

Brane inflation in background supergravitySayantan Choudhury^{1,*} and Supratik Pal^{1,2,†}¹*Physics and Applied Mathematics Unit, Indian Statistical Institute, 203 B. T. Road, Kolkata 700 108, India*²*Bethe Center for Theoretical Physics and Physikalisches Institut der Universität Bonn, Nussallee 12, 53115 Bonn, Germany*

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We propose a model of inflation in the framework of brane cosmology driven by background supergravity. Starting from bulk supergravity we construct the inflaton potential on the brane and employ it to investigate for the consequences to inflationary paradigm. To this end, we derive the expressions for the important parameters in brane inflation, which are somewhat different from their counterparts in standard cosmology, using the one-loop radiative corrected potential. We further estimate the observable parameters and find them to fit well with recent observational data by confronting with Wilkinson Microwave Anisotropy Probe 7 (WMAP) using the Code for Anisotropies in the Microwave Background (CAMB). We also analyze the typical energy scale of brane inflation with our model, which resonates well with present estimates from cosmology and the standard model of particle physics.

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I. INTRODUCTION

Investigations for the crucial role of Supergravity in explaining cosmological inflation date back to the early eighties of the last century (for two exhaustive reviews see [1,2], and references therein). One of the generic features of the inflationary paradigm based on supergravity (SUGRA) is the well-known η problem, which appears in the F-term inflation due to the fact that the energy scale of F-term inflation is induced by all the couplings via vacuum energy density. Precisely, in the expression of F-term inflationary potential a factor $\exp(K/M_{\text{PL}})$ appears, leading to the second slow-roll parameter $\eta \gg 1$, thereby violating an essential condition for slow-roll inflation. The usual way out is to impose additional symmetry to the framework. One such symmetry is Nambu-Goldstone shift symmetry [3] under which Kähler metric becomes diagonal, which serves the purpose of canonical normalization and stabilization of the volume of the compactified space. Consequently, the imaginary part of the scalar field gives a flat direction leading to a successful model of inflation. An alternative approach is to apply noncompact Heisenberg group transformations of two or more complex scalar fields where one can exploit Heisenberg symmetry [4] to solve η problem. The role of Kähler geometry to solve η problem in the context of $N = 1$ SUGRA under certain constraints can be found in [5].

Of late the idea of braneworlds came forward [6]. From a cosmological point of view, the most appealing feature of brane cosmology is that the four-dimensional (4D) Friedmann equations are, to some extent, different from the standard ones due to the nontrivial embedding in the S^1/Z_2 orbifold [7]. This opens up new perspectives to look at the nature in general and cosmology in specific. To

mention a few, the role of the projected bulk Weyl tensor appearing in the modified Friedmann equations has been studied extensively for metric-based perturbations [8], density perturbations on large scales [9], curvature perturbations [10] and Sachs-Wolfe effect [11], vector perturbations [12], tensor perturbations [13], and CMB anisotropies [14]. Brane inflation in the above framework has also been studied to some extent [15–17]. Apart from these phenomenological approaches, some other approaches which are more appealing in dealing with fundamental aspects, such as possible realization in string theory, can be found in [18–21]. For example, an apparent conflict between self-tuning mechanism and volume stabilization has been shown in [19], subsequently, this problem has been resolved in [20], where the credentials of the dilatonic field in providing a natural explanation for dark energy by an effective scalar field on the brane has been demonstrated using self-tuning mechanism in $(4 + 2)$ -dimensional bulk space time. The role of the axions as quintessential candidates has been revealed in [21].

In the Randall-Sundrum two-brane scenario [6], where the bulk is five-dimensional (5D) with the fifth dimension compactified on the orbifold S^1/Z_2 of comoving radius R , the separation between the two branes gives rise to a field—the so-called *radion*—which plays a crucial role in governing dynamics on the brane. The well-known Goldberger-Wise mechanism [22] leading to several interesting ideas deal with different issues related to radion. Subsequently, in order to incorporate observationally constraint cosmology of the brane, a fine-tuning between the brane tension of the visible and invisible brane has been proposed [23]. It has been pointed out in [24,25] how the radion coupled with bulk fields may give rise to an effective inflaton field on the brane. In the same vein, we construct the brane-inflaton potential of our consideration starting from 5D SUGRA. In brane inflation, the modified Friedmann equations lead to a modified version of the

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slow-roll parameters [7]. So, by construction, η problem is smoothed to some extent by modification of Friedmann equations on the brane [17,26]. In a sense, this is a parallel approach to the usual string inflationary framework, where η problem is resolved by fine-tuning [27]. As it will appear, there is still some fine-tuning required in brane inflation, which arises via a new avatar of 5D Planck mass, but it is softened to some extent due to the modified Friedmann equations.

As we will find in the present article, the proposed model of brane inflation matches quite well with latest observational data from WMAP [28] and is expected to fit well with upcoming data from Planck [29]. To this end, we explicitly derive the expressions for different observable parameters from our model and further estimate their numerical values, finally leading to confrontation with observation using the publicly available code CAMB [30]. We have also analyzed the typical energy scale of brane inflation and found it to be in good agreement with present estimates of cosmological frameworks as well as the standard model of particle physics.

II. MODELING BRANE INFLATION

Let us consider an effective $N = 1$, $D = 4$ SUGRA inflationary potential in the brane derived from $N = 2$, $D = 5$ SUGRA in the bulk. How we have arrived at an effective $N = 1$, $D = 4$ SUGRA in the brane starting from $N = 2$, $D = 5$ SUGRA in the bulk and the subsequent form of the loop-corrected potential stated in Eq. (2.1) has been discussed in details in the Appendix. For convenience, let us express the one-loop-corrected renormalizable potential in terms of inflationary parameters as

$$V(\phi) = \Delta^4 \left[1 + \left(D_4 + K_4 \ln\left(\frac{\phi}{M}\right) \right) \left(\frac{\phi}{M}\right)^4 \right], \quad (2.1)$$

where we introduce new constants defined by (C_4 is negative in tree-level) $K_4 = \frac{9\Delta^4 C_4^2}{2\pi^2 M^4}$, $D_4 = C_4 - \frac{25K_4}{12}$. The Coleman-Weinberg potential [31], [32], provided the

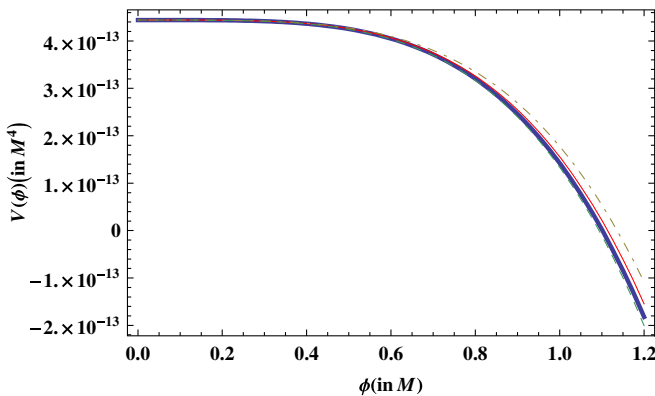


FIG. 1 (color online). Variation of one-loop-corrected potential $V(\phi)$ versus inflaton field (ϕ).

coupling constant that satisfies the Gellmann-Low equation in the context of renormalization group [33,34]. Here, the first-term is constant and physically represents the energy scale of inflation (Δ).

Figure (1) represents the inflaton potential for different values of C_4 , D_4 , and K_4 . From the observational constraints the best-fit model is given by the range $-0.70 < D_4 < -0.60$ so that while doing numerals we shall restrict ourselves to this range of D_4 . In what follows, our primary intention will be to engage ourselves in modeling brane inflation and to search for its pros and cons with the above potential (2.1). We shall indeed find that brane inflation with such a potential successfully explains the CMB observations and thus leads to a promising model of inflation.

