New parton distributions from large-x and low- Q^2 data

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We report results of a new global next-to-leading order fit of parton distribution functions in which cuts on W and Q are relaxed, thereby including more data at high values of x. Effects of target mass corrections, higher twist contributions, and nuclear corrections for deuterium data are significant in the large-x region. The leading twist parton distributions are found to be stable to target mass correction model variations as long as higher twist contributions are also included. The behavior of the d quark as $x \rightarrow 1$ is particularly sensitive to the deuterium corrections, and using realistic nuclear smearing models the d -quark distribution at large x is found to be softer than in previous fits performed with more restrictive cuts.

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I. INTRODUCTION

The distribution of up and down quarks in the proton is one of the most fundamental characterizations of the structure of the ground state of QCD. Several decades of accumulated data from a variety of hard scattering processes, together with sophisticated, next-to-leading order QCD analyses, has produced a detailed mapping of the proton's parton distribution functions (PDFs) over a large range of kinematics [\[1](#page-12-0)[–4\]](#page-12-1).

A dominant role in this endeavor has been played by lepton-nucleon deep inelastic scattering (DIS) data, which provide direct information on the behavior of the quark PDFs, as well as on the gluon distribution via the observed logarithmic scaling violations and the imposition of the momentum sum rule on the PDFs. However, the kinematics of many deep inelastic experiments limits the coverage in Bjorken x, so that our knowledge of PDFs does not extend uniformly over the entire x-range, especially so at large x. The invariant mass squared of the produced hadronic system is given by

$$
W^2 = M^2 + Q^2 \left(\frac{1}{x} - 1\right),\tag{1}
$$

where M denotes the mass of the target nucleon and Q^2 the photon virtuality. As $x \to 1$ at fixed Q^2 , W approaches values in the nucleon resonance region. This region may be treated using the concept of quark-hadron duality [[5\]](#page-12-2), but this is beyond the scope of the present analysis. In order to simultaneously stay in the region of large W and access high values of x , one must therefore go to increased values of Q^2 ; in practice, though, this is limited by the available beam energy. Finally, the cross section falls rapidly as x and Q^2 increase, so the data samples can become statistics limited in this region.

Knowledge of PDFs at large x, defined here to be $x \geq$ 0:5, is important for a number of reasons. Apart from its intrinsic value in providing a laboratory for studying the flavor and spin dynamics of quarks, the large-x region is unique in allowing perturbative QCD predictions to be made for the x dependence of PDFs in the limit $x \rightarrow 1$ [\[6\]](#page-12-3). Furthermore, the d/u quark ratio at large x is very sensitive to different mechanisms of spin-flavor symmetry breaking in the nucleon [[7](#page-12-4)]. Reliable knowledge of PDFs at large x may also be important for searches of new physics signals in collider experiments, where uncertainties in PDFs at large x and low Q^2 percolate through Q^2 evolution to affect cross sections at smaller x and larger Q^2 [\[8\]](#page-12-5). This is especially true if the search involves a region where the rapidity is large, where one is sensitive to products of PDFs evaluated with one value of x being small and the other large. An example is provided by the planned PHENIX measurements of polarized gluon distributions Δg at small x by detecting W-bosons at large rapidity: since Δg is convoluted with large-x unpolarized quark distributions, the precision of the measurements will depend on the precision to which the quark PDFs are known at large x.

Nuclear PDFs at large x are also important in the analysis of neutrino oscillation experiments such as T2K [[9\]](#page-12-6), $NO\nu A$ [[10\]](#page-12-7), and DUSEL [\[11\]](#page-12-8). A large part of the theoretical uncertainty is due to lack of precise knowledge of the neutrino-nucleus interaction in the kinematics between the DIS and resonance regions, as well as in the implementation of the nonisoscalarity correction. Better control of nuclear corrections at large x and a precise knowledge of the d/u ratio will have a direct and measurable impact on the interpretation of such experiments. This analysis is also timely given the increasing base of large-x measurements available, including, among others, DIS data from Jefferson Lab, and Drell-Yan and W-asymmetry data from Fermilab.

In order to improve our knowledge of PDFs in the large- x region, and to thereby reduce their errors, in this work we expand the coverage in x provided by the deep inelastic data by relaxing the $W > 3.5$ GeV and $Q >$ 2 GeV cuts traditionally used to limit the theoretical analysis to leading twist. This requires the development of the methodology for treating $1/Q^2$ suppressed terms such as target mass corrections and higher twist contributions. Furthermore, as one probes deeper into the large-x region, nuclear corrections must be included when dealing with nuclear targets, as these become increasingly important as $x \rightarrow 1$.

It is a priori not obvious that the uncertainties on the PDFs will be reduced by relaxing the cuts to include more data since the various new theoretical contributions will have uncertainties of their own which could increase the resulting uncertainties on the extracted PDFs. It is the purpose of this paper to explore precisely this question. While some previous attempts have been made in the literature to include lower- Q and lower-W data in global fits and to explore the related uncertainties [\[12–](#page-12-9)[14](#page-12-10)], in this work we specifically focus on the large-x region.

