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Higgs mass prediction for realistic string $/M$ theory vacua

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Recently it has been recognized that in compactified string/ M theories that satisfy cosmological constraints, it is possible to derive some robust and generic predictions for particle physics and cosmology with very mild assumptions. When the matter and gauge content below the compactification scale is that of the minimal supersymmetric standard model (MSSM), it is possible to make precise predictions. In this case, we predict that there will be a single standard model-like Higgs boson with a calculable mass 105 GeV $\leq M_h \leq 129$ GeV depending on tan β (the ratio of the Higgs vevs in the MSSM). For tan $\beta > 7$, the prediction is 122 GeV $\leq M_h \leq 129$ GeV.

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I. MOTIVATION

Most physicists agree that understanding the origin of electroweak symmetry breaking is essential for progress in going beyond the standard model. The LHC experiments have made tremendous progress in constraining the Higgs mass in the past year or so. The combined results from the LEP, the Tevatron, and the LHC will soon cover the entire region below about 500 GeV. We will demonstrate that, with some broad and mild assumptions motivated by cosmological constraints, generic compactified string/ M theories with stabilized moduli and low-scale supersymmetry imply a standard model-like single Higgs boson with a mass 105 GeV $\leq M_h \leq 129$ GeV if the matter and gauge spectrum surviving below the compactification scale is that of the minimal supersymmetric standard model (MSSM), as seen from Fig. [1.](#page-2-0) For an extended gauge and/or matter spectrum, there can be additional contributions to M_h . Furthermore, in G_2 -MSSM models [\[1](#page-6-0)], we find that the range of possible Higgs masses is apparently much smaller, 122 GeV $\leq M_h \leq 129$ GeV.

The standard model suffers from ''naturalness'' or "hierarchy" problem(s). In addition to the well-known technical naturalness problem of the Higgs, there is the basic question of the origin of the electroweak scale. In the context considered here, the embedding of the (supersymmetric) standard model in a UV complete microscopic theory like string/M theory has to explain why the electroweak scale is so much smaller than the natural scale in string theory, the string scale, which is usually assumed to be many of orders of magnitude above the TeV scale. The μ parameter (which sets the masses of Higgsinos and contributes to the masses of Higgs bosons) must also be around TeV scale. The models we describe here, with softly broken supersymmetry, include solutions for all of these problems. Although understanding phenomenologically relevant supersymmetry breaking in string theory is a challenging task, many results, including those needed to calculate the Higgs boson mass, can be obtained with

rather mild, well motivated assumptions. The rest of this section outlines and motivates these simple assumptions.

In connecting string/M theory to low-energy particle physics, one has to compactify the extra dimensions. Motivated by grand unification and its successful embedding into string/M theory, we assume that the string/M scale, the Kaluza-Klein scale, and the unification scale are all within an order of magnitude of 10^{16} GeV. Within the theoretical precision desired, numerical results for M_h are not sensitive to variations of an order of magnitude or so in these scales.

Even though the energy scale of the extra dimensions is assumed to be much above the center-of-mass energy of collisions at the LHC, the extra dimensions still manifest themselves at lower energies through the presence of ''moduli'' fields. These are modes of the extra dimensional graviton whose vacuum-expectation values (vevs) determine the shapes and sizes that the extra dimensions take. Being modes of the extra dimensional graviton, the moduli couple to matter with Planck suppressed interactions universally. The moduli have to be stabilized since all couplings and masses are determined from their vevs.

In recent years, significant progress has been made in understanding moduli stabilization and supersymmetry breaking in different corners of string/M theory, see [\[2–](#page-6-1)[11](#page-6-2)]. In this work, we will be interested in supersymmetry breaking mechanisms which give rise to TeV-scale supersymmetry, and hence solve the naturalness problems in the standard model. The basic mechanisms were de-scribed in [[7](#page-6-3)[,8\]](#page-6-4) for *M* theory and in [[3](#page-6-5),[4](#page-6-6)[,6\]](#page-6-7) for type IIB compactifications, where it was shown that all moduli can be stabilized and supersymmetry can be broken with \sim TeV-scale superpartners with a natural choice of parameters—in which the only dimensionful scale is M_{pl} . In a vacuum with broken supersymmetry and vanishing cosmological constant, the mass of the gravitino $(m_{3/2})$, which is the superpartner of the massless graviton, is the order parameter of supersymmetry breaking and sets the mass scale for all superpartners and also indirectly the Higgs mass.

