## Higgs boson finder and mass estimator: The Higgs boson to WW to leptons decay channel at the LHC

Vernon Barger and Peisi Huang

Department of Physics, University of Wisconsin, Madison, Wisconsin 53706, USA (Received 26 July 2011; revised manuscript received 29 September 2011; published 7 November 2011)

We exploit the spin and kinematic correlations in the decay of a scalar boson into a pair of real or virtual W-bosons, with both W-bosons decaying leptonically, for Higgs boson discovery at 7 TeV LHC energy with 10 fb<sup>-1</sup> luminosity. Without reconstruction of the events, we obtain estimators of the Higgs mass from the peak and width of the signal distribution in  $m_{ll}$ . The separation of signal and background with other distributions, such as the azimuthal angle between two W decay planes, the rapidity difference between the two leptons, missing  $E_T$ , and the  $p_T$  of leptons, are also prescribed. Our approach identifies the salient Higgs to dilepton signatures that allow subtraction of the continuum  $W * W *$  background.

DOI: [10.1103/PhysRevD.84.093001](http://dx.doi.org/10.1103/PhysRevD.84.093001) PACS numbers: 14.80.Bn

The Higgs boson is the only missing brick of the stan-dard model (SM) [\[1\]](#page-6-0). The  $h \to W^+W^- \to l\nu l\nu$  channel has been of long interest for Higgs discovery [\[2–](#page-6-1)[7](#page-6-2)] because of its relatively clean signal and the large branching fraction for  $m_h$  near  $2m_W$ . The CDF and D0 experiments at the Tevatron and the ATLAS and CMS experiments at the LHC have searched for the  $h \to W^*W^* \to \mu \bar{\nu}_{\mu} \nu_{\mu} \bar{\mu}$  process and have excluded a SM Higgs in a range of  $m<sub>h</sub>$ around 166 GeV [\[8](#page-6-3)[–12\]](#page-6-4). The SM Higgs production cross section times the branching fraction to two W's in the SM is plotted in Fig. [1](#page-1-0). The maximum  $h \to W^*W^*$  signal from gluon fusion is at  $m_h = 165$  GeV. The dominant production at  $m_h < 1$  TeV occurs via the parton subprocess gluon + gluon  $\rightarrow h$  and WW-fusion takes over at  $m_h$  > 1 TeV [[13](#page-6-5)]. Higgs production via gluon fusion could be larger than this estimate if extra colored states contribute to the gluon fusion loop [\[14\]](#page-6-6), or it could be smaller if the weak coupling is shared by two neutral Higgs states, as would be the case in supersymmetry [[15](#page-6-7)], or if the Higgs has invisible decay modes.

Many phenomenological studies have been made of the  $h \to W^*W^*$  signal [\[16–](#page-6-8)[20](#page-7-0)] and that of the closely related  $h \rightarrow Z^*Z^*$  channel [[21](#page-7-1)[–25\]](#page-7-2). The \*WW\* signal identification with leptonic  $W*$  decay is challenging. With two missing neutrinos, the events are not fully reconstructible. Also, the  $W * W *$  signal may have similar kinematics as the continuum  $W * W*$  background. Since the background is much larger than the signal at the LHC, differences in the distributions of the signal and background must be used to identify and quantify the Higgs signal. A typical signal event in this channel for  $m_h = 160 \text{ GeV}$  is shown in the N (number of events) vs  $\eta$  (rapidity difference of the leptons) vs  $\phi$  (azimuthal angular difference of the leptons) plot in Fig. [2,](#page-1-1) along with that of a sample background event, illustrating that there can be distinguishing features. Our aim is to utilize the differences in the signal and background characteristics to enable a background subtraction and make a clear identification of any Higgs signal in novel ways that have not been fully explored in other studies. Our approach relies on the SM prediction of the background distributions from the  $q\bar{q} \rightarrow W^*W^*$  subprocess at next-toleading order (NLO) order [\[26\]](#page-7-3) with the rejection of QCD jets. The theory normalization of this background can be tested in ranges of the distributions where the Higgs signal of a given  $m_H$  does not contribute. Also, diboson production with final states one W and one Z (WZ) production can serve as an independent calibration of the WW background, since the WZ final state does not have a neutral Higgs signal contribution. Our focus is on the dilepton signal with missing transverse energy and no jets. Other backgrounds, such as  $t\bar{t}$  and single top production, can be suppressed by jet vetoing (for the zero jet signal), and the Drell-Yan background can be suppressed by a missing transverse energy requirement [\[27](#page-7-4)].