As already mentioned, the most appealing feature of brane cosmology is that the 4D Friedmann equations are to some extent different from the standard ones due to the nontrivial embedding in the S^1/Z_2 manifold [7]. At high-energy regime one can neglect the contribution from Weyl term and consequently, the brane-Friedmann equations are given by [7,35] $H^2 = \frac{8\pi V}{3M_{\text{PL}}^2} \left[1 + \frac{V}{2\lambda} \right]$. The modified Friedmann equations, along with the Klein-Gordon equation, lead to new slow-roll conditions and new expressions for observable parameters as well, [7,35]. For convenience, throughout the analysis we define the following global functions of the inflaton field

$$\begin{aligned} L(\phi) &= \left[1 + \frac{\alpha}{2} S(\phi) \right], & T(\phi) &= [1 + \alpha S(\phi)], \\ S(\phi) &= \left[1 + \left\{ D_4 + K_4 \ln\left(\frac{\phi}{M}\right) \right\} \left(\frac{\phi}{M}\right)^4 \right], \\ U(\phi) &= \left[(K_4 + 4D_4) + 4K_4 \ln\left(\frac{\phi}{M}\right) \right], \\ E(\phi) &= \left[(7K_4 + 12D_4) + 12K_4 \ln\left(\frac{\phi}{M}\right) \right], \\ F(\phi) &= \left[(26K_4 + 24D_4) + 24K_4 \ln\left(\frac{\phi}{M}\right) \right], \\ J(\phi) &= \left[(50K_4 + 24D_4) + 24K_4 \ln\left(\frac{\phi}{M}\right) \right], \\ \tilde{P}(\phi) &= \sqrt{[1 + 2\alpha S(\phi)L(\phi)]} \\ &\quad - 2\alpha S(\phi)L(\phi) \sinh^{-1}([2\alpha S(\phi)L(\phi)])^{-1/2} \end{aligned} \quad (2.2)$$

with $\alpha = \Delta^4/\lambda$. Incorporating the potential of our consideration from Eq. (2.1), the slow-roll parameters turn out to be

$$\epsilon_V = \frac{M_{\text{PL}}^2}{16\pi} \left(\frac{V'}{V}\right)^2 \frac{1 + \frac{V}{\lambda}}{\left(1 + \frac{V}{2\lambda}\right)^2} = \frac{U^2(\phi)T(\phi)}{2S^2(\phi)L^2(\phi)} \left(\frac{\phi}{M}\right)^6, \quad (2.3)$$

$$\eta_V = \frac{M_{\text{PL}}^2}{8\pi} \left(\frac{V''}{V}\right) \frac{1}{\left(1 + \frac{V}{2\lambda}\right)} = \frac{E(\phi)}{S(\phi)L(\phi)} \left(\frac{\phi}{M}\right)^2, \quad (2.4)$$

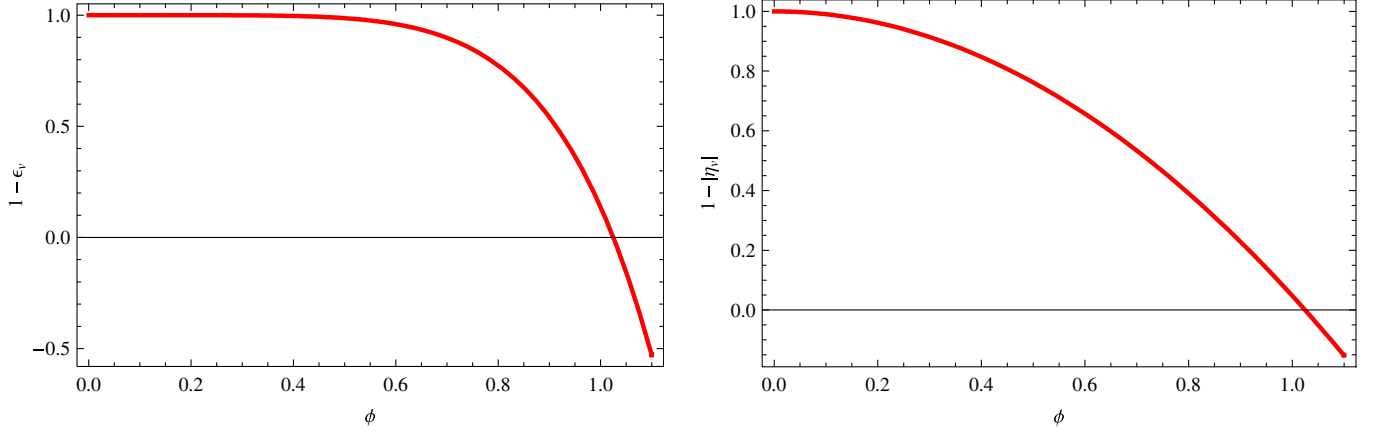


FIG. 2 (color online). Left: variation of the $1 - \epsilon_V$ versus inflaton field ϕ for $C_4 = -0.68$. Right: variation of the $1 - |\eta_V|$ versus inflaton field ϕ for $C_4 = -0.68$.

$$\xi_V = \frac{M_{\text{PL}}^4}{(8\pi)^2} \left(\frac{V' V'''}{V^2} \right) \frac{1}{\left(1 + \frac{V}{2\lambda}\right)^2} = \frac{U(\phi)F(\phi)}{S^2(\phi)L^2(\phi)} \left(\frac{\phi}{M}\right)^4, \quad (2.5)$$

$$\sigma_V = \frac{M_{\text{PL}}^6}{(8\pi)^3} \frac{(V')^2 V''''}{V^3} \frac{1}{\left(1 + \frac{V}{2\lambda}\right)^3} = \frac{U^2(\phi)J(\phi)}{S^3(\phi)L^3(\phi)} \left(\frac{\phi}{M}\right)^6, \quad (2.6)$$

Figure (2) depicts how the first two slow-roll parameters vary with the inflaton field for the allowed range of D_4 , and they give us a clear picture of the starting point as well as the end of the cosmic inflation. Nevertheless, Fig. 2 further reveals that the η problem is smoothed to some extent in brane cosmology. However, we are yet to figure out if there are any underlying dynamics that may lead to the solution of this generic feature of SUGRA.

The number of e-foldings are defined in brane cosmology [7] for our model as

$$\begin{aligned} N &= \frac{a(t_f)}{a(t_i)} \simeq \frac{8\pi}{M_{\text{PL}}^2} \int_{\phi_f}^{\phi_i} \left(\frac{V}{V'}\right) \left(1 + \frac{V}{2\lambda}\right) d\phi \\ &\simeq \frac{M^2}{U} \left[\frac{1}{2} \left(1 + \frac{\alpha}{2}\right) \left(\frac{1}{\phi_f^2} - \frac{1}{\phi_i^2}\right) + \frac{D_4}{2M^4} (1 + \alpha) (\phi_i^2 - \phi_f^2) \right. \\ &\quad \left. + \frac{\alpha D_4^2}{12M^8} (\phi_i^6 - \phi_f^6) \right], \end{aligned} \quad (2.7)$$

which in the high-energy regime reduces to $N \simeq \frac{\alpha M^2}{4|U|} \times \left[\frac{1}{\phi_i^2} - \frac{1}{\phi_f^2}\right]$. Here ϕ_i and ϕ_f are the corresponding values of the inflaton field at the start and end of inflation.

Let us now engage ourselves in analyzing quantum fluctuation in our model and its observational imprints via primordial spectra generated from cosmological perturbation [36]. In brane inflation the expressions for amplitude of the scalar perturbation, tensor perturbation, and tensor to scalar ratio [7,17,37],[17,37] are given by

$$\Delta_s^2 \simeq \frac{512\pi}{75M_{\text{PL}}^6} \left[\frac{V^3}{(V')^2} \left[1 + \frac{V}{2\lambda}\right]^3 \right]_{k=aH} = \frac{M^2 \alpha \lambda S^3(\phi_*) L^3(\phi_*)}{75\pi^2 U^2(\phi_*) (\phi_*)^6}, \quad (2.8)$$

$$\begin{aligned} \Delta_t^2 &\simeq \frac{32}{75M_{\text{PL}}^4} \left[\frac{V \left[1 + \frac{V}{2\lambda}\right]}{\left[\sqrt{1 + \frac{2V}{\lambda} \left(1 + \frac{V}{2\lambda}\right)} - \frac{2V}{\lambda} \left(1 + \frac{V}{2\lambda}\right) \sinh^{-1} \left[\frac{1}{\sqrt{\frac{2V}{\lambda} \left(1 + \frac{V}{2\lambda}\right)}} \right]} \right] \right]_{k=aH} \\ &= \frac{\lambda \alpha}{150\pi^2 M^4} \frac{S(\phi_*) L(\phi_*)}{\tilde{P}(\phi_*)}, \end{aligned} \quad (2.9)$$

$$r = 16 \frac{\Delta_t^2}{\Delta_s^2} \simeq \frac{8(\phi_*)^6 U^2(\phi_*)}{M^6 S^2(\phi_*) L^2(\phi_*) \tilde{P}(\phi_*)}. \quad (2.10)$$

Here and throughout the rest of the article ϕ_* represents the value of the inflaton field at the horizon crossing and all

the global function defined in Eq. (2.2) is evaluated at the horizon crossing.

