Minimal flavor violation supersymmetry: A natural theory for R-parity violation

Csaba Csáki[,*](#page-0-0) Yuval Grossman,^{[†](#page-0-1)} and Ben Heidenreich^{[‡](#page-0-2)}

Department of Physics, LEPP, Cornell University, Ithaca, New York 14853, USA (Received 5 January 2012; published 14 May 2012)

We present an alternative approach to low-energy supersymmetry. Instead of imposing R -parity we apply the minimal flavor violation (MFV) hypothesis to the R-parity violating MSSM. In this framework, which we call MFV SUSY, squarks can be light and the proton long-lived without producing missing energy signals at the LHC. Our approach differs from that of Nikolidakis and Smith in that we impose holomorphy on the MFV spurions. The resulting model is highly constrained and R -parity emerges as an accidental approximate symmetry of the low-energy Lagrangian. The size of the small R-parity violating terms is determined by the flavor parameters, and in the absence of neutrino masses there is only one renormalizable R-parity violating interaction: the baryon-number violating $\bar{u} \, d \bar{d}$ superpotential term. Low-energy observables (proton decay, dinucleon decay, and $n - \bar{n}$ oscillation) pose only mild constraints on the parameter space. LHC phenomenology will depend on whether the LSP is a squark, neutralino, chargino, or slepton. If the LSP is a squark it will have prompt decays, explaining the non-observation of events with missing transverse energy at the LHC.

DOI: [10.1103/PhysRevD.85.095009](http://dx.doi.org/10.1103/PhysRevD.85.095009) PACS numbers: 12.60.Jv, 14.80.Ly

I. INTRODUCTION

Supersymmetric extensions of the standard model do not automatically posses the requisite global symmetries of the standard model: baryon- and lepton-number violation can be mediated by squark and gaugino exchange, and flavor-non-universal soft-breaking terms can mediate flavor-changing neutral currents (FCNCs). In order to remove baryon- and lepton-number violating processes one usually assumes the additional presence of R-parity, while to remove FCNCs one usually assumes flavor universality (possibly at a high scale). R-parity has very important consequences for the phenomenology of the MSSM: it renders the lightest superpartner stable, forces superpartners to be pair-produced, and implies that (when produced) superparticles will always decay to the LSP, which will escape the detector, resulting in events with large missing energy.

 R -parity is clearly not necessary $[1-6]$ $[1-6]$: very small R-parity violating terms can be added to the supersymmetric Lagrangian, fundamentally changing the phenomenology of the model without conflicting with any current experimental bound (for an excellent review see [[7](#page-20-2)]). The introduction of R-parity is therefore linked to the idea of naturalness: if R-parity were not imposed, many dimensionless couplings in the superpotential would have to be extremely small in order to ensure a sufficiently long-lived proton.

LHC data, however, is beginning to place severe constraints on the R-parity conserving MSSM, ruling out squark masses up to about 1 TeV in some scenarios, due

to the absence of the expected missing transverse energy events [[8](#page-20-3)[,9\]](#page-20-4). Increasing the scale of supersymmetry breaking leads to increasingly large radiative corrections to the Higgs mass, suggesting that low-scale supersymmetry with R-parity may not be the correct solution to the hierarchy problem. In light of this it is natural to consider R-parity violation, which allows the LSP to decay promptly, and thus evades searches based on missing transverse energy or displaced vertices. However, besides naturalness, such an undertaking suffers from a proliferation of undetermined couplings, making it very difficult to constrain the theory from experimental data.

Here, we consider an alternate approach to low-energy supersymmetry. Instead of assuming R-parity, we only impose the minimal flavor violation hypothesis on the theory [[10](#page-20-5)–[13](#page-20-6)], positing that the non-abelian flavor symmetries are only broken by the holomorphic spurions corresponding to the Yukawa couplings. $¹$ As a consequence,</sup> all R-parity violating operators will be suppressed by Yukawa couplings and CKM factors, and the smallness of the R-parity violating terms is explained in terms of the smallness of the flavor parameters. We find that this assumption is sufficient to naturally avoid present bounds on baryon- and lepton-number violation, while automatically suppressing FCNCs as in any MFV model. Thus, we are able to replace two independent *ad hoc* assumptions, those of R-parity and flavor universality, with the single assumption of minimal flavor violation. R-parity then emerges as an approximate accidental symmetry of the low-energy

[^{*}c](#page-0-3)saki@cornell.edu

[[†]](#page-0-3) yg73@cornell.edu

[[‡]](#page-0-3) bjh77@cornell.edu

¹While the most general flavor symmetry, $U(3)^5$, is not semisimple, the abelian $U(1)^5$ component contains R-parity, and would imply the complete absence of lepton- and baryonnumber violating operators. In our spurion analysis, we only impose the non-abelian $SU(3)^5$ component.

Lagrangian, where the $$ mined by the flavor sector.

We will argue that the simplest form of this model is viable with natural $\mathcal{O}(1)$ coefficients for all operators and low, ~100–300 GeV, superpartner masses. This provides a natural alternative framework for studying supersymmetric extensions of the standard model. While the R-parity violating couplings are sufficiently small to prevent proton decay, they are sufficiently large to make the LSP decay promptly. The phenomenology is distinctive, and depends on only a relatively small number of unknown $\mathcal{O}(1)$ parameters, in contrast to the generic R-parity violating MSSM.

The idea that minimal flavor violation can replace R-parity was originally explored in an important paper by Nikolidakis and Smith a few years ago [[14](#page-20-7)] (see also [\[15\]](#page-20-8)). Our approach differs from theirs in that we take the spurions to be holomorphic, which is necessary since they appear in the superpotential as Yukawa couplings, and should be thought of as VEVs of chiral superfields. Thus, Y^{\dagger} cannot appear in the superpotential, nor in soft-breaking A -terms,² which, combined with the MFV hypothesis, severely constrains the form of these terms.

We will show that in the absence of neutrino masses there is no holomorphic invariant violating lepton number, and there is only a single renormalizable term violating baryon number, the \bar{u} d d term in the superpotential. Furthermore, an unbroken \mathbb{Z}_3^L subgroup of $U(1)_L$ —a necessary consequence of MFV—ensures that the first non-holomorphic (Kähler) corrections violating lepton number appear at dimension eight, and are very strongly suppressed for even a moderately high cutoff scale. Thus, in the limit of vanishing neutrino masses the proton will be effectively stable. The constraints from $n - \bar{n}$ oscillations are easily satisfied, while those from dinucleon decay place a mild upper bound on $tan \beta$ for light squark masses.

Majorana neutrino masses require additional holomorphic spurions charged under \mathbb{Z}_3^L , and we find that once they are incorporated into the model through the seesaw mechanism, current bounds on proton decay will impose interesting, though not too onerous, constraints on the right-handed neutrino sector. Other methods of neutrino mass generation should also be constrained by proton stability.

The phenomenology of such models is largely determined by the choice of the LSP. If it is a squark, it can decay directly via the baryon number violating $\bar{u} d d$ vertex, which yields a lifetime short enough for these decays to be prompt. If a sparticle other than a squark is the LSP (such as a neutralino, chargino, or slepton) then the decays will involve more particles in the final state and the lifetime will increase, potentially leading to displaced vertices, and in some cases also to missing energy via neutrinos and tops in the final state.

The paper is organized as follows. In Sec. [II](#page-1-0), we introduce the MFV SUSY framework and list possible superpotential terms, neglecting neutrino masses. In Sec. [III,](#page-4-0) we focus on the most interesting of these terms, a baryon number violating vertex. In Sec. [IV,](#page-5-0) we discuss constraints arising from $n - \bar{n}$ oscillations and dinucleon decay induced by this vertex. In Sec. [V,](#page-6-0) we modify the model to incorporate neutrino masses, focusing on the seesaw mechanism, and list the relevant operators, VEVs, and mixings. In Sec. [VI](#page-8-0), we discuss constraints on the righthanded neutrino sector arising from bounds on proton decay. In Sec. [VII](#page-11-0) we estimate the LSP lifetime and comment on LHC signals/constraints. We conclude in Sec. [VIII.](#page-15-0) In a collection of appendixes, we classify all possible holomorphic superpotential terms, discuss nonholomorphic corrections from supersymmetry breaking, argue that diagrams other than those considered in the main text will be subdominant for the processes of interest, and show that higher-dimensional operators will not affect our conclusions for a sufficiently high cutoff.

II. MFV SUSY WITHOUT NEUTRINO MASSES

We first consider the limit of vanishing neutrino masses (we introduce them in Sec. [V\)](#page-6-0). The MSSM consists of the standard model (SM) gauge group $SU(3)_C \times SU(2)_L \times$ $U(1)_y$, together with the usual chiral superfields as shown in Table [I](#page-1-1). The matter fields Q , \bar{u} , d , L , and \bar{e} are flavored, and come in three generations. The superpotential

$$
W = \mu H_u H_d + Y_e L H_d \bar{e} + Y_u Q H_u \bar{u} + Y_d Q H_d \bar{d}, \quad (2.1)
$$

is necessary to generate the SM fermion masses and charged higgsino masses. The additional (renormalizable) superpotential terms allowed by gauge invariance are

$$
W' = \lambda L L \bar{e} + \lambda' Q L \bar{d} + \lambda'' \bar{u} \, \bar{d} \, \bar{d} + \bar{\mu} L H_u.
$$
 (2.2)

These superpotential terms violate lepton and baryon number, and therefore should be absent or very small. The traditional approach is to impose a \mathbb{Z}_2 symmetry, called matter parity, under which the matter fields Q , \bar{u} , d , L , and

TABLE I. The MSSM fields and their representations under the SM gauge group.

	$SU(3)_C$	SU(2) _L	$U(1)_Y$
ϱ	$\vert \ \ \vert$		
	п		$\frac{1/6}{-2/3}$
\bar{u} \bar{d}	□		1/3
L		H	$-1/2$
\bar{e}			
		H	1/2
$\frac{H_u}{H_d}$		H	$-1/2$

 2^2 Nonholomorphic corrections to the A-terms are possible. However, these corrections are subleading, as explored in Appendix [B](#page-16-0). In addition, bilinear corrections to the superpotential can be generated nonholomorphically at the scale m_{soft} .

 \bar{e} are odd and the Higgs fields H_u and H_d are even. This \mathbb{Z}_2 symmetry forbids all unwanted superpotential terms in W' , leaving only those in [\(2.1\)](#page-1-2). A combination of matter parity with a discrete subgroup of the Lorentz group gives R-parity, under which all SM fields are even and superpartners odd.

The imposition of R-parity is not the only *ad hoc* assumption needed to make the MSSM phenomenologically acceptable. Soft terms needed to break supersymmetry and mass-up the superpartners generically induce large flavorchanging neutral currents. In order to reduce FCNCs, one usually imposes flavor universality: i.e. the assumption that at some scale all soft-breaking masses are flavor-universal and the A-terms are proportional to the corresponding Yukawa couplings.

Our approach will be to replace these two ad hoc assumptions with the single assumption of Minimal Flavor Violation (MFV). MFV is based on the observation that apart from the μ term, most of the terms in the superpotential [\(2.1\)](#page-1-2) are small due to the smallness of the Yukawa couplings. It is then natural to analyze the spurious symmetries preserved by the μ -term but broken by the Yukawa couplings, which are given in Table [II.](#page-2-0) Excepting $U(1)_{B-L}$ and a U(1)² subgroup of $SU(3)_L \times SU(3)_e$ representing intergenerational lepton number differences, the Yukawa couplings are charged under all of these symmetries, which are therefore broken by the superpotential.

The basic assumption of minimal flavor violation [\[10–](#page-20-5)[13\]](#page-20-6) is that the Yukawa couplings Y_u , Y_d , and Y_e are the *only* spurions which break the non-abelian $SU(3)^5$ flavor symmetry. No assumption on baryon or lepton number is made. Thus, while flavor nonsinglet terms may be written in the superpotential, or as soft-breaking terms, their coefficients must be built out of combinations of Yukawa couplings and their complex conjugates in a way which respects the underlying spurious flavor symmetry. The main new ingredient in applying MFV to SUSY

TABLE II. The transformation properties of the chiral superfields and the spurions under the nonanomalous flavor symmetries preserved by the μ term. We omit discrete symmetries and a nonanomalous $U(1)_R$ which is broken by the soft terms, including the B_{μ} term.

			$SU(3)_Q$ $SU(3)_u$ $SU(3)_d$ $SU(3)_L$ $SU(3)_e$ $U(1)_{B-L}$ $U(1)_H$	
			1/3	
\overline{u}			$-1/3$	
			$-1/3$	
\bar{e}				
H_u				
H_d				
Y_u				
Y_d				
Y_e				

theories is that the spurions also have to be assigned to representations of supersymmetry. Since the spurions $Y_{u,d,e}$ appear in the superpotential in the Yukawa terms, the most natural assumption is to assign these spurions to chiral superfields, with the expectation that in a UV completion these spurions would emerge as VEVs of some heavy chiral superfields. This assignment for the spurions ensures that the conjugate Yukawa couplings Y^{\dagger} cannot appear in the superpotential, which will lead to a very restrictive ansatz, both for R-parity violating terms and for higherdimensional operators.

The MFV hypothesis can be shown to naturally suppress FCNCs [\[12](#page-20-9)[,13\]](#page-20-6), thereby solving the new physics flavor problem. It is also RGE stable, due to the spurious flavor symmetries, which prevent flavor violating terms from being generated radiatively except those proportional to the original spurions themselves. As explored in [[14](#page-20-7)], it is possible to impose the MFV hypothesis on spurious (and even anomalous) U(1) symmetries as well. However, we will not do so, since the abelian symmetries are not needed to suppress FCNCs, and furthermore, imposing such a hypothesis will generally lead to phenomenology which is closer to the R-parity conserving MSSM, while our primary goal is to demonstrate a viable supersymmetric model with vastly different phenomenology.

In addition to FCNCs, low-energy CP violation (CPV) searches and measurements also impose strong constraints on new physics. Experimentally, CPV has been discovered only in flavor-changing processes in K and B decays. In the SM, this is explained by the fact that the only source of CPV is the one physical phase of the CKM matrix. When extending the SM, however, many new sources of CPV can arise, both in flavor changing as well as flavor conserving couplings. The MFV framework suppresses all new flavorchanging CPV effects, but does not address the problem of flavor diagonal sources of CPV. In SUSY, in particular, new flavor diagonal couplings can give rise to large EDMs, and thus the new phases cannot be order one, and must be tuned to satisfy experimental constraints [\[16\]](#page-20-10). Within MFV, one solution is to assume that all CP violating spurions come from the Yukawa matrices. In this work, we will not consider the problem of CP violation any further, as we do not expect that the problem will be qualitatively different for MFV SUSY than for other MFV models [[17\]](#page-20-11).

Thus, we will make the ''minimal'' assumption that the holomorphic spurions Y_u , Y_d , Y_e are the only sources of $SU(3)^5$ breaking, discarding R-parity as a means of stabilizing the proton. This assumption, together with the holomorphy of the Yukawa couplings, turns out to be very restrictive. It is straightforward to find the complete list of irreducible holomorphic flavor singlets, shown in Table [III](#page-3-0). The superpotential is therefore built from gauge invariant combinations of these operators. In particular, since none of these operators carry lepton number, $U(1)_L$ is an exact symmetry of the superpotential.