A natural prediction of such compactifications is that the mass of the lightest modulus is close to $m_{3/2}$. In fact, this is a generic result for compactified string/M theories with stabilized moduli within the supergravity approximation. In vacua in which the superpotential W is not tuned, it essentially arises from the fact that there is a relationship between the dynamics stabilizing the moduli and the dynamics breaking supersymmetry due to the extremely tiny value of the cosmological constant. Thus, the modulus mass becomes related to the gravitino mass. For more details, see [[12](#page-6-8)[,13](#page-6-9)]. For the generic case with many moduli, at least some of the moduli are stabilized by perturbative effects in the Kähler potential $[6,8]$ $[6,8]$ $[6,8]$ $[6,8]$. Then, it can be shown that the lightest modulus¹ has a mass of the same order as $m_{3/2}$ [[14](#page-6-10)[,15\]](#page-6-11).

Generic predictions

The fact that, generically, the lightest modulus mass is of the same order as the gravitino mass has significant implications for the phenomena described by a typical string/M theory vacuum, with some rather mild assumptions. In addition to the requirement of stabilizing all moduli in a vacuum with TeV-scale supersymmetry (as described in the previous section) which picks the set of string compactifications we choose to study, the assumptions are essentially that the supergravity approximation is valid and that the Hubble scale during inflation is larger than $m_{3/2}$.

In particular, the above implies that the light moduli fields (of order $m_{3/2}$) are generically displaced during inflation, causing the Universe to become moduli dominated shortly after the end of inflation due to coherent oscillations of the moduli. Requiring that these decay before big-bang nucleosynthesis (BBN) so as to not ruin its predictions, puts a lower bound on $m_{3/2}$ of about 25 TeV or so. Thus, the cosmological moduli problem [[16](#page-6-12)] generically requires that $m_{3/2} > 25$ TeV. Since $m_{3/2} \approx \frac{F}{M_{\text{pl}}}$ for vacua with a vanishingly small cosmological constant, this further implies that the supersymmetry breaking scale \sqrt{F} has to be "high," as is natural in gravity mediation models. Low-scale supersymmetry breaking scenarios like gauge mediation do not seem to be compatible with these cosmological constraints.

Historically, other approaches have been suggested to solve the moduli problem, but they have largely been shown to not work, or to be very nongeneric. Most recently, [\[13\]](#page-6-9) excluded a number of approaches involving late in-flation [[17](#page-6-13)]. One approach involving saxion inflation was not yet excluded but fails for M theory [[18](#page-6-14)]. A recent highly speculative proposal assumes an otherwise unknown ad hoc interaction [\[19\]](#page-6-15).

As an aside, the requirement of stabilizing a large number of moduli in a realistic compactification with a simple mechanism naturally picks mechanisms in which many axions² are exponentially lighter than $m_{3/2}$, one of which can naturally be the QCD axion [[6](#page-6-7),[20](#page-6-16)]. Hence, this provides a string theory solution of the strong-CP problem with stabilized moduli and axions, and also naturally predicts an $\mathcal{O}(1)$ fraction of dark matter (DM) in the form of axions, the abundance of which must now be computed with a nonthermal cosmological history [[20](#page-6-16)].

Generically, within high-scale supersymmetry breaking mechanisms such as gravity mediation, the squark, slepton, and heavy Higgs masses are also of order $m_{3/2}$. It has been argued that in special cases, squarks and sleptons may be ''sequestered'' from supersymmetry breaking, giving rise to a suppression in their masses relative to $m_{3/2}$. However, it was shown in [\[21\]](#page-6-17) that, in string/M theory compactifications with moduli stabilization, the squark and slepton masses are generically not sequestered from supersymmetry breaking once all relevant effects are taken into account. This has important implications for collider physics, implying, in particular, that squarks and sleptons should not be directly observed at the LHC [\[15,](#page-6-11)[22\]](#page-6-18).