The outline of the paper is as follows. Section II summarizes the theoretical issues which must be addressed in the region of large x , while Sec. III addresses the choice of data sets and the procedures utilized in the fitting. In Sec. IV, the results of the fits are presented and discussed, and Sec. V describes the resulting d/u ratio. Our conclusions are presented in Sec. VI. In keeping with the convention adopted in previous CTEQ Collaboration fits [\[1,](#page-12-0)[15\]](#page-12-11), we shall refer to the new fit from this analysis as ''CTEQ6X.''

II. THEORETICAL ISSUES AT LARGE x

From a theoretical standpoint the large-x region requires the inclusion not only of leading twist PDFs, but also of contributions suppressed by at least one power of Q^2 , which include target mass corrections and higher twist corrections. The former are kinematic in origin and involve terms suppressed by powers of M^2/Q^2 ; the latter are dynamical in origin and are suppressed as powers of Λ^2/Q^2 at large Q^2 , with Λ measuring the scale of nonperturbative parton-parton correlations. Furthermore, if a nuclear target is used, one must include nuclear corrections which account for the difference between the PDFs in free nucleons and those in nucleons bound in a nucleus. These corrections are not suppressed at high Q^2 , and are most significant at large x . Historically, to limit the effects of the target mass and higher twist corrections it has been customary to restrict the data included in the fits to large values of Q and W . In this section, we discuss the implications of these cuts and the theoretical tools needed to relax them.

A. Kinematic cuts

To avoid theoretical complications in PDF analyses at large x , it has been common to limit the deep inelastic data

used to those points which satisfy $Q \ge 2$ GeV and $W \ge$
3.5 GeV. These combined cuts have the effect of severely 3:5 GeV. These combined cuts have the effect of severely limiting the number of DIS data points in the large-x region that may be used to constrain PDFs in a global fit. However, as discussed in Refs. [[16](#page-12-12),[17](#page-12-13)], they do not completely eliminate the need for $\mathcal{O}(1/\mathcal{Q}^2)$ power corrections, whose neglect is a source of tension between several DIS data sets.

Other hard scattering processes, such as the production of lepton pairs, vector bosons, high- p_T jets, and direct photons, involve a large momentum scale analogous to Q^2 in deep inelastic scattering. The values are typically sufficiently large that one avoids target mass corrections and higher twist contributions. However, the relevant range in x is typically set by $x_T = 2p_T/\sqrt{s}$ for high- p_T scattering
or by M_{min}/\sqrt{s} for the production of a lepton pair of mass or by $M_{l^+l^-}/\sqrt{s}$ for the production of a lepton pair of mass $M_{l^+l^-}$, and data for such processes rarely constrain the large-x behavior of PDFs (although some exceptions to this will be discussed below).

Given all of the restrictions described above, one might well wonder how it is that any constraints at all are provided on the possible behavior of PDFs at large x . The answer is that there are indirect constraints which are provided by sum rules and the Q^2 evolution of the PDFs. The momentum and number sum rules provide some constraints since they involve integrations over the entire range of x. However, since the PDFs fall off as powers of $(1 - x)$, the large- x region contributes only small amounts to these sum rules. In addition, the DGLAP Q^2 evolution equations, used to calculate the PDFs at values of Q^2 above that where the initial PDFs are parametrized, have the property that the PDFs at high values of x and low Q^2 feed the behavior at lower values of x and higher Q^2 . Hence, there are indirect constraints placed on the large-x PDF behavior by data in regions of lower x and higher Q^2 .

It is important to understand that when one uses a supplied parametrization of PDFs in the large-x region the results represent extrapolations of the PDFs into regions where they have not been directly constrained by data. In order to reduce the size of the unconstrained region and check the validity of the large-x extrapolations obtained in standard global fits, one needs to account for the neglected theoretical corrections, which we discuss below.

B. Nuclear corrections

To probe the x dependence of the d quark to the same level of accuracy attained for the u quark requires lepton scattering data from a neutron target. Since free neutron targets do not exist, the next best choice is to utilize a deuterium target. Because the deuteron is a very weakly bound nucleus, many analyses which include proton and deuteron data make the assumption that it can be treated as a sum of a free proton and neutron. On the other hand, it has long been known from experiments on a range of nuclei that a nontrivial x dependence exists for ratios of nuclear to deuteron F_2 structure functions. These effects include nuclear shadowing at small values of x , antishadowing at intermediate x values $x \sim 0.1$, a reduction in the structure function ratio below unity for $0.3 \le x \le 0.7$, known as the European Muon Collaboration (EMC) effect, and a rapid rise as $x \rightarrow 1$ due to Fermi motion. Moreover, deviations from unity of the ratio of deuteron to proton structure functions corrected for nonisoscalarity, as well as many theoretical studies, strongly suggest the presence of nuclear effects also in the deuteron.

In the absence of experiments with free neutron targets, the size of the nuclear effects in the deuteron has yet to be determined empirically, although expectations are that it should be somewhat smaller than for heavy nuclei on the basis of its much lower binding energy. Nevertheless, in the region $x \ge 0.5$, the effects of nuclear Fermi motion lead to a rapidly increasing ratio of deuteron to nucleon structure function, which diverges as $x \rightarrow 1$. Any high-precision analysis of the large-x region must therefore account for the nuclear effects if data on deuterium (or other nuclei) are used in the fit.

