptonic decays like $D^+ \rightarrow \bar{K}^0 l_i^+ \nu_i$ [30], experimental values of CKM matrix elements [30] and so on) which can give constraints on our RPV parameter setting. Among all the available constraints, the one from indirect evidence of the neutrino mass, i.e., $\sum_i m_{\nu_i} \leq 1 \text{ eV}$ [31] is quite crucial. Note that all LFV couplings/mass mixings that conserve *R* parity have been turned off during our analysis. That is to single out the effects of the RPV ones. The reported numerical branching ratios are the most significant numbers we found under the framework.

A. Contribution from $B_i B_j$ combinations

The constraints on this type of combination are mainly from neutrino mass experiments. The RPV parameter B_i can give contributions to neutrino masses via one-loop diagrams [32]. Generally speaking, larger sneutrino and neutralino masses will raise the upper bound of B_i .

Except for the combinations B_2B_3 and B_1B_1 , B_iB_j combinations can only give contributions to the decay from the type 2 no. 4 diagram (in Appendix A). Since heavy charged scalar masses will severely suppress this diagram, we can have relatively larger amplitudes only in the existence of light charged scalar(s). For the B_2B_3 combination many diagrams contribute; hence its behavior is quite complicated. Basically, the decay amplitude from B_2B_3 tends to increase when soft SUSY breaking scalar masses and gaugino masses get heavier due to the rise of the upper bound on B_i from neutrino masses as mentioned above. Note that B_2 or B_3 alone can give contributions to the $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ decay as well. Such contributions are, unavoidably, included in all combinations containing B_2 or B_3 . Combinations that are not listed give zero contribution at one-loop level—similar to the other kinds of RPV parameter combinations given below. Our results are shown in Table II.

B. Contribution from $B_i \mu_i$ combinations

The $B_i \mu_j$ type of combination gets constrained from several sources. The values of B_i and $B_i \mu_j$ are highly constrained separately by their loop contribution to neutrino masses [32]. On the other hand, a nonzero μ_j will induce a tree level neutrino mass; hence it is also constrained. The nonobservation of leptonic radiative decays like $\mu \rightarrow e\gamma$, etc. also gives upper bounds on $B_i \mu_j$, say, $|B_1^* \mu_3|$, $|B_2^* \mu_3|$, $|B_3 \mu_1^*|$ and $|B_3 \mu_2^*| \leq 10^{-4} |\mu_0|^3$; $|B_1^* \mu_2|$ and $|B_2 \mu_1^*| \leq 7 \times 10^{-7} |\mu_0|^3$ [21].

All $B_i \mu_j$ combinations except $B_2 \mu_3$ and $B_3 \mu_2$ can give contributions to the Higgs decay only from the type 2 no. 4 diagram. Again light charged scalars are preferred for the case. However, these contributions (from the type 2 no. 4 diagram) cannot provide a significant branching ratio. Hence we have the uninterestingly tiny numbers as shown in Table III.

As for $B_2\mu_3$ and $B_3\mu_2$, both give contributions to the Higgs decay via many diagrams. Among them, the tree

TABLE II. $B_i B_i$ contributions to $Br(h^0 \rightarrow \mu^{\pm} \tau^{\pm})$.

RPV parameter combinations	Admissible Br within known experimental constraints
$ \begin{array}{r} B_1 B_2 \\ B_1 B_3 \\ B_2 B_2 \\ B_2 B_3 \\ B_3 B_3 \end{array} $	$\begin{array}{c} 4 \times 10^{-22} \\ 3 \times 10^{-22} \\ 9 \times 10^{-23} \\ 2 \times 10^{-11} \\ 8 \times 10^{-23} \end{array}$

PHYSICAL REVIEW D 87, 015025 (2013)

TABLE III. $B_i \mu_i$ contributions to $Br(h^0 \rightarrow \mu \bar{\tau} + \tau \bar{\mu})$.

RPV parameter combinations	Admissible Br within know experimental constraints	
$\overline{B_1\mu_2}$	1×10^{-24}	
$B_1\mu_3$	$1 imes 10^{-24}$	
$B_2\mu_1$	9×10^{-23}	
$B_2\mu_2$	$4 imes 10^{-26}$	
$B_2\mu_3$	1×10^{-15}	
$B_3\mu_1$	$8 imes 10^{-23}$	
$B_3\mu_2$	1×10^{-13}	
$B_3\mu_3$	4×10^{-26}	

diagram (Fig. 1, left panel) is the most important over a wide range of parameter space. Especially for the $B_3\mu_2$ combination, a key contribution to the decay amplitude is enhanced by the tau Yukawa coupling y_{e_3} via a term

$$\approx y_{e_3} M_2^* B_3 \mu_2^* (\tan\beta \sin\alpha - \cos\alpha) / \left[\sqrt{2g_2(\mu_0 M_2)} - M_W^2 \sin 2\beta \right] M_s^2 \right]$$

 $(M_s^2$ denotes a generic real scalar mass eigenvalue). The latter makes the branching ratio from $B_3\mu_2$ the largest among all $B_i\mu_j$'s. There is a similar feature for the contributions from the $B_2\mu_3$ combination, but with a muon Yukawa y_{e_2} instead. These two combinations get their most significant values under small μ_0 and M_s^2 as can be seen from the expression above. Note that the contribution from loop diagrams is in general roughly smaller than that from the tree diagram, but can still be sizeable.

In fact, analyses similar to the above can be applied to $h^0 \rightarrow e^{\mp} \mu^{\pm}$ and $h^0 \rightarrow e^{\mp} \tau^{\pm}$ as well. The $B_i \mu_j$ contributions to $h^0 \rightarrow e^{\mp} \mu^{\pm}$ are expected to be tiny due to the smallness of the corresponding Yukawa couplings y_{e_1} and y_{e_2} . On the other hand, while the contributions from $B_1 \mu_3$ are also suppressed by a relative factor of y_{e_1}/y_{e_2} , the contributions from $B_3 \mu_1$ to $h^0 \rightarrow e^{\mp} \tau^{\pm}$ could be roughly the same order as that of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$. Hence, the $h^0 \rightarrow e^{\mp} \tau^{\pm}$ decay may also be of interest.

C. Contribution from $B_i \lambda$ combinations

Apart from the constraint on the B_i parameters, the λ type parameters are bounded by charged current experiments [30]. Generally speaking, increasing soft SUSY breaking slepton masses and gaugino masses leads to heavier charged slepton, sneutrino and neutralino masses and hence raises the upper bounds for B_i and λ .

Among all the $B_i\lambda$ combinations, $B_1\lambda_{123}$, $B_1\lambda_{132}$, $B_2\lambda_{232}$ and $B_3\lambda_{233}$ are most important. They can provide large amplitudes via tree level diagrams (Fig. 1, middle panel), which are roughly 1 order of magnitude larger than that from loop diagrams. The amplitude can be approximated by $\mathcal{M} \approx B_i\lambda(\tan\beta\sin\alpha - \cos\alpha)/(\sqrt{2}M_s^2)$, where α is the mixing angle between two *CP*-even neutral Higgs

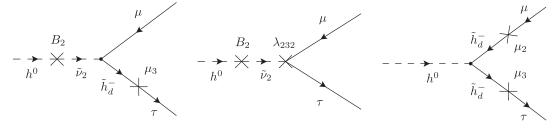


FIG. 1. Left panel: An example of $B_2\mu_3$ contribution to $h^0 \to \tau^-\mu^+$ via tree diagram. The Higgsino \tilde{h}_d^- transforms into charged lepton τ via RPV parameter μ_3 , while the light Higgs transforms into sneutrino $\tilde{\nu}_2$ via B_2 . Middle panel: An example of $B_2\lambda_{232}$ contribution to $h^0 \to \tau^-\mu^+$ via tree diagram. The light Higgs transforms into sneutrino $\tilde{\nu}_2$ via RPV parameter B_2 and then couples to μ and τ via trilinear RPV parameter λ_{232} . Right panel: An example of $\mu_2\mu_3$ contribution to $h^0 \to \tau^-\mu^+$ via tree diagram. The Higgs ino \tilde{h}_d^- mixes with charged leptons μ and τ via RPV parameters μ_2 and μ_3 separately.