Nelson [[28](#page-7-5)] investigated the correlation between the two W decay planes to distinguish the Higgs signal from the WW background. Choi et al [\[24,](#page-7-6)[29\]](#page-7-7) studied the signal distributions in transverse mass variables [[30\]](#page-7-8). Dobrescu and Lykken [\[20\]](#page-7-0) computed the fully differential width for Higgs decays to  $l\nu jj$  and constructed distributions of  $m_{l\nu}$ ,  $m_{ij}$ , polar ( $\theta_l$ ) and azimuthal ( $\phi_l$ ) angles between the charged lepton in the  $l\nu$  rest frame and the  $W^+$  in the Higgs rest frame, and  $\theta_j$ , the angle between  $-(\rightarrow_{p_l} +$  $\rightarrow$ <sub>n</sub>) and the fastest jet direction in the Higgs rest frame.

Estimating the Higgs mass from the invariant mass of two leptons,—The matrix element for the Higgs signal is similar to that of muon decay, except for the placement of muon spinor and inclusion of off shell W propagators [[28\]](#page-7-5). We generated 200,000 events at four different Higgs mass points and  $W \times W \times$  background with Sherpa [\[31](#page-7-9)], which includes the exact tree level matrix element and QCD radiation, at 7 TeV LHC center of mass (cm) energy. Jets are defined using the anti-kt algorithm [\[32\]](#page-7-10) with  $R = 0.4$ , and the jet clusterings are implemented using the FASTJET package [[33](#page-7-11)]. We use HIGGSDECAY [\[34\]](#page-7-12) for calculation of the Higgs total and partial widths. We normalize the dilepton signal rate,  $l = e$ ,  $\mu$  for no jets to the

<span id="page-1-0"></span>

FIG. 1 (color online). SM Higgs production cross section times the branching fractions to two W's that decay leptonically.  $l = e, \mu.$ 

next-to-next-to-leading order (NNLO) calculation [\[35\]](#page-7-13), which is 104 fb at  $m_H = 120$  GeV, 389 fb at  $m_H =$ 160 GeV, 182 fb at  $m_H = 200$  GeV, and 83 fb at  $m_H =$ 300 GeV. The  $WW \rightarrow l\nu l\nu$  background is normalized to the NLO prediction [\[36\]](#page-7-14) of 2095 fb. These cross sections are for the dilepton final states with  $l = e$ ,  $\mu$  including the leptonic branching fractions. The  $m_{ll}$  distributions, with and without the WW background, are given in Fig. [3,](#page-1-2) each for 1 fb<sup>-1</sup> integrated luminosity. The width (w) of the  $m_{ll}$ distribution is given in Fig. [4.](#page-1-3) This width is large compared

<span id="page-1-1"></span>

FIG. 2. Sample events for the  $m_h = 160$  GeV signal and the  $W * W*$  background with no jets.

<span id="page-1-2"></span>

FIG. 3 (color online).  $m_{ll}$  event distribution of the SM Higgs signal at various  $m_h$  and the background from continuum  $W^*W^*$  production for 1 fb<sup>-1</sup> luminosity at 7 TeV, summed over  $l = e, \mu$ 

<span id="page-1-3"></span>

FIG. 4. Width (w) of the  $m_{ll}$  distribution of the Higgs signal compared to  $m_h$ . Note that at  $m_h = 150 \text{ GeV}(200 \text{ GeV})$ , w =  $\frac{1}{4}m_h(w = \frac{1}{3}m_h).$ 

<span id="page-2-0"></span>TABLE I. The signal and WW continuum background events at 7 TeV within the specified  $m_{ll}$ windows around the peak values. The number of events in the signal and background columns are for 10  $fb^{-1}$  integrated luminosity anticipated from ATLAS and CMS combined. Event numbers are summed over  $l = e$ ,  $\mu$ . No experimental cuts are applied here

$m_h$ (GeV)	$m_{II}$ window (GeV)	Signal inside window	Background inside window	Background outside window	
120	$10 - 50$	373	2746	7723	
160	$20 - 70$	1478	4326	6144	
200	$30 - 110$	687	6713	3756	
300	$60 - 200$	324	5901	4568	

to the total decay width of the Higgs boson, making it sensitive only to the Higgs mass. Here we only require two leptons and no jets, with no acceptance cuts.

The following empirical relationship between  $m_H$  and  $m_{ll}$  of the signal is found, where "peak" is the maximum and "end" is the end point of the  $m_{ll}$  distribution.

