PHYSICAL REVIEW D 83, 054007 (2011)

Exclusive rare decay $b \rightarrow s \gamma$ of heavy b baryons

Yong-Lu Liu, Long-Fei Gan, and Ming-Qiu Huang

Department of Physics, College of Science, National University of Defense Technology, Changsha, Hunan 410073, People's Republic of China (Received 11 January 2011; published 7 March 2011)

We present an analysis on the exclusive rare radiative decay modes $\Sigma_b \to \Sigma \gamma$ and $\Xi_b \to \Xi \gamma$. The transition form factors which parametrize these processes are calculated using QCD light-cone sum rules. The decay widths we predict are $\Gamma(\Sigma_b \to \Sigma \gamma) = (7.21 \pm 0.04) \times 10^{-18}$ GeV and $\Gamma(\Xi_b \to \Xi \gamma) = (1.34 \pm 0.07) \times 10^{-16}$ GeV. The branching ratio of $\Xi_b \to \Xi \gamma$ is predicted to be $\text{Br}(\Xi_b \to \Xi \gamma) = (3.03 \pm 0.10) \times 10^{-4}$.

DOI: 10.1103/PhysRevD.83.054007 PACS numbers: 14.20.-c, 11.25.Hf, 11.55.Hx, 13.40.-f

I. INTRODUCTION

Heavy flavor physics plays an important role both in the precise test of the standard model in the relatively high energy region and in the investigation of the hadronization of quarks at low energy. Hence, a lot of effort has been paid into it and a large amount of experimental data have been accumulated [1–4]. Theoretically, much progress has been made in the heavy flavor meson sector for its comparatively simple structure while knowledge about baryons appears to be limited. Although much literature has been provided to decipher these heavy flavor states (such as Refs. [5–8]), a deep understanding of them undoubtedly demands the information on the dynamical details which are encoded in various decay modes [9,10]. Among these modes, the rare radiative decay processes of the b-baryons are important in that they are not only the ways to study the Cabibbo-Kobayashi-Maskawa matrix elements V_{ts} and V_{tb} which are closely attached with the dynamics inside the baryons, but also the ways to probe new physics beyond the standard model.

These types of processes (such as $b \rightarrow s\gamma$), which are forbidden at the tree level in the standard model of electroweak theory, are induced by the flavor-changing neutral current (FCNC) of the b-quark. Their amplitudes are dominated by the one-loop diagrams with a virtual top quark and a W boson, and thus are strongly suppressed by Glashow-Iliopoulos-Maiani mechanism. The relative bmeson rare radiative decay modes have been investigated experimentally since the early 1990's [11–14], while not so many experimental data are available for the corresponding b-baryon processes. Theoretical studies on the exclusive processes are available for both b-mesons and b-baryons [15–19], despite the fact that the dynamics of the b-baryons' decays are far less clarified in comparison with that of the b-mesons. However, most of the existing literature is about the process $\Lambda_b \to \Lambda \gamma$, the branching ratio of which has been predicted to be $Br(\Lambda_b \to \Lambda \gamma) \le$ 1.3×10^{-3} experimentally [20]. Unfortunately, this decay mode is not expected to be measured easily in the experiments due to the fact that the final state Λ baryon is of

neutral charged, as argued in Ref. [21]. For this reason, we turn to study the possible decay modes of other octet heavy baryons Σ_b and Ξ_b , in which charged final states arise and may be easily tested in experiments. It has been estimated early in the 1990s that a number of b-baryons may be produced at the c.m. energy level of the LHC [22]. Thus we can expect that these rare decay modes could be measured by the LHC experiments in the near future, the updated energy of which is expected to be \sim 14 TeV.

The remainder of this paper is organized as follows. We give an introduction to the exclusive rare decay mode $b \rightarrow s\gamma$ and derive the formula of the decay widths in Sec. II. Then the light-cone QCD sum rules for the relative transition form factors are derived in Sec. III. Finally, Sec. IV is devoted to the numerical analysis and a summary is given at the end of this section.

