# **Discrete dark matter**

M. Hirsch,<sup>\*</sup> S. Morisi,<sup>†</sup> E. Peinado,<sup>‡</sup> and J. W. F. Valle<sup>§</sup>

AHEP Group, Institut de Física Corpuscular—C.S.I.C./Universitat de València, Edificio Institutos de Paterna,

Apartado 22085, E-46071 Valencia, Spain

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We propose a new motivation for the stability of dark matter (DM). We suggest that the same non-Abelian discrete flavor symmetry which accounts for the observed pattern of neutrino oscillations, spontaneously breaks to a  $Z_2$  subgroup which renders DM stable. The simplest scheme leads to a scalar doublet DM potentially detectable in nuclear recoil experiments, inverse neutrino mass hierarchy, hence a neutrinoless double beta decay rate accessible to upcoming searches, while  $\theta_{13} = 0$  gives no *CP* violation in neutrino oscillations.

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## I. INTRODUCTION

The existence of dark matter (DM) plays a central role in the modeling of structure formation and galaxy evolution, affecting also the cosmic microwave background. Despite the strong evidence in favor of DM, its detailed nature remains rather elusive. Viable particle physics candidates for dark matter must be electrically neutral and provide the correct relic abundance. Therefore they must be stable over cosmological time scales. A simple way to justify the stability of the DM is by *assuming* some parity symmetry  $Z_2$ , which might arise from the spontaneous breaking of an Abelian U(1) gauge symmetry [1-3],<sup>1</sup> or from a non-Abelian discrete symmetry, as might be the case in some string models [4].

Non-Abelian discrete symmetries are motivated by neutrino oscillation data [5,6]. Here we propose that the same symmetry explaining neutrino mixing angles is also responsible for the dark matter stability. In our simplest type-I seesaw [7] realization the flavor symmetry  $A_4$  spontaneously breaks to  $Z_2$  providing a stable DM candidate. We extend the scalar sector of the standard model by adding three Higgs doublets transforming as a triplet of  $A_{4}$ . We show that there is a consistent pattern of vacuum expectation values (VEVs) for which only one of the three extra Higgs doublets takes a VEV, while the other two give rise to the dark matter candidate. The model accounts for the observed pattern of mixing angles [8] indicated by current neutrino oscillation data, predicting  $\theta_{13} = 0$  and inverted spectrum of neutrino masses. It will therefore be tested in upcoming double beta and neutrino oscillation searches [9], while the dark matter has potentially detectable rates within reach of nuclear recoil experiments.

<sup>1</sup>In supersymmetry a viable DM particle is the neutralino, whose stability stems from the imposition of the so-called R parity.

### **II. MODEL**

We assign matter fields to irreducible representations of  $A_4$ , the group of even permutations of four objects, isomorphic to the symmetry group of the tetrahedron. All elements are generated from two elements S and T with  $S^2 = T^3 = (ST)^3 = I$ .  $A_4$  has four irreducible representations, three singlets 1, 1', and 1", and one triplet. In the basis where S is real diagonal,

$$S = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}; \qquad T = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}; \quad (1)$$

one has the following triplet multiplication rules,

$$(ab)_{1} = a_{1}b_{1} + a_{2}b_{2} + a_{3}b_{3};$$

$$(ab)_{1'} = a_{1}b_{1} + \omega a_{2}b_{2} + \omega^{2}a_{3}b_{3};$$

$$(ab)_{1''} = a_{1}b_{1} + \omega^{2}a_{2}b_{2} + \omega a_{3}b_{3};$$

$$(ab)_{3_{1}} = (a_{2}b_{3}, a_{3}b_{1}, a_{1}b_{2});$$

$$(ab)_{3_{2}} = (a_{3}b_{2}, a_{1}b_{3}, a_{2}b_{1}),$$

$$(ab)_{3_{2}} = (a_{3}b_{2}, a_{1}b_{3}, a_{2}b_{1}),$$

where  $\omega^3 = 1$ ,  $a = (a_1, a_2, a_3)$ , and  $b = (b_1, b_2, b_3)$ . We assign the standard model Higgs doublet *H*, to the singlet 1, and we assume three additional Higgs doublets transforming as an  $A_4$  triplet, namely,  $\eta = (\eta_1, \eta_2, \eta_3) \sim 3$ . We have four right-handed neutrinos, three transforming as an  $A_4$  triplet  $N_T = (N_1, N_2, N_3)$ , and one singlet  $N_4$ . The lepton and Higgs assignments of our model are given in Table I. The resulting Yukawa Lagrangian is

TABLE I. Summary of relevant model quantum numbers.