bosons. Even though heavy sneutrino masses tend to suppress the amplitudes, they would relax the bounds on B_i and λ more significantly, and hence are favorable (Fig. 2, left panel). Moreover, μ_0 should not be too small in order to make the product of B_i and λ be below the bounds from leptonic radiative decays, i.e., $|B_1^*\lambda_{132}|$, $|B_1\lambda_{123}^*|$, $|B_2^*\lambda_{232}|$ and $|B_3\lambda_{233}^*| \leq 1.4 \times 10^{-3} |\mu_0|^2$ [21]. It is noteworthy that even under the stringent neutrino mass ≤ 1 eV constraint, the four combinations could give branching ratios beyond 10^{-5} (Fig. 2, right panel), which may be large enough to be probed at the LHC (or future linear collider). As to other $B_i\lambda$ combinations, they can be from several diagrams. However, they only play minor roles and hardly give any meaningful branching ratio, as shown in Table IV.

As a matter of fact, the class of $B_i\lambda$ combinations gives the most important contributions to the flavor violating Higgs decays among all RPV parameter combinations. Moreover, the approximation of tree level amplitudes as above could apply to $h^0 \rightarrow e^{\mp} \tau^{\pm}$ and $h^0 \rightarrow e^{\mp} \mu^{\pm}$ as well. As a result, under the same parameter setting, it is expected for $h^0 \rightarrow e^{\mp} \tau^{\pm}$ and $h^0 \rightarrow e^{\mp} \tau^{\pm}$ to give branching ratios with roughly the same order of magnitude as in $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$. However, it has been pointed out [33] that the LFV effective coupling between a light Higgs boson, electron and muon could not be large because of the constraint set by two-loop Barr-Zee diagrams [34] on $\mu \rightarrow e\gamma$. Therefore, only $h^0 \rightarrow e^{\mp} \tau^{\pm}$ is expected to give a branching ratio comparable to that of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$.

D. Contribution from $B_i A^{\lambda}$ combinations

Under our parametrization, A^{λ} 's do not contribute to radiative decays such as $b \rightarrow s\gamma$ in one-loop level [21]. Therefore, A^{λ} 's do not have known experimental constraints and, naively, can take any value. But the B_i parameters are limited by loop neutrino masses as before. Contributions from $B_i A^{\lambda}$ may be quite interesting since this will be like the first experimental signature of the RPV A parameters. However, an A^{λ} only plays its role in the

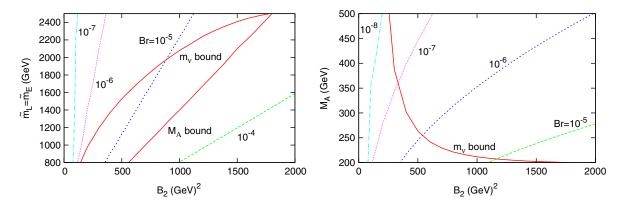


FIG. 2 (color online). Left panel: Branching ratio from $B_2\lambda_{232}$, with $M_2 = 2500$ GeV, $\mu_0 = 1800$ GeV $= A_u = -A_d$, $\tan\beta = 60$. λ_{232} is set to be the maximum dependent on the values of B_2 and $\tilde{m}_L^2 = \tilde{m}_E^2$. The solid red line (m_ν bound) comes from demanding that the 22 element of the neutrino mass matrix <1 eV, while the right-hand side of the M_A bound line is the area with *CP*-odd neutral Higgs mass $M_A < 200$ GeV. Right panel: Branching ratio from $B_2\lambda_{232}$, with $M_2 = 2500$ GeV, $\tilde{m}_{Lii}^2 = \tilde{m}_{Eii}^2 = (2500 \text{ GeV})^2$, $\mu_0 = 1800$ GeV = $A_u = -A_d$, $\tan\beta = 60$, $\lambda_{232} = 1.7488$. The solid red line (m_ν bound) comes from demanding that the 22 element of the neutrino mass matrix <1 eV.

RPV parameter combinations	Admissible Br within known experimental constraints	
$\overline{B_1\lambda_{123}}$	1×10^{-5}	
$\frac{B_1 \lambda_{123}}{B_1 \lambda_{132}}$	3×10^{-5}	
$B_1\lambda_{232}$	4×10^{-22}	
$\frac{B_1 \lambda_{232}}{B_1 \lambda_{233}}$	5×10^{-25}	
$B_2\lambda_{123}$	7×10^{-23}	
$B_2\lambda_{131}$	$9 imes 10^{-24}$	
$B_2\lambda_{132}$	$5 imes 10^{-22}$	
$B_2\lambda_{232}$	3×10^{-5}	
$B_2\lambda_{233}$	$7 imes 10^{-23}$	
$B_3\lambda_{121}$	$5 imes 10^{-24}$	
$B_3\lambda_{123}$	$7 imes 10^{-23}$	
$B_3\lambda_{132}$	$5 imes 10^{-22}$	
$B_3\lambda_{232}$	$5 imes 10^{-22}$	
$B_3\lambda_{233}$	3×10^{-5}	

TABLE IV. $B_i \lambda$ contributions to $Br(h^0 \rightarrow \mu^{\pm} \tau^{\pm})$.

Higgs decay through the type 2 no. 4 diagram with a neutral scalar-charged scalar-charged scalar $(h^0\phi^+\phi^-)$ coupling. It is then expected to give a larger contribution at low charged scalar mass (Fig. 3, left panel).

In our parameter setting, branching ratios from $B_i A^{\lambda}$ combinations can reach the order of 10^{-11} at most as shown in Table V. However, if we allow A^{λ} to be larger than hundreds of TeV, notable branching ratios are possible. Since decay rate is proportional to amplitude squared and hence A^{λ} squared, it is easy to see how the branching ratio changes as A^{λ} increases. As an example, we illustrate in Fig. 3 (both left and right panels) the branching ratio from the $B_2 A_{232}^{\lambda}$ contribution for $A_{232}^{\lambda} = 2500$ GeV and 2500 TeV. In the extreme case of $A_{232}^{\lambda} = 2500$ TeV, the branching ratio could reach the order of 10^{-5} .

E. Contribution from $\mu_i \lambda$ combinations

All $\mu_i \lambda$ combinations which can contribute to $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ at one-loop level, except $\mu_1 \lambda_{123}$ and $\mu_1 \lambda_{132}$, are constrained by their loop contributions to neutrino masses [32]. Again, a single μ_i is constrained by its contribution to the tree level neutrino mass. Leptonic radiative decays also give upper bounds on $\mu_i \lambda$, i.e., $|\mu_2^* \lambda_{232}|$, $|\mu_1^* \lambda_{132}|$, $|\mu_3 \lambda_{233}^*|$ and $|\mu_1 \lambda_{123}^*| \lesssim 7.0 \times 10^{-4} |\mu_0|$ [21]. Further bounds for single λ by charged current experiments can be found in Ref. [30].

Many diagrams contribute to the $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ process via $\mu_i \lambda$ combinations. Among these, type 1 no. 3 and type 1 no. 4 diagrams play the most important roles. The requirement of neutrino mass $\leq 1 \text{ eV}$ still sets the most stringent bounds as in the case of other type combinations. However, $\mu_1 \lambda_{123}$ and $\mu_1 \lambda_{132}$ do not give loop contribution to neutrino masses, and thus they are mainly bounded by the constraints from radiative leptonic decays. Generally speaking, large slepton masses are favorable in order to have larger branching ratios since they can relax the constraints from loop neutrino masses and raise the upper bounds on the λ 's.