The conventional approach to describing nuclear structure functions in the intermediate- and large- x regions is the nuclear impulse approximation, in which the virtual photon scatters incoherently from the individual bound nucleons in the nucleus. There have been many formulations of nuclear structure functions in the literature within this framework (see e.g. Refs. [[18](#page-12-14)[–21\]](#page-12-15)). In this analysis, we adopt the weak binding approximation (WBA) of Refs. [\[22](#page-12-16)–[25](#page-12-17)], where a covariant framework is used to relate the nucleon and deuteron scattering amplitudes, which are systematically expanded in powers of p/M , with p the bound nucleon momentum in the deuteron. The deuteron structure function can then be written as a convolution of the bound nucleon structure function and the distribution of nucleons in the nucleus. Because the struck nucleon is off its mass shell with virtuality $p^2 =$ $p_0^2 - p^2 < M^2$, its structure function can, in principle,
depend on n^2 in addition to x and Q^2 depend on p^2 , in addition to x and Q^2 .

Since the deuteron is weakly bound, with binding energy $\varepsilon_d = -2.2$ MeV and average nucleon momenta of the order $|p| \sim 130$ MeV, the typical nucleon virtuality will be \sim 4% smaller than the free nucleon mass *M*. One can therefore approximate the bound nucleon structure function by its on-shell value, in which case the deuteron structure function can be written, to order p^2/M^2 , as [\[24–](#page-12-18)[26\]](#page-12-19)

$$
F_2^d(x, Q^2) \approx \sum_{N=p,n} \int_x^{y_{\text{max}}} dy f_{N/d}(y, \gamma) F_2^N\bigg(\frac{x}{y}, Q^2\bigg). \tag{2}
$$

Here, F_2^N is the nucleon (proton p or neutron n) structure function, and $f_{N/d}$ gives the light-cone momentum distribution of nucleons in the deuteron. The scaling variable $y = (M_d/M)(p \cdot q/p_d \cdot q)$ is the deuteron's momentum fraction carried by the struck nucleon, where q is the virtual photon momentum, and p_d and M_d are the deuteron four-momentum and mass. The maximum value of y, to order p^2/M^2 , is given by $y_{\text{max}} = 1 + \gamma^2/2 + \varepsilon_d/M$, so that in the Biorken limit $y \to 1.5 + \varepsilon_d/M$ that in the Bjorken limit $y_{\text{max}} \rightarrow 1.5 + \varepsilon_d/M$. Relativistically, the upper limit on y is given by M_d/M , which suggests that the nonrelativistic approximation breaks down at large y. A careful treatment of relativistic corrections will be important at $x \ge 1$; however, for the x range covered in this analysis a nonrelativistic treatment is sufficient. In the Bjorken limit, the nucleon distribution function $f_{N/d}$ (also called the "smearing function") is a function of y only. At finite Q^2 , however, it depends in addition on $\gamma = \sqrt{1 + 4x^2M^2/Q^2}$, which in the nucleus rest frame coincides with the virtual photon "velocity" rest frame coincides with the virtual photon ''velocity'' $|q|/q_0$, with significant consequences when fitting large-x deuterium data [[25](#page-12-17)]. Furthermore, at finite Q^2 the limits of integration in y in general become x and Q^2 dependent, although their effects are negligible for $x \le 0.85$ [\[24](#page-12-18)[,26\]](#page-12-19).

The function $f_{N/d}$ is computed from the deuteron wave function, and accounts for the effects of Fermi motion and binding energy of the nucleons in the nucleus, as well as kinematic $1/Q^2$ corrections [\[24–](#page-12-18)[26](#page-12-19)]. In our numerical calculations, we use several different nonrelativistic deuteron wave functions, based on the Paris [\[27\]](#page-12-20), AV18 [[28\]](#page-12-21), and CD-Bonn [[29](#page-12-22)] nucleon-nucleon potentials, but find that the differences are small for $x \le 0.85$.

Including explicit off-shell dependence in the bound nucleon structure function, leads to a two-dimensional convolution in terms of y and the nucleon virtuality p^2 . For small values of $\frac{|p^2-M^2|}{M^2} \ll 1$, the off-shell effects can be incorporated into a generalization of Eq. ([2](#page-2-0)) in which the nucleon distribution function depends explicitly on x, in addition to y and γ . However, at larger x, higherorder corrections in p/M become increasingly important, and the factorization of the nucleon and nuclear functions inherent in the convolution approximation is expected to break down [\[30,](#page-12-23)[31\]](#page-12-24). In this case, relativistic effects can be incorporated through an additive correction $F_2^d \rightarrow F_2^d + \delta^{(off)}F_2^d$, which arises from explicit p^2 dependence
in the quark-nucleon correlation functions and relativistic in the quark-nucleon correlation functions and relativistic P-state components of the deuteron wave function. The latter have been computed, for instance, within the relativistic spectator theory for the deuteron [[32](#page-12-25)].