	$L_e$	$L_{\mu}$	$L_{\tau}$	$l_e^c$	$l^c_\mu$	$l^c_{ au}$	$N_T$	$N_4$	Η	η
SU(2)	2	2	2	1	1	1	1	1	2	2
$A_4$	1	1'	1''	1	$1^{\prime\prime}$	1'	3	1	1	3

<sup>\*</sup>mahirsch@ific.uv.es

<sup>&</sup>lt;sup>†</sup>morisi@ific.uv.es

<sup>&</sup>lt;sup>‡</sup>epeinado@ific.uv.es

<sup>&</sup>lt;sup>§</sup>valle@ific.uv.es

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$$\begin{aligned} \mathcal{L} &= y_e L_e l_e^c H + y_\mu L_\mu l_\mu^c H + y_\tau L_\tau l_\tau^c H + y_1^\nu L_e (N_T \eta)_1 \\ &+ y_2^\nu L_\mu (N_T \eta)_{1''} + y_3^\nu L_\tau (N_T \eta)_{1'} + y_4^\nu L_e N_4 H \\ &+ M_1 N_T N_T + M_2 N_4 N_4 + \text{H.c.} \end{aligned}$$

This way H is responsible for quark and charged lepton masses, the latter automatically diagonal. Note that we do

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not discuss the quark sector, assumed to be blind to  $A_4$ , namely, all left- and right-handed up- and down-type quarks transform trivially under  $A_4$ ; their mass and mixing hierarchies might arise from an extra family symmetry, for example, Frogatt-Nielsen-like [10]. Neutrino masses arise from H and  $\eta$ , see below. The relevant terms of the scalar potential are of the form

$$V = \mu_{\eta}^{2} \eta^{\dagger} \eta + \mu_{H}^{2} H^{\dagger} H + \lambda_{1} [H^{\dagger} H]^{2} + \lambda_{2} [\eta^{\dagger} \eta]_{1}^{2} + \lambda_{3} [\eta^{\dagger} \eta]_{1'} [\eta^{\dagger} \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1'} [\eta \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1'} [\eta \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} [\eta^{\dagger} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} [\eta^{\dagger} \eta^{\dagger}]_{1''} [\eta^{\dagger} \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} [\eta^{\dagger} \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} \eta^{\dagger} \eta]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1'''} + \lambda_{4} [\eta^{\dagger} \eta^{\dagger}]_{1'''} + \lambda_{4} [\eta^{\dagger}$$

where *i*, *j* = 1, 2, and the product of two triplets contracted into a triplet of  $A_4$ , see Eq. (2);  $[\cdots]_1$  means the product of two triplets contracted into a singlet of  $A_4$  and so on. Note that  $[\eta^{\dagger}\eta]_{1,1',1''} \equiv [\eta\eta^{\dagger}]_{1,1',1''}$ ,  $[\eta\eta]_{3_1} \equiv [\eta\eta]_{3_2}$ , and so on.

We have studied the minimization of the potential V solving the equations  $\partial V / \partial v_i = 0$ , where  $v_i$  are the VEVs of the fields H,  $\eta_1$ ,  $\eta_2$ , and  $\eta_3$ . For simplicity we assume real VEVs. We have checked that for suitable parameter choices of the potential V, an allowed local minimum is

$$\langle H^0 \rangle = v_h \neq 0, \qquad \langle \eta_1^0 \rangle = v_\eta \neq 0 \qquad \langle \eta_{2,3}^0 \rangle = 0, \quad (4)$$

with the eigenvalues of the Hessian  $\partial^2 V / \partial v_i \partial v_j$  all positive.

Note that the alignment  $\langle \eta \rangle \sim (1, 0, 0)$  breaks spontaneously  $A_4$  to  $Z_2$  since (1, 0, 0) is invariant under the S generator in Eq. (1). The  $Z_2$  is defined as

$$N_2 \to -N_2, \qquad h_2 \to -h_2, \qquad A_2 \to -A_2, N_3 \to -N_3, \qquad h_3 \to -h_3, \qquad A_3 \to -A_3.$$
(5)

This residual symmetry is responsible for the stability of our DM candidate and the stability of the minimum. Note that the potential cannot break spontaneously  $A_4$  into  $Z_3$ because in this case the alignment  $\langle \eta \rangle \sim (1, 1, 1)$  is not a minimum unless a fine-tuning in the parameters  $\lambda_9 + \lambda_{10} = 0$  is assumed. This attractive feature reminds one of the inert doublet model [11], with the difference that here it follows naturally from the underlying flavor symmetry which accounts for neutrino oscillations.