While scalar superpartner masses are tied to $m_{3/2}$, gaugino masses need not be. Within many classes of string compactifications which satisfy all the requirements stated above, it can be shown that the gaugino masses [\[1,](#page-6-0)[23\]](#page-6-19) and μ [[24](#page-6-20)] are suppressed by 1 to 2 orders of magnitude relative to $m_{3/2}$. The gaugino masses are suppressed compared to scalar masses because they do not get mass from some of the mechanisms that break supersymmetry, and μ may be suppressed because it must vanish by symmetry argument when supersymmetry is unbroken or moduli are not stabilized. In this case, it can be shown that the lightest supersymmetric particle could naturally provide the DM abundance with a nonthermal mechanism [\[25,](#page-6-21)[26\]](#page-6-22). However, it is not clear at present if this is a generic feature of all realistic compactifications. For example, it is possible in classes of string compactifications to stabilize moduli in such a way that the gaugino masses are of the same order as $m_{3/2}$ [\[27\]](#page-6-23). Similarly, it is possible for μ to be concreted at the same order as $m_{1/2}$ [28]. A review of generated at the same order as $m_{3/2}$ [[28](#page-6-24)]. A review of particle physics and cosmology in this general framework will appear shortly in [\[29\]](#page-6-25).

II. THE HIGGS AND BEYOND STANDARD MODEL PHYSICS

We are interested in making predictions for the Higgs mass arising from realistic compactifications satisfying the conditions above. In a supersymmetric theory, two Higgs

¹More precisely, we mean the real part of the chiral superfield making up the complex modulus in the 4D theory.

²The axions are the imaginary parts of the complex moduli.

doublets are required for anomaly cancellation; so by the ''Higgs mass'' we mean the mass of the lightest CP-even neutral scalar in the Higgs sector. A remarkable fact about the Higgs mass in general supersymmetric theories is that an upper limit on M_h of order $2M_Z$ exists just from the requirement of validity of perturbation theory up to the high scale of order 10^{16} GeV [[30](#page-6-26)]. This is due to the fact that the Higgs mass at tree level only depends on SM gauge couplings (which have been measured), and possibly other Yukawa or gauge couplings (which are bounded from above by perturbativity). However, in addition to the gauge and matter spectrum, the precise value of the Higgs mass depends crucially on radiative effects, which in turn depend on all the soft parameters including the μ and $B\mu$ parameters.

In this work we assume that the visible sector consists of the SM gauge group with the MSSM matter content below the unification scale, as suggested by gauge coupling unification and radiative electroweak symmetry breaking (EWSB) in the MSSM. In addition, we consider compactifications in which the gravitino mass $m_{3/2}$ is not too far above the lower bound of \sim 25 TeV from the moduli decay constraint, and the gaugino masses are suppressed by 1 to 2 orders of magnitude relative to $m_{3/2}$. For μ we study two cases, one in which μ is suppressed by 1 to 2 orders of magnitude relative to $m_{3/2}$ as predicted in [\[24\]](#page-6-20), and the other in which μ is of the same order as $m_{3/2}$ [[28](#page-6-24)]. We
denote these two agents as "Small", u and "Large", u denote these two cases as "Small" μ and "Large" μ , respectively (the Higgs mass in the Large μ scenario was studied within the *M*-theory framework in [\[1\]](#page-6-0)). The two cases are studied as they pick out different regions of $tan \beta$ and, hence, give different predictions for the Higgs mass as seen from Fig. [1.](#page-2-0) For more discussion, see Sec. [IV.](#page-4-0)

Note that only one of the five scalars in the Higgs sector of the MSSM is light, the rest are all of order $m_{3/2}$. Hence, we are in the ''decoupling limit'' of the MSSM where the lightest CP-even Higgs scalar has precisely the same properties as the SM Higgs. 3 The low-energy theory arising from M theory studied in [\[1\]](#page-6-0) naturally gives rise to these features, but the results apply to all compactifications with scalars heavier than about 25 TeV and \leq TeV gauginos. The Higgs mass can then be reliably computed with a small and controlled theoretical uncertainty. This will be the subject of the following sections.

