

**Effect of the reactor antineutrino anomaly on the first Double-Chooz results**

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We investigate the possible effects of short-baseline  $\bar{\nu}_e$  disappearance implied by the reactor antineutrino anomaly on the Double-Chooz determination of  $\vartheta_{13}$  through the normalization of the initial antineutrino flux with the Bugey-4 measurement. We show that the effects are negligible and the value of  $\vartheta_{13}$  obtained by the Double-Chooz collaboration is accurate only if  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ . For smaller values of  $\Delta m_{41}^2$  the short-baseline oscillations are not fully averaged at Bugey-4 and the uncertainties due to the reactor antineutrino anomaly can be of the same order of magnitude of the intrinsic Double-Chooz uncertainties.

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The first results [1] of the Double-Chooz experiment [2] led to the following result for the amplitude of long-baseline  $\bar{\nu}_e$  disappearance:

$$\sin^2 2\vartheta_{13}^{\text{DC}} = 0.085 \pm 0.029 \pm 0.042. \quad (1)$$

This amplitude enters in the effective long-baseline (LBL) survival probability of  $\bar{\nu}_e$  in the case of three-neutrino mixing (see Ref. [3]),

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{DC}} = 1 - \sin^2 2\vartheta_{13}^{\text{DC}} \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right), \quad (2)$$

which has been assumed in the analysis of the data by the Double-Chooz collaboration [1]. Here we adopt the standard parameterization of the mixing matrix, with  $|U_{e3}| = \sin\vartheta_{13}$ .

An essential ingredient in the extraction of the value of  $\sin^2 2\vartheta_{13}^{\text{DC}}$  from the data is the normalization of the initial flux prediction on the value measured by the Bugey-4 experiment [4], since the first results of the Double-Chooz experiment have been obtained with the far detector only [1]. This normalization is important because the recent recalculations of the reactor  $\bar{\nu}_e$  flux [5,6] indicate a value which is larger than that measured by Bugey-4 and other short-baseline reactor antineutrino experiments, leading to the reactor antineutrino anomaly [7]. The ratio of observed and theoretically predicted  $\bar{\nu}_e$  flux for the Bugey-4 experiment is [7]

$$\frac{\phi_{\text{Bugey-4}}^{\text{obs}}}{\phi_{\text{Bugey-4}}^{\text{the}}} = 0.942 \pm 0.042, \quad (3)$$

and the average ratio of observed and theoretically predicted  $\bar{\nu}_e$  fluxes in short-baseline reactor antineutrino experiments is [8]

$$\frac{\phi_{\text{SBL}}^{\text{obs}}}{\phi_{\text{SBL}}^{\text{the}}} = 0.946 \pm 0.024, \quad (4)$$

which is a  $2.2\sigma$  effect. Several experiments which could check the reactor antineutrino anomaly have been proposed and some are already under preparation [9–18].

In this letter we investigate if the short-baseline  $\bar{\nu}_e$  disappearance implied by the reactor antineutrino anomaly has an effect in the determination of  $\vartheta_{13}$ , in spite of the normalization of the initial antineutrino flux with the Bugey-4 measurement.

In general, the  $\bar{\nu}_e$  flux measured in the Double-Chooz far detector is given by

$$\phi_{\bar{\nu}_e}^{\text{LBL}} = \phi_{\bar{\nu}_e}^0 P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{LBL}}, \quad (5)$$

where  $\phi_{\bar{\nu}_e}^0$  is the  $\bar{\nu}_e$  flux produced by the reactor and  $P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{LBL}}$  is the effective LBL  $\bar{\nu}_e$  survival probability.

In the simplest framework of  $3 + 1$  neutrino mixing, which can accommodate short-baseline neutrino oscillations together with the well-established atmospheric (long-baseline) and solar neutrino oscillations (see the recent Refs. [8,19–23], and references therein), the effective long-baseline  $\bar{\nu}_e$  survival probability is given by [24]

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{LBL}} = 1 - \cos^4 \vartheta_{14} \sin^2 2\vartheta_{13} \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) - \frac{1}{2} \sin^2 2\vartheta_{14}, \quad (6)$$

where the oscillations due to  $\Delta m_{41}^2 \gg \Delta m_{31}^2$  have been averaged and we adopted a parameterization of the four-neutrino mixing matrix in which  $|U_{e3}| = \sin\vartheta_{13} \cos\vartheta_{14}$  and  $|U_{e4}| = \sin\vartheta_{14}$ .

