

Discovery potential of selectron or smuon as the lightest supersymmetric particle at the LHC

H. K. Dreiner*

Bethe Center for Theoretical Physics and Physikalisches Institut, Universität Bonn, Bonn, Germany

S. Grab†

SCIPP, University of California Santa Cruz, Santa Cruz, California 95064, USA

T. Stefaniak‡

*Bethe Center for Theoretical Physics and Physikalisches Institut, Universität Bonn, Bonn, Germany,
and II. Physikalisches Institut, Universität Göttingen, Göttingen, Germany*

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We investigate the LHC discovery potential of R -parity violating supersymmetric models with a right-handed selectron or smuon as the lightest supersymmetric particle. These particles arise naturally in R -parity violating minimal supergravity models. We classify the hadron collider signatures and perform for the first time within these models a detailed signal over background analysis. We develop an inclusive three-lepton search and give prospects for a discovery at a center-of-mass energy of $\sqrt{s} = 7$ TeV as well as $\sqrt{s} = 14$ TeV. There are extensive parameter regions which the LHC can already test with $\sqrt{s} = 7$ TeV and an integrated luminosity of 1 fb^{-1} . We also propose a method for the mass reconstruction of the supersymmetric particles within our models at $\sqrt{s} = 14$ TeV.

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I. INTRODUCTION

Since 2010, the Large Hadron Collider (LHC) has been collecting data at a center of mass energy of $\sqrt{s} = 7$ TeV, and first searches for physics beyond the standard model (SM) have been published [1–12]. Even with an integrated luminosity of only 35 pb^{-1} , the LHC has already tested supersymmetric models [13,14] beyond the Tevatron searches [11,12]. Furthermore, it is expected that the LHC will collect 1 fb^{-1} of data by the end of 2011.

One of the most promising LHC signatures for supersymmetry (SUSY) are multilepton final states [15–17]. On the one hand, electrons and muons are easy to identify in the detectors. On the other hand, the SM background for multilepton final states is low. In this publication, we focus on such signatures.

We consider the supersymmetric extension of the SM with minimal particle content (SSM) [13,14]. Without further assumptions, the proton usually has a short lifetime in this model [18–20], in contradiction with experimental observations [21]. The proton decays because renormalizable lepton- and baryon-number violating interactions are jointly present. One must therefore impose an additional discrete symmetry. The most common choice for this discrete symmetry is R -parity, or equivalently at low-energy, proton-hexality (P_6). Either suppresses all lepton- and baryon-number violating interactions [22–24]. The SSM

with R -parity is usually denoted as the minimal supersymmetric SM (MSSM).

We consider here a different discrete symmetry, baryon-triality (B_3) [22–25], which suppresses only the baryon-number violating terms but allows for lepton-number violating interactions. The B_3 SSM has the advantage that neutrino masses are generated naturally [26–29] without the need to introduce a new (seesaw) energy scale [30–32]. The lepton-number violating interactions can be adjusted such that the observed neutrino masses and mixing angles can be explained [33,34]. Note that both P_6 and B_3 are discrete gauge anomaly-free symmetries [22–24,35]. There is no such symmetry that allows only the baryon-number violating interactions.

In the B_3 SSM, the lightest supersymmetric particle (LSP) will decay via the lepton-number violating interactions and is thus not bounded by cosmological observations to be the lightest neutralino, $\tilde{\chi}_1^0$ [36]. Unlike in the MSSM, the $\tilde{\chi}_1^0$ is not a valid dark matter (DM) candidate. However, several possible DM candidates are easily found in simple extensions of the B_3 SSM, for example, the axino [37–40], the gravitino [41,42] or the lightest U -parity particle [43,44].

We consider in this paper the B_3 SSM with a right-handed scalar electron (selectron, \tilde{e}_R) or scalar muon (smuon, $\tilde{\mu}_R$) as the LSP. These LSP candidates naturally arise in the B_3 minimal supergravity (mSUGRA) model [45], on which we focus in the following. Here, large lepton-number violating interactions at the grand unification theory (GUT) scale drive the selectron or smuon mass toward small values at the electroweak scale via the renormalization group equations (RGEs) [46]. We describe this

*dreiner@th.physik.uni-bonn.de

†sgrab@scipp.ucsc.edu

‡tim@th.physik.uni-bonn.de

effect and the selectron and smuon LSP parameter space in the next section in more detail. Further LSP candidates within B_3 mSUGRA (besides the $\tilde{\chi}_1^0$) are the lightest stau, $\tilde{\tau}_1$ [16,45,47], and the sneutrino, $\tilde{\nu}_{e,\mu,\tau}$ [45,48], depending on the dominant lepton-number violating operator [46].

If SUSY exists, the pair production of strongly interacting SUSY particles (sparticles), like scalar quarks (squarks), is usually the main source for SUSY events at hadron colliders like the LHC [49]. Furthermore, squarks, \tilde{q} , are much heavier than the $\tilde{\chi}_1^0$ in most supersymmetric models [50]. Assuming that we have a right-handed selectron or smuon, $\tilde{\ell}_R$, as the LSP, a natural cascade process at the LHC is

$$\tilde{q} \tilde{q} \rightarrow qq \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow qq \ell \ell \tilde{\ell}_R \tilde{\ell}_R, \quad (1)$$

where the squarks decay into a quark, q , and the $\tilde{\chi}_1^0$. The $\tilde{\chi}_1^0$ decays into the $\tilde{\ell}_R$ LSP and an oppositely charged lepton, ℓ , of the same flavor.

The $\tilde{\ell}_R$ LSP can then decay via the lepton-number violating interactions, for example,

$$\tilde{\ell}_R \rightarrow \ell' \nu, \quad (2)$$

i.e. into another charged lepton ℓ' and a neutrino ν . As we argue in the following, this is the case for large regions of the B_3 SSM parameter space. We thus obtain from Eqs. (1) and (2) an event with four charged leptons in the final state. Taking into account that some leptons might not be well identified, we design in this paper an inclusive three-lepton search for $\tilde{\ell}_R$ -LSP scenarios. Although we concentrate on the B_3 mSUGRA model, our results apply also to more general models as long as Eqs. (1) and (2) hold. We will show that, because of the high lepton multiplicity in B_3 models, the discovery reach at the LHC with $\sqrt{s} = 7$ TeV exceeds searches in the R -parity conserving case [51]. We also give prospects for a discovery at $\sqrt{s} = 14$ TeV and propose a method for the reconstruction of sparticle masses within our model.

The phenomenology of slepton LSPs has been investigated mainly for the case of a stau LSP. See, for example, Refs. [16,33,45,47,52–62]. Recently, Ref. [16] proposed a trilepton search for stau LSP scenarios, which is similar to our analysis, although the stau in Ref. [16] decays via four-body decays. LEP II has searched for slepton LSPs [63,64]. No signals were found, and lower mass limits around 90–100 GeV were set. Refs. [53,54] investigated the decay length of slepton LSPs assuming trilinear as well as bilinear R -parity violating interactions. Finally, in Ref. [65], the signature of Eqs. (1) and (2) was pointed out. But in contrast to this work, no signal over background analysis was performed.

The remainder of this paper is organized as follows. In Sec. II we review the B_3 mSUGRA model and show how a $\tilde{\ell}_R$ LSP can arise. We present the B_3 mSUGRA parameter

regions with a $\tilde{\ell}_R$ LSP and propose a set of benchmark points for LHC searches. We then classify in Sec. III the $\tilde{\ell}_R$ LSP signatures at hadron colliders as a function of the dominant R -parity violating interaction. Based on this, we develop in Sec. IV a set of cuts for an inclusive three-lepton search at the LHC and give prospects for a discovery at $\sqrt{s} = 7$ TeV as well as at $\sqrt{s} = 14$ TeV. In Sec. V we propose a method for the reconstruction of the supersymmetric particle masses. We conclude in Sec. VI.

Appendix A reviews the mass spectrum and branching ratios of our benchmark models, and Appendix B shows the cutflow for our $\sqrt{s} = 14$ TeV analysis. We give in Appendix C the relevant equations for the kinematic endpoints for the mass reconstruction of Sec. V, and we calculate in Appendix D some missing three-body decays of sleptons.

II. THE SELECTRON AND SMUON AS THE LSP IN THE R -PARITY VIOLATING MSUGRA MODEL

A. The B_3 mSUGRA Model

In the B_3 mSUGRA model the boundary conditions at the GUT scale (M_{GUT}) are described by the six parameters [45,47]

$$M_0, M_{1/2}, A_0, \tan\beta, \text{sgn}(\mu), \Lambda. \quad (3)$$

Here, M_0 , $M_{1/2}$ and A_0 are the universal scalar mass, the universal gaugino mass and the universal trilinear scalar coupling, respectively. $\tan\beta$ denotes the ratio of the two Higgs vacuum expectation values, and $\text{sgn}(\mu)$ fixes the sign of the bilinear Higgs mixing parameter μ . Its magnitude is derived from radiative electroweak symmetry breaking [66]. Λ is described below.

In B_3 mSUGRA, the superpotential is extended by the lepton-number violating (LNV) terms [67],

$$W_{\text{LNV}} = \frac{1}{2} \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \kappa_i L_i H_2, \quad (4)$$

which are absent in the MSSM. Here, L_i and Q_i denote the lepton and quark $SU(2)$ doublet superfields, respectively. H_2 is the Higgs $SU(2)$ doublet superfield which couples to up-type quarks, and \bar{E}_i and \bar{D}_i denote the lepton and down-type quark $SU(2)$ singlet superfields, respectively. $i, j, k \in \{1, 2, 3\}$ are generation indices. λ_{ijk} is antisymmetric in the first two indices ($i \leftrightarrow j$) and thus denotes nine, λ'_{ijk} 27 dimensionless couplings. The bilinear lepton-number violating couplings κ_i are three dimensional parameters, which vanish in B_3 mSUGRA at M_{GUT} due to a redefinition of the lepton and Higgs superfields [45]. However, they are generated at lower scales via RGE running with interesting phenomenological consequences for neutrino masses [29,34].

In the B_3 mSUGRA model, we assume that exactly one of the 36 dimensionless couplings in Eq. (4) is nonzero and positive at the GUT scale.¹ The parameter Λ in Eq. (3) refers to this choice, i.e.

$$\Lambda \in \{\lambda_{ijk}, \lambda'_{ijk}\}, \quad i, j, k = 1, 2, 3. \quad (5)$$

Given one coupling at the GUT scale, other couplings that violate only the same lepton number are generated at the weak scale, M_Z , by the RGEs [45,52,69,70].

B. The selectron and smuon LSP

1. Renormalization group evolution of the $\tilde{\ell}_R$ mass

In order to understand the dependence of the right-handed slepton,² $\tilde{\ell}_R$, mass at M_Z on the boundary conditions at M_{GUT} , we have to take a closer look at the relevant RGEs, which receive additional contributions from the LNV terms in Eq. (4). The dominant one-loop contributions to the running mass of the right-handed slepton of generation $k = 1, 2$ are [45]

$$16\pi^2 \frac{d(M_{\tilde{\ell}_R^k}^2)}{dt} = -\frac{24}{5} g_1^2 |M_1|^2 + \frac{6}{5} g_1^2 \mathcal{S} + 2(\mathbf{h}_{\mathbf{E}^k})_{ij}^2 + 4\lambda_{ijk}^2 [(\mathbf{m}_{\mathbf{L}}^2)_{ii} + (\mathbf{m}_{\mathbf{L}}^2)_{jj} + (\mathbf{m}_{\mathbf{E}}^2)_{kk}] \quad (6)$$

with

$$(\mathbf{h}_{\mathbf{E}^k})_{ij} \equiv \lambda_{ijk} \times A_0 \quad \text{at } M_{\text{GUT}}, \quad (7)$$

and

$$\mathcal{S} = \text{Tr}[\mathbf{m}_{\mathbf{Q}}^2 - \mathbf{m}_{\mathbf{L}}^2 - 2\mathbf{m}_{\mathbf{U}}^2 + \mathbf{m}_{\mathbf{D}}^2 + \mathbf{m}_{\mathbf{E}}^2] + m_{H_2}^2 - m_{H_1}^2. \quad (8)$$

Here, $g_1(M_1)$ is the $U(1)$ gauge coupling (gaugino mass) and $t = \ln Q$ with Q the renormalization scale. $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ is the trilinear scalar soft-breaking coupling corresponding to λ_{ijk} . The bold-faced soft mass parameters in Eqs. (6) and (8) are 3×3 matrices in flavor space: $\mathbf{m}_{\mathbf{Q}}$ and $\mathbf{m}_{\mathbf{L}}$ for the left-handed doublet squarks and sleptons, $\mathbf{m}_{\mathbf{U}}$, $\mathbf{m}_{\mathbf{D}}$ and $\mathbf{m}_{\mathbf{E}}$ for the singlet up-squarks, down-squarks and sleptons, respectively. m_{H_1} and m_{H_2} are the scalar Higgs soft-breaking masses.

The first two terms on the right-hand side in Eq. (6) are proportional to the gauge coupling squared, g_1^2 , and also present in R -parity conserving models. The sum of these two terms is *negative* at any scale and thus leads to an *increase* of $M_{\tilde{\ell}_R^k}$ when running from M_{GUT} down to

¹On the one hand, bounds on products of two different couplings are in general much stronger than on single couplings [68]. On the other hand, one observes also a large hierarchy between the Yukawa couplings within the SM.

²We consider only the first two generations of sleptons, i.e. $\tilde{\ell}_R \in \{\tilde{e}_R, \tilde{\mu}_R\}$, because a stau LSP can also be obtained without (large) R -parity violating interactions [45,47].

TABLE I. List of $L_i L_j \bar{E}_k$ couplings (first column) needed to generate a \tilde{e}_R or $\tilde{\mu}_R$ LSP (second column). The third column gives the most recent experimental bounds [95% confidence level (C.L.)], taken from Ref. [71]. The bounds apply at M_{GUT} . The bounds on λ_{212} and λ_{232} from the generation of too-large neutrino masses are in general too strong to allow for a $\tilde{\mu}_R$ LSP [45], although exceptions might exist [29].

$L_i L_j \bar{E}_k$	LSP candidate	2σ bound
$\lambda_{121}, \lambda_{131}$	\tilde{e}_R	$0.020 \times (M_{\tilde{e}_R}/100 \text{ GeV})$
λ_{231}	\tilde{e}_R	$0.033 \times (M_{\tilde{e}_R}/100 \text{ GeV})$
λ_{132}	$\tilde{\mu}_R$	$0.020 \times (M_{\tilde{\mu}_R}/100 \text{ GeV})$

M_Z . Here, the main contribution comes from the term proportional to the gaugino mass squared, M_1^2 , because \mathcal{S} is identical to zero at M_{GUT} for universal scalar masses. Moreover, the coefficient of the M_1^2 term is larger than that of the \mathcal{S} term.

The remaining contributions are proportional to λ_{ijk}^2 and $(\mathbf{h}_{\mathbf{E}^k})_{ij}^2$; the latter also implies a proportionality to λ_{ijk}^2 at M_{GUT} ; cf. Eq. (7). These terms are *positive* and will therefore *reduce* $M_{\tilde{\ell}_R^k}$, when going from M_{GUT} down to M_Z . They are new to the B_3 mSUGRA model compared to R -parity conserving mSUGRA. We can see from Eq. (6) that, if the LNV coupling is roughly of the order of the gauge coupling g_1 , i.e. $\lambda_{ijk} \gtrsim \mathcal{O}(10^{-2})$, these terms contribute substantially. Then the $\tilde{\ell}_R$ can be lighter than the lightest neutralino, $\tilde{\chi}_1^0$, and lightest stau, $\tilde{\tau}_1$, at M_Z , leading to a $\tilde{\ell}_R$ LSP [46].

The respective $L_i L_j \bar{E}_k$ couplings Λ , which can lead to a \tilde{e}_R or $\tilde{\mu}_R$ LSP, are given in Table I with their most recent experimental 2σ upper bounds at M_{GUT} [71]. Because of its RGE running, Λ at M_Z is roughly 1.5 times larger than at M_{GUT} [70,72].

As an example, in Fig. 1, we demonstrate the impact of a nonvanishing coupling λ_{231} at M_{GUT} on the running of the \tilde{e}_R mass. Note that we can obtain a \tilde{e}_R LSP ($\tilde{\mu}_R$ LSP) with a nonzero coupling λ_{121} or λ_{131} (λ_{132}) at M_{GUT} in a completely analogous way. We employ SOFTSUSY3.0.13 [73,74] for the evolution of the RGEs. We have chosen a fairly large absolute value of $A_0 = -1000 \text{ GeV}$ (see the discussion in Sec. II B 2). The other mSUGRA parameters are $M_0 = 150 \text{ GeV}$, $M_{1/2} = 500 \text{ GeV}$, $\tan\beta = 5$ and $\mu > 0$. In the corresponding R -parity conserving case ($\lambda_{231}|_{\text{GUT}} = 0$), the $\tilde{\chi}_1^0$ is the LSP and the $\tilde{\tau}_1$ is the next-to LSP (NLSP).

The \tilde{e}_R mass decreases for increasing λ_{231} , as described by Eq. (6). Furthermore, the masses of the (mainly) left-handed second- and third-generation sleptons, $\tilde{\mu}_L$, $\tilde{\tau}_2$, and sneutrinos, $\tilde{\nu}_\mu$, $\tilde{\nu}_\tau$, decrease,³ since these fields couple directly via λ_{231} . In contrast, the mass of the $\tilde{\chi}_1^0$ is not

³However, these (negative) R -parity violating contributions are always smaller than those to the right-handed slepton mass [45]. Thus, the left-handed sleptons and sneutrinos cannot become the LSP within B_3 mSUGRA with $\lambda_{ijk}|_{\text{GUT}} \neq 0$ [46].

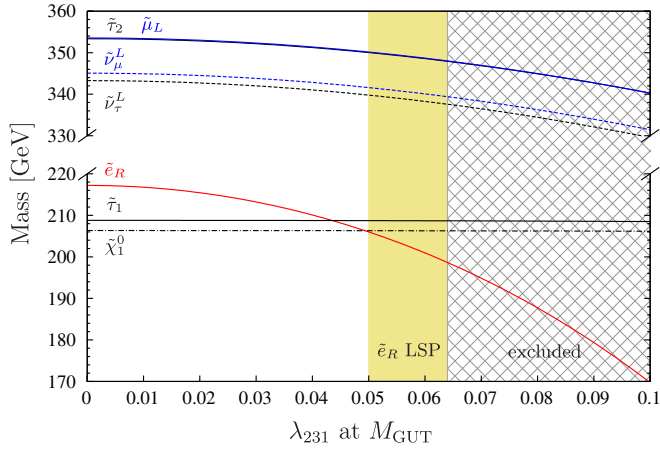


FIG. 1 (color online). Masses of the \tilde{e}_R , $\tilde{\chi}_1^0$, $\tilde{\tau}_1$, $\tilde{\tau}_2$, $\tilde{\nu}_\tau$, $\tilde{\mu}_L$ and $\tilde{\nu}_\mu$ at M_Z as a function of λ_{231} at M_{GUT} . The other mSUGRA parameters are $M_0 = 150$ GeV, $M_{1/2} = 500$ GeV, $A_0 = -1000$ GeV, $\tan\beta = 5$ and $\mu > 0$. The shaded [yellow] region corresponds to the experimentally allowed \tilde{e}_R LSP region. The [gray] patterned region is excluded by the upper bound on λ_{231} ; cf. Table I.

changed, since it does not couple to the λ_{231} operator at the one-loop level. Also the impact on the mass of the $\tilde{\tau}_1$, which is mostly right-handed, is small. We therefore obtain in Fig. 1, at $\lambda_{231}|_{\text{GUT}} \cong 0.05$, a right-handed selectron as the LSP.

Because of the experimental upper bound on λ_{231} (see Table I), the gray patterned region in Fig. 1 with $\lambda_{231}|_{\text{GUT}} > 0.064$ is excluded at 95% C.L. Note that the valid parameter region with a \tilde{e}_R LSP becomes larger once we consider scenarios with heavier sparticles. Moreover, once we go beyond the mSUGRA model and consider nonuniversal masses, a \tilde{e}_R LSP can also be obtained with

much smaller LNV couplings. The collider study that we present in this publication also applies to these more general $\tilde{\ell}_R$ LSP models, provided that we still have a non-vanishing and dominant $L_i L_j \bar{E}_k$ operator.

In the following, we investigate which other conditions at M_{GUT} are vital to obtain a $\tilde{\ell}_R$ LSP within B_3 mSUGRA. The dependence on the trilinear coupling strength A_0 plays an especially crucial role.

2. A_0 dependence

According to Eqs. (6) and (7), A_0 enters the running of $M_{\tilde{\ell}_R^k}$ via the LNV soft-breaking trilinear scalar coupling $(\mathbf{h}_{\mathbf{E}^k})_{ij}$. As $t = \ln Q$ is decreased, the $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ term gives a negative contribution to $M_{\tilde{\ell}_R^k}$. Its full contribution is proportional to the integral of $(\mathbf{h}_{\mathbf{E}^k})_{ij}^2$ over t , from $t_{\min} = \ln(M_Z)$ to $t_{\max} = \ln(M_{\text{GUT}})$. We now show that a negative A_0 with a large magnitude enhances the (negative) λ_{ijk} contribution to the $M_{\tilde{\ell}_R^k}$ mass. This discussion is similar to the case of a sneutrino LSP [48].

In Fig. 2 we show the running of the trilinear coupling $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ [Fig. 2(a)] and the resulting running for $(\mathbf{h}_{\mathbf{E}^k})_{ij}^2$ [Fig. 2(b)]. We assume a nonvanishing coupling $\lambda_{ijk}|_{\text{GUT}} = 0.1$ and a universal gaugino mass $M_{1/2} = 1000$ GeV. Different lines correspond to different values of A_0 , as indicated in Fig. 2(b).

The dominant contributions to the RGE of $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ are given by [45]

$$16\pi^2 \frac{d(\mathbf{h}_{\mathbf{E}^k})_{ij}}{dt} = -(\mathbf{h}_{\mathbf{E}^k})_{ij} \left[\frac{9}{5} g_1^2 + 3g_2^2 \right] + \lambda_{ijk} \left[\frac{18}{5} g_1^2 M_1 + 6g_2^2 M_2 \right]. \quad (9)$$

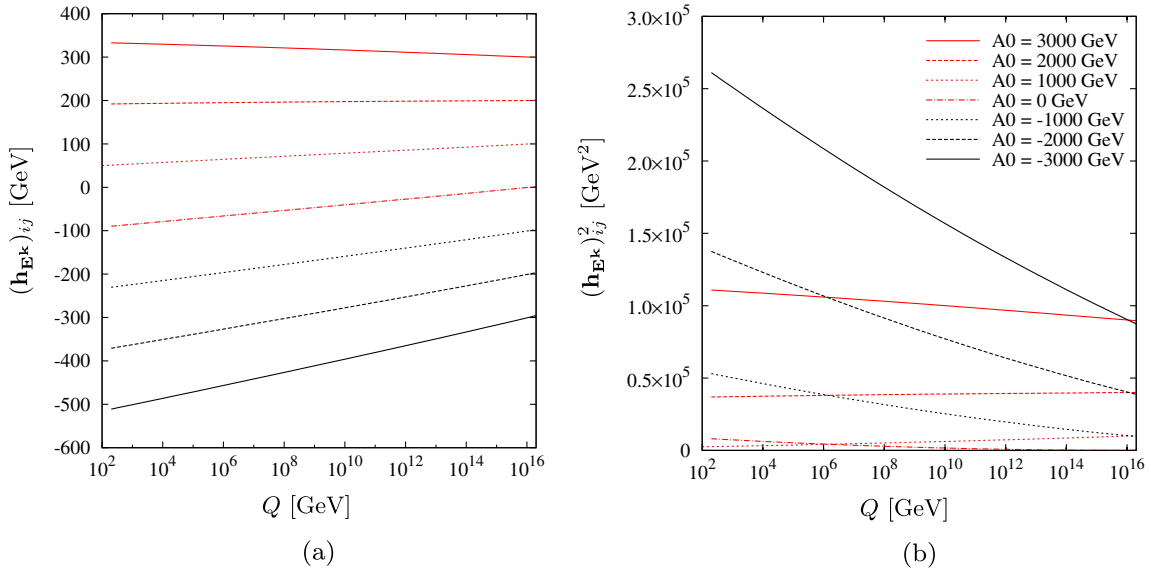


FIG. 2 (color online). Running of $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ (left) and $(\mathbf{h}_{\mathbf{E}^k})_{ij}^2$ (right) from M_{GUT} to M_Z for the different values of A_0 given in (b). At M_{GUT} , we choose $M_{1/2} = 1000$ GeV and $\lambda_{ijk} = 0.1$.