II. PARAMETRIZATION OF THE TRANSITION FORM FACTORS

In the standard model, the process of the exclusive rare decay $b \rightarrow s\gamma$ can be described by the following effective Hamiltonian [23]:

$$H_{\rm eff}(b \to s\gamma) = -4 \frac{G_F}{\sqrt{2}} V_{ts}^* V_{tb} C_7(\mu) \mathcal{O}_7(\mu), \qquad (1)$$

with

$$\mathcal{O}_7 = \frac{e}{16\pi^2} \bar{s} \sigma_{\mu\nu} (m_b R + m_s L) b F^{\mu\nu}, \tag{2}$$

where $L/R=(1\mp\gamma_5)/2$ and $F^{\mu\nu}$ is the field strength tensor of the photon. G_F is the Fermi coupling constant and $C_7(\mu)$ is the Wilson coefficient at the scale μ . Considering the general form beyond the standard model, \mathcal{O}_7 can be represented as

$$\mathcal{O}_7 = \frac{e}{32\pi^2} m_b \bar{s} \sigma_{\mu\nu} (g_V + \gamma_5 g_A) b F^{\mu\nu}. \tag{3}$$

The decay amplitude is given by the expectation value of the effective Hamiltonian between the initial and final states at the hadron level YONG-LU LIU, LONG-FEI GAN, AND MING-QIU HUANG

$$M(X_b \to X\gamma) = \langle X\gamma | H_{\text{eff}} | X_b \rangle,$$
 (4)

where *X* stands for the baryon involved in the process.

By considering the Lorentz structure, the contribution of the hadronic part to the process, which is written as the hadronic matrix elements, is generally parametrized in terms of the following form factors:

$$\langle X_{b}(P')|j_{\nu}|X(P)\rangle = \bar{X}_{b}(P')[f_{1}\gamma_{\nu} - f_{2}i\sigma_{\mu\nu}q^{\mu} + f_{3}q_{\nu} - (g_{1}\gamma_{\nu} + g_{2}i\sigma_{\mu\nu}q^{\mu} + g_{3}q_{\nu})\gamma_{5}]X(P),$$
(5)

where X_b and X are the spinors of the baryons and the weak current j_{ν} is defined as

$$j_{\nu}(x) = i\bar{b}(x)\sigma_{\mu\nu}(1 - \gamma_5)q^{\mu}s(x).$$
 (6)

In fact, form factors f_3 and g_3 do not contribute to the process due to the conservation of the vector current. Therefore, the form factors we need to calculate are $f_1(g_1)$ and $f_2(g_2)$, which can be determined from the QCD light-cone sum rules. It is noted that the processes are only related to the form factors at the point $q^2 = 0$, thus we just consider this case in the following analysis.

With the form factors defined above, the decay width is represented as

$$\Gamma(X_b \to X\gamma) = \frac{G_F^2 |V_{tb}V_{ts}^*|^2 \alpha_{em} |C_7|^2 m_b^2}{32\pi^4} \times \left(\frac{M_{X_b}^2 - M_X^2}{M_{X_b}}\right)^3 (g_V^2 f_2^2 + g_A^2 g_2^2).$$
 (7)

III. LIGHT-CONE SUM RULES FOR THE FORM FACTORS

Now we apply the light-cone QCD sum rule approach to calculate the transition form factors $f_1(g_1)$ and $f_2(g_2)$. The interpolating currents to the heavy baryons are chosen as $j_{\Sigma_b}(0) = \epsilon^{ijk}[q^i(0)Czq^j(0)]\gamma_5zb^k(0)$ for Σ_b and $j_{\Xi_b}(0) = \epsilon^{ijk}[s^i(0)Czb^j(0)]\gamma_5zq^k(0)$ for Ξ_b , respectively. Herein q stands for u or d quark, C is the charge conjugation matrix, and z is the vector defined on the light-cone $z^2 = 0$. The normalization of these currents is defined by the parameters f_{Σ_b} and f_{Ξ_b} :

$$\langle 0|j_{\Sigma_b}|\Sigma_b(P')\rangle = f_{\Sigma_b}(z \cdot P') \not z \Sigma_b(P'),$$

$$\langle 0|j_{\Xi_b}|\Xi_b(P')\rangle = f_{\Xi_b}(z \cdot P') \not z \Xi_b(P').$$
 (8)

In the following part, we will take $\Sigma_b^+ \to \Sigma^+ \gamma$ as an example. Our starting point for calculating the form factors is the correlation function

$$T_{\mu} = i \int d^4x e^{iqx} \langle 0|j_{\Sigma_b(0)}j_{\nu}(x)|\Sigma(P,s)\rangle \tag{9}$$

at $q^2 = 0$ and with Euclidean $m_b^2 - P'^2$ of about several GeV². Following the standard procedure of the light-cone sum rule method, we need to express the correlation function both phenomenologically and theoretically. By inserting a complete set of intermediate states and using the definitions (5) and (8), the phenomenological side is represented as

$$z^{\nu}T_{\nu}(P,q) = \frac{2f_{\Sigma_{b}}(z \cdot P')^{2}}{M_{\Sigma_{b}}^{2} - P'^{2}} [f_{1} \not z - f_{2} \not q \not z - g_{1} \not z \gamma_{5} + g_{2} \not q \not z \gamma_{5}] \Sigma(P) + \dots,$$
(10)

where "..." stands for the continuum contributions. The correlation function (9) is contracted by z^{ν} to remove contributions proportional to the light-cone vector z^{ν} which is subdominant on the light-cone.