TABLE III. The irreducible holomorphic flavor singlets. We omit flavor-singlet spurions (irrelevant to our analysis) as well as flavor singlets formed from $SU(3)_C \times SU(2)_L$ contractions of products of the operators listed here.

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$ $U(1)_B$		U(1) _L	\mathbb{Z}_2^R
$\left(\mathcal{Q}\mathcal{Q}\mathcal{Q}\right)$			1/2		0	
QQQQ	8	L	1/2		0	
$(Y_u\bar{u})(Y_u\bar{u})(Y_d\bar{d})$	$8 \oplus 1$		-1	-1	0	
$(Y_u\bar{u})(Y_d\bar{d})(Y_d\bar{d})$	$8 \oplus 1$		θ	-1	0	
$det\bar{u}$			-2	-1	0	
det d				-1		
$QY_u\bar{u}$	$8 \oplus 1$		$-1/2$	0		
QY_d d	$8 \oplus 1$		1/2	0		
LY_ee	1		1/2	0		$^+$
H_u			1/2	0		\pm
H_d			$-1/2$			

While holomorphy also forbids lepton-number violation in the soft-breaking A terms, lepton-number violation can still occur in the Kähler potential, and in bilinear superpotential terms, 3 B terms, and the soft mass-mixing term $\tilde{L}\tilde{H}_{d}^{\star}$ + c.c.. However, while such terms will play an important role when we introduce neutrino masses in Sec. [V,](#page-6-0) in the case of massless neutrinos they are absent for the following symmetry reason. There is a \mathbb{Z}_3^L \in $SU(3)_L \times SU(3)_e$ symmetry of the form:

$$
L \to \omega L, \qquad \bar{e} \to \omega^{-1} \bar{e}, \qquad Y_e \to Y_e, \tag{2.3}
$$

where $\omega \equiv e^{2\pi i/3}$ and the other fields and spurions are not charged under \mathbb{Z}_3^L . In particular, \mathbb{Z}_3^L lies within the $\mathbb{Z}_3 \times \mathbb{Z}_3$ center of $SU(3)_L \times SU(3)_e$, and is also a \mathbb{Z}_3 subgroup of $U(1)_L$. As all spurions are neutral under \mathbb{Z}_3^L , we conclude that lepton number can only be violated in multiples of three. Soft terms of this type are not possible, whereas the lowest-dimension $\Delta L = \pm 3$ Kähler potential corrections are dimension eight, and are strongly suppressed for a sufficiently high cutoff.

Since, in the absence of light unflavored fermions, proton decay requires lepton-number violation, we conclude that the proton is effectively stable for massless neutrinos. Thus, proton stability will only constrain the neutrino sector, as discussed in Sec. [VI](#page-8-0).⁴

In addition to the R -parity conserving terms (2.1) , MFV allows only one additional renormalizable correction to the superpotential,

$$
W_{\rm BNV} = \frac{1}{2} w''(Y_u \bar{u})(Y_d \bar{d})(Y_d \bar{d}), \tag{2.4}
$$

where w'' is an unknown $\mathcal{O}(1)$ coefficient. In combination with the MFV structure of the soft terms, most of the interesting phenomenology of our model arises from this baryon-number and R-parity violating term.

The Kähler potential need not be canonical, and is subject to nonuniversal corrections. At the renormalizable level, these take the form,

$$
K = Q^{\dagger} [1 + f_Q(Y_u Y_u^{\dagger}, Y_d Y_d^{\dagger})^T + \text{H.c.}]Q
$$

+ $\bar{u}^{\dagger} [1 + Y_u^{\dagger} f_u(Y_u Y_u^{\dagger}, Y_d Y_d^{\dagger}) Y_u + \text{H.c.}] \bar{u}$
+ $\bar{d}^{\dagger} [1 + Y_d^{\dagger} f_u(Y_u Y_u^{\dagger}, Y_d Y_d^{\dagger}) Y_d + \text{H.c.}] \bar{d}$
+ $L^{\dagger} [1 + f_L(Y_e Y_e^{\dagger})^T + \text{H.c.}]L$
+ $\bar{e}^{\dagger} [1 + f_e(Y_e^{\dagger} Y_e) + \text{H.c.}] \bar{e},$ (2.5)

where the f_i are polynomials in the indicated (Hermitean) matrices. While the renormalizable Kähler potential can be made canonical by an appropriate change of basis, such a change of basis is not compatible with the holomorphy of the spurions. The situation is analogous to that of the supersymmetric beta function, where the one-loop NSVZ result can be shown to be exact in an appropriate holomorphic basis, but the ''physical'' all-loop beta function is still subject to wave function renormalization, since the gauge boson kinetic term is noncanonical in the holomorphic basis. Similarly, in MFV SUSY the form of the superpotential is highly constrained, but the Kähler potential is still subject to a large number of unknown corrections. Fortunately, these unknown corrections are suppressed by the smallness of the Yukawa couplings.

The allowed A and B terms are in direct correspondence with the allowed superpotential terms, and carry the same flavor structure, except that the A-terms are subject to certain subleading nonholomorphic corrections,

$$
\mathcal{L}_{soft} \supset Y_u (1 + Y_u^{\dagger} Y_u + ...)\tilde{\bar{u}} (Y_d \tilde{\bar{d}})(Y_d \tilde{\bar{d}}) \n+ (Y_u \tilde{\bar{u}})(Y_d \tilde{\bar{d}}) Y_d (Y_d^{\dagger} Y_d + ...)\tilde{\bar{d}},
$$
\n(2.6)

and similar corrections to the other A terms, as explained in Appendix [B](#page-16-0). However, as with corrections to the Kähler potential, these corrections are suppressed by the smallness of the Yukawa couplings.

The soft-breaking scalar masses have the same basic flavor structure as the Kähler terms listed above. This implies, in particular, that, while FCNCs can occur via squark exchange, they are suppressed by the GIM mechanism [[18](#page-20-12)], just as in the standard model. This automatic suppression of FCNCs is a universal feature of MFV scenarios. We will quantify the flavor-changing squark mass-mixings in Sec. [IVA](#page-5-1).

We defer consideration of higher-dimensional operators to Appendix [E](#page-20-13), where we show that such operators will give subdominant contributions to baryon-number violating processes.

³These can be generated non-holomorphically after SUSY breaking, as shown in Appendix [B](#page-16-0). ⁴

⁴The situation changes if the gravitino (or another unflavored fermion, such as an axino) is lighter than m_p . We discuss the resulting constraints on $m_{3/2}$ in Sec. [VI](#page-8-0).

III. THE BARYON-NUMBER VIOLATING VERTEX

Most of the interesting phenomenology of our model arises from the interaction ([2.4](#page-3-1)), which we now discuss in more detail. Performing an $SU(3)^5$ transformation, we choose a basis where

$$
Y_{u} = \frac{1}{v_{u}} V_{CKM}^{\dagger} \begin{bmatrix} m_{u} & 0 & 0 \\ 0 & m_{c} & 0 \\ 0 & 0 & m_{t} \end{bmatrix},
$$

\n
$$
Y_{d} = \frac{1}{v_{d}} \begin{bmatrix} m_{d} & 0 & 0 \\ 0 & m_{s} & 0 \\ 0 & 0 & m_{b} \end{bmatrix},
$$

\n
$$
Y_{e} = \frac{1}{v_{d}} \begin{bmatrix} m_{e} & 0 & 0 \\ 0 & m_{\mu} & 0 \\ 0 & 0 & m_{\tau} \end{bmatrix},
$$

\n(3.1)

where V_{CKM} is the CKM matrix and $v_{u,d} = \langle H_{u,d} \rangle$ are the Higgs VEVs, with $v^2 = v_u^2 + v_d^2 \approx (174 \text{ GeV})^2$ the standard model Higgs VEV. Since the Yukawa couplings are RG-dependent quantities, we should in principle evaluate them at the squark-mass scale to estimate [\(2.4\)](#page-3-1), integrate out the superpartners, and then run the resulting couplings down to the QCD scale. However, to obtain a rough estimate, it is sufficient to estimate them using the following low-energy quark masses [\[19\]](#page-21-0),

$$
m_u \sim 3 \text{ MeV}, \quad m_c \sim 1.3 \text{ GeV}, \quad m_t \sim 173 \text{ GeV} \sim v,
$$

$$
m_d \sim 6 \text{ MeV}, \quad m_s \sim 100 \text{ MeV}, \quad m_b \sim 4 \text{ GeV}, \quad (3.2)
$$

together with the lepton masses,

$$
m_e \approx 0.511 \text{ MeV}, \quad m_\mu \approx 106 \text{ MeV}, \quad m_\tau \approx 1.78 \text{ GeV}.
$$
 (3.3)

For the magnitudes of the CKM elements, we take

$$
V_{\text{CKM}} \sim \begin{pmatrix} 1 & \lambda & \lambda^3/2 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}, \tag{3.4}
$$

where $\lambda \sim 1/5$ approximates all elements to better than 20% accuracy.

The lepton and down-type Yukawa couplings depend strongly on tan $\beta \equiv v_u/v_d$. We consider a broad range, $3 \leq \tan \beta \leq 45$, where the lower bound is motivated by electroweak symmetry breaking, and the upper bound by perturbativity of the bottom Yukawa coupling, $y_b \le 1$. Consistent with the lower bound $\tan \beta \geq 3$, we will usually assume $\tan \beta \gg 1$, which simplifies many formulas.

Using the assumptions outlined above, we now estimate the size of the baryon-number violating term ([2.4](#page-3-1)), which is conventionally written in the form,

TABLE IV. Numerical estimates of λ''_{ijk} for tan $\beta = 45$ and $w'' \sim 1.$

	sh	bd	ds
\mathcal{U}	5×10^{-7}	6×10^{-9}	3×10^{-12}
	4×10^{-5}	1.2×10^{-5}	1.2×10^{-8}
	2×10^{-4}	6×10^{-5}	4×10^{-5}

$$
W_{\text{BNV}} = \frac{1}{2} \lambda_{ijk}^{\prime\prime} \epsilon^{abc} \bar{u}_a^i \bar{d}_b^j \bar{d}_c^k, \tag{3.5}
$$

where a, b, c are color indices and i, j, k are the flavor indices, with summation over repeated indices understood. The factor of one-half is due to the antisymmetry of the operator in the down-type flavor indices (which is a consequence of the color contraction). Using the basis (3.1) , we find

$$
\lambda_{ijk}^{"'} = w^{"}y_i^{(u)}y_j^{(d)}y_k^{(d)}\epsilon_{jkl}V_{il}^{\star},\tag{3.6}
$$

where $y_i^{(u)}$ and $y_i^{(d)}$ are the up- and down-type Yukawa couplings, and the coupling scales like $(\tan \beta)^2$ for large $tan \beta$. Using the CKM estimate [\(3.4\)](#page-4-2), we find

$$
\lambda_{usb}'' \sim t_{\beta}^2 \frac{m_b m_s m_u}{m_i^3}, \qquad \lambda_{ubd}'' \sim \lambda t_{\beta}^2 \frac{m_b m_d m_u}{m_i^3},
$$

\n
$$
\lambda_{uds}'' \sim \lambda^3 t_{\beta}^2 \frac{m_d m_s m_u}{2m_i^3}, \qquad \lambda_{csb}'' \sim \lambda t_{\beta}^2 \frac{m_b m_c m_s}{m_i^3},
$$

\n
$$
\lambda_{cbd}'' \sim t_{\beta}^2 \frac{m_b m_c m_d}{m_i^3}, \qquad \lambda_{cds}'' \sim \lambda^2 t_{\beta}^2 \frac{m_c m_d m_s}{m_i^3},
$$

\n
$$
\lambda_{tsb}'' \sim \lambda^3 t_{\beta}^2 \frac{m_b m_s}{m_i^2}, \qquad \lambda_{tbd}'' \sim \lambda^2 t_{\beta}^2 \frac{m_b m_d}{m_i^2},
$$

\n
$$
\lambda_{tds}'' \sim t_{\beta}^2 \frac{m_d m_s}{m_i^2}.
$$

\n(3.7)

where we t_β as a shorthand for tan β . Taking the extreme value tan $\beta = 45$, and using the quark masses [\(3.2\)](#page-4-3) and $\lambda \sim 1/5$, we obtain the numerical estimates shown in Table [IV.](#page-4-4)

Because of the Yukawa suppression, the largest coupling, $\lambda_{\text{tsb}}^{\prime\prime}$, involves as many third-generation quarks as possible, without any first-generation quarks. This coupling, however, will contribute subdominantly to lowenergy baryon-number violation, due to the CKM suppression required for the third-generation quarks to flavor change into first-generation external state quarks.

There are many bounds on specific combinations of RPV couplings [[7\]](#page-20-2). These bounds typically assume a generic form for the soft-masses, and thus do not necessarily apply to MFV SUSY. However, due to the flavor suppression, the predicted values of the RPV couplings in our case are small, and all of these bounds are satisfied.

IV. CONSTRAINTS FROM $\Delta B = 2$ PROCESSES

The baryon number violating interaction [\(2.4\)](#page-3-1) will lead to baryon number violating processes which are, in theory, observable at low energy [\[20](#page-21-1)]. In particular, the most stringent limits on baryon number violation without lepton number violation come from the lower bound on the neutron-antineutron oscillation time [\[21\]](#page-21-2)

$$
\tau_{n-\bar{n}} \ge 2.44 \times 10^8 \text{ s}, \tag{4.1}
$$

and from the lower bound on the partial lifetime for $pp \rightarrow K^+K^+$ dinucleon decay [\[22](#page-21-3)]

$$
\tau_{pp \to K^+ K^+} \ge 1.7 \times 10^{32} \text{ yrs.}
$$
 (4.2)

Both limits come from null observation of 16O decay to various final states in the Super-Kamiokande water Cherenkov detector. Present limits on other dinucleon partial lifetimes are somewhat weaker, at $\sim 10^{30}$ yrs [[19](#page-21-0)].

In this section, we will only consider the simplest, tree-level diagrams for the processes of interest. While these will turn out the be the dominant diagrams, it is necessary to check that other contributions are subdominant. We outline a systematic scheme for doing so in Appendixes [C](#page-17-0) and [D.](#page-18-0)

A. $n - \bar{n}$ oscillations

There is a unique tree-level diagram for $n - \bar{n}$ oscillations, up to crossing symmetry, the choice of the exchanged fermionic sparticle, and the squark flavors (see Fig. [1\)](#page-5-2). The down-type squarks cannot be first generation, due to the antisymmetry of $\lambda_{ijk}^{\prime\prime}$ in the last two indices. Thus, to achieve the required flavor-changing, the squarks must change flavor via mass insertions, arising from softterms of the form:

$$
\mathcal{L}_{soft} \supset m_{soft}^{2} \tilde{Q}^{\star} (Y_{u} Y_{u}^{\dagger} + Y_{d} Y_{d}^{\dagger}) \tilde{Q} + ..., \qquad (4.3)
$$

where the omitted terms are higher-order in the Yukawa couplings or are diagonal in the quark mass basis.