M_1 and M_2 are the $U(1)$ and $SU(2)$ gaugino masses, respectively. The running in Eq. (9) is governed by two terms with opposite sign; one proportional to $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ and one proportional to λ_{ijk} . In contrast to the sneutrino LSP case (cf. Ref. [48]), the running is independent of the strong coupling g_3 and the gluino mass M_3 .

According to Eq. (7), the sign of the term proportional to $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ in Eq. (9) depends on the sign of A_0 . At M_{GUT} , this term is positive (negative) for negative (positive) A_0 . Hence, for positive A_0 , the term proportional to $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ increases $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ when we run from M_{GUT} to M_Z . Note that the gauge couplings g_1 and g_2 decrease from M_{GUT} to M_Z .

Assuming λ_{ijk} to be positive, the second term is always positive and thus decreases $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ when running from M_{GUT} to M_Z . The λ_{ijk} coupling increases by roughly a factor of 1.5 when we run from M_{GUT} to M_Z . However, at the same time, the gaugino masses M_1 and M_2 as well as the gauge couplings g_1 and g_2 decrease. Therefore, this term gets relatively less important toward lower scales.

Now we can understand the running of $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ in Fig. 2(a). Given a positive A_0 (top four [red] lines), both terms in Eq. (9) have opposite signs and thus partly compensate each other, resulting in only a small change of $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ during the running. Moreover, due to the running of the gauge couplings and gaugino masses, both terms in Eq. (9) decrease when we run from M_{GUT} to M_Z . In contrast, if we start with a negative A_0 (lower three black lines), both terms give negative contributions to the running of $(\mathbf{h}_{\mathbf{E}^k})_{ij}$. Still, the magnitude of the λ_{ijk} term in Eq. (9) decreases. However, the contribution from the term proportional to $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ does not necessarily decrease when running from M_{GUT} to M_Z . Thus, for negative A_0 , $(\mathbf{h}_{\mathbf{E}^k})_{ij}$ decreases with a large slope.

Recall from Eq. (6) that $M_{\tilde{\ell}_R^k}^2$ is reduced proportional to the integral of $(\mathbf{h}_{\mathbf{E}^k})_{ij}^2$ over t . Thus, according to Fig. 2(b), a negative value of A_0 leads to a smaller $M_{\tilde{\ell}_R^k}$ compared to a positive A_0 with the same magnitude.

3. Selectron and smuon LSP parameter space

In this section, we present two-dimensional B_3 mSUGRA parameter regions which exhibit a $\tilde{\ell}_R$ LSP. As we have seen in Sec. II B 1, the running of the $\tilde{\ell}_R$ mass is analogous for the first and second generation. Therefore, we study here only the case of a \tilde{e}_R LSP with a nonvanishing coupling λ_{231} at M_{GUT} . We can obtain the $\tilde{\mu}_R$ LSP region by replacing coupling λ_{231} with λ_{132} .

We give in Fig. 3 the \tilde{e}_R LSP region in the A_0 - $M_{1/2}$ plane [Fig. 3(a)] and M_0 - $\tan\beta$ plane [Fig. 3(b)] for a coupling $\lambda_{231}|_{\text{GUT}} = 0.045$. We show the mass difference, ΔM , between the NLSP and LSP. For the shown region, a lower bound of 135 GeV on the selectron mass is employed to fulfill the bound on λ_{231} ; cf. Table I. The gray patterned regions are excluded by the LEP bound on the light Higgs

mass [75,76]. However, we have reduced this bound by 3 GeV to account for numerical uncertainties of SOFTSUSY [77–79] which was used to calculate the SUSY and Higgs mass spectrum.

The entire displayed region fulfills the 2σ constraints on the branching ratio of the decay $b \rightarrow s\gamma$ [80],

$$3.03 \times 10^{-4} < \mathcal{B}(b \rightarrow s\gamma) < 4.07 \times 10^{-4}, \quad (10)$$

and the upper limit on the flavor-changing neutral current decay $B_s^0 \rightarrow \mu^+ \mu^-$ [81], i.e.

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) < 3.6 \times 10^{-8}, \quad (11)$$

at 90% C.L.

However, the parameter points in Fig. 3 cannot explain the discrepancy between experiment (using pion spectral functions from e^+e^- data) and the SM prediction of the anomalous magnetic moment of the muon, a_μ ; see Ref. [82] and references therein. There exists a \tilde{e}_R LSP region consistent with the measured value of a_μ at 2σ . But this region is already excluded by Tevatron trilepton SUSY searches [83]. We note, however, that the SM prediction is consistent with the experimental observations at the 2σ level, if one uses spectral functions from τ data [82]. We have employed MICROMEGAS2.2 [84] to calculate the SUSY contribution to a_μ , $\mathcal{B}(b \rightarrow s\gamma)$ and $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$.

We observe in Fig. 3 that the \tilde{e}_R LSP lives in an extended region of the B_3 mSUGRA parameter space. Competing LSP candidates are the lightest stau, $\tilde{\tau}_1$, and the lightest neutralino, $\tilde{\chi}_1^0$.

In the A_0 - $M_{1/2}$ plane, Fig. 3(a), we find a \tilde{e}_R LSP for larger values of $M_{1/2}$, because $M_{1/2}$ increases the mass of the (binolike) $\tilde{\chi}_1^0$ faster than the mass of the right-handed sleptons [85,86]. We can also see that a \tilde{e}_R LSP is favored by a negative A_0 with a large magnitude as discussed in Sec. II B 2. In this region of parameter space, the mass difference between the \tilde{e}_R LSP and the $\tilde{\tau}_1$ NLSP increases with increasing $|A_0|$. In principle, there can also be a \tilde{e}_R LSP for a large positive A_0 ; cf. Fig. 2(b). However this configuration is disfavored due to a too-small light Higgs mass [85]. Note that a negative A_0 with a large magnitude naturally leads to a light top squark, \tilde{t}_1 , since the top Yukawa coupling enters the RGE running of the \tilde{t}_1 mass in a similar way as the λ_{ijk} Yukawa coupling does for the $\tilde{\ell}_R$ mass [85,86]. This behavior plays an important role for the mass reconstruction of the \tilde{t}_1 ; cf. Sec. V.

In the M_0 - $\tan\beta$ plane, Fig. 3(b), we find a \tilde{e}_R LSP for $\tan\beta \lesssim 5$ and $M_0 \lesssim 100$ GeV. The mass of the $\tilde{\tau}_1$ decreases with increasing $\tan\beta$ while the mass of the \tilde{e}_R is unaffected by $\tan\beta$. Increasing $\tan\beta$ increases the tau Yukawa coupling and thus its (negative) contribution to the stau mass from RGE running [85,86]. Furthermore, a larger value of $\tan\beta$ usually leads to a larger mixing between the left- and right-handed stau. Thus, $\tan\beta$ is a handle for the mass difference of the $\tilde{\tau}_1$ and \tilde{e}_R . In contrast, M_0 increases the masses of all the scalar particles like the

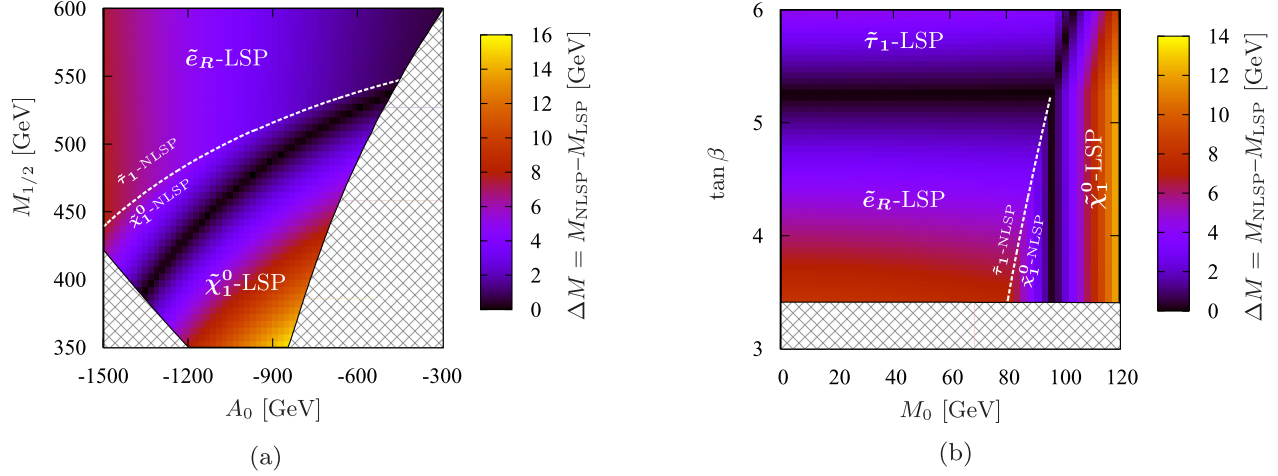


FIG. 3 (color online). Mass difference, ΔM , between the NLSP and LSP. The LSP candidates are explicitly mentioned. The [gray] patterned regions correspond to models excluded by the LEP Higgs bound. The white dashed line separates \tilde{e}_R -LSP scenarios with different mass hierarchies: $M_{\tilde{e}_R} < M_{\tilde{\tau}_1} < M_{\tilde{\chi}_1^0}$ (left) and $M_{\tilde{e}_R} < M_{\tilde{\chi}_1^0} < M_{\tilde{\tau}_1}$ (right). (a) A_0 - $M_{1/2}$ plane with B_3 mSUGRA parameter $M_0 = 90$ GeV, $\tan\beta = 4$, $\text{sgn}(\mu) = +$, and $\lambda_{231}|_{\text{GUT}} = 0.045$. (b) M_0 - $\tan\beta$ plane with B_3 mSUGRA parameter $M_{1/2} = 450$ GeV, $A_0 = -1250$ GeV, $\text{sgn}(\mu) = +$, and $\lambda_{231}|_{\text{GUT}} = 0.045$.

$\tilde{\tau}_1$ and \tilde{e}_R , while the mass of the $\tilde{\chi}_1^0$ is nearly unaffected by both $\tan\beta$ and M_0 . Therefore, at larger values of M_0 , we obtain a $\tilde{\chi}_1^0$ LSP.

We find basically two possible mass hierarchies for the \tilde{e}_R LSP parameter space, indicated by the white dashed line in Figs. 3(a) and 3(b). Close to the $\tilde{\chi}_1^0$ LSP region, we observe a $\tilde{\chi}_1^0$ NLSP and a $\tilde{\tau}_1$ next-to-NLSP (NNLSP), i.e.

$$M_{\tilde{e}_R} < M_{\tilde{\chi}_1^0} < M_{\tilde{\tau}_1}. \quad (12)$$

However, for most of the parameter space, we have

$$M_{\tilde{e}_R} < M_{\tilde{\tau}_1} < M_{\tilde{\chi}_1^0}, \quad (13)$$

i.e. the $\tilde{\tau}_1$ is the NLSP and the $\tilde{\chi}_1^0$ is the NNLSP. For some regions with a large mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP, the $\tilde{\mu}_R$ can even be the NNLSP, i.e. we have

$$M_{\tilde{e}_R} < M_{\tilde{\tau}_1} < M_{\tilde{\mu}_R} < M_{\tilde{\chi}_1^0}, \quad (14)$$

where the $\tilde{\chi}_1^0$ is the next-to-NNLSP (NNNLSP). These three mass hierarchies lead to a different collider phenomenology and will be our guideline in the selection of benchmark scenarios.

C. Benchmark scenarios

In order to investigate the LHC phenomenology of a \tilde{e}_R LSP model in more detail, we select for each mass hierarchy, Eqs. (12)–(14), one representative \tilde{e}_R LSP benchmark point. The B_3 mSUGRA parameters and the masses of the lightest four sparticles of these benchmark points, denoted BE1, BE2 and BE3, are given in Table II. All benchmark points exhibit a coupling $\lambda_{231}|_{\text{GUT}} = 0.045$ (cf. Table I) and fulfill the experimental constraints of Sec. II B 3 and the constraints from Tevatron tripleton

SUSY searches [83]. The supersymmetric mass spectra and branching ratios are given in Appendix A.

The benchmark points BE1 and BE2 both feature a $\tilde{\tau}_1$ NLSP. In BE1, the $\tilde{\tau}_1$ is nearly mass degenerate with the \tilde{e}_R and decays exclusively via λ_{231} into an electron and a muon neutrino. In contrast, in BE2 the (mainly right-handed) $\tilde{\tau}_1$ is 7 GeV heavier than the \tilde{e}_R LSP and thus mainly decays via three-body decays into the \tilde{e}_R due to larger phase space. Similarly, the $\tilde{\mu}_R$ NNLSP in BE1 decays via three-body decays into the \tilde{e}_R or the $\tilde{\tau}_1$. The three-body decays of the heavier supersymmetric sleptons to the \tilde{e}_R LSP are new and are calculated in Appendix D.

TABLE II. B_3 mSUGRA parameter and the masses of the four lightest SUSY particles of the \tilde{e}_R LSP benchmark points BE1, BE2 and BE3. The complete mass spectra and the branching ratios are given in Appendix A.

B_3 mSUGRA parameter	Benchmark models		
	BE1	BE2	BE3
M_0 [GeV]	0	90	90
$M_{1/2}$ [GeV]	475	460	450
A_0 [GeV]	-1250	-1400	-1250
$\tan\beta$	5	4	4
$\text{sgn}(\mu)$	+	+	+
$\lambda_{231} _{\text{GUT}}$	0.045	0.045	0.045
Light sparticles (mass/GeV)			
LSP	\tilde{e}_R (168.7)	\tilde{e}_R (182.3)	\tilde{e}_R (182.0)
NLSP	$\tilde{\tau}_1$ (170.0)	$\tilde{\tau}_1$ (189.0)	$\tilde{\chi}_1^0$ (184.9)
NNLSP	$\tilde{\mu}_R$ (183.6)	$\tilde{\chi}_1^0$ (189.5)	$\tilde{\tau}_1$ (187.2)
NNNLSP	$\tilde{\chi}_1^0$ (195.7)	$\tilde{\mu}_R$ (199.0)	$\tilde{\mu}_R$ (195.9)

In BE1, there is a fairly large mass difference between the \tilde{e}_R LSP and the $\tilde{\chi}_1^0$ NNLSP of about 27 GeV. The mass difference between the \tilde{e}_R and $\tilde{\chi}_1^0$ is smaller in BE2 (compared to BE1), i.e. about 7 GeV. The NNLSP is the $\tilde{\mu}_R$. Finally, the benchmark point BE3 features a $\tilde{\chi}_1^0$ NLSP that is 3 GeV heavier than the \tilde{e}_R LSP. The $\tilde{\tau}_1$ is the NNLSP and decays into the $\tilde{\chi}_1^0$ and a τ . The $\tilde{\mu}_R$ is the NNLSP.

III. SELECTRON AND SMUON LSP SIGNATURES AT THE LHC

We now classify the main LHC signatures of selectron and smuon, $\tilde{\ell}_R$, LSP models, under the simplifying assumption that each decay chain of heavy SUSY particles ends in the LSP and that the LSP decay is dominated by only one R -parity violating operator Λ ; cf. Table I. If we assume squark pair production as the main sparticle production process,⁴ we obtain as one of the major cascades

$$qq/gg \rightarrow \tilde{q}\tilde{q} \rightarrow jj\tilde{\chi}_1^0\tilde{\chi}_1^0 \rightarrow jj\ell\ell\tilde{\ell}_R\tilde{\ell}_R, \quad (15)$$

where \tilde{q} is a squark and j denotes a (parton-level) jet. The two leptons ℓ are of the same flavor as the LSP. The $\tilde{\ell}_R$ LSP will promptly decay via the R -parity violating $L_i L_j \bar{E}_k$ operator into a charged lepton and a neutrino. The resulting collider signatures are classified in Table III according to the possible $\tilde{\ell}_R$ LSP decays.

Assuming the SUSY cascade in Eq. (15), the resulting collider signatures involve two (parton-level) jets from squark decays, two charged leptons from the neutralino decay with the same flavor as the LSP, as well as additional charged leptons and missing transverse energy, \cancel{E}_T , from the LSP decays. Because of the Majorana nature of the $\tilde{\chi}_1^0$, every charge combination of the two $\tilde{\ell}_R$ LSPs is possible. In what follows, it is important to note that the transverse momentum, p_T , spectrum of the leptons from the decay $\tilde{\chi}_1^0 \rightarrow \ell\tilde{\ell}_R$ will depend on the mass difference between the $\tilde{\ell}_R$ LSP and the $\tilde{\chi}_1^0$. For smaller mass differences, we get on average a smaller lepton p_T .⁵

In general, more complicated SUSY production and decay processes than Eq. (15) can occur. Figure 4 gives an example of (left-handed) squark-gluino production followed by two lengthy decay chains. Typically, these processes lead to *additional* final state particles [compared to Eq. (15) and Table III], most notably

- (i) additional jets from the production of gluinos and their subsequent decays into squarks and quarks; cf. the upper decay chain of Fig. 4,

⁴For all of our benchmark points, the gluinos are heavier than the squarks and dominantly decay to a squark and a quark. Thus for gluino pair production we simply obtain two jets more per event.

⁵Some of the low- p_T leptons might even fail the object selection cuts. We therefore found that a three-lepton search strategy leads in general to a better signal-to-background ratio than a four-lepton search; see also the discussion in Sec. IV C.

- (ii) additional leptons from the decays of heavier neutralinos and charginos, which may come from the decay of left-handed squarks, like in the lower decay chain of Fig. 4, and
- (iii) additional leptons from a $\tilde{\chi}_1^0$ decay into a non-LSP right-handed slepton $\tilde{\ell}'_R$ (or lightest stau $\tilde{\tau}_1$), e.g. $\tilde{\chi}_1^0 \rightarrow \ell'^- \tilde{\ell}'_R$, followed by the three-body decay $\tilde{\ell}'_R \rightarrow \ell'^+ \ell^\pm \tilde{\ell}_R^\mp$ via a virtual neutralino, $(\tilde{\chi}_n^0)^*$; see the upper decay chain of Fig. 4 for an example. Here, $\tilde{\ell}_R$ is the LSP.

These three-body slepton decays are special to \tilde{e}_R and $\tilde{\mu}_R$ LSP scenarios. The corresponding decay rates are calculated in Appendix D and are taken into account in the following collider analysis.

The coupling Λ in $\tilde{\ell}_R$ LSP scenarios is of similar size as the gauge couplings and thus enables R -parity violating decays with a significant branching ratio of sparticles which are not the LSP. Thus, not every SUSY decay chain involves the LSP. Of particular importance are the two-body R -parity violating decays of the $\tilde{\tau}_1$ [16], especially in the case when a $\tilde{\tau}_1$ NLSP is nearly mass degenerate with the $\tilde{\ell}_R$ LSP, like for the benchmark point BE1; cf. Table VII. Furthermore, sneutrinos (left-handed charged sleptons) may decay into two hard charged leptons (one charged lepton and a neutrino) if they couple directly to the dominant R -parity violating operator. This leads to a sharp sneutrino mass peak in the respective dilepton invariant mass distribution, as we will show in Sec. V. From the R -parity violating left-handed slepton decays we expect large amounts of missing energy from the neutrino.

The lightest top squark, \tilde{t}_1 , is in most B₃ mSUGRA scenarios the lightest squark. Thus, \tilde{t}_1 pair production forms a sizable fraction of all SUSY production processes. The decay of each \tilde{t}_1 yields at least one b -quark (either directly from the decay $\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b$ and/or from the top quark decay after $\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t$). We therefore expect an enhanced b -quark multiplicity for \tilde{t}_1 pair production. We will use the b -quark multiplicity in Sec. V to discriminate these events from other SUSY processes.

To conclude this discussion, as one can see from Table III, we expect multilepton final states for \tilde{e}_R and $\tilde{\mu}_R$ LSP scenarios at the LHC. On the one hand, we obtain charged leptons from the $\tilde{\chi}_1^0$ decay into the $\tilde{\ell}_R$ LSP. On the other hand, each LSP decay involves a charged lepton. Furthermore, as explained above, non-LSPs can also decay via the dominant R -parity violating operator into leptons. Therefore, a multilepton analysis will be the best search strategy for our $\tilde{\ell}_R$ LSP scenarios.

Multicharged lepton final states (especially electrons and muons) are one of the most promising signatures to be tested with early LHC data. Electrons and muons can be easily identified and the SM background for high lepton multiplicities is very low [17]. We therefore investigate in the following the discovery potential of \tilde{e}_R LSP scenarios

TABLE III. LHC signatures (right column) for selectron and smuon LSP scenarios (second column) assuming one dominant $L_i L_j \bar{E}_k$ operator Λ (left column) and the SUSY cascade of Eq. (15).

Λ coupling	LSP decay	LHC signature
λ_{121}	$\tilde{e}_R \rightarrow \begin{cases} e\nu_\mu \\ \mu\nu_e \end{cases}$	$2j + 2e + E_T + \begin{cases} 2e \\ e\mu \\ 2\mu \end{cases}$
λ_{131}	$\tilde{e}_R \rightarrow \begin{cases} e\nu_\tau \\ \tau\nu_e \end{cases}$	$2j + 2e + E_T + \begin{cases} 2e \\ e\tau \\ 2\tau \end{cases}$
λ_{231}	$\tilde{e}_R \rightarrow \begin{cases} \mu\nu_\tau \\ \tau\nu_\mu \end{cases}$	$2j + 2e + E_T + \begin{cases} 2\mu \\ \mu\tau \\ 2\tau \end{cases}$
λ_{132}	$\tilde{\mu}_R \rightarrow \begin{cases} e\nu_\tau \\ \tau\nu_e \end{cases}$	$2j + 2\mu + E_T + \begin{cases} 2e \\ e\tau \\ 2\tau \end{cases}$

with an inclusive three-lepton search analysis. We will treat electrons and muons equally and thus expect similar results for $\tilde{\mu}_R$ LSP scenarios. However, after a signal above the SM backgrounds has been discovered, the flavor of the leptons might reveal some additional information about the underlying new physics model; see e.g. Table III.

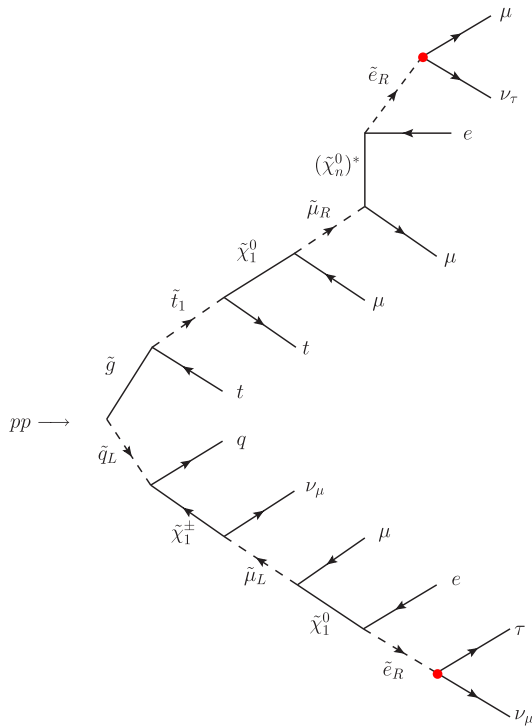


FIG. 4 (color online). Example for squark-gluino production with successive cascade decay into two \tilde{e}_R LSPs. The R -parity violating decays are marked by [red] dots. $(\tilde{\chi}_n^0)^*$ denotes a virtual neutralino. Note that R -parity violating decays can occur earlier in the chain. In this case, the LSP is not produced. See the tables of benchmark branching ratios in Appendix A.

IV. DISCOVERY POTENTIAL AT THE LHC

In this section, we study the discovery potential of \tilde{e}_R and $\tilde{\mu}_R$ LSP models with an inclusive search analysis for tripleton final states at the LHC. Because of the striking multileptonic signature of these models (see Sec. III), a discovery of new physics might be possible with early LHC data. We therefore study the prospects at the LHC assuming separately a center-of-mass system (cms) energy of 7 TeV and 14 TeV.