In any case, branching ratios from $\mu_i \lambda$ can only achieve at most the order of 10^{-8} in our analysis because of the stringent constraints from leptonic decays. Our results are shown in Table VI.

F. Contribution from the other insignificant combinations

In addition to the above combinations, there are some other types of combinations (i.e., $B_i\lambda'$, $\mu_i\mu_j$, $\mu_i\lambda'$, $\lambda\lambda$ and $\lambda'\lambda'$) which can merely give negligible contributions. Hence we only list the combinations which are most illustrative or give the largest branching ratios in each type of combination, as shown in Table VII. Note that the types of

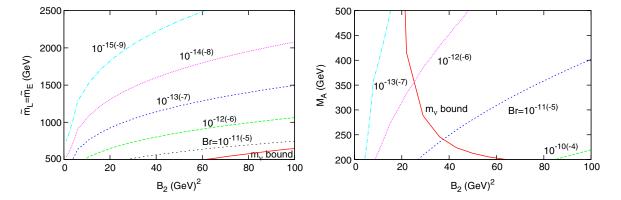


FIG. 3 (color online). Left panel: Branching ratio from $B_2 A_{232}^{\lambda}$, with $M_2 = 2500 \text{ GeV}$, $M_A \approx 200 \text{ to } 202 \text{ GeV}$, $\mu_0 = 1800 \text{ GeV} = A_u = -A_d$, $\tan\beta = 60$, $A_{232}^{\lambda} = 2500 \text{ GeV}(2500 \text{ TeV})$. The solid red line $(m_\nu \text{ bound})$ comes from demanding that the 22 element of the neutrino mass matrix <1 eV. Right panel: Branching ratio from $B_2 A_{232}^{\lambda}$, with $M_2 = 2500 \text{ GeV}$, $\tilde{m}_{Lii}^2 = \tilde{m}_{Eii}^2 = (500 \text{ GeV})^2$, $\mu_0 = 1800 \text{ GeV} = A_u = -A_d$, $\tan\beta = 60$, $A_{232}^{\lambda} = 2500 \text{ GeV}(2500 \text{ TeV})$. Solid red line $(m_\nu \text{ bound})$ comes from demanding that the 22 element of the neutrino mass matrix <1 eV. Right panel: Branching ratio from $B_2 A_{232}^{\lambda}$, with $M_2 = 2500 \text{ GeV}$, $\tilde{m}_{Lii}^2 = \tilde{m}_{Eii}^2 = (500 \text{ GeV})^2$, $\mu_0 = 1800 \text{ GeV} = A_u = -A_d$, $\tan\beta = 60$, $A_{232}^{\lambda} = 2500 \text{ GeV}(2500 \text{ TeV})$. Solid red line $(m_\nu \text{ bound})$ comes from demanding that the 22 element of the neutrino mass matrix <1 eV.

COMPREHENSIVE ANALYSIS ON LEPTON FLAVOR ...

TABLE V.	$B_i A^{\lambda}$	contributions 1	to E	$\operatorname{Br}(h^0 \rightarrow$	$\mu^{\mp} au^{\pm}$).
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RPV parameter combinations	Admissible Br within known experimental constraints	
$B_1 A_{123}^{\lambda}$	5×10^{-11}	
$B_1 A_{123}^{\lambda} \ B_1 A_{132}^{\lambda}$	5×10^{-11}	
$B_2 A_{232}^{\lambda} B_3 A_{233}^{\lambda}$	5×10^{-11}	
$B_3 A_{233}^{\overline{\lambda}}$	5×10^{-11}	

combinations which are not mentioned, $\lambda''\lambda''$ for example, give zero contributions at one-loop level.

In the $B_i \lambda'$ combinations, besides the constraints mentioned before on B_i , λ' also gets constrained by charged/neutral current experiments [30,35]. $B_i \lambda'$ combinations contribute to $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ mainly via no. 1 and no. 2 diagrams of types 6 and 7 (in Appendix A). To get better branching ratios, it is advantageous if we raise the upper bounds on B_i by the heavy sneutrino and neutralino masses. Heavy squark masses could also raise the upper bounds on λ' . However, in our computation, contributions from $B_i \lambda'$ cannot provide sizable branching ratios.

As to $\mu_i \mu_j$ combinations, only $\mu_2 \mu_3$ contributes to $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ up to the one-loop level. With nonzero μ_i , one of the neutrinos gets tree level mass. However, leptonic radiative decays set more stringent bounds on $\mu_2 \mu_3$ than the neutrino mass does [29], i.e.,

$$\frac{|\mu_2 \mu_3|}{\mu_0 M_2 - M_W^2 \sin 2\beta} \lesssim 4.3 \times 10^{-3} (1 + \tan^2 \beta) \times \frac{\mu_0 M_2 - M_W^2 \sin 2\beta}{M_W^2}.$$

Interestingly enough, though the $\mu_2\mu_3$ combination contributes to the decay in tree level (Fig. 1, right panel), a loop contribution from the type 1 no. 4 diagram is generally more important due to the smallness of neutrino masses in the loop. For example, where $\mu_2\mu_3$ gives its most significant branching ratio, the amplitude from loop diagrams compared to that from tree diagram is roughly 10000:1. At any rate, $\mu_2\mu_3$ could only give a negligible branching ratio.

TABLE VI. $\mu_i \lambda$ contributions to Br $(h^0 \rightarrow \mu^{\pm} \tau^{\pm})$.

RPV parameter combinations	Admissible Br within known experimental constraints	
$ \frac{\mu_1 \lambda_{123}}{\mu_1 \lambda_{132}} \\ \mu_2 \lambda_{232} \\ \mu_2 \lambda_{131} \\ \mu_3 \lambda_{233} \\ \mu_3 \lambda_{121} $	$5 \times 10^{-8} 5 \times 10^{-8} 3 \times 10^{-12} 2 \times 10^{-24} 1 \times 10^{-14} 1 \times 10^{-24}$	

TABLE VII. Most interesting examples in other RPV combinations.

RPV parameter combinations	Admissible Br within known experimental constraints
$\overline{B_2 \lambda'_{333}}$	1×10^{-14}
$B_3\lambda'_{233}$	1×10^{-15}
$\mu_{2}\mu_{3}$	$2 imes 10^{-18}$
$\mu_2 \lambda'_{323}$	3×10^{-18}
$\mu_3 \lambda'_{223}$	$5 imes 10^{-19}$
$\lambda_{232}\lambda_{233}$	$2 imes 10^{-19}$
$\lambda_{121}\lambda_{131}$	1×10^{-15}
$\lambda_{123}\lambda_{133}$	$2 imes 10^{-10}$
$\lambda'_{211}\lambda'_{311}$	$7 imes 10^{-18}$
$\lambda'_{222}\lambda'_{322}$	$4 imes 10^{-22}$
$\lambda_{223}^{\prime}\lambda_{323}^{\prime}$	$4 imes 10^{-12}$
$\lambda'_{233}\lambda'_{333}$	$5 imes 10^{-26}$

Among all $\mu_i \lambda'$'s which give nonzero contributions, some combinations are constrained by their loop contributions to neutrino masses [32]. Besides, every $\mu_i \lambda'$ is bounded by tree level neutrino mass constraints on μ_i and experimental constraints on single λ' [30,35]. In this type of combination, there is no obvious dominant diagram. Several diagrams can give comparable major contributions to the $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ process. Generally speaking, heavy gaugino masses can relax the tree level neutrino mass constraints while heavy down squark masses can raise the upper bounds of λ' and relax loop neutrino mass constraints; hence they are favorable for larger branching ratios. Unfortunately, in the whole parameter space, it is hard for the $\mu_i \lambda'$ to give any significant branching ratios.