The off-shell dependence of the bound nucleon structure functions computed in Ref. [\[30](#page-12-23)] has been estimated within a simple quark-spectator model [\[31\]](#page-12-24) with the parameters fitted to proton and deuteron F_2 data, and leads to a reduction of about 2% of F_2^d compared to the on-shell approximation. A simple parametrization of the relativistic and off-shell effects in the model of Ref. [\[30\]](#page-12-23), relative to the total F_2^d , is given by

$$
\frac{\delta^{(off)}F_2^d}{F_2^d} = a_0(1 + a_1 x^{a_2})(1 - [a_3 - x^{a_4}]^{a_5}),
$$
 (3)

with $a_i = \{-0.014, 3, 20, 1.067, 1.5, 18\}$ at a scale of $Q^2 \approx$ 5 GeV2. Note that this correction is applicable only for $x \ge 0.2$, and for the values of x relevant to the current analysis one finds $\delta^{(off)}F_2^d/F_2^d \le 1.5\%$. Furthermore, because the off-shell nucleon-deuteron amplitude was evaluated in Ref. [\[30\]](#page-12-23) using wave functions derived from a pseudoscalar πN interaction [\[32](#page-12-25)], which is known to produce large P -state contributions, the correction (3) (3) (3) is likely to provide an upper limit on the size of the relativistic, convolution-breaking effects.

Finally, we note that while a few global PDF analyses [\[12–](#page-12-9)[14,](#page-12-10)[33\]](#page-12-26) have incorporated nuclear effects in the deuteron using smearing functions similar to those employed here, some studies [[34](#page-12-27)] have corrected deuteron data using a parametrization [\[35\]](#page-12-28) of the nuclear density model [\[36\]](#page-12-29). This model is motivated by the observation that for heavy nuclei the ratio of nuclear to deuterium structure functions scales with the nuclear matter density [\[21,](#page-12-15)[36](#page-12-29)]. Assuming the density scaling extends all the way down to the deuteron, one can obtain the ratio of deuteron to nucleon structure functions from the ratio of iron to deuterium structure functions $F_2^d/F_2^N \approx 1 + 0.25(F_2^{\text{Fe}}/F_2^d - 1)$, us-
ing the empirical nuclear density for ⁵⁶Fe and an *ansatz* ing the empirical nuclear density for $56Fe$ and an *ansatz* for the charge density of deuterium [\[36](#page-12-29)[,37\]](#page-12-30). Consequently, the F_2^d/F_2^N ratio displays a relatively large depletion at $x \sim 0.6$ and a rise above unity which does not set in until $x \sim$ 0.6 and a rise above unity which does not set in until $x \sim$ 0:8, significantly higher than typically found in smearing models. Unfortunately for light nuclei, and especially deuterium, it is difficult to define physically meaningful nuclear densities [[37](#page-12-30)], so that the application of the density model to deuteron data inevitably suffers from ambiguities. Furthermore, even for heavy nuclei, the authors of Ref. [\[36\]](#page-12-29) caution that the density model should only be considered qualitative beyond $x \approx 0.6{\text -}0.7$.

C. Target mass corrections

In the context of the operator product expansion (OPE) in QCD, deep inelastic scattering is formulated through moments of structure functions, which are related to forward matrix elements of local operators. The x dependence of structure functions is formally reconstructed from the moments via an inverse Mellin transform. At large Q^2 , the process is dominated by matrix elements of operators of twist two, such as the quark bilinear $\bar{\psi} \gamma^{\mu} \psi$. Operators which include insertions of covariant derivatives $\bar{\psi}\gamma^{\mu}D^{\mu_1}\cdots D^{\mu_n}\psi$ do not alter the twist, but have matrix
elements that enter as M^2/Q^2 corrections to the $\mathcal{O}(1)$ terms elements that enter as M^2/Q^2 corrections to the $\mathcal{O}(1)$ terms [\[38](#page-12-31)[,39\]](#page-12-32). These "target mass corrections" (TMCs), which are of purely kinematic origin, need to be removed from the empirical structure function data before information on the twist-two PDFs can be extracted.

One of the limitations of the OPE formulation of TMCs is the so-called ''threshold problem,'' in which the target mass corrected structure functions remain nonzero at $x \ge$ 1. This arises from the difficulty in consistently incorpo-1. This arises from the difficulty in consistently incorporating the elastic threshold in moments of structure functions at finite Q^2 , resulting in nonuniformity of the $Q^2 \rightarrow \infty$ and $n \rightarrow \infty$ limits, where *n* is the rank of the moment. A number of attempts to address the unphysical $x \rightarrow 1$ behavior have been made [\[24,](#page-12-18)[40,](#page-12-33)[41](#page-12-34)], although none of the proposed approaches is free of additional assumptions or complications [[42\]](#page-12-35).

Alternatively, using the collinear factorization (CF) formalism [\[43](#page-12-36)[,44\]](#page-12-37), one can avoid the threshold ambiguities from the outset by formulating TMCs directly in momentum space. Recently, this formalism was applied [[45](#page-12-38)] to deep inelastic structure functions at large x at next-toleading order, carefully taking into account the elastic threshold to render the structure functions zero above $x =$ 1. However, in the handbag approximation, without introducing a suitable jet function to account for the invariant mass of the final hadronic state, leading order structure functions can still be nonzero at $x = 1$ [\[45\]](#page-12-38). A simplified version of the CF formalism, which involves replacing the Bjorken variable x with the Nachtmann variable $\xi =$ $2x/(1+\sqrt{1+4x^2M^2/Q^2})$, was proposed in Refs. [\[46,](#page-12-39)[47\]](#page-12-40).
At leading order this " ξ -scaling" prescription coincides At leading order this " ξ -scaling" prescription coincides with the CF results. Beyond leading order, however, this overestimates the CF results by about 20–30% [[45](#page-12-38),[48](#page-12-41)].