We can calculate the value of  $\sin^2 2\vartheta_{13}$ , taking into account the reactor antineutrino anomaly, by noting that in the analysis of the Double-Chooz collaboration the  $\bar{\nu}_e$  flux measured in the far detector has been fitted with

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$$\phi_{\bar{\nu}_e}^{\text{LBL}} = \phi_{\bar{\nu}_e}^{\text{SBL}} P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{DC}}. \quad (7)$$

where  $\phi_{\bar{\nu}_e}^{\text{SBL}}$  is the short-baseline  $\bar{\nu}_e$  flux inferred from the Bugey-4 measurement, taking into account the differences between the Bugey and Chooz reactors. In the framework of 3 + 1 neutrino mixing, the short-baseline  $\bar{\nu}_e$  flux is given by

$$\phi_{\bar{\nu}_e}^{\text{SBL}} = \phi_{\bar{\nu}_e}^0 (1 - A_{\text{B4}} \sin^2 2\vartheta_{14}), \quad (8)$$

where  $A_{\text{B4}}$  is the average of  $\sin^2(\Delta m_{41}^2 L/4E)$  in the Bugey-4 experiment. The value of this quantity is plotted in Fig. 1 as a function of  $\Delta m_{41}^2$ . One can see that  $\sin^2(\Delta m_{41}^2 L/4E)$  is fully averaged ( $A_{\text{B4}} \approx 1/2$ ) for  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ , but for smaller values of  $\Delta m_{41}^2$  the average  $A_{\text{B4}}$  can be significantly different from 1/2.

Let us first consider the case of  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ , for which  $A_{\text{B4}} \approx 1/2$ . In this case, from Eqs. (5), (6), and (8), the  $\bar{\nu}_e$  flux measured in the Double-Chooz far detector can be written as

$$\phi_{\bar{\nu}_e}^{\text{LBL}} = \phi_{\bar{\nu}_e}^{\text{SBL}} \left[ 1 - \frac{\cos^4 \vartheta_{14} \sin^2 2\vartheta_{13}}{1 - \frac{1}{2} \sin^2 2\vartheta_{14}} \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right) \right]. \quad (9)$$

Comparing Eq. (7) with  $P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{\text{DC}}$  given by Eq. (2) and (9), we obtain

$$\sin^2 2\vartheta_{13} = \sin^2 2\vartheta_{13}^{\text{DC}} \frac{1 - \frac{1}{2} \sin^2 2\vartheta_{14}}{\cos^4 \vartheta_{14}}, \quad (10)$$

which gives the connection between  $\vartheta_{13}^{\text{DC}}$  and the pair  $\vartheta_{13}$ ,  $\vartheta_{14}$  for  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ .

Equation (10) shows that in principle, normalizing the initial neutrino flux at a value measured by a short-baseline

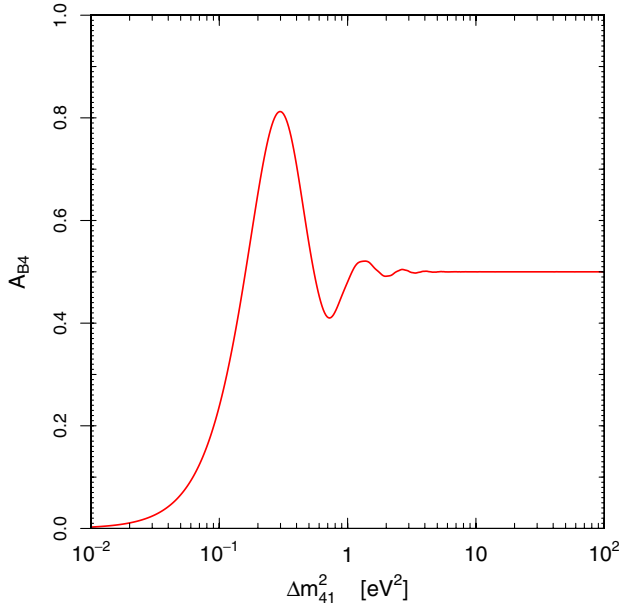


FIG. 1 (color online). Averaged value of  $\sin^2(\Delta m_{41}^2 L/4E)$  in the Bugey-4 experiment as a function of  $\Delta m_{41}^2$ .