From a bottom up point of view, some authors have noted that heavy scalars have some attractive features [\[32\]](#page-7-0) and related phenomenology has been studied in [\[33](#page-7-1)[,34\]](#page-7-2). Their conclusions are consistent with ours where they overlap. The framework considered here is quite different from split supersymmetry [[35](#page-7-3)] and high-scale

FIG. 1 (color online). The prediction for the Higgs mass at two loops for realistic string/M theory vacua defined in the text, as a function of tan β for three different values of the gravitino mass $m_{3/2}$, and varying the theoretical and experimental inputs as described below. SPHENO 2.2.3 was used to evolve grand unified theory scale parameters to M_{SUSY} . For precise numbers and more details, see Sec. [IV.](#page-4-0) The central band within the dashed curves for which scatter points are plotted corresponds to $m_{3/2}$ = 50 TeV. This band includes the total uncertainty in the Higgs mass arising from the variation of three theoretical inputs at the unification scale, and from those in the top mass m_t and the $SU(3)$ gauge coupling α_s within the allowed uncertainties. The innermost (white) band bounded by solid curves includes the uncertainty in the Higgs mass for $m_{3/2} = 50$ TeV only from theoretical inputs. The upper (dark gray) band bounded by solid curves corresponds to the total uncertainty in the Higgs mass for $m_{3/2} = 100$ TeV while the lower (light gray) band bounded by solid curves corresponds to that for $m_{3/2}=25$ TeV. For $m_{3/2} =$ 50 TeV, the red scatter points (with $tan \beta$ less than about 4.5) and blue scatter points (with $tan \beta$ greater than about 4.5) correspond to Large μ and Small μ , respectively, as described in Secs. [II](#page-1-0) and [IV.](#page-4-0) The lower bound of the Higgs mass is from [[46](#page-7-5)]. We assume the currently almost excluded regime 117.5–118.5 GeV will soon be fully excluded.

supersymmetry [\[36\]](#page-7-4) which have much heavier scalars. In split supersymmetry *both* gaugino masses and trilinears are suppressed relative to scalars by a symmetry—in this case an R symmetry, together with supersymmetry breaking of the D type as described in [[35](#page-7-3)]. In contrast, in the class of compactifications considered here, the gaugino masses are suppressed by dynamics, since the F term for the modulus determining the gaugino masses is suppressed relative to the dominant F term. Hence, gaugino masses can only be suppressed by 1 to 2 orders of magnitude, not arbitrarily as in split supersymmetry. For the same reason, the gluinos are not "long lived" in the realistic string/M theory vacual under consideration here. Also, the trilinears are not suppressed at all. With large trilinears, one has to be careful about charge and color breaking minima, and we have confirmed the absence of these in models of interest. Another notable difference from split supersymmetry and high-scale supersymmetry is that, in those models, (radiative) electroweak symmetry breaking is not implemented

³In the decoupling limit, the Higgs mixing angle denoted by α in [[31](#page-7-6)] is given by $\alpha = \beta - \frac{\pi}{2}$, where $\beta \equiv \tan^{-1}(\frac{v_u}{v_d})$. v_u , and v_d are the vacuum expectation values (vevs) of the two neutral Higgs fields H_u^0 and H_d^0 in the MSSM.

when computing the Higgs mass since a huge fine-tuning is present by assumption. In contrast, in the string/M theory models considered in this work, (radiative) electroweak symmetry breaking occurs naturally in a large subset of the parameter space. However, the ease in obtaining the correct value of the Higgs vev (or Z-boson mass) depends on the value of μ . For Small μ , it can be shown that the fine-tuning involved in obtaining the correct Higgs vev is significantly reduced compared to the naive expectation for heavy scalars due to an automatic cancellation between scalar masses and trilinears which are both close to $m_{3/2}$ in this setup; for details see [[34](#page-7-2)]. This can naturally give rise to $\mu \leq \text{TeV}$, even when the scalar mass parameters are
 $> 30 \text{ TeV}$. For Large μ , the fine-tuning is quite severe as \approx 30 TeV. For Large μ , the fine-tuning is quite severe as one would expect. We include both cases here one would expect. We include both cases here.

III. COMPUTATION OF THE HIGGS MASS

Computing the Higgs mass in the MSSM with scalar masses and trilinears at $M_{\text{susy}} \geq 25 \text{ TeV}$, and gauginos and μ suppressed by 1 to 2 orders of magnitude relative to the scalar masses, is nontrivial. Although conceptually quite different, some of the technical issues involved have an overlap with split-supersymmetry and high-scale supersymmetry.