In this analysis, we consider both the traditional OPE approach and the collinear factorization formulations of TMCs for DIS reactions. For deuterium data, we first apply the TMCs to the nucleon structure function, which is then convoluted through Eq. [\(2](#page-2-0)) to obtain the deuteron F_2^d . Although there is some residual dependence on the TMC prescription adopted, we will see in Sec. IV below that the resulting PDFs are essentially independent of the choice once allowance is made for dynamical higher twist and other power corrections. For non-DIS data, such as Drell-Yan, W-asymmetry and jet production in hadronic collisions, the target mass and nuclear corrections should play a negligible role because of the limited reach at large x and the typically large momentum scales involved, and are therefore neglected in our analysis.

D. Dynamical power corrections

In the OPE framework, dynamical higher twist contributions to DIS structure functions are associated with matrix elements of operators involving multiquark or quark and gluon fields, which give rise to $1/Q^2$ or higher order corrections to structure functions. As with the kinematic target mass corrections, these must be taken into account in analyses of data at low Q^2 and especially at large x. Because dynamical higher twists involve nonperturbative multiparton interactions, it is notoriously difficult to quantify their magnitude and shape from first principles.

The usual approach in analyses whose main aim is the extraction of leading twist PDFs is either to parametrize the higher twist contributions by a phenomenological form and fit the parameters to the experimental data [[49](#page-12-42)[,50](#page-12-43)], or to

extract the Q^2 dependence by fitting it in individual bins in x [\[13,](#page-12-44)[17](#page-12-13),[51](#page-12-45)[–53\]](#page-12-46). Such an approach effectively includes contributions from multiparton correlations (the true higher twist contributions) along with other power corrections that are not yet part of the theoretical treatment of DIS at low Q^2 . These include $\mathcal{O}(1/Q^2)$ contributions such as jet mass corrections [[45](#page-12-38)] and soft gluon resummation [\[54\]](#page-12-47), as well as contributions which are of higher order in α_s but whose logarithmic Q^2 behavior mimics terms ∞ $1/Q²$ at low virtuality [\[53,](#page-12-46)[55\]](#page-12-48). For these reasons, it is more appropriate to speak about residual power corrections rather than higher twist corrections. Nevertheless, we shall refer to all of these $1/Q^2$ suppressed effects as "higher twist'' corrections in order to conform with the terminology frequently used in the literature, but keeping in mind their possibly disparate origins.

We employ the commonly-used phenomenological form for the total structure function,

$$
F_2(x, Q^2) = F_2^{\text{LT}}(x, Q^2) \left(1 + \frac{C(x)}{Q^2} \right), \tag{4}
$$

where F_2^{LT} is the leading twist (LT) component including TMCs, and the coefficient of the $1/Q^2$ term is parametrized (in units of GeV^2) as

$$
C(x) = c_1 x^{c_2} (1 + c_3 x). \tag{5}
$$

The parameter c_1 reflects the overall scale of the higher twist corrections, while c_2 controls the well-known rise of the coefficient $C(x)$ at large x; the parameter c_3 allows for the possibility of negative higher twists at smaller x . For deuterium targets, we use the same higher twist term $C(x)$ for the bound proton and neutron F_2 structure functions. In so doing, we neglect higher twist contributions coming from parton rescattering on the spectator nucleon [\[56\]](#page-12-49) due to the small atomic number, which would slightly increase the deuteron's dynamical higher twist contribution compared to that of the proton. These assumptions may need to be relaxed in future analyses, see e.g. Refs. [\[53](#page-12-46)[,57\]](#page-12-50).

We stress the importance of explicitly including *both* the TMCs and the higher twist corrections, which have very different physical origin and can have a very different x dependence. Since the higher twists are fitted phenomenologically, one could, in principle, simulate TMC effects with an empirical power corrections function with a sophisticated enough parametrization. We have considered several alternative forms for $C(x)$, but were not able to find an efficient parametrization which embodies both the higher twist and TMC effects and allows a good fit. On the contrary, inclusion of TMCs in the LT structure function in Eq. ([4](#page-4-0)) allows us to adopt a very economical 3 parameter functional form for $C(x)$.

III. DATA SETS AND FITTING

We perform NLO global PDF fits to proton and deuteron data from inclusive deep inelastic fixed-target scattering experiments at Jefferson Lab (JLab), SLAC, and the BCDMS and New Muon Collaborations (NMC) at CERN; ep collider data from H1 and ZEUS; E605 and E866 Drell-Yan data from pp and pd collisions; W-lepton asymmetry data from CDF and D0; W asymmetry data from CDF; and jet and γ + jet cross sections from D0. The full list of data sets, together with a comparison to the data full list of data sets, together with a comparison to the data

TABLE I. Data sets and number of data points (total and deuterium) used in the global fits discussed in the text. The data sets with a check mark $\binom{1}{k}$ were used in the CTEO6.1 fits [\[15\]](#page-12-11).

