Updated CMB constraints on dark matter annihilation cross sections

Silvia Galli,^{1,2} Fabio Iocco,³ Gianfranco Bertone,^{3,4} and Alessandro Melchiorri¹

¹Physics Department and INFN, Universita' di Roma "La Sapienza", Ple Aldo Moro 2, 00185, Rome, Italy

²Laboratoire Astroparticule et Cosmologie (APC), Université Paris Diderot, 75205 Paris cedex 13, France ³ Institut d'Astrophysique de Paris UMP 7005 CNPS Paris Université Pierre et Marie Curie

³Institut d'Astrophysique de Paris, UMR 7095-CNRS Paris, Université Pierre et Marie Curie,

boulevard Arago 98bis, 75014, Paris, France
⁴Institute for Theoretical Physics, Univ. of Zürich, Winterthurerst. 190, 8057 Zürich CH

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The injection of secondary particles produced by dark matter (DM) annihilation at redshift $100 \le$ $z \le 1000$ affects the process of recombination, leaving an imprint on cosmic microwave background (CMB) anisotropies. Here we provide a new assessment of the constraints set by cosmic microwave background data on the mass and self-annihilation cross section of DM particles. Our new analysis includes the most recent WMAP (7-year) and ACT data, as well as an improved treatment of the timedependent coupling between the DM annihilation energy with the thermal gas. We show, in particular, that the improved measurement of the polarization signal places already stringent constraints on light DM particles, ruling out "thermal" WIMPs with mass $m_x \le 10$ GeV annihilating into electrons and WIMPs with mass $m_{\chi} \leq 4$ GeV annihilating into muons.

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I. INTRODUCTION

Precision measurements of the cosmic microwave background (CMB) anisotropy in temperature and polarization represent powerful tools to constrain new physics processes (see, e.g., [\[1](#page-3-0)]). In particular, the remarkable agreement between the theoretical description of the recombination process, occurring at $z_r \sim 1000$, and CMB data, severely constrains new sources of ionizing photons, and more in general any deviation from standard recombination [[2\]](#page-3-1), as recently shown by several groups of authors $(see, e.g., [3-7]).$ $(see, e.g., [3-7]).$ $(see, e.g., [3-7]).$

In our previous paper [[8\]](#page-3-4) (hereafter GIBM09), we studied the constraints that this analysis can set on the properties of dark matter (DM) particles [\[9](#page-3-5)–[12](#page-3-6)], under the assumption that standard recombination is modified by dark matter annihilation only.

Here, we present an update of GIBM09 and obtain new constraints on the DM particle annihilation cross section and mass, based on more recent data (WMAP 7-year [\[13\]](#page-3-7) and ACT 2008 [[14](#page-3-8)] data), and on a new and more accurate parametrization of the coupling of the DM-induced energy shower to the thermal gas.

Our results turn out to be competitive with constraints of diverse astrophysical nature, such as radio observation of the Galaxy, antiprotons, gamma rays from the Galactic center and Galactic halo [\[15–](#page-3-9)[18](#page-3-10)], but with respect to them, they have the advantage of not being affected by large astrophysical uncertainties. In fact, our CMB constraints arise from redshifts in the range $100 \le z \le 1000$, i.e., well before the formation of any sizable gravitationally bound structure, and they therefore do not depend on highly uncertain parameters related to structure formation, such as halo shape, concentration or minimal mass.