Figure [3(I)] represents the graphical behavior of a number of e-folding vs the inflaton field in the high-energy limit for different values of D_4 , and the most satisfactory

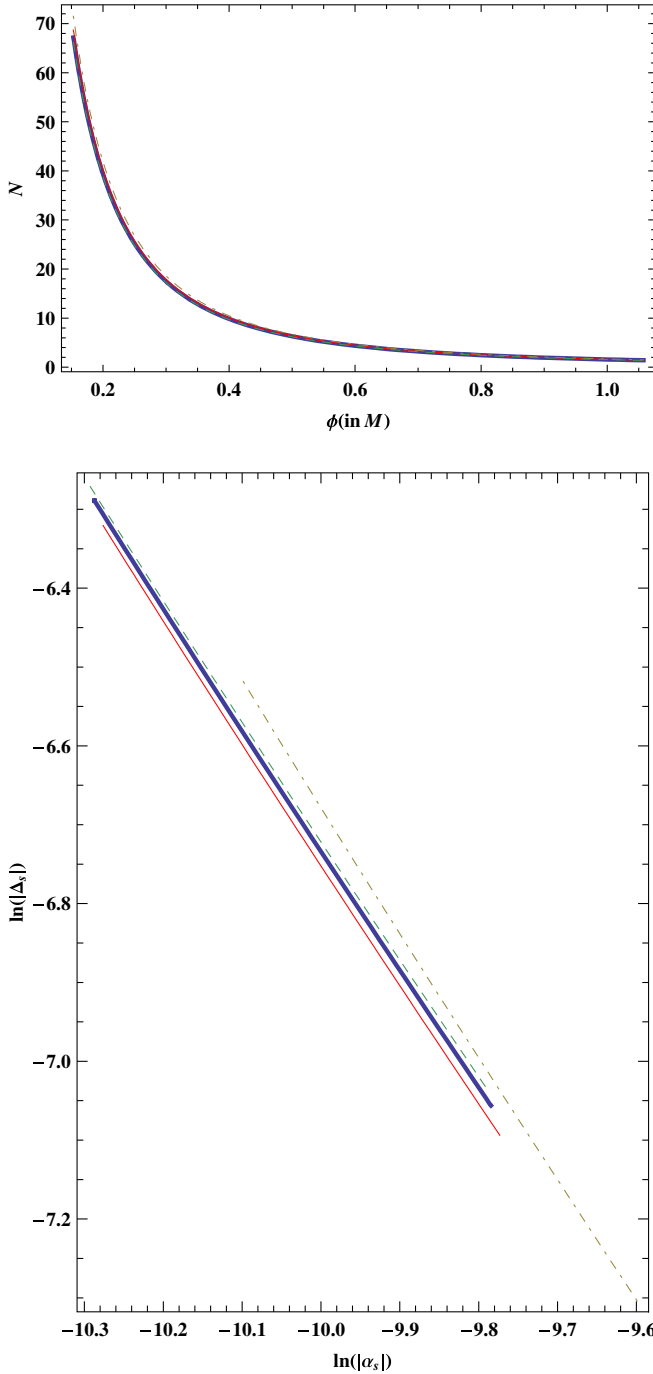


FIG. 3 (color online). Top: variation of the number of e-folding (N) versus inflation field (ϕ) measured in the units of M . Bottom: variation of the logarithmic-scaled amplitude of the scalar fluctuation ($\ln(\Delta_s)$) versus logarithmic-scaled amplitude of the running of the spectral index ($\ln(|\alpha_s|)$).

point in this context is the number of e-folding lies within the observational window $56 < N < 70$. The end of the inflation leads to the constraint $\alpha = \frac{2}{(|U|)} (|E|)^{(3/2)}$, which is required for numerical estimations. Here, Fig. [3(II)] represents the logarithmically scaled plots of the physical set

of parameter (Δ_s, α_s) for different values of D_4 . The plots themselves present a good fit with observations.

Further, the scale dependence of the perturbations, described by the scalar and tensor-spectral indices are as follows [16,38]:

$$\begin{aligned} n_s - 1 &= \frac{d(\ln(\Delta_s^2))}{d(\ln(k))} \simeq (2\eta_V^* - 6\epsilon_V^*) \\ &= \frac{2E(\phi_*)}{S(\phi_*)L(\phi_*)} \left(\frac{\phi_*}{M}\right)^2 - \frac{3U(\phi_*)T(\phi_*)}{S^2(\phi_*)L^2(\phi_*)} \left(\frac{\phi_*}{M}\right)^6, \\ n_t &= \frac{d(\ln(\Delta_t^2))}{d(\ln(k))} \simeq -3\epsilon_V^* = -\frac{3U^2(\phi_*)T(\phi_*)}{2S^2(\phi_*)L^2(\phi_*)} \left(\frac{\phi_*}{M}\right)^6, \end{aligned} \quad (2.11)$$

where $d(\ln(k)) = Hdt$. Here, one can check that [39] the validity of the consistency condition $r = 24\epsilon_V = 24\epsilon_V^*$; $n_t = -3\epsilon_V \simeq -3\epsilon_V^* = -\frac{r}{8}$.

The expressions for the running of the scalar and tensor-spectral index in this specific model, with respect to the logarithmic pivot scale at the horizon crossing, are given by

$$\begin{aligned} \alpha_s &= (16\eta\epsilon - 18\epsilon^2 - 2\xi) \\ &= \frac{8E(\phi_*)U^2(\phi_*)T(\phi_*)}{S^3(\phi_*)L^3(\phi_*)} \left(\frac{\phi_*}{M}\right)^8 - \frac{2F(\phi)U(\phi_*)}{S^2(\phi_*)L^2(\phi_*)} \\ &\quad \times \left(\frac{\phi_*}{M}\right)^4 - \frac{9U^4(\phi_*)T^2(\phi_*)}{2S^4(\phi_*)L^4(\phi_*)} \left(\frac{\phi_*}{M}\right)^{12}, \end{aligned} \quad (2.12)$$

$$\begin{aligned} \alpha_t &= (6\epsilon\eta - 9\epsilon^2) \\ &= \frac{3E(\phi_*)U^2(\phi_*)T(\phi_*)}{S^3(\phi_*)L^3(\phi_*)} \left(\frac{\phi_*}{M}\right)^8 - \frac{9U^4(\phi_*)T^2(\phi_*)}{4S^4(\phi_*)L^4(\phi_*)} \\ &\quad \times \left(\frac{\phi_*}{M}\right)^{12}, \end{aligned} \quad (2.13)$$

One can also calculate the running of the fourth slow-roll parameter as $\frac{d\sigma}{d(\ln(k))} = (\epsilon\sigma - 2\eta\sigma)$, but its numerical value turns out to be too small to be detected even in the near future for which it can be treated as consistency condition in brane.

To estimate 5D Planck mass from the observational parameters we use the relation $\sqrt{8\pi}M = M_{\text{PL}} = \frac{M_5^3}{\sqrt{\lambda}} \sqrt{\frac{3}{4\pi}}$ and Eq. (2.8), which leads to

$$M_5 = \sqrt{\frac{800\pi^4 \Delta_s^2 U^2(\phi_*)}{\alpha S^3(\phi_*) L^3(\phi_*)}} \phi_*. \quad (2.14)$$

Finally, using the thermodynamic definition of density at the time of reheating $\rho(t_{\text{reh}}) = \frac{\pi^2 N^* T_{\text{breh}}^4}{30}$ in the inflaton decay width $\Gamma_{\text{total}} = 3H(T^{\text{breh}}) = 3\sqrt{\frac{\rho(t_{\text{reh}})}{3M^2}} [1 + \frac{\rho(t_{\text{reh}})}{2\lambda}] \simeq \frac{\Delta^6}{(2\pi)^3 M^3}$ we have estimated the reheating temperature in the brane-world in terms of the 5D Planck mass as

TABLE I. Different observational parameters related to the cosmological perturbation for our model of inflation including one-loop radiative correction.