A. Major backgrounds

In the following Monte Carlo (MC) study, we consider SM backgrounds that can produce three or more charged leptons (electrons or muons) in the final state at the particle level, i.e. after (heavy flavor) hadron and tau lepton decays. For the heavy flavor quarks, we consider bottom, b , and charm, c , quarks [87]. Moreover, we expect the SUSY signal events to contain additional energy from hard jets arising from decays of the heavier (colored) sparticles. We thus consider the following SM processes as the major backgrounds in our analysis:

- (i) Top production. We consider top pair production ($t\bar{t}$), single-top production associated with a W boson (Wt) and top pair production in association with a gauge boson ($Wt\bar{t}$, $Zt\bar{t}$). Each top quark decays into a W boson and a b quark. Leptons may then originate from the W and/or b decay.
- (ii) Z + jets, i.e. Z boson production in association with one or two (parton-level) jets. For the associated jet(s) we consider only c and b quarks. We force the Z boson to decay leptonically.
- (iii) W + jets, i.e. W boson production in association with two heavy flavor quarks (c or b) at parton level. We demand that the W decays into a charged lepton and a neutrino.
- (iv) Di-boson (WZ, ZZ) and di-boson + jet (WWj, WZj, ZZj) production. For the WZ and ZZ background, the gauge bosons are forced to decay leptonically. For WWj , we consider only the heavy flavor quarks c and b for the (parton-level) jet, while for WZj and ZZj every quark flavor is taken into account.

We have also included the processes where we have a virtual gamma instead of a Z boson.

For the backgrounds with heavy flavor quarks, we demand (at parton level) a minimal transverse momentum for the c or b quarks of $p_T \geq 10$ GeV corresponding to our object selection cut for the leptons; cf. Sec. IV B. Table IV gives an overview of the background samples used in our analysis. In principle, QCD production of four heavy flavor quarks, like $b\bar{b}b\bar{b}$ production, can also produce three lepton events. However, these backgrounds are negligible compared to the other backgrounds in Table IV, because

TABLE IV. SM background MC samples (first and second column) used for our analysis. The third and fourth (fifth and sixth) column shows the leading-order cross section (number of simulated events) for pp collisions at a cms energy of $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV, respectively. For the event simulation, we employ the MC generator listed in the last column. We have also included the processes where we have a virtual gamma instead of a Z boson.

Sample	Subsample	LO cross section [pb]		Simulated events		Generator
		7 TeV	14 TeV	7 TeV	14 TeV	
Top	$t\bar{t}$	86.7	460	200 000	5 000 000	HERWIG
	Wt	10.2	60.7	100 000	1 200 000	MADGRAPH+HERWIG
	$Wt\bar{t}$	0.14	0.52	10 000	10 000	MADGRAPH+HERWIG
	$Zt\bar{t}$	0.066	0.43	10 000	10 000	HERWIG
$Z + \text{jets}$	$Zc\bar{c}$	49.5	187	100 000	2 000 000	HERWIG
	$Zb\bar{b}$	44.6	171	100 000	2 000 000	HERWIG
	$Z(\rightarrow \ell^+ \ell^-) + j$ ($j = c, b$)	59.6	203	180 000	3 700 000	MADGRAPH+HERWIG
$W + \text{jets}$	$W(\rightarrow \ell\nu) + jj$ ($j = c, b$)	38.2	95.2	135 000	1 400 000	MADGRAPH+HERWIG
Di-boson	$WZ \rightarrow \text{leptons}$	0.20	0.40	100 000	100 000	MADGRAPH+HERWIG
	$ZZ \rightarrow \text{leptons}$	0.03	0.06	22 000	75 000	MADGRAPH+HERWIG
	$WW + j$ ($j = c, b$)	10.9	64.0	120 000	1 000 000	MADGRAPH+HERWIG
	$WZ + j$ ($j = \text{all flavors}$)	7.0	25.0	77 000	100 000	MADGRAPH+HERWIG
	$ZZ + j$ ($j = \text{all flavors}$)	3.2	10.2	16 000	280 000	MADGRAPH+HERWIG

the probability of obtaining three *isolated* leptons from heavy flavor decay is too low [88].

B. Monte Carlo simulation and object selection

The $t\bar{t}$, $Zt\bar{t}$, $Zc\bar{c}$ and $Zb\bar{b}$ backgrounds are simulated with HERWIG6.510 [89–91]. For the other SM processes we employ MADGRAPH4.4.30 [92] for the generation of the hard process which is then fed into HERWIG. The employed MC generators are listed in Table IV. We also give the leading-order (LO) cross section and the number of simulated events for each background sample for both cms energies. The cross sections are taken from HERWIG (for the $t\bar{t}$, $Zt\bar{t}$, $Zc\bar{c}$ and $Zb\bar{b}$ backgrounds) or MADGRAPH (else). We consider only the leading-order cross sections for the signal and background samples. We note however that the next-to-leading-order (NLO) corrections can be large (see e.g. Refs. [93–97]) and should be included in a more dedicated analysis. Furthermore, our simulation does not account for detector effects, i.e. we neglect backgrounds with leptons

faked by jets or photons. However, we expect these backgrounds to be small, because the fake rate for electrons and muons is quite low [17].

The SUSY mass spectra were calculated with SOFTSUSY3.0.13 [73,74]. The SOFTSUSY output was then fed into ISAWIG1.200 and ISAJET7.64 [98] in order to calculate the decay widths of the SUSY particles. We added the missing three-body slepton decays $\tilde{\ell}'_R \rightarrow \ell' \ell \tilde{\ell}_R$ and $\tilde{\tau}_1 \rightarrow \tau \ell \tilde{\ell}_R$ to the ISAJET code; see Appendix D for the calculation and a discussion of these new slepton decays. The signal processes, i.e. pair production of *all* SUSY particles, were simulated with HERWIG6.510.

We give in Table V leading-order cross sections for sparticle pair production at the LHC for the three benchmark scenarios BE1, BE2 and BE3; cf. Table II. We separately assume cms energies of $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV. We present the cross sections for the signal (last row), i.e. pair production of all sparticles, and for three of its subprocesses: the production of sparton pairs (second

TABLE V. Total LO cross section (in fb) for the benchmark scenarios BE1, BE2 and BE3 for pair production of all SUSY particles (last row) and three of its subprocesses: sparton (i.e. squark and gluino) pair production (second row), slepton pair production (third row) and electroweak (EW) gaugino pair or EW gaugino plus sparton production (fourth row). We separately assume pp collisions at cms energies of $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV. The cross sections are calculated with HERWIG. We have simulated $\approx 15\,000$ ($\approx 250\,000$) SUSY events for the 7 TeV (14 TeV) MC signal sample.

Production process	Cross section (in fb) at $\sqrt{s} = 7$ TeV			Cross section (in fb) at $\sqrt{s} = 14$ TeV		
	BE1	BE2	BE3	BE1	BE2	BE3
$pp \rightarrow \text{sparton pairs}$	86.7	152	139	1970	2770	2760
$pp \rightarrow \text{slepton pairs}$	24.0	19.9	21.1	96.7	83.9	88.1
$pp \rightarrow \text{gaugino pairs, gaugino + sparton}$	32.2	38.6	43.3	224	259	284
$pp \rightarrow \text{sparticle pairs}$	143	210	203	2290	3110	3130

row), where we consider squarks and gluinos as spartons, slepton pair production (third row) and the production of electroweak (EW) gaugino pairs or an EW gaugino in association with a squark or gluino (fourth row). For all benchmark points, sparton pair production is the dominant SUSY production process. Therefore, the majority of the SUSY events will fulfill our signature expectations including at least two hard jets; cf. Sec. III.

For the reconstruction of jets, we employ FASTJET 2.4.1 [99,100] using the kt-algorithm with cone radius $\Delta R = 0.4$. Here $\Delta R \equiv \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$, where η (ϕ) is the pseudorapidity (azimuthal angle). We select jets and leptons (i.e. electrons and muons) only if $|\eta| < 2.5$ and if their transverse momentum is larger than 10 GeV. In addition, leptons are rejected if the total transverse momentum of all particles within a cone of $\Delta R < 0.2$ around the lepton three-momentum axis exceeds 1 GeV.

C. Kinematic distributions

In this section we discuss kinematic distributions for the benchmark points of Table II and motivate our cuts of Sec. IV D. The distributions correspond to our 7 TeV event sample and are normalized to one.

The p_T distribution of all electrons [muons] after object selection (cf. the last paragraph of Sec. IV B) is shown in Fig. 5(a) [Fig. 5(b)] for the B_3 mSUGRA benchmark models BE1, BE2 and BE3. In all scenarios, the electrons mostly stem from the neutralino decay $\tilde{\chi}_1^0 \rightarrow \tilde{e}_R e$, while many of the muons come from the LSP decay $\tilde{e}_R \rightarrow \mu \nu_\tau$; cf. Appendix A.

We observe in Fig. 5(a) that BE1 leads to the on average hardest electrons. In this scenario, the mass difference between the $\tilde{\chi}_1^0$ (decaying often via $\tilde{\chi}_1^0 \rightarrow e\tilde{e}_R$) and the \tilde{e}_R LSP is about 27 GeV and thus quite large (compared to the other benchmark points). Furthermore, the $\tilde{\tau}_1$ NLSP

decays dominantly via the R -parity violating decay $\tilde{\tau}_1 \rightarrow e\nu_\mu$. A large fraction of the $\tilde{\tau}_1$ mass is thus transformed into the 3-momentum of an electron. From both sources, we obtain electrons with large p_T . For example, 81% of all selected electrons have $p_T^{\text{el}} \geq 25$ GeV in BE1.

The situation for BE2 and BE3 is different. Because of the smaller mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP (compared to BE1), the electrons from $\tilde{\chi}_1^0$ decay are less energetic. For instance, the fraction of selected electrons with $p_T^{\text{el}} \leq 25$ GeV is 55% (34%) for BE2 (BE3). Furthermore, the electron multiplicity is reduced in these scenarios, because many electrons fail the lower p_T cut ($p_T^{\text{el}} > 10$ GeV) of the object selection. Because of this, 30% (50%) of all events do not contain any selected electron in BE2 (BE3).

In contrast, the situation for the muons, Fig. 5(b), is reversed (compared to the electrons). A large amount of the muons are soft in BE1, whereas BE2 and BE3 have a harder muon p_T spectrum. Note that, for BE1, a sizable fraction of all muons do not even fulfill the object selection requirement of $p_T > 10$ GeV, so that 34% of all events does not contain any selected muon. These muons in BE1 stem, for example, from the three-body decays of the $\tilde{\mu}_R$ into the \tilde{e}_R or the $\tilde{\tau}_1$ and are in general soft due to decreased phase space; cf. Table VII. In contrast, the muons in BE2 and BE3 are on average much harder, since the majority of these muons originate from the \tilde{e}_R LSP decay.

We conclude that the lepton p_T spectrum strongly depends on the sparticle mass spectrum. Therefore, we desist from making further requirements on the lepton p_T since this would imply a strong model dependence in the event selection. We will require only at least three charged (and isolated) leptons as one of our cuts in the next section.

We show in Fig. 6(a) [Fig. 6(b)] the p_T distribution of the [second] hardest jet for the benchmark points BE1,

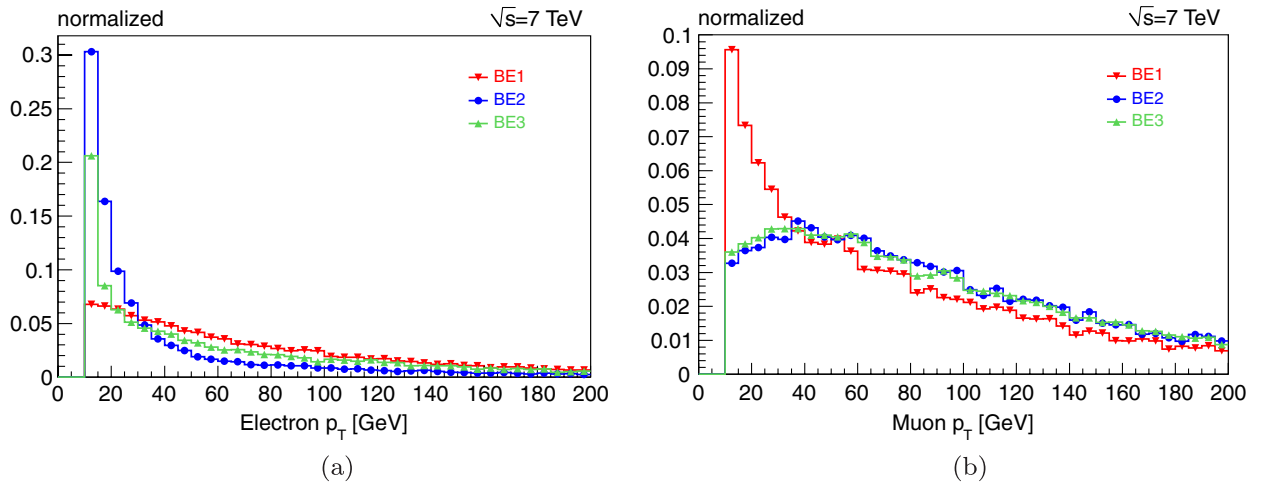


FIG. 5 (color online). p_T distribution of (a) all selected electrons and (b) of all selected muons at the LHC for the B_3 mSUGRA benchmark models BE1 (red), BE2 (blue) and BE3 (green) for a cms energy of $\sqrt{s} = 7$ TeV and after object selection cuts. The distributions are normalized to one.

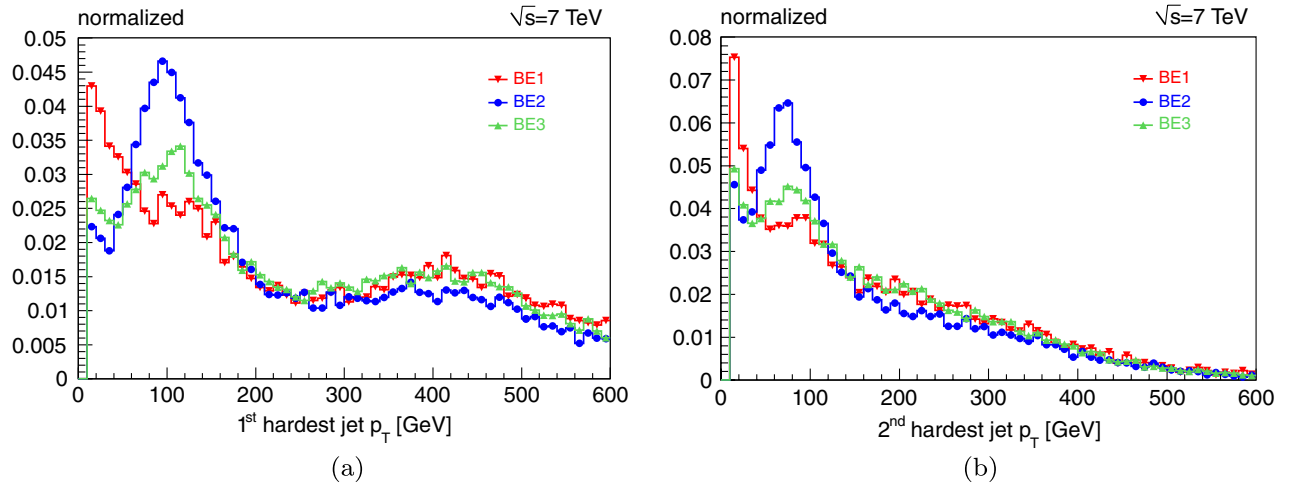


FIG. 6 (color online). Hardest jet (a) and second-hardest jet (b) p_T distributions at the LHC for the B_3 mSUGRA benchmark models BE1 (red), BE2 (blue) and BE3 (green) for a cms energy of $\sqrt{s} = 7$ TeV and after object selection cuts. The distributions are normalized to one.

BE2 and BE3. For all scenarios, we observe a broad peak of the hardest jet p_T at around 400 GeV. Many of these jets stem from the decays of first- and second-generation squarks into the $\tilde{\chi}_1^0$; cf. Tables VII, VIII, and IX.

We find another peak in Fig. 6(a) as well as in Fig. 6(b) at around 100 GeV. These jets stem mainly from the t quark decay products from $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$ decay. The peak is most pronounced in BE2, since here we have a light \tilde{t}_1 mass, $M_{\tilde{t}_1} = 448$ GeV, and thus an enhanced \tilde{t}_1 pair production cross section. In contrast, the \tilde{t}_1 mass is about 80 GeV heavier in BE1 and therefore the peak is hardly visible in Fig. 6.

For BE1, the p_T distribution of the hardest and second hardest jet peaks at low values. These soft jets stem from initial and final state radiation. They appear as the hardest jets in EW gaugino and slepton pair production which forms a sizable fraction (39%) of all SUSY production processes in BE1; cf. Table V. They are less important for BE2 and BE3. However, this picture will change for a cms energy of $\sqrt{s} = 14$ TeV, where sparton pair production is much more dominant in BE1.

Because most events possess at least two jets, we demand in the following section at least two jets as one of our cuts. Furthermore, we take into account that many jets (and some of the leptons) are hard, i.e. we demand the visible effective mass to be larger than a few 100 GeV; see the next section for details.

D. Event selection and outflow

We now develop a set of cuts in order to obtain a statistically significant signal and a good signal to (SM) background ratio. To motivate the different selection steps, we show in Fig. 7 the event distributions that correspond to the different cut variables before the respective cut is applied. We give distributions for the three $\tilde{\epsilon}_R$ LSP

benchmark models (BE1, BE2, BE3), for the SM background, and, for comparison, for the R -parity conserving benchmark model SPS1a [50].⁶ The distributions correspond to an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7$ TeV.

In Table VI, we give the number of background and signal events after each cut of the analysis. Furthermore, we provide for each signal benchmark scenario the significance estimator S/\sqrt{B} , where S (B) is the number of signal (SM background) events. In general, the signal can be defined to be observable if [51]

$$S \geq \max[5\sqrt{B}, 5, 0.5B]. \quad (16)$$

The requirement $S \geq 0.5B$ avoids the possibility that a small signal on top of a large background could otherwise be regarded as statistically significant, although this would require the background level to be known to an excellent precision. In the case of a very low background expectation, $B < 1$, we still require five signal events for a discovery.

As we have seen in Sec. III, we expect an extensive number of charged leptons in the final state. However, the lepton flavor multiplicity, i.e. the multiplicity of electrons and muons, depends strongly on the LSP flavor as well as on the dominant Λ coupling; cf. Table III. In addition, as we have seen in the last section, the p_T spectrum of the leptons is strongly correlated to the details of the mass hierarchy. Therefore, in order to be as model independent as possible, we simply demand as our first cut three charged leptons (electrons or muons) in the final state

⁶SPS1a has a mass spectrum similar to BE1, BE2, and BE3. The main difference lies in the light part of the spectrum, where we have in SPS1a a stable and invisible $\tilde{\chi}_1^0$ LSP. The $\tilde{\tau}_1$ is the NLSP. Furthermore, the overall mass scale is a bit lower, e.g. the squark and gluino masses are around 500–600 GeV.

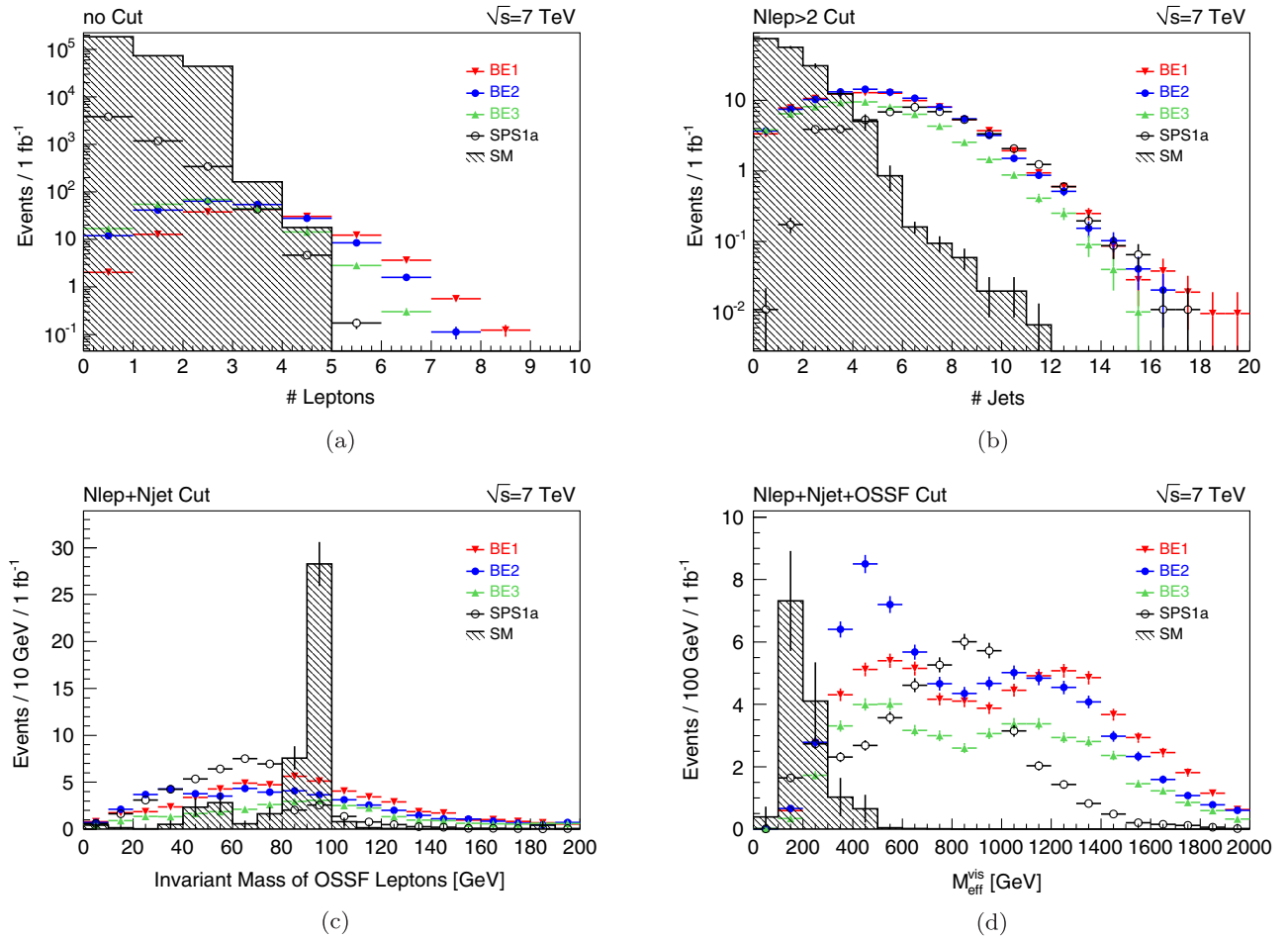


FIG. 7 (color online). Event distributions of several cut variables: (a) lepton (e, μ) multiplicity with no cut applied; (b) jet multiplicity after the tripleton cut has been applied; (c) invariant mass distribution of OSSF lepton pairs after the tripleton and jet multiplicity cuts have been applied; and (d) effective visible mass distribution for the SM background ([gray] patterned) and the SUSY models BE1 [red], BE2 [blue], BE3 [green] and SPS1a (empty circle). Note that Figs. 7(a) and 7(b) are given on a logarithmic scale. The distributions show the number of events before the event selection cut on the respective variable (see text) is applied. They are normalized to an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$. The error bars correspond to the statistical fluctuations of our MC samples.

without further requirements on the p_T (besides the object selection cut of $p_T > 10 \text{ GeV}$).

How useful this cut is can be seen in Fig. 7(a), where we show the lepton multiplicity after object selection cuts. The distribution for the B_3 benchmark scenarios peaks around 2–3 leptons, whereas most of the SM background events possess fewer than three electrons or muons. In principle, by demanding at least five charged leptons in the final state, we can already get a (nearly) background free event sample. However, such a cut would also significantly reduce the number of signal events and is therefore less suitable for an analysis of early data. We also observe in Fig. 7(a) many more leptons in the R -parity violating scenarios than in SPS1a. This is expected, due to the additional leptons from the decays of and into the selectron LSP.

As can be seen in the third column of Table VI, after demanding three leptons, the main SM background comes from di-boson events. They account for 68% of

the background. Furthermore, no $W + \text{jets}$ events survive this cut, indicated by “ ≤ 1.0 ” events in the fourth row of Table VI. At the same time, the number of signal events is reduced to 63%, 44% and 30% for BE1, BE2 and BE3, respectively. Because of the low mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP in BE3, many electrons from $\tilde{\chi}_1^0$ decay fail the object selection cuts; cf. the discussion of Fig. 5(a). BE1 and BE2 might already be observable after the first cut, i.e. $S/\sqrt{B} > 5$.