Contributions from $\lambda\lambda$ combinations are mainly from the nos. 3 and 4 diagrams of types 2, 6, and 7. Among all $\lambda\lambda$ combinations which contribute to $h^0 \rightarrow \mu^{\pm} \tau^{\pm}$, only $\lambda_{232}\lambda_{233}$ and $\lambda_{121}\lambda_{131}$ are constrained by their loop contributions to neutrino masses [32]. However, leptonic decays could also provide upper bounds for $\lambda\lambda$ combinations [21,30,36]. Specifically, the neutrino mass constraint on $\lambda_{121}\lambda_{131}$ contains a factor of electron mass, and hence is relaxed by the smallness of electron mass. Therefore the branching ratio from $\lambda_{121}\lambda_{131}$ is mainly limited by restriction from leptonic decays. On the other hand, the neutrino mass constraint on $\lambda_{232}\lambda_{233}$ is enhanced by a τ mass factor. The latter gives a major restriction on the branching ratio from $\lambda_{232}\lambda_{233}$. The most significant branching ratio from $\lambda\lambda$ we can have is of the order 10^{-10} .

Many diagrams can contribute to the Higgs decay via $\lambda'\lambda'$ combinations. Among these, type 1 no. 2 and type 2 no. 1 diagrams are the most important ones. Just like the $\lambda\lambda$ case, among all $\lambda'\lambda'$ combinations which contribute to $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$, only $\lambda'_{211}\lambda'_{311}$, $\lambda'_{222}\lambda'_{322}$, and $\lambda'_{233}\lambda'_{333}$ as listed contribute to neutrino masses [32] and hence get

TABLE VIII. Interesting contributions to the branching ratio of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$.

RPV parameter combinations	Admissible Br within known experimental constraints	
$ \begin{array}{r} B_1 \lambda_{123} \\ B_1 \lambda_{132} \\ B_2 \lambda_{232} \\ B_3 \lambda_{233} \\ B_2 A_{232}^{\lambda} \\ B_3 A_{233}^{\lambda} \end{array} $	$ \begin{array}{r} 1 \times 10^{-5} \\ 3 \times 10^{-5} \\ 3 \times 10^{-5} \\ 3 \times 10^{-5} \\ 5 \times 10^{-11(-5)} \\ 5 \times 10^{-11(-5)} \end{array} $	

additional constraints. Besides, radiative *B* decays and leptonic decays also give upper bounds on $\lambda'\lambda'$ [30,36–38]. Particularly, constraints on $\lambda'_{211}\lambda'_{311}$, $\lambda'_{222}\lambda'_{322}$, and $\lambda'_{233}\lambda'_{333}$ are suppressed/enhanced separately by the electron, muon, and tau mass factors. This makes the differences between their branching ratios. Nevertheless, $\lambda'\lambda'$ type of combination could only give negligible contributions to $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$.

IV. SUMMARY

We have analyzed thoroughly Higgs to $\mu^{\pm}\tau^{\pm}$ decay in the framework of the minimal supersymmetric standard model without R parity. By means of full one-loop diagrammatic calculations and taking the RPV terms as the only source of lepton flavor violation, we showed that the branching ratio of $h^0 \rightarrow \mu^{\mp} \tau^{\pm}$ could exceed 10^{-5} without contradicting experimental constraints. We pull together the most interesting RPV parameter combinations and corresponding branching ratios in Table VIII for easy reference. The numbers in the parentheses indicate the branching ratios in the case of $A^{\lambda} = 2500 \text{ TeV}$ as mentioned in the $B_i A^{\lambda}$ section. Moreover, $h^0 \rightarrow e^{\pm} \tau^{\pm}$ is expected to be able to give roughly the same order of branching ratio with that of $h^0 \to \mu^{\pm} \tau^{\pm}$ from RPV terms, while $h^0 \to e^{\pm} \tau^{\pm}$ is suppressed due to stringent constraint from two-loop Barr-Zee diagrams.

Generally speaking, a heavy SUSY spectrum is preferred for large branching ratios of LFV Higgs decays obtainable from RPV couplings. The resulting relaxations of the experimental constraints from other processes and especially neutrino masses on the couplings leave more room for the Higgs decay. However, the statement may not hold for the contributions involving the A^{λ} parameters. In the extreme case that such a parameter is larger than around hundreds of TeV, notable branching ratios are possible, especially with relatively light slepton masses (below 1 TeV). Meanwhile, a smaller value of the Higgs mass parameter M_A is favored in the LFV Higgs decays of the RPV scenario.

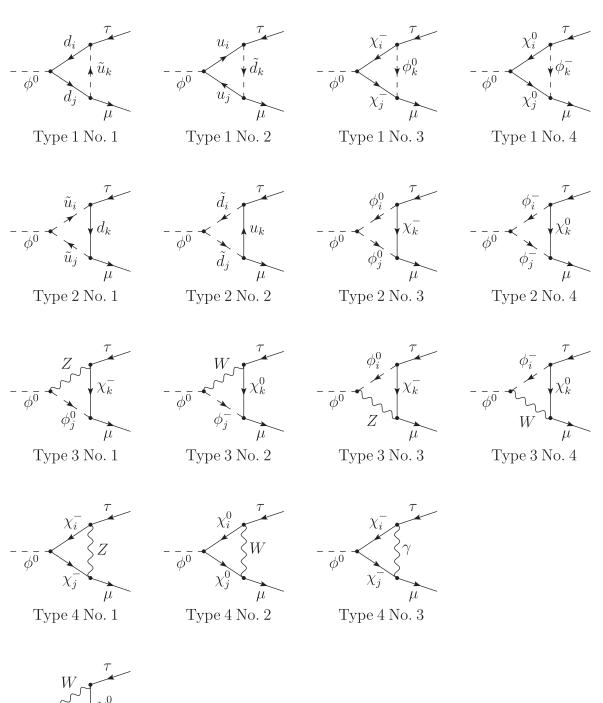
From an experimental point of view, a typical cross section of the MSSM 125 GeV Higgs boson at 8 TeV energy is of the order 10 pb. Short of a reliable full simulation study, we can only carry out a rough estimate on the observability of the Br($h^0 \rightarrow \mu^{\mp} \tau^{\pm}$) $\geq 10^{-5}$. With a luminosity of the order 10 fb⁻¹, this would lead to several raw $\mu^{\mp} \tau^{\pm}$ events with almost no SM background.⁵ If we allow more free parameters or a larger parameter space during our analysis, the branching ratios can become even larger. Together with the 14 TeV energy for future LHC runs, we may have more events and a better chance to probe lepton flavor violation, and physics beyond the standard model.

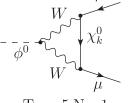
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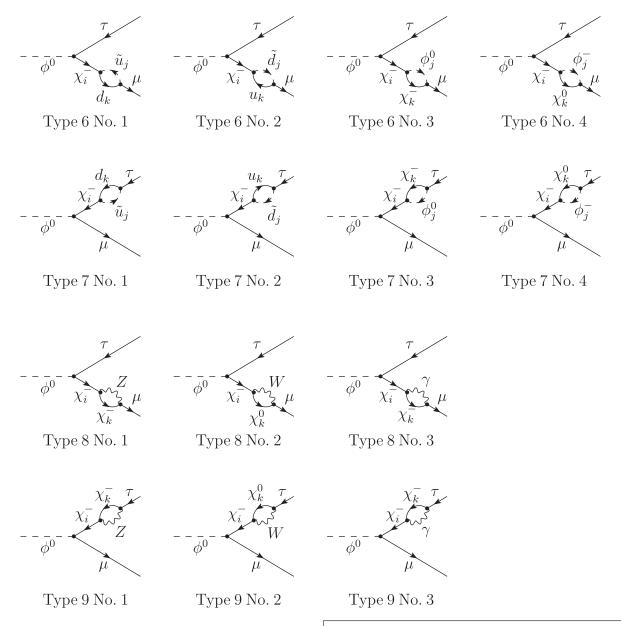
⁵Our estimate is likely to be on the optimistic side when detector properties are fully taken into consideration. Some complete experimental analyses with realistic cuts may be needed to improve the situation. The case for the 14 TeV running or a future linear collider will be much better. We also want to bring to the reader's attention that after we finished our work, a preprint [39] on the relevant branching ratio reach of the 8 TeV LHC appeared, claiming a quite disappointing number.