$C_4 \simeq D_4$	α	λ $\times 10^{-14} M^4$	$\phi_f M$	$\phi_i M$	N	$\phi_* M$	Δ_s^2 $\times 10^{-9}$	Δ_t^2 $\times 10^{-14}$	n_s	n_t $\times 10^{-5}$	r $\times 10^{-5}$	α_s $\times 10^{-3}$	α_t $\times 10^{-6}$	M_5 $\times 10^{-3} M$	T^{breh} $\times 10^{-8} M$
-0.70	17.389	2.553	1.017	0.147	70	0.158	3.126		0.951	-4.352	2.176	-0.798	-2.125	11.792	3.119
				0.158	60	0.173	1.835	6.803	0.941	-7.412	3.706	-1.142	-4.323		
				0.164	56	0.180	1.440		0.936	-9.447	4.723	-1.345	-5.975		
-0.65	16.757	2.632	1.036	0.150	70	0.161	2.902		0.951	-4.352	2.176	-0.798	-2.125	11.865	3.133
				0.161	60	0.176	1.704	6.317	0.941	-7.412	3.706	-1.142	-4.323		
				0.167	56	0.184	1.327		0.936	-9.447	4.723	-1.345	-5.975		
-0.60	16.099	2.758	1.057	0.153	70	0.165	2.679		0.951	-4.352	2.176	-0.798	-2.125	11.944	3.149
				0.165	60	0.180	1.573	5.831	0.941	-7.412	3.706	-1.142	-4.323		
				0.170	56	0.187	1.234		0.936	-9.447	4.723	-1.345	-5.975		

$$T^{\text{breh}} = \sqrt{\frac{3}{4\pi^2}} \sqrt{\frac{5}{N^*}} \frac{M_5^3}{M} \sqrt[4]{\left[\sqrt{1 + \frac{64M^4 \pi^2 \Gamma_{\text{total}}^2}{9M_5^6}} - 1 \right]} = \sqrt[4]{\frac{2250 \Delta_s^2 U^2(\phi_*) \phi_*^3}{N^* M^2 \alpha S^3(\phi_*) L^3(\phi_*)}} \sqrt[4]{\left[\sqrt{1 + \frac{2M^4 \Gamma_{\text{total}}^2 \alpha S^3(\phi_*) L^3(\phi_*)}{225 \pi^2 \Delta_s^2 \phi_*^6 U^2(\phi_*)}} - 1 \right]}, \quad (2.15)$$

where N^* is the effective number of particles incorporating the relativistic degrees of freedom.

III. PARAMETER ESTIMATION

A. Direct numerical estimation

Table I represents numerical estimation for different observational parameters related to the cosmological perturbation as estimated from our model. Here a “ \times ” implies “in units of.” It is worthwhile to point out the salient features of the parameters in the above table as obtained from our model.

- (i) An estimation for the brane tension in the above observable parameters is $\lambda \gg (1 \text{ MeV})^4$, provided that the energy scale of the inflation is in the vicinity of the grand unified theory (GUT) scale and exactly of the order of $0.2 \times 10^{16} \text{ GeV}$, which resolves Polonyi problem [40] and Gravitino problem [41].
- (ii) The scalar power spectrum corresponding to different best-fit values of D_4 mentioned above is of the order of 5×10^5 and perfectly matches the observational data [28].
- (iii) The scalar spectral index for lower values of $N \rightarrow 55$ are pretty close to observational window $0.948 < n_s < 1$ [28], whereas for higher values of $N \rightarrow 70$, the scalar spectral index lies well within the window. Thus, this small observational window reveals that $N \approx 70$ is more favored in brane cosmology compared to its lower values.
- (iv) Though the tensor to scalar ratio as estimated from our model is well within its upper bound fixed by WMAP7 [28] ($r < 0.45$ at 95% C.L.), facing no contradiction with observations, its detected value is small in WMAP [28] and the forthcoming Planck [29]. For more discussion see [42].

- (v) For our model, the running of the scalar spectral index $\alpha_s \sim -10^{-3}$ is quite consistent with WMAP3 [43]. Also, the running of the tensor-spectral index $\alpha_t \sim -6 \times 10^{-6}$ may serve as an additional observable parameter to be investigated further.
- (vi) Five-dimensional Planck mass turns out to be $M_5 \sim (11.792 - 11.944) \times 10^{-3} M$, which is the prime input for the estimation of brane reheating temperature as shown in Eq. (2.15). For our model, it is estimated as $T^{\text{breh}} \sim (3.119 - 3.149) \times 10^{-8} M$ and clearly depicts the deviation from standard cosmology.

B. Data analysis with CAMB

In this context we shall make use of the cosmological code CAMB [30] in order to confront our results directly with observation. To operate CAMB, the values of the initial parameters associated with inflation are taken from Table I for $D_4 = -0.60$. Additionally, WMAP7 data set in Λ CDM background has been used in CAMB to obtain CMB-angular power spectrum at the pivot scale $k_0 = 0.002 \text{ Mpc}^{-1}$. Tables II and III show input from the WMAP7 data set and the output obtained from CAMB, respectively.

The curvature perturbation is generated due to the fluctuations in the *inflaton*. At the end of inflation, it makes horizon reentry, creating matter-density fluctuations which are the origin of the structure formation in the universe. In Figs. 4(a)–4(c) we confront CAMB output of CMB-angular power spectrum C_l^{TT} , C_l^{TE} , and C_l^{EE} for best-fit with WMAP seven-years-data for the scalar mode. From Fig. 4(a) we see that the Sachs-Wolfe plateau [44] obtained from our model is almost flat, confirming a nearly scale invariant spectrum. For larger value of the multipole l , CMB-anisotropy spectrum is dominated by the Baryon

TABLE II. Input parameters in CAMB.

H_0 km/sec/Mpc	τ_{Reion}	$\Omega_b h^2$	$\Omega_c h^2$	T_{CMB}
71.0	0.09	0.0226	0.1119	2.725

TABLE III. Output parameters from CAMB.

t_0 Gyr	z_{Reion}	Ω_m	Ω_Λ	Ω_k	η_{Rec} Mpc	η_0 Mpc
13.707	10.704	0.2670	0.7329	0.0	285.10	14345.1

Acoustic Oscillations [45], giving rise to several ups and downs in the spectrum. Also, the peak positions are sensitive on the dark energy and other forms of the matter. In Fig. 4(a) the first and most prominent peak arises at $l = 221$ at a height of $5818 \mu\text{K}^2$ followed by two equal height peaks at $l = 529$ and $l = 822$. This is in good agreement with WMAP7 data for ΛCDM -background apart from the two outliers at $l = 21$ and $l = 42$. The gravitational waves generated during inflation also remain constant on *super Hubble* scales, having small amplitudes which die off very rapidly due to smaller wavelength than horizon. So, the small scale modes have no impact in the CMB-anisotropy spectrum; only the large scale modes have a little contribution, which is obvious from Figs. 5(a)–5(d) where we have plotted the CAMB output of CMB-angular power spectrum C_l^{TT} , C_l^{TE} , C_l^{EE} , and C_l^{BB} for best-fit with WMAP7 data for the tensor mode. Thus, from the entire data analysis with CAMB, our model confronts extremely well with the WMAP7 data set and leads to constrain of the best-fit value of the parameter D_4 at -0.60 .

IV. DYNAMICAL SIGNATURE OF THE MODEL

Let us now engage ourselves in finding out the dynamical signature of the model from the first principle. Precisely, we are interested in obtaining a solution of the modified Friedmann equation and Klein-Gordon equation in brane cosmology with our proposed model. Under slow-roll approximations, the inflaton field as a function of cosmic time can be expressed as

$$\phi(t) = \frac{M^2}{\sqrt{2D_4}} \sqrt{[\tilde{\Phi}(f) - \bar{G}t]} \times \sqrt{\left[1 - \sqrt{1 + \frac{4D_4}{M^4[\tilde{\Phi}(f) - \bar{G}t]^2}}\right]}, \quad (4.1)$$

where $\bar{G} = \frac{2U\sqrt{2\lambda}}{\sqrt{3}M^3}$, $\tilde{\Phi}(f) = \frac{1}{\phi_f^2} \left(\frac{D_4 \phi_f^4}{M^4} - 1 \right) + \bar{G}t_f$. It may be noted that in the high-energy limit, Eq. (4.1) reduces to a much tractable form $\phi(t) = \phi_f \left[1 + \frac{2U\phi_f^2}{M^3} \sqrt{\frac{2\lambda}{3}} (t - t_f) \right]^{-1/2}$.

