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## Self-gravitating system made of axions

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We show that the inclusion of an axionlike effective potential in the construction of a self-gravitating system of scalar fields decreases its compactness when the value of the self-interaction coupling constant is increased. By including the current values for the axion mass m and decay constant  $f_a$ , we have computed the mass and the radius for self-gravitating systems made of axion particles. It is found that such objects will have asteroid size masses and radii of a few meters, thus a self-gravitating system made of axions could play the role of scalar mini-MACHOs and mimic a cold dark matter model for the galactic halo.

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The necessity of introducing dark matter (DM) as the main component of galactic matter has become a solid fact due to its observational support [1]. Nevertheless, the nature of DM is one of the most intriguing mysteries in physics. A large variety of particles have been considered as the main component of DM in the Universe and only a few of them are still considered as good prospects since they must fulfill several requirements [2]. Among the survivors, the neutralino and the axion are leading candidates [3]. The question we address in the present work is the following: If DM is mainly composed of axions, what type of astrophysical objects will the axions form?

In order to answer this question, we have solved the Einstein-Klein-Gordon (EKG) equations in the semiclassical limit. The source for the Einstein equations is the mean value of the energy-momentum tensor operator  $\langle \hat{T}^{\mu\nu} \rangle$  of a real, quantized scalar field constructed with potential energy density given by [4]

$$V(\phi) = m^2 f_a^2 \left[ 1 - \cos\left(\frac{\phi}{f_a}\right) \right]. \tag{1}$$

It is found that the resulting self-gravitating system, the axion star, will have an asteroid-size mass ( $M \sim 10^{-16} M_{\odot}$ ) and radius of a few meters. This work improves our previous attempts [5,6] by solving numerically the EKG system for current allowed values for the axion mass m and decay constant  $f_a$  without the necessity of any interpolation. Our findings differ from previous estimates where the effect of the potential energy density was either neglected

[7] or was taken into account with a wrong sign in the self-interacting term of the potential [8,9]. In the first case, it is known that there is a maximum mass for such self-gravitating system given by  $M_{\rm max}=0.633m_p^2/m$ , where m is the mass associated with the scalar field and  $m_p$  is the Planck mass. For the allowed values of the axion mass,  $10^{-5}~{\rm eV} < m < 10^{-3}~{\rm eV}$  [4,10], the maximum mass for a self-gravitating system with the potential energy density (1) neglected lies in the range  $10^{-8}M\odot < M_{\rm max}^{\rm axionstar} < 10^{-5}M\odot$ . On the other hand, when the axion is considered to have a repulsive self-interacting term, instead of the attractive one given by (1), the maximum mass will be as big as  $M\sim 10^4 M\odot$ .

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Here we solve the EKG system including a Taylor expansion of the potential energy density (1) and we observe that its inclusion tends to decrease the mass and consequently the compactness of the self-gravitating system made of axions. Because of the smallness of the axion star's masses they could play the role of scalar field mini-MACHOs [11] and they will be the final state of axion miniclusters [12] originated in the early Universe at the QCD epoch [13]. Assuming that the axion is the main component of DM, the galactic halo will be a collisionless ensemble of axion stars and will be indistinguishable to the standard CDM scenario since N-body simulations of CDM with ultrahigh resolution are insensitive to particle mass granularity smaller than  $10^5 M_{\odot} - 10^3 M_{\odot}$  [14,15].

The paper is organized as follows: In Sec. I, the EKG equations for a real, quantized scalar field with a Taylor expansion of the potential energy density (1) are obtained and are solved for arbitrary values of the axion mass m and the decay constant  $f_a$ . In Sec. II we include the current values of m and  $f_a$  and we obtain the mass and radius of the axion stars. We finish Sec. II by commenting on some consequences derived in the case that the axion star has the properties calculated here.