			Total		Deuterium		
			cut0	cut3	cut0	cut3	CTEQ6.1
DIS	JLab	[58]		272		136	
	SLAC	[59]	206	1147	104	582	
	NMC	[60]	324	464	123	189	
	BCDMS	[61]	590	605	251	254	
	H1	[62]	230	251			
	ZEUS	[63]	229	240			
ν A DIS	CCFR	[64, 65]					
DY	E ₆₀₅	[66]	119				
	E866	[67]	375		191		
W asymmetry	CDF '98 (ℓ)	[68]	11				
	CDF '05 (ℓ)	[69]	11				
	D0 '08 (ℓ)	$[70]$	10				
	D0 '08 (e)	[71]	12				
	CDF'09(W)	[72]	13				
jet	CDF	[73]	33				
	D ₀	[74]	90				
γ + jet	D ₀	$[75]$	56				
	TOTAL		2408	3709	569	1161	

sets included in the most recent CTEQ6.1 fits [\[15\]](#page-12-11), is provided in Table [I](#page-4-1).

The standard cuts on DIS data in previous global analyses have excluded data with $Q^2 < 4 \text{ GeV}^2$ and W^2 < 12.25 GeV², which means that effectively the PDFs have only been constrained up to $x \approx 0.7$. As discussed

in Sec. I, extending the coverage to larger x requires relaxing the Q^2 and W^2 cuts. To test the effects on the PDFs as the kinematic cuts are relaxed, we consider several cuts in addition to the standard one, which we denote as follows:

- (i) cut0: $Q^2 > 4$ GeV², $W^2 > 12.25$ GeV² (standard)
- (ii) cut1: $Q^2 > 3$ GeV², $W^2 > 8$ GeV²
- (iii) cut2: $\tilde{Q}^2 > 2 \text{ GeV}^2$, $W^2 > 4 \text{ GeV}^2$
- (iv) cut3: $\tilde{Q}^2 > m_c^2 = 1.69 \text{ GeV}^2$, $W^2 > 3 \text{ GeV}^2$.

In Fig. [1,](#page-5-0) we plot the (x, Q^2) coverage of the DIS data sets used in this analysis, along with the above kinematic cuts. The approximate doubling of the number of data points included in the fits going from cut0 ($N_{\text{DIS}} = 1579$) to cut3 ($N_{\text{DIS}} = 3079$) is evident. In particular, we can include most of the SLAC data points, which reach the lowest Q^2 values, and about half of the recent JLab data points. At the lower Q^2 values, we include only those JLab data for which an estimate of the uncertainties related to parametrizations of the longitudinal to transverse cross section ratio is available.

The methodology used in the global fits follows that of the CTEQ6 series of global fits [[15](#page-12-11)]. In particular, the same functional forms for the PDF parametrizations at the initial scale $Q_0 = 1.3$ GeV are employed. Several of the parameters are fixed at representative values and a total of 20 PDF parameters are varied in the fits. An additional 3 free parameters are introduced for the parametrization of the higher twist corrections, and error bands are calculated using the Hessian technique. The $\Delta \chi$ tolerance used to define the errors in global fits has been extensively discussed in the literature, and various groups use values ranging from $\Delta \chi = 1$ to 10. We quote the error bands with $\Delta \chi = 1$, and simply use them to show the relative variation of the errors as the cuts are varied and between different PDFs.

IV. FIT RESULTS

Having described the expanded data sets used in this study and the new ingredients necessary for fitting the data in the large-x region, in this section we present the numerical results of our analysis.

A. Reference fit and kinematic cuts

The first step in this study is to define a reference fit in order to have a standard against which to compare the results of subsequent fits as new terms are added and new sets of cuts are imposed. This is achieved using the data listed in Table [I](#page-4-1) with the cut0 set of kinematic cuts. Target mass, higher twist, and nuclear corrections (for deuterium data) are not included in the reference fit, which should therefore yield results similar to those of the CTEQ6.1 PDFs [[15](#page-12-11)]. Small differences can be expected, however, due to some additional data sets used. For example, the inclusion of the SLAC and E866 data induces a small reduction of the *u*-quark distribution at large *x*. The E866 data also lead to a sizable enhancement of the d -quark distribution at large x , which is partially offset by the W-asymmetry and γ + jet data.
The results for the *u* and *d*

The results for the u and d distributions are shown in Fig. [2\(a\)](#page-6-0) as ratios to the corresponding CTEQ6.1 PDFs. As anticipated, the u distribution is slightly reduced in the large-x region, while the d distribution shows a small increase for $x \ge 0.3$, leading to a modest increase of the d/u ratio at intermediate x. The dotted vertical line at $x =$ 0.7 indicates the restriction on the range in x for which there are sufficient DIS data to constrain the PDFs with

FIG. 1 (color online). DIS data points and cuts for proton (left) and deuterium (right) targets, with the cut0–cut3 kinematic cuts drawn from top to bottom with solid lines. The data points are from JLab (open red squares), SLAC (open blue triangles), NMC (filled green triangles), BCDMS (crosses), H1 (filled black circles), ZEUS (open black circles).

FIG. 2 (color online). (a) Impact of the expanded data set, with the standard cuts (cut0) and no target mass, higher twist or nuclear corrections applied. Illustrated are ratios of the PDFs from the resulting ''reference'' fit to those from the CTEQ6.1 fit. (b) Effects on the reference fit as TMC (using the CF prescription), higher twist (HT), and nuclear corrections (WBA) are added.

cut0 kinematic limits. Accordingly, the portion of each curve extending beyond the dotted line represents an extrapolation of the fitted results.