Thus, off-diagonal mass-mixing between left-handed down-type squarks of flavors i and j is suppressed by

$$
V_{ij}^{\text{(neutral)}} \equiv \frac{\delta m_{ij}^2}{m_{\text{soft}}^2} \sim \sum_k V_{ik}^{\dagger} [y_k^{(u)}]^2 V_{kj}, \tag{4.4}
$$

FIG. 1. The leading contribution to $n - \bar{n}$ oscillation. mixing is still possible.

with a similar expression for up-type squarks. The sum in [\(4.4\)](#page-5-3) is dominated by the third generation except in the case of $V_{uc}^{(neutral)}$, where there is a competitive (though not dominant) contribution from the second generation. We find:

$$
V_{ds}^{(\text{neutral})} \sim \lambda^5, \quad V_{db}^{(\text{neutral})} \sim \lambda^3, \quad V_{sb}^{(\text{neutral})} \sim \lambda^2,
$$

\n
$$
V_{uc}^{(\text{neutral})} \sim y_b^2 \lambda^5 / 2, \quad V_{ut}^{(\text{neutral})} \sim y_b^2 \lambda^3 / 2, \quad V_{ct}^{(\text{neutral})} \sim y_b^2 \lambda^2.
$$
\n(4.5)

Since the squarks in Fig. [1](#page-5-2) are initially right-handed, the required flavor changing is suppressed by an additional Yukawa coupling. Depending on the initial flavor of the squark, we obtain

$$
\tilde{b}_R \to \tilde{d}_L \sim y_b \lambda^3, \qquad \tilde{s}_R \to \tilde{d}_L \sim y_s \lambda^5. \tag{4.6}
$$

As the vertex factor is also larger for a \tilde{b} squark, $\tilde{b}_R \rightarrow \tilde{d}_L$ is clearly dominant.

Gathering all factors, we obtain the amplitude

$$
\mathcal{M}_{n-\bar{n}} \sim \tilde{\Lambda} t_{\beta}^{6} \lambda^{8} \frac{m_{u}^{2} m_{d}^{2} m_{b}^{4}}{m_{t}^{8}} \left(\frac{\tilde{\Lambda}}{m_{\tilde{q}}}\right)^{4} \left[g_{s}^{2} \left(\frac{\tilde{\Lambda}}{m_{\tilde{g}}}\right) + \ldots\right], \quad (4.7)
$$

where we write the hadronic matrix element as $\tilde{\Lambda}^6$, with $\tilde{\Lambda} \sim \Lambda_{\text{QCD}}$ in rough agreement with the estimates of [\[7,](#page-20-2)[23\]](#page-21-4). The omitted terms come from neutralino, rather than gluino, exchange and can be important if the gluino is very heavy.

The $n - \bar{n}$ oscillation time is approximately $t_{\rm osc} \sim \mathcal{M}^{-1}$. Therefore, assuming that the tree-level amplitude ([4.7](#page-5-4)) gives the dominant contribution, we find

$$
t_{\text{osc}} \sim (9 \times 10^9 \text{ s}) \left(\frac{250 \text{ MeV}}{\tilde{\Lambda}}\right)^6 \left(\frac{m_{\tilde{q}}}{100 \text{ GeV}}\right)^4 \left(\frac{m_{\tilde{g}}}{100 \text{ GeV}}\right)
$$

$$
\times \left(\frac{45}{\tan \beta}\right)^6, \tag{4.8}
$$

where we take $\alpha_s \equiv g_s^2/4\pi \sim 0.12$. This must be com-pared to the experimental bound ([4.1](#page-5-5)), $\tau \ge 2.44 \times 10^8$ s. Thus, unless we have substantially underestimated the hadronic matrix element, $n - \bar{n}$ oscillations place no constraint on our model.

B. Dinucleon decay

The simplest diagrams for dinucleon decay take the same form as the tree-level $n - \bar{n}$ diagram (see Fig. [1\)](#page-5-2), with the addition of two spectator quarks, as shown in Fig. [2.](#page-6-1) There are two possibilities, depending on whether the exchanged sparticle is a chargino or a gluino/neutralino. In the former case, the squarks undergo charged flavor changing while converting to quarks, much like quarks exchanging a W boson; charge conservation then requires that one squark is up-type and the other down-type. In the latter case, the squark/quark/neutralino vertex is flavor diagonal, but neutral flavor changing via squark mass-

FIG. 2. Dinucleon decay via neutral gaugino exchange (left) and chargino exchange (right).

For simplicity, we only consider diagrams of this type.⁵ The external quarks must be light quarks, no more than two of which may be strange quarks. Since the quark legs do not change flavor, only ubs, ubd, uds, cds, and tds vertices may be used. By enumerating all possibilities, one can check that the dominant diagram involving chargino exchange combines a *tds* vertex with a *ubs* vertex, whereas the dominant diagram involving gluino/neutralino exchange combines two *tds* vertices with $\tilde{t} \rightarrow \tilde{u}$ flavorchanging mass-mixing along the squark lines. The two diagrams are shown in Fig. [2](#page-6-1), with flavor suppressions $y_{\mu}y_{\mu}y_{\xi}^2y_{\beta}^2\lambda^6/2$ for the chargino exchange diagram, and $y_d^2 y_s^2 y_b^4 \lambda^6/4$ for the gluino/neutralino exchange diagram. Ignoring order-one factors (including gauge couplings), the gluino/neutralino diagram is dominant if

$$
\frac{y_d y_b^2}{2y_u} \simeq \frac{m_d}{2m_u} \left(\frac{m_b}{m_t}\right)^2 \tan^3 \beta \gtrsim 1.
$$
 (4.9)

Thus, for tan $\beta \ge 12$ the gluino/neutralino diagram dominates; we focus on this possibility for the time being.

Following Goity and Sher [\[23\]](#page-21-4), we obtain the dinucleon $NN \rightarrow KK$ width,

$$
\Gamma \sim \rho_N \frac{128\pi\alpha_s^2 \tilde{\Lambda}^{10}}{m_N^2 m_{\tilde{g}}^2 m_{\tilde{q}}^8} \left(\frac{\lambda^3 m_d m_s m_b^2}{2m_t^4} \tan^4 \beta\right)^4, \qquad (4.10)
$$

where $m_N \simeq m_p$ is the nucleon mass, $\rho_N \sim 0.25 \text{ fm}^{-3}$ is the nucleon density, and $\tilde{\Lambda}$ is the "hadronic scale," arising from the hadronic matrix element and phase-space integrals. Thus,

$$
\tau_{NN \to KK} \sim (1.9 \times 10^{32} \text{ yrs}) \left(\frac{150 \text{ MeV}}{\tilde{\Lambda}}\right)^{10} \left(\frac{m_{\tilde{q}, \tilde{g}}}{100 \text{ GeV}}\right)^{10} \times \left(\frac{17}{\tan \beta}\right)^{16},\tag{4.11}
$$

where, as before, we take $\alpha_s \sim 0.12$. Comparing with the experimental bound [\(4.2\)](#page-5-6), $\tau \ge 1.7 \times 10^{32}$ yrs, we obtain an upper bound

$$
\tan \beta \le 17 \left(\frac{150 \text{ MeV}}{\tilde{\Lambda}} \right)^{5/8} \left(\frac{m_{\tilde{q}, \tilde{g}}}{100 \text{ GeV}} \right)^{5/8}.
$$
 (4.12)

This bound is illustrated in Fig. [3.](#page-7-0)

There remains considerable uncertainty in the hadronic matrix element. Goity and Sher consider values for $\bar{\Lambda}/m_{\tilde{q}, \tilde{g}}$ between 10^{-3} and 10^{-6} [\[23\]](#page-21-4). An earlier paper by Barbieri and Masiero, while taking a substantially different approach, obtains a result consistent with $\tilde{\Lambda} \sim 150$ MeV [\[24\]](#page-21-5). We will take $\tilde{\Lambda} = 150$ MeV as a representative value. While this is somewhat smaller than the "natural" $\sim \Lambda_{\text{QCD}}$ scale that one might expect, the matrix element is expected to be suppressed by hard-core repulsion between the nucleons, motivating the yet-smaller scales considered by [\[23\]](#page-21-4). Because of the uncertainty in $\tilde{\Lambda}$, we leave the dependence on it explicit in [\(4.12\)](#page-6-2); Fig. [3](#page-7-0) illustrates the effect of varying Λ .

Assuming $m_{\tilde{q}, \tilde{g}} \gtrsim 100 \text{ GeV}$, the charged flavorchanging diagram does not alter the above bounds, since both amplitudes increase with tan β , whereas the neutral flavor-changing diagram is already sufficiently suppressed at $tan \beta \sim 12$, below which charged flavor-changing becomes dominant.

V. INCORPORATING NEUTRINO MASSES

We have seen that in the absence of neutrino masses the MFV SUSY approach approximately conserves lepton number, leaving an exact \mathbb{Z}_3^L lepton number symmetry unbroken. To introduce neutrino masses, we therefore require additional spurions, which will lead to additional allowed operators in the Lagrangian [[25](#page-21-6),[26](#page-21-7)]. It is important to fully characterize such operators as, in combination with the baryon number violating vertex [\(2.4\)](#page-3-1), they can induce proton decay.

We focus on the seesaw mechanism to generate Majorana masses for the neutrinos. We add three righthanded sterile neutrinos, \overline{N} , which obtain Majorana masses at a heavy scale M_R . Through a Yukawa coupling Y_N to the left-handed neutrinos, this gives the left-handed neutrinos a small Majorana mass of order $Y_N^2 v^2/M_R$ upon electroweak symmetry breaking. Because of the additional flavored

⁵For a more systematic treatment, see Appendixes [C](#page-17-0) and [D](#page-18-0).

FIG. 3 (color online). Constraints on $tan \beta$ and superparter masses due to the nonobservation of dinucleon decay. The (red) region is excluded assuming that $\Lambda \ge 100$ MeV, whereas the (orange) region is also excluded when $\Lambda \ge 150$ MeV, and the (yellow) region for $\tilde{\Lambda} \ge 200$ MeV.

field, the non-abelian spurious symmetry of the lepton sector is extended to $SU(3)_L \times SU(3)_e \times SU(3)_N$. The superpotential required to generate neutrino masses is

$$
W_{\text{lept}} = Y_e L H_d \bar{e} + Y_N L H_u \bar{N} + \frac{1}{2} M_N \bar{N} \bar{N}, \qquad (5.1)
$$

where the elements of M_N are assumed to be of order M_R . Thus, there are now three spurions in the lepton sector: Y_e , Y_N , and M_N . The transformation properties of the leptonic sector under the spurious symmetries are shown in Table [V.](#page-7-1) As before, we do not impose the MFV hypothesis on the (spurious) U(1) symmetries.

A subtlety arises when applying the MFV hypothesis to M_N , since it is dimensionful. Instead, we will expand in the dimensionless spurion,

$$
\mu_N \equiv \frac{1}{\Lambda_R} M_N,\tag{5.2}
$$

where Λ_R is an unknown heavy scale. Perturbativity of the spurion expansion requires $M_R \leq \Lambda_R$. In addition

TABLE V. The spurious leptonic flavor symmetries of the MSSM with right-handed neutrinos. We omit discrete and anomalous symmetries.

		$SU(3)_L$ $SU(3)_e$ $SU(3)N$ $U(1)_{B-L}$ $U(1)_H$		U(1)N
L				
\bar{e}				
Ñ				
Y_e		$\mathbf{\Omega}$		
Y_N		$\mathbf{\Omega}$	– 1	
M_N				

TABLE VI. A complete list of holomorphic flavor singlets involving Y_N and M_N . We indicate the lepton number of the fields only, not counting that "carried" by the spurion M_N .

	SU(2) _L	$U(1)_Y$	U(1) _L	\mathbb{Z}_2^R
$(LL)(\tilde{Y}_N M_N \tilde{Y}_N)(LL)$		-2		
$(LL)(\tilde{Y}_N M_N \tilde{Y}_N)(Y_e \bar{e})$	1	$\mathbf{0}$		
$(LL)\tilde{Y}_N M_N \bar{N}$	1	-1		
$L(Y_N \tilde{M}_N Y_N)(Y_e \bar{e})(Y_N \bar{N})$	H	1/2	-1	
$LY_N\bar N$	L	$-1/2$	0	
$\bar{e}Y_{e}\tilde{Y}_{N}M_{N}\bar{N}$	1		-2	
$(Y_e \bar{e}) (\tilde{Y}_N M_N \tilde{Y}_N)(Y_e \bar{e})$		2	-2	
$L(Y_N \tilde{M}_N Y_N)L$		-1	$\mathcal{D}_{\mathcal{A}}$	
$M_N\bar N\,\bar N$	1	$\left(\right)$	-2	

 $\Lambda_R \gg m_{\text{soft}}$ is required for a valid low-energy description. Otherwise, Λ_R is an unknown scale, which may or may not be related to other cutoff scales in the theory.

As shown in Appendix [A,](#page-16-1) the complete list of holomorphic flavor singlets involving Y_N , M_N , or \overline{N} is that given in Table [VI](#page-7-2), where we denote the matrix of cofactors of a matrix Y as $\tilde{Y} \equiv (\text{det}Y)Y^{-1}$. From these flavor singlets, only one of the three renormalizable lepton number violating superpotential terms of (2.2) , $\lambda LL\bar{e}$, can be constructed,

$$
W_{\text{LNV}}^{(\text{hol})} = \frac{1}{2\Lambda_R} w(LL)(\tilde{Y}_N M_N \tilde{Y}_N)(Y_e \bar{e}), \tag{5.3}
$$

where w is an unknown $\mathcal{O}(1)$ coefficient.

In addition, as shown in Appendix [B](#page-16-0), bilinear superpotential terms, and, in particular, the lepton-number violating term LH_u , can be generated nonholomorpically after SUSY breaking. As we saw before in the absence of neutrino masses, a \mathbb{Z}_3^L symmetry ensures that lepton number is preserved mod 3, forbidding this term. However, while the \mathbb{Z}_3^L symmetry is not broken by Y_N , it is broken by M_N , which is charged under \mathbb{Z}_3^L . Therefore, bilinear lepton-number violating terms are allowed, though they necessarily involve at least one factor of $\mu_N \sim M_R/\Lambda_R$.

The nonholomorphic corrections to the superpotential take the form

$$
W_{\text{LNV}}^{(\text{non-hol})} = m_{\text{soft}} [\mathcal{V}^{\dagger}]^{a} L_{a} H_{u}, \tag{5.4}
$$

where there are two potentially leading contributions to the dimensionless spurion \mathcal{V} ,

$$
\mathcal{V}_a^{(1)} = \frac{1}{\Lambda_R} \varepsilon_{abc} [\tilde{Y}_N^\dagger]_i^b [M_N^\dagger]^{ij} [Y_N]_j^c,
$$

$$
\mathcal{V}_a^{(2)} = \frac{1}{\Lambda_R} \varepsilon_{abc} [Y_e Y_e^\dagger]_d^b [Y_N M_N^\dagger Y_N]^{cd}.
$$

(5.5)

 $\mathcal{V}^{(2)}$ contains more spurions, but if $Y_N \ll 1$ then the presence of the additional Y_e spurions can be easily compensated by the omission of one Y_N insertion, especially at large tan β .