On the other hand, the theoretical side is obtained by contracting the heavy b quarks in the correlation function and using the distribution amplitudes presented in Refs. [24–26]. To make the paper self-contained, we present in the Appendix the definition and the explicit expressions of the distribution amplitudes of Σ and Ξ used in this paper. After assuming the quark-hadron duality and performing the Borel transformation, we arrive at the final light-cone sum rule of the form factor $f_2(0)$:

$$f_{\Sigma_{b}}f_{2}(0)e^{-(M_{\Sigma_{b}}^{2}/M_{B}^{2})}$$

$$= \int_{\alpha_{30}}^{1} d\alpha_{3}e^{-(s/M_{B}^{2})} \Big\{ B_{0}(\alpha_{3}) + \frac{M^{2}}{M_{B}^{2}} B_{1}(\alpha_{3})$$

$$- \frac{M^{4}}{M_{B}^{4}} B_{2}(\alpha_{3}) \Big\} - \frac{M^{2}\alpha_{30}^{2}e^{-(s_{0}/M_{B}^{2})}}{\alpha_{30}^{2}M^{2} + m_{b}^{2}}$$

$$\times \Big\{ B_{1}(\alpha_{30}) - \frac{M^{2}}{M_{B}^{2}} B_{2}(\alpha_{30}) - \frac{d}{d\alpha_{30}} \frac{\alpha_{30}^{2}M^{2} B_{2}(\alpha_{30})}{\alpha_{30}^{2}M^{2} + m_{b}^{2}} \Big\},$$

$$(11)$$

where $s = (1 - \alpha_3)M^2 + m_b^2/\alpha_3$, M is the mass of the final baryon, and M_B^2 is the Borel parameter which is introduced to suppress the contributions from the higher resonances and the continuum states. Our calculation shows that $f_1 = g_1 = 0$ and $f_2 = g_2$. In Eq. (11), the following abbreviations are used for convenience:

$$\begin{split} B_0(\alpha_3) &= \int_0^{1-\alpha_3} d\alpha_1 V_1(\alpha_1, 1 - \alpha_1 - \alpha_3, \alpha_3), \\ B_1(\alpha_3) &= (2\tilde{V}_1 - \tilde{V}_2 - \tilde{V}_3 - \tilde{V}_4 - \tilde{V}_5)(\alpha_3), \\ B_2(\alpha_3) &= (-\tilde{\tilde{V}}_1 + \tilde{\tilde{V}}_2 + \tilde{\tilde{V}}_3 + \tilde{\tilde{V}}_4 + \tilde{\tilde{V}}_5 - \tilde{\tilde{V}}_6)(\alpha_3). \end{split} \tag{12}$$

The distribution amplitudes with tildes which come from the integration by parts in α_3 are defined as

EXCLUSIVE RARE DECAY $b \rightarrow s \gamma$ OF ...

$$\tilde{V}_{i}(\alpha_{3}) = \int_{0}^{\alpha_{3}} d\alpha'_{3} \int_{0}^{1-\alpha'_{3}} d\alpha_{1} V_{i}(\alpha_{1}, 1-\alpha_{1}-\alpha'_{3}, \alpha'_{3}),
\tilde{\tilde{V}}_{i}(\alpha_{3}) = \int_{0}^{\alpha_{3}} d\alpha'_{3} \int_{0}^{\alpha'_{3}} d\alpha''_{3}
\times \int_{0}^{1-\alpha''_{3}} d\alpha_{2} V_{i}(\alpha_{1}, 1-\alpha_{1}-\alpha''_{3}, \alpha''_{3}).$$
(13)