Figure [6(I)] shows the evolution of the inflaton field under high-energy approximation, which shows a smooth increasing behavior of the inflaton field with respect to the

inflationary time scale where the span of the scale are within the window $t_i < t < t_f$. In Fig. [6(II)] the evolution of the Hubble parameter shows deviations from the de Sitter as given by the bending of the plots toward the end of inflation, which leads to a physically more realistic scenario so as to fit with observational data as demonstrated earlier.

Substituting Eq. (4.1) in the modified Friedmann equation in brane for our model we obtain

$$H(t) = \sqrt{\frac{\lambda}{6}} \frac{\alpha}{M} \left[2 + \frac{M^4}{2D_4} [\tilde{\Phi}(f) - \bar{G}t]^2 \right] \times \left(1 - \sqrt{1 + \frac{4D_4}{M^4[\tilde{\Phi}(f) - \bar{G}t]^2}} \right), \quad (4.2)$$

which shows the time evolution as well as the susceptance of Hubble parameter in the context of brane.

Consequently, the solution of the modified Friedmann equation, after rearranging terms, gives rise to the scale factor as follows:

$$a(t) = a(t_f) \exp \left[\sqrt{\frac{\lambda}{6}} \frac{\alpha}{M} \left[2(t - t_f) + \tilde{A}(t - t_f) + \frac{\tilde{B}}{3}(t^3 - t_f^3) - \frac{\tilde{C}}{2}(t^2 - t_f^2) - \tilde{I}(t) \right] \right], \quad (4.3)$$

where $\tilde{I}(t) = \int_{t_f}^t dt \sqrt{[(\tilde{A} + \tilde{B}t^2 - \tilde{C}t + 1)^2 - 1]}$, $\tilde{A} = \frac{M^4 \tilde{\Phi}(f)}{2D_4}$, $\tilde{B} = \frac{\bar{G}^2 M^4}{2D_4}$, $\tilde{C} = \frac{\tilde{\Phi}(f) \bar{G} M^4}{D_4}$. Thus, the scale factor can be obtained analytically except for the integrand $\tilde{I}(t)$, and it readily shows the deviation from the standard de Sitter model. However, the above form of the scale factor (4.3) is more or less sufficient to study the dynamical behavior, as represented in Fig. [6(II)]. As a matter of fact, the leading-order contribution from Hubble parameter and the scale factor are indeed closed to de Sitter with the parameters involving brane cosmology.

V. ANALYSIS OF THE ENERGY SCALE OF BRANE INFLATION

Let us now estimate the typical scale of inflation in brane cosmology with the potential of our consideration. For this we shall make use of two initial conditions, namely, initial time $t_i = 0.737 \times 10^{10} M^{-1}$ and $a(t_i) = 0.369 \times 10^{-1} M^{-1}$. Consequently, for $N = 70$ we have $a(t_f) = 0.929 \times 10^{11} M^{-1}$. Now, taking leading-order contribution from Eq. (4.3), the time corresponding to the horizon exit and reentry can be obtained as

$$t_* = t_f + \frac{1}{\bar{G}} \left[\tilde{\Phi}(f) - \frac{[1 \pm \sqrt{1 - 8D_4[(\phi_*)^2 + 2M^4]}]}{M^4} \right], \quad (5.1)$$

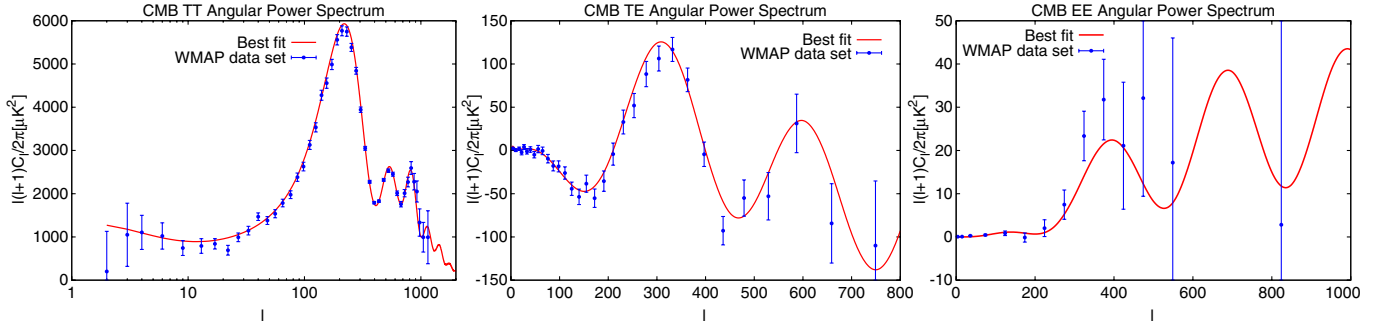


FIG. 4 (color online). Left: variation of CMB-angular power spectrum (a) C_l^{TT} . Center: C_l^{TE} . Right: C_l^{EE} for best-fit and WMAP7 with the multipoles l for scalar modes.

with $t_f = t_i + \frac{NM}{\alpha} \sqrt{\frac{6}{\lambda}}$. Using Eqs. (5.1), (4.1), and (2.4), energy scale of brane inflation can be expressed as

$$\Delta \approx \sqrt[4]{\left[\frac{2E\lambda\phi_f^2}{|\eta_V|M^2 \left[1 + \frac{2U\phi_f^2}{M^3} \sqrt{\frac{2\lambda}{3}}(t - t_f) \right]} \right]} \quad (5.2)$$

Figure (7) shows the energy scale of inflation (Δ) versus the magnitude of the second slow-roll parameter ($|\eta_V|$) for different values of the constant D_4 , including two feasible roots of horizon crossing. From the figure, it is obvious that for two feasible roots of time corresponding to the horizon, crossing an allowed region with finite bandwidth appears for our proposed model. The above figure further reveals