II. ANNIHILATING DM AND RECOMBINATION

We briefly recall here the effect of energy injection from DM annihilation on the recombination history (see GIBM09 for further details). High-energy particles injected in the high-redshift thermal gas by DM annihilation (or decay) are typically cooled down to the keV scale by high-energy processes (see details below); once the shower has reached this energy scale, the produced secondary particles can (i): ionize the thermal gas, (ii): induce Lyman- α excitation of the hydrogen, and (iii): heat the plasma; the first two modify the evolution of the free electron fraction x_e , the third affects the temperature of baryons. The rate of energy release $\frac{dE}{dt}$ per unit volume by a relic self-annihilating DM particle is given by

$$
\frac{dE}{dt}(z) = \rho_c^2 c^2 \Omega_{\text{DM}}^2 (1+z)^6 p_{\text{ann}}, \quad p_{\text{ann}} \equiv f(z) \frac{\langle \sigma v \rangle}{m_\chi}, \quad (1)
$$

where $\langle \sigma v \rangle$ is the effective self-annihilation rate and m_{χ} the mass of the DM particle, Ω_{DM} the DM density parameter and ρ_c the critical density of the Universe today; the parameter $f(z)$ indicates the fraction of energy which is absorbed overall by the gas, under the approximation that the energy absorption takes place locally. We note that the presence of the brackets in $\langle \sigma v \rangle$ denote a thermal average, as appropriate for relativistic particles at decoupling. At the redshifts of interest here ($z \sim 1000$) the relative velocities of DM particles are $v \sim v_{-8} = 10^{-8}c$, i.e., in the extreme nonrelativistic limit. Though holding for s-wave annihilations, $\langle \sigma v \rangle_{-8} \simeq \langle \sigma v \rangle_{\text{dec}}$, the same is not true in general. For instance, $\langle \sigma v \rangle_{-8} \ge \langle \sigma v \rangle_{\text{dec}}$ in models with so-called Sommerfeld enhancement, and $\langle \sigma v \rangle_{-8} \leq \langle \sigma v \rangle_{\text{dec}}$ in models with *p*-wave annihilations (e.g. $[9-12]$ $[9-12]$ $[9-12]$).

In GIBM09, we considered the fraction of energy $f(z)$ absorbed by the plasma to be constant with redshift, $f(z) = f$. In the following sections, we will present updated constraints obtained by supposing that f is constant with redshift, as well as constraints considering the actual DM model dependent redshift shape of $f(z)$, as calculated in Slatyer et al. [[19\]](#page-3-11).

The formalism we use to introduce the extra energy terms in the recombination equations are the same as in GIBM09, but here we additionally consider the modifications to both helium and hydrogen recombination and we change the extra ionization term (Eq. 6 in GIBM09). In this equation we do not include Peebles' C factor, since we assume that the extra ionization photons only ionize the ground state. We checked that excluding the factor C in this term in any case does not change the constraints by more than 6% in the case of a constant f. The extra Lyman alpha term remains the same as in Eq. 7 of GIBM09.

The most remarkable effect of injecting energy around the recombination epoch is that the amount of free electrons that survive at low redshift after recombination is larger compared to the standard case where no annihilation happens. The CMB spectra are therefore affected as follows (see Ref. [[20](#page-3-12)] for a more detailed discussion): the enhanced amount of x_e at low redshift increases the width of the last scattering surface, and consequently the width of the visibility function. This results in a suppression of the amplitude of the oscillation peaks in the temperature and polarization power spectra, especially at scales smaller than the width of the last scattering surface.

This effect is degenerate with that of other cosmological parameters, affecting the amplitude of peaks at low/high multipoles, such as the scalar spectral index n_s and the baryon density $\omega_b = \Omega_b h^2$. In particular, a value of p_{ann} different from zero can be compensated by a higher value of the scalar spectral index n_s , that gives more power to smaller scales of the spectrum and, to a much smaller extent, by a higher value of the baryon density ω_b . Nevertheless, this last parameter changes the relative amplitudes of the peaks and is therefore less degenerate with p_{ann} than n_s . A smaller degeneracy is also found with the dark matter density $\omega_c \equiv \Omega_c h^2$.