<span id="page-2-4"></span>
$$
m_H = 2(m_{llpeak}) + m_W
$$
  $m_H = m_{llend} + \frac{m_W}{2}$ . (1)



<span id="page-2-1"></span>

FIG. 5 (color online). The azimuthal angle between the two W decay planes, before cuts.

This relationship holds for all the Higgs mass points, including when one W is off shell, near the  $2m<sub>W</sub>$  threshold and well above the threshold. The signal and  $W \times W \times W$ background within windows around the peak values of  $m_{ll}$  are listed in Table [I.](#page-2-0) In addition, we find a rather tight correlation of the Higgs mass with the width of the  $m_{ll}$ distribution, as discussed below.

<span id="page-2-2"></span>Parametrization of the azimuthal angular distribution.— The correlation function for the azimuthal angle between the two W decay planes can be parametrized as [\[28\]](#page-7-5)

$$
F(\phi) = 1 + \alpha \cos \phi + \beta \cos 2\phi.
$$
 (2)

The direction of the normal to a W decay plane is defined as the cross product of momentum direction of the lepton with the beam direction. In Fig. [5](#page-2-1) we plot the  $\phi$  distribution of signal and the WW background and fit the normalized distributions to Eq. [\(2](#page-2-2)). The resulting  $\alpha$  and  $\beta$  values are given in Table [II](#page-2-3).

It can be seen that  $\alpha > 0$  in the transverse-transverse (TT) dominant region, while  $\alpha$  < 0 in the longitudinallongitudinal (LL) dominant region. At  $m_H = 1 +$  $\sqrt{17} m_W = 182 \text{ GeV}, \quad \Gamma(h \to W_T W_T) = \Gamma(h \to W_L W_L).$ The  $\phi$  distribution at  $m_H = 200$  GeV is almost flat, as expected. The WW background has  $\alpha < 0$  because it is LL dominant. The  $\phi$  distributions within different  $m_{ll}$  bins are shown in Fig. [6.](#page-3-0) In the  $m<sub>ll</sub> < 50$  GeV bin, signal and background are both dominantly TT, and in the high  $m_{ll}$ bin, both are dominantly LL.

The pseudorapidity difference  $\Delta \eta = |\eta_1 - \eta_2|$  of the two leptons is plotted in Fig. [7.](#page-4-0) Note that the charged leptons from signal are closer in  $\Delta \eta$  than for the background.

Background estimation.— Other variables can also differentiate signal from the background, such as  $E_T = p_T(l)$ 

<span id="page-2-3"></span>TABLE II. The  $\alpha$  and  $\beta$  parametrization from fit of Eq. [\(2\)](#page-2-2) to the  $\phi$  distributions

Higgs mass (GeV) 120 160 200 300 Background				
$\alpha$			$0.36$ $0.68$ $0.12$ $-0.95$	$-0.43$
	$-0.06$ $0.04$ $-0.17$ 0.22			0.09

<span id="page-3-0"></span>

FIG. 6 (color online).  $\phi$  distributions in different  $m_{ll}$  bins of the Higgs signals and the background, before cuts.

<span id="page-4-0"></span>

FIG. 7 (color online). Pseudorapidity difference  $\Delta \eta = |\eta_1 - \eta_2|$  $\eta_2$  of the two leptons, before cuts.

and the  $p_T$  distribution of the fastest lepton,  $p_{T1}$ , shown in Fig. [8.](#page-4-1)

The  $p<sub>T</sub>$  distribution of the fastest lepton is very sensitive to the Higgs mass. This distribution is sharply peaked for  $m_h = 160$  GeV. A recent proposed variable,  $\phi^*$  [\[37\]](#page-7-15), is plotted in Fig. [9.](#page-5-0)  $\phi^*$  is defined as  $\phi^* = \tan[(\pi - \phi)/2] \times$  $\sin\theta^*$ , where  $\phi$  is the azimuthal angle between the two leptons and  $\cos \theta^* = \tanh[(\eta^- - \eta^+)/2]$ , with  $\eta^- (\eta^+)$ being the pseudorapidity of the negatively charged lepton. It has been argued that  $\phi^*$  may be more precisely determined than  $\phi$ .

The sum of the energy of the two leptons is shown in Fig. [10.](#page-5-1) The peak value of the  $E(l^+) + E(l^-)$  distribution of the signal is corelated with  $m_H$ .