We have four Higgs doublets<sup>2</sup> giving three physical charged scalar bosons, plus four neutral scalars, and three pseudoscalars. After electroweak symmetry breaking we can write

$$H = \begin{pmatrix} 0 \\ v_h + h \end{pmatrix}, \qquad \eta_1 = \begin{pmatrix} \eta_1^+ \\ v_\eta + h_1 + iA_1 \end{pmatrix}, \qquad (6)$$
$$\eta_2 = \begin{pmatrix} \eta_2^+ \\ h_2 + iA_2 \end{pmatrix}, \qquad \eta_3 = \begin{pmatrix} \eta_3^+ \\ h_3 + iA_3 \end{pmatrix}.$$

There are 3 physical charged scalar bosons, 4 *CP* even and 3 *CP* odd neutral scalars. The mass of the neutral scalar fields is block diagonal with the standard model Higgs h mixed with  $h_1$ , but not with the scalar fields with zero VEVs  $h_{2,3}$ .

#### **III. DARK MATTER**

The lightest combination of the stable scalar fields  $h_2$ ,  $h_3$  plays the role of our dark matter particle, which we will denote generically by  $\eta_{\text{DM}}$ . We list below all interactions of  $\eta_{\text{DM}}$ :

(1) Yukawa interactions:

$$\eta_{\rm DM}\bar{\nu}_i N_{2,3},\tag{7}$$

where  $i = e, \mu$ , and  $\tau$ .

(2) Higgs-vector boson couplings:

$$\eta_{\rm DM} \eta_{\rm DM} ZZ, \qquad \eta_{\rm DM} \eta_{\rm DM} WW, \eta_{\rm DM} \eta_{2,3}^{\pm} W^{\pm} Z, \qquad \eta_{\rm DM} \eta_{2,3}^{\pm} W^{\pm}, \qquad (8) \eta_{\rm DM} A_{2,3} Z.$$

(3) Scalar interactions from the Higgs potential:

$$\eta_{\rm DM} A_1 A_2 h, \qquad \eta_{\rm DM} A_1 A_3 h_1, \qquad \eta_{\rm DM} A_1 A_2 h_1, \eta_{\rm DM} A_1 A_3 h, \qquad \eta_{\rm DM} A_2 A_3 h_3, \qquad \eta_{\rm DM} h_1 h_3 h,$$
(9)  
 
$$\eta_{\rm DM} \eta_{\rm DM} hh, \qquad \eta_{\rm DM} \eta_{\rm DM} h_1 h_1.$$

After electroweak symmetry breaking, the VEVs  $v_h$  and  $v_\eta$  are generated, so that additional terms are obtained from those in Eq. (9) by replacing  $h \rightarrow v_h$  and  $h_1 \rightarrow v_\eta$ . The flavor symmetry  $A_4$  is broken down to the residual  $Z_2$ 

<sup>&</sup>lt;sup>2</sup>Lepton flavor violating processes are suppressed by the large right-handed neutrino scale.

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symmetry in Eq. (5), implying the stability of our dark matter candidate. As we will see, despite the many mass and coupling parameters appearing in the potential, Eq. (3), for  $M_{\eta} \gg M_z$ , only two determine the relic dark matter abundance and its direct detection rates.

## **IV. RELIC DENSITY**

Assuming that our DM candidate arises as thermal relic in the early universe, one of the most important requirements one must check is its relic abundance. For definiteness we require that  $\eta_{\text{DM}}$  makes up all the observed DM. For  $M_{\eta} \gg M_z$  the most important annihilation and coanihilation processes are those with vector bosons, though for large  $\lambda \ge g_2$ , where  $16\lambda^2 = (\lambda_7 + \lambda'_7 + 2\lambda_8)^2 + (2\lambda_2 - \lambda_3 - 2\lambda_4 + \lambda'_4 + 2\lambda_5 + \lambda'_5 + \lambda_6)^2$ , annihilation into Higgs bosons plays an important role; see Eq. (11). The DM abundance can be approximated as [12]