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# I. EINSTEIN-KLEIN-GORDON WITH AN AXIONLIKE POTENTIAL

Since axions are real scalar particles, it is very useful to remember how self-gravitating systems made of spin zero particles are constructed. We will follow the method developed by Ruffini and Bonazzola [16]. The self-gravitating system arises as a solution of the EKG equations:

$$G_{\mu\nu} = 8\pi G < \hat{T}_{\mu\nu} >, \tag{2}$$

$$\left(\Box - \frac{dV(\Phi)}{d\Phi^2}\right)\Phi = 0,\tag{3}$$

where  $\Box = (1/\sqrt{-g})\partial_{\mu}[\sqrt{-g}g^{\mu\nu}\partial_{\nu}]$  and  $V(\phi)$  are the scalar field potential. Here <...> denotes an average over the ground state of a system of many particles. Its presence refers to the fact that we are working in the semiclassical limit of Einstein's equations. We will work with units where  $c = \hbar = 1$ . In the case of a spherically symmetric, static space-time described by

$$ds^{2} = B(r)dt^{2} - A(r)dr^{2} - r^{2}(\sin^{2}\theta d\phi^{2} + d\theta)$$
 (4)

has shown that such self-gravitating systems are fully characterized by the scalar field properties, i.e. the mass m of the scalar field and its energy density potential  $V(\Phi)$  [9,17]. The total mass of the resulting object and the typical radius depend mainly on these two properties of the scalar field. The axion is no exception. To deal with the quantum nature of the axion field, we have to compute the average  $\langle \hat{T}^{\mu\nu} \rangle$  in Eq. (2). What is usually done is to quantize the scalar field  $\Phi \to \hat{\Phi} = \hat{\Phi}^+ + \hat{\Phi}^-$  where

$$\hat{\Phi}^{+} = \sum_{nlm} \mu_{nlm}^{+} R_{nl}(r) Y_{m}^{l}(\theta, \psi) e^{-iE_{n}t}$$

$$\hat{\Phi}^{-} = \sum_{nlm} \mu_{nlm}^{-} R_{nl}(r) Y_{m}^{l*}(\theta, \psi) e^{+iE_{n}t}$$
(5)

and  $\mu_{nlm}^{+(-)}$  are the usual creation (annihilation) operators for a particle with angular momentum l, azimuthal momentum m and energy  $E_n$ . These operators satisfy the usual commutation relations  $[\mu_{nlm}^+, \mu_{n'l'm'}^+] = [\mu_{nlm}^-, \mu_{n'l'm'}^-] = 0$  and  $[\mu_{nlm}^+, \mu_{n'l'm'}^-] = \delta_{nn'}\delta_{ll'}\delta_{mm'}$ . With the operator  $\hat{\Phi}$ , it is now possible to construct the energy-momentum tensor operator  $\hat{T}_{\mu\nu}$  just by inserting the operator  $\hat{\phi}$  into the classical expression for the energy-momentum tensor

$$T^{\mu}_{\nu} = g^{\mu\sigma}\partial_{\sigma}\phi\partial_{\nu}\phi - \frac{1}{2}\delta^{\mu}_{\nu}g^{\lambda\sigma}\partial_{\lambda}\phi\partial_{\sigma}\phi - \delta^{\mu}_{\nu}V(\phi). \tag{6}$$

The average  $\langle Q|\hat{T}_{\mu\nu}|Q\rangle$  is done by considering a state  $|Q\rangle$  for which all N particles are in the ground state  $(l=m=0,\ n=1)$ . The ground state satisfies  $\mu_{100}^-|Q\rangle=0$ . This procedure, as pointed out in [16], cancels all time dependence on the vacuum expectation value  $\langle Q|\hat{T}_{\mu\nu}|Q\rangle$  and, for the case of a free scalar field  $(V(\Phi)=\frac{m^2}{2}\Phi^2)$ , the real

quantized scalar field yields the same field equations as those obtained by using a classical complex scalar field. At this level, the self-gravitating system for a real quantized scalar field does not differ from a complex classical scalar field, hence, a real quantized scalar field does not produce the so-called "oscillations" [18], which are time-dependent. In our case we are interested in the axion-potential (1). In order to compute  $\langle \hat{T}^{\mu\nu} \rangle$ , we perform a Taylor expansion of (1), i.e.,

$$V(\Phi) \sim \frac{m^2}{2} \Phi^2 - \frac{1}{4!} \frac{m^2}{f_a^2} \Phi^4 + \frac{1}{6!} \frac{m^2}{f_a^4} \Phi^6 - \dots$$
 (7)