The same procedure is also carried out to calculate the transition form factors of the process $\Xi_b \to \Xi \gamma$. We obtain the final sum rule as follows:

$$\begin{split} f_{\Xi_{b}} f_{2}(0) e^{-(M_{\Xi_{b}}^{2}/M_{B}^{2})} \\ &= \int_{\alpha_{20}}^{1} d\alpha_{2} e^{-(s'/M_{B}^{2})} \Big\{ C_{0}(\alpha_{2}) + \frac{M^{2}}{M_{B}^{2}} C_{1}(\alpha_{2}) \\ &+ \frac{M^{2}}{\alpha_{2} M_{B}^{2}} C_{2}(\alpha_{2}) - \frac{M^{4}}{M_{B}^{4}} C_{3}(\alpha_{2}) \Big\} + \frac{M^{2} \alpha_{20}^{2} e^{-(s_{0}/M_{B}^{2})}}{\alpha_{20}^{2} M^{2} + m_{b}^{2}} \\ &\times \Big\{ C_{1}(\alpha_{20}) + \frac{1}{\alpha_{20}} C_{2}(\alpha_{20}) - \frac{M^{2}}{M_{B}^{2}} C_{3}(\alpha_{20}) \\ &+ \frac{d}{d\alpha_{20}} \frac{\alpha_{20}^{2} M^{2} C_{3}(\alpha_{20})}{\alpha_{20}^{2} M^{2} + m_{b}^{2}} \Big\}, \end{split}$$
(14)

where $s' = (1 - \alpha_2)M^2 + m_b^2/\alpha_2$, M is the mass of Ξ , and the following abbreviations are used:

$$C_{0}(\alpha_{2}) = \int_{0}^{1-\alpha_{2}} d\alpha_{1} T_{1}(\alpha_{1}, \alpha_{2}, 1 - \alpha_{1} - \alpha_{2}),$$

$$C_{1}(\alpha_{2}) = (2\tilde{T}_{1} - \tilde{T}_{2} - \tilde{T}_{5} - 2\tilde{T}_{7} - 2\tilde{T}_{8})(\alpha_{2}),$$

$$C_{2}(\alpha_{2}) = (\tilde{T}_{2} - \tilde{T}_{3} - \tilde{T}_{4} + \tilde{T}_{5} + \tilde{T}_{7} + \tilde{T}_{8})(\alpha_{2}),$$

$$C_{3}(\alpha_{2}) = (-\tilde{T}_{1} + \tilde{T}_{2} + \tilde{T}_{5} - \tilde{T}_{6} + 2\tilde{T}_{7} + 2\tilde{T}_{8})(\alpha_{2}).$$
(15)

The functions with tildes are defined as

$$\tilde{T}_{i}(\alpha_{2}) = \int_{0}^{\alpha_{2}} d\alpha'_{2} \int_{0}^{1-\alpha'_{2}} d\alpha_{1} T_{i}(\alpha_{1}, \alpha'_{2}, 1 - \alpha_{1} - \alpha'_{2}),
\tilde{T}_{i}(\alpha_{2}) = \int_{0}^{\alpha_{2}} d\alpha'_{2} \int_{0}^{\alpha'_{2}} d\alpha''_{2}
\times \int_{0}^{1-\alpha''_{2}} d\alpha_{2} T_{i}(\alpha_{1}, \alpha''_{2}, 1 - \alpha_{1} - \alpha''_{2}).$$
(16)

IV. NUMERICAL ANALYSIS AND THE SUMMARY

Before the numerical evaluation of the sum rules (11) and (14), we need to determine the input parameters. Two important parameters are the decay constants f_{Σ_b} and f_{Ξ_b} , which can be calculated with the QCD sum rule approach. Using the same expressions in Refs. [25,26] with the replacements $m_s \to m_b$ for f_{Σ_b} and $m_c \to m_b$ for f_{Ξ_b} , we get the estimations $f_{\Sigma_b} = (6.18 \pm 0.03) \times 10^{-3} \text{ GeV}^2$ and $f_{\Xi_b} = (3.32 \pm 0.46) \times 10^{-3} \text{ GeV}^2$. Other input parameters needed in our calculation can be read from Ref. [27]:

$$m_b = 4.8 \text{ GeV},$$
 $m_s = 0.15 \text{ GeV},$ $M_{\Sigma} = 1.189 \text{ GeV},$ $M_{\Xi} = 1.314 \text{ GeV},$ $M_{\Sigma_b} = 5.729 \text{ GeV},$ $M_{\Xi_b} = 5.81 \text{ GeV},$ $V_{ts} = 0.0403,$ $V_{tb} = 0.9992,$ (17)

and

$$\alpha_{em} = 1/137,$$

$$G_F = 1.166364 \times 10^{-5} \text{ GeV}^{-2},$$

$$C_7(m_b) = -0.31.$$
(18)