$$\frac{n_{\rm DM}(T)}{s(T)} \approx \sqrt{\frac{180}{\pi g_*}} \frac{1}{M_{\rm Pl} T_f \langle \sigma_A v \rangle},\tag{10}$$

where  $\frac{M_{\eta}}{T_f} \approx 26$  and  $g_* = 106.75 + n$  is the number of standard model (SM) degrees of freedom plus  $1 \le n \le 12$  degrees of freedom arising from the extra scalars, and  $M_{\rm Pl} = 1.22 \times 10^{19}$  GeV is the Planck scale. The cross section for  $\eta_{\rm DM} \eta_{\rm DM} \rightarrow VV$ , where V are vector bosons in the limit of massless final states, is given by [12]

$$\langle \sigma_A v \rangle \simeq \frac{3g_2^4 + g_Y^4 + 6g_2^2 g_Y^2 Y^2 + 4\lambda^2}{256\pi M_n^2},$$
 (11)

where Y = 1/2 is the weak hypercharge,  $g_2 = \sqrt{4\pi\alpha/(1 - M_W^2/M_Z^2)}$ , and  $g_Y = \sqrt{4\pi\alpha}M_Z/M_W$ . From these equations it follows that, in order to provide the correct relic abundance  $\Omega_{\rm DM}h^2 = 0.110 \pm 0.006$ , i.e.,  $n_{\rm DM}/s = (0.40 \pm 0.02) \text{ eV}/M_{\eta}$  [13], a correlation between the mass of the dark matter  $M_{\eta}$  and the quartic coupling constant  $\lambda$  is required. For simplicity if we take the limit of small  $\lambda$  we obtain a mass for the DM candidate of  $M_{\eta} \approx 0.51$  TeV. For large  $\lambda$  values we have that the DM mass  $M_{\eta}$  scales as  $\lambda$ .

#### **V. DIRECT DETECTION**

The quartic couplings  $\eta^{\dagger} \eta H^{\dagger} H$  and  $\eta^{\dagger} \eta^{\dagger} H H$  give an interaction of the DM candidate with the nucleon through the interchange of the SM Higgs boson. Hence our DM candidate can be detected through the elastic scattering with a nucleus  $\eta_{\text{DM}} N \rightarrow \eta_{\text{DM}} N$  via the exchange of a Higgs, or through inelastic scattering with a nucleus  $\eta_{\text{DM}} N \rightarrow AN$  with the exchange of a Z boson, see Fig. 1, where A is the lightest pseudoscalar, in general a mixture of  $A_2$  and  $A_3$ .

Barring fine-tuned choices of parameters for which the threshold for inelastic scattering opens up, the detection



FIG. 1. Feynman diagrams relevant for direct DM detection. Elastic scattering (left panel) is generically more important than inelastic (right panel).

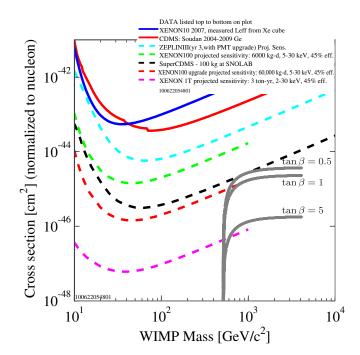


FIG. 2 (color online). Elastic DM scattering cross section with a nucleon versus DM mass. We compare present [20,21] and future [22,23] sensitivities with our model expectations, for  $m_H = 120$  GeV and  $\tan\beta = 0.5$ , 1, 5 (gray solid lines).

will be dominated by the elastic process, whose cross section is given by [14]

$$\sigma_{\rm el}(\rm nucleon) \approx \lambda^2 \frac{1}{1 + (\tan\beta)^2} \left(\frac{100 \text{ GeV}}{M_h}\right)^4 \\ \times \left(\frac{50 \text{ GeV}}{M_\eta}\right)^2 (5 \times 10^{-42} \text{ cm}^2), \quad (12)$$

where  $\tan\beta = v_h/v_\eta$ . Note that all uncertainties associated with the nuclear form factor in Eq. (12) have been neglected. From the requirement of correctly reproducing the relic density, Eqs. (10) and (11), one can find an expression for  $\lambda$  as function of the DM mass,  $M_\eta$ . Using this relation and Eq. (12) one can plot the estimated cross section for the direct detection for each value of  $\tan\beta$  and mass of the Higgs,  $M_h$ , as illustrated in Fig. 2.<sup>3</sup> The figure has been generated using [15] and compares the experi-

<sup>&</sup>lt;sup>3</sup>Here we focus on the region  $M_{\eta} \gg M_z$ . The interesting case of light DM will be treated elsewhere.

mental sensitivities with our model expectations, fixing  $m_H = 120$  GeV and three tan $\beta$  values. This choice of Higgs mass is motivated by the LEP bounds  $m_H > 114$  GeV, which however is not strictly valid in our model due to the additional Higgs doublets.