Since the scalar masses are much larger than a TeV, they could lead to nontrivial quantum corrections in the gaugino-Higgsino and Higgs sectors enhanced by ''large logarithms'' of the ratio between the electroweak scale and the scalar mass scale. Many numerical codes tend to become less reliable for scalar masses larger than a few TeV for the above reason. However, in contrast to split supersymmetry and high-scale supersymmetry models, the scalar masses here are 25–100 TeV which is not that large, since $\log(\frac{M_{\text{susy}}}{M_{\text{EW}}})$ is not large. So, numerical codes should still provide a reasonable estimate. The ratio of the two Higgs fields vevs, $tan \beta$ cannot yet be calculated accurately, and significantly affects the value of M_h if tan $\beta \leq 10$, so we include the variation from $tan \beta$. This dependence actually allows an approximate measurement or useful limit on $tan \beta$ which is otherwise very difficult to do.

In light of the above, we adopt the following procedure. At the unification scale around 10^{16} GeV, in accord with theoretical expectations we fix the soft parameters—the scalar masses equal to $m_{3/2}$, the trilinears A close to $m_{3/2}$, and the gaugino masses suppressed by 1 to 2 orders of magnitude relative to the scalar masses as described in [[1\]](#page-6-0). Then, for a given value of $tan \beta$, the numerical codes SOFTSUSY 3.2.4 [[37](#page-7-7)] and SPHENO 2.2.3 [\[38\]](#page-7-8) are used to renormalize these quantities down to $M_{\text{susy}} \approx m_{3/2}$, where electroweak symmetry breaking is implemented. This determines μ and $B\mu$. The quantities are chosen such that the values of μ and $B\mu$ are consistent with the theoretical expectations. One consequence of this is that tan β is not expected to span the fully phenomenologically allowed range from \sim 2 to \sim 60, but only a restricted range from \sim 2 to \sim 15 [\[34\]](#page-7-2). In any case, from Fig. [1,](#page-2-0) since the Higgs mass saturates for $tan \beta \ge$ 12, plotting higher values of tan β will not provide new information.

Then, we compute the Higgs mass in the ''match-andrun" approach using values of gaugino masses, μ and $B\mu$ at M_{susv} determined from above. We follow a procedure similar to that in [[39](#page-7-9)] except that we only consider those parameters at the unification scale which after renormalization group evolution to M_{susv} give rise to viable electroweak symmetry breaking. We also compute the Higgs mass directly with SOFTSUSY using theoretical inputs at the unification scale, and compare to the results obtained with the "match-and-run" approach, the detailed procedure for which is described below.

A. Matching at M_{susy}

At the scale M_{susy} , the full supersymmetric theory is matched to a low-energy theory with fewer particles, consisting of the SM particles, the gauginos, and the Higgsinos for the Small μ case, and only the SM particles and the gauginos for the Large μ case. The matching condition for the quartic coupling of the Higgs in the low-energy theory is given at M_{susy} by

$$
\lambda = \frac{1}{4} [g_2^2 + \frac{3}{5} g_1^2] \cos^2 2\beta + \delta_{\text{th}}^{\lambda}, \tag{1}
$$

where g_1 , g_2 are the $U(1)_Y$ and $SU(2)_L$ gauge couplings evaluated at M_{susy} . The threshold corrections to the quartic coupling at one loop consist of leading log (LL) as well as finite corrections. The above matching condition is strictly valid only in the \overline{DR} scheme, so there is an additional correction if one wants to convert to the \overline{MS} scheme as explained in the Appendix of [[40](#page-7-10)]. We use the standard choice $M_{\text{susy}} = \sqrt{M_{\tilde{t}_1} M_{\tilde{t}_2}}$, where $M_{\tilde{t}_1}$, $M_{\tilde{t}_2}$ are the masses of the two stap squares and include all the relevant L and the two stop squarks, and include all the relevant LL and finite threshold corrections. The dominant finite threshold effects to the Higgs quartic coupling comes from stop squarks, and is given by

$$
\delta_{\text{th}}^{\lambda} \approx \frac{3y_t^4}{8\pi^2} \left(\frac{A_t^2}{m_{\tilde{t}}^2} - \frac{A_t^4}{12m_{\tilde{t}}^4} \right). \tag{2}
$$

Since the trilinears A are of the same order as scalars, this is a nontrivial correction when the scalars and trilinears are around 25 TeV. Other finite threshold corrections are smaller, and have been neglected as they do not affect the result to within the accuracy desired.