An important step in the numerical analysis of the QCD sum rules is to determine the Borel mass parameter M_R^2 and the continuum threshold s_0 . The continuum threshold s_0 can be chosen by demanding that the continuum contribution is subdominant in comparison with that of the ground state which we are concerned about. Simultaneously, the resulting form factors should not vary drastically along with the threshold. Thus s_0 is generally connected with the first resonance which has the same quantum numbers as the particle we care about. Here we fix the threshold s_0 in the region 39 GeV² $\leq s_0 \leq 41$ GeV². As for the Borel parameter M_B^2 , which is introduced to suppress the higher resonance contributions efficiently, we also demand that the higher twists contributions are less significant and the form factors should vary mildly along with it. Our calculation shows that the working windows can be chosen properly in the region 8 GeV² $\leq M_B^2 \leq 11 \text{ GeV}^2$ for $\Sigma_b \rightarrow \Sigma \gamma$ and 9 GeV² $\leq M_B^2 \leq 12 \text{ GeV}^2$ for $\Xi_b \rightarrow \Xi \gamma$.

Using the distribution amplitudes given in Refs. [25,26], we obtain the form factors at the zero momentum transfer $f_2(g_2)(0)$ as functions of the Borel parameter M_B^2 , which are displayed in Fig. 1. We have also analyzed the contributions from the distributions of different twists, which are shown in Fig. 2. The results show that the contributions of the leading-order and next-to-leading-order twists are dominant while the contributions from higher twists are suppressed efficiently. This implies that the light-cone expansion is reasonable in the cases we considered in this paper.

By using of the form factors we have estimated above, the decay widths of the processes can be easily evaluated with the formula (7), which turns out to be $\Gamma(\Sigma_b \to \Sigma \gamma) = (7.21 \pm 0.04) \times 10^{-18}$ GeV and $\Gamma(\Xi_b \to \Xi \gamma) = (1.34 \pm 0.07) \times 10^{-16}$ GeV. Although the mean life of Ξ_b^- has been estimated experimentally [3,4,28–30], here we use the average value given in Ref. [27] to estimate the branching ratio of the process $\Xi_b^- \to \Xi^- \gamma$ which turns out to be $Br(\Xi_b^- \to \Xi^- \gamma) = (3.03 \pm 0.10) \times 10^{-4}$. The errors in the widths come from the choices of the threshold, the sum rule windows, and the uncertainties in the decay constants f_{Σ_b} and f_{Ξ_b} . It is worth noting that errors from other sources are not considered here because the sum rule method itself brings in an amount of uncertainties (about

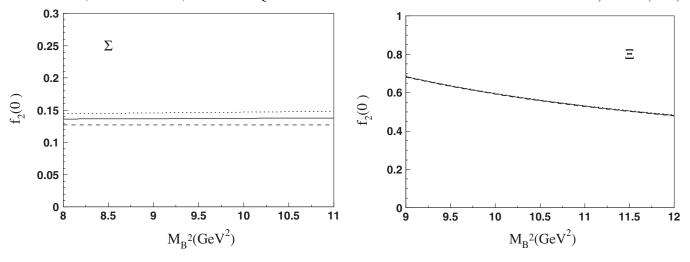


FIG. 1. The dependence of the form factors $f_2(0)$'s on the Borel parameter with $s_0 = 39$, 40 41 GeV² from the top down.

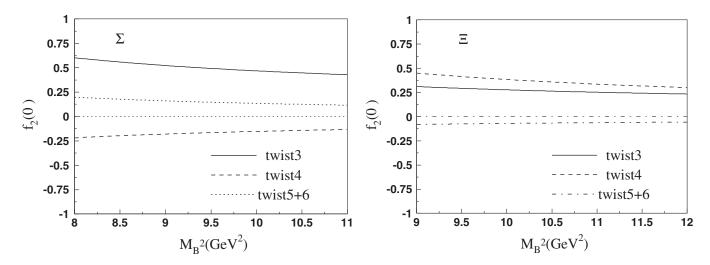


FIG. 2. The contributions to the form factors $f_2(0)$'s from different twists on the Borel parameter with $s_0 = 40 \text{ GeV}^2$.

20%), which makes it less significant to take into account the errors of the input parameters.