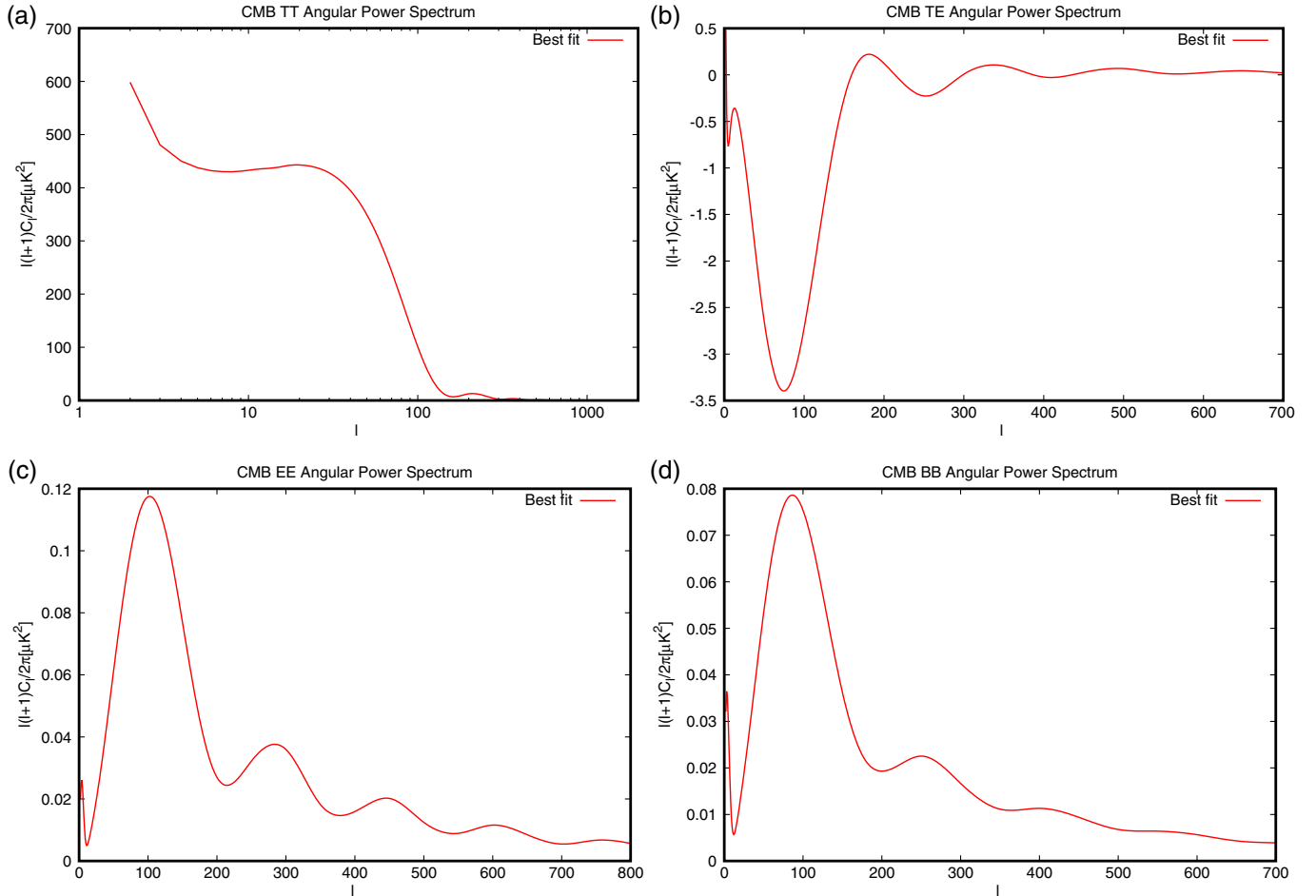


FIG. 5 (color online). Variation of CMB-angular power spectrum (a) C_l^{TT} ; (b) C_l^{TE} ; (c) C_l^{EE} , and (d) C_l^{BB} with the multipoles l for tensor mode.

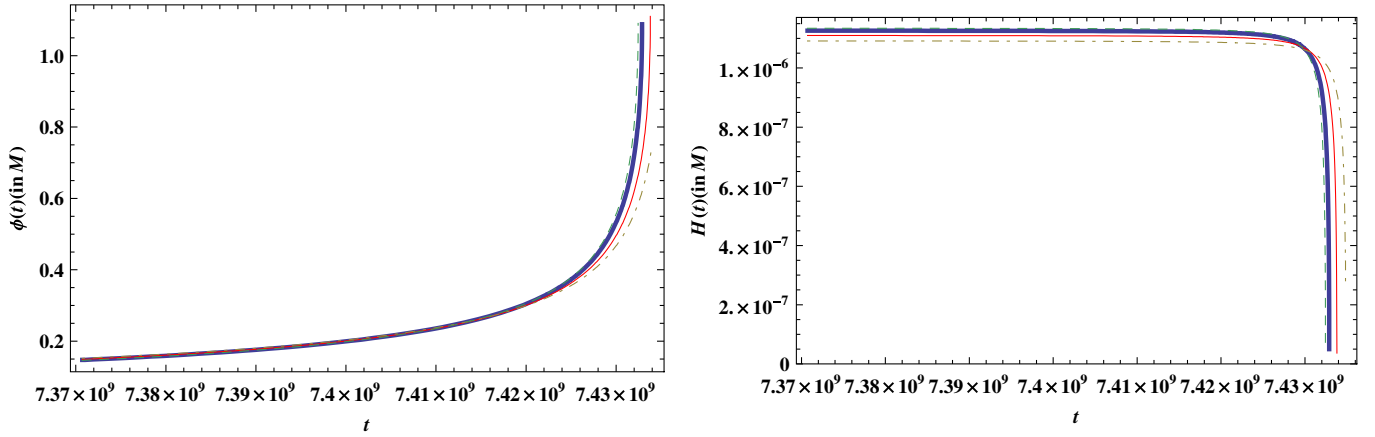


FIG. 6 (color online). Left: variation of the inflaton field (ϕ) with time (t). Right: variation of the Hubble parameter ($H(t)$) with time (t).

that the typical energy scale of brane inflation with our proposed model is $\Delta \simeq 2 \times 10^{15}$ GeV, which is supported from cosmological as well as particle physics frameworks.

VI. SUMMARY AND OUTLOOK

In this article we have proposed a model of inflation in brane cosmology. We have demonstrated how we can construct an effective 4D inflationary potential starting from $N = 2$, $D = 5$ supergravity in the bulk leads to an effective $N = 1$, $D = 4$ supergravity in the brane. Then we engaged ourselves in analyzing radiative corrections of the tree-level potential. The effective potential (calculated from one-loop correction) was then employed in estimating the observable parameters both analytically and numerically, leading to more precise estimation of the quantities and confronting them with WMAP7 data set using the publicly available code CAMB, which reveals consistency of our model with latest observations. The increase in precision level is worth analyzing, considering the advent of more and more sophisticated techniques both in WMAP [28] and in the forthcoming Planck [29] data.

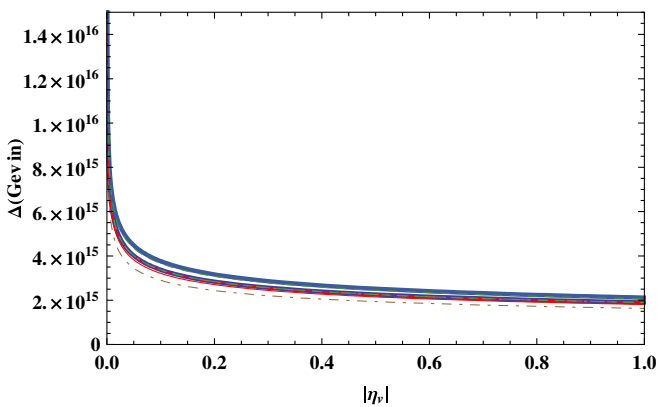


FIG. 7 (color online). Variation of the energy scale of inflation (Δ) versus $|\eta_V|$, including two roots of the horizon crossing time for the best-fit model.

We have also solved the modified Friedmann equations on the brane, leading to an analytical expression for the scale factor during inflation. Finally, we have estimated the typical energy scale of brane inflation with the potential of our consideration and found it to be consistent with cosmological as well as particle physics frameworks. This model thus leads to an inflationary scenario in the framework of supergravity-inspired brane cosmology.

A detailed survey of thermal history of the universe via reheating baryogenesis and leptogenesis with the loop-corrected potential and gravitino phenomenology remains an open issue, which may eventually provide interesting signatures of brane inflation. A detailed analysis on these aspects have been reported in a separate paper [46].

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APPENDIX

For systematic development of the formalism, let us demonstrate briefly how one can construct the effective 4D inflationary potential of our consideration starting from $N = 2$, $D = 5$ SUGRA in the bulk leads to an effective $N = 1$, $D = 4$ SUGRA in the brane. As mentioned, we

consider the bulk to be 5D where the fifth dimension is compactified on the orbifold S^1/Z_2 of comoving radius R . The system is described by the following action [47,48]:

$$S = \frac{1}{2} \int d^4x \int_{-\pi R}^{+\pi R} dy \sqrt{g_5} \left[M_5^3 (R_{(5)} - 2\Lambda_5) + L_{\text{bulk}} + \sum_i \delta(y - y_i) L_{4i} \right]. \quad (\text{A1})$$

Here, the sum includes the walls at the orbifold points $y_i = (0, \pi R)$ and 5D coordinates $x^m = (x^\alpha, y)$, where y parameterizes the extra dimension compactified on the closed interval $[-\pi R, +\pi R]$, and Z_2 symmetry is imposed. For $N = 2, D = 5$ supergravity in the bulk Eq. (A1) can be written as

$$S = \frac{1}{2} \int d^4x \int_{-\pi R}^{+\pi R} dy \sqrt{g_5} \left[M_5^3 (R_{(5)} - 2\Lambda_5) + L_{\text{SUGRA}}^{(5)} + \sum_i \delta(y - y_i) L_{4i} \right], \quad (\text{A2})$$

which is a generalization of the scenario described in [47]. Written explicitly, the contribution from bulk SUGRA in the action is given by [24]

$$e_{(5)}^{-1} L_{\text{SUGRA}}^{(5)} = -\frac{R^{(5)}}{2} + \frac{i}{2} \bar{\Psi}_{i\bar{m}} \Gamma^{\bar{m}\bar{n}\bar{q}} \nabla_{\bar{n}} \Psi_{\bar{q}}^i - S_{IJ} F_{\bar{m}\bar{n}}^I F^{I\bar{m}\bar{n}} - \frac{1}{2} g_{\alpha\beta} (D_{\bar{m}} \phi^\mu) (D^{\bar{m}} \phi^\nu) + \text{Fermionic} + \text{Chern - Simons}, \quad (\text{A3})$$