The matching conditions for the gaugino-Higgsino-Higgs couplings (denoted by κ in general) at M_{susy} in the \overline{DR} scheme are given by

$$
\kappa_{2u} = g_2 \sin \beta; \qquad \kappa_{2d} = g_2 \cos \beta; \n\kappa_{1u} = \sqrt{\frac{3}{5}} g_1 \sin \beta; \qquad \kappa_{1d} = \sqrt{\frac{3}{5}} g_1 \cos \beta,
$$
\n(3)

where the gauge couplings are to be evaluated at M_{susy} . As for the Higgs quartic coupling, additional corrections are present in the \overline{MS} scheme, which can be obtained from [\[40\]](#page-7-10).

B. Two-loop RGEs and weak scale matching

We use two-loop renormalization group equations (RGEs) computed in [[39](#page-7-9)] for the gauge couplings, thirdgeneration Yukawa couplings y_t , y_b , y_τ , the Higgs quartic λ , and the gaugino-Higgsino-Higgs (κ) couplings (for Small μ), to renormalize them down to the weak scale. For Large μ , the κ couplings are not present in the lowenergy theory, and [\(3\)](#page-3-0) is used to compute the threshold correction from Higgsinos at M_{susy} .

Note that unlike the κ couplings and the quartic coupling, the boundary conditions for which are defined at M_{susy} , the boundary conditions for the gauge and Yukawa couplings y_b , y_τ are defined at M_Z —the Z pole—while that for the top Yukawa coupling y_t is defined at the top pole mass $m_t = 173.1 \pm 0.9$ GeV [[41\]](#page-7-11). In particular, the boundary values of the running gauge and Yukawa couplings in the \overline{MS} scheme are extracted from experimental observables at the weak scale by including threshold ef-fects, as explained in [[40](#page-7-10)]. For the top Yukawa coupling y_t , nontrivial three-loop QCD corrections, and one-loop electroweak and superpartner threshold corrections are also included as they are non-negligible and play an important role in the precise prediction for the Higgs mass. Since the boundary conditions are given at different scales, an iterative procedure is required to solve the coupled differential RGE equations. We follow a procedure similar to that in [\[39](#page-7-9)[,40,](#page-7-10)[42](#page-7-12)]. Then, the Higgs mass is given by

$$
M_h = \sqrt{2}v\sqrt{\lambda(Q) + \delta_\lambda(Q) + \tilde{\delta}_\lambda(Q)},
$$
 (4)

where $v = 174.1$ GeV, δ_{λ} stands for the corrections from the SM particles, and δ_{λ} stands for the corrections from the supersymmetric fermions at the weak scale, and all couplings are evaluated at the \overline{MS} scale $Q = m_t$. The expressions are given in [[39](#page-7-9)]. Finally, as mentioned earlier, since numerical codes are expected to give a good estimate of the Higgs mass, we compute the Higgs mass directly with SOFTSUSY. We find very good agreement between the two results, to within 1 GeV.

IV. RESULT

Figure [1](#page-2-0) gives the Higgs mass as a function of $tan \beta$ by varying the theoretical inputs at the unification scale in ranges predicted by the theory, and m_t and α_s within the allowed uncertainties. The values of the Higgs mass shown are in the ''match-and-run'' approach. The ranges of the theoretical and experimental inputs, and the resulting uncertainties are discussed in detail below. The μ and $B\mu$ parameters are related by electroweak symmetry breaking to tan β , so by varying tan β one is effectively varying μ
and Ru . As pointed out in Sec. I, theoretical considerations and $B\mu$. As pointed out in Sec. [I](#page-0-0), theoretical considerations typically give rise to two different classes of phenomenologically viable predictions for μ —one in which μ is suppressed by 1 to 2 orders of magnitude relative to $m_{3/2}$, and the other in which μ is comparable to $m_{3/2}$. As seen from Fig. [1](#page-2-0), the two classes of predictions for μ give rise to different values of tan β because of the EWSB constraints that relate them; hence, a measurement of the Higgs mass will not only determine or constrain tan β , it will also favor one class of μ -generating mechanisms over the other. For instance, in G_2 -MSSM models arising from M theory, Witten's solution to the doublet-triplet splitting problem [\[43\]](#page-7-13) results in μ being suppressed by about an order of magnitude. Hence, in these vacua, the Higgs mass sits in the range 122 GeV $\leq M_h \leq 129$ GeV.