Next, we will use the fact that we expect several jets from squark and gluino decays; see Sec. III. The jet multiplicity after demanding three leptons is shown in Fig. 7(b). Because of the weak object selection criteria for the jets ($p_T > 10 \text{ GeV}$) and the small radius for the jet reconstruction ($\Delta R = 0.4$), we observe a high jet multiplicity. As discussed in Sec. III, we expect at least two jets from squark and gluino decays. Therefore, we demand as our second cut (fourth column of Table VI) the number of jets

TABLE VI. Number of SM background and signal events after each step in the event selection corresponding to an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$. For each signal model (BE1, BE2 and BE3; see Table II), we show S/\sqrt{B} as significance estimator. The uncertainties correspond to statistical fluctuations.

Sample	Before cuts	$N_{\text{lep}} \geq 3$	$N_{\text{jet}} \geq 2$	M_{OSSF}	$M_{\text{eff}}^{\text{vis}} \geq 300 \text{ GeV}$
Top	$97\,111 \pm 197$	14.9 ± 2.2	13.8 ± 2.1	12.0 ± 2.1	2.1 ± 0.8
Z + jets	$153\,591 \pm 254$	51.9 ± 4.3	16.6 ± 2.4	1.0 ± 0.6	≤ 1.0
W + jets	$38\,219 \pm 103$	≤ 1.0	≤ 1.0	≤ 1.0	≤ 1.0
Di-boson	$21\,331 \pm 48$	179.2 ± 3.0	53.5 ± 2.0	2.6 ± 0.4	0.7 ± 0.2
All SM	$310\,252 \pm 341$	264.0 ± 5.7	83.9 ± 3.8	15.6 ± 2.2	2.8 ± 0.8
BE1	143.1 ± 1.2	90.5 ± 0.9	79.4 ± 0.9	68.8 ± 0.8	65.5 ± 0.8
S/\sqrt{B}		5.6	8.7	17.4	39.1
BE2	210.4 ± 1.5	92.6 ± 1.0	81.4 ± 0.9	73.8 ± 0.9	70.4 ± 0.8
S/\sqrt{B}		5.7	8.9	18.7	42.1
BE3	202.7 ± 1.4	61.6 ± 0.8	51.3 ± 0.7	45.2 ± 0.7	43.2 ± 0.7
S/\sqrt{B}		3.8	5.6	11.4	25.8

to be larger than 2, i.e. $N_{\text{jet}} \geq 2$. This cut suppresses roughly two-thirds of the di-boson backgrounds WZ and ZZ as well as of the $Z + \text{jets}$ background. However, di-boson production, especially $WZ + j$, still accounts for most of the background. The number of signal events is reduced by only 12–17%. After this cut, all our benchmark points fulfill the criteria in Eq. (16) and are thus observable.

In order to further reduce the SM backgrounds involving Z bosons, we construct all possible combinations of the invariant mass of opposite-sign-same-flavor (OSSF) leptons. The distributions (after the three-lepton and $N_{\text{jet}} \geq 2$ cut) are shown in Fig. 7(c). As expected, the SM background has a large peak at the Z boson mass $M_Z = 91.2 \text{ GeV}$, while the signal distribution is mostly flat in that region. Thus, as the third cut (fifth column of Table VI) of our event selection, we reject all events where the invariant mass of at least one OSSF lepton pair lies within a 10 GeV window around the Z boson mass, i.e. we demand

$$M_{\text{OSSF}} \notin [81.2 \text{ GeV}, 101.2 \text{ GeV}]. \quad (17)$$

This cut strongly reduces the $Z + \text{jets}$ and di-boson backgrounds, leaving $t\bar{t}$ as the dominant SM background. Roughly 90% of the signal events (for all benchmark scenarios) survive this cut. The statistical significance now lies between 10 and 20 for all benchmark points.

As we have shown in Sec. IV C, our SUSY events contain a large amount of energy in the form of high- p_T jets and leptons. Thus, we construct the visible⁷ effective mass,

$$M_{\text{eff}}^{\text{vis}} \equiv \sum_{i=1}^4 p_T^{\text{jet},i} + \sum_{\text{all}} p_T^{\text{lep}}, \quad (18)$$

⁷We denote this variable as *visible* effective mass because it does not include the missing transverse energy as in other definitions of the effective mass [17].

i.e. the scalar sum of the absolute value of the transverse momenta of the four hardest jets and all selected leptons in the event. The visible effective mass distribution is shown in Fig. 7(d). The SM background dominates for $M_{\text{eff}}^{\text{vis}} < 300 \text{ GeV}$, while most of the signal events exhibit a visible effective mass above 300 GeV. This value is slightly higher for the 14 TeV data set. Therefore, we demand as the last cut of our event selection (last column of Table VI)

$$M_{\text{eff}}^{\text{vis}} > \begin{cases} 300 \text{ GeV}, & \text{if } \sqrt{s} = 7 \text{ TeV}, \\ 400 \text{ GeV}, & \text{if } \sqrt{s} = 14 \text{ TeV}. \end{cases} \quad (19)$$

After this cut, only 2.8 ± 0.8 SM events remain at $\sqrt{s} = 7 \text{ TeV}$ and an integrated luminosity of 1 fb^{-1} . The background is dominated by $t\bar{t}$ production. The signal is nearly unaffected by this cut as can be seen in Table VI. The statistical significance is now roughly as large as 25 (40) for the benchmark point(s) BE3 (BE1 and BE2). Furthermore, the signal-to-background ratio is now of $\mathcal{O}(10)$. Therefore, systematic uncertainties of the SM backgrounds are not problematic. A signal is clearly visible.

We observe in Fig. 7(d) two peaks in the visible effective mass distributions for our benchmark scenarios. The peak at lower values of $M_{\text{eff}}^{\text{vis}}$ contains mainly events from \tilde{t}_1 pair production, while events from (right-handed) first- and second-generation squark or gluino production build the second peak at higher $M_{\text{eff}}^{\text{vis}}$ values. Because of the large mass difference between the \tilde{t}_1 and the other squarks of about 400 GeV–500 GeV (depending on the model; see Tables VII, VIII, and IX), these peaks are clearly separated in the visible effective mass. We make use of this fact in Sec. V when we present a method to reconstruct the masses of both the \tilde{t}_1 and the right-handed first- and second-generation squarks.

In order to test the flavor sensitivity of our analysis, we have applied our cuts to a modified version of the benchmark models presented in Table II. Instead of λ_{231} , we chose λ_{131} (λ_{132}) as the dominant R -parity violating

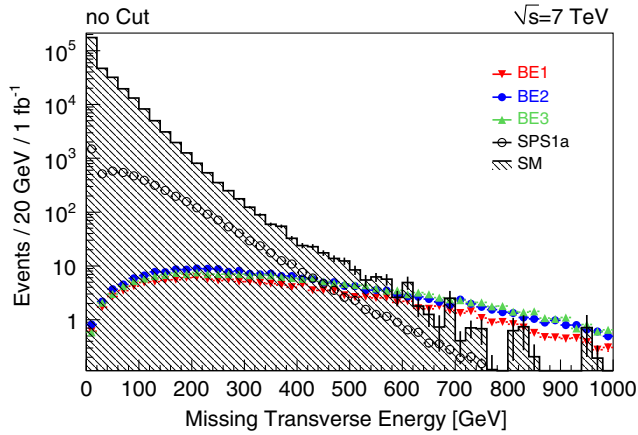


FIG. 8 (color online). Missing transverse energy, \cancel{E}_T , distribution for BE1, BE2, BE3, SPS1a and the SM background. No cuts are applied. The number of events corresponds to an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$.

coupling at M_{GUT} to obtain the \tilde{e}_R ($\tilde{\mu}_R$) as the LSP, while leaving the other B_3 mSUGRA parameters unchanged. The results for the $\tilde{\mu}_R$ LSP scenarios are in agreement with the original benchmark scenarios within statistical fluctuations of the MC samples.

However, for the \tilde{e}_R LSP scenarios with a dominant λ_{131} coupling at M_{GUT} , the cut on the invariant mass of OSSF leptons rejects more signal events than for scenarios with λ_{231} . For the modified scenario of BE1 (BE2), the number of signal events passing the M_{OSSF} cut is reduced by around 15% (3%) compared to the original results; cf. Table VI. This difference is strongest for BE1-like scenarios, because the endpoint of the di-electron invariant mass distribution, where one electron comes from the $\tilde{\chi}_1^0$ decay and the other from the \tilde{e}_R LSP decay [cf. also Eq. (25a)], coincides with the upper value of the Z boson mass window. However, this is just a coincidence and a different mass spectrum (compared to BE1) with a \tilde{e}_R LSP and λ_{131} at M_{GUT} will not have such a suppression.

We conclude that, in most cases, our detailed study of \tilde{e}_R LSP models with a dominant R -parity violating coupling λ_{231} is representative for all B_3 mSUGRA models with a \tilde{e}_R or $\tilde{\mu}_R$ LSP.

To end this subsection, we present in Fig. 8 the missing transverse energy, \cancel{E}_T , distribution for the benchmark scenarios, for SPS1a and for the combined SM backgrounds before any cuts are applied. In R -parity conserving scenarios like SPS1a, the $\tilde{\chi}_1^0$ LSP is stable and escapes detection, leading to large amounts of \cancel{E}_T . However, for our benchmark points, even though the \tilde{e}_R LSP decays within the detector, we observe a significant amount of missing energy due to the neutrinos from the LSP decay. Moreover, the \cancel{E}_T distribution for SPS1a falls off more rapidly than in the B_3 scenarios. This is because the neutrinos are quite hard, resulting from a two-body decay with a large mass difference. Thus, B_3 scenarios can lead to even

more missing transverse energy than R -parity conserving scenarios. We have not employed \cancel{E}_T in our analysis because our simple cuts already sufficiently suppress the SM background. Furthermore, it is easier to reconstruct electrons and muons than missing energy, especially in the early stages of the experiments.

E. Discovery potential at the LHC

In this subsection, we extend our previous analysis. We perform a two-dimensional parameter scan in the $M_{1/2}$ - M_0 plane around the benchmark point BE1 (Table II). For each parameter point, we generate 1000 signal events, i.e. the pair production of all SUSY particles. We then apply the same cuts developed in the previous section. We estimate the discovery potential of B_3 mSUGRA models with a \tilde{e}_R LSP for the early LHC run at $\sqrt{s} = 7 \text{ TeV}$ and also give prospects for the design energy of $\sqrt{s} = 14 \text{ TeV}$.

Because of the RGE running, all sparticle masses at the weak scale, especially those of the strongly interacting particles, increase with increasing $M_{1/2}$ [85,86]. Thus, by varying $M_{1/2}$, we can investigate the discovery potential as a function of the SUSY mass scale. Furthermore, as we have seen in the previous two sections, the discovery potential is quite sensitive to the mass hierarchy of the lighter sparticles and, in particular, to the mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP. Increasing M_0 increases the masses of the scalar particles, while the gaugino masses are nearly unaffected. Thus, M_0 provides a handle to control the mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R (or $\tilde{\mu}_R$) LSP.

We show in Fig. 9(a) the signal cross section (in pb) for the LHC with $\sqrt{s} = 7 \text{ TeV}$ and in Fig. 9(b) the respective signal efficiency, i.e. the fraction of signal events that pass our cuts. The results are given only for models with a \tilde{e}_R LSP, while models with a $\tilde{\chi}_1^0$ LSP ($\tilde{\tau}_1$ LSP) are indicated by the striped (checkered) region. The solid gray region (lower left corner of Fig. 9) is excluded by the experimental bound on the λ_{231} coupling; cf. Table I.

The signal cross section, Fig. 9(a), which is dominated by the production of colored sparticles, clearly decreases with increasing $M_{1/2}$, i.e. with an increasing SUSY mass scale. For instance, increasing $M_{1/2}$ from 400 GeV to 500 GeV reduces the cross section from 0.6 pb to 0.1 pb, while the right-handed squark (gluino) mass increases from around 820 GeV (930 GeV) to 1010 GeV (1150 GeV). In contrast, the M_0 dependence of the signal cross section is negligible, over the small range that it is varied.

For the benchmark scenario BE1, we find in Fig. 9(b) a signal efficiency of 46%. Going beyond BE1, we observe that the signal efficiency lies between 30% and 50% for most of the \tilde{e}_R LSP parameter space. Therefore, our analysis developed in Sec. IV D also works quite well for a larger set of \tilde{e}_R LSP models.

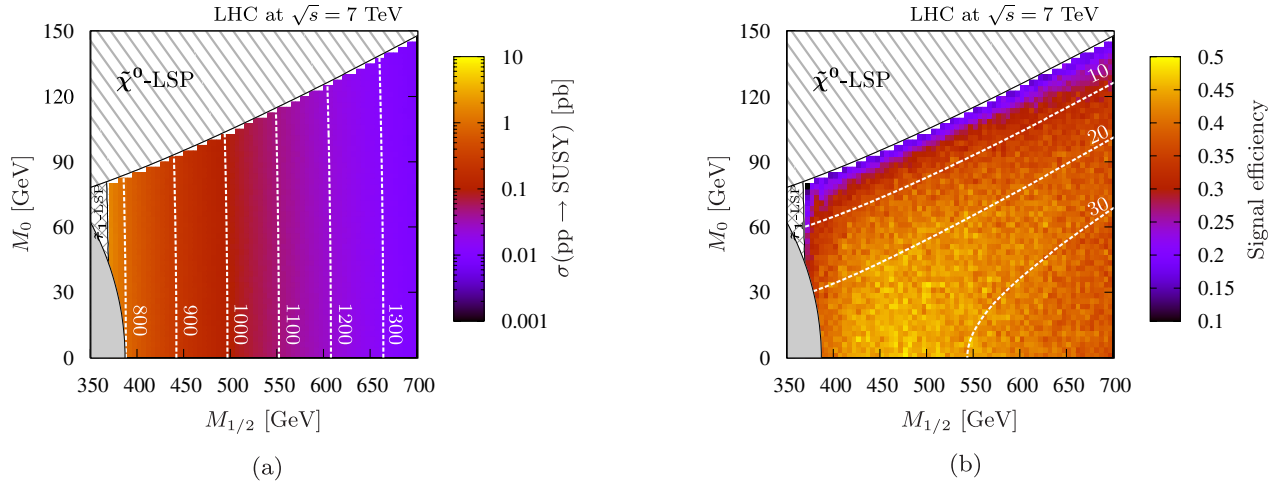


FIG. 9 (color online). (a) Signal cross section (in pb) and (b) signal efficiency at the LHC at $\sqrt{s} = 7$ TeV in the $M_{1/2}$ - M_0 plane. The other parameters are those of BE1 ($A_0 = -1250$ GeV, $\tan\beta = 5$, $\text{sgn}(\mu) = +$, and $\lambda_{231}|_{\text{GUT}} = 0.045$). In (a), the [white] dashed contour lines give the (first- and second-generation) \tilde{q}_R mass in GeV. In (b), the [white] dashed contour lines give the mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP in GeV. The patterned regions correspond to scenarios with either a $\tilde{\tau}_1$ or a $\tilde{\chi}_1^0$ LSP. The solid gray region in the lower left-hand corner is excluded by the bound on λ_{231} ; cf. Table I.

However, the signal efficiency decreases dramatically if the mass difference, ΔM , between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP approaches zero. For models with $\Delta M \lesssim 2.5$ GeV, the signal efficiency lies just around 10–20%. As described in detail in Sec. IV C, the electrons in this parameter region from the decay $\tilde{\chi}_1^0 \rightarrow \tilde{e}_R e$ are usually very soft and thus tend to fail the minimum p_T requirement of the

object selection, i.e. $p_T > 10$ GeV. For models with $\Delta M > 10$ GeV, the signal efficiency becomes more or less insensitive to ΔM . Note that, if we choose a stronger minimum lepton p_T requirement in our analysis, the band of low signal efficiency will become wider.

The signal efficiency also depends slightly on $M_{1/2}$. At low values, $M_{1/2} \lesssim 400$ GeV, i.e. for models with a light

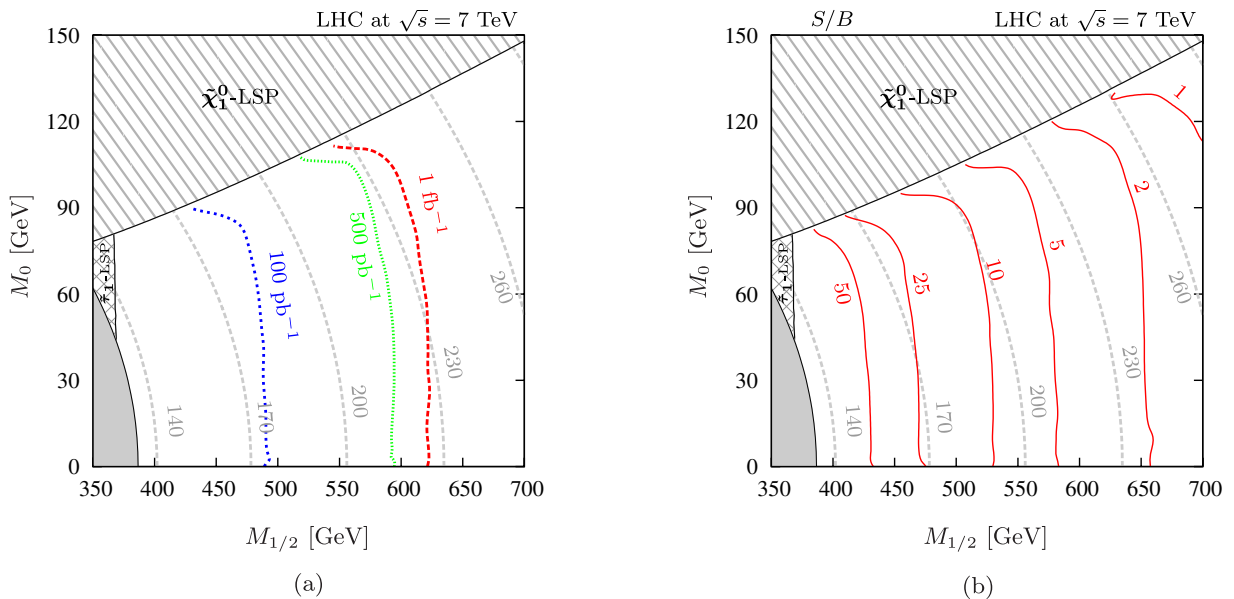


FIG. 10 (color online). Discovery reach at the LHC at $\sqrt{s} = 7$ TeV in the $M_{1/2}$ - M_0 plane. The other B_3 mSUGRA parameters are $A_0 = -1250$ GeV, $\tan\beta = 5$, $\text{sgn}(\mu) = +$ and $\lambda_{231}|_{\text{GUT}} = 0.045$. In (a) we give the minimal required integrated luminosity for a discovery; cf. Eq. (16). We show contours for 100 pb^{-1} ([blue] dotted line), 500 pb^{-1} ([green] fine dotted line), and 1 fb^{-1} ([red] dashed line). In (b) we show contours for the signal-to-background ratio, S/B ([red] solid curves). The patterned regions correspond to scenarios with either a $\tilde{\tau}_1$ or a $\tilde{\chi}_1^0$ LSP. The solid gray region in the lower left-hand corner is excluded by the bound on λ_{231} ; cf. Table I. The [gray] dashed contour lines give the \tilde{e}_R mass (in GeV) as indicated by the labels 140, 170, and so on.

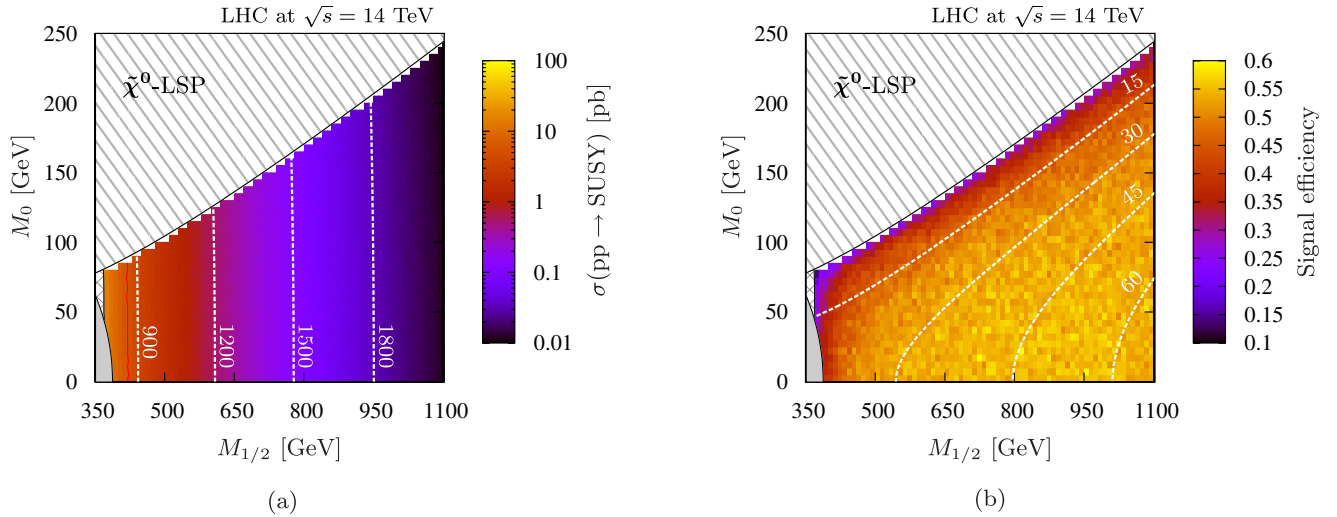


FIG. 11 (color online). Same as Fig. 9, but for a cms energy of $\sqrt{s} = 14$ TeV. (a) Signal cross section in pb at the LHC. The white dashed contour lines give the (first- and second-generation) \tilde{q}_R mass in GeV. (b) Selection efficiency for the signal events at the LHC. The white dashed contour lines give the mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP in GeV.

sparticle mass spectrum, more events are rejected by the cut on the visible effective mass. Moreover, the SM particles from cascade decays and LSP decays have in this case on average smaller momenta than in scenarios with a heavier mass spectrum, and thus may fail to pass the object selection.⁸ The signal efficiency is highest for values of $M_{1/2}$ between 450 GeV and 550 GeV and reaches up to 50%. However, when going to very large $M_{1/2}$, the signal efficiency again decreases. Here, the production of sparton pairs is suppressed due to their large masses and the jet multiplicity is reduced. Fewer events will then pass the $N_{\text{jet}} \geq 2$ and $M_{\text{eff}}^{\text{vis}}$ cut. For example, for $M_{1/2} = 500$ GeV ($M_{1/2} = 700$ GeV), sparton pair production contributes (only) 58% (24%) to the total sparticle pair production cross section.

We give in Fig. 10(a) the discovery potential of \tilde{e}_R LSP scenarios at the LHC with $\sqrt{s} = 7$ TeV. The discovery reach for the integrated luminosities 100 pb^{-1} , 500 pb^{-1} and 1 fb^{-1} is shown. We use Eq. (16) as criterion for a discovery. Furthermore, we present in Fig. 10(b) the signal-to-background ratio, S/B , as a measure for the sensitivity on systematic uncertainties of the SM background. As shown in the previous section, the SM background is reduced to 2.8 ± 0.8 events when we employ the cuts of Table VI.

Figure 10(a) suggests that \tilde{e}_R LSP scenarios up to $M_{1/2} \lesssim 620$ GeV can be discovered with an integrated luminosity of 1 fb^{-1} . This corresponds to squark masses of 1.2 TeV and \tilde{e}_R LSP masses of around 230 GeV. For these models, we have a signal-to-background ratio of $S/B \approx 3$ and thus systematic uncertainties of the SM

⁸However, due to our rather weak p_T requirements for jets and leptons, this effect does not play a major role.

background are not problematic. Furthermore, we see that BE1 ($M_{1/2} = 475$ GeV, $M_0 = 0$ GeV) can already be discovered with $\lesssim 100 \text{ pb}^{-1}$ of data. We also see in Fig. 10 that scenarios with a small mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP are more difficult to discover, as expected from Fig. 9(b).

We now discuss the prospects of a discovery at the LHC at $\sqrt{s} = 14$ TeV. In Fig. 11(a), we give the signal cross section and in Fig. 11(b) the signal efficiency. We employ the cuts developed in Sec. IV D. The cutflow at $\sqrt{s} = 14$ TeV for the benchmark scenarios can be found in Appendix B.