We also investigate the sensitivity of the form factors to the variation of m_b at different points $m_b = 4.7$, 4.8 and 4.9 GeV. The corresponding predictions for the decay widths and branching ratios are given in Table I.

In summary, we have investigated the exclusive rare decay processes $\Sigma_b \to \Sigma \gamma$ and $\Xi_b \to \Xi \gamma$. The corresponding transition form factors are estimated through the light-cone QCD sum rule approach and the decay

widths of these processes are predicted to be $\Gamma(\Sigma_b \to \Sigma \gamma) = (7.21 \pm 0.04) \times 10^{-18}$ GeV and $\Gamma(\Xi_b \to \Xi \gamma) = (1.34 \pm 0.04) \times 10^{-16}$ GeV. We also estimate the branching ratio of $\Xi_b^- \to \Xi^- \gamma$, which is $Br(\Xi_b^- \to \Xi^- \gamma) = (3.03 \pm 0.10) \times 10^{-4}$. As we can see, our prediction is larger than the theoretical estimations for the branching ratio of the $\Lambda_b \to \Lambda \gamma$. Therefore it is reasonable to assume that this mode may be tested easily, provided that a good source of Σ_b or Ξ_b is available in the future experiments, such as the LHC experiments.

TABLE I. Decay widths and branching ratios at different points of m_b .

$m_b(\text{GeV})$	4.7	4.8	4.9
$\Gamma(\Sigma_b \to \Sigma \gamma) (\times 10^{-18} \text{ GeV})$	6.92 ± 0.03	7.21 ± 0.04	7.26 ± 0.07
$\Gamma(\Xi_b \to \Xi \gamma)(\times 10^{-16} \text{ GeV})$	0.98 ± 0.04	1.34 ± 0.04	1.75 ± 0.05
$Br(\Xi_b^- \to \Xi^- \gamma)(\times 10^{-4})$	2.21 ± 0.08	3.03 ± 0.10	3.96 ± 0.11

ACKNOWLEDGMENTS

This work was supported in part by the National Natural Science Foundation of China under Contract Nos. 10975184 and 11047117.

APPENDIX

In the following we give the distribution amplitudes of Σ and Ξ used in the paper. In general, the distribution amplitudes are defined by the matrix element of the three-quark operator as

$$\begin{split} 4\langle 0|\epsilon^{ijk}q_{1\alpha}^{i}(a_{1}z)q_{2\beta}^{j}(a_{2}z)q_{3\gamma}^{k}(a_{3}z)|X(P)\rangle &= V_{1}(\not pC)_{\alpha\beta}(\gamma_{5}X^{+})_{\gamma} + V_{2}(\not pC)_{\alpha\beta}(\gamma_{5}X^{-})_{\gamma} + \frac{V_{3}}{2}M(\gamma_{\perp}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{+})_{\gamma} \\ &+ \frac{V_{4}}{2}M(\gamma_{\perp}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{-})_{\gamma} + V_{5}\frac{M^{2}}{2pz}(zC)_{\alpha\beta}(\gamma_{5}X^{+})_{\gamma} \\ &+ \frac{M^{2}}{2pz}V_{6}(zC)_{\alpha\beta}(\gamma_{5}X^{-})_{\gamma} + T_{1}(i\sigma_{\perp p}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{+})_{\gamma} \\ &+ T_{2}(i\sigma_{\perp p}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{-})_{\gamma} + T_{3}\frac{M}{pz}(i\sigma_{pz}C)_{\alpha\beta}(\gamma_{5}X^{+})_{\gamma} \\ &+ T_{4}\frac{M}{pz}(i\sigma_{zp}C)_{\alpha\beta}(\gamma_{5}X^{-})_{\gamma} + T_{5}\frac{M^{2}}{2pz}(i\sigma_{\perp z}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{+})_{\gamma} \\ &+ \frac{M^{2}}{2pz}T_{6}(i\sigma_{\perp z}C)_{\alpha\beta}(\gamma^{\perp}\gamma_{5}X^{-})_{\gamma} + M\frac{T_{7}}{2}(\sigma_{\perp \perp'}C)_{\alpha\beta}(\sigma^{\perp \perp'}\gamma_{5}X^{+})_{\gamma} \\ &+ M\frac{T_{8}}{2}(\sigma_{\perp \perp'}C)_{\alpha\beta}(\sigma^{\perp \perp'}\gamma_{5}X^{-})_{\gamma}, \end{split} \tag{A1}$$