## VI. NEUTRINO PHENOMENOLOGY

Our model has four heavy right-handed neutrinos, and is a special case, called (3,4), of the general type-I seesaw mechanism [16]. After electroweak symmetry breaking, it is characterized by Dirac and Majorana mass terms given as

$$m_D = \begin{pmatrix} x_1 & 0 & 0 & y_1 \\ x_2 & 0 & 0 & 0 \\ x_3 & 0 & 0 & 0 \end{pmatrix},$$
(13)  
$$M_R = \operatorname{diag}(M_1, M_1, M_1, M_2),$$

so that the light neutrinos get Majorana mass by means of the type-I seesaw relation  $m_{\nu} = -m_{D_{3\times4}}M_{R_{4\times4}}^{-1}m_{D_{3\times4}}^{T}$ , the light-neutrinos mass matrix  $M_{\nu}$  being given as

$$\begin{pmatrix} x_1^2 + y_1^2 & x_1x_2 & x_1x_3 \\ \overline{M_1} & \overline{M_1} & \overline{M_1} \\ \frac{x_1x_2}{\overline{M_1}} & \frac{x_2^2}{\overline{M_1}} & \frac{x_2x_3}{\overline{M_1}} \\ \frac{x_1x_3}{\overline{M_1}} & \frac{x_2x_3}{\overline{M_1}} & \frac{x_3^2}{\overline{M_1}} \end{pmatrix} = \begin{pmatrix} y^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{pmatrix}.$$
 (14)

It falls within the class of scaling matrices introduced in Ref. [17]. This form of the light neutrino mass matrix has an inverse hierarchical neutrino mass spectrum and a zero eigenvalue with  $m_3 = 0$  and corresponding eigenvector  $(0, -c/b, 1)^T$  implying a vanishing reactor mixing angle  $\theta_{13} = 0$ . One can see explicitly that the solar and atmospheric square mass differences and mixing angles indicated by neutrino oscillation data [8] can indeed be fitted by taking, as an example, the tribimaximal (TBM) *ansatz* [18]. When b = c and  $y^2 = 2c^2 - ac$  the neutrino mass matrix Eq. (14) is  $\mu - \tau$  invariant yielding maximal at-

mospheric mixing,  $\sin^2 \theta_{23} = 1/2$  and  $M_{\nu,11} + M_{\nu,13} = M_{\nu,22} + M_{\nu,23}$ , which gives the TBM value of the solar angle,  $\sin\theta_{12}^2 = 1/3$ , in good agreement with experimental data within  $1\sigma$ . The eigenvalues are  $\{m_1, m_2, m_3\} = \{2ac + 2c^2, 2c^2 - ac, 0\}$ , which can fit the two mass-squared differences required to account for the observed pattern of neutrino oscillations. By relaxing the condition b = c and  $y^2 = 2c^2 - ac$  one generates deviations from the TBM limit, while keeping  $\theta_{13} = 0$ . Note that the above implies a neutrinoless double beta decay effective mass parameter in the range 0.03 to 0.05 eV at  $3\sigma$ , within reach of upcoming experiments [19].

## **VII. CONCLUSIONS**

In summary we have suggested that DM stability follows from the same non-Abelian discrete flavor symmetry which accounts for the observed pattern of neutrino oscillations. In the realization we have given we have an  $A_4$  symmetry which spontaneously breaks to a  $Z_2$  parity that stabilizes a scalar doublet dark matter, potentially detectable in nuclear recoil experiments, as well as accelerators. Despite the complexity of the scalar potential, in the heavy dark matter limit both the relic dark matter abundance and its direct detection cross section depend just on the DM mass and a single coupling strength parameter. The model is also manifestly unifiable and agrees with electroweak searches as well as precision tests, as will be shown elsewhere. Our simple example gives  $0\nu\beta\beta$  rates accessible to upcoming experiments and no *CP* violation in neutrino oscillations.

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