APPENDIX A: ONE-LOOP FEYNMAN DIAGRAMS IN MSSM WITHOUT *R* PARITY FOR THE NEUTRAL HIGGS $\phi^0 \rightarrow \mu^- \tau^+$





Type 5 No. 1 $\,$



APPENDIX B: EFFECTIVE COUPLINGS IN MSSM WITHOUT *R* PARITY

We list all relevant effective mass eigenstate couplings for our analysis here. Indices run from 1 to 10 for neutral scalars (sleptons), 1 to 8 for charged scalars (sleptons), 1 to 6 for squarks, 1 to 7 for neutral fermions (neutralinos) and 1 to 5 for charged fermions (charginos) while all dummy indices run from 1 to 3. Moreover,

$$y_{u_i} = \frac{g_2 m_{u_i}}{\sqrt{2}M_W \sin\beta}, \qquad y_{d_i} = \frac{g_2 m_{d_i}}{\sqrt{2}M_W \cos\beta},$$

and
$$y_{e_i} = \frac{g_2 m_i}{\sqrt{2}M_W \cos\beta}$$

are the diagonal quark and charged lepton Yukawa couplings, where m_i 's ($\approx m_{e_i}$ under the small- μ_i scenario) are mass parameters in the charged fermion mass matrix [23].

Neutral scalar (sneutrino)- W^+ - W^- vertices

$$\mathcal{L} = g_m^W W^+ W^- \phi_m^0,$$

where

$$g_m^W = g_2 M_W (\sin\beta \mathcal{D}_{1m}^s + \cos\beta \mathcal{D}_{2m}^s).$$
(B1)

Neutral scalar-charged scalar (slepton)-W vertices

$$\mathcal{L} = \mathcal{G}_{mn}^{W}[p(\phi_{n}^{-}) - p(\phi_{m}^{0})]_{\mu}W^{+}\phi_{n}^{-}\phi_{m}^{0} + \text{H.c.},$$

$$G_{mn}^{W} = \frac{1}{2} g_2 [(\mathcal{D}_{1m}^s - i\mathcal{D}_{6m}^s)\mathcal{D}_{1n}^l - (\mathcal{D}_{2m}^s - i\mathcal{D}_{7m}^s)\mathcal{D}_{2n}^l - (\mathcal{D}_{(p+2)m}^s - i\mathcal{D}_{(p+7)m}^s)\mathcal{D}_{(p+2)n}^l].$$
(B2)

COMPREHENSIVE ANALYSIS ON LEPTON FLAVOR ...

Neutral scalar-neutral scalar-Z vertices

$$\mathcal{L} = \mathcal{G}_{ij}^Z [p(\phi_j^0) - p(\phi_i^0)]_{\mu} Z \phi_i^0 \phi_j^0,$$

where

$$G_{ij}^{Z} = \frac{i}{2} g_{Z} (\mathcal{D}_{6i}^{s} \mathcal{D}_{1j}^{s} - \mathcal{D}_{1i}^{s} \mathcal{D}_{6j}^{s} + \mathcal{D}_{7i}^{s} \mathcal{D}_{2j}^{s} - \mathcal{D}_{2i}^{s} \mathcal{D}_{7j}^{s} + \mathcal{D}_{(q+7)i}^{s} \mathcal{D}_{(q+2)j}^{s} - \mathcal{D}_{(q+2)i}^{s} \mathcal{D}_{(q+7)j}^{s}).$$
(B3)

Neutral lepton (neutralino)-charged lepton (chargino)-W vertices

$$\begin{split} \mathcal{L} &= g_2 \bar{\Psi}(\chi_m^0) \Phi^{\dagger}(W^-) \bigg[\mathcal{N}_{mi}^{wL} \gamma_{\mu} \frac{1 - \gamma_5}{2} \\ &+ \mathcal{N}_{mi}^{wR} \gamma_{\mu} \frac{1 + \gamma_5}{2} \bigg] \Psi(\chi_i^-) + \text{H.c.}, \end{split}$$

where

$$\mathcal{N}_{mi}^{wL} = -X_{2m}^* U_{1i} - \frac{1}{\sqrt{2}} X_{4m}^* U_{2i} - \frac{1}{\sqrt{2}} X_{(q+4)m}^* U_{(q+2)i}$$
$$\mathcal{N}_{mi}^{wR} = V_{1i} X_{2m} + \frac{1}{\sqrt{2}} V_{2i} X_{3m}^*.$$
(B4)

Charged lepton-charged lepton-Z vertices

$$\mathcal{L} = g_Z \bar{\Psi}(\chi_i^-) \left[\mathcal{C}_{ij}^{zL} \gamma_\mu \frac{1 - \gamma_5}{2} + \mathcal{C}_{ij}^{zR} \gamma_\mu \frac{1 + \gamma_5}{2} \right] \Phi(Z) \Psi(\chi_j^-),$$

where

$$C_{ij}^{zL} = -(-1 + \sin^2 \theta_W) U_{1i}^* U_{1j} - \left(-\frac{1}{2} + \sin^2 \theta_W\right) U_{2i}^* U_{2j}$$
$$- \left(-\frac{1}{2} + \sin^2 \theta_W\right) U_{(q+2)i}^* U_{(q+2)j}$$
$$C_{ij}^{zR} = (1 - \sin^2 \theta_W) V_{1j} V_{1i}^* + \left(\frac{1}{2} - \sin^2 \theta_W\right) V_{2j} V_{2i}^*$$
$$- \sin^2 \theta_W V_{(q+2)j} V_{(q+2)i}^*.$$
(B5)

Charged lepton-charged lepton- γ vertices

$$\begin{split} \mathcal{L} &= e \bar{\Psi}(\chi_i^-) \bigg[\mathcal{C}_{ij}^{\gamma L} \gamma_\mu \frac{1 - \gamma_5}{2} \\ &+ \mathcal{C}_{ij}^{\gamma R} \gamma_\mu \frac{1 + \gamma_5}{2} \bigg] \Phi(A^\mu) \Psi(\chi_j^-), \end{split}$$

where

$$C_{ij}^{\gamma L} = U_{1i}^* U_{1j} + U_{2i}^* U_{2j} + U_{(q+2)i}^* U_{(q+2)j}$$

$$C_{ij}^{\gamma R} = V_{1j} V_{1i}^* + V_{2j} V_{2i}^* + V_{(q+2)j} V_{(q+2)i}^*.$$
(B6)

Charged lepton-down quark-up squark vertices

$$\mathcal{L}^{\chi^{-}} = g_2 \bar{\Psi}(\chi_n^{-}) \Phi^{\dagger}(\tilde{u}_m) \bigg[\mathcal{C}^{dL}_{nmi} \frac{1 - \gamma_5}{2} + \mathcal{C}^{dR}_{nmi} \frac{1 + \gamma_5}{2} \bigg] \Psi(d_i) + \text{H.c.},$$

where

$$\mathcal{C}_{nmi}^{dL} = -V_{1n}^* \mathcal{D}_{im}^{u*} + \frac{y_{u_j}}{g_2} V_{CKM}^{ji} V_{2n}^* \mathcal{D}_{(j+3)m}^{u*}$$

$$\mathcal{C}_{nmi}^{dR} = \frac{y_{d_i}}{g_2} U_{2n}^* \mathcal{D}_{im}^{u*} + \frac{\lambda_{jhi}^{\prime*}}{g_2} U_{(j+2)n}^* \mathcal{D}_{hm}^{u*}.$$
(B7)