experiment as the Bugey-4 experiment is not sufficient to take into account the effects of short-baseline oscillations. However, in practice the correction is small because the reactor antineutrino anomaly implies that  $\vartheta_{14}$  is small, which leads to

$$\left( 1 - \frac{1}{2} \sin^2 2\vartheta_{14} \right) / \cos^4 \vartheta_{14} = 1 + \mathcal{O}(\vartheta_{14}^4). \quad (11)$$

In this case, the long-baseline Double-Chooz data determine the value of  $\sin^2 2\vartheta_{13}$  independently from the value of  $\sin^2 2\vartheta_{14}$ , which is determined by the short-baseline reactor antineutrino anomaly.

Let us now consider values of  $A_{\text{B4}}$  different from 1/2, which can be realized if  $\Delta m_{41}^2 \lesssim 3 \text{ eV}^2$ , and as one can see from Fig. 1. In this case, the contribution of  $\phi_{\bar{\nu}_e}^{\text{SBL}}$  to  $\phi_{\bar{\nu}_e}^{\text{LBL}}$  cannot be factorized as in Eq. (9). Therefore, in order to find the value of  $\sin^2 2\vartheta_{13}$  given by Double-Chooz data, we must fit these data. We performed an approximate fit, extracting the necessary information from the figures in Ref. [1]. The results are shown in Fig. 2, where we plotted the value of  $\sin^2 2\vartheta_{13}$  as a function of  $\sin^2 2\vartheta_{14}$  for different values of  $A_{\text{B4}}$ . Figure 2 also shows the best-fit value of  $\sin^2 2\vartheta_{14}$  and its  $1\sigma$ ,  $2\sigma$  and  $3\sigma$  allowed ranges obtained from the fit of short-baseline reactor antineutrino data [22]. One can see that the deviation of  $\sin^2 2\vartheta_{13}$  from  $\sin^2 2\vartheta_{13}^{\text{DC}}$  in the allowed-band of  $\sin^2 2\vartheta_{14}$  is negligible for  $A_{\text{B4}} = 1/2$ , according to the discussion above. On the other hand, the deviation of  $\sin^2 2\vartheta_{13}$  from  $\sin^2 2\vartheta_{13}^{\text{DC}}$  can be relatively