On the other hand, a larger width of the recombination epoch due to DM annihilation increases the quadrupole moment of the radiation field as well, enhancing the amplitude of the polarization power spectrum at large scales. Furthermore, the fractional contribution to the quadrupole of the temperature monopole with respect to the temperature dipole is increased, therefore slightly shifting the position of the peaks of the polarization power spectrum (see [\[20\]](#page-3-12) for further details). An accurate measurement of the polarization power spectrum can therefore help breaking the degeneracy with n_s .

III. UPDATED CMB CONSTRAINTS

Following GIBM09, we compute here the theoretical angular power in presence of DM annihilations, by modifying the RECFAST routine [\[21\]](#page-3-13), along the lines described in the previous section, in the CAMB code [\[22\]](#page-3-14), and by making use of package COSMOMC [\[23\]](#page-3-15) for Monte-Carlo parameter estimation (see GIBM09 for the details of our statistical analysis, including convergence tests and priors). The fractions of energy release inducing ionization, Lyman- α excitation or heating of the baryonic gas are the same as in Chen and Kamionkowski's paper [[24](#page-3-16)], based on the results of Shull and Van Steenberg [[25](#page-3-17)]. The dependence on the properties of the DM particles is encoded in the quantity p_{ann} , appearing in Eq. ([1\)](#page-0-0), that we use as a parameter in the code. We start by considering f as a constant parameter in order to quantify the impact of the new CMB data sets on the analysis presented in GIBM09.

Besides p_{ann} , we sample the following six-dimensional set of cosmological parameters (with flat priors): the physical baryon and CDM densities, ω_b and ω_c , the scalar spectral index, n_s , the normalization, $ln 10^{10} A_s(k=0.002/\text{Mpc})$, the optical depth to reionization, τ , and the Hubble parameter H_0 . We consider purely adiabatic initial conditions.

We include the seven-year WMAP data (WMAP7) [\[13\]](#page-3-7) (temperature and polarization), and the 2008 ACT telescope data [[14](#page-3-8)] (temperature only), that probes the temperature angular power spectrum at small scales (600 $\le l \le 8000$, but in our analysis we consider $l_{\text{max}} = 3500$). The routines for computing the likelihoods for each experiment are supplied by the WMAP and ACT teams, respectively.

The results of our analysis are in Table [I,](#page-1-0) there we show the constraints on the DM annihilation parameter p_{ann} and on the parameters that are more degenerate with it (i.e. n_s , ω_b , ω_c) obtained using WMAP7 data and the combination of WMAP7 plus ACT data. We also report he constraints

TABLE I. Constraints on the annihilation parameter p_{ann} and on the cosmological parameters that are more degenerate with it, i.e., the scalar spectral index n_s , the baryon density ω_b , and the dark matter density ω_c . We report the results using WMAP7 data and WMAP7 + ACT data. The constraints on p_{ann} are upper bound at 95% C.L., while for the other parameters we show the marginalized value and their errors at 68% C.L. The last two columns report the value of the cosmological parameters in the standard Λ CDM case with no annihilation, as found by the WMAP7 team [\[26\]](#page-3-18) and the ACT team [[27](#page-3-19)].

	WMAP7	WMAP7+ACT	WMAP7 Standard	WMAP7+ACT Standard
$p_{\text{ann}}[\text{cm}^3/\text{s}/\text{GeV}]$	\leq 2.42 \times 10 ⁻²⁷	$< 2.09 \times 10^{-27}$	\cdots	\cdots
$n_{\rm s}$	0.977 ± 0.015	0.971 ± 0.014	0.963 ± 0.014	0.962 ± 0.013
$100\Omega_b h^2$	2.266 ± 0.057	2.237 ± 0.053	$2.258_{-0.056}^{+0.057}$	2.214 ± 0.050
$\Omega_c h^2$	0.1115 ± 0.0054	0.1119 ± 0.0053	0.1109 ± 0.0056	0.1127 ± 0.0054

obtained by the WMAP7 team [\[26\]](#page-3-18) and by the ACT team [\[27\]](#page-3-19) on the cosmological parameters in the standard case (no DM annihilation) in order to show the bias introduced on the cosmological parameters by not considering DM annihilation in the analysis.