Because of the higher cms energy, the cross section is $\mathcal{O}(10)$ times larger than for $\sqrt{s} = 7$ TeV; cf. Fig. 9(a). For instance, at $M_{1/2} = 400$ GeV (500 GeV), the signal cross section at $\sqrt{s} = 14$ TeV is now 7.2 pb^{-1} (1.7 pb^{-1}). Furthermore, the signal, i.e. sparticle pair production, is now always dominated by sparton pair production; cf. also Table V.

The signal efficiency at $\sqrt{s} = 14$ TeV is slightly improved compared to $\sqrt{s} = 7$ TeV. Because of the enhanced sparton pair production cross section, more signal events pass our cut on the jet multiplicity, $N_{\text{jet}} \geq 2$; cf. also Appendix B. We now obtain a signal efficiency of about 51% (compared to 46% at $\sqrt{s} = 7$ TeV) for the benchmark point BE1. Most of the parameter points in Fig. 11(b) exhibit a signal efficiency in the range of 40–60%. For the scenarios with low mass difference between the $\tilde{\chi}_1^0$ and the \tilde{e}_R LSP, $\Delta M \lesssim 2.5$ GeV, the signal efficiency is reduced to around 15–25%. As for $\sqrt{s} = 7$ TeV, the signal efficiency decreases at very large values of $M_{1/2}$ because of the increasing sparton mass and the reduced sparton pair production cross section. Here, this effect slowly sets in at values $M_{1/2} \gtrsim 1100$ GeV, i.e. for scenarios with squark and gluino masses around 2 TeV. However, even at

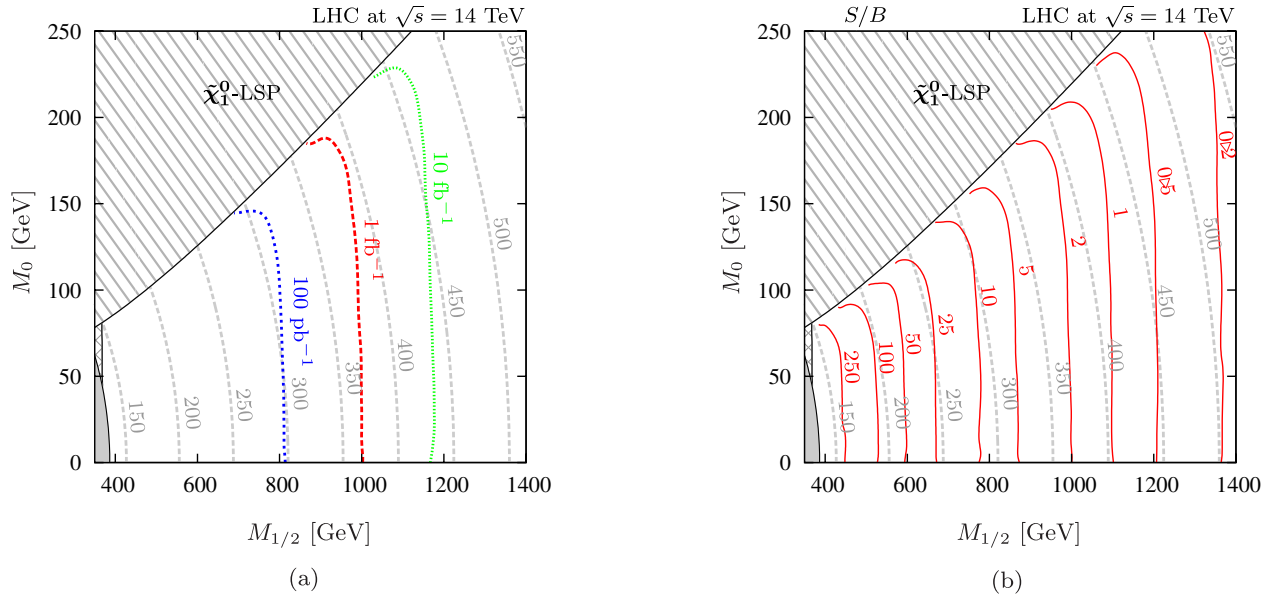


FIG. 12 (color online). Same as Fig. 10, but for a cms energy of $\sqrt{s} = 14$ TeV. In (a) we give the minimal required integrated luminosity for a discovery; cf. Eq. (16). We show contours for 100 pb $^{-1}$ ([blue] dotted line), 1 fb $^{-1}$ ([red] dashed line), and 10 fb $^{-1}$ ([green] fine dotted line). In (b) we show contours for the signal-to-background ratio, S/B ([red] solid curves).

$M_{1/2} = 1100$ GeV, sparton pair production still forms half of the total signal cross section.

We show in Fig. 12(a) the discovery potential for the LHC at $\sqrt{s} = 14$ TeV. We give the discovery reach for integrated luminosities of 100 pb $^{-1}$, 1 fb $^{-1}$ and 10 fb $^{-1}$, respectively. Our cuts of Sec. IV D reduce the SM background to 64.7 ± 7.2 events for an integrated luminosity of 10 fb $^{-1}$; see Table X. We observe that scenarios with $M_{1/2} \lesssim 1$ TeV (1.15 TeV) can be discovered with 1 fb $^{-1}$ (10 fb $^{-1}$). This corresponds to squark masses of around 1.9 TeV (2.2 TeV) and LSP masses of roughly 370 GeV (450 GeV). The respective signal-to-background ratio is 2 (0.6) as can be seen in Fig. 12(b). Therefore, systematic uncertainties of the SM background estimate are still not problematic as long as the SM events can be estimated to a precision of $\mathcal{O}(10\%)$. This is a reasonable assumption after a few years of LHC running.

Note that the vast reach in $M_{1/2}$ is also due to the typically light \tilde{t}_1 which has a large production cross section. For instance, at $M_{1/2} = 525$ GeV, the \tilde{t}_1 mass is around 630 GeV and thus can still be produced numerously at the LHC at $\sqrt{s} = 7$ TeV.

We conclude that, due to the striking multilepton signature, the prospects for an early signal of B_3 mSUGRA with a $\tilde{\ell}_R$ LSP are better than for R -parity conserving mSUGRA models [51]. As soon as a signal has been established, the lepton multiplicity, the lepton flavors and especially the mass spectrum will give further information about the underlying model. The reconstruction of the mass spectrum is thus the topic of the next section.

We want to remark that, for scenarios with a low mass difference between the $\tilde{\chi}_1^0$ and the $\tilde{\ell}_R$ LSP,

$\Delta M \lesssim 2.5$ GeV, the search for like-sign dilepton final states might be a more promising approach [51,101–103]. However, a detailed analysis of these search channels is beyond the scope of this paper.

V. MASS RECONSTRUCTION

We have shown in the previous section that large regions of the B_3 mSUGRA parameter space with a $\tilde{\ell}_R$ LSP can already be tested with early LHC data. If a discovery consistent with our models has been made, the next step would be to try to determine the sparticle mass spectrum. We present now a strategy for how the sparticle masses can be reconstructed. We use the benchmark point BE2 as an example. We assume an integrated luminosity of 100 fb $^{-1}$ and a cms energy of $\sqrt{s} = 14$ TeV in order to have enough events for the mass reconstruction.

The sparticle decay chains cannot be directly reconstructed because the \tilde{e}_R LSP always decays into an invisible neutrino. Thus, we focus on the measurement of edges and thresholds of invariant mass distributions which are a function of the masses of the involved SUSY particles. Our strategy is analogous to the one that is widely used to reconstruct the mass spectrum in R -parity conserving SUSY where a stable $\tilde{\chi}_1^0$ LSP escapes detection [17,104–108].

A. The basic idea

We first discuss the general idea of the method. We assume the decay chain

$$D \rightarrow Cc \rightarrow Bbc \rightarrow Aabc, \quad (20)$$

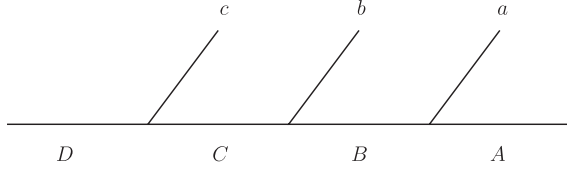


FIG. 13. Decay chain assumed for the mass reconstruction.

illustrated in Fig. 13, where the particles D , C , B , and A are massive⁹ and their masses satisfy

$$m_D > m_C > m_B > m_A. \quad (21)$$

The particles c , b and a are observable (massless) SM particles. Particle A is assumed to be invisible.

From the 4-momenta of the decay products a , b and c , we can form the invariant mass combinations m_{ba} , m_{ca} , m_{cb} and m_{cba} . The maximal (denoted “max”) and minimal (denoted “min”) endpoints of these distributions,

$$m_{ba}^{\max}, m_{ca}^{\max}, m_{cb}^{\max}, m_{cba}^{\max} \quad \text{and} \quad m_{cba}^{\min}, \quad (22)$$

are functions of the (unknown) particle masses in Eq. (21).¹⁰ The respective equations are given in Appendix C [114]. Note that m_{ba}^{\min} , m_{ca}^{\min} and m_{cb}^{\min} are always equal to zero.

A prominent application of this method is the cascade decay of a left-handed squark in R -parity conserving SUSY [17],

$$\tilde{q}_L \rightarrow q\tilde{\chi}_2^0 \rightarrow q\ell_n^\pm \tilde{\ell}^\mp \rightarrow q\ell_n^\pm \ell_f^\mp \tilde{\chi}_1^0. \quad (23)$$

Here, the $\tilde{\chi}_1^0$ LSP is stable and escapes the detector unseen. Note that, in R -parity conserving SUSY, the “near” lepton, ℓ_n , and “far” lepton, ℓ_f , are of the same flavor and thus indistinguishable on an event-by-event basis. In our scenarios this is not necessarily the case, as shown below.

For our $\tilde{\ell}_R$ LSP scenarios, we investigate the decay chain of a right-handed squark, i.e. we assume

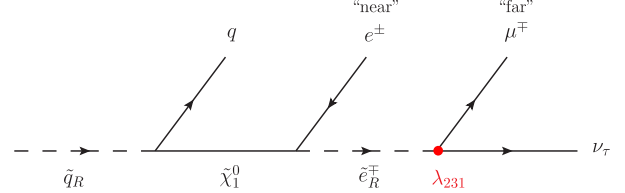
$$\tilde{q}_R \rightarrow q\tilde{\chi}_1^0 \rightarrow q\ell^\pm \tilde{\ell}_R^\mp \rightarrow q\ell^\pm \ell'^\mp \nu. \quad (24)$$

The LSP decays into a charged lepton ℓ' and a neutrino, where the flavor depends on the dominant Λ coupling; cf. Table III. In contrast to the R -parity conserving scenarios, we can actually distinguish the near and far lepton if we have $\Lambda \in \{\lambda_{231}, \lambda_{132}\}$. The $\tilde{\ell}_R$ LSP then decays into a charged lepton of different flavor from its own. However, we still have to deal with combinatorial backgrounds because we might wrongly combine leptons (and jets) from different cascades within the same event.

In the following, we demonstrate our method for the \tilde{e}_R LSP benchmark model BE2 ($\lambda_{231}|_{\text{GUT}} \neq 0$); cf. Table II. We focus on the case where the \tilde{e}_R LSP decays into a muon

⁹Particle A does not necessarily need to be massive. In our case, it is a massless neutrino.

¹⁰Another variable which can in principle be used for our scenarios is the Stranverse mass, m_{T2} [107,109–113].


FIG. 14 (color online). Relevant decay chain of a right-handed squark, Eq. (24), for the benchmark scenario BE2. The R -parity violating decay of the \tilde{e}_R LSP via λ_{231} is marked with a [red] dot.

(instead of a τ) and a neutrino. On the one hand, muons are much easier to reconstruct than τ leptons. On the other hand, muon events have a higher probability to pass our cuts; cf. Sec. IV D. The relevant cascade decay, Eq. (24), is shown in Fig. 14. It yields one jet (at parton level) and two charged leptons of different flavor and opposite charge. From these objects, we can form the invariant masses $m_{e\mu}$, $m_{\mu q}$, m_{eq} and $m_{e\mu q}$.

In the mass determination, one can leave the mass of the neutrino as a free parameter. If one measures this parameter consistent with zero, it would be an important piece of information toward confirming our model. However, once the R -parity violating decay chain of Fig. 14 is experimentally verified (or assumed), the knowledge of $m_A = 0$, Eq. (21), simplifies the equations in Appendix C and reduces the number of fit parameters by one. The endpoints of the invariant mass distributions are then given by

$$(m_{e\mu}^{\max})^2 = M_{\tilde{\chi}_1^0}^2 - M_{\tilde{e}_R}^2, \quad (25a)$$

$$(m_{\mu q}^{\max})^2 = M_{\tilde{q}_R}^2 - M_{\tilde{\chi}_1^0}^2, \quad (25b)$$

$$(m_{eq}^{\max})^2 = (M_{\tilde{q}_R}^2 - M_{\tilde{\chi}_1^0}^2)(M_{\tilde{\chi}_1^0}^2 - M_{\tilde{e}_R}^2)/M_{\tilde{\chi}_1^0}^2, \quad (25c)$$

$$(m_{e\mu q}^{\max})^2 = M_{\tilde{q}_R}^2 - M_{\tilde{e}_R}^2, \quad (25d)$$

$$(m_{e\mu q}^{\min})^2 = M_{\tilde{q}_R}^2 (M_{\tilde{\chi}_1^0}^2 - M_{\tilde{e}_R}^2)/(2M_{\tilde{\chi}_1^0}^2). \quad (25e)$$

In BE2 (and more generally in most $\tilde{\ell}_R$ LSP models within B₃ mSUGRA), the (mostly right-handed) \tilde{t}_1 is much lighter than the first- and second-generation \tilde{q}_R . Therefore, we typically have two distinct squark mass scales. This enables a measurement of the \tilde{t}_1 and (first- and second-generation) \tilde{q}_R mass simultaneously, if we are able to separate \tilde{t}_1 and \tilde{q}_R production from each other.¹¹ This is possible, as we show next.

B. Event selection

For the mass reconstruction, we slightly extend our cuts developed in Sec. IV D for $\sqrt{s} = 14$ TeV. Each event has to contain at least one electron and one muon with opposite charge. In order to enhance the probability of selecting the right muon, i.e. the μ from the \tilde{e}_R LSP decay, we require a minimal transverse momentum of the muon of

¹¹From now on, \tilde{q}_R stands only for right-handed squarks of the first and second generation.

$p_T^\mu \geq 25$ GeV. We then construct all possible opposite-sign-different-flavor (OSDF) dilepton invariant masses, $m_{e\mu}$, of electrons and muons (with $p_T^\mu \geq 25$ GeV). In order to reduce combinatorial backgrounds, we subtract the dilepton invariant mass distribution of the same-sign-different-flavor (SSDF) leptons. Note that this also suppresses (R -parity conserving) SUSY background processes, where the charges of the selected leptons are uncorrelated, because of an intermediate Majorana particle, i.e. a neutralino. For example, SUSY decay chains involving the cascade $\tilde{\mu}_L^- \rightarrow \mu^- \tilde{\chi}_1^0 \rightarrow \mu^- e^\pm \tilde{e}_R^\mp$ are thus suppressed.

For the invariant mass distributions containing a jet, we design further selection cuts to discriminate between \tilde{t}_1 and \tilde{q}_R events. We expect at least two b jets in the \tilde{t}_1 events from the top quark decays. Thus, we introduce a simple b -tagging algorithm in our simulation, assuming a b -tagging efficiency of 60% [17]. We demand two tagged b jets for the \tilde{t}_1 event candidates while we require that no b jet must be present for the \tilde{q}_R event candidates. Moreover, we use the visible effective mass, $M_{\text{eff}}^{\text{vis}}$, as a handle to discriminate between \tilde{t}_1 and \tilde{q}_R events, i.e. we impose the cuts

$$\begin{aligned} 400 \text{ GeV} &\leq M_{\text{eff}}^{\text{vis}} \leq 900 \text{ GeV} && \text{for } \tilde{t}_1 \text{ events,} \\ 900 \text{ GeV} &\leq M_{\text{eff}}^{\text{vis}} && \text{for } \tilde{q}_R \text{ events,} \end{aligned} \quad (26)$$

respectively.

For the construction of invariant mass distributions involving quarks, we consider the hardest and second hardest jet, j_1 and j_2 in each event, respectively. Because of the lighter \tilde{t}_1 mass, the jets are expected to be somewhat softer in \tilde{t}_1 events than in \tilde{q}_R events. Therefore, for BE2, we choose the following p_T selection criteria for the jets:

$$\begin{aligned} 50 \text{ GeV} &\leq p_T^{j_1} \leq 250 \text{ GeV} && \text{for } \tilde{t}_1 \text{ events,} \\ 25 \text{ GeV} &\leq p_T^{j_2} && \\ 250 \text{ GeV} &\leq p_T^{j_1} && \text{for } \tilde{q}_R \text{ events.} \\ 100 \text{ GeV} &\leq p_T^{j_2} && \end{aligned} \quad (27)$$

The invariant mass distributions $m_{e\mu q}$, m_{eq} , and $m_{\mu q}$ are now constructed as follows:

- (i) $m_{e\mu q}$: We take the invariant masses of the opposite sign electron and muon with j_1 and j_2 . The smaller (larger) value is taken for the edge (threshold) distribution. Note that we repeat this procedure for *all possible* combinations of electrons and muons. For the threshold distribution, we demand in addition the dilepton invariant mass to lie within $m_{e\mu}^{\text{max}}/\sqrt{2} \leq m_{e\mu} \leq m_{e\mu}^{\text{max}}$, corresponding to the subset of events in which the angle between the two leptons (in the center of mass frame of the \tilde{e}_R LSP) is greater than $\pi/2$ [104]. In the edge distribution, we require $m_{e\mu} \leq m_{e\mu}^{\text{max}}$ and employ SSDF subtraction to reduce the combinatorial background.

- (ii) m_{eq} ($m_{\mu q}$): We construct the invariant mass of all selected electrons (muons with $p_T^\mu \geq 25$ GeV) with j_1 and j_2 and take the lower value.¹² Furthermore, we require $m_{e\mu} \leq m_{e\mu}^{\text{max}}$.

For these constructions, the dilepton invariant mass edge, $m_{e\mu}^{\text{max}}$, must have already been fitted. We use the true value of the dilepton edge because it can be reconstructed to a very high precision; cf. Sec. V C 1.

C. Results

We now show our results for BE2 for an integrated luminosity of 100 fb^{-1} at $\sqrt{s} = 14 \text{ TeV}$. We assume that the SM background can be reduced to a negligible amount (cf. Appendix B) and present only the invariant mass distributions for the SUSY sample, i.e. pair production of all SUSY particles. We employ the cuts described in the last section. We give a rough estimate of how accurately the kinematic endpoints may be determined and investigate whether the result can be biased due to SUSY background processes or systematic effects of the event selection. Our discussion should be understood as a proof-of-principle of the feasibility of the method. It should be followed by a detailed experimental study including a detector simulation.

1. Dilepton invariant mass

We show in Fig. 15 the SSDF subtracted dilepton invariant mass distribution, $m_{e\mu}$. According to Eq. (25a), we expect for the cascade decay in Fig. 14 a dilepton edge at 51.7 GeV [dashed vertical line in Fig. 15(a)]. The observed edge quite accurately matches the expected value and should already be observable with a few fb^{-1} if the underlying new physics model is similar to BE2.

For an invariant mass below the dilepton edge, the distribution shape slightly deviates from the (expected) triangular shape. This is because the \tilde{e}_R LSP can also decay into a neutrino and a τ lepton (see Table III), which then decays into a muon and neutrinos. In this case, the muon carries only a fraction of the τ lepton p_T , and we obtain an on-average lower $m_{e\mu}$ value compared to the LSP decay $\tilde{e}_R \rightarrow \mu \nu_\tau$.

We observe another small edge at about 70 GeV. These events stem from the decay of a left-handed smuon, i.e. $\tilde{\mu}_L^\pm \rightarrow \mu^\pm \tilde{\chi}_1^0 \rightarrow \mu^\pm e^\mp \tilde{e}_R$; cf. Table VIII. The true endpoint is 70.7 GeV.

Furthermore, as shown in Fig. 15(b), we have a sharp peak at 309.8 GeV in the dilepton invariant mass distribution. Here, the mass of the tau sneutrino, $\tilde{\nu}_\tau$, is fully reconstructed. It decays via the R -parity violating decay $\tilde{\nu}_\tau \rightarrow e^- \mu^+$ with a branching ratio of 12%; see Table VIII.

¹²Here, we make use of the fact that we can distinguish the near and far lepton. However, we have checked that the model-independent construction of the variables $m_{\ell q(\text{near/far})}$ as proposed in Ref. [104] leads to similar results.

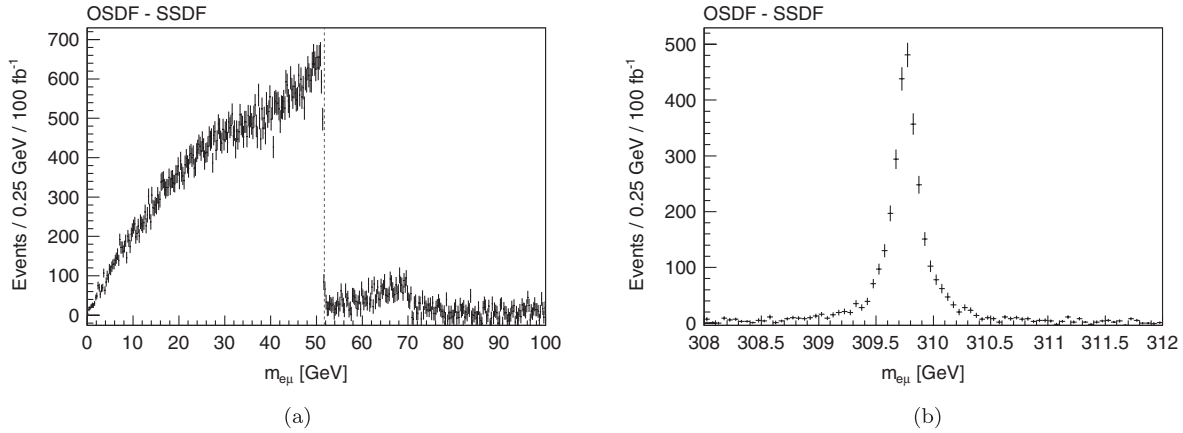


FIG. 15. Dilepton invariant mass distribution, $m_{e\mu}$, for the benchmark point BE2. The distributions are same-sign-different-flavor (SSDF) subtracted. The error bars correspond to statistical uncertainties at 100 fb^{-1} . In (a), we show the dilepton edge, $m_{e\mu}^{\max}$, Eq. (25a); the dashed vertical line gives the expected value of 51.7 GeV. In (b), we show the mass peak of the tau sneutrino, $\tilde{\nu}_\tau$, due to the R-parity violating decay $\tilde{\nu}_\tau \rightarrow e\mu$; the true mass is $M_{\tilde{\nu}_\tau} = 309.8 \text{ GeV}$; cf. Table VIII.

Analogously, we also expect a mass peak in the $e\tau$ invariant mass distribution from the respective muon sneutrino decay. However, the observation of this peak requires the reconstruction of the τ lepton momentum, which is beyond the scope of this paper. The sneutrino mass peaks are expected to be observable with only a few fb^{-1} of data and are thus a smoking gun for our scenarios.

2. Dilepton plus jet invariant mass

We show in Fig. 16 the dilepton plus jet invariant mass distribution, $m_{e\mu q}$, to obtain the kinematic edge for the \tilde{q}_R event [Fig. 16(a)] and \tilde{t}_1 event [Fig. 16(b)] selection; cf. Sec. VB. Recall that we employ different selection criteria to obtain the edge and the threshold of the $m_{e\mu q}$ distribution; see the end of Sec. VB for details.

According to Eq. (25d) and Table VIII, we expect the edge in Fig. 16(a) [Fig. 16(b)] to lie at 925 GeV [410 GeV]. For the \tilde{q}_R event selection, this is the case as can be seen¹³ by the dashed vertical line in Fig. 16(a).