Neutral scalar-quark-quark vertices: Down sector

$$\begin{split} \mathcal{L}^{\phi^0} &= g_2 \bar{\Psi}(d_h) \Phi^{\dagger}(\phi_m^0) \bigg[\tilde{\mathcal{N}}_{hmi}^{dL} \frac{1 - \gamma_5}{2} \\ &+ \tilde{\mathcal{N}}_{hmi}^{dR} \frac{1 + \gamma_5}{2} \bigg] \Psi(d_i), \end{split}$$

where

$$\tilde{\mathcal{N}}_{hmi}^{dL} = -\frac{y_{d_i}}{\sqrt{2}g_2} \delta_{ih} (\mathcal{D}_{2m}^s + i\mathcal{D}_{7m}^s) -\frac{\lambda'_{kih}}{\sqrt{2}g_2} (\mathcal{D}_{(k+2)m}^s + i\mathcal{D}_{(k+7)m}^s) \tilde{\mathcal{N}}_{hmi}^{dR} = -\frac{y_{d_i}}{\sqrt{2}g_2} \delta_{ih} (\mathcal{D}_{2m}^s - i\mathcal{D}_{7m}^s) -\frac{\lambda'_{khi}}{\sqrt{2}g_2} (\mathcal{D}_{(k+2)m}^s - i\mathcal{D}_{(k+7)m}^s).$$
(B8)

Neutral scalar-quark-quark vertices: Up sector

$$\begin{split} \mathcal{L}^{u} &= g_{2} \bar{\Psi}(u_{h}) \Phi^{\dagger}(\phi_{m}^{0}) \bigg[\tilde{\mathcal{N}}_{hmi}^{uL} \frac{1 - \gamma_{5}}{2} \\ &+ \tilde{\mathcal{N}}_{hmi}^{uR} \frac{1 + \gamma_{5}}{2} \bigg] \Psi(u_{i}), \end{split}$$

where

$$\tilde{\mathcal{N}}_{hmi}^{uL} = -\frac{y_{u_i}}{\sqrt{2g_2}} \delta_{ih} (\mathcal{D}_{1m}^s - i\mathcal{D}_{6m}^s)$$

$$\tilde{\mathcal{N}}_{hmi}^{uR} = -\frac{y_{u_i}}{\sqrt{2g_2}} \delta_{ih} (\mathcal{D}_{1m}^s + i\mathcal{D}_{6m}^s).$$
(B9)

Charged lepton-up quark-down squark vertices

$$\mathcal{L}^{\chi^+} = g_2 \bar{\Psi}(\chi_n^+) \Phi^{\dagger}(\tilde{d}_m) \\ \times \left[\mathcal{C}_{nmi}^{uL} \frac{1-\gamma_5}{2} + \mathcal{C}_{nmi}^{uR} \frac{1+\gamma_5}{2} \right] \Psi(u_i) + \text{H.c.},$$

$$C_{nmi}^{uL} = -V_{CKM}^{ip*} U_{1n} \mathcal{D}_{pm}^{d*} + \frac{y_{d_p}}{g_2} V_{CKM}^{ip*} U_{2n} \mathcal{D}_{(p+3)m}^{d*} + \frac{\lambda'_{jhp}}{g_2} V_{CKM}^{ih*} U_{(j+2)n} \mathcal{D}_{(p+3)m}^{d*} C_{nmi}^{uR} = \frac{y_{u_i}}{g_2} V_{CKM}^{ip*} V_{2n} \mathcal{D}_{pm}^{d*}.$$
(B10)

ABDESSLAM ARHRIB, YIFAN CHENG, AND OTTO C. W. KONG

Neutral scalar-charged lepton-charged lepton vertices

$$\mathcal{L} = g_2 \bar{\Psi}(\chi_{\bar{n}}^-) \left[\mathcal{C}_{\bar{n}mn}^{\chi L} \frac{1-\gamma_5}{2} + \mathcal{C}_{\bar{n}mn}^{\chi R} \frac{1+\gamma_5}{2} \right] \Psi(\chi_n^-) \Phi(\phi_m^0),$$

where

$$\mathcal{C}_{\bar{n}mn}^{\chi L} = -\frac{1}{\sqrt{2}} V_{2\bar{n}}^* U_{1n} (\mathcal{D}_{1m}^s + i\mathcal{D}_{6m}^s) - \frac{1}{\sqrt{2}} V_{1\bar{n}}^* U_{2n} (\mathcal{D}_{2m}^s - i\mathcal{D}_{7m}^s) - \frac{1}{\sqrt{2}} V_{1\bar{n}}^* U_{(j+2)n} (\mathcal{D}_{(j+2)m}^s - i\mathcal{D}_{(j+7)m}^s) \\
- \frac{y_{e_j}}{\sqrt{2}g_2} V_{(j+2)\bar{n}}^* U_{(j+2)n} (\mathcal{D}_{2m}^s + i\mathcal{D}_{7m}^s) + \frac{y_{e_j}}{\sqrt{2}g_2} V_{(j+2)\bar{n}}^* U_{2n} (\mathcal{D}_{(j+2)m}^s + i\mathcal{D}_{(j+7)m}^s) \\
+ \frac{\lambda_{ijk}}{\sqrt{2}g_2} V_{(k+2)\bar{n}}^* U_{(i+2)n} (\mathcal{D}_{(j+2)m}^s + i\mathcal{D}_{(j+7)m}^s) \\
\mathcal{C}_{\bar{n}mn}^{\chi R} = -\frac{1}{\sqrt{2}} U_{1\bar{n}}^* V_{2n} (\mathcal{D}_{1m}^s - i\mathcal{D}_{6m}^s) - \frac{1}{\sqrt{2}} U_{2\bar{n}}^* V_{1n} (\mathcal{D}_{2m}^s + i\mathcal{D}_{7m}^s) - \frac{1}{\sqrt{2}} U_{(j+2)\bar{n}}^* V_{1n} (\mathcal{D}_{(j+2)m}^s + i\mathcal{D}_{(j+7)m}^s) \\
- \frac{y_{e_j}}{\sqrt{2}g_2} U_{(j+2)\bar{n}}^* V_{(j+2)n} (\mathcal{D}_{2m}^s - i\mathcal{D}_{7m}^s) + \frac{y_{e_j}}{\sqrt{2}g_2} U_{2\bar{n}}^* V_{(j+2)n} (\mathcal{D}_{(j+2)m}^s - i\mathcal{D}_{(j+7)m}^s) \\
+ \frac{\lambda_{ijk}^*}{\sqrt{2}g_2} U_{(i+2)\bar{n}}^* V_{(k+2)n} (\mathcal{D}_{(j+2)m}^s - i\mathcal{D}_{(j+7)m}^s).$$
(B11)

Neutral scalar-neutral lepton-neutral lepton vertices

$$\mathcal{L} = g_2 \bar{\Psi}(\chi_{\bar{n}}^0) \bigg[\mathcal{N}_{\bar{n}mn}^{\chi L} \frac{1-\gamma_5}{2} + \mathcal{N}_{\bar{n}mn}^{\chi R} \frac{1+\gamma_5}{2} \bigg] \Psi(\chi_n^0) \Phi(\phi_m^0),$$

where

$$\mathcal{N}_{\bar{n}mn}^{\chi L} = \frac{1}{2} (-\tan\theta_W X_{1\bar{n}} + X_{2\bar{n}}) X_{3n}^* (\mathcal{D}_{1m}^s + i\mathcal{D}_{6m}^s) + \frac{1}{2} (\tan\theta_W X_{1\bar{n}} - X_{2\bar{n}}) X_{4n} (\mathcal{D}_{2m}^s - i\mathcal{D}_{7m}^s) + \frac{1}{2} (\tan\theta_W X_{1\bar{n}} - X_{2\bar{n}}) X_{(k+4)n} (\mathcal{D}_{(k+2)m}^s - i\mathcal{D}_{(k+7)m}^s) \mathcal{N}_{\bar{n}mn}^{\chi R} = \frac{1}{2} X_{3\bar{n}} (-\tan\theta_W X_{1n}^* + X_{2n}^*) (\mathcal{D}_{1m}^s - i\mathcal{D}_{6m}^s) + \frac{1}{2} X_{4\bar{n}}^* (\tan\theta_W X_{1n}^* - X_{2n}^*) (\mathcal{D}_{2m}^s + i\mathcal{D}_{7m}^s) + \frac{1}{2} X_{(k+n)\bar{n}}^* (\tan\theta_W X_{1n}^* - X_{2n}^*) (\mathcal{D}_{(k+2)m}^s + i\mathcal{D}_{(k+7)m}^s).$$
(B12)