It is important to understand the origin of the spread in the Higgs mass for a given value of $m_{3/2}$ and tan β , seen in Fig. [1.](#page-2-0) This spread arises from theoretical and experimental uncertainties schematically shown in Table [I.](#page-4-1) The two cases in Table [I](#page-4-1) correspond to Small μ and Large μ as mentioned in Sec. [II.](#page-1-0) As the name suggests, ''Theoretical'' in the second column corresponds to the variation of input quantities from the theory at the unification scale. For a given $m_{3/2}$, this includes the variation in the trilinears A and those in the gaugino mass parameters M_1 , M_2 , M_3 consistent with theoretical expectations. ''Experimental,'' on the other hand, stands for the variation of the experimental inputs, the top mass m_t and the $SU(3)$ gauge coupling α_s , within the current uncertainties. The precise variations in the theoretical and experimental inputs are shown in Table [II](#page-4-2).

The variations in the bino and wino mass parameters M_1 and M_2 have a negligible effect on the Higgs mass, and are

TABLE I. Uncertainties in the calculation of the Higgs mass for a given value of $m_{3/2}$ and tan β , as shown in Fig. [1](#page-2-0). All masses are in GeV. Uncertainties from higher loops are about the same order, not included in the table.

Case	Variation of input	ΔM_h
Small μ	theoretical	± 0.5
$0.05m_{3/2} \leq \mu \leq 0.15m_{3/2}$	$theoretical + experimental$	±1.1
Large μ	theoretical	$+0.5$
$0.5m_{3/2} \leq \mu \leq 1.5m_{3/2}$	$theoretical + experimental$	±1.25

TABLE II. Variation of the theoretical and experimental inputs. All masses are in GeV.

not shown above. Although we have not fully estimated uncertainties arising from higher-loop effects in the RGE and threshold effects, which should be about 1–2 GeV [[45\]](#page-7-15), the fact that our results agree so well with SOFTSUSY/ SPHENO suggests that these are at most of the same order as those listed in Table [I](#page-4-1). Finally, let us discuss the uncertainty in the gravitino mass scale. Figure [1](#page-2-0) shows the Higgs mass for three different values of $m_{3/2}$ —25, 50, and 100 TeV. As explained at the end of Sec. [I,](#page-0-0) the lower limit on $m_{3/2}$ of about 25 TeV arises from the general result that the lightest modulus mass is generically of the same order as $m_{3/2}$. The modulus decays with a decay constant which is effectively suppressed by the string scale, and the requirement of generating a sufficiently high reheat temperature so that BBN occurs in the usual manner, puts a lower bound on $m_{3/2}$. Therefore, the lower limit on $m_{3/2}$ is uncertain only by a small amount. Although the upper limit is less tightly constrained, theoretical expectations constrain it to be not much above 100 TeV. This is because in the string/M theory vacua considered here, gaugino masses are suppressed only by 1 to 2 orders of magnitude relative to $m_{3/2}$ in accord with theoretical expectations [\[1,](#page-6-0)[23\]](#page-6-19). Therefore, the requirement of gauginos to be light enough (with masses \leq TeV) such that they are part of the low-energy theory at M_{susy} , as assumed in Sec. [III A,](#page-3-1) puts an upper limit on $m_{3/2}$ of about 100 TeV. A similar upper bound also arises in realistic moduli stabilization mechanisms satisfying the supergravity approximation [[1\]](#page-6-0). Improvements in data as well as theory in the future will be extremely helpful in constraining the gravitino mass.