Including the contribution from the radion fields $\chi = -\psi_5^2$ and $T = \frac{1}{\sqrt{2}} (e_5^5 - i\sqrt{\frac{2}{3}} A_5^0)$, the effective brane-SUGRA counterpart turns out to be

$$\delta(y) L_4 = -e_{(5)} \Delta(y) [(\partial_\alpha \phi)^\dagger (\partial^\alpha \phi) + i \bar{\chi} \bar{\sigma}^\alpha D_\alpha \chi]. \quad (\text{A4})$$

Here, $\Delta(y) = e_5^5 \delta(y)$ is the modified Dirac delta function which satisfies the normalization conditions $\int_{-\pi R}^{+\pi R} dy e_5^5 \Delta(y) = 1$, $\int_{-\pi R}^{+\pi R} dy e_5^5 = \mathcal{L}$, where \mathcal{L} is the 5D volume. The Chern-Simons terms can be gauged away, assuming cubic constraints [24,25] and Z_2 symmetry. It is useful to define the 5D generalized *kähler* function (G) in this context as [24,25] $G = -3 \ln(\frac{T+T^\dagger}{\sqrt{2}}) + \delta(y) \times \frac{\sqrt{2}}{T+T^\dagger} K(\phi, \phi^\dagger)$, which precisely represents interaction of the radion with gauge fields. Including the kinetic term of the 5D field ϕ , the singular terms measured from the modified Dirac delta function can be rearranged into a perfect square thereby leading to the following expression for the action:

$$S \supset \frac{1}{2} \int d^4x \int_{-\pi R}^{+\pi R} dy \sqrt{g_5} e_{(4)} e_5^5 \left[g^{\alpha\beta} G_m^n (\partial_\alpha \phi^m)^\dagger (\partial_\beta \phi_n) + \frac{1}{g_{55}} (\partial_5 \phi - \sqrt{H(G)} \Delta(y))^2 \right], \quad (\text{A5})$$

where $H(G) = \exp(\frac{G}{M^2}) [(\frac{\partial W}{\partial \phi_m} + \frac{\partial G}{\partial \phi_m} \frac{W}{M^2})^\dagger (G_m^n)^{-1} (\frac{\partial W}{\partial \phi^n} + \frac{\partial G}{\partial \phi^n} \frac{W}{M^2}) - 3 \frac{|W|^2}{M^2}]$. It is worthwhile to mention that from Eq. (A5) we can compute energy momentum tensor for $N = 2, D = 5$ SUGRA can be expressed as

$$T_{\alpha\beta} = G_m^n (\partial_\alpha \phi^m)^\dagger (\partial_\beta \phi_n) - g_{\alpha\beta} [g^{\rho\sigma} (\partial_\rho \phi^m)^\dagger (\partial_\sigma \phi_n) G_m^n + g^{55} (\partial_5 \phi - \sqrt{H(G)} \Delta(y))^2], \quad (\text{A6})$$

$$T_{55} = \frac{1}{2} (\partial_5 \phi - \sqrt{H(G)} \Delta(y))^2 - \frac{1}{2} g_{55} g^{\rho\sigma} G_m^n (\partial_\rho \phi^m)^\dagger (\partial_\sigma \phi_n). \quad (\text{A7})$$

On the other hand, by varying the action written in Eq. (A5) with respect to the scalar field ϕ , the equation of motion for $N = 2, D = 5$ SUGRA can be expressed as

$$\partial_5 \left[\frac{e_5^5 \sqrt{g_5}}{g_{55}} (\partial_5 \phi - \sqrt{H(G)} \Delta(y)) \right] + \sum_n e_5^5 \left\{ \partial_\beta [\sqrt{g_5} g^{\alpha\beta} G_m^n (\partial_\alpha \phi^m)] - \frac{\sqrt{g_5}}{g_{55}} \Delta(y) \partial_n (\sqrt{H(G)}) (\partial_5 \phi - \sqrt{H(G)} \Delta(y)) \right\} = 0. \quad (\text{A8})$$

Further, imposing Z_2 symmetry to ϕ via $\phi(0) = \phi(\pi R) = 0$ and compactifying around a circle (S^1), $\partial_5 \phi = \sqrt{H(G)} (\Delta(y) - \frac{1}{2\pi R})$ we get

$$S = \frac{1}{2} \int d^4x \int_{-\pi R}^{+\pi R} dy \sqrt{g_5} \left[M_5^3 (R_{(5)} - 2\Lambda_5) + e_{(4)} e_5^5 \left\{ g^{\alpha\beta} G_m^n (\partial_\alpha \phi^m)^\dagger (\partial_\beta \phi_n) - g^{55} \frac{H(G)}{4\pi^2 R^2} \right\} \right]. \quad (\text{A9})$$

To discuss, in greater detail, the dimensional reduction technique in the regularized fashion here, the metric structure in $D = 5$ in conformal form is given by

$$ds_5^2 = e^{2A(y)} (ds_4^2 + R^2 \beta^2 dy^2), \quad (\text{A10})$$

where the $D = 4$ metric $ds_4^2 = g^{\alpha\beta} dx_\alpha dx_\beta$ is the well-known Friedmann Lemaître Robertson Walker (FLRW) metric. The numerical constant β has been introduced just for convenience and physically determines the slope of the warp factor $e^{2A(y)}$. Consequently, we can express the solution of $D = 5$ Einstein equations explicitly in terms of β when the warp factor is expressed as

$$e^{2A(y)} = \frac{b_0^2}{R^2(e^{\beta y} + \frac{\Lambda_5 b_0^4}{24R^2} e^{-\beta y})}, \tag{A11}$$

where b_0 is a constant having dimension of length. To trace out all the significant contribution from the fifth dimension using the dimensional reduction technique, we use method of separation of variable $\phi^m = \phi(x^\mu, y) = \phi(x^\mu)\chi(y)$, which leads to

$$\begin{aligned} S &= \frac{1}{2} \int d^4x \sqrt{g_4} \int_{-\pi R}^{+\pi R} dy \left\{ \beta M_5^3 R e^{3A(y)} \left[R_{(4)} - \frac{12}{\beta^2 R^2} \left(\frac{dA(y)}{dy} \right)^2 - \frac{8}{\beta^2 R^2} \left(\frac{d^2 A(y)}{dy^2} \right) - 2\Lambda_5 e^{2A(y)} \right] + \frac{e_4}{b_0} \Delta(y) (\partial_\alpha \phi^\mu)^\dagger \right. \\ &\quad \times (\partial^\alpha \phi_\mu) \left(\frac{\partial^2 K(\phi, \phi^\dagger)}{\partial \phi_\mu^\dagger \partial \phi^\nu} \right) + C(T, T^\dagger) \frac{e_4}{b_0} \frac{\Delta(y)}{4\pi^2 R^2} e^{(K(\phi, \phi^\dagger)/M^2)} \left[\left(\frac{\partial W}{\partial \phi_\alpha} + \left(\frac{\partial K(\phi, \phi^\dagger)}{\partial \phi_\alpha} \right) \frac{W}{M^2} \right)^\dagger \left(\frac{\partial^2 K(\phi, \phi^\dagger)}{\partial \phi^\alpha \partial \phi_\beta^\dagger} \right)^{-1} \right. \\ &\quad \left. \left. \times \left(\frac{\partial W}{\partial \phi^\beta} + \left(\frac{\partial K(\phi, \phi^\dagger)}{\partial \phi^\beta} \right) \frac{W}{M^2} \right) - 3 \frac{|W|^2}{M^2} \right] \right\}, \\ &= \frac{1}{2} \int d^4x \sqrt{g_4} \left\{ M_{\text{PL}}^2 \left[R_{(4)} - P \int_{-\pi R}^{+\pi R} dy \frac{4(3e^{2\beta y} + 3\lambda^2 e^{-2\beta y} - 2\lambda)}{R^2(e^{\beta y} + \lambda e^{-\beta y})^5} \right] + \frac{e_4}{b_0} (\partial_\alpha \phi^\mu)^\dagger (\partial^\alpha \phi_\mu) \left(\frac{\partial^2 K(\phi, \phi^\dagger)}{\partial \phi_\mu^\dagger \partial \phi^\nu} \right) \right. \\ &\quad \left. + \frac{e_4 C(T, T^\dagger)}{4\pi^2 R^2 b_0} e^{(K(\phi, \phi^\dagger)/M^2)} \left[\left(\frac{\partial W}{\partial \phi_\alpha} + \left(\frac{\partial K(\phi, \phi^\dagger)}{\partial \phi_\alpha} \right) \frac{W}{M^2} \right)^\dagger \left(\frac{\partial^2 K(\phi, \phi^\dagger)}{\partial \phi^\alpha \partial \phi_\beta^\dagger} \right)^{-1} \left(\frac{\partial W}{\partial \phi^\beta} + \left(\frac{\partial K(\phi, \phi^\dagger)}{\partial \phi^\beta} \right) \frac{W}{M^2} \right) - 3 \frac{|W|^2}{M^2} \right] \right\} \\ &= \frac{M_{\text{PL}}^2}{2} \int d^4x \sqrt{g_4} \left[R_{(4)} - P \int_{-\pi R}^{+\pi R} dy \frac{4(3e^{2\beta y} + 3\lambda^2 e^{-2\beta y} - 2\lambda)}{R^2(e^{\beta y} + \lambda e^{-\beta y})^5} + \left(\frac{\partial^2 K(\phi, \phi^\dagger)}{\partial \phi_\mu^\dagger \partial \phi^\nu} \right) (\partial_\alpha \phi^\mu)^\dagger (\partial^\alpha \phi_\nu) - Q V_F \right], \tag{A12} \end{aligned}$$