In contrast, in the \tilde{t}_1 event selection, the identification of the endpoint [dashed vertical line in Fig. 16(b)] is more difficult. The observable edge is smeared to higher values. On the one hand, cascade decays of *heavier* squarks and gluinos can leak into the \tilde{t}_1 event selection. On the other hand, the distribution flattens out as it approaches the nominal endpoint, because the jet (from t decay) carries only a fraction of the t quark p_T . Moreover, the cut imposed on the jet transverse momentum, $p_T < 250 \text{ GeV}$, Eq. (27), tends to reject events at high $m_{e\mu q}$ values. Therefore, the endpoint tends to be smeared. However, the intersection of the x-axis with a linear fit on the right flank of Fig. 16(b) would still provide a quite good estimate of the true edge. Such a procedure is also employed for the

¹³The endpoint values are usually determined by employing straight line fits, see e.g. Ref. [17,104–106].

mass reconstruction of R-parity conserving models [17,104–107].

In Fig. 17, we present the $m_{e\mu q}$ threshold-distribution for the \tilde{q}_R [Fig. 17(a)] and \tilde{t}_1 event [Fig. 17(b)] selection. In Fig. 17(a), we observe an edge slightly below the expected threshold of 181 GeV (dashed vertical line). This shift toward lower values is due mainly to final state radiation of the quark from \tilde{q}_R decay [114], i.e. the reconstructed jet is less energetic than the original quark. This is not surprising because we use a relatively small radius, $\Delta R = 0.4$, for the jet algorithm; cf. Sec. IV B.

In general, the $m_{e\mu q}$ threshold value is set by the lightest squark. Therefore, events in Fig. 17(a) with values far below the endpoint at 181 GeV usually contain third-generation squarks. These events can leak into the \tilde{q}_R event selection when the b quarks are not tagged.

For the \tilde{t}_1 event selection, Fig. 17(b), the observed $m_{e\mu q}$ threshold matches quite accurately the expected value of 86 GeV (dashed vertical line). Although we note that detector effects, especially jet mismeasurements, are expected to smear the thresholds and edges, this lies beyond the scope of this paper.

3. Lepton plus jet invariant masses

We now discuss the invariant mass distributions formed by one charged lepton and a jet, i.e. m_{eq} and $m_{\mu q}$. For these invariant masses, we generally have larger SUSY backgrounds (compared to the dilepton and dilepton plus jet invariant mass distributions), because we cannot employ SSDF subtraction.

The electron-jet invariant mass distributions, m_{eq} , are presented in Fig. 18. In the \tilde{q}_R event selection [Fig. 18(a)], we observe an edge near the expected endpoint of 251 GeV (dashed vertical line). In contrast, in the \tilde{t}_1 event selection [Fig. 18(b)], the endpoint, which is expected to lie at 111 GeV, cannot be easily identified.

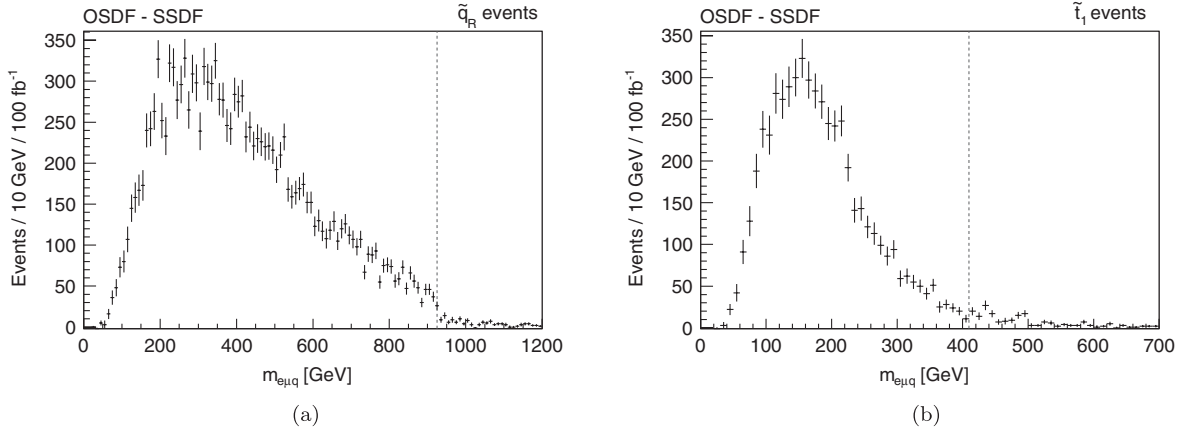


FIG. 16. Dilepton plus jet invariant mass distributions, $m_{e\mu q}$, for the kinematic edge (a) for the \tilde{q}_R event selection and (b) for the \tilde{t}_1 event selection. For the \tilde{q}_R event selection [\tilde{t}_1 event selection], the dashed vertical line in (a) [(b)] gives the expected value of 925 GeV [410 GeV]; cf. Eq. (25d). The distributions are SSDF subtracted. The errors correspond to statistical uncertainties at 100 fb^{-1} .

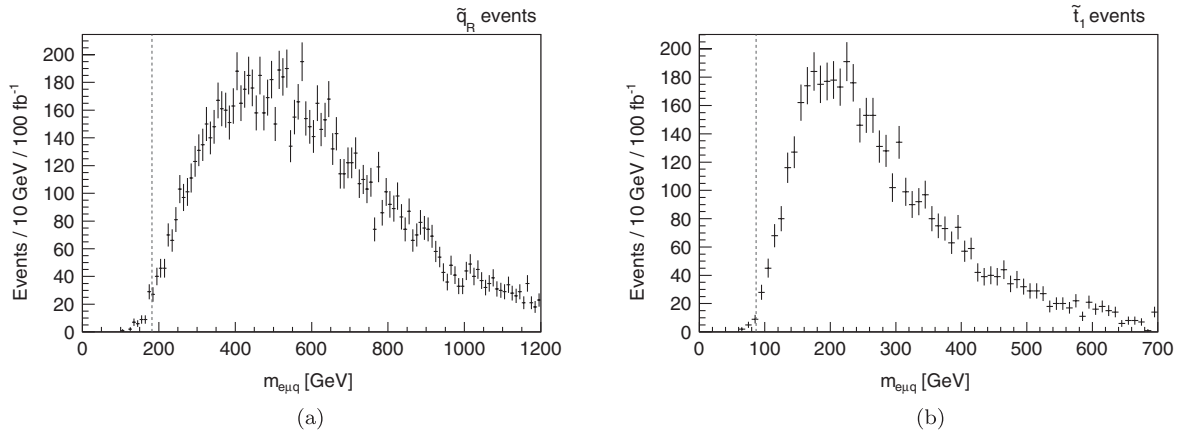


FIG. 17. Dilepton plus jet invariant mass threshold distributions, $m_{e\mu q}$, for the kinematic threshold for (a) the \tilde{q}_R event selection and (b) the \tilde{t}_1 event selection. For the \tilde{q}_R event selection [\tilde{t}_1 event selection], the dashed vertical line in (a) [(b)] gives the expected value of 181 GeV [86 GeV]; cf. Eq. (25e). The errors correspond to statistical uncertainties at 100 fb^{-1} .

The jet used for Fig. 18(b) usually carries only a fraction of the t quark momentum reducing the invariant mass. In addition, the \tilde{t}_1 cascade decay

$$\tilde{t}_1 \xrightarrow{28.1\%} b\tilde{\chi}_1^+ \xrightarrow{19.9\%} b\mu^+ \tilde{\nu}_\mu \xrightarrow{14.2\%} b\mu^+ e^- \tau^+, \quad (28)$$

possesses an endpoint at 267 GeV in $m_{e\mu q}$ which produces events beyond the expected endpoint. As a result, a measurement of the 111 GeV endpoint will be difficult.

In Fig. 19 we show the muon-jet invariant mass distributions for the \tilde{q}_R event [Fig. 19(a)] and \tilde{t}_1 event [Fig. 19(b)] selection. Assuming the \tilde{q}_R cascade decay of Fig. 14, the $m_{\mu q}$ distribution, Fig. 19(a), has an expected endpoint at 921 GeV, Eq. (25b). We can clearly observe an endpoint in Fig. 19(a). However, in general, it might be slightly underestimated, due to final state radiation of the quark from squark decay.

In the \tilde{t}_1 event selection, the endpoint is again more difficult to observe; cf. Fig. 19(b). For $m_{\mu q} \gtrsim 300 \text{ GeV}$,

the distribution approaches the endpoint with a very flat slope. Thus, the determination of the endpoint requires high statistics. Moreover, we have background events beyond the endpoint from heavier squark cascade decays or combinations with a jet from a decaying gluino.

We conclude that the standard method that is used to reconstruct sparticle masses in R -parity conserving SUSY also works very well for our $\tilde{\ell}_R$ LSP models, where the LSP decays semi-invisibly.¹⁴ We therefore expect that most of the SUSY masses in our model can be reconstructed with a similar precision as in R -parity conserving models [17,104–108], i.e. we expect for our benchmark model a relative error of about 10% or less. We have not calculated the sparticle masses from the kinematic edges because, for a reliable estimate of the errors, one has to include detector effects. However, this lies beyond the scope of this work.

¹⁴In addition, we will also observe a clear resonance peak from the R -parity violating sneutrino decay; cf. Fig. 15(b).

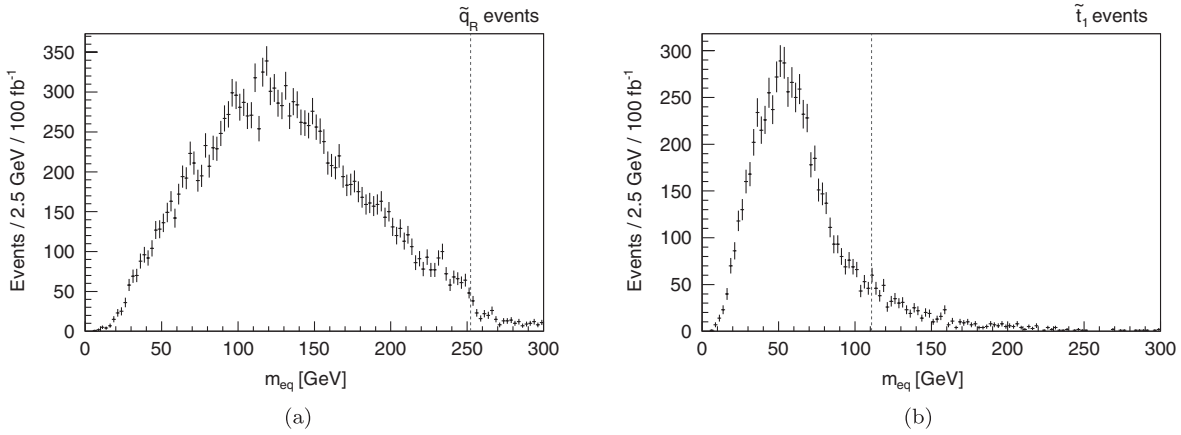


FIG. 18. Electron plus jet invariant mass distribution, m_{eq} , for (a) the \tilde{q}_R event selection and for (b) the \tilde{t}_1 event selection. The errors correspond to statistical uncertainties at 100 fb^{-1} . For the \tilde{q}_R event selection [\tilde{t}_1 event selection], the dashed vertical line in (a) [(b)] gives the expected value of 251 GeV [111 GeV]; cf. Eq. (25c).

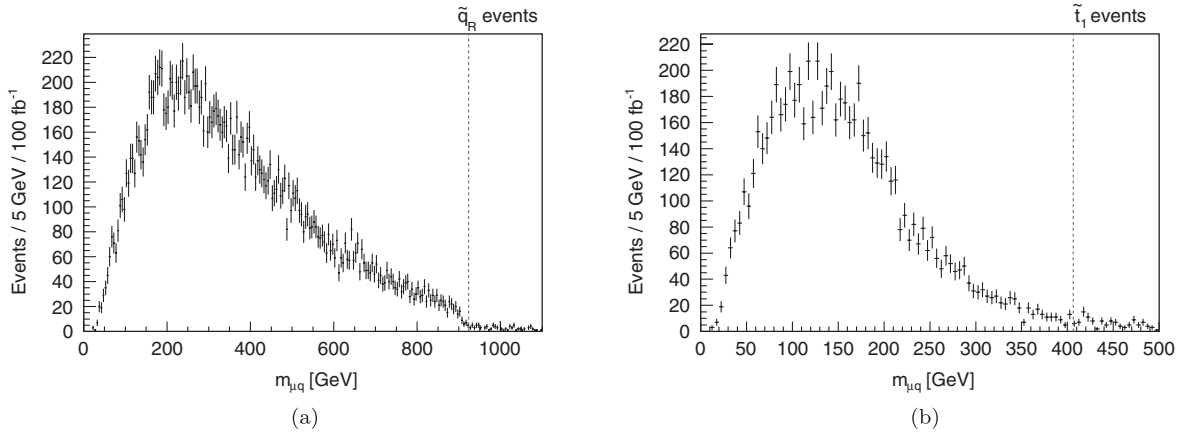


FIG. 19. Muon plus jet invariant mass distribution, $m_{\mu q}$, for (a) the \tilde{q}_R event selection and (b) the \tilde{t}_1 event selection. The errors correspond to statistical uncertainties at 100 fb^{-1} . For the \tilde{q}_R event selection [\tilde{t}_1 event selection], the dashed vertical line in (a) [(b)] gives the expected value of 921 GeV [406 GeV]; cf. Eq. (25b).

VI. SUMMARY AND CONCLUSION

If R -parity is violated, new lepton-number violating interactions can significantly alter the renormalization group running of SUSY particle masses if the coupling strength is of the order of the gauge couplings. Within the framework of the B_3 mSUGRA model, we showed that a selectron and smuon LSP can arise in large regions of the SUSY parameter space (cf. Fig. 3) if a nonvanishing lepton-number violating coupling λ_{ijk} with $k = 1, 2$ is present at the GUT scale; see Table I for a list of all allowed couplings.

The selectron or smuon LSP decays mainly into a charged lepton and a neutrino. Additional charged leptons are usually produced via cascade decays of heavier sparticles into the LSP. Keeping in mind that sparticles at the LHC are mostly produced in pairs, we end up with roughly four charged leptons in each event at parton level. Furthermore, two or more jets are expected from decays

of strongly interacting SUSY particles. Table III gives an overview of the expected LHC signatures.

Based on these facts, we developed in Sec. IV a dedicated tripleton search for our SUSY scenarios. We found that demanding three charged leptons and two jets in the final state as well as employing a Z -veto and a lower cut on the visible effective mass is sufficient to obtain a good signal-to-background ratio. For example, for an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$, only approximately three SM events survive, whereas the number of SUSY events passing our cuts can be of $\mathcal{O}(10\text{--}100)$; cf. Table VI.

We found within the B_3 mSUGRA model that a signal of scenarios with squark (selectron or smuon LSP) masses up to 1.2 TeV (230 GeV) can be discovered with an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$, thus exceeding the discovery reach of R -parity conserving models. Our scenarios are therefore well suited for an analysis with early LHC data. Going to a cms energy of $\sqrt{s} = 14 \text{ TeV}$

TABLE VII. Branching ratios (BRs) and sparticle masses for the benchmark scenario BE1; see Table II. BRs smaller than 1% are neglected. R -parity violating decays and masses which are reduced by more than 5 GeV (compared to the R -parity conserving case) are shown in boldface.

Mass (in GeV)	Channel	BR	Channel	BR	
\tilde{e}_R^-	168.7	$\mu^- \nu_\tau$	50%	$\tau^- \nu_\mu$	50%
$\tilde{\tau}_1^-$	170.0	$e^- \bar{\nu}_\mu$	100%		
$\tilde{\mu}_R^-$	183.6	$\tilde{e}_R^+ e^- \mu^-$	34.6%	$\tilde{e}_R^+ e^- \mu^-$	28.3%
		$\tilde{\tau}_1^+ \tau^- \mu^-$	20.4%	$\tilde{\tau}_1^+ \tau^+ \mu^-$	16.7%
$\tilde{\chi}_1^0$	195.7	$\tilde{e}_R^- e^+$	23.8%	$\tilde{e}_R^+ e^-$	23.8%
		$\tilde{\tau}_1^- \tau^+$	21.0%	$\tilde{\tau}_1^+ \tau^-$	21.0%
		$\tilde{\mu}_R^- \mu^+$	5.1%	$\tilde{\mu}_R^+ \mu^-$	5.1%
$\tilde{\nu}_\tau$	306.5	$\tilde{\chi}_1^0 \nu_\tau$	60.2%	$W^+ \tilde{\tau}_1^-$	28.4%
		$e^- \mu^+$	11.4%		
$\tilde{\nu}_\mu$	309.4	$\tilde{\chi}_1^0 \nu_\mu$	84.4%	$e^- \tau^+$	15.6%
$\tilde{\nu}_e$	313.5	$\tilde{\chi}_1^0 \nu_e$	100%		
$\tilde{\tau}_2^-$	318.4	$\tilde{\chi}_1^0 \tau^-$	59.0%	$H^0 \tilde{\tau}_1^-$	16.5%
		$Z^0 \tilde{\tau}_1^-$	14.1%	$e^- \bar{\nu}_\mu$	10.4%
$\tilde{\mu}_L^-$	318.7	$\tilde{\chi}_1^0 \mu^-$	84.1%	$e^- \bar{\nu}_\tau$	15.9%
\tilde{e}_L^-	322.8	$\tilde{\chi}_1^0 e^-$	100%		
$\tilde{\chi}_2^0$	372.0	$\tilde{\nu}_\tau \nu_\tau$	10.0%	$\tilde{\nu}_\tau \bar{\nu}_\tau$	10.0%
		$\tilde{\nu}_\mu \nu_\mu$	9.2%	$\tilde{\nu}_\mu \bar{\nu}_\mu$	9.2%
		$\tilde{\nu}_e \nu_e$	8.1%	$\tilde{\nu}_e \bar{\nu}_e$	8.1%
		$\tilde{\mu}_L^- \mu^+$	7.2%	$\tilde{\mu}_L^+ \mu^-$	7.2%
		$\tilde{\tau}_2^- \tau^+$	7.1%	$\tilde{\tau}_2^+ \tau^-$	7.1%
		$\tilde{e}_L^- e^+$	6.2%	$\tilde{e}_L^+ e^-$	6.2%
		$\tilde{\tau}_1^- \tau^+$	1.6%	$\tilde{\tau}_1^+ \tau^-$	1.6%
$\tilde{\chi}_1^-$	372.0	$\tilde{\nu}_\tau \tau^-$	20.6%	$\tilde{\nu}_\mu \mu^-$	19.0%
		$\tilde{\nu}_e e^-$	16.8%	$\tilde{\mu}_L^- \bar{\nu}_\mu$	13.9%
		$\tilde{\tau}_2^- \bar{\nu}_\tau$	13.7%	$\tilde{e}_L^- \bar{\nu}_e$	12.0%
		$\tilde{\tau}_1^- \bar{\nu}_\tau$	3.1%		
\tilde{t}_1	531.1	$\tilde{\chi}_1^0 t$	62.2%	$\tilde{\chi}_1^+ b$	37.8%
\tilde{b}_1	847.3	$W^- \tilde{t}_1$	71.5%	$\tilde{\chi}_1^- t$	17.5%
		$\tilde{\chi}_2^0 b$	10.4%		
$\tilde{\chi}_3^0$	898.0	$\tilde{t}_1 \bar{t}$	19.7%	$\tilde{t}_1^* t$	19.7%
		$\tilde{\chi}_1^+ W^+$	18.4%	$\tilde{\chi}_1^+ W^-$	18.4%
		$\tilde{\chi}_2^0 Z^0$	16.5%	$\tilde{\chi}_1^0 Z^0$	4.8%
		$\tilde{\chi}_2^0 H^0$	1.2%		
$\tilde{\chi}_2^-$	906.0	$\tilde{t}_1^* b$	47.6%	$\tilde{\chi}_2^0 W^-$	15.9%
		$\tilde{\chi}_1^- Z^0$	15.4%	$\tilde{\chi}_1^- H^0$	14.6%
		$\tilde{\chi}_1^0 W^-$	4.2%		
$\tilde{\chi}_4^0$	906.4	$\tilde{t}_1 \bar{t}$	29.6%	$\tilde{t}_1^* t$	29.6%
		$\tilde{\chi}_1^+ W^+$	12.1%	$\tilde{\chi}_1^+ W^-$	12.1%
		$\tilde{\chi}_2^0 H^0$	10.3%	$\tilde{\chi}_1^0 H^0$	2.9%
\tilde{t}_2	919.4	$Z^0 \tilde{t}_1$	49.1%	$H^0 \tilde{t}_1$	24.6%
		$\tilde{\chi}_1^+ b$	17.3%	$\tilde{\chi}_2^0 t$	7.6%
		$\tilde{\chi}_1^0 t$	1.5%		
\tilde{b}_2	959.5	$\tilde{\chi}_1^0 b$	67.0%	$W^- \tilde{t}_1$	28.9%
		$\tilde{\chi}_1^- t$	2.1%	$\tilde{\chi}_2^0 b$	1.2%

TABLE VII. (Continued)

Mass (in GeV)	Channel	BR	Channel	BR	
$\tilde{d}_R(\tilde{s}_R)$	962.3	$\tilde{\chi}_1^0 d(s)$	100%		
$\tilde{u}_R(\tilde{c}_R)$	965	$\tilde{\chi}_1^0 u(c)$	100%		
$\tilde{u}_L(\tilde{c}_L)$	1001.8	$\tilde{\chi}_1^+ d(s)$	65.9%	$\tilde{\chi}_2^0 u(c)$	32.9%
		$\tilde{\chi}_1^0 u(c)$	1.2%		
$\tilde{d}_L(\tilde{s}_L)$	1004.7	$\tilde{\chi}_1^- u(c)$	65.5%	$\tilde{\chi}_2^0 d(s)$	32.8%
		$\tilde{\chi}_1^0 d(s)$	1.7%		
\tilde{g}	1093.7	$\tilde{t}_1 \bar{t}$	20.9%	$\tilde{t}_1^* t$	20.9%
		$\tilde{b}_1 \bar{b}$	8.5%	$\tilde{b}_1^* b$	8.5%
		$\tilde{b}_2 \bar{b}$	2.9%	$\tilde{b}_2^* b$	2.9%
		$\tilde{d}_R \bar{d}(\tilde{s}_R \bar{s})$	2.7%	$\tilde{d}_R^* d(\tilde{s}_R^* s)$	2.7%
		$\tilde{u}_R \bar{u}(\tilde{c}_R \bar{c})$	2.6%	$\tilde{u}_R^* u(\tilde{c}_R^* c)$	2.6%
		$\tilde{t}_2 \bar{t}$	1.6%	$\tilde{t}_2^* t$	1.6%
		$\tilde{u}_L \bar{u}(\tilde{c}_L \bar{c})$	1.4%	$\tilde{u}_L^* u(\tilde{c}_L^* c)$	1.4%
		$\tilde{d}_L \bar{d}(\tilde{s}_L \bar{s})$	1.3%	$\tilde{d}_L^* d(\tilde{s}_L^* s)$	1.3%

and assuming an integrated luminosity of 10 fb^{-1} allows a discovery of 2.2 TeV (450 GeV) squarks (selectron and smuon LSPs).

After a discovery consistent with our models has been made, a next step would be the reconstruction of the SUSY mass spectrum. Unfortunately, although the LSPs decay, a direct mass reconstruction is often not possible [see Fig. 15(b) for an exception], because (invisible) neutrinos are always part of the LSP decays. We therefore proposed in Sec. V a method relying on the measurement of kinematic edges of invariant mass distributions. This method is analogous to the one usually used for R -parity conserving models, although different SUSY particles are involved in the decay chain. For example, the neutrino from the LSP decay in our models plays the role of the lightest neutralino in R -parity conserving models. We also showed that decay chains from heavier (first- and second-generation) squarks can be distinguished from those of the lighter (third-generation) top squarks. Therefore, a measurement of both squark mass scales is possible.

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APPENDIX A: PROPERTIES OF THE BENCHMARK MODELS

We show in Tables VII, VIII, and IX the mass spectra and the dominant decays of the supersymmetric particles of the

TABLE VIII. Same as Table VII, but for the benchmark scenario BE2.