Application of acceptance cuts for background rejection.— Other backgrounds include  $t\bar{t}$  pair production, single top production,  $W($ or  $Z$  $)$  + jets, the Drell-Yan process (which does not contribute to the  $e\mu$  events), and  $\tau\bar{\tau}$ 

<span id="page-4-1"></span>

FIG. 8 (color online). The  $\not{E}_T = pT(l)$  distribution and the  $p_T$ distribution of the fastest lepton, before cuts. Note the sharply peaked  $p_{T1}$  from  $m_H = 160$  GeV.

<span id="page-5-0"></span>

FIG. 9 (color online).  $\phi^*$  distribution, before cuts.

<span id="page-5-1"></span>

FIG. 10 (color online). Sum of energy of the two leptons, before cuts.

production. All these backgrounds can be suppressed by vetoing the jets and suitable cuts on the distributions of the variables discussed above. We apply cuts following a recent ATLAS study [\[27\]](#page-7-4).

- (i) Cut 1: no jets.
- (ii) Cut 2:  $m_{ll} > 15$  GeV.
- (iii) Cut 3 :  $E_T > 30$  GeV.
- (iv) Cut 4:  $p_T^{l_l} > 30$  GeV.
- (v) Cut 5:  $\delta \phi_{ll} < 1.8$ .

Figure [11](#page-5-2) shows that the shape of the  $m_{ll}$  distribution does not change under those cuts.

The  $\phi$  distribution after experimental cuts is shown in Fig. [12.](#page-6-9) The TT component is reduced by the  $m_{ll}$  cut.

The analysis of ATLAS shows that all the backgrounds  $φ*$  except  $W * W*$  can be suppressed by cuts similar to those

<span id="page-5-2"></span>

FIG. 11 (color online).  $m_{ll}$  event distribution, after cuts, of the SM Higgs signal (for various  $m_h$ ) and the continuum  $W * W*$  background for 1 fb<sup>-1</sup> luminosity at 7 TeV, summed over  $l = e, \mu$ 

<span id="page-6-10"></span>TABLE III. The signal and background events at 7 TeV, after cuts, within the specified  $m<sub>ll</sub>$  windows around the peak values. The number of events in the signal and background columns are for 10 fb<sup>-1</sup> integrated luminosity anticipated from ATLAS and CMS combined. Event numbers are summed over  $l = e, \mu$ .

$m_h$ (GeV)	(GeV)	window	window	window	window	window	window	$m_{\rm II}$ window Signal inside WW inside $t\bar{t}$ inside Background inside WW outside $t\bar{t}$ outside Background outside window
120	$15 - 50$	45	638	151	789	743	118	861
160	$20 - 70$	303	899	189	1088	482	80	562
200	$30 - 110$	88	1022	220	1242	359	49	408
300	$60 - 200$	16	530	89	619	851	180	1031

<span id="page-6-9"></span>

FIG. 12 (color online). The azimuthal angle between the two W decay planes, after cuts.

given above [\[27\]](#page-7-4). Table [III](#page-6-10) shows signal and backgrounds within windows around peak value of  $m_{ll}$  after application of those cuts. Multivariable techniques, such as neural networks and boost decision trees, are another effective approach to background rejection.

Conclusions and outlook.—After subtracting the WW continuum background from the dilepton data, the Higgs mass can be estimated using Eq. ([1](#page-2-4)). The width of the  $m_{ll}$ distribution provides another good estimator of the Higgs mass. The  $m_{ll}$ ,  $p_T$ , and E distributions are truncated at their lower ends by the  $p_T$  and  $\eta$  acceptance cuts.

Our analysis techniques can be applied to scalars in other models that decay via the WW mode such as the radion [[38](#page-7-16)–[43](#page-7-17)] or a dilaton [\[44\]](#page-7-18). The merit of the  $m_{\mu}$  peak estimator in Eq. [\(1](#page-2-4)) and width estimator in Fig. [4](#page-1-3) is their simple dependences on the Higgs boson mass.

This work was supported in part by the U.S. Department of Energy under Grant No. DE-FG02-95ER40896.