where M is the mass of the baryon X and C is the charge conjugation matrix. Note that the other Lorentz structures which do not contribute to the calculations are omitted. For each of the distribution amplitudes $F_i = V_i$, T_i defined above, it can be presented as

$$F(a_i p \cdot z) = \int \mathcal{D}x e^{-ipz \sum_i x_i a_i} F(x_i), \tag{A2}$$

with the relationship $0 < x_i < 1$, $\sum_i x_i = 1$, and x_i corresponds to the distribution of the baryon momentum on the quarks. The integration measure is defined as

$$\int \mathcal{D}x = \int_0^1 dx_1 dx_2 dx_3 \delta(x_1 + x_2 + x_3 - 1).$$
 (A3)

The distribution amplitudes can be expanded with a conformal spin. The detailed process is referred to in Refs. [24–26]. The explicit expressions of the distribution amplitudes are collected below:

$$V_{1}(x_{i}) = 120x_{1}x_{2}x_{3}\phi_{3}^{0}, \qquad V_{2}(x_{i}) = 24x_{1}x_{2}\phi_{4}^{0}, \qquad V_{3}(x_{i}) = 12x_{3}(1 - x_{3})\psi_{4}^{0},$$

$$V_{4}(x_{i}) = 3(1 - x_{3})\psi_{5}^{0}, \qquad V_{5}(x_{i}) = 6x_{3}\phi_{5}^{0}, \qquad V_{6}(x_{i}) = 2\phi_{6}^{0},$$

$$T_{1}(x_{i}) = 120x_{1}x_{2}x_{3}\phi_{3}^{\prime 0}, \qquad T_{2}(x_{i}) = 24x_{1}x_{2}\phi_{4}^{\prime 0}, \qquad T_{3}(x_{i}) = 6x_{3}(1 - x_{3})(\xi_{4}^{0} + \xi_{4}^{\prime 0}),$$

$$T_{4}(x_{i}) = -\frac{3}{2}(x_{1} + x_{2})(\xi_{5}^{\prime 0} + \xi_{5}^{0}) \qquad T_{5}(x_{i}) = 6x_{3}\phi_{5}^{\prime 0}, \qquad T_{6}(x_{i}) = 2\phi_{6}^{\prime 0}$$

$$T_{7}(x_{i}) = 6x_{3}(1 - x_{3})(\xi_{4}^{\prime 0} - \xi_{4}^{0}), \qquad T_{8}(x_{i}) = \frac{3}{2}(x_{1} + x_{2})(\xi_{5}^{\prime 0} - \xi_{5}^{0}).$$
(A4)

The parameters in the expressions are as follows:

PHYSICAL REVIEW D 83, 054007 (2011)

$$\phi_{3}^{0} = \phi_{6}^{0} = f_{X}, \qquad \psi_{4}^{0} = \psi_{5}^{0} = \frac{1}{2}(f_{X} - \lambda_{1}), \qquad \phi_{4}^{0} = \phi_{5}^{0} = \frac{1}{2}(f_{X} + \lambda_{1}),$$

$$\phi_{3}^{0} = \phi_{6}^{0} = -\xi_{5}^{0} = \frac{1}{6}(4\lambda_{3} - \lambda_{2}), \qquad \phi_{4}^{0} = \xi_{4}^{0} = \frac{1}{6}(8\lambda_{3} - 3\lambda_{2}), \qquad \phi_{5}^{0} = -\xi_{5}^{0} = \frac{1}{6}\lambda_{2},$$

$$\xi_{4}^{0} = \frac{1}{6}(12\lambda_{3} - 5\lambda_{2}).$$
(A5)

The nonperturbative parameters f_X , λ_1 and λ_2 are determined with QCD sum rules to be

$$f_{\Sigma} = (9.4 \pm 0.4) \times 10^{-3} \text{ GeV}^2, \qquad \lambda_1 = -(2.5 \pm 0.1) \times 10^{-2} \text{ GeV}^2,$$

 $\lambda_2 = (4.4 \pm 0.1) \times 10^{-2} \text{ GeV}^2, \qquad \lambda_3 = (2.0 \pm 0.1) \times 10^{-2} \text{ GeV}^2$ (A6)

for Σ and

$$f_{\Xi} = (9.9 \pm 0.4) \times 10^{-3} \text{ GeV}^2, \qquad \lambda_1 = -(2.8 \pm 0.1) \times 10^{-2} \text{ GeV}^2,
\lambda_2 = (5.2 \pm 0.2) \times 10^{-2} \text{ GeV}^2, \qquad \lambda_3 = (1.7 \pm 0.1) \times 10^{-2} \text{ GeV}^2$$
(A7)

for Ξ .