Charged scalar-neutral lepton-charged lepton vertices

$$\mathcal{L} = g_2 \bar{\Psi}(\chi_{\bar{n}}) \left[\tilde{\mathcal{C}}_{\bar{n}mn}^{\chi L} \frac{1-\gamma_5}{2} + \tilde{\mathcal{C}}_{\bar{n}mn}^{\chi R} \frac{1+\gamma_5}{2} \right] \Psi(\chi_n^0) \Phi(\phi_m^-) + \text{H.c.},$$

$$\tilde{\mathcal{C}}_{\bar{n}mn}^{\chi L} = -V_{1\bar{n}}^* X \mathcal{D}_{1m}^l + \frac{\sqrt{2}}{2} V_{2\bar{n}}^* (-\tan\theta_W X_{1n} - X_{2n}) \mathcal{D}_{1m}^l - \sqrt{2} \tan\theta_W V_{(j+2)\bar{n}}^* X_{1n} \mathcal{D}_{(j+5)m}^l \\ - \frac{y_{e_j}}{g_2} (V_{(j+2)\bar{n}}^* X_{4n} \mathcal{D}_{(j+2)m}^l - V_{(j+2)\bar{n}}^* X_{(j+4)n} \mathcal{D}_{2m}^l) - \frac{\lambda_{ijk}}{g_2} V_{(k+2)\bar{n}}^* X_{(i+4)n} \mathcal{D}_{(j+2)m}^l \\ \tilde{\mathcal{C}}_{\bar{n}mn}^{\chi R} = -U_{1\bar{n}}^* X_{4n}^* \mathcal{D}_{2m}^l - U_{1\bar{n}}^* X_{(k+4)n}^* \mathcal{D}_{(k+2)m}^l + \frac{\sqrt{2}}{2} U(\tan\theta_W X_{1n}^* + X_{2n}^*) \mathcal{D}_{2m}^l + \frac{\sqrt{2}}{2} U_{(k+2)\bar{n}}^* (\tan\theta_W X_{1n}^* + X_{2n}^*) \mathcal{D}_{(k+2)m}^l \\ - \frac{y_{e_k}}{g_2} (U_{(k+2)\bar{n}}^* X_{4n}^* \mathcal{D}_{(k+5)m}^l - U_{2\bar{n}}^* X_{(k+4)n}^* \mathcal{D}_{(k+5)m}^l) - \frac{\lambda_{ijk}^*}{g_2} U_{(j+2)\bar{n}}^* X_{(i+4)n}^* \mathcal{D}_{(k+5)m}^l.$$
(B13)

Neutral scalar-squark-squark vertices: Down sector

$$\mathcal{L} = \boldsymbol{g}_{abm}^d \Phi^{\dagger}(\tilde{d}_a) \Phi(\tilde{d}_b) \Phi(\boldsymbol{\phi}_m^0),$$

where

$$\begin{aligned} g_{abm}^{d} &= \frac{g_{2}M_{Z}}{\cos\theta_{W}} \Big(\frac{1}{2} - \frac{1}{3} \sin^{2}\theta_{W} \Big) (\cos\beta \mathcal{D}_{2m}^{s} - \sin\beta \mathcal{D}_{1m}^{s}) \mathcal{D}_{qa}^{d*} \mathcal{D}_{qb}^{d} + \frac{g_{2}M_{Z}}{\cos\theta_{W}} \Big(\frac{1}{3} \sin^{2}\theta_{W} \Big) (\cos\beta \mathcal{D}_{2m}^{s} - \sin\beta \mathcal{D}_{1m}^{s}) \mathcal{D}_{(q+3)a}^{d*} \mathcal{D}_{(q+3)b}^{d} \\ &- \sqrt{2} y_{d_{q}} m_{d_{q}} \mathcal{D}_{qa}^{d*} \mathcal{D}_{qb}^{d} \mathcal{D}_{2m}^{s} - \sqrt{2} y_{d_{q}} m_{d_{q}} \mathcal{D}_{(q+3)a}^{d*} \mathcal{D}_{(q+3)b}^{d} \mathcal{D}_{2m}^{s} + \frac{1}{\sqrt{2}} (\mu_{0}^{*} \delta_{pq} y_{d_{q}} + \mu_{i}^{*} \lambda_{ipq}^{i}) \mathcal{D}_{(q+3)a}^{d*} \mathcal{D}_{pb}^{d} (\mathcal{D}_{1m}^{s} + i \mathcal{D}_{6m}^{s}) \\ &+ \frac{1}{\sqrt{2}} (\mu_{0} \delta_{pq} y_{d_{q}} + \mu_{i} \lambda_{ipq}^{i}) \mathcal{D}_{pa}^{d*} \mathcal{D}_{(q+3)b}^{d} (\mathcal{D}_{1m}^{s} - i \mathcal{D}_{6m}^{s}) - \frac{1}{\sqrt{2}} A_{pq}^{D} \mathcal{D}_{(q+3)a}^{d} \mathcal{D}_{pb}^{d} (\mathcal{D}_{2m}^{s} + i \mathcal{D}_{7m}^{s}) \\ &- \frac{1}{\sqrt{2}} A_{pq}^{D*} \mathcal{D}_{pa}^{d*} \mathcal{D}_{(q+3)b}^{d} (\mathcal{D}_{2m}^{s} - i \mathcal{D}_{5m}^{s}) - \frac{1}{\sqrt{2}} A_{pq}^{\lambda_{ip}^{*}} \mathcal{D}_{(q+3)a}^{d*} \mathcal{D}_{pb}^{d} (\mathcal{D}_{2m}^{s} + i \mathcal{D}_{7m}^{s}) \\ &- \frac{1}{\sqrt{2}} A_{pq}^{D*} \mathcal{D}_{pa}^{d*} \mathcal{D}_{(q+3)b}^{d} (\mathcal{D}_{2m}^{s} - i \mathcal{D}_{7m}^{s}) - \frac{1}{\sqrt{2}} A_{jpq}^{\lambda_{ip}^{*}} \mathcal{D}_{(q+3)a}^{d} \mathcal{D}_{pb}^{d} (\mathcal{D}_{(j+2)m}^{s} + i \mathcal{D}_{7m}^{s}) \\ &- \frac{1}{\sqrt{2}} A_{jpq}^{\lambda_{ip}^{*}} \mathcal{D}_{pa}^{d} \mathcal{D}_{(q+3)b}^{d} (\mathcal{D}_{(j+2)m}^{s} - i \mathcal{D}_{7m}^{s}) - \frac{1}{\sqrt{2}} [m_{d_{p}}^{*} \lambda_{jpq}^{i} \mathcal{D}_{(p+3)a}^{d} \mathcal{D}_{(p+3)b}^{d} \mathcal{D}_{(q+3)a}^{d} + m_{d_{q}}^{*} \lambda_{ipq}^{i} \mathcal{D}_{qa}^{d*} \mathcal{D}_{qb}^{d} \right] \\ &\times (\mathcal{D}_{(i+2)m}^{s} + i \mathcal{D}_{(i+7)m}^{s}) - \frac{1}{\sqrt{2}} [m_{d_{p}}^{*} \lambda_{ipq}^{i} \mathcal{D}_{(q+3)b}^{d} + m_{d_{q}}^{*} \lambda_{ipq}^{i} \mathcal{D}_{qb}^{d} \mathcal{D}_{pa}^{d*}] (\mathcal{D}_{(i+2)m}^{s} - i \mathcal{D}_{(i+7)m}^{s}). \tag{B14}$$