The corresponding B-term can also be generated, and takes the form

$$
\mathcal{L}_{\text{soft}} \supset m_{\text{soft}}^2 [\mathcal{V}^\dagger] \tilde{L}_a H_u + \text{H.c.}
$$
 (5.6)

This will lead to a left-handed sneutrino VEV

$$
\langle L_a \rangle \sim -v_u \mathcal{V}_a,\tag{5.7}
$$

up to an unknown $\mathcal{O}(1)$ coefficient. Inserting this VEV into the canonical Kähler potential $L^{\dagger}L$, we obtain the gaugino/ lepton mixing

$$
\mathcal{L} \supset -v_u \lambda (\mathcal{V}^\dagger L) + \text{c.c.}
$$
 (5.8)

This mixing is of approximately the same order as the lepton/higgsino mixing arising from ([5.4](#page-7-3)). Lepton number violation can also appear in the Kähler potential,

$$
K_{\text{LNV}} \sim [\mathcal{V}^{\dagger}]^{a} L_{a} H_{d}^{\dagger} + \text{H.c.}, \tag{5.9}
$$

and in the corresponding soft-mass term. This will lead to further gaugino/lepton mixing, but proportional to v_d instead of v_{μ} .

In the presence of $$ simple to define which linear combination of the four fields L_i , H_d is the Higgs, and which are leptons [[27](#page-21-8)]. The physical effects of R-parity violation arise from a basis independent misalignment of the different mixings between the lepton and Higgs superfields. In our case there are several mixing terms, and cancellations can occur. As supersymmetric sources of bilinear lepton-number violation can be eliminated by the field redefinition $L \rightarrow L - \gamma H_d$, these cancellations will depend on the mechanism of supersymmetry breaking.

Indeed, some cancellation may naturally occur in gaugemediated supersymmetry-breaking models, since, due to the flavor-blind nature of gauge interactions, SUSY breaking effects are flavor-universal, up to RGE running and subleading corrections induced by the supersymmetric sources of flavor-breaking. We do not, however, assume a particular mechanism for SUSY breaking, and thus will take the mixings [\(5.4\)](#page-7-3) and ([5.8](#page-8-1)) and to be representative without substantial cancellation. Any such cancellation will only make the lepton-number violating effects smaller, and so ignoring such a possibility is a conservative assumption.

The mixing ([5.8](#page-8-1)) can lead to additional contributions to the left-handed neutrino masses via a weak-scale seesaw mechanism. We find

$$
\delta m_{\nu} \sim \frac{\gamma^2 v_{u}^2}{m_{\lambda}}.\tag{5.10}
$$

Imposing $|\delta m_{\nu}| \le 1$ eV, we obtain an upper bound

$$
\mathcal{V} \le 2 \times 10^{-6} \left(\frac{m_{\lambda}}{100 \text{ GeV}} \right)^{1/2}.
$$
 (5.11)

Proton decay, however, will impose a much stronger bound on $\mathcal V$, and consequently the weak seesaw contribution to the left-handed neutrino masses will be negligible.

In the above discussion, we have focused on the seesaw mechanism for generating small neutrino masses. If we instead integrate out the heavy neutrinos and consider the theory below the scale M_R , only one combination of the Y_N and M_N spurions, $Y_N M_N^{-1} Y_N^T$, is relevant for neutrino mass generation. If we ignored all other spurions built from Y_N and M_N , taking a viewpoint that is agnostic about the highscale mechanism for neutrino mass generation, we would obtain a theory for low-energy lepton-number violation which is more restrictive than that considered above. We have also neglected the effects of RGE running below the scale M_R . While such effects can be significant in detailed numerical calculations [\[28\]](#page-21-9), they will not substantially alter our order of magnitude estimates.

VI. CONSTRAINTS FROM PROTON DECAY

In combination with the baryon-number violating interactions studied in Secs. [III](#page-4-0) and [IV,](#page-5-0) the lepton-number violating interactions enumerated in Sec. [V](#page-6-0) will lead to a finite proton lifetime. The strongest constraint on the proton lifetime comes from the bound [[29](#page-21-10)]

$$
\tau_{p \to \pi^0 e^+} \ge 8.2 \times 10^{33} \text{ yrs.}
$$
 (6.1)

However, this bound only constrains the partial lifetime for the particular final state $\pi^0 e^+$. For other final states, the partial lifetime bounds are weaker, often substantially [[19\]](#page-21-0).

As we show below, MFV SUSY has a strong preference for final states with positive strangeness. Such decay modes are also strongly constrained [\[19](#page-21-0)[,30\]](#page-21-11),

$$
\tau_{p \to e^+ K^0} \ge 1.0 \times 10^{33} \text{ yrs}, \quad \tau_{n \to e^- K^+} \ge 3.2 \times 10^{31} \text{ yrs},
$$

\n
$$
\tau_{p \to \mu^+ K^0} \ge 1.3 \times 10^{33} \text{ yrs}, \quad \tau_{n \to \mu^- K^+} \ge 5.7 \times 10^{31} \text{ yrs},
$$

\n
$$
\tau_{p \to \nu K^+} \ge 2.3 \times 10^{33} \text{ yrs}, \quad \tau_{n \to \nu K^0} \ge 1.3 \times 10^{32} \text{ yrs},
$$

\n(6.2)

where we also show the (weaker) limits on bound-neutron partial lifetimes. There are similar bounds on some threebody decays of the form $N \rightarrow \ell + \pi + K$.

Before discussing the constraints arising from these bounds, we first estimate the size of the coefficients of the lepton-number violating operators. We use the generic parametrization of the neutrino Yukawa couplings of Casas and Ibarra [[31](#page-21-12)],

$$
Y_N^T = \frac{1}{v_u} \operatorname{diag}(\sqrt{M_{R1}}, \sqrt{M_{R2}}, \sqrt{M_{R3}})
$$

 $\times R \operatorname{diag}(\sqrt{m_{\nu 1}}, \sqrt{m_{\nu 2}}, \sqrt{m_{\nu 3}}) U^{\dagger},$ (6.3)

where R is a complex orthogonal matrix describing mixing among the right-handed neutrinos, U is the left-handed neutrino mixing matrix giving rise to atmospheric and solar

FIG. 4. The leading charged (left) and neutral (right) flavor-changing diagrams for $n \to \ell^- K^+$ and $p \to K^+ \bar{\nu}$ nucleon decay, respectively. Arrows indicate chirality. The charged flavor-changing diagram has less flavor suppression, but suffers from a chiral suppression due to the right \rightarrow right chargino propagator.

neutrino oscillations, and M_{Ri} and m_{vi} ($i = 1, 2, 3$) are the heavy right-handed neutrino masses and the light lefthanded neutrino masses, respectively. The mixing angles in U are large and the elements of U nonhierarchical.

Since R and the right-handed neutrino masses cannot be measured at low energies, we will assume a generic flavorstructure for Y_N . For simplicity we will assume that the right-handed neutrinos have masses of the same magnitude, and that the left-handed neutrinos also have roughly equal masses of order 0.1 eV, with order-one neutrino mixing angles. Substantially lighter neutrino masses would imply a more hierarchical spectrum, with small Yukawa couplings Y_N and consequently more suppressed leptonnumber violations, whereas substantially heavier neutrino masses begin to conflict with cosmological bounds.

The neutrino Yukawa coupling is then approximately

$$
Y_N \sim \frac{\sqrt{M_R m_\nu}}{v_u},\tag{6.4}
$$

where we assume that the entire Y_N matrix has elements of this order. The $LL\bar{e}$ coupling is therefore

$$
\lambda_{ijk} \sim \frac{M_R^3 m_\nu^2}{\Lambda_R v_u^4} y_k^{(e)},\tag{6.5}
$$

whereas the $\mathcal V$ spurions are

$$
\mathcal{V}_{i}^{(1)} \sim \frac{M_{R}^{5/2} m_{\nu}^{3/2}}{\Lambda_{R} v_{u}^{3}}, \qquad \mathcal{V}_{e,\mu}^{(2)} \sim \frac{M_{R}^{2} m_{\nu}}{\Lambda_{R} v_{u}^{2}} y_{\tau}^{2},
$$

$$
\mathcal{V}_{\tau}^{(2)} \sim \frac{M_{R}^{2} m_{\nu}}{\Lambda_{R} v_{u}^{2}} y_{\mu}^{2}.
$$
 (6.6)

Note that

$$
\lambda_{ijk} \sim y_k^{(e)} Y_N \mathcal{V}^{(1)},\tag{6.7}
$$

up to flavor structure. Therefore, due to the smallness of the Yukawa couplings, the $LL\bar{e}$ superpotential term will be a subdominant source of lepton-number violation.

We now search for the largest possible nucleon decay diagram. The simplest diagrams for nucleon decay to a meson and a lepton are those shown in Fig. [4,](#page-9-0) where the squark emits a chargino or neutralino, which mixes into an outgoing charged lepton or neutrino, respectively, via ([5.8](#page-8-1)).6 Requiring the external quarks to be light, with at most one strange quark, it is straightforward to check that the leading diagram for charged lepton emission involves a *tds* vertex with $\tilde{t} \rightarrow d$ flavor changing at the chargino vertex, whereas the leading diagram for neutrino emission also involves a tds vertex, but with $\tilde{t} \rightarrow \tilde{u}$ mass-mixing on the squark line.

The neutrino diagram has an additional flavor suppression of order $y_b^2/2$ relative to the charged-lepton diagram. However, the latter diagram, which leads to $n \rightarrow K^+ \mu^$ decay, suffers from a chiral suppression, as we illustrate in Fig. [4.](#page-9-0) The suppression occurs because the right-to-right chargino propagator is roughly $p/m_{\tilde{C}}^2$, leading to an additional suppression of at least $\sim m_p/m_{\tilde{C}}$ relative to the rightto-left propagator. This chiral suppression is not present in the $p \to K^+ \bar{\nu}$ diagram. Combined with the stronger partial lifetime bound for this decay mode, the latter diagram will give the strongest constraints.

The amplitude is

$$
\mathcal{M}_{p \to K^{+}\bar{p}} \sim \frac{\lambda^3 m_d m_s m_b^2}{2 m_t^3 m_{\tilde{N}}} \left(\frac{\tilde{\Lambda}}{m_{\tilde{q}}}\right)^2 \mathcal{V} \tan^4 \beta. \tag{6.8}
$$

up to order-one mixing angles and gauge couplings, where $\tilde{\Lambda}^2$ is a hadronic matrix element. We will take $\tilde{\Lambda} \sim$ 250 MeV, in rough agreement with lattice computations [\[32](#page-21-13)[,33\]](#page-21-14). The width is

$$
\Gamma \sim \frac{m_p}{8\pi} |\mathcal{M}|^2. \tag{6.9}
$$

Comparing with the experimental bound [\(6.2\)](#page-8-2), we obtain

$$
\mathcal{V}\tan^4\beta \le (3 \times 10^{-14}) \left(\frac{m_{\tilde{q}}}{100 \text{ GeV}}\right)^2 \left(\frac{m_{\tilde{N}}}{100 \text{ GeV}}\right). (6.10)
$$

⁶The lepton/Higgsino mixing ([5.4](#page-7-3)) gives another contribution to this mixing of a similar form.

FIG. 5 (color online). Left: the upper bound on M_R due to the nonobservation of nucleon decay, in units of 10⁶ GeV. For this plot, we have fixed $\Lambda_R = 10^{16}$ GeV and $m_\nu = 0.1$ eV. Near the left edge, the dominant constraint comes from the $V^{(1)}$ spurion; elsewhere $V^{(2)}$ is dominant. Right: the approximate lower bound on $m_{3/2}$, in KeV, due to the nonobservation of $p \to K^+ \tilde{G}$.

For sufficiently large $\tan\beta$, we have $\mathcal{V}^{(2)} \gg \mathcal{V}^{(1)}$ and $\mathcal{V}^{(2)}$ gives the dominant contribution to \mathcal{V} . Using $m_{\nu} = 0.1$ eV, we then obtain the upper bound on M_R

$$
M_R \leq (3 \times 10^7 \,\text{GeV}) \left(\frac{10}{\tan \beta}\right)^3 \left(\frac{m_{\tilde{q}, \tilde{N}}}{100 \,\text{GeV}}\right)^{3/2} \left(\frac{\Lambda_R}{10^{16} \,\text{GeV}}\right)^{1/2}.
$$
\n(6.11)

One can check that $\mathcal{V}^{(1)}$ gives a weaker bound than this as long as

$$
\tan \beta \gtrsim 6 \left(\frac{m_{\tilde{q},\chi}}{1 \text{ TeV}}\right)^{3/14} \left(\frac{\Lambda_R}{10^{16} \text{ GeV}}\right)^{1/14}.\tag{6.12}
$$

Thus, for $\Lambda_R = 10^{16}$ GeV and $m_{\tilde{a},\tilde{N}} \lesssim 1$ TeV, $V^{(2)}$ is dominant for tan $\beta \ge 6$, whereas for tan $\beta \le 6$, $V^{(1)}$ is dominant for sufficiently large superpartner masses. The bound on M_R , including both contributions, is illustrated in Fig. [5.](#page-10-0)

The bound on M_R depends strongly on Λ_R . For instance, if $\Lambda_R \sim 10 \text{ TeV}$, the bound ([6.11](#page-10-1)) is reduced by six orders of magnitude. If the right-handed neutrinos are sufficiently light, they could be produced at colliders, though the Yukawa couplings are necessarily very small, so that such a scenario is unlikely to be excluded in the near future.

If the gravitino is sufficiently light, proton decay can proceed via the baryon-number violating vertex ([2.4\)](#page-3-1) alone, without lepton number violation [\[34\]](#page-21-15). In particular, the gravitino is derivatively coupled to chiral superfields [\[35\]](#page-21-16)

$$
\mathcal{L}_{\text{int}} = -\frac{1}{\sqrt{3}m_{3/2}M_{\text{pl}}}\bar{\psi}_L \gamma^\mu \gamma^\nu (\partial_\mu \tilde{G})(D_\nu \phi) + \text{c.c., } (6.13)
$$

FIG. 6. The leading contribution to $p \rightarrow K^+ \tilde{G}$ decay.

where G is the gravitino, (ϕ, ψ) is any chiral superfield, and M_{pl} is the reduced Planck mass. If kinematically allowed, the decay $p \rightarrow K^+ \tilde{G}$ will proceed via the diagram in Fig. [6,](#page-10-2) with the width

$$
\Gamma \sim \frac{m_p}{8\pi} \left(\frac{\tilde{\Lambda}}{m_{\tilde{q}}}\right)^4 \left(\frac{\Lambda^2}{\sqrt{3}m_{3/2}M_{\rm pl}}\right)^2 \frac{\lambda^6 m_d^2 m_s^2 m_b^4}{4m_t^8} \tan^8 \beta, \quad (6.14)
$$

where we use the same matrix element as above, replacing the momentum insertions with a characteristic energy scale, Λ .