Mass (in GeV)	Channel	BR	Channel	BR
\tilde{e}_R^-	182.3	$\mu^- \nu_\tau$ 50%	$\tau^- \nu_\mu$ 50%	
$\tilde{\tau}_1^-$	189.0	$\tilde{e}_R^+ e^- \tau^-$ 50.2%	$\tilde{e}_R^- e^+ \tau^-$ 49.5%	
$\tilde{\chi}_1^0$	189.5	$\tilde{e}_R^- e^+$ 50%	$\tilde{e}_R^+ e^-$ 50%	
$\tilde{\mu}_R^-$	199.0	$\tilde{\chi}_1^0 \mu^-$ 100%		
$\tilde{\nu}_\tau$	309.8	$\tilde{\chi}_1^0 \nu_\tau$ 71.0% $e^- \mu^+$ 12.0%	$W^+ \tilde{\tau}_1^-$ 17.0%	
$\tilde{\nu}_\mu$	312.0	$\tilde{\chi}_1^0 \nu_\mu$ 85.8%	$e^- \tau^+$ 14.2%	
$\tilde{\nu}_e$	317.0	$\tilde{\chi}_1^0 \nu_e$ 100%		
$\tilde{\tau}_2^-$	320.8	$\tilde{\chi}_1^0 \tau^-$ 69.9% $H^0 \tilde{\tau}_1^-$ 10.2%	$e^- \tilde{\nu}_\mu$ 11.3% $Z^0 \tilde{\tau}_1^-$ 8.6%	
$\tilde{\mu}_L^-$	320.8	$\tilde{\chi}_1^0 \mu^-$ 85.2%	$e^- \tilde{\nu}_\tau$ 14.8%	
\tilde{e}_L^-	325.7	$\tilde{\chi}_1^0 e^-$ 100%		
$\tilde{\chi}_2^0$	360.1	$\tilde{\nu}_\tau \nu_\tau$ 10.5% $\tilde{\nu}_\mu \nu_\mu$ 9.7% $\tilde{\nu}_e \nu_e$ 7.9% $\tilde{\mu}_L^- \mu^+$ 7.0% $\tilde{\tau}_2^+ \tau^+$ 6.8% $\tilde{e}_L^- e^+$ 5.4% $\tilde{\tau}_1^- \tau^+$ 2.0% $\tilde{\chi}_1^0 H^0$ 1.3%	$\tilde{\nu}_\tau \tilde{\nu}_\tau$ 10.5% $\tilde{\nu}_\mu \tilde{\nu}_\mu$ 9.7% $\tilde{\nu}_e \tilde{\nu}_e$ 7.9% $\tilde{\mu}_L^+ \mu^-$ 7.0% $\tilde{\tau}_2^+ \tau^-$ 6.8% $\tilde{e}_L^+ e^-$ 5.4% $\tilde{\tau}_1^+ \tau^-$ 2.0%	
$\tilde{\chi}_1^-$	360.2	$\tilde{\nu}_\tau \tau^-$ 21.7% $\tilde{\nu}_e e^-$ 16.3% $\tilde{\tau}_2^- \tilde{\nu}_\tau$ 13.2% $\tilde{\tau}_1^- \tilde{\nu}_\tau$ 3.8%	$\tilde{\nu}_\mu \mu^-$ 19.9% $\tilde{\mu}_L^- \tilde{\nu}_\mu$ 13.4% $\tilde{e}_L^- \tilde{\nu}_e$ 10.5% $\tilde{\chi}_1^0 W^-$ 1.3%	
\tilde{t}_1	448.3	$\tilde{\chi}_1^0 t$ 71.9%	$\tilde{\chi}_1^+ b$ 28.1%	
\tilde{b}_1	809.1	$W^- \tilde{t}_1$ 78.1% $\tilde{\chi}_2^0 b$ 8.1%	$\tilde{\chi}_1^- t$ 13.3%	
\tilde{t}_2	887.0	$Z^0 \tilde{t}_1$ 52.7% $\tilde{\chi}_1^+ b$ 14.1% $\tilde{\chi}_1^0 t$ 1.2%	$H^0 \tilde{t}_1$ 25.9% $\tilde{\chi}_2^0 t$ 6.1%	
$\tilde{\chi}_3^0$	936.7	$\tilde{t}_1 \tilde{t}$ 26.0% $\tilde{\chi}_1^- W^+$ 14.6% $\tilde{\chi}_2^0 Z^0$ 13.3%	$\tilde{t}_1^* t$ 26.0% $\tilde{\chi}_1^+ W^-$ 14.6% $\tilde{\chi}_1^0 Z^0$ 3.8%	
\tilde{b}_2	937.7	$\tilde{\chi}_1^0 b$ 67.9% $\tilde{\chi}_1^- t$ 2.7%	$W^- \tilde{t}_1$ 26.0% $\tilde{\chi}_2^0 b$ 1.5%	
$\tilde{d}_R(\tilde{s}_R)$	939.8	$\tilde{\chi}_1^0 d(s)$ 100%		
$\tilde{u}_R(\tilde{c}_R)$	942.9	$\tilde{\chi}_1^0 u(c)$ 100%		
$\tilde{\chi}_2^-$	944.5	$\tilde{t}_1^* b$ 55.6% $\tilde{\chi}_1^- Z^0$ 13.1% $\tilde{\chi}_1^0 W^-$ 3.4%	$\tilde{\chi}_2^0 W^-$ 13.5% $\tilde{\chi}_1^- H^0$ 12.4%	
$\tilde{\chi}_4^0$	945.1	$\tilde{t}_1 \tilde{t}$ 33.3% $\tilde{\chi}_1^- W^+$ 10.0% $\tilde{\chi}_2^0 H^0$ 8.5%	$\tilde{t}_1^* t$ 33.3% $\tilde{\chi}_1^+ W^-$ 10.0% $\tilde{\chi}_1^0 H^0$ 2.4%	
$\tilde{u}_L(\tilde{c}_L)$	977.6	$\tilde{\chi}_1^+ d(s)$ 65.9% $\tilde{\chi}_1^0 u(c)$ 1.2%	$\tilde{\chi}_2^0 u(c)$ 32.9%	

TABLE VIII. (Continued)

Mass (in GeV)	Channel	BR	Channel	BR
$\tilde{d}_L(\tilde{s}_L)$	980.4	$\tilde{\chi}_1^- u(c)$ 65.6% $\tilde{\chi}_1^0 d(s)$ 1.6%	$\tilde{\chi}_2^0 d(s)$ 32.8%	
\tilde{g}	1063.1	$\tilde{t}_1 \tilde{t}$ 23.0% $\tilde{b}_1 \tilde{b}$ 8.7% $\tilde{b}_2 \tilde{b}$ 2.4% $\tilde{d}_R \tilde{d}(\tilde{s}_R \tilde{s})$ 2.4% $\tilde{u}_R \tilde{u}(\tilde{c}_R \tilde{c})$ 2.3% $\tilde{t}_2 \tilde{t}$ 2.0% $\tilde{u}_L \tilde{u}(\tilde{c}_L \tilde{c})$ 1.2% $\tilde{d}_L \tilde{d}(\tilde{s}_L \tilde{s})$ 1.1%	$\tilde{t}_1^* t$ 23.0% $\tilde{b}_1^* b$ 8.7% $\tilde{b}_2^* b$ 2.4% $\tilde{d}_R^* d(\tilde{s}_R^* s)$ 2.4% $\tilde{u}_R^* u(\tilde{c}_R^* c)$ 2.3% $\tilde{t}_2^* t$ 2.0% $\tilde{u}_L^* u(\tilde{c}_L^* c)$ 1.2% $\tilde{d}_L^* d(\tilde{s}_L^* s)$ 1.1%	

benchmark points BE1, BE2 and BE3, respectively; see Table II for a definition. Sparticle masses that are reduced by more than 5 GeV (compared to the R -parity conserving case) and R -parity violating decays are marked in boldface. Note that only the masses of those sparticles which couple directly to the $L_i L_j \bar{E}_k$ operator are significantly reduced; cf. Sec. II B 1. Therefore, in our benchmark models ($\lambda_{231}|_{\text{GUT}} \neq 0$), only the \tilde{e}_R , $\tilde{\mu}_L$, $\tilde{\nu}_\mu$, $\tilde{\tau}_2$ and $\tilde{\nu}_\tau$ are affected.

These sparticles then also exhibit R -parity violating decays to SM particles via λ_{231} . For the $\tilde{\nu}_\tau$, this can lead to a striking peak in the electron-muon invariant mass distribution; cf. Fig. 15(b). In addition, the $\tilde{\tau}_1$ can also decay via the λ_{231} coupling because of its (small) left-handed component. This happens, in particular, in scenarios where the $\tilde{\tau}_1$ is the NLSP and its mass is close to the LSP mass (as in BE1, Table VII); i.e. the R -parity conserving decay into the LSP is phase-space suppressed. The \tilde{e}_R LSP can decay only via R -parity violating interactions: $\tilde{e}_R \rightarrow \mu \nu_\tau$ and $\tilde{e}_R \rightarrow \tau \nu_\mu$.

Common to all benchmark points is a rather light \tilde{t}_1 (compared to the other squarks). For all benchmark points, the \tilde{t}_1 mass is around 450–550 GeV and the other squark masses are in the range of 800 GeV–1 TeV. Because of the large top Yukawa coupling, the stop mass receives large negative contributions from RGE running, especially for a negative A_0 with a large magnitude [85,86]; see Sec. II B 2 for a similar case. Furthermore, the light stop mass is reduced by large mixing between the left- and right-handed states. As one can see in Tables VII, VIII, and IX, the (mainly right-handed) \tilde{t}_1 dominantly decays into the (binolike) $\tilde{\chi}_1^0$ and a top quark, while the decay into the (winolike) lightest chargino, $\tilde{\chi}_1^\pm$, is subdominant.

The \tilde{e}_R , $\tilde{\mu}_R$, $\tilde{\tau}_1$ and $\tilde{\chi}_1^0$ always form the lightest four sparticles in B_3 mSUGRA models with a \tilde{e}_R or $\tilde{\mu}_R$ LSP. The scenario BE1, Table VII, exhibits a $\tilde{\tau}_1$ NLSP that is nearly degenerate in mass with the \tilde{e}_R LSP. Thus, it undergoes the R -parity violating decay $\tilde{\tau}_1 \rightarrow e \nu_\mu$, yielding high- p_T electrons. The $\tilde{\mu}_R$ is the NNLSP and decays into the \tilde{e}_R or the $\tilde{\tau}_1$ via three-body decays, producing in general two low- p_T charged leptons due to the reduced

TABLE IX. Same as Table VII, but for the benchmark scenario BE3.

Mass (in GeV)	Channel	BR	Channel	BR
\tilde{e}_R^-	$\mu^- \nu_\tau$	50%	$\tau^- \nu_\mu$	50%
$\tilde{\chi}_1^0$	$\tilde{e}_R^- e^+$	50%	$\tilde{e}_R^+ e^-$	50%
$\tilde{\tau}_1^-$	$\tilde{\chi}_1^0 \tau^-$	64.5%	$e^- \bar{\nu}_\mu$	35.5%
$\tilde{\mu}_R^-$	$\tilde{\chi}_1^0 \mu^-$	100%		
$\tilde{\nu}_\tau$	$\tilde{\chi}_1^0 \nu_\tau$	73.6%	$W^+ \tilde{\tau}_1^-$	14.2%
	$e^- \mu^+$	12.2%		
$\tilde{\nu}_\mu$	$\tilde{\chi}_1^0 \nu_\mu$	86.0%	$e^- \tau^+$	14.0%
$\tilde{\nu}_e$	$\tilde{\chi}_1^0 \nu_e$	100%		
$\tilde{\mu}_L^-$	$\tilde{\chi}_1^0 \mu^-$	85.2%	$e^- \bar{\nu}_\tau$	14.8%
$\tilde{\tau}_2^-$	$\tilde{\chi}_1^0 \tau^-$	72.5%	$e^- \bar{\nu}_\mu$	11.7%
	$H^0 \tilde{\tau}_1^-$	8.5%	$Z^0 \tilde{\tau}_1^-$	7.3%
\tilde{e}_L^-	$\tilde{\chi}_1^0 e^-$	100%		
$\tilde{\chi}_2^0$	$\tilde{\nu}_\tau \nu_\tau$	10.5%	$\tilde{\nu}_\tau \bar{\nu}_\tau$	10.5%
	$\tilde{\nu}_\mu \nu_\mu$	9.7%	$\tilde{\nu}_\mu \bar{\nu}_\mu$	9.7%
	$\tilde{\nu}_e \nu_e$	8.1%	$\tilde{\nu}_e \bar{\nu}_e$	8.1%
	$\tilde{\mu}_L^- \mu^+$	6.8%	$\tilde{\mu}_L^+ \mu^-$	6.8%
	$\tilde{\tau}_2^- \tau^+$	6.6%	$\tilde{\tau}_2^+ \tau^-$	6.6%
	$\tilde{e}_L^- e^+$	5.4%	$\tilde{e}_L^+ e^-$	5.4%
	$\tilde{\tau}_1^- \tau^+$	2.0%	$\tilde{\tau}_1^+ \tau^-$	2.0%
	$\tilde{\chi}_1^0 H^0$	1.6%		
$\tilde{\chi}_1^-$	$\tilde{\nu}_\tau \tau^-$	21.7%	$\tilde{\nu}_\mu \mu^-$	20.1%
	$\tilde{\nu}_e e^-$	16.8%	$\tilde{\mu}_L^- \bar{\nu}_\mu$	13.0%
	$\tilde{\tau}_2^- \bar{\nu}_\tau$	12.7%	$\tilde{e}_L^- \bar{\nu}_e$	10.4%
	$\tilde{\tau}_1^- \bar{\nu}_\tau$	3.8%	$\tilde{\chi}_1^0 W^-$	1.6%
\tilde{t}_1	$\tilde{\chi}_1^0 t$	62.1%	$\tilde{\chi}_1^+ b$	37.9%
\tilde{b}_1	$W^- \tilde{t}_1$	73.9%	$\tilde{\chi}_1^- t$	15.9%
	$\tilde{\chi}_2^0 b$	9.7%		
\tilde{t}_2	$Z^0 \tilde{t}_1$	51.3%	$H^0 \tilde{t}_1$	24.2%
	$\tilde{\chi}_1^+ b$	16.1%	$\tilde{\chi}_2^0 t$	7.0%
	$\tilde{\chi}_1^0 t$	1.4%		
$\tilde{\chi}_3^0$	$\tilde{t}_1 \bar{t}$	22.1%	$\tilde{t}_1^* t$	22.1%
	$\tilde{\chi}_1^- W^+$	17.0%	$\tilde{\chi}_1^+ W^-$	17.0%
	$\tilde{\chi}_2^0 Z^0$	15.4%	$\tilde{\chi}_1^0 Z^0$	4.5%
	$\tilde{\chi}_2^0 H^0$	1.0%		
$\tilde{\chi}_2^-$	$\tilde{t}_1^* b$	50.8%	$\tilde{\chi}_2^0 W^-$	15.1%
	$\tilde{\chi}_1^- Z^0$	14.6%	$\tilde{\chi}_1^- H^0$	13.7%
	$\tilde{\chi}_1^0 W^-$	3.8%		
$\tilde{\chi}_4^0$	$\tilde{t}_1 \bar{t}$	31.4%	$\tilde{t}_1^* t$	31.4%
	$\tilde{\chi}_1^- W^+$	11.1%	$\tilde{\chi}_1^+ W^-$	11.1%
	$\tilde{\chi}_2^0 H^0$	9.4%	$\tilde{\chi}_1^0 H^0$	2.7%
\tilde{b}_2	$\tilde{\chi}_1^0 b$	70.5%	$W^- \tilde{t}_1$	26.0%
	$\tilde{\chi}_1^- t$	1.8%	$\tilde{\chi}_2^0 b$	1.1%
$\tilde{d}_R(\tilde{s}_R)$	$\tilde{\chi}_1^0 d(s)$	100%		
$\tilde{u}_R(\tilde{c}_R)$	$\tilde{\chi}_1^0 u(c)$	100%		

TABLE IX. (Continued)

Mass (in GeV)	Channel	BR	Channel	BR
$\tilde{u}_L(\tilde{c}_L)$	$\tilde{\chi}_1^+ d(s)$	65.9%	$\tilde{\chi}_2^0 u(c)$	33.0%
	$\tilde{\chi}_1^0 u(c)$	1.1%		
$\tilde{d}_L(\tilde{s}_L)$	$\tilde{\chi}_1^- u(c)$	65.5%	$\tilde{\chi}_2^0 d(s)$	32.7%
	$\tilde{\chi}_1^0 d(s)$	1.7%		
\tilde{g}	$\tilde{t}_1 \bar{t}$	22.6%	$\tilde{t}_1^* t$	22.6%
	$\tilde{b}_1 \bar{b}$	8.9%	$\tilde{b}_1^* b$	8.9%
	$\tilde{b}_2 \bar{b}$	2.7%	$\tilde{b}_2^* b$	2.7%
	$\tilde{d}_R \bar{d}(\tilde{s}_R \bar{s})$	2.6%	$\tilde{d}_R^* d(\tilde{s}_R^* s)$	2.6%
	$\tilde{u}_R \bar{u}(\tilde{c}_R \bar{c})$	2.5%	$\tilde{u}_R^* u(\tilde{c}_R^* c)$	2.5%
	$\tilde{u}_L \bar{u}(\tilde{c}_L \bar{c})$	1.3%	$\tilde{u}_L^* u(\tilde{c}_L^* c)$	1.3%
	$\tilde{d}_L \bar{d}(\tilde{s}_L \bar{s})$	1.2%	$\tilde{d}_L^* d(\tilde{s}_L^* s)$	1.2%

phase space. We calculate and discuss these decays in detail in Appendix D. The $\tilde{\chi}_1^0$ is the NNNLSP. Besides the decay into the \tilde{e}_R LSP and an electron (47.6%), it also decays to a sizable fraction (42.0%) into the $\tilde{\tau}_1$ NLSP and a τ lepton.

The benchmark scenario BE2, Table VIII, also has a $\tilde{\tau}_1$ NLSP. However, the $\tilde{\tau}_1$ NLSP is nearly mass degenerate with the $\tilde{\chi}_1^0$ NNLSP. Therefore, it decays exclusively via three-body decays into the \tilde{e}_R LSP, yielding a low- p_T tau lepton and an electron; cf. Appendix D. The $\tilde{\chi}_1^0$ NNLSP always decays into the \tilde{e}_R LSP and an electron.

In contrast to BE1 and BE2, the NLSP in BE3, Table IX, is the $\tilde{\chi}_1^0$ which is roughly 3 GeV heavier than the \tilde{e}_R LSP. Therefore, the electrons from the $\tilde{\chi}_1^0$ decay into the LSP are very soft. We have a $\tilde{\tau}_1$ NNLSP, which decays R -parity conserving into the $\tilde{\chi}_1^0$ and a tau as well as via R -parity violating decays into an electron and a neutrino. In both BE2 and BE3, the $\tilde{\mu}_R$ is the NNNLSP and decays exclusively into the $\tilde{\chi}_1^0$ and a muon.

The remaining sparticle mass spectra and decays look very similar to those of R -parity conserving mSUGRA [50].

APPENDIX B: CUTFLOW FOR $\sqrt{s} = 14$ TeV

We present in Table X the cutflow of the signal and SM background events for an integrated luminosity of 10 fb^{-1} at $\sqrt{s} = 14$ TeV. Although the benchmark scenarios BE1, BE2 and BE3 (see Table II) are already observable with very early LHC data (cf. Sec. IV D), we provide their expected event yields as a reference in order to compare the signal efficiencies at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV.

We apply the inclusive three-lepton analysis developed in Sec. IV D. After the three-lepton requirement (third column of Table X), the expected SM background is reduced to roughly 5110 events. Already at this stage, the expected signal event yield of the benchmark points BE1, BE2 and BE3 is overwhelming, i.e. a factor of 2–3 larger than the SM backgrounds. The signal efficiency of this first cut is the same as for the LHC at $\sqrt{s} = 7$ TeV.

TABLE X. Number of SM background and signal events after each step in the event selection at $\sqrt{s} = 14$ TeV, scaled to an integrated luminosity of 10 fb^{-1} . We provide the results for the benchmark scenarios BE1, BE2 and BE3 (Table II). The uncertainties correspond to statistical fluctuations.

Sample	Before cuts	$N_{\text{lep}} \geq 3$	$N_{\text{jet}} \geq 2$	M_{OSSF}	$M_{\text{eff}}^{\text{vis}} \geq 400 \text{ GeV}$
Top	$(5215 \pm 2) \times 10^3$	553 ± 21	491 ± 20	397 ± 19	55.9 ± 7.0
Z + jets	$(5601 \pm 2) \times 10^3$	1980 ± 41	571 ± 22	48.7 ± 6.4	2.6 ± 1.5
W + jets	$(9516 \pm 9) \times 10^2$	4.8 ± 2.0	1.6 ± 1.1	≤ 1.0	≤ 1.0
Di-boson	$(7719 \pm 8) \times 10^2$	2573 ± 17	605 ± 11	56.7 ± 4.4	6.1 ± 1.1
All SM	$(12\,540 \pm 3) \times 10^3$	5110 ± 49	1669 ± 32	503 ± 20	64.7 ± 7.2
BE1	$23\,040 \pm 47$	$14\,412 \pm 37$	$13\,925 \pm 37$	$12\,204 \pm 34$	$11\,854 \pm 34$
BE2	$30\,980 \pm 57$	$13\,910 \pm 38$	$13\,442 \pm 37$	$12\,227 \pm 36$	$11\,569 \pm 35$
BE3	$31\,160 \pm 55$	$9\,118 \pm 30$	$8\,700 \pm 29$	$7\,807 \pm 28$	$7\,533 \pm 27$

The jet multiplicity requirement (fourth column of Table X) reduces the SM background to 1670 events. It originates mainly from Zj (26%), $t\bar{t}$ (24%) and WZ (15%) production. Because sparton pair production strongly dominates the signal for all benchmark scenarios at $\sqrt{s} = 14$ TeV (cf. Table V), almost every signal event has at least two hard jets. Therefore, the signal efficiency of this cut is large, i.e. 95% or higher for all benchmark points. This is higher than for the $\sqrt{s} = 7$ TeV sample; cf. Table VI.

The Z veto (fifth column of Table X) effectively reduces the Z + jets and di-boson backgrounds, leaving only a total SM background of roughly 500 events. The background is now dominated by the $t\bar{t}$ production. The number of signal events is reduced only by roughly 10%.

Finally, after the requirement on the visible effective mass (last column of Table X), the SM background is reduced to approximately 65 events. At the same time, nearly all signal events pass this cut. The

signal-to-background ratio is now of $\mathcal{O}(100)$. This justifies neglecting the SM background events for the mass reconstruction; cf. Sec. V.

APPENDIX C: KINEMATIC ENDPOINTS OF INVARIANT MASS DISTRIBUTIONS

Assuming the cascade decay of Fig. 13, analytic formulas for the (measurable) kinematic endpoints of the two- and three-particle invariant masses, Eq. (22), can be derived [104,114]:

$$(m_{ba}^{\max})^2 = (m_C^2 - m_B^2)(m_B^2 - m_A^2)/m_B^2, \quad (\text{C1})$$

$$(m_{ca}^{\max})^2 = (m_D^2 - m_C^2)(m_B^2 - m_A^2)/m_B^2, \quad (\text{C2})$$

$$(m_{cb}^{\max})^2 = (m_D^2 - m_C^2)(m_C^2 - m_B^2)/m_C^2, \quad (\text{C3})$$

$$(m_{cba}^{\max})^2 = \begin{cases} \max \left[\frac{(m_D^2 - m_C^2)(m_C^2 - m_A^2)}{m_C^2}, \frac{(m_D^2 - m_B^2)(m_B^2 - m_A^2)}{m_B^2}, \frac{(m_D^2 m_B^2 - m_C^2 m_A^2)(m_C^2 - m_B^2)}{m_C^2 m_B^2} \right], \\ \text{or } (m_D - m_A)^2 \text{ if } m_B^2 < m_A m_D < m_C^2 \text{ and } m_A m_C^2 < m_B^2 m_D. \end{cases} \quad (\text{C4})$$

$$(m_{cba}^{\min})^2 = \left[2m_B^2(m_D^2 - m_C^2)(m_C^2 - m_A^2) + (m_D^2 + m_C^2)(m_C^2 - m_B^2)(m_B^2 - m_A^2) - (m_D^2 - m_C^2) \right. \\ \left. \times \sqrt{(m_C^2 + m_B^2)^2(m_B^2 + m_A^2)^2 - 16m_C^2 m_B^4 m_A^2} \right] / (4m_B^2 m_C^2). \quad (\text{C5})$$

These equations can be solved for the unknown particle masses in the decay chain.