Neutral scalar-squark-squark vertices: Up sector

$$\mathcal{L} = \boldsymbol{g}^{u}_{abm} \Phi^{\dagger}(\tilde{u}_{a}) \Phi(\tilde{u}_{b}) \Phi(\boldsymbol{\phi}^{0}_{m}),$$

where

$$\begin{aligned} \boldsymbol{g}_{abm}^{u} &= \frac{g_{2}M_{Z}}{\cos\theta_{W}} \left(-\frac{1}{2} + \frac{2}{3}\sin^{2}\theta_{W} \right) (\cos\beta\mathcal{D}_{2m}^{s} - \sin\beta\mathcal{D}_{1m}^{s}) \mathcal{D}_{qa}^{u*} \mathcal{D}_{qb}^{u} - \frac{g_{2}M_{Z}}{\cos\theta_{W}} \left(\frac{2}{3}\sin^{2}\theta_{W} \right) (\cos\beta\mathcal{D}_{2m}^{s} - \sin\beta\mathcal{D}_{1m}^{s}) \mathcal{D}_{(q+3)a}^{u*} \mathcal{D}_{(q+3)b}^{u} \\ &- \sqrt{2}y_{u_{l}}m_{u_{l}}V_{CKM}^{lp*}V_{CKM}^{lq} \mathcal{D}_{pa}^{u*} \mathcal{D}_{qb}^{u} \mathcal{D}_{1m}^{s} - \sqrt{2}y_{u_{q}}m_{u_{q}} \mathcal{D}_{(q+3)a}^{u*} \mathcal{D}_{(q+3)b}^{u} \mathcal{D}_{1m}^{s} + \frac{1}{\sqrt{2}}y_{u_{q}}V_{CKM}^{qp} [\mu_{0}^{*}(\mathcal{D}_{2m}^{s} - i\mathcal{D}_{7m}^{s}) \\ &+ \mu_{j}^{*}(\mathcal{D}_{(j+2)m}^{s} - i\mathcal{D}_{(j+7)m}^{s})]\mathcal{D}_{(q+3)a}^{u*} \mathcal{D}_{pb}^{u} + \frac{1}{\sqrt{2}}y_{u_{q}}V_{CKM}^{qp*} [\mu_{0}(\mathcal{D}_{2m}^{s} + i\mathcal{D}_{7m}^{s}) + \mu_{j}(\mathcal{D}_{(j+2)m}^{s} + i\mathcal{D}_{(j+7)m}^{s})]\mathcal{D}_{pa}^{u*} \mathcal{D}_{(q+3)b}^{u} \\ &- \frac{1}{\sqrt{2}}A_{pq}^{U}\mathcal{D}_{(q+3)a}^{u}\mathcal{D}_{pb}^{u}(\mathcal{D}_{1m}^{s} - i\mathcal{D}_{6m}^{s}) - \frac{1}{\sqrt{2}}A_{pq}^{U*}\mathcal{D}_{pa}^{u*}\mathcal{D}_{(q+3)b}^{u}(\mathcal{D}_{1m}^{s} + i\mathcal{D}_{6m}^{s}). \end{aligned}$$
(B15)

Cubic neutral scalar vertices

$$\mathcal{L} = \boldsymbol{g}^0_{abm} \Phi(\boldsymbol{\phi}^0_a) \Phi(\boldsymbol{\phi}^0_b) \Phi(\boldsymbol{\phi}^0_m),$$

where

$$\boldsymbol{g}_{abm}^{0} = \frac{g_2 M_Z}{4\cos\theta_W} (\cos\beta \mathcal{D}_{2m}^s - \sin\beta \mathcal{D}_{1m}^s) \times (\mathcal{D}_{1a}^s \mathcal{D}_{1b}^s + \mathcal{D}_{6a}^s \mathcal{D}_{6b}^s - \mathcal{D}_{2a}^s \mathcal{D}_{2b}^s - \mathcal{D}_{7a}^s \mathcal{D}_{7b}^s - \mathcal{D}_{(q+2)a}^s \mathcal{D}_{(q+2)b}^s - \mathcal{D}_{(q+7)a}^s \mathcal{D}_{(q+7)b}^s) + \text{permutations in } (a, b, m).$$
(B16)

Neutral scalar-charged scalar-charged scalar vertices

$$\mathcal{L} = \boldsymbol{g}_{abm}^{-} \Phi^{\dagger}(\boldsymbol{\phi}_{a}^{-}) \Phi(\boldsymbol{\phi}_{b}^{-}) \Phi(\boldsymbol{\phi}_{m}^{0}),$$

$$\begin{split} \mathbf{g}_{abm}^{-} &= -\frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} \sin\beta \mathcal{D}_{1m}^{+} \mathcal{D}_{1a}^{+} \mathcal{D}_{1b}^{+} + \frac{g_{2}M_{2}}{\cos\theta_{W}} \left(-\frac{1}{2} + \sin^{2}\theta_{W} \right) \cos\beta \mathcal{D}_{2m}^{+} \mathcal{D}_{1b}^{+} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) \left[\cos\beta (\mathcal{D}_{1m}^{*} + i\mathcal{D}_{6m}^{*}) + \sin\beta (\mathcal{D}_{2m}^{*} + i\mathcal{D}_{7m}^{*}) \right] \mathcal{D}_{2m}^{+} \mathcal{D}_{1b}^{+} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) \left[\cos\beta (\mathcal{D}_{1m}^{*} + i\mathcal{D}_{6m}^{*}) + \sin\beta (\mathcal{D}_{2m}^{*} - i\mathcal{D}_{2m}^{*}) \mathcal{D}_{1m}^{+} \mathcal{D}_{2b}^{+} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) (\sin\beta \mathcal{D}_{1m}^{*} + i\mathcal{D}_{6m}^{*}) \right] \\ &+ \sin\beta (\mathcal{D}_{2m}^{*} - i\mathcal{D}_{2m}^{*}) \left[\mathcal{D}_{1m}^{*} \mathcal{D}_{2b}^{+} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) (\sin\beta \mathcal{D}_{1m}^{*} + \cos\beta \mathcal{D}_{2m}^{*}) (\mathcal{D}_{1}^{*} + 2)m - i\mathcal{D}_{2m}^{*}) \mathcal{D}_{1m}^{*} + i\mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) (\cos\beta \mathcal{D}_{2m}^{*} - i\mathcal{D}_{2m}^{*}) \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \sin^{2}\theta_{W}) (\cos\beta \mathcal{D}_{2m}^{*} - i\mathcal{D}_{2m}^{*}) \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} \left(\frac{1}{2} - \sin^{2}\theta_{W} \right) (\cos\beta \mathcal{D}_{2m}^{*} - \sin\beta \mathcal{D}_{2m}^{*}) \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \frac{1}{2} \frac{g_{2}M_{2}}{\cos\theta_{W}} (1 - \frac{1}{2} \frac{g_{2}M_{2}}{2} \cos\theta_{W}^{*}) \left(\cos\beta \mathcal{D}_{2m}^{*} - \sin\beta \mathcal{D}_{2m}^{*}) \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} \\ - \frac{g_{2}M_{2}}{\cos\theta_{W}} \left(\frac{1}{2} - \sin^{2}\theta_{W} \right) (\cos\beta \mathcal{D}_{2m}^{*} - \sin\beta \mathcal{D}_{1m}^{*}) \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} \mathcal{D}_{2m}^{*} \mathcal{D}_{2b}^{*} \\ - \sqrt{2} v_{e_{0}} m_{e_{0}} \mathcal{D}_{1m}^{*} \mathcal{D}_{2m}^{*} \mathcal{$$

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