While we are unaware of a direct search for $p \rightarrow K^+ \tilde{G}$, for a very light gravitino $p \to K^+ \nu$ gives the same experimental signature. If we conservatively assume that the $p \to K^+ \nu$ bound ([6.2](#page-8-2)) applies to $p \to K^+ \tilde{G}$ decays for any gravitino mass, we obtain an approximate lower bound on $m_{3/2}$:

$$
m_{3/2} \gtrsim (300 \text{ KeV}) \left(\frac{300 \text{ GeV}}{m_{\tilde{q}}}\right)^2 \left(\frac{\tan \beta}{10}\right)^4, \qquad (6.15)
$$

where we take $\Lambda \sim \tilde{\Lambda} \sim 250$ MeV. This bound is illustrated in Fig. [5.](#page-10-0)

VII. LSP DECAY AND LHC PHENOMENOLOGY

The phenomenology of MFV SUSY models will be very different from the R-parity conserving MSSM, and is distinctive among R-parity violating theories. In this section, we attempt to explore the general phenomenological features of these models. The results depend on the spectrum,

$$
M_{\tilde{U}}^2 = \begin{pmatrix} m_{\tilde{Q}}^2 (1 + \alpha_u Y_u Y_u^\dagger + \alpha_d Y_d Y_d^\dagger) + d_{u,L} \\ A_u^\star Y_u^\dagger & m_{\tilde{u}}^2 \end{pmatrix}
$$

where the omitted terms are higher-order in the Yukawa couplings, A_u is some combination of holomorphic parameters specifying the left-right mixing (coming from the Yukawa couplings and A-terms), $\alpha_{u,d}$ and β_u are nonholomorphic parameters coming from the left- and righthanded squark masses, respectively, and $d_{u,L}$ and $d_{u,R}$ are the flavor-universal D-term contributions to the squark masses.

Naturalness, in this context, indicates that $\alpha_{u,d}$ and β_u should be order-one numbers, whereas $m_{\tilde{O}}$, $m_{\tilde{u}}$, and A_u are of order m_{soft} . Thus, the leading deviations from universality will involve only the $\mathcal{O}(1)$ top Yukawa coupling, and, in particular, it is very easy to make one of the stops very light. Since other nonuniversal terms are suppressed by Yukawa couplings and/or CKM factors, the remaining squarks are expected to be nearly degenerate. A similar argument applies to down-type squarks, where the bottom squark can be made light. In the charged slepton sector, the leading nonuniversal term comes from the y_τ suppressed left/right mixing, implying a nearly degenerate spectrum, except at very large $tan \beta$. The sneutrinos will be even more degenerate, since this left/right term is absent, and the leading nonuniversality comes from y_τ^2 suppressed soft-mass corrections.

Thus, it is very natural for the stop or the sbottom to be the LSP. A stau (or tau sneutrino) LSP, however, typically implies a nearly degenerate spectrum, and is somewhat less natural in this context. Other squarks or sleptons are not likely to be the LSP.

FIG. 7. The leading diagrams for stop (left) and left-handed sbottom (right) LSP decay. A right-handed sbottom decays similarly, without the mass insertion.

and we will not attempt to exhaustively enumerate all possibilities, instead focusing on the general features for various LSPs.

We will not assume that the LSP is electrically and color neutral; since it decays there is no particular motivation for that requirement. Thus the LSP could be either a squark, a slepton, a neutralino, a chargino, or the gluino. However, MFV places restrictions on the squark and slepton masses. In particular, the mass matrix for up-type squarks must be of the form

$$
\begin{pmatrix} \n\frac{1}{d} + d_{u,L} & A_u Y_u \\ \nm_{\tilde{u}}^2 (1 + \beta_u Y_u^{\dagger} Y_u) + d_{u,R} \n\end{pmatrix} + \dots, \tag{7.1}
$$

Since the largest R-parity violating operator is in the quark sector, the most interesting scenario is when the LSP is the stop or the sbottom. We consider the stop LSP case in detail. The direct decay of the stop is given by the diagram in Fig. [7.](#page-11-1) The partial widths $\Gamma(\tilde{t} \to \bar{d}_i \bar{d}_j)$ are given by

$$
\Gamma_{ij} \sim \frac{m_{\tilde{l}}}{8\pi} \sin^2 \theta_{\tilde{l}} |\lambda''_{3ij}|^2, \tag{7.2}
$$

where $\theta_{\tilde{t}}$ is the stop-mixing angle. To estimate the lifetime numerically, we use the renormalized quark masses at a scale $m_t \sim v \sim 174 \text{ GeV}$, which are approximately [\[36,](#page-21-17)[37\]](#page-21-18):

$$
m_u \sim 1.2 \text{ MeV}, \quad m_c \sim 600 \text{ MeV}, \quad m_t \sim v \sim 174 \text{ GeV},
$$

 $m_d \sim 3 \text{ MeV}, \quad m_s \sim 50 \text{ MeV}, \quad m_b \sim 2.8 \text{ GeV},$ (7.3)

Using these masses to compute the relevant Yukawa couplings, we find a lifetime

$$
\tau_{\tilde{t}} \sim (2 \ \mu \text{m}) \left(\frac{10}{\tan \beta}\right)^4 \left(\frac{300 \ \text{GeV}}{m_{\tilde{t}}}\right) \left(\frac{1}{2 \sin^2 \theta_{\tilde{t}}}\right). \tag{7.4}
$$

Thus no displaced vertices are expected except for very small values of tan β and a very light LSP. The decay length of the stop LSP is shown in Fig. [8.](#page-12-0)

Note that in this case one does not expect a large number of top quarks in the final state, nor, of course, any missing energy. Roughly 90% of decays will go to bottom and strange quarks, about 8% to bottom plus down, and a few percent to down plus strange. These branching ratios are fixed by the flavor structure. Thus, most of the events will contain b-quarks, and a generic signal for supersymmetry will be an overall increase in the number of events with b-jets, but with possible resonances in the jet spectrum at the squark masses. Since production of the superpartners would still be mainly through the R-parity conserving couplings, most SUSY events would actually end up with at least four jets, two of which are b-jets. Other superpartners will first decay to the stop. For example the neutralino is expected to decay to a stop plus charm as in Fig. [9.](#page-12-1) The neutralino lifetime for the case of a stop LSP is given by

FIG. 8 (color online). The decay length $(c\tau)$ of a stop (or right-handed sbottom) (left) or left-hand sbottom (right) LSP, in units of μ m. Displaced vertices are expected only for small tan β and a light LSP.

FIG. 9. Neutralino NLSP decay.

$$
\Gamma_{\tilde{N}} \sim \frac{m_{\tilde{N}}}{8\pi} g^2 \lambda^4 \frac{m_b^4}{m_t^4} \tan^4 \beta,
$$
\n
$$
\tau_{\tilde{N}} \sim (10^{-19} \text{ s}) \left(\frac{10}{\tan \beta}\right)^4 \left(\frac{300 \text{ GeV}}{m_{\tilde{N}}}\right).
$$
\n(7.5)

Thus, absent a nearly degenerate spectrum, the other superpartners are expected to be short-lived.

It is also possible for a bottom squark to be the LSP, decaying as shown in Fig. [7.](#page-11-1) For a right-handed sbottom, the lifetime is similar to that of a stop LSP lifetime, unless the decay is near threshold. The decay of a left-handed sbottom LSP is further suppressed by a left-right mass insertion. In this case, the partial widths $\Gamma(\tilde{b}_L \to \bar{u}_i \bar{d}_j)$ are

$$
\Gamma_{ij} \sim \frac{m_{\tilde{b}}}{8\pi} y_b^2 |\lambda''_{ij3}|^2, \tag{7.6}
$$

giving a total lifetime

$$
\tau_{\tilde{b}_L} \sim (41 \ \mu \text{m}) \left(\frac{10}{\tan \beta}\right)^6 \left(\frac{300 \ \text{GeV}}{m_{\tilde{b}_L}}\right). \tag{7.7}
$$

Thus, displaced vertices are expected at low tan β , as illustrated in Fig. [8.](#page-12-0) The phenomenology is distinct from that of a stop LSP: roughly 99% of decays will be to top and strange or top and down quarks, with less than 1% going to charm and strange quarks, and a small fraction to other final states. Thus, an increase in top quark production is expected, with most SUSY events containing at least two

FIG. 10. Neutralino/gluino (left) and chargino (right) LSP decays.

top-jets. However, fewer b-jets will be produced, except those arising from top decays.

Otherwise, the LSP can be a chargino, a neutralino, or a slepton. Each of these will give a distinct phenomenology. Assuming that the LSP is a neutralino, its decay will be dominated by the diagram in Fig. [10.](#page-12-2) The width is approximately

$$
\Gamma_{\tilde{N}} \sim \frac{m_{\tilde{N}}}{128\pi^3} |\lambda_{tsb}''|^2, \tag{7.8}
$$

where we estimate a phase-space suppression of $1/16\pi^2$ for each additional final-state particle. The lifetime is then

$$
\tau_{\tilde{N}} \sim (12 \ \mu \text{m}) \left(\frac{20}{\tan \beta}\right)^4 \left(\frac{300 \ \text{GeV}}{m_{\tilde{N}}}\right). \tag{7.9}
$$

As shown in Fig. [11](#page-13-0), this scenario is much more likely to produce displaced vertices, although they can still be avoided in a sizable region of parameter space. Thus, for the case of a neutralino LSP the expected signal of SUSY would be an increase in the top production cross section (since the LSP decay involves top quarks), including potentially same-sign tops, and possibly also displaced vertices for the lights jets. A gluino LSP would decay in a very similar fashion to a neutralino LSP, whereas a

⁷If $m_{\tilde{b}_L} \leq m_t$, the phenomenology will be different yet again, with displaced vertices more likely due the reduced width, but no extra top production.

FIG. 11 (color online). The decay length ($c\tau$) of a neutralino (left) or stau (right) LSP, in units of μ m. For a neutralino LSP, displaced vertices can arise in a substantial region of parameter space, whereas for the stau, they are expected nearly everywhere.

chargino LSP would have a similar lifetime, but would usually decay via two b-jets without a top quark, as shown in Fig. [10.](#page-12-2)

The case of a chargino LSP is very similar to that of a neutralino. The one significant difference, as can be seen from Fig. [10,](#page-12-2) is that in the chargino case we expect no top in the final state, and instead expect more b jets.

Finally, the LSP could be a slepton, mostly likely the lighter stau. This would probably be much easier to observe at the LHC. The leading decay of the stau would be a four-body decay involving top and bottom quarks, a light jet and either a lepton or missing energy, as shown in Fig. [12.](#page-13-1) Since it is a four-body decay, the NDA estimate for the width of the stau LSP is

$$
\Gamma_{\tilde{\tau}} \sim \frac{m_{\tilde{\tau}}}{2048 \pi^5} |\lambda''_{tsb}|^2, \tag{7.10}
$$

with lifetime of order

$$
\tau_{\tilde{\tau}} \sim (44 \ \mu\text{m}) \left(\frac{45}{\tan\beta}\right)^4 \left(\frac{500 \ \text{GeV}}{m_{\tilde{\tau}}}\right). \tag{7.11}
$$

Such long lifetimes will give displaced vertices in almost all of the relevant parameter space, as shown in Fig. [11](#page-13-0). Thus the signal of SUSY in the case of a stau LSP would be events with displaced vertices, top and bottom quarks, and either a lepton or missing energy.

Current searches for R-parity violating supersymmetry are not very restrictive for MFV SUSY. The more restrictive searches look for leptons among the final-state particles, and set bounds on the coupling λ' : this is exactly the one vanishing in MFV SUSY. For the case of a stop LSP one could expect a resonance in the dijet searches; however the production cross section of the stop is typically about three orders of magnitudes smaller [[38](#page-21-19)] than the experimental sensitivities both at the Tevatron [[39](#page-21-20)] and at the LHC [\[40](#page-21-21)[,41\]](#page-21-22).

The more relevant searches are the ones carried out by CMS [[42](#page-21-23)] (and also by CDF [\[43\]](#page-21-24)): here the R-parity violating decay of the gluino in the presence of a $\bar{u} d d$ coupling is considered by searching for a resonance in 3-jet final states, after appropriate kinematic cuts are introduced to separate potential SUSY events from QCD background. The most stringent CMS search (using 35 pb⁻¹ of data) yields a bound on the gluino mass $m_{\tilde{g}} > 280$ GeV. However, we should emphasize that in these models the gluino does not play an essential role. Thus even if the gluino is in the TeV energy range the model could be completely natural. While these searches are very promising, an eventual null-result of this particular experiment would not remove the motivation for these theories, since this search relies on the production of a light gluino.

FIG. 12. Slepton LSP decay without neutrinos (left) and with neutrinos (and thus missing energy) on the right.

FIG. 13. Gravitino decay via neutrino-photino mixing (left) for gravitinos below \sim 1 GeV, and to hadrons (right) for masses above ~1 GeV. The illustrated hadronic decay $\tilde{G} \rightarrow B^+ \Xi_c^-$, along with other decays arising from permutations of the *cbs* flavor labels and from changing the flavor of spectator quark, is dominant when kinematically allowed.

Another relevant search is for massive colored scalars in 4-jet events [\[44\]](#page-21-25). Here the four most energetic jets are paired up and a resonance in the average invariant masses of the two pairs is searched for. Stop pair production followed by decays to jets would contribute to this channel. The current bounds on the mass of a colored scalar octet using 2010 LHC data are in the 150–180 GeV range. However, the production cross section for scalar triplets is smaller, and this bound will be substantially weakened or eliminated if applied to the stop. Better background rejection can be achieved using b-tagging, since almost all the stop quarks include at least one b-jet. A recent simulation [[45](#page-21-26)] showed that such a search at the 14 TeV LHC will be able to discover stops decaying through the \bar{u} d d coupling up to 650 GeV with 300 fb⁻¹ data. A search for a lepton together with many jets has also been suggested [[46](#page-21-27)]. This search could probe MFV SUSY if the LSP is a slepton, or if it decays to top quarks, which can produce a lepton in the final state.

Throughout this paper we have been assuming a squark mass scale of order a few hundred GeV. This is necessary to make SUSY a natural solution of the hierarchy problem. However, in this case the Higgs mass in the simplest MSSM-type extension will usually be too light. One needs an extension of the Higgs sector, for example, to NMSSMtype models, to raise the Higgs mass over the 114 GeV LEP bound. Such an extension should not significantly alter the MFV structure of the theory. For example, while the \mathbb{Z}_3 symmetric version of the NMSSM has restricted couplings due to the (weakly broken) discrete symmetry, the superpotential [\(2.4\)](#page-3-1) is \mathbb{Z}_3 invariant, leaving the essential features of our model intact.

One of the outstanding problems of the SM and the MSSM is the issue of baryogenesis. The Higgs mass is too high in both of these theories to account for the observed matter/antimatter asymmetry directly, and the leading explanation is baryogenesis via leptogenesis. In MFV SUSY, the appearance of the λ'' baryon number violating operator, ([2.4](#page-3-1)), opens new possibilities for baryogenesis. Several scenarios that make use of this coupling have been proposed in [[47](#page-21-28)[–51\]](#page-21-29). For example the model of [\[51\]](#page-21-29) would rely on out-of-equilibrium decays of the lightest neutralino $\tilde{N} \rightarrow \bar{u} \, \bar{d} \, \bar{d}$ and needs λ'' couplings in the 10^{-4} – 10^{-3} range.