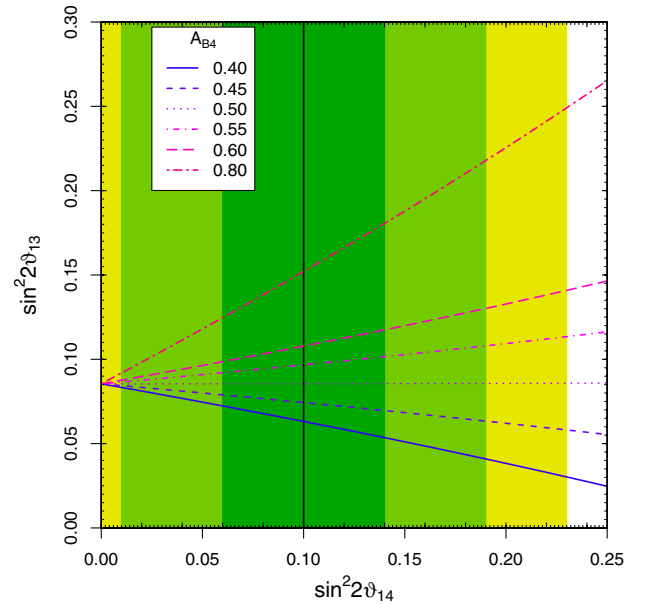


FIG. 2 (color online).  $\sin^2 2\vartheta_{13}$  as a function of  $\sin^2 2\vartheta_{14}$  obtained from Eq. (10) and the best-fit value of the Double-Chooz measure in Eq. (1) for different values of  $A_{\text{B4}}$ . The vertical solid black line gives the best-fit value of  $\sin^2 2\vartheta_{14}$  obtained from the fit of short-baseline reactor antineutrino data [22]. The colored vertical bands show the corresponding  $1\sigma$ ,  $2\sigma$ ,  $3\sigma$  allowed ranges.

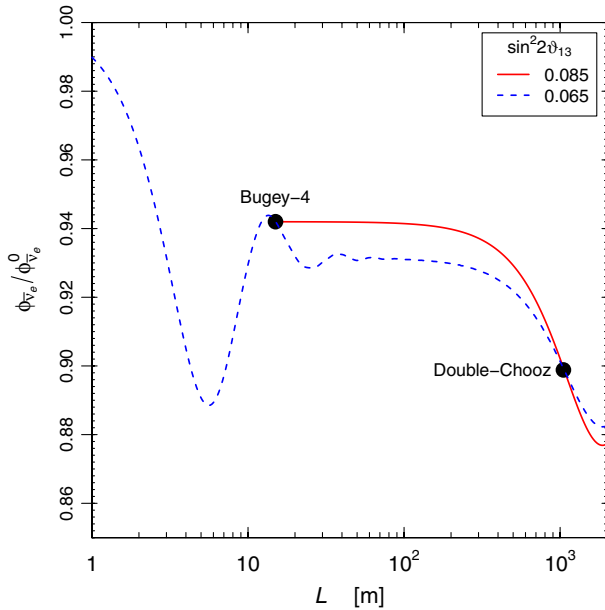


FIG. 3 (color online). Relative suppression of the averaged reactor electron antineutrino flux as a function of distance. The red, solid curve is calculated using the three-neutrino mixing survival probability in Eq. (2) with  $\Delta m_{31}^2 = 2.4 \times 10^{-3} \text{ eV}^2$  and the Double-Chooz best-fit value of  $\sin^2 2\vartheta_{13}^{\text{DC}}$  in Eq. (1) and by normalizing the flux at the value measured by the Bugey-4 experiment at  $L = 15 \text{ m}$ . The blue, dashed curve is calculated with the four-neutrino mixing survival probability (see Eq. (2.8) of Ref. [24]) and  $\Delta m_{31}^2 = 2.4 \times 10^{-3} \text{ eV}^2$ ,  $\sin^2 2\vartheta_{13} = 0.065$ ,  $\Delta m_{41}^2 = 0.8 \text{ eV}^2$  and  $\sin^2 2\vartheta_{14} = 0.14$ . The values of  $\sin^2 2\vartheta_{13}$  and  $\sin^2 2\vartheta_{14}$  have been chosen in order to fit both the Bugey-4 and Double-Chooz data points.

large for values of  $A_{B4}$  different from  $1/2$ . Therefore, the uncertainty due to short-baseline oscillations must be taken into account in the extraction of  $\sin^2 2\vartheta_{13}$  from the Double-Chooz data if  $\Delta m_{41}^2 \lesssim 3 \text{ eV}^2$ .

The cause of the deviation of  $\sin^2 2\vartheta_{13}$  from  $\sin^2 2\vartheta_{13}^{\text{DC}}$  when the short-baseline oscillations are not fully averaged at Bugey-4 is illustrated in Fig. 3, where we plotted the relative decrease of the averaged reactor electron antineutrino flux as a function of distance. The red, solid curve shows the suppression of the Bugey-4 flux for larger distances calculated using the three-neutrino mixing survival probability in Eq. (2) with the Double-Chooz best-fit value of  $\sin^2 2\vartheta_{13}^{\text{DC}}$  in Eq. (1). The blue, dashed curve is calculated with the four-neutrino mixing survival probability (see Eq. (2.8) of Ref. [24]) and oscillation parameters chosen in order to fit both the Bugey-4 and Double-Chooz data points. One can see that since the short-baseline oscillations are not fully averaged at Bugey-4, the residual short-baseline oscillations at larger distances contribute to the suppression of the flux and the fit of the Double-Chooz data point requires a value of  $\sin^2 2\vartheta_{13}$ , which is smaller than  $\sin^2 2\vartheta_{13}^{\text{DC}}$ .