We will show that the final results do not depend strongly on the number of terms considered in the Taylor expansion of (1). The relevant term that should be considered is the self-interacting term  $\Phi^4$  and the sign it carries with itself, which differs from the one considered in Boson Stars (BS) [8]. With the potential (7), it is possible to compute  $\langle \hat{T}^{\mu}_{\nu} \rangle$  by performing the quantization and averaging procedure previously discussed. The computed average of the stress energy tensor is

$$\langle T_0^0 \rangle = -\frac{E^2 R^2}{2B} - \frac{R'^2}{2A} - \frac{m^2 R^2}{2} + \frac{m^2 R^4}{12 f_a^2} - \frac{m^2 R^6}{144 f_a^4} + \dots,$$

$$\langle T_1^1 \rangle = \frac{E^2 R^2}{2B} + \frac{R'^2}{2A} - \frac{m^2 R^2}{2} + \frac{m^2 R^4}{12 f_a^2} - \frac{m^2 R^6}{144 f_a^4} + \dots,$$

$$\langle T_2^2 \rangle = \frac{E^2 R^2}{2B} - \frac{R'^2}{2A} - \frac{m^2 R^2}{2} + \frac{m^2 R^4}{12 f_a^2} - \frac{m^2 R^6}{144 f_a^4} + \dots.$$

$$(8)$$

We have dropped all subindexes since, as we have already pointed out, we will assume that the axion is in its ground state. We can observe that there is no time dependence in (8). Furthermore, there are new numerical factors that appear due to the averaging performed in  $\hat{T}_{\mu\nu}$  [19]. For instance,  $\langle \Phi^4 \rangle = 2R^4$  and  $\langle \Phi^6 \rangle = 5R^6$  in such a way that we cannot recover the original  $\cos(\Phi/f_a)$  from which we departed. Following a similar procedure, but now applied to the scalar wave Eq. (3), with a potential (7) and the spherically symmetric metric (4), the Einstein-Klein-Gordon system is obtained:

$$\frac{A'}{A^2r} + \frac{1}{r^2} \left( 1 - \frac{1}{A} \right) = -8\pi G \langle T_0^0 \rangle,$$

$$\frac{B'}{ABr} - \frac{1}{r^2} \left( 1 - \frac{1}{A} \right) = 8\pi G \langle T_1^1 \rangle,$$

$$R'' + \left( \frac{2}{r} + \frac{B'}{2B} - \frac{A'}{2A} \right) R' + A \left[ \left( \frac{E^2}{B} - \frac{m^2}{2} \right) R \right]$$

$$+ \frac{m^2 R^3}{6f_a^2} - \frac{m^2 R^5}{48f_a^4} = 0.$$
(9)

Following standard definitions [8], we rewrite the system (9) in dimensionless variables: x = rm,  $R = \sigma/\sqrt{4\pi G}$  and

 $\tilde{B} = m^2 B/E^2$ , and we have found it convenient to define the dimensionless self-interaction term