Finally we comment on dark matter. One of the main motivations for *-parity is that it provides a stable heavy* superpartner, which in many cases can be a candidate for a WIMP. In MFV SUSY we are obviously forgoing this possibility. However, this does not necessarily imply that there cannot be a good dark matter candidate in these models. While we are assuming the LSP within the SM superpartners to be the stop or another sparticle, the gravitino can still be lighter and be the real LSP. A gravitino dark matter scenario within R-parity violating SUSY has been advocated in [\[52\]](#page-21-30). There it was found that the leading decay of the gravitino is $\tilde{G} \rightarrow \gamma \nu$ (see Fig. [13\)](#page-14-0) with a width of

$$
\Gamma_{\tilde{G}} \sim \frac{1}{32\pi} |U_{\gamma\nu}|^2 \frac{m_{3/2}^3}{M_{\text{Pl}}^2},\tag{7.12}
$$

where $U_{\gamma\nu}$ is the photino-neutrino mixing due to the small sneutrino VEV. In our case the mixing is set by the spurion $V: U_{\gamma\nu} \sim v_u V/m_{\tilde{N}}$, where $m_{\tilde{N}}$ is a characteristic gaugino mass. Imposing the bound ([6.10](#page-9-1)), we obtain a lower bound on the gravitino lifetime,

$$
\tau_{\tilde{G}} \gtrsim (4 \times 10^{39} \text{ yr}) \left(\frac{1 \text{ GeV}}{m_{3/2}}\right)^3 \left(\frac{300 \text{ GeV}}{m_{\tilde{q}}}\right)^4 \left(\frac{\tan \beta}{10}\right)^8. \tag{7.13}
$$

If the gravitino is heavier than \sim 1 GeV it can decay to hadrons via the R-parity violating $\bar{u} \, \bar{d} \, \bar{d}$ vertex. While the exact decay mode will depend on what is kinematically available, for $m_{3/2} \ge 10$ GeV all hadronic two-body decays are kinematically allowed, and the dominant mode will be that shown in Fig. [13.](#page-14-0) The width for the illustrated decay is

$$
\Gamma_{\tilde{G}\rightarrow B^+\Xi_c^-} \sim \frac{m_{3/2}^3}{24\pi M_{\rm pl}^2} \left(\frac{\tilde{\Lambda}}{m_{\tilde{c}}}\right)^4 \frac{\lambda^2 m_c^2 m_s^2 m_b^2}{m_t^6} \tan^4 \beta. \tag{7.14}
$$

Taking the matrix element to be large, $\tilde{\Lambda} \sim 1 \text{ GeV}$, we find that

$$
\tau_{\tilde{G}} \sim (2 \times 10^{22} \text{ yrs}) \left(\frac{m_{\tilde{q}}}{300 \text{ GeV}}\right)^4 \left(\frac{10}{\tan\beta}\right)^4 \left(\frac{100 \text{ GeV}}{m_{3/2}}\right)^3. \tag{7.15}
$$

In either case a gravitino LSP is generically very longlived, with a lifetime much greater than the age of the Universe. Thus, the gravitino is a dark matter candidate, though more study is needed to determine if it is a realistic one.

If the gravitino is the LSP, the NLSP can either decay to jets via the R -parity violating vertex, (2.4) (2.4) (2.4) , or to the gravitino itself. The partial width for the simplest gravitino decay, e.g. $\tilde{t} \rightarrow t + \tilde{G}$, takes the form

$$
\Gamma \sim \frac{m_{\rm NLSP}^5}{24\,\pi m_{3/2}^2 M_{\rm pl}^2} \tag{7.16}
$$

for a squark or slepton NLSP, with a similar expression in the case of a gaugino NLSP. Thus, the rate is enhanced for a lighter gravitino, and if we assume that $m_{3/2}$ saturates the lower bound [\(6.15\)](#page-10-3), then we obtain a branching ratio

$$
\frac{\Gamma_{\tilde{t}\to t\tilde{G}}}{\Gamma_{\tilde{t}\to SM}} \sim (7 \times 10^{-10}) \left(\frac{m_{\tilde{t}}}{300 \text{ GeV}}\right)^8 \left(\frac{10}{\tan\beta}\right)^{12} \tag{7.17}
$$

for a stop NLSP. Thus, the branching ratio is generically small, but depends strongly on the NLSP mass and on $tan \beta$.⁸ For other NLSPs, this branching ratio is enhanced, whereas it can always be suppressed by increasing $m_{3/2}$. Depending on all the parameters, NLSP to gravitino decays could generate a significant gravitino relic density, which is of cosmological interest. We defer further consideration of this interesting topic to a future work.

VIII. CONCLUSIONS

We have presented an alternative approach to *-parity in* supersymmetric extensions of the standard model. We have shown that imposing minimal flavor violation in a manifestly supersymmetric way is powerful enough to reduce all baryon and lepton number violating amplitudes below current experimental bounds, while allowing a sufficiently rapid decay of the LSP such that no events with large missing transverse energy would be expected at the LHC.

The basic MFV assumption is that the only sources of flavor violation are the SM Yukawa coupling matrices $Y_{u,d,e}$. In a supersymmetric context these spurions should be treated as VEVs of chiral superfields. The flavor symmetry together with supersymmetry will pose very stringent restrictions on the low-energy effective Lagrangian, and R-parity will be an approximate accidental symmetry. The R-parity violating terms will be determined in terms of the flavor parameters of the theory, giving an underlying theory for these parameters.⁹

In the absence of neutrino masses only a single renormalizable R-parity violating flavor structure is allowed, and the proton is effectively stable, while $n - \bar{n}$ oscillations and dinucleon decay are sufficiently suppressed with mild restrictions on tan β . In the presence of neutrino masses there are more R-parity violating spurions, including a cubic superpotential term, and quadratic Kähler and soft-breaking terms. Proton decay will now place a mild bound on the right-handed neutrino mass scale.

The phenomenology of the model depends strongly on the nature of the LSP. The most plausible candidate for the LSP is the stop, which can decay to two quarks via the R-parity violating superpotential term. If the LSP is a neutralino/chargino, the decay might include displaced vertices and top quarks, while a slepton LSP would most likely decay with displaced vertices, and might also involve missing energy. While the LSP is necessarily unstable in such models, a gravitino LSP is sufficiently longlived to be a dark matter candidate.

There are a number of interesting directions for future work. The constraints on MFV SUSY arising from dinucleon decay are nontrivial, and a better understanding of the relevant hadronic matrix elements would help to establish a robust set of bounds on the parameter space of the model, as well as clarifying how the model can be probed using low-energy observables. Detailed collider studies are needed to determine the cleanest experimental signatures of this model at the LHC, especially in light of the various possibilities for the LSP. Furthermore, the cosmological implications for baryogenesis and dark matter should be explored in detail.

Finally, possible UV completions of the model should be explored. In R-parity conserving models, MFV is usually applied only to the SUSY breaking terms, which can be motivated by RGE evolution from flavor-universal soft terms, as in gauge mediation scenarios. In MFV SUSY, however, it is necessary to apply the MFV hypothesis to the superpotential as well, which cannot be similarly motivated. Nonetheless, an MFV structure can arise from weakly broken flavor symmetries, and constructing a well-motivated UV completion should prove to be an interesting challenge. If such a model can be found, it would give more information about the unknown flavorsinglet parameters.

ACKNOWLEDGMENTS

We thank Brando Bellazzini, Josh Berger, Andrey Katz, Mariangela Lisanti, Maxim Perelstein, David Shih, and Jesse Thaler for useful discussions, and Liam McAllister and Maxim Perelstein for comments on the manuscript. We also thank Yossi Nir for pointing out Refs. [[14](#page-20-7),[15](#page-20-8)] to us. This research was supported in part by the NSF Grant No. PHY-0757868. C.C. and Y.G. thank the Aspen Center for Physics for its hospitality while this work was in progress.

APPENDIXES—SYSTEMATICS OF MFV SUSY

MFV SUSY is a highly constrained theory, and its structure allows for a systematic approach to many problems. We outline several examples of this in these appendices. In Appendix [A,](#page-16-1) we show that the form of the

⁸For a very heavy NLSP at low tan β , it is possible for gravitino decay to dominate, though not in a particularly promising region of parameter space.

For other theories of the \overline{R} -parity violating terms see [\[53,](#page-21-31)[54\]](#page-21-32).

superpotential is highly constrained by systematically classifying holomorphic flavor singlets. In Appendix [B,](#page-16-0) we examine the effect of supersymmetry breaking on arguments based on holomorphy. In Appendix [C,](#page-17-0) we develop a heuristic scheme for estimating the flavor suppression of a given diagram, and in Appendix [D](#page-18-0) we apply this technique to demonstrate that the diagrams presented in Secs. [IV](#page-5-0)and [VI](#page-8-0) are the leading contributions to low-energy baryonnumber violating observables. Finally, in Appendix [E](#page-20-13), we show that higher-dimensional baryon and lepton-number violating operators are not dangerous for a sufficiently high cutoff $\Lambda \leq M_{\text{GUT}}$.

APPENDIX A: CLASSIFYING HOLOMORPHIC FLAVOR SINGLETS

To classify all terms which can appear in the superpotential, we now systematically construct all holomorphic flavor singlets, treating the spurions as holomorphic. In the quark sector, the irreducible holomorphic $SU(3)_u \times$ $SU(3)_d$ singlets are $Y_u\bar{u}$, $Y_d\bar{d}$, det \bar{u} , det \bar{d} , and the flavorsinglet spurions $detY_{u,d}$. Ignoring the flavor-singlet spurions, and combining $Y_u \bar{u}$ and $Y_d d$ with Q to form $SU(3)_O$ singlets, it is straightforward to show that Table [III](#page-3-0) contains a complete list of the irreducible $SU(3)_Q \times SU(3)_u \times$ $SU(3)_d$ singlets.

The lepton sector is more complicated. We first write down all possible holomorphic $SU(3)_N$ singlets. Note that for any 3×3 matrix M

$$
M^{ij}M^{kl}\varepsilon_{ikm} = \varepsilon^{jln}\tilde{M}_{nm},\tag{A1}
$$

where \tilde{M} is the matrix of cofactors, satisfying $\tilde{M}M =$ $M\tilde{M} = (det M)1$. Thus, while in general a flavor singlet can contain an arbitrary number of ε -tensors, by repeated application of [\(A1](#page-16-2)) we can reduce such a singlet to a form where no two M_N 's, \tilde{M}_N 's, Y_N 's, or \tilde{Y}_N 's are contracted with the same $SU(3)_N$ ε -tensor, apart from factors of det Y_N and det M_N . Since at most one \overline{N} can contract with a given ε -tensor, the only surviving ε -tensors must be contracted as follows:

$$
\tilde{M}_{N}^{ij}\tilde{Y}_{a}^{k}\bar{N}^{l}\epsilon_{jkl} = -\epsilon_{abc}(\tilde{M}_{N}^{ij}Y_{j}^{b})(Y_{k}^{c}\bar{N}^{k}),\qquad\text{(A2)}
$$

which is a reducible product of $SU(3)_N$ singlets. Incorporating $Y_e \bar{e}$ and L, we obtain a relatively short list of irreducible $SU(3)_N \times SU(3)_e$ singlets, as shown in Table [VII.](#page-16-3)

The next step is to classify irreducible $SU(3)_L$ singlets. Note that

$$
(\tilde{Y}_N M_N \tilde{Y}_N)(Y_N \tilde{M}_N Y_N) = (\det Y_N)^2 (\det M_N) \mathbf{1}.
$$
 (A3)

Thus, up to normalization, $\tilde{Y}_N M_N \tilde{Y}_N$ is the matrix of cofactors of $Y_N \tilde{M}_N Y_N$, and we can omit singlets containing more than one of either contracting with the same $SU(3)_L$ ε -tensor. There is then a finite list of possible irreducible flavor singlets. Of these, some will be reducible due to the

TABLE VII. The irreducible $SU(3)_N \times SU(3)_e$ singlets (we omit flavor-singlet spurions.)

	SU(2) _L	$U(1)_Y$	SU(3) _L	\mathbb{Z}_2^R
$\bar{N}M_N\bar{N}$				
$Y_N\bar N$				
$Y_e \bar{e}$			H	
L	H	$-1/2$	帀	
$\tilde{Y}_N M_N \bar{N}$			ក	
$\tilde{Y}_N M_N \tilde{Y}_N$				
$Y_N \tilde{M}_N Y_N$				

identities satisfied by Y_N and \tilde{Y}_N and M_N and \tilde{M}_N . For instance, any contraction involving $Y_N\tilde{Y}_N$ or \tilde{Y}_NY_N is obviously reducible, since $Y_N \tilde{Y}_N = \tilde{Y}_N Y_N = (\det Y_N) \mathbf{1}.$ Furthermore, certain ε -tensor contractions of Y_N with itself or \tilde{Y}_N with itself will be reducible. In particular, we have

$$
(Y_N\bar{N})(Y_N\tilde{M}_N Y_N)(Y_N\bar{N}) \sim \bar{N}\tilde{Y}_N\tilde{M}_N\tilde{Y}_N\bar{N}
$$

\n
$$
\sim (\bar{N}M_N\tilde{Y}_N)(\tilde{Y}_N M_N\bar{N})
$$

\n
$$
-(\bar{N}M_N\bar{Y})(\tilde{Y}_N M_N\bar{Y}_N),
$$

\n
$$
(\tilde{Y}_N M_N\tilde{Y}_N)\tilde{Y}_N M_N\bar{N} \sim (\det Y_N)(M_N\tilde{Y}_N)(M_N\bar{N})Y_N
$$

\n
$$
\sim (\det Y_N)Y_N\tilde{M}_N\tilde{Y}_N\bar{N}
$$

\n
$$
\sim (\det Y_N)(Y_N\tilde{M}_N Y_N)(Y_N\bar{N}), \quad (A4)
$$

up to unimportant factors.

Keeping these reductions in mind, it is straightforward to verify that Table [VI](#page-7-2) contains a complete list of $SU(3)_L \times$ $\text{SU}(3)_{e} \times \text{SU}(3)_{N}$ invariants, apart from $LY_{e}\bar{e}$, which appears in Table [III.](#page-3-0)

APPENDIX B: NONHOLOMORPHIC OPERATORS FROM SUSY BREAKING

In the absence of supersymmetry breaking, the superpotential is constrained to be holomorphic, and only holomorphic combinations of spurions can appear there. We now explore the role of supersymmetry breaking in introducing nonholomorphic spurion combinations into the superpotential. To keep the discussion of supersymmetry breaking generic, we introduce a supersymmetry-breaking spurion X , a chiral superfield which acquires an F -term vev $\langle X \rangle_F = F$. We assume that X couples to the MSSM fields via nonrenormalizable operators, where the cutoff M is the messenger scale.