In the following we estimate the uncertainty of the determination of  $\sin^2 2\vartheta_{13}$  from Double-Chooz data

implied by the fit of short-baseline reactor antineutrino data [22].

Figure 4 shows the value of  $\sin^2 2\vartheta_{14}$  as a function of  $\Delta m_{41}^2$  obtained from the fit of short-baseline reactor antineutrino data (see Ref. [22]). Note that Fig. 4 is obtained from a one-dimensional  $\chi^2$  analysis of short-baseline reactor antineutrino data for each fixed value of  $\Delta m_{41}^2$ . Hence, it is different from the usual two-dimensional  $\chi^2$  analyses which give allowed regions in the  $\sin^2 2\vartheta_{14}$ - $\Delta m_{41}^2$  plane (as, for example, Fig. 1 of Ref. [22]). The rapid decrease of the best-fit value of  $\sin^2 2\vartheta_{14}$  for  $\Delta m_{41}^2 \lesssim 0.2 \text{ eV}^2$  reflects the fact that the oscillation explanation of the reactor antineutrino anomaly requires larger values of  $\Delta m_{41}^2$ .

Figure 5 shows the value of  $\sin^2 2\vartheta_{13}$  as a function of  $\Delta m_{41}^2$  obtained from our approximate fit of Double-Chooz data and  $\sin^2 2\vartheta_{14}$  in Fig. 4. One can see that the deviation from  $\sin^2 2\vartheta_{13}^{\text{DC}}$  is smaller than about 1% for  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ , in agreement with the discussion above. On the other hand, the deviation of  $\sin^2 2\vartheta_{13}$  from  $\sin^2 2\vartheta_{13}^{\text{DC}}$  can be relatively large for smaller values of  $\Delta m_{41}^2$ , reaching about 40% at  $2\sigma$  for  $\Delta m_{41}^2 \approx 0.3 - 0.4 \text{ eV}^2$ .

Finally, using the constraints on  $\Delta m_{41}^2$  and  $\sin^2 2\vartheta_{14}$  obtained from a two-dimensional  $\chi^2$  analysis of short-baseline reactor antineutrino data [22], for the best-fit value of  $\sin^2 2\vartheta_{13}$  in our approximate fit of Double-Chooz data we obtain

$$\sin^2 2\vartheta_{13} = 0.084_{-0.010}^{+0.025}. \quad (12)$$

Here, the uncertainties are only those due to the analysis of short-baseline reactor antineutrino data. Hence, they must be added to the intrinsic Double-Chooz uncertainties in Eq. (1).

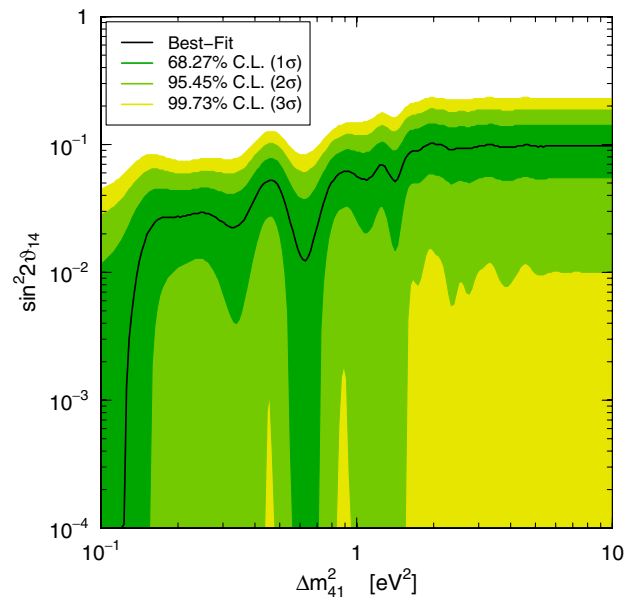


FIG. 4 (color online).  $\sin^2 2\vartheta_{14}$  as a function of  $\Delta m_{41}^2$  obtained from the fit of short-baseline reactor antineutrino data (see Ref. [22]).