Note, in particular, that the constraint on p_{ann} with WMAP7 data is improved by a factor \sim 1.8 with respect to the WMAP5 constraint obtained in GIBM09. The 7-year data release has in fact a better measurement of the third peak of the temperature power spectrum at $l \sim 1000-1200$ and of the second dip in the temperature-polarization power spectrum at $l \sim 450$. This allows a better measurement of ω_b and ω_c and a partial break of the degeneracy with p_{ann} . On the other hand, the bias on n_s remains noticeable at the 1- σ level, as the measurement of the polarization power spectrum is still not sufficient to break the degeneracy with p_{ann} . Adding the information at small scales from the ACT data additionally improves the constraint on p_{ann} by \sim 13%. As we can see from the table, the Harrison-Zel'dovic model $n = 1$ is consistent with the $WMAP + ACT$ analysis in between 2 standard deviations when dark matter annihilation is considered.

We have also checked our results when other nonstandard parameters are considered in addition to the standard ones and p_{ann} . We have considered one of the following additional parameters at the time: the fraction of helium abundance Y_{He} , the massive neutrino density, Ω_{ν} , and the running of the scalar spectral index α . None of these parameters appeared to be degenerate with p_{ann} , therefore not affecting the results on the upper limits reported in Table [I](#page-1-0).

IV. IMPLEMENTING THE REDSHIFT DEPENDENCE OF *f*

We have so far worked under the assumption that the fraction of the rest DM mass energy absorbed by the plasma is constant with redshift. Yet, the fraction of the initial energy deposited into the gas is not constant with cosmic time, even if the on-the-spot approximation holds true at all redshifts of interest. This problem has been addressed in [\[19](#page-3-11)], where the authors have computed the

FIG. 1 (color online). Constraints on the cross section $\langle \sigma v \rangle$ in the function of the mass, obtained using a variable $f(z)$ for particles annihilating in muons $(x \text{ signs})$ and in electrons (diamonds) using WMAP7 data (red) and WMAP7 $+$ ACT data (black) at 95% C.L. The exclusion shaded areas are obtained for the interpolation of the WMAP7 $+$ ACT data points for muons (dark shading) and electrons (light shading). The black solid line indicates the thermal cross-section $\langle \sigma v \rangle = 3 \times 10^{-26}$ cm³/s.

evolution of the energy fraction $f(z)$ for different primary species and DM particle mass. As it can be seen from their Fig. 4, the $f(z)$ is a smoothly varying function of redshift (even more so for the values of interest in our problem $100 \le z \le 1000$. We show the constraints for timevarying $f(z)$ in Fig. [1](#page-2-0). Interestingly, the new results rule out thermal WIMPs with mass $m_x \le 10$ GeV annihilating into electrons and WIMPs with mass $m_x \le 4$ GeV annihilating into muons.

We have checked the constraints which is possible to place using the redshift dependent shape of f presented in Eq. A1 and Table 1 of [[19](#page-3-11)]. We have obtained constraints for purely DM models annihilating solely (and separately) into electrons and muons, with different DM masses, reported in Table [II.](#page-2-1) This choice of annihilation channels brackets the possible values of $f(z)$: the case of annihilation to other channels (except of course neutrinos, which practically do

TABLE II. Upper limits on self-annihilation cross section at 95% C.L. using WMAP7 data and a combination of WMAP7 and ACT data. On the left side of the table, we show the results obtained using the proper variable $f(z)$ for each model. On the right side, for the sake of comparison, we show the results obtained by taking the constraints for a constant generic f reported in Table [I,](#page-1-0) and then calculating $\langle \sigma v \rangle$ for each case imposing that f is equal to the corresponding $f(z = 600)$ for each model. We show the results for particles annihilating in electrons and muons.