The resulting soft supersymmetry-breaking terms will appear a scale $m_{soft} \sim F/M$. In particular, since we assume the absence of renormalizable couplings between X and the MSSM, the leading contributions to supersymmetry breaking come from the superpotential interactions

$$
W_{\text{SUSY}} \supset \frac{X}{M} A_{ijk} \Phi^i \Phi^j \Phi^k + \frac{X}{M} M_{\lambda}^{(i)} \text{Tr} W_{(i)}^2 \tag{B1}
$$

and the Kähler potential interactions

$$
K_{\text{SUSY}} \supset \frac{X^{\dagger}}{M} \tilde{\mu}_{ij} \Phi^i \Phi^j + \frac{X}{M} \tilde{J}_i^j \Phi^i \Phi_j^{\dagger} + \frac{X^{\dagger} X}{M^2} \tilde{B}_{ij} \Phi^i \Phi^j
$$

+ c.c. + $\frac{X^{\dagger} X}{M^2} \tilde{M}_i^j \Phi^i \Phi_j^{\dagger}$ (B2)

where nonholomorphic couplings are denoted with a tilde. The couplings A_{ijk} and M_{λ} generate A-terms and gaugino masses, whereas \tilde{B}_{ij} and \tilde{M}_{i}^{j} generate B-terms and softmasses, $\tilde{\mu}_{ij}$ generates bilinear superpotential terms, and \tilde{J}_i^j gives rise to a scalar/ F -term mixing, the effects of which we discuss in detail below. In singlet extensions of the MSSM, including the NMSSM and seesaw models, supersymmetry-breaking tadpoles can also arise:

$$
K_{\text{SUSY}}^{\text{(tad)}} = \frac{X^{\dagger} X}{M} \tilde{E}_i \Phi^i, \tag{B3}
$$

where the dimensionful coefficient is large, $F^2/M \sim$ $Mm_{\text{soft}}^2 \gg m_{\text{soft}}^3$. While these tadpoles are potentially problematic, whether they are generated and at what level will depend on the particular model of supersymmetry breaking. We will assume that they are suppressed by some mechanism, and will not consider them further.¹⁰

Thus, we conclude that A-terms are generated holomorphically, whereas the other soft terms are generated nonholomorphically. Furthermore, nonholomorphic bilinear couplings can appear in the superpotential at the scale m_{soft} . Nonholomorphic contributions to the A-terms and trilinear superpotential terms are suppressed. The leading contributions arise from the interactions

$$
K_{\text{SUSY}} \supset \frac{X^{\dagger}}{M^2} \tilde{\lambda}_{ijk} \Phi^i \Phi^j \Phi^k + \frac{XX^{\dagger}}{M^3} \tilde{A}_{ijk} \Phi^i \Phi^j \Phi^k
$$

which are suppressed by $\mathcal{O}(m_{soft}/M)$ relative to the leading holomorphic contributions.

So far we have ignored the nonholomorphic scalar/F-term mixing \tilde{J}_i^j . We will show that these couplings give rise to nongeneric nonholomorphic contributions to the A-terms after a field redefinition, similar in form to (nonholomorphic) wave function renormalization effects.

We first write the renormalizable superpotential and Kähler potential in the form

$$
W = m_{\text{soft}} \mu_{ij} \Phi^i \Phi^j + \lambda_{ijk} \Phi^i \Phi^j \Phi^k \qquad K = \tilde{K}_i^j \Phi^i \Phi_j^{\dagger},
$$

where \tilde{K}_i^j is the Hermitean positive-definite Kähler metric. (Note that we cannot in general set $\tilde{K}_i^j = \delta_i^j$ by a field redefinition without introducing nonholomorphic couplings into the superpotential.) The scalar/ F -term mixing can be eliminated by redefining

$$
\Phi^i \to \Phi^i + \frac{X}{M} \tilde{P}^i_j \Phi^j
$$

for $\tilde{P}^i_j = -[\tilde{K}^{-1}]^i_k \tilde{J}^k_j$. This redefinition produces additional A-terms of the form

$$
W_{\text{SUSY}} \supset \frac{X}{M} [\lambda_{ljk} \tilde{P}_i^l + \lambda_{ilk} \tilde{P}_j^l + \lambda_{ijl} \tilde{P}_k^l] \Phi^i \Phi^j \Phi^k
$$

as well as corrections to the soft-masses and B-terms. By contrast, writing the Kähler potential in the form

$$
\tilde{K}^i_j = \delta^i_j + \tilde{k}^i_j
$$

and assuming that \tilde{k}_j^i is a subleading correction, we obtain similar nonholomorphic corrections to the superpotential itself (as well as the A-terms) upon moving to a canonical basis. Thus, we conclude that the qualitative effects of nonholomorphic scalar/ F -term mixing are captured by nonholomorphic corrections to the Kähler potential, though \tilde{J}_j^i leads to some additional "splitting" between the A-terms and superpotential terms.

APPENDIX C: A HEURISTIC ESTIMATION SCHEME

In Secs. [IV](#page-5-0) and [VI](#page-8-0), we estimated the dominant contribution to low-energy baryon-number violating processes by choosing the simplest diagrams and then finding the dominant flavor structure. The resulting diagrams were heavily suppressed by Yukawa couplings, CKM factors, and heavy propagators. Thus, in principle other diagrams could give competitive contributions. However, classifying all possible diagrams is a difficult task. Instead, we develop a scheme to estimate the flavor-suppression of a diagram based on its flavor structure alone. This will allow us to isolate potentially competitive diagrams, which can then be computed by more conventional means.

To do so, it is helpful to reinterpret a Feynman diagram for a candidate process in terms of the flow of ''flavor,'' i.e. of $SU(3)_Q \times SU(3)_u \times SU(3)_d$ charge. If quarks and squarks carry ''flavor'' and antiquarks and antisquarks carry ''antiflavor,'' then flavor can only be created or destroyed at baryon number violating vertices, such as [\(2.4\)](#page-3-1). Otherwise, the rest of the diagram contains unbroken flavor lines, which either form closed loops or join to external quark lines.

Along flavor lines, flavor is altered through left \leftrightarrow right mixing, charged CKM mixing, and neutral squark massmixing, where each subprocess has an associated cost. In particular, for squarks, left \leftrightarrow right mixing is suppressed by the associated Yukawa coupling, whereas charged-current flavor changing (on left-handed squarks) is CKM suppressed. FCNCs are suppressed by ([4.5](#page-5-7)), and flavor changing of right-handed squarks is suppressed by the associated Yukawa couplings to convert them to left-handed squarks, together with the suppression for left-handed flavor changing.

If we assume similar suppressions for flavor-changing processes involving quarks, we obtain a useful heuristic

 10 For instance, a right-handed snuetrino tadpole is forbidden by $\mathbb{Z}_3^{(L)}$ in the case of Dirac neutrino masses $(M_N = 0)$.

MINIMAL FLAVOR VIOLATION SUPERSYMMETRY: A ... PHYSICAL REVIEW D 85, 095009 (2012)

estimate scheme for the MFV-dictated flavor-suppression of any given diagram. In particular, the least suppressed diagrams for a given process will involve a minimum number of baryon-number violating vertices, and a minimum of flavor changing. For each baryon number violating vertex ([2.4](#page-3-1)), all three flavor lines should connect to external quarks; otherwise the diagram involves extra insertions of [\(2.4\)](#page-3-1), and is subdominant.

Thus, we can estimate the amplitude for the diagram by specifying the flavor structure, by which we mean the flavors of the right-handed quarks/squarks connected to the baryon-number violating vertex [\(2.4\)](#page-3-1), as well as the flavors of the external quarks on the flavor lines emanating from the BNV vertex. In addition to the vertex factor, the required charged and/or neutral flavor changes then come with a right \rightarrow left Yukawa suppression, together with a CKM suppression for charged flavor-changing or a suppression of the form [\(4.4\)](#page-5-3) for neutral flavor-changing, whereas quarks/squarks which do not change flavor receive no additional Yukawa suppression.

Given a flavor structure, the heuristic estimation scheme outlined above should give an approximate upper bound on the amplitude, once suppression from the superpartner propagators and loop suppression (if applicable) is accounted for. As the number of possible flavor structures is finite, and much smaller than the number of possible diagrams, it becomes straightforward to obtain an approximate upper bound on the amplitude for all relevant flavor structures.

If we can find a diagram with amplitude equal to the upper bound, then this diagram is probably the dominant contribution to the process in question. The simplest diagrams will often involve only squark flavor-changing, since otherwise additional W bosons are required. In this case, the heuristic scheme outlined above is essentially exact (up to unknown MFV coefficients, which are assumed to be order one). However, if quark flavor changing is involved, the amplitude is somewhat dependent on the details. In particular, while CKM suppression is still present, Yukawa suppression is less obvious. We now consider this point in detail.

For a light quark, the left \leftrightarrow right propagator takes the approximate form m_q/E^2 , where $E \sim \Lambda_{\text{QCD}} \gg m_q$ is the characteristic energy for the baryon-number violating process. By contrast, for a heavy quark ($m_q \gg E$) the left \leftrightarrow right propagator will take the approximate form $1/m_q$. In either case, the contribution to the overall amplitude will be made dimensionless by a factor of $\sim E$ in the numerator, arising either from loop integrals or from a hadronic matrix element. Thus, the overall left \leftrightarrow right suppression appears to be only m_q/E and E/m_q for light and heavy quarks, respectively, whereas (for light quarks), the assumed Yukawa suppression is much smaller. However, in general left \leftrightarrow right mixing will be followed by charged flavor-changing—this is the reason for including it in the

diagram—with an associated $g^2/M_W^2 = 2/v^2$ from the W boson propagator, where the dimensions will again be cancelled by factors of E. Counting one-half of the W propagator suppression. (the other end of W boson line will lead to flavor changing elsewhere in the diagram), we obtain a net suppression of approximately

$$
\frac{m_q}{v/\sqrt{2}} \quad \text{or} \quad \frac{E^2}{m_q v/\sqrt{2}},\tag{C1}
$$

for light and heavy quarks, respectively. Thus, for a light quark, the net suppression is the same as Yukawa suppression (for tan $\beta = 1$), whereas for a heavy quark, the diagram is suppressed by an additional factor of $\sim (E/m_q)^2$. At large tan β , the suppression is greater than Yukawa suppression for all quarks except for the up-quark, but the difference here is only $1/\sqrt{2}$, and is effectively negligible.

The above argument is more subtle in the case of a loop diagram, since q^2 within the loop may be much higher than Λ_{QCD}^2 . Roughly, the net effect is to change the distinction between ''light'' and ''heavy'' quarks; for instance, if $q^2 \sim M_W^2$ within the loop, then only the top quark is "heavy." Yet more subtleties arise for flavor-changing neutral currents of right-handed quarks, since there are then more mass insertions than W vertices. However, the discrepancy is not very important if the mass insertions lie within a loop dominated by loop momentum $q^2 \ge M_W^2$. Thus, the estimation scheme outlined above also applies qualitatively to quark flavor changing, where the Yukawa suppression now comes partly from W boson propagators and/or loop suppression. Although the exact amplitude will depend on the specifics, this heuristic scheme is a useful way to isolate the larger diagrams contributing to a process of interest.

APPENDIX D: A SYSTEMATIC SEARCH FOR ADDITIONAL LARGE DIAGRAMS

We now apply the estimation scheme developed in Appendix [C](#page-17-0) to search for additional large diagrams which are potentially competitive with those considered in Secs. [IV](#page-5-0) and [VI.](#page-8-0)

1. $n - \bar{n}$ oscillations

We first consider $n - \bar{n}$ oscillations. The amplitude must be built from two insertions of [\(2.4\)](#page-3-1), each of which carries at least one second-generation down-type quark/squark, with all flavor lines connected to external quarks (there are no spectator quarks). As the external quarks are precisely two up-quarks and four down-quarks, the second and third-generation quarks must all flavor change to firstgeneration quarks. Furthermore, converting the two squarks into quarks requires the exchange of at least one gaugino or Higgsino; any additional three or four-point interactions can only be present at one-loop or higher.

TABLE VIII. The minimum flavor-dependent suppression required for flavor changing to first-generation quarks, where the rows and columns correspond to the flavors of the quarks/ squarks attached to the BNV vertex.

	sh	bd	ds
\mathcal{U}	$y_u y_s^2 y_h^2 \lambda^4/2$	$y_u y_h^2 y_d \lambda^4/2$	$y_u y_d y_s^2 \lambda^4/2$
\mathcal{C}	$y_c^2 y_s^2 y_h^2 \lambda^6/2$	$y_c^2 y_b^2 y_d \lambda^4/2$	$y_c^2 y_d y_s^2 \lambda^4$
\boldsymbol{t}	$y_s^2 y_h^2 \lambda^{10}/2$	$y_h^2 y_d \lambda^8/2$	$y_d y_s^2 \lambda^4$

Because of the strong Yukawa suppression of the treelevel amplitude ([4.7](#page-5-4)), it is conceivable that one-loop amplitudes can be competitive with it. We now search for the largest such diagrams. In any $n - \bar{n}$ oscillation diagram of interest, the external quarks must all be first-generation quarks. Thus, for a given flavor structure for the BNV vertex, we can estimate a minimum flavor suppression by assuming charged flavor-changing to first-generation quarks for each leg, since neutral flavor changing is never dominant over charged flavor changing in this context. The resulting flavor-dependent minimum suppression is shown in Table [VIII](#page-19-0). It is straightforward to check that, for the assumed range $3 \le \tan \beta \le 45$, $tds \sim tbd$ gives the weakest suppression, whereas the next weakest, ϵbd , is $\leq 1/20$ as large.

There is only one possible one-loop diagram with two flavor-changing quarks (Fig. [14](#page-19-1)). Assuming that the dominant contribution to the loop integral occurs in the range $M_W^2 \le q^2 \le m_t^2$, we estimate:

$$
\mathcal{M} \sim \frac{g^2}{16\pi^2} \tilde{\Lambda} t_\beta^5 \lambda^8 \frac{m_d^2 m_s^4}{m_t^6} \left(\frac{\tilde{\Lambda}}{m_{\tilde{q}}}\right)^4 \left(\frac{\tilde{\Lambda}}{m_\chi}\right), \qquad (D1)
$$

for two *tds* vertices, where the tan β dependence is less strong than our naive estimate because the strange-quark left \leftrightarrow right mass insertion is not enhanced at large tan β , unlike the corresponding Yukawa coupling. While ([D1\)](#page-19-2) is competitive with ([4.7](#page-5-4)) at tan $\beta = 3$, it grows more slowly at large tan β , and becomes subdominant. Other combinations of tds and tbd give a similar result. Since other flavor structures ought to lead to further suppression, we conclude that the tree-level result [\(4.7\)](#page-5-4) is the dominant contribution to $n - \bar{n}$ oscillations at large tan β , where the

FIG. 14. The leading one-loop contribution to $n - \bar{n}$ oscillation.

predicted oscillation time is closest to present experimental bounds.

2. Dinucleon decay

We now consider additional contributions to dinucleon decay. Conservation of electric charge requires that each up-type \rightarrow down-type flavor change has a corresponding $down-type \rightarrow up-type$ flavor change, which can in principle occur on one of the ''spectator'' flavor lines (those not connected to the BNV vertices). However, each such occurrence is strongly suppressed—by about $g\Lambda_{\text{OCD}}/M_W$ due to the W boson propagator, since at most half of the propagator suppression accounts for necessary Yukawa suppression on the ''primary'' flavor lines (those connected to the BNV vertices), as discussed in Appendix [C](#page-17-0).

Keeping this suppression in mind, we can search for additional large diagrams by exhaustively cataloging the possible flavor structures for each BNV vertex, grouped together on the basis of the flavors of their external light quarks, estimating the suppression for each flavor structure according to the scheme of Appendix [C](#page-17-0). To find the largest diagrams, we find the least suppressed flavor structures for each set of external quarks, and then take the products of all pairs of these suppressions, bearing in mind that for final-state strangeness $|S| \geq 3$, two-body decays are not possible (leading to phase-space suppression), and appending a factor of $-g\Lambda_{\rm QCD}/M_W$ for each unit of net charge of the external quarks.