APPENDIX D: THREE-BODY SLEPTON DECAYS

As we have shown in Sec. II B 3, some regions of the $\tilde{\ell}_R$ LSP parameter space exhibit the SUSY mass hierarchies

$$M_{\tilde{\ell}_R} < M_{\tilde{\tau}_1} < M_{\tilde{\ell}'_R} < M_{\tilde{\chi}_1^0} \quad (\text{D1})$$

and

$$M_{\tilde{\ell}_R} < M_{\tilde{\tau}_1} < M_{\tilde{\chi}_1^0}, \quad (\text{D2})$$

where $\tilde{\ell}'_R$ is a right-handed non-LSP slepton of the first- or second-generation. In this case, the three-body decays

$$\tilde{\ell}'_R \rightarrow \ell'^- \ell^\pm \tilde{\ell}_R^\mp, \quad \tilde{\tau}_1^- \rightarrow \tau^- \ell^\pm \tilde{\ell}_R^\mp, \quad (\text{D3})$$

can be the dominant decay modes of the $\tilde{\ell}'_R$ and $\tilde{\tau}_1$. This is the case, for example, in the benchmark scenario BE1 (BE2) for the $\tilde{\mu}_R$ ($\tilde{\tau}_1$); cf. Table VII (Table VIII).

In ISAJET7.64, which we employ to calculate the two- and three-body decays of the SUSY particles, the decays in Eq. (D3) are not implemented because, in most SUSY

scenarios, the $\tilde{\tau}_1$ is considered to be lighter than the other sleptons.

In this Appendix, we fill this gap and calculate the missing three-body slepton decays of Eq. (D3). We show the resulting squared matrix elements and give numbers for the respective branching ratios. The phase-space integration is performed numerically within ISAJET. We use the two-component spinor techniques and notation from Ref. [115] for the calculation of the matrix elements. To our knowledge, the calculation of the three-body decays is not yet given in the literature.

1. Three-body slepton decay $\tilde{\ell}'_R \rightarrow \ell' - \ell^\pm \tilde{\ell}'_R$

We now calculate the three-body slepton decays $\tilde{\ell}'_R \rightarrow \ell' - \ell^\pm \tilde{\ell}'_R$, Eq. (D3), that are mediated by a virtual neutralino.¹⁵ Because $\tilde{\ell}_R$ and $\tilde{\ell}'_R$ are sleptons of the first two generations, we can neglect contributions proportional to the (R -parity conserving) Yukawa couplings.

The relevant Feynman diagram for the decay $\tilde{\ell}'_R \rightarrow \ell' - \ell^\pm \tilde{\ell}'_R$ is shown in Fig. 20, where the momenta (p, k_1, k_2, k_3) and polarizations (λ_1, λ_2) of the particles are indicated. The neutralino mass eigenstates are denoted by $\tilde{\chi}_j^0$ with $j = 1, \dots, 4$. Using the rules and notation of Ref. [115], we obtain for the amplitude

$$i\mathcal{M} = (-ia_j^*)(-ia_j)x_2^\dagger \frac{i(p-k_1) \cdot \bar{\sigma}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} y_1, \quad (\text{D4})$$

where $a_j \equiv \sqrt{2}g'N_{j1}$, and the spinor wave functions are $y_1 = y(\vec{k}_1, \lambda_1)$ and $x_2^\dagger = x^\dagger(\vec{k}_2, \lambda_2)$. Squaring the amplitude then yields

$$|\mathcal{M}|^2 = Ax_2^\dagger(p-k_1) \cdot \bar{\sigma} y_1 y_1^\dagger(p-k_1) \cdot \bar{\sigma} x_2, \quad (\text{D5})$$

with

$$A \equiv \sum_{j,k=1}^4 \frac{|a_j|^2}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} \cdot \frac{|a_k|^2}{(p-k_1)^2 - m_{\tilde{\chi}_k^0}^2}. \quad (\text{D6})$$

Summing Eq. (D5) over the spins leads to

$$\sum_{\lambda_1, \lambda_2} |\mathcal{M}|^2 = A[m_{13}^2 m_{23}^2 - p^2 k_3^2], \quad (\text{D7})$$

where

$$m_{13}^2 \equiv (p-k_2)^2 = (k_1+k_3)^2, \quad (\text{D8})$$

$$m_{23}^2 \equiv (p-k_1)^2 = (k_2+k_3)^2. \quad (\text{D9})$$

Here, we have neglected the lepton masses, i.e. $k_1^2, k_2^2 = 0$, in Eq. (D7).

¹⁵In principle, there are also three-body decays with virtual charginos. However, these decays are negligible due to the heavier propagators. Furthermore, the right-handed sleptons cannot couple to winolike charginos.

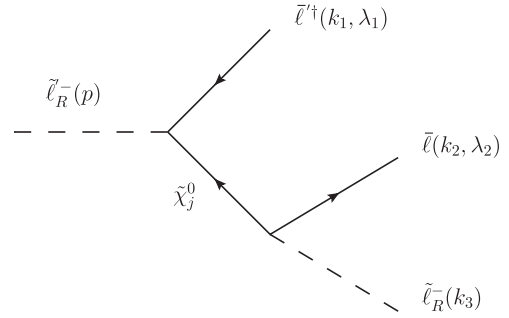


FIG. 20. Feynman diagram for the three-body slepton decay $\tilde{\ell}'_R \rightarrow \ell' - \ell^+ \tilde{\ell}'_R$.

We now turn to the decay $\tilde{\ell}'_R \rightarrow \ell' - \ell^- \tilde{\ell}'_R$. The respective Feynman diagram is given in Fig. 21. The amplitude is

$$i\mathcal{M} = (-ia_j^*)(-ia_j) \frac{im_{\tilde{\chi}_j^0}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} y_1 y_2, \quad (\text{D10})$$

which leads to the following expression for the total amplitude squared:

$$|\mathcal{M}|^2 = By_1 y_2 y_2^\dagger y_1^\dagger, \quad (\text{D11})$$

with

$$B \equiv \sum_{j,k=1}^4 \frac{|a_j|^2 m_{\tilde{\chi}_j^0}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} \cdot \frac{|a_k|^2 m_{\tilde{\chi}_k^0}}{(p-k_1)^2 - m_{\tilde{\chi}_k^0}^2}. \quad (\text{D12})$$

Summing Eq. (D10) over the spins, we arrive at

$$\sum_{\lambda_1, \lambda_2} |\mathcal{M}|^2 = B(-m_{13}^2 - m_{23}^2 + p^2 + k_3^2). \quad (\text{D13})$$

Here, the proportionality to the neutralino mass, $m_{\tilde{\chi}_j^0}$, in the amplitude is due to the helicity flip of the neutralino in Fig. 21.

2. Three-body slepton decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^\pm \tilde{\ell}'_R$

In this section, we calculate the more complicated decays $\tilde{\tau}_1^- \rightarrow \tau^- \ell^\pm \tilde{\ell}'_R$. On the one hand, the $\tilde{\tau}_1$ is a mixture of the left- and right-handed eigenstates. On the other hand,

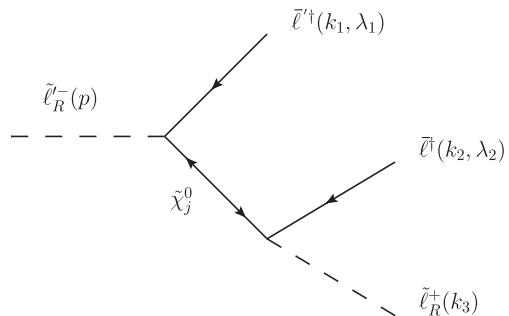
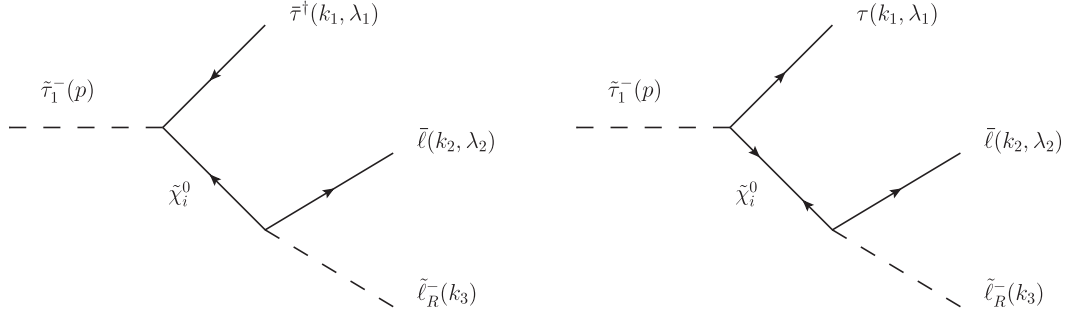


FIG. 21. Feynman diagram for the three-body slepton decay $\tilde{\ell}'_R \rightarrow \ell' - \ell^- \tilde{\ell}'_R$.


 FIG. 22. Feynman diagrams for the three-body slepton decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^+ \tilde{\ell}_R^-$.

we cannot neglect the Yukawa couplings for the third generation.

The Feynman diagrams for the decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^+ \tilde{\ell}_R^-$ are given in Fig. 22 and the respective matrix elements are [115]

$$i\mathcal{M}_I = (-ia_j^{\tilde{\tau}})(-ia_j^{\tilde{\ell}^*})x_2^\dagger \frac{i(p-k_1) \cdot \bar{\sigma}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} y_1, \quad (\text{D14})$$

$$i\mathcal{M}_{II} = (ib_j^{\tilde{\tau}})(-ia_j^{\tilde{\ell}^*}) \frac{im_{\tilde{\chi}_j^0}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} x_2^\dagger x_1^\dagger, \quad (\text{D15})$$

with

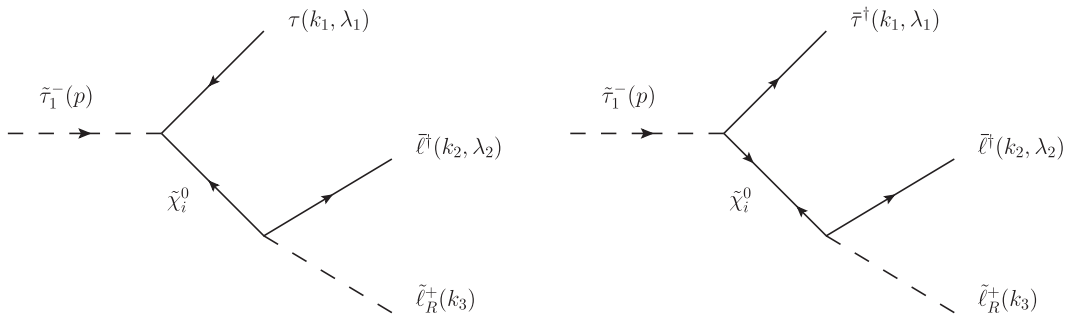
$$a_j^{\tilde{\ell}} \equiv \sqrt{2}g'N_{j1}, \quad (\text{D16})$$

$$a_j^{\tilde{\tau}} \equiv Y_\tau N_{j3} L_{\tilde{\tau}_1}^* + \sqrt{2}g'N_{j1} R_{\tilde{\tau}_1}^*, \quad (\text{D17})$$

$$b_j^{\tilde{\tau}} \equiv Y_\tau N_{j3}^* R_{\tilde{\tau}_1}^* - \frac{1}{\sqrt{2}}(gN_{j2}^* + g'N_{j1}^*)L_{\tilde{\tau}_1}^*. \quad (\text{D18})$$

The total amplitude squared is

$$\begin{aligned} |\mathcal{M}|^2 = & \sum_{j,k=1}^4 C_{jk} [a_j^{\tilde{\tau}} a_k^{\tilde{\tau}*} x_2^\dagger (p-k_1) \cdot \bar{\sigma} y_1 y_1^\dagger (p-k_1) \cdot \bar{\sigma} x_2 \\ & - [a_j^{\tilde{\tau}} b_k^{\tilde{\tau}*} m_{\tilde{\chi}_k^0} + a_k^{\tilde{\tau}} b_j^{\tilde{\tau}*} m_{\tilde{\chi}_j^0}] x_2^\dagger (p-k_1) \cdot \bar{\sigma} y_1 x_1 x_2 \\ & + b_j^{\tilde{\tau}} b_k^{\tilde{\tau}*} m_{\tilde{\chi}_j^0} m_{\tilde{\chi}_k^0} x_2^\dagger x_1^\dagger x_1 x_2], \end{aligned} \quad (\text{D19})$$


 FIG. 23. Feynman diagrams for the three-body slepton decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^- \tilde{\ell}_R^+$.

where

$$C_{jk} \equiv \frac{a_j^{\tilde{\ell}^*}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} \cdot \frac{a_k^{\tilde{\ell}}}{(p-k_1)^2 - m_{\tilde{\chi}_k^0}^2}. \quad (\text{D20})$$

Summing over the spins of the final state leptons, we obtain

$$\begin{aligned} \sum_{\lambda_1, \lambda_2} |\mathcal{M}|^2 = & \sum_{j,k=1}^4 C_{jk} \{ a_j^{\tilde{\tau}} a_k^{\tilde{\tau}*} [(-m_{23}^2 + p^2 - k_1^2)(-m_{13}^2 + p^2) \\ & - (p^2 + k_3^2 - m_{13}^2 - m_{23}^2)(p^2 - k_1^2)] \\ & - (a_j^{\tilde{\tau}} b_k^{\tilde{\tau}*} m_{\tilde{\chi}_k^0} + a_k^{\tilde{\tau}} b_j^{\tilde{\tau}*} m_{\tilde{\chi}_j^0}) m_\tau (m_{23}^2 - k_3^2) \\ & + b_j^{\tilde{\tau}} b_k^{\tilde{\tau}*} m_{\tilde{\chi}_j^0} m_{\tilde{\chi}_k^0} (p^2 + k_3^2 - m_{13}^2 - m_{23}^2) \}, \end{aligned} \quad (\text{D21})$$

where we have neglected the mass of the first- or second-generation lepton, i.e. $k_2^2 = 0$.

Finally, we calculate the related decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^- \tilde{\ell}_R^+$, where the $\tilde{\chi}_j^0$ exhibits a helicity flip; cf. Figure 23. The matrix elements for these diagrams are

$$i\mathcal{M}_I = (-ib_j^{\tilde{\tau}*})(-ia_j^{\tilde{\ell}^*})x_2^\dagger \frac{i(p-k_1) \cdot \bar{\sigma}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} y_1, \quad (\text{D22})$$

$$i\mathcal{M}_{II} = (ia_j^{\tilde{\tau}*})(-ia_j^{\tilde{\ell}^*}) \frac{im_{\tilde{\chi}_j^0}}{(p-k_1)^2 - m_{\tilde{\chi}_j^0}^2} x_2^\dagger x_1^\dagger. \quad (\text{D23})$$

The calculation of the squared amplitude is analogous to those for the decay $\tilde{\tau}_1^- \rightarrow \tau^- \ell^+ \tilde{\ell}_R^-$ if one changes the coefficients $a_j^{\tilde{\tau}} \leftrightarrow b_j^{\tilde{\tau}*}$.

3. Resulting branching ratios

We now briefly study the new three-body slepton decays for the \tilde{e}_R LSP parameter space in the $M_{1/2}$ - M_0 plane. In Fig. 24 we show the same parameter region as for the LHC discovery in Fig. 10. Dashed and dotted contour lines indicate sparticle mass differences (in GeV) that are relevant for the three-body slepton decays; see captions for more details.

We show in Fig. 24(a) the branching ratio for the decay $\tilde{\mu}_R^- \rightarrow \mu^- e^- \tilde{e}_R^+$. The dashed (dotted) contour lines

correspond to the mass difference between the $\tilde{\mu}_R$ and the \tilde{e}_R LSP ($\tilde{\chi}_1^0$). In the white region, the $\tilde{\mu}_R$ is heavier than the $\tilde{\chi}_1^0$ and decays nearly exclusively via a two-body decay into the $\tilde{\chi}_1^0$ and a muon. In the shaded [colored] region in Fig. 24(a), the $\tilde{\mu}_R$ is more than 10 GeV heavier than the \tilde{e}_R LSP. Therefore, there is enough phase space for our decay $\tilde{\mu}_R^- \rightarrow \mu^- e^- \tilde{e}_R^+$ at a significant rate. We observe that the branching ratio increases with $M_{1/2}$ and is rather insensitive to M_0 . This increase is due to the competing decay $\tilde{\mu}_R^- \rightarrow \mu^- \tau^- \tilde{\tau}_1^+$ [Fig. 24(b)] becoming relatively less important with increasing $M_{1/2}$; see the discussion below. The decay $\tilde{\mu}_R^- \rightarrow \mu^- e^+ \tilde{e}_R^-$ behaves similarly to the decay $\tilde{\mu}_R^- \rightarrow \mu^- e^- \tilde{e}_R^+$, although there are some small differences due to the different results for

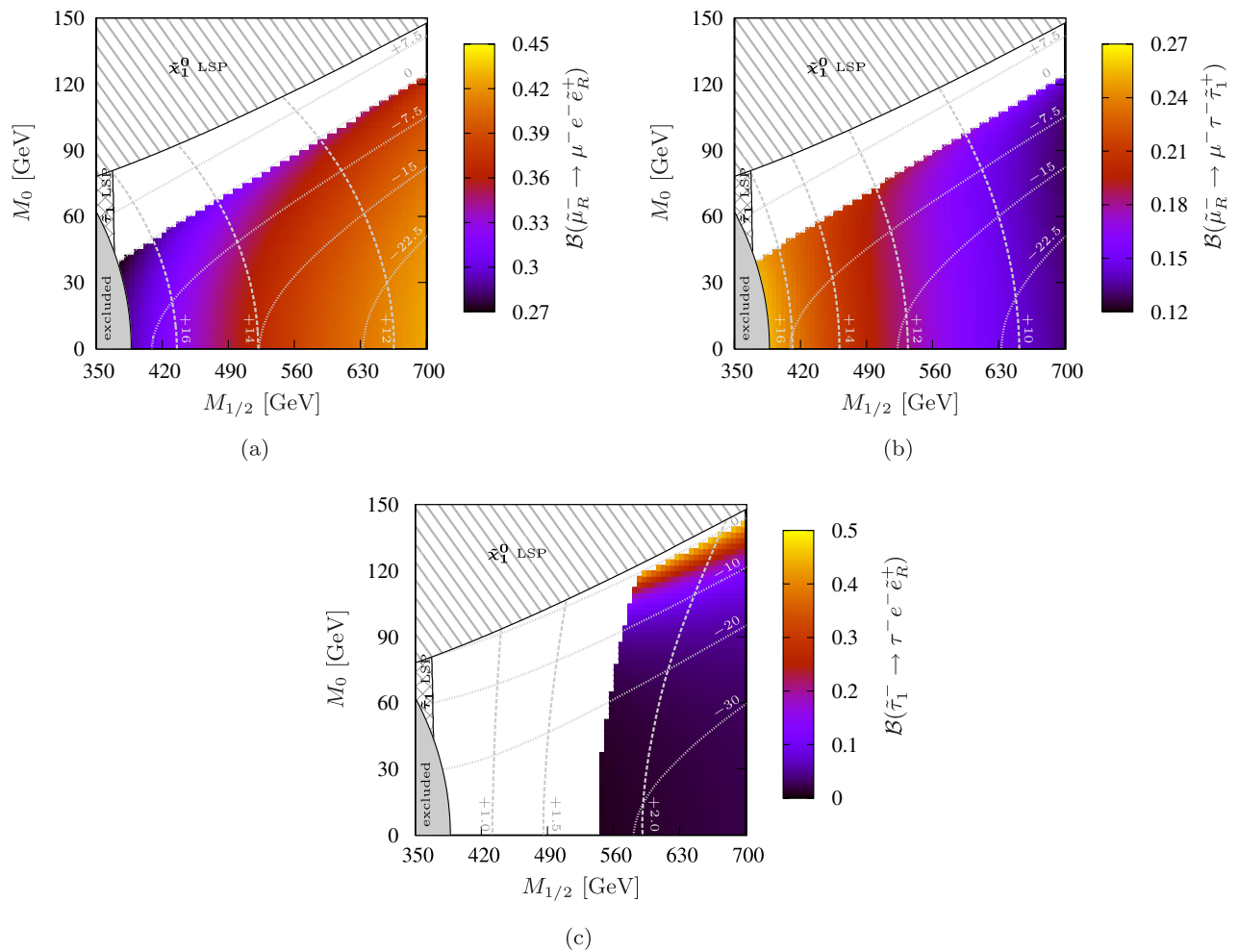


FIG. 24 (color online). Branching ratios for the three-body slepton decays calculated in Secs. D 1 and D 2 as a function of $M_{1/2}$ and M_0 . The other B_3 mSUGRA parameters are $A_0 = -1250$ GeV, $\tan\beta = 5$, $\text{sgn}(\mu) = +$ and $\lambda_{231}|_{\text{GUT}} = 0.045$. In the white region, the decays are kinematically not allowed or heavily suppressed. In (a), we show the branching ratio for the decay $\tilde{\mu}_R^- \rightarrow \mu^- e^- \tilde{e}_R^+$. The dotted and dashed contour lines correspond to the mass difference $M_{\tilde{\mu}_R} - M_{\tilde{\chi}_1^0}$ and $M_{\tilde{\mu}_R} - M_{\tilde{e}_R}$, respectively. In (b), we give the branching ratio for the decay $\tilde{\mu}_R^- \rightarrow \mu^- \tau^- \tilde{\tau}_1^+$. The dotted and dashed contour lines correspond to the mass difference $M_{\tilde{\mu}_R} - M_{\tilde{\chi}_1^0}$ and $M_{\tilde{\mu}_R} - M_{\tilde{\tau}_1}$, respectively. In (c), we present the branching ratio for the decay $\tilde{\tau}_1^- \rightarrow \tau^- e^- \tilde{e}_R^+$. The dotted and dashed contour lines correspond to the mass difference $M_{\tilde{\tau}_1} - M_{\tilde{\chi}_1^0}$ and $M_{\tilde{\tau}_1} - M_{\tilde{e}_R}$, respectively.

the spin-summed squared matrix element; cf. Eqs. (D7) and (D13).

The branching ratio of the decay $\tilde{\mu}_R^- \rightarrow \mu^- \tau^- \tilde{\tau}_1^+$ is shown in Fig. 24(b). The decay $\tilde{\mu}_R^- \rightarrow \mu^- \tau^+ \tilde{\tau}_1^-$ behaves similarly. The dashed (dotted) contour lines correspond now to the mass difference between the $\tilde{\mu}_R$ and the $\tilde{\tau}_1$ ($\tilde{\chi}_1^0$). For light \tilde{e}_R LSP scenarios, i.e. at $M_{1/2} \approx 380$ GeV, the $\tilde{\mu}_R$ decays with almost the same rate into the $\tilde{\tau}_1$ and the \tilde{e}_R LSP because both particles are nearly degenerate in mass. However, the branching ratio $\mathcal{B}(\tilde{\mu}_R^- \rightarrow \mu^- \tau^- \tilde{\tau}_1^+)$ decreases with increasing $M_{1/2}$ because the $\tilde{\tau}_1$ mass increases more rapidly with $M_{1/2}$ than the \tilde{e}_R mass due to the left-handed component of the $\tilde{\tau}_1$. Therefore, at higher values of $M_{1/2}$, the $\tilde{\mu}_R$ prefers to decay into the \tilde{e}_R LSP.

We finally present the branching ratio for the decay $\tilde{\tau}_1^- \rightarrow \tau^- e^- \tilde{e}_R^+$ in Fig. 24(c). The dashed (dotted) contour lines give the mass difference between the $\tilde{\tau}_1$ and the \tilde{e}_R LSP ($\tilde{\chi}_1^0$). Since the \tilde{e}_R and $\tilde{\tau}_1$ are nearly mass degenerate for small $M_{1/2}$, this decay is only allowed kinematically for higher $M_{1/2}$ values; cf. the shaded [colored] region in Fig. 24(c). Here, the branching ratio strongly depends on M_0 ; i.e. it significantly increases with increasing M_0 . This is because there is also the competing R -parity violating decay $\tilde{\tau}_1 \rightarrow e \nu_\mu$ via λ_{231} . Thus, only for scenarios with a low mass difference between the $\tilde{\chi}_1^0$ and $\tilde{\tau}_1$, i.e. where the $\tilde{\chi}_1^0$ in Fig. 22 and Fig. 23 is nearly on shell, do the three-body decays $\tilde{\tau}_1^- \rightarrow \tau^- e^- \tilde{e}_R^+$ (and $\tilde{\tau}_1^- \rightarrow \tau^- e^+ \tilde{e}_R^-$) become important.

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