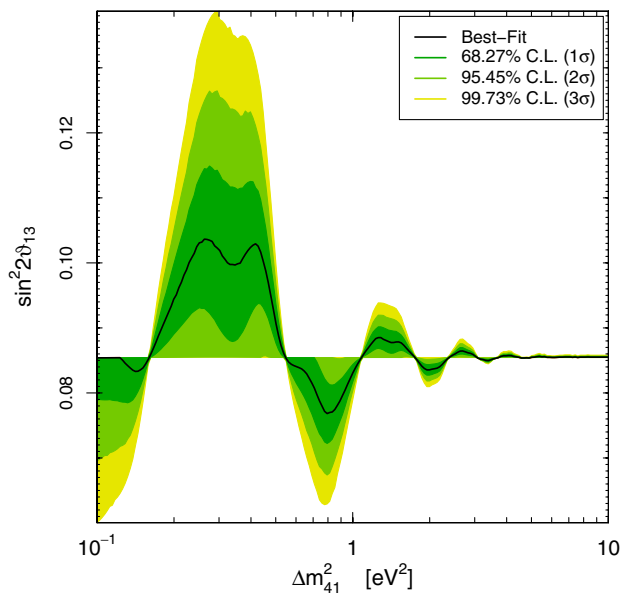


FIG. 5 (color online).  $\sin^2 2\vartheta_{13}$  as a function of  $\Delta m_{41}^2$  obtained from the best-fit value of the Double-Chooz measure in Eq. (1) and  $\sin^2 2\vartheta_{14}$  in Fig. 4.

The result in Eq. (12) shows that the uncertainties on the determination of  $\sin^2 2\vartheta_{13}$  due to the reactor antineutrino anomaly are comparable with the intrinsic Double-Chooz uncertainties in Eq. (1). Therefore, the reactor antineutrino anomaly must be taken into account in the extraction of the value of  $\sin^2 2\vartheta_{13}$  from Double-Chooz data.

In conclusion, we have shown that if the short-baseline oscillations indicated by the reactor antineutrino anomaly exists, in order to obtain the value of  $\vartheta_{13}$  in long-baseline reactor neutrino oscillation experiments it is not sufficient to normalize the flux at a value measured by a short-baseline experiment, because the short-baseline oscillations may be not fully averaged at such reference point. In the case of the first results of the Double-Chooz experiment [1], the flux has been normalized at the value measured by the Bugey-4 experiment [4], for which the short-baseline oscillations are fully averaged only for  $\Delta m_{41}^2 \gtrsim 3 \text{ eV}^2$ . We have shown that for smaller values of  $\Delta m_{41}^2$  the corrections due to short-baseline oscillations must be taken into account and that a neutrino oscillation analysis of the reactor antineutrino anomaly indicates that these corrections may be relevant.

Let us finally note that in the long-baseline reactor experiments with a near detector which is farther from the reactor than about 100 m (RENO [25], Daya Bay [26], Double-Chooz [2]) short-baseline oscillations are fully averaged for  $\Delta m_{41}^2 \gtrsim 0.1 \text{ eV}^2$ . Therefore, even if the reactor antineutrino anomaly is due to short-baseline oscillations, the value of  $\sin^2 2\vartheta_{13}$  can be extracted accurately from the data by comparing the near and far detection rates using the three-neutrino mixing survival probability in Eq. (2), independently of the reactor antineutrino anomaly. However, if  $\Delta m_{41}^2$  is sufficiently small, the medium-baseline  $\bar{\nu}_e$  flux measured in the near detector could be smaller than that measured in the Bugey-4 experiment and in other short-baseline reactor experiments (see Ref. [7]). This would be a confirmation of the reactor antineutrino anomaly.

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