where $P = \frac{2M_5^3 \beta b_0^6}{M_{\text{PL}}^2 R^5}$, $Q = \frac{C(T, T^\dagger)}{4\pi^2 R^2}$, $M_{\text{PL}} = M_4 = \sqrt{\frac{e_4}{b_0}} = \sqrt{\frac{6e_4}{\lambda}} = M_5^{3/2} \sqrt{V_{\text{EXTRA}}} = \frac{1}{\kappa_4} = \sqrt{\frac{6}{\lambda} \frac{1}{\kappa_5^2}}$, $\lambda = \frac{\Lambda_5 b_0^4}{24R^2}$ and the compactification volume of the extra dimension $V_{\text{EXTRA}} = \frac{3M_5^3}{4\pi\lambda}$. Here $C(T, T^\dagger)$ represents an arbitrary function of T and T^\dagger . So Eq. (A12) explicitly shows that the theory is reduced to an effective $N = 1, D = 4$ SUGRA theory. For a general physical situation of $N = 1, D = 4$ supergravity in the brane where the F-term potential on the brane defined earlier is modified as [1,2]

$$\begin{aligned} V_F &= \exp\left(\frac{K(\phi, \phi^\dagger)}{M^2}\right) \left[\left(\frac{\partial W}{\partial \Psi_\alpha} + \left(\frac{\partial K}{\partial \Psi_\alpha} \right) \frac{W}{M^2} \right)^\dagger \right. \\ &\quad \left. \times \left(\frac{\partial^2 K}{\partial \Psi_\alpha \partial \Psi_\beta^\dagger} \right)^{-1} \left(\frac{\partial W}{\partial \Psi^\beta} + \left(\frac{\partial K}{\partial \Psi^\beta} \right) \frac{W}{M^2} \right) - 3 \frac{|W|^2}{M^2} \right]. \tag{A13} \end{aligned}$$

Here Ψ^α is the chiral superfield and ϕ^α is the complex scalar field. From now on the inflaton field ϕ appears to be 4D, as demonstrated earlier. Consequently, for effective $N = 1, D = 4$ SUGRA Eqs. (A6) and (A8) reduce to $T_{\alpha\beta} = \frac{g_{\alpha\beta} e_4 V_F}{2\pi b_0 R}$ and $\partial_\beta (\sqrt{g_4} \partial^\beta \phi) + Q V'_F(\phi) = 0$. In this context, we assume that the Kähler potential is dominated by the leading-order term (first-term) in canonical basis of the series representation i.e. $K = \sum_\alpha \phi_\alpha^\dagger \phi^\alpha$. The superpotential in Eq. (A13) is given by $W = \sum_{n=0}^\infty D_n W_n(\phi^\alpha)$ with the constraint $D_0 = 1$. Here, $W_n(\phi^\alpha)$ is a holomor-

phic function of ϕ^α in the complex plane. Consequently, in the canonical basis Eq. (A12) takes the following form:

$$\begin{aligned} S &= \frac{M_{\text{PL}}^2}{2} \int d^4x \sqrt{g_4} \\ &\quad \times \left[R_{(4)} - P \int_{-\pi R}^{+\pi R} dy \frac{4(3e^{2\beta y} + 3\lambda^2 e^{-2\beta y} - 2\lambda)}{R^2(e^{\beta y} + \lambda e^{-\beta y})^5} \right. \\ &\quad \left. + (\partial_\alpha \phi^\mu)^\dagger (\partial^\alpha \phi_\mu) - Q V_F \right], \tag{A14} \end{aligned}$$

where the F-term potential can be recast as ($V_D = 0 \Leftrightarrow U(1)$ gauge interaction is absent) [49]

$$\begin{aligned} V &= V_F = \exp\left[\frac{1}{M^2} \sum_\alpha \phi_\alpha^\dagger \phi^\alpha \right] \\ &\quad \times \left[\sum_\beta \left| \frac{\partial W}{\partial \phi_\beta} \right|^2 - 3 \frac{|W|^2}{M^2} \right]. \tag{A15} \end{aligned}$$

Now we expand the slowly varying inflaton potential derived from F-term around the value of the inflaton field, where the quantum fluctuation is governed by $\phi \rightarrow \tilde{\phi} + \phi$ ($\tilde{\phi}$ being the value of the inflaton field where structure formation occurs) and by imposing Z_2 , removing all odd-order terms responsible for gravitational instabilities, the required renormalizable inflaton potential turns out to be [50] $V = \Delta^4 \sum_{m=0}^2 C_{2m} \left(\frac{\phi}{M}\right)^{2m}$, with another constraint $C_0 = 1$. The mass term decides the steepness of the

potential. Absence of this term indicates that the process is slow, which is compensated by brane tension in the brane-world scenario [51]. For the phenomenological purpose, this specific choice is completely viable. But to incorporate thermal history of the universe leading to reheating and baryogenesis among others, we need to perform the one-loop-corrected finite temperature extension [52] of our model. Now translating the momentum integral within a specified cutoff (Λ), the effective potential turns out to be

$$V(\phi) = \Delta^4 + \frac{g}{4!} \phi^4 + \frac{g^2 \phi^4}{(16\pi)^2} \left[\ln\left(\frac{\phi^2}{\Lambda^2}\right) - \frac{25}{6} \right] + O(\lambda^3), \quad (\text{A16})$$

where the coupling constant $g = \frac{24\Delta^4 C_4}{M^4}$. Here C_4 is a tree-level constant, which [34] is, in general, defined as $g(M) = \frac{d^4 V(\phi)}{d\phi^4} \Big|_{\phi=M} = g + \frac{g^2}{(8\pi)^2} [6 \ln(\frac{M^2}{\Lambda^2})] + O(g^3)$ so that

the general expression for the effective potential in terms of all finite physical parameters is given by

$$V(\phi) = \Delta^4 + \frac{g(M)}{4!} \phi^4 + \frac{g^2(M) \phi^4}{(16\pi)^2} \left[\ln\left(\frac{\phi^2}{M^2}\right) - \frac{25}{6} \right] + O(g(M)^3), \quad (\text{A17})$$

which is the Coleman-Weinberg potential [31,32]. After substituting the expression for g in terms of C_4 , the one-loop-corrected potential can be expressed as

$$V(\phi) = \Delta^4 \left[1 + \left(D_4 + K_4 \ln\left(\frac{\phi}{M}\right) \right) \left(\frac{\phi}{M} \right)^4 \right], \quad (\text{A18})$$

where $K_4 = \frac{9\Delta^4 C_4^2}{2\pi^2 M^4}$, $D_4 = C_4 - \frac{25K_4}{12}$. This is precisely the potential Eq. (2.1) mentioned in inflationary model building in the present paper.

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