Besides the two diagrams already considered in Sec. [IV B,](#page-5-8) such a search turns up no flavor structures with a lesser suppression for any $3 \leq \tan \beta \leq 45$. Thus we conclude that, to the extent to which the scheme of Appendix [C](#page-17-0) is valid, the two dominant diagrams are the charged and neutral flavor-changing diagrams already considered.

3. Proton decay

Finally, we consider additional contributions to proton decay. In the quark sector, we require a single baryon number violating vertex ([2.4](#page-3-1)), with a corresponding squark propagator suppression. Requiring that the external quarks be light with strangeness $|\Delta S| \le 1$ and applying the method of Appendix [C](#page-17-0), we find that a *tds* vertex with $t \rightarrow d$ flavor-changing is the least suppressed, with $t \rightarrow u$ neutral flavor-changing competitive at large tan β . These are the same flavor structures that were considered in Sec. [VI.](#page-8-0)

However, as argued in Sec. [VI,](#page-8-0) the charged-lepton diagram suffers from a chiral suppression. This will occur whenever the squark is up-type and undergoes charged flavor changing, emitting an ℓ^- (via mixing with the chargino), i.e. when the net-charge of the external quarks connected to the baryon-number violating vertex is -1 , since charge conservation otherwise requires the exchange of a W boson with one of the spectator quarks, resulting in a comparable suppression, as discussed in Sec. [D 2.](#page-19-3) Accounting for the chiral suppression and reapplying the methods of Appendix [C](#page-17-0), we conclude that the neutral flavor-changing diagram considered in Sec. [VI](#page-8-0) is always dominant.

As the bounds on $|\Delta S| = 0$ decays are somewhat stronger, one might be tempted to consider diagrams of this type. However, according to our estimation scheme, the largest $|\Delta S| = 0$ processes—tbd with $b \rightarrow u$, d, and $t \rightarrow d$ flavor changing or tds with $t \rightarrow d$, and $s \rightarrow u$ flavor changing—receive an additional flavor suppression of about $y_s \lambda$, or at least 10^{-2} for the assumed range $3 \leq$ $tan \beta \le 45$. Consequently, $|\Delta S| = 1$ decays are strongly preferred, and their nonobservation will lead to the strongest constraints.

APPENDIX E: HIGHER-DIMENSIONAL **OPERATORS**

We now consider whether higher-dimensional operators can affect our conclusions. We first consider $|\Delta B| = 2$ processes. Lepton-number violating interactions are irrelevant, since they are strongly suppressed by Y_N and $\mu_N =$ M_N/Λ_R . At dimension five, there is only one allowed baryon-number violating correction, which appears in the Kähler potential:

$$
K_{\text{BNV}}^{(5)} = \frac{1}{\Lambda} (Y_u Y_u^{\dagger} + Y_d Y_d^{\dagger}) Q Q Y_d^{\dagger} \bar{d}^{\dagger}.
$$
 (E1)

After integrating out the auxiliary fields, this term (combined with the $QY_d\bar{d}H_d$ Yukawa coupling), has a similar effect to a Q^3H_d superpotential term, but with at least two Y_d spurions, leading to a minimum Yukawa suppression of

 y_b^2 . Together with the dimension-five $\sim v/\Lambda$ suppression and CKM suppression (of the same form as for ([2.4](#page-3-1))), it is straightforward to check that the vertex factor must be substantially smaller than any of those contributing to the dominant diagrams considered in Sec. [IV—](#page-5-0)in the latter case we also include any additional suppression from flavor changing—so long as $\Lambda \ge 10^{12}$ GeV.¹¹ Thus, for a GUT scale cutoff, such contributions are strongly subdominant, whereas dimension six and higher operators are sufficiently suppressed without any flavor suppression.

In the case of nucleon decay, higher-dimensional $|\Delta L| = 1$ operators are potentially dangerous. However, they necessarily come with a suppression of at least $\mu_N Y_N^2$ (ignoring flavor structure) in addition to their $\sim v/\Lambda$ cutoff suppression, and are therefore subdominant to the leptongaugino mixing induced by the $\mathcal{V}^{(2)}$ spurion. Thus, for a high cutoff, higher-dimensional lepton-number violating operators can only be significant if they lead to an enhancement in the quark sector. Specifically, operators which violate lepton and baryon number can be dangerous, but these occur first at dimension six, both in the Kähler potential and the superpotential. Notably, the dangerous (R-parity even) dimension-five operators Q^3L , $\bar{u} \bar{u} d\bar{d} \bar{e}$, and $\bar{u} \bar{d} d\bar{N}$ are absent from the superpotential due to holomorphy constraints. Dimensionsix operators are not dangerous in this context, since the smallness of $\mathcal V$ spurion (cf. ([6.10\)](#page-9-1)) combined with cutoff suppression is sufficient to easily evade bounds on the proton lifetime.

- [1] L. J. Hall and M. Suzuki, [Nucl. Phys.](http://dx.doi.org/10.1016/0550-3213(84)90513-3) B231, 419 [\(1984\)](http://dx.doi.org/10.1016/0550-3213(84)90513-3).
- [2] G. G. Ross and J. Valle, *[Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(85)91658-2)* **151**, 375 (1985).
- [3] V.D. Barger, G. Giudice, and T. Han, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.40.2987) 40, [2987 \(1989\)](http://dx.doi.org/10.1103/PhysRevD.40.2987).
- [4] H. K. Dreiner, in Perspectives on Supersymmetry, edited by G. L. Kane (World Scientific, Singapore, 1998), pp. 462–479.
- [5] G. Bhattacharyya, in Beyond the Desert 1997: Accelerator and Non-Accelerator Approaches, Proceedings of the First International Conference on Particle Physics Beyond the Standard Model, held June 8–14, 1997, at Castle Ringberg, Germany, edited by H. V. Llapdor-Lleingrothaus and H. Päs (Institute of Physics Publishing, 1998), p. 194.
- [6] C. Aulakh and R. N. Mohapatra, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(82)90262-3) 119, 136 [\(1982\)](http://dx.doi.org/10.1016/0370-2693(82)90262-3).
- [7] R. Barbier, C. Berat, M. Besancon, M. Chemtob, and A. Deandrea et al., [Phys. Rep.](http://dx.doi.org/10.1016/j.physrep.2005.08.006) 420, 1 (2005).
- [8] S. Chatrchyan et al. (CMS Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.221804) 107[, 221804 \(2011\)](http://dx.doi.org/10.1103/PhysRevLett.107.221804).
- [9] G. Aad et al. (ATLAS Collaboration), [arXiv:1109.6572.](http://arXiv.org/abs/1109.6572)
- [10] R. Chivukula and H. Georgi, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(87)90713-1) 188, 99 [\(1987\)](http://dx.doi.org/10.1016/0370-2693(87)90713-1).
- [11] L. Hall and L. Randall, *[Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.65.2939)* **65**, 2939 (1990).
- [12] A. Buras, P. Gambino, M. Gorbahn, S. Jager, and L. Silvestrini, [Phys. Lett. B](http://dx.doi.org/10.1016/S0370-2693(01)00061-2) 500, 161 (2001).
- [13] G. D'Ambrosio, G. Giudice, G. Isidori, and A. Strumia, Nucl. Phys. B645[, 155 \(2002\).](http://dx.doi.org/10.1016/S0550-3213(02)00836-2)
- [14] E. Nikolidakis and C. Smith, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.77.015021) 77, 015021 [\(2008\)](http://dx.doi.org/10.1103/PhysRevD.77.015021).
- [15] C. Smith, [arXiv:0809.3152.](http://arXiv.org/abs/0809.3152)
- [16] Y. Grossman, Y. Nir, and R. Rattazzi, [Adv. Ser. Dir. High](http://dx.doi.org/10.1142/9789812812667_0011) [Energy Phys.](http://dx.doi.org/10.1142/9789812812667_0011) 15, 755 (1998).
- [17] A. L. Kagan, G. Perez, T. Volansky, and J. Zupan, [Phys.](http://dx.doi.org/10.1103/PhysRevD.80.076002) Rev. D 80[, 076002 \(2009\)](http://dx.doi.org/10.1103/PhysRevD.80.076002).
- [18] S. Glashow, J. Iliopoulos, and L. Maiani, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.2.1285) 2, [1285 \(1970\)](http://dx.doi.org/10.1103/PhysRevD.2.1285).

¹¹A more detailed analysis might reveal that an even lower cutoff is permissible.

- [19] K. Nakamura et al. (Particle Data Group), [J. Phys. G](http://dx.doi.org/10.1088/0954-3899/37/7A/075021) 37, [075021 \(2010\)](http://dx.doi.org/10.1088/0954-3899/37/7A/075021).
- [20] F. Zwirner, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(83)90230-7) 132, 103 (1983).
- [21] S.-.K. Abe et al. (Kamiokande collaboration), [arXiv:1109.4227.](http://arXiv.org/abs/1109.4227)
- [22] M. D. Litos, Ph.D. thesis, Boston University, 2010.
- [23] J. Goity and M. Sher, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(94)01688-9) 346, 69 (1995).
- [24] R. Barbieri and A. Masiero, [Nucl. Phys.](http://dx.doi.org/10.1016/0550-3213(86)90136-7) B267, 679 [\(1986\)](http://dx.doi.org/10.1016/0550-3213(86)90136-7).
- [25] V. Cirigliano, B. Grinstein, G. Isidori, and M. B. Wise, Nucl. Phys. B728[, 121 \(2005\).](http://dx.doi.org/10.1016/j.nuclphysb.2005.08.037)
- [26] G.C. Branco, A.J. Buras, S. Jager, S. Uhlig, and A. Weiler, [J. High Energy Phys. 09 \(2007\) 004.](http://dx.doi.org/10.1088/1126-6708/2007/09/004)
- [27] T. Banks, Y. Grossman, E. Nardi, and Y. Nir, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.52.5319) 52[, 5319 \(1995\).](http://dx.doi.org/10.1103/PhysRevD.52.5319)
- [28] Y. Grossman and S. Ray, [J. High Energy Phys. 10 \(2011\)](http://dx.doi.org/10.1007/JHEP10(2011)019) [019.](http://dx.doi.org/10.1007/JHEP10(2011)019)
- [29] H. Nishino et al. (Super-Kamiokande Collaboration), Phys. Rev. Lett. 102[, 141801 \(2009\).](http://dx.doi.org/10.1103/PhysRevLett.102.141801)
- [30] K. Kobayashi et al. (Super-Kamiokande Collaboration), Phys. Rev. D 72[, 052007 \(2005\).](http://dx.doi.org/10.1103/PhysRevD.72.052007)
- [31] J. Casas and A. Ibarra, Nucl. Phys. **B618**[, 171 \(2001\).](http://dx.doi.org/10.1016/S0550-3213(01)00475-8)
- [32] P. Cooney, Ph.D. thesis, University of Edinburgh, 2009, [http://hdl.handle.net/1842/4042.](http://hdl.handle.net/1842/4042)
- [33] Y. Aoki et al. (RBC-UKQCD), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.78.054505) 78, 054505 [\(2008\)](http://dx.doi.org/10.1103/PhysRevD.78.054505).
- [34] K. Choi, E. J. Chun, and J. S. Lee, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.55.R3924) 55, R3924 [\(1997\)](http://dx.doi.org/10.1103/PhysRevD.55.R3924).
- [35] G. Giudice and R. Rattazzi, *Phys. Rep.* **322**[, 419 \(1999\).](http://dx.doi.org/10.1016/S0370-1573(99)00042-3)
- [36] Z.-z. Xing, H. Zhang, and S. Zhou, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.77.113016) 77, [113016 \(2008\)](http://dx.doi.org/10.1103/PhysRevD.77.113016).
- [37] H. Fusaoka and Y. Koide, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.57.3986) 57, 3986 [\(1998\)](http://dx.doi.org/10.1103/PhysRevD.57.3986).
- [38] W. Beenakker, S. Brensing, M. Kramer, A. Kulesza, E. Laenen, and I. Niessen, [J. High Energy Phys. 08 \(2010\) 098.](http://dx.doi.org/10.1007/JHEP08(2010)098)
- [39] T. Aaltonen et al. (CDF Collaboration), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.79.112002) 79, [112002 \(2009\).](http://dx.doi.org/10.1103/PhysRevD.79.112002)
- [40] V. Khachatryan et al. (CMS Collaboration), [Phys. Rev.](http://dx.doi.org/10.1103/PhysRevLett.105.211801) Lett. 105[, 211801 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.105.211801)
- [41] G. Aad et al. (ATLAS Collaboration), [New J. Phys.](http://dx.doi.org/10.1088/1367-2630/13/5/053044) 13, [053044 \(2011\).](http://dx.doi.org/10.1088/1367-2630/13/5/053044)
- [42] S. Chatrchyan et al. (CMS Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.101801) 107[, 101801 \(2011\)](http://dx.doi.org/10.1103/PhysRevLett.107.101801).
- [43] T. Aaltonen et al. (CDF), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.042001) **107**, 042001 [\(2011\)](http://dx.doi.org/10.1103/PhysRevLett.107.042001).
- [44] G. Aad et al. (ATLAS Collaboration), [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s10052-011-1828-6) 71, [1828 \(2011\)](http://dx.doi.org/10.1140/epjc/s10052-011-1828-6).
- [45] D. Choudhury, M. Datta, and M. Maity, [J. High Energy](http://dx.doi.org/10.1007/JHEP10(2011)004) [Phys. 10 \(2011\) 004.](http://dx.doi.org/10.1007/JHEP10(2011)004)
- [46] M. Lisanti, P. Schuster, M. Strassler, and N. Toro, [arXiv:1107.5055.](http://arXiv.org/abs/1107.5055)
- [47] S. Dimopoulos and L.J. Hall, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(87)90593-4) 196, 135 [\(1987\)](http://dx.doi.org/10.1016/0370-2693(87)90593-4).
- [48] J.M. Cline and S. Raby, Phys. Rev. D 43[, 1781 \(1991\).](http://dx.doi.org/10.1103/PhysRevD.43.1781)
- [49] R.J. Scherrer, J.M. Cline, S. Raby, and D. Seckel, [Phys.](http://dx.doi.org/10.1103/PhysRevD.44.3760) Rev. D 44[, 3760 \(1991\).](http://dx.doi.org/10.1103/PhysRevD.44.3760)
- [50] S. Mollerach and E. Roulet, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(92)91145-Y) 281, 303 [\(1992\)](http://dx.doi.org/10.1016/0370-2693(92)91145-Y).
- [51] R. Adhikari and U. Sarkar, [Phys. Lett. B](http://dx.doi.org/10.1016/S0370-2693(98)00305-0) 427, 59 [\(1998\)](http://dx.doi.org/10.1016/S0370-2693(98)00305-0).
- [52] F. Takayama and M. Yamaguchi, [Phys. Lett. B](http://dx.doi.org/10.1016/S0370-2693(00)00726-7) 485, 388 [\(2000\)](http://dx.doi.org/10.1016/S0370-2693(00)00726-7).
- [53] P. Fileviez Perez and S. Spinner, [Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2009.02.047) 673, 251 [\(2009\)](http://dx.doi.org/10.1016/j.physletb.2009.02.047).
- [54] P. Fileviez Perez and M. B. Wise, [J. High Energy Phys. 08](http://dx.doi.org/10.1007/JHEP08(2011)068) [\(2011\) 068.](http://dx.doi.org/10.1007/JHEP08(2011)068)