- [1] D. Acosta *et al.* (CDF Collaboration), Phys. Rev. Lett. **96**, 202001 (2006).
- [2] V. Abazov *et al.* (D0 Collaboration), Phys. Rev. Lett. 99, 052001 (2007).
- [3] T. Aaltonen *et al.* (CDF Collaboration), Phys. Rev. Lett. **99**, 052002 (2007).
- [4] T. Aaltonen *et al.* (CDF Collaboration), Phys. Rev. Lett. **99**, 202001 (2007).
- [5] D. Ebert, R. N. Faustov, and V. O. Galkin, Phys. Rev. D 72, 034026 (2005); Phys. Lett. B 659, 612 (2008).
- [6] Jian-Rong Zhang and Ming-Qiu Huang, Phys. Rev. D 78, 094015 (2008).
- [7] R. Roncaglia, D. B. Lichtenberg, and E. Predazzi, Phys. Rev. D 52, 1722 (1995).
- [8] N. Mathur, R. Lewis, and R. M. Woloshyn, Phys. Rev. D **66**, 014502 (2002).
- [9] K. Azizi, M. Bayar, A. Ozpineci, and Y. Sarac, Phys. Rev. D 80, 036007 (2009).
- [10] M. Q. Huang and D. W. Wang, Phys. Rev. D 69, 094003 (2004).
- [11] R. Ammar *et al.* (CLEO Collaboration), Phys. Rev. Lett. **71**, 674 (1993).
- [12] T. E. Coan *et al.* (CLEO Collaboration), Phys. Rev. Lett. 84, 5283 (2000).
- [13] B. Aubert *et al.* (BaBar Collaboration), Phys. Rev. Lett.
 88, 101805 (2002); Phys. Rev. D 70, 112006 (2004); Phys. Rev. D 72, 052004 (2005).
- [14] M. Nakao *et al.* (Belle Collaboration), Phys. Rev. D **69**, 112001 (2004); P. Koppenburg *et al.* (Belle Collaboration), Phys. Rev. Lett. **93**, 061803 (2004).
- [15] T. Mannel and S. Recksiegel, J. Phys. G 24, 979 (1998).

- [16] R. Mohanta, A. K. Gin, M. P. Khanna, and M. Ishida, Prog. Theor. Phys. 102, 645 (1999).
- [17] H. Y. Cheng, C. Y. Cheung, G. L. Lin, Y. C. Lin, T. M. Yan, and H. L. Yu, Phys. Rev. D 51, 1199 (1995); H. Y. Cheng and C. K. Chua, Phys. Rev. D 69, 094007 (2004).
- [18] C. K. Chua, X. G. He, and W. S. Hou, Phys. Rev. D **60**, 014003 (1999).
- [19] T. Hurth, Rev. Mod. Phys. 75, 1159 (2003), and references therein.
- [20] D. Acosta *et al.* (CDF Collaboration), Phys. Rev. D 66, 112002 (2002).
- [21] L. Oliver, J. C. Raynal, and R. Sinha, Phys. Rev. D 82, 117502 (2010).
- [22] A. Fridman and R. Kinnunen, CERN-PPE/93-61, Contribution to the 5th International Symposium on Heavy Flavor Physics, Montreal, 1993.
- [23] G. Buchalla, A.J. Buras, and M.E. Lautenbacher, Rev. Mod. Phys. 68, 1125 (1996).
- [24] V. M. Braun, R. J. Fries, N. Mahnke, and E. Stein, Nucl. Phys. B589, 381 (2000).
- [25] Y. L. Liu and M. Q. Huang, Nucl. Phys. A821, 80 (2009).
- [26] Y. L. Liu and M. Q. Huang, Phys. Rev. D 80, 055015 (2009).
- [27] K. Nakamura *et al.* (Particle Data Group), J. Phys. G **37**, 075021 (2010).
- [28] D. Buskulic *et al.* (ALEPH Collaboration), Phys. Lett. B **384**, 449 (1996).
- [29] J. Abdallah *et al.* (DELPHI Collaboration), Eur. Phys. J. C 44, 299 (2005).
- [30] T. Aaltonen *et al.* (CDF Collaboration), Phys. Rev. D **80**, 072003 (2009).