$$\Lambda = \frac{1}{24\pi} \left( \frac{m_p}{f_a} \right)^2. \tag{10}$$

By imposing regularity at the origin and flatness at infinity, system (9) is solved using a shooting method. Even though the set of Eqs. (9) is very similar to the case for typical BS, [8], the behavior we found for the family of solutions with zero-nodes is completely different. A full set of equilibrium configurations is shown in Fig. 1, where the gravitational mass is plotted for different values of  $\sigma(0)$  and  $\Lambda$ . The equilibrium configurations have a maximum mass  $M_{\rm max}$  at some  $\sigma(0)=\sigma_c$  for each value of  $\Lambda$ . But the switch in the potential sign of the  $\Phi^4$  term produces a significant change in the behavior of  $M_{\text{max}}$  in comparison with standard BS [8]. The relation  $M_{\rm max} \sim \Lambda^{1/2}$  is no longer satisfied. Instead of increasing  $M_{\rm max}$  as we increase the value of  $\Lambda$ , we found a decreasing  $M_{\text{max}}$ . This effect is expected since instead of adding a repulsive interaction between the particles of the system, the change in the sign due to the cosinelike potential (1) implies an attractive potential. Thus the total number of particles needed to form an equilibrium configuration that balance the gravitational collapse against the quantum pressure is lower than the case of a repulsive potential. One can think that this effect is apparent and as soon as the complete potential (1) is implemented in the EKG system, a different behavior would be seen. But the decrease in the mass of the equilibrium configurations is a robust behavior. The masses of equilibrium configurations including up to the fourth power of  $\Phi$  in the Taylor series are plotted also in Fig. 1, illustrating this robustness.

The bigger the value of  $\Lambda$ , the lower the differences on the masses. This is because when  $\Lambda$  is increased,  $\sigma_c$  decreases (and equivalently  $\Phi(r)$  where we are interested).

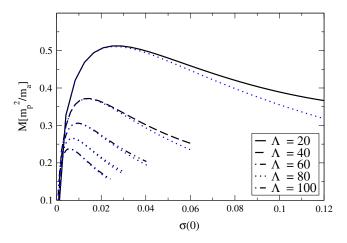


FIG. 1 (color online). Gravitational mass as a function of the central value of the scalar field  $\sigma(0)$  for different values of  $\Lambda$ . Dotted lines include only an expansion of the axion-potential up to the term  $\Phi^4$ .

Then, the true expansion parameter of (1) is  $\Lambda\Phi$ , and it is always a small parameter. Another interesting issue is that the dependence of the radius  $R_{99}$  (defined as the radius where 99% of the total gravitational mass is reached) on the value of  $\Lambda$  is weak, as it is shown in upper panel of Fig. 2. Combining the invariance of the radius as  $\Lambda$  increases, with the decrease in the mass, means that the self-gravitating system made of a scalar field that has an axionlike potential has a lower compactness  $(2M/R_{99})$  as the self-interaction term increases. This "Newtonization" of the system is shown on the lower panel of Fig. 2.

### II. AXION STAR

The previous results were obtained assuming arbitrary values of the mass m of the scalar field associated with the axion as well as free values for the decay constant  $f_a$ . But the mass of the axion is constrained by astrophysical and cosmological considerations to lie in the range  $10^{-5}$  eV  $\leq m \leq 10^{-3}$  eV and the decay constant is related to the axion mass by  $m = 6\mu \text{eV}\left(\frac{10^{12} \text{ GeV}}{f_a}\right)$  [4,20]. With these two restrictions we have  $10^{13} < \Lambda < 10^{17}$  and then, the previous selection of dimensionless variables  $\{x, \sigma, A.\tilde{B}\}$  is now inadequate in order to numerically solve the system (9). After some frustrated attempts, we found that a more suitable set of variables to solve the system (9) is the following:

$$R = \frac{f_a}{\sqrt{m}}\sigma, \qquad r = \frac{m_p}{f_a}\sqrt{\frac{m}{4\pi}}x, \qquad \frac{1}{\tilde{B}} = \frac{E^2}{m^2B}.$$
 (11)

Since  $\Lambda > 1$ , it is natural to think that the resulting axion star will have a small compactness and low mass. So, besides the change in variables (11), it is convenient to solve for a(x) = 1 - A(x). Solving the system (9) for the new set of variables  $\{x, \sigma(x), a(x), \tilde{B}(x)\}$  we obtained

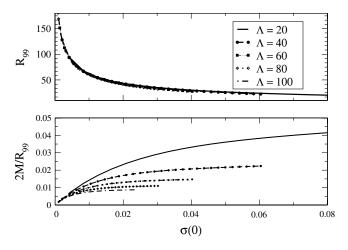


FIG. 2 (color online).  $R_{99}$  and compactness for different configurations. The dependence of  $R_{99}$  on  $\Lambda$  is negligible. For a given value of  $\sigma(0)$ , the compactness decreases as  $\Lambda$  increases.