- <span id="page-6-1"></span><span id="page-6-0"></span>[1] Abdelhak Djouadi, [Phys. Rep.](http://dx.doi.org/10.1016/j.physrep.2007.10.004) **457**, 1 (2008).
- [2] Wai-Yee Keung and W. J. Marciano, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.30.248) 30248 [\(1984\)](http://dx.doi.org/10.1103/PhysRevD.30.248).
- [3] E. W. N. Glover, J. Ohnemus, and Scott S. D. Willenbrock, Phys. Rev. D 37[, 3193 \(1988\)](http://dx.doi.org/10.1103/PhysRevD.37.3193).
- [4] V. Barger, G. Bhattacharya, T. Han, and B. A. Kniehl, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.43.779) 43, 779 (1991).
- [5] V. Barger, Kingman Cheung, T. Han, and D. Zeppenfeld, Phys. Rev. D 44[, 2701 \(1991\)](http://dx.doi.org/10.1103/PhysRevD.44.2701).
- [6] Vernon D. Barger, Kingman Cheung, Tao Han, and D. Zeppenfeld, Phys. Rev. D 48[, 5433 \(1993\)](http://dx.doi.org/10.1103/PhysRevD.48.5433).
- <span id="page-6-2"></span>[7] Tao Han, André S. Turcot, and Ren-Jie Zhang, [Phys. Rev.](http://dx.doi.org/10.1103/PhysRevD.59.093001) D 59[, 093001 \(1999\)](http://dx.doi.org/10.1103/PhysRevD.59.093001).
- <span id="page-6-3"></span>[8] T. Aaltonen et al., Phys. Rev. Lett. **104**[, 061802 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.104.061802)
- [9] T. Aaltonen *et al.*, Phys. Rev. Lett. **104**[, 061803 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.104.061803)
- [10] Victor Mukhamedovich Abazov et al., [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.106.171802) 106[, 171802 \(2011\)](http://dx.doi.org/10.1103/PhysRevLett.106.171802).
- [11] Georges Aad et al., Limits on the Production of the Standard Model Higgs Boson in pp Collisions at sqrt $(s)$  = 7 TeV With the ATLAS Detector (2011).
- <span id="page-6-5"></span><span id="page-6-4"></span>[12] Serguei Chatrchyan et al., [Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2011.03.056) 699, 25 (2011).
- [13] S. Dittmaier et al., Handbook of LHC Higgs Cross Sections: 1. Inclusive Observables (2011).
- <span id="page-6-6"></span>[14] Qiang Li, Michael Spira, Jun Gao, and Chong Sheng Li, Phys. Rev. D 83[, 094018 \(2011\).](http://dx.doi.org/10.1103/PhysRevD.83.094018)
- <span id="page-6-8"></span><span id="page-6-7"></span>[15] Robert Harlander, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjcd/s2003-03-426-4) 33, s454 (2003).
- [16] Tao Han and Ren-Jie Zhang, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.82.25) 82, 25 [\(1999\)](http://dx.doi.org/10.1103/PhysRevLett.82.25).

## VERNON BARGER AND PEISI HUANG PHYSICAL REVIEW D 84, 093001 (2011)

- [17] Edmond L. Berger, Qing-Hong Cao, C. B. Jackson, Tao Liu, and Gabe Shaughnessy, Phys. Rev. D 82[, 053003 \(2010\)](http://dx.doi.org/10.1103/PhysRevD.82.053003).
- [18] Charalampos Anastasiou, Guenther Dissertori, Massimiliano Grazzini, Fabian Stockli, and Bryan R. Webber, [J. High Energy Phys. 08 \(2009\) 099.](http://dx.doi.org/10.1088/1126-6708/2009/08/099)
- [19] Alan J. Barr, Ben Gripaios, and Christopher Gorham Lester, [J. High Energy Phys. 07 \(2009\) 072.](http://dx.doi.org/10.1088/1126-6708/2009/07/072)
- <span id="page-7-0"></span>[20] Bogdan A. Dobrescu and Joseph D. Lykken, [J. High](http://dx.doi.org/10.1007/JHEP04(2010)083) [Energy Phys. 04 \(2010\) 083.](http://dx.doi.org/10.1007/JHEP04(2010)083)
- <span id="page-7-1"></span>[21] M.J. Duncan, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(86)90499-5) 179, 393 (1986).
- [22] C. Zecher, T. Matsuura, and J. J. van der Bij, [Z. Phys. C](http://dx.doi.org/10.1007/BF01557393) 64[, 219 \(1994\)](http://dx.doi.org/10.1007/BF01557393).
- [23] C. P. Buszello, I. Fleck, P. Marquard, and J. J. van der Bij, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s2003-01392-0) 32, 209 (2004).
- <span id="page-7-6"></span>[24] Kiwoon Choi, Suyong Choi, Jae Sik Lee, and Chan Beom Park, Phys. Rev. D 80[, 073010 \(2009\)](http://dx.doi.org/10.1103/PhysRevD.80.073010).
- <span id="page-7-2"></span>[25] Yanyan Gao, Andrei V. Gritsan, Zijin Guo, Kirill Melnikov, Markus Schulze, and Nhan V. Tran, [Phys.](http://dx.doi.org/10.1103/PhysRevD.81.075022) Rev. D 81[, 075022 \(2010\)](http://dx.doi.org/10.1103/PhysRevD.81.075022).
- <span id="page-7-3"></span>[26] J. Ohnemus, Phys. Rev. D **50**[, 1931 \(1994\)](http://dx.doi.org/10.1103/PhysRevD.50.1931).
- <span id="page-7-4"></span>[27] ATLAS Collaboration, Report No. ATLAS-CONF-2011- 005, Geneva, 2011.
- <span id="page-7-5"></span>[28] Charles A. Nelson, *Phys. Rev. D* **37**[, 1220 \(1988\).](http://dx.doi.org/10.1103/PhysRevD.37.1220)
- <span id="page-7-7"></span>[29] Kiwoon Choi, Jae Sik Lee, and Chan Beom Park, [Phys.](http://dx.doi.org/10.1103/PhysRevD.82.113017) Rev. D 82[, 113017 \(2010\)](http://dx.doi.org/10.1103/PhysRevD.82.113017).