The gluon and sea quark PDFs are not discussed here because they are too poorly constrained at large x by the chosen data sets. More specifically, the gluon distribution is partially constrained at intermediate and low x by the scaling violations in DIS and by the jet data. At larger x , however, it is only indirectly constrained by the momentum sum rule. This can be seen by considering the effects of a small change in one of the valence distributions, such as described above, which alters their average momentum. With the gluon already constrained somewhat in the intermediate- to low-x region, it is the large-x gluon which is modified in order to satisfy the momentum sum rule; since the gluon distribution is much smaller than the valence distributions at large x, this results in large variations of the high- x gluons in order to compensate the rather small changes in the valence PDFs. The large variations in the shape of the gluon PDF at large x then propagate to the sea PDFs via the actions of the evolution equations. Discussions on how to better experimentally constrain the gluon distributions at large x are contained in Refs. [\[13](#page-12-44)[,14\]](#page-12-10).

Having verified that the earlier CTEQ6.1 results could be reproduced up to small variations due to the different data sets used, the next step consists of a systematic investigation of the effects of including target mass, higher twist, and nuclear corrections, while also reducing the cuts on W and Q . It is instructive to first consider the impact of each of these corrections on the reference fit, which is illustrated in Fig. $2(b)$. One can see that the cut0 constraints effectively limit any change to the reference fit u PDF. On the other hand, while the d PDF shows little sensitivity to the target mass and higher twist effects, it does show that the nuclear corrections to the deuterium data have a profound effect. The nuclear effects, as calculated in the framework of the weak binding approximation [\[22](#page-12-16)[,24,](#page-12-18)[25](#page-12-17)], cause a large reduction in the d PDF relative to the reference fit starting at $x \approx 0.5$. The lesson for PDF global fits is that, even with the cut0 constraints on the data selection, one should include nuclear corrections for the deuterium data. The cut0 constraints, however, effectively remove the need for the inclusion of the TMC and higher twist (HT) contributions, as was the original intent (which also confirms the analogous results of Ref. [[33](#page-12-26)]). Of course, the PDFs are then directly constrained only for $x \leq$ 0:7.

With the reference fit as a starting point, we next turn on the TMC, add the higher twist parametrization, include the deuteron nuclear correction, and then perform fits for the various sets of cuts denoted by cut0 through cut3. Progressively loosening the cuts naturally brings more data into play. These data provide additional constraints at high values of x, and one can see in Fig. $3(a)$ that the reduction in the d PDF is less pronounced than with $cut0$. Thus the extrapolation of the cut0 results into the region beyond $x \approx 0.7$ actually shows too strong a reduction. Remarkably, the lowering of the W and Q cuts does not qualitatively affect the d-quark suppression beyond $x \approx$ 0:5, which remains a stable feature for all fits considered.

B. Sensitivity to nuclear corrections

As suggested in Fig. $2(a)$ for cut3 kinematics, and illustrated in Fig. [3\(b\)](#page-7-0) for cut3, the behavior of the

FIG. 3 (color online). (a) Effect on the d-quark distribution from varying the Q and W cuts, including target mass (CF), higher twist, and nuclear corrections (using the WBA nuclear smearing model). The vertical dotted lines indicate the x region which is not directly constrained by DIS data ($x \ge 0.7$ for cut0 and $x \ge 0.8$ for cut3). (b) Sensitivity of the d-quark distribution to nuclear correction models with cut3 kinematics: no nuclear effects ("free", dot-dashed line), nuclear density model (long-dashed line), WBA nuclear smearing model without (solid line), and with (short-dashed line) off-shell corrections.

d-quark distribution at large x is driven primarily by the nuclear effects. With no nuclear corrections (treating the deuteron as a sum of a free proton and free neutron), the d quark is strongly enhanced above $x \approx 0.5$. This occurs because the Fermi motion in the deuteron causes an enhancement of the data for F_2^d beyond what would be expected by treating the deuteron as the sum of free nucleons; if no smearing corrections are included, the resulting d-quark distribution must make up this enhancement as the u distribution is already well constrained at large values of x by the proton data. A qualitatively similar result is found using the nuclear density model [\[36\]](#page-12-29), which arises directly from the delayed onset of Fermi motion in this model to $x \ge 0.8$, and the corresponding smaller deviation of the F_2^d/F_2^N ratio from unity in this region.

On the other hand, correcting for the nuclear effects in the F_2^d data using the WBA finite- Q^2 smearing model discussed in Sec. II B leads to a d -quark distribution with the opposite trend at large x relative to the reference fit, as Fig. [3\(b\)](#page-7-0) illustrates. At $x = 0.8$ this amounts to a $\sim 40\%$ reduction of the d PDF relative to the reference fit. Not accounting for the nuclear smearing in deuterium data will thus lead to a significant overestimate of the d distribution at $x \ge 0.6$. This will be the case, in fact, for a wide range of nuclear smearing models, and regardless of the details of the deuteron wave function.