V. CONCLUSIONS

Recent progress in string/M theory compactifications which stabilize the moduli and give rise to low-scale supersymmetry imply that once cosmological constraints are imposed, generically the gravitino mass is heavier than about 25 TeV and the scalar masses and trilinears are close to the gravitino mass. This in turn implies that the twodoublet Higgs sector of supersymmetric models is a decoupling one, i.e. the physical mass spectrum has one light standard model-like Higgs boson, with the additional states being heavier, also of order the gravitino mass. The resulting effective low-scale theory depends only on a few input quantities from which many effects relevant for collider physics can be computed. With current understanding, these quantities are constrained by the theory but not yet fully calculable. The Higgs mass, in particular, depends on these inputs mainly through tan β , which is equivalent to a particular combination of the inputs, and to the gravitino mass scale $m_{3/2}$ to a smaller extent. The dependence on other combinations of input quantities turns out to be rather mild. It is, therefore, possible to calculate the predictions for the observable Higgs boson mass as a function of $tan \beta$ quite accurately. The resulting value holds generically in all corners of four-dimensional string/M theory vacual which satisfy the criteria and assumptions outlined in Sec. [I](#page-0-0).

We evaluate M_h by writing the effective fourdimensional theory at the compactification scale, and carrying out the renormalization group running down to the weak scale, including two-loop effects in the RGEs and all relevant threshold corrections. This gives an absolute prediction of M_h as a function of tan β to an accuracy of about 2 GeV for a given $m_{3/2}$ when all relevant theoretical and experimental uncertainties are included. The uncertainty mainly arises from the uncertainty in the top mass and the variation of the soft parameters at the unification scale within the theoretically allowed limits. $tan \beta$ is not yet accurately calculable from string/ M theory, although theoretical arguments suggest that within the framework considered, it should lie in the range from around 2 to 15. Since μ and $B\mu$ are related by the EWSB constraint, one finds that in these vacua, low $\tan \beta \le 5$ is only possible when μ is comparable to $m_{\beta/2}$, while $\tan \beta \ge 5$ is possible for μ is comparable to $m_{3/2}$, while tan $\beta \ge 5$ is possible for μ
suppressed by 1 to 2 orders of magnitude relative to m_{tot} . suppressed by 1 to 2 orders of magnitude relative to $m_{3/2}$. This is an important result as the measurement of the Higgs mass would determine (or constrain) tan β and, hence, the value of μ .

The dependence on $tan \beta$ is quite valuable. If the experimental result for M_h lies within the range predicted in Fig. [1,](#page-2-0) then the value of tan β is measured within this framework, something which is extremely difficult to do by other methods. Initially the measurement will be of limited precision but will improve fast as the experimental resolution and the accuracy of the theory improve. If M_h is greater than about 125 GeV, it puts a lower limit on $tan \beta$ which is also quite useful. Depending on the value and the accuracy with which M_h is measured, it may be possible to draw conclusions about the gravitino mass and the associated scalar masses and trilinear couplings as well. The knowledge of $tan \beta$ (and possibly scalar masses and trilinears) obtained from the Higgs mass measurement can be used as a consistency check and to look for correlated observables such as gluino pair production with enhanced branching ratios to third-generation final states (top and bottom quarks) [[1](#page-6-0)[,22\]](#page-6-18).

Note that our result is strictly only valid when the matter and gauge spectrum below the compactification scale is precisely that of the MSSM and gauginos are suppressed by an order of magnitude or so relative to the scalars. As is well known, extended gauge groups can give new D-term contributions to the Higgs mass. Similarly, existence of additional states [such as SM singlets, $SU(2)$ triplets, $SU(3)$ charged states, etc.] with Yukawa couplings to the Higgs sector can give rise to new tree-level and radiative contributions to the Higgs mass. Even if the matter and gauge content is exactly that of the MSSM but gauginos are not suppressed, then the beta function for the Higgs quartic below M_{susy} would be different and would lead to a HIGGS MASS PREDICTION FOR REALISTIC STRING ... PHYSICAL REVIEW D 85, 075026 (2012)

different prediction for the Higgs mass in general. Such alternatives can be studied in a straightforward manner if necessary.

If the prediction for the Higgs mass turns out to be correct, it would be an extremely important step forward in relating the string/ M theory framework to the real world and would open up many opportunities for learning about the string vacuum we live in. In addition to learning about $\tan \beta$ and μ as described earlier, it could tell us that the gauge and matter content of nature is indeed that of gauge and matter content of nature is indeed that of the MSSM. If not, this would imply that one or more of the attractive assumptions in the paper have to be relaxed.

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