- <span id="page-7-8"></span>[30] V. Barger and R.J. Phillips, *Collider Physics* (Addison-Wesley, Reading, MA, 1987).
- <span id="page-7-9"></span>[31] T. Gleisberg et al., [J. High Energy Phys. 02 \(2009\) 007.](http://dx.doi.org/10.1088/1126-6708/2009/02/007)
- <span id="page-7-10"></span>[32] Matteo Cacciari, Gavin P. Salam, and Gregory Soyez, [J.](http://dx.doi.org/10.1088/1126-6708/2008/04/063) [High Energy Phys. 04 \(2008\) 063.](http://dx.doi.org/10.1088/1126-6708/2008/04/063)
- <span id="page-7-11"></span>[33] Matteo Cacciari and Gavin P. Salam, [Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2006.08.037) 641, 57 [\(2006\)](http://dx.doi.org/10.1016/j.physletb.2006.08.037).
- <span id="page-7-12"></span>[34] A. Djouadi, J. Kalinowski, and M. Spira, [Comput. Phys.](http://dx.doi.org/10.1016/S0010-4655(97)00123-9) Commun. 108[, 56 \(1998\).](http://dx.doi.org/10.1016/S0010-4655(97)00123-9)
- <span id="page-7-13"></span>[35] Julien Baglio and Abdelhak Djouadi, [J. High Energy Phys.](http://dx.doi.org/10.1007/JHEP03(2011)055) [03 \(2011\) 055.](http://dx.doi.org/10.1007/JHEP03(2011)055)
- <span id="page-7-14"></span>[36] H Yang, Report No. ATL-COM-PHYS-2010-1012, 2011.
- <span id="page-7-15"></span>[37] A. Banfi, S. Redford, M. Vesterinen, P. Waller, and T. R. Wyatt, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s10052-011-1600-y) 71, 1600 (2011).
- <span id="page-7-16"></span>[38] Walter D. Goldberger and Mark B. Wise, [Phys. Lett. B](http://dx.doi.org/10.1016/S0370-2693(00)00099-X) 475[, 275 \(2000\).](http://dx.doi.org/10.1016/S0370-2693(00)00099-X)
- [39] Kingman Cheung, Phys. Rev. D 63[, 056007 \(2001\)](http://dx.doi.org/10.1103/PhysRevD.63.056007).
- [40] Thomas G. Rizzo, [J. High Energy Phys. 06 \(2002\) 056.](http://dx.doi.org/10.1088/1126-6708/2002/06/056)
- [41] Graham D. Kribs, [arXiv:hep-ph/0605325.](http://arXiv.org/abs/hep-ph/0605325)
- [42] Hooman Davoudiasl, Thomas McElmurry, and Amarjit Soni, Phys. Rev. D 82[, 115028 \(2010\).](http://dx.doi.org/10.1103/PhysRevD.82.115028)
- <span id="page-7-17"></span>[43] Yochay Eshel, Seung J. Lee, Gilad Perez, and Yotam Soreq, [arXiv:1106.6218.](http://arXiv.org/abs/1106.6218)
- <span id="page-7-18"></span>[44] Walter D. Goldberger, Benjamín Grinstein, and Witold Skiba, Phys. Rev. Lett. 100[, 111802 \(2008\)](http://dx.doi.org/10.1103/PhysRevLett.100.111802).