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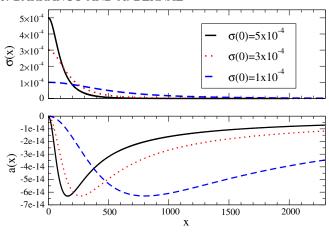


FIG. 3 (color online). Scalar field and potential for a typical axion star with different values of  $\sigma(0)$  and an axion mass of  $m_a = 1.0 \times 10^{-5}$  eV.

typical nodeless configurations for these axion stars. Some of them are shown in Fig. 3, where we have taken axion mass  $m = 10^{-5}$  eV. The total gravitational mass and the radius  $R_{99}$ , both in physical units, for those configurations are shown in Table I.

A possible scenario emerges with the hypothesis that DM is mainly composed by axions. As already pointed out by Kolb and Tkachev [12], nonlinear effects in the evolution of the axion field in the early Universe may lead to the formation of "axion miniclusters". These miniclusters may relax, due to the collisional  $2a \rightarrow 2a$  process or by gravitational cooling [21], and they will evolve to a BS. In the present work we have constructed those BSs for axion particles by solving the EKG system for a real quantized scalar field which is regulated by an axion-potential (1). These self-gravitating systems, the axion stars, have very small masses and radii of meters (Table I) and consequently very low compactness. The resulting densities are not enough to produce stimulated decays of the axion to photons since they occur when  $\Gamma_{\pi} m_p^2 V_e f_{\pi}/(R m_{\pi}^4 f_a) >$ 1 which implies densities  $\rho > 10^{15} \text{ Kg/m}^3$  for m = $10^{-5}$  eV [21,22]. Typical densities for axion stars are shown in Table I.

The galactic halo will be an ensemble of axion stars, and this picture is not in contradiction with observations since the size of axions stars fit into the limits coming from microlensing or gravothermal instability [11]. Previous studies that construct models for galactic dark matter halos out of scalar fields assume that each galactic halo is a

TABLE I. Masses and  $R_{99}$  for the configurations shown in Fig. 3.

$\sigma(0)$	Mass (Kg)	R <sub>99</sub> (meters)	density $\rho$ (Kg/m <sup>3</sup> )
$5 \times 10^{-4}$	$3.90 \times 10^{13}$	1.83	$6.3 \times 10^{12}  2.7 \times 10^{12}  3.1 \times 10^{11}$
$3 \times 10^{-4}$	$6.48 \times 10^{13}$	2.86	
$1 \times 10^{-4}$	$1.94 \times 10^{14}$	8.54	

spherical Bose-Einstein condensate made of an ultralight scalar field [23–28]. In the present work, the axion stars will play the role of the scalar field mini-MACHOs, that is, a scenario where the scalar field (the axion) form a large number of stable asteroid-sized scalar condensations which end up clustering into structures similar to CDM halos with all their advantages. The stability of structures made of scalar fields have been extensively studied [29–31], and those analyses could be extended to our case with potential energy density given by (1).

Furthermore, axion stars present similar characteristics to the recently proposed neutralino stars [32], with the advantage that they could survive longer periods of time [33].

If DM is distributed as axion stars, their detection will be very difficult. The proposed femtolensing to detect axion compact objects [34] is close to its lower detectable limit. Another related issue is the low number of axion stars around the earth. Assuming for instance a Navarro-Frenk-White profile for the galactic halo, and a local halo density of 0.3 GeV/cm<sup>3</sup> around the Sun, there will be  $\sim$ 1 axion star in the volume cover between Jupiter and the Sun. Nevertheless, another axion property can shed light on the axion, such as the conversion of axions into photons in the presence of strong magnetic fields [35]. Collisions of axion stars with neutron stars [36] will produce flashes of light that could be detected by Gamma ray Observatories [37]. A more detailed analysis of these ideas, together with a more detailed study of the stability of the axion stars, could help us to determine if DM is mainly composed by scalar field particles as the axions.

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