$\langle \sigma v \rangle$ in [cm ³ /s] with Variable f			$\langle \sigma v \rangle$ in [cm ³ /s] with Constant $f = f(z = 600)$			
m_{χ} [GeV]	channel	WMAP7	$WMAP7 + ACT$	$f(z = 600)$	WMAP7	$WMAP7 + ACT$
1 GeV	e^+e^-	$< 2.90 \times 10^{-27}$	$< 2.41 \times 10^{-27}$	0.87	\leq 2.78 \times 10 ⁻²⁷	$< 2.41 \times 10^{-27}$
100 GeV	e^+e^-	$<$ 3.95 \times 10 ⁻²⁵	$<$ 3.55 \times 10 ⁻²⁵	0.63	$<$ 3.87 \times 10 ⁻²⁵	$<$ 3.35 \times 10 ⁻²⁵
1 TeV	e^+e^-	$\leq 4.68 \times 10^{-24}$	$<$ 3.80 \times 10 ⁻²⁴	0.60	$\leq 4.02 \times 10^{-24}$	$<$ 3.48 \times 10 ⁻²⁴
1 GeV	$\mu^+\mu^-$	$\leq 8.68 \times 10^{-27}$	$\leq 6.93 \times 10^{-27}$	0.30	$\leq 8.03 \times 10^{-27}$	$\leq 6.95 \times 10^{-27}$
100 GeV	$\mu^+\mu^-$	$\leq 9.82 \times 10^{-25}$	\leq 8.94 \times 10 ⁻²⁵	0.23	$\leq 1.03 \times 10^{-24}$	$\leq 8.91 \times 10^{-25}$
1 TeV	$\mu^+\mu^-$	$\leq 1.20 \times 10^{-23}$	\leq 9.41 \times 10 ⁻²⁴	0.21	$\leq 1.15 \times 10^{-23}$	\leq 9.96 \times 10 ⁻²⁴

not couple at all with the plasma) falls between the two limiting cases studied here.

Although the implementation of the z dependence of f clearly leads to more accurate results, we found that taking a simplified analysis with constant f , such that $f(z = 600) = f_{const}$, leads to a difference with respect to the full $f(z)$ approach of less than \sim 15%, depending on the annihilation channel considered.

V. DISCUSSION AND CONCLUSIONS

In this article we have provided new updated CMB constraints on WIMP annihilations, with an improved analysis that includes more recent CMB data (WMAP7 and the ACT2008) and implements the redshift evolution of the thermal gas opacity to the high-energy primary shower. We have also found that a simplified analysis with constant $f = f(z = 600)$ leads to an error on the maximum DM self-annihilation cross section smaller than \sim 15%, with respect to a treatment that fully takes into account the redshift dependence of $f(z)$.

While we were finalizing this paper, Hutsi *et al.* (HCHR2011) [\[28\]](#page-3-20) have reported results from a similar analysis, using an averaged evolution of the $f(z)$. They provide 2- σ upper limits from WMAP7 with 1- σ uncertainties on these limits due to the method used. These results are a factor between 1.2 and 2 weaker than ours. This is partially due to the fact that we account for extra Lyman radiation in our code, but this can account for only less than 10% of the difference between the results.

As in GIBM09, we have calculated how much the Planck satellite and a hypothetical cosmic variance limited experiment will improve the constraints compared to WMAP7 in the case of constant f (constraints for Planck and CVL reported in GIBM09). We obtain improvement factors of 8 and 23 for Planck and CVL, respectively, which are compatible with the ones reported in HCHR2011, 6, and 13. The difference for the CVL experiment is attributed to the slightly different specifications used for the CVL experiment in HCHR2011 and in GIBM09, namely, the maximum multipole considered in the analysis, as also stated in HCHR2011. Clearly the data from the on-going Planck satellite mission, expected to be released by early 2013, will play a crucial role in constraining additional sources of ionization, such as DM annihilation, in the early universe.

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