Because the nucleons in the deuteron are slightly offshell, with $\vert p^2 - M^2 \vert / M^2 = \mathcal{O}(\text{few} \%)$, in principle, this can affect the extracted neutron structure function and resulting d-quark distribution. Using the model for offshell corrections discussed in Sec. II B does indeed result in an increase in the d distribution at large x compared with the on-shell calculation, which reflects the larger deviation

from unity of the F_2^d/F_2^N ratio in the presence of off-shell effects [\[22](#page-12-16)[,24](#page-12-18)[,30](#page-12-23)[,31,](#page-12-24)[76\]](#page-13-11). A simple way of understanding this is to consider the struck nucleon as having a slightly smaller mass than a free nucleon, $p^2 = M^{*2} < M^2$. In the target rest frame the effective scaling variable is then $x^* =$ $Q^2/2M^*\nu$, so the actual value of x is larger than would be expected for a free nucleon. This leads to the observed structure function being slightly reduced in this region, as can be seen from Eq. ([3](#page-2-1)) where the reduction is $\approx -1.5\%$.

To quantify the impact of the off-shell corrections on the d-quark distribution, one may consider the leading order structure functions in the large-x region, which is dominated by the valence PDFs,

$$
F_2^p = \frac{4}{9} x u \left(1 + \frac{d}{4u} \right) \quad \text{and} \quad F_2^d = \frac{5}{9} x u \left(1 + \frac{d}{u} \right), \tag{6}
$$

and examine the effect of a small variation in F_2^d caused by correcting for off-shell effects. Since there is no variation in F_2^p , as an approximation, the proton structure function can be assumed to remain the same. The modifications to the *u*- and *d*-quark PDFs are then related by $\delta u = -\frac{1}{4}\delta d$, and using Eq. ([6\)](#page-7-1) gives

$$
\frac{\delta d}{d} = \frac{4}{3} \frac{\delta F_2^d}{F_2^d} \left(1 + \frac{u}{d} \right).
$$
 (7)

A small change in F_2^d thus results in a relative shift in the d-quark distribution that is enhanced by a factor of order u/d . For example, at $x = 0.8$, the ratio $u/d \approx 20$, and a shift of 1.5% in F_2^d leads to a increase of the d distribution of about 40%. This is similar to what is observed in Fig. [3\(b\).](#page-7-0)

The same argument also explains the large sensitivity of the large- x d-quark PDF to the choice of the nuclear correction model. Currently, this represents the single most important theoretical uncertainty on large-x PDFs, which can affect not only the extraction of the d/u ratio at large x (see Sec. V), but also the determination of Tevatron and LHC parton luminosities at large produced mass [[12\]](#page-12-9).

C. Sensitivity to TMC and HT corrections

The sensitivity of the d -quark distribution to the finite- Q^2 corrections associated with target mass and higher twist effects is illustrated in Fig. [4,](#page-8-0) where three different TMC prescriptions are illustrated: the OPE-based prescription [[39](#page-12-32),[42](#page-12-35)], the Nachtmann ξ -scaling [\[46,](#page-12-39)[47\]](#page-12-40), and the collinear factorization prescription [[45](#page-12-38)], along with a fit with no TMCs. Although there is some dependence on the choice of TMCs, with the addition of the phenomenological higher twist correction (4) (4) the resulting fits in Fig. $4(a)$ are almost identical, with $\chi^2/\text{d.o.f.} \sim 1$. This reveals an important interplay between the target mass and higher twist corrections, which tend to compensate each other in the fitting procedure.

As discussed in Sec. II, given a sophisticated enough parametrization of the higher twist corrections, one could,

FIG. 4 (color online). (a) Effects of target mass and higher twist corrections on the d-quark distribution, using the ξ -scaling (shortdashed line), OPE (long-dashed line), and CF (solid line) TMC prescriptions, as well as no TMC (dot-dashed line). In each case, a phenomenological higher twist correction is included in the fit, and the $\chi^2/\text{d.o.f.}$ is indicated. (b) Extracted higher twist coefficient $C(x)$ for the different TMC prescriptions, compared with the higher twist determination from the MRST fit [\[52\]](#page-12-58).

in principle, accommodate the entire TMC effect, even though the existence of TMCs is well-established theoretically. In practice, however, it is preferable to include the TMC and HT terms separately because of the different models in use for the TMCs, and the separate HT parametrization is able to compensate the different model choices. Furthermore, it allows us to use a very economical functional form for the higher twist corrections with only 3 parameters. In contrast, with no TMCs, we found no suitable parametrization able to produce a satisfactory fit with a similar χ^2 .

Given that there is very little difference between the d-quark distribution obtained using the different TMC choices, it is clear that one cannot determine which is the preferred TMC prescription from these fits alone. On the other hand, the gluon distribution at large x obtained by analyzing the scaling violations of $F₂$ does depend somewhat on the chosen TMC prescription because of the different dependence on Q^2 . One can therefore include longitudinal structure function or cross section data in the fits to directly constrain the gluon distribution. A comparison of the fitted gluon distribution with the scaling violations of F_2 may then allow the TMC models to be distinguished.

The interplay between TMCs and higher twists is more vividly demonstrated in Fig. [4\(b\)](#page-8-1), where the higher twist coefficient $C(x)$ is plotted for the various TMC prescriptions. The characteristic rise with increasing x is evident, with the higher twist term being larger for the CF prescription than for the others. The extracted higher twist coefficient for the case with no TMCs is also qualitatively similar to that obtained in the MRST analysis [\[52](#page-12-58)], which did not include target mass or deuterium corrections. The negative higher twist term at $x \sim 0.3$ evident with the OPE and no TMC prescriptions disappears when using the CF or ξ -scaling approaches.

The extracted HT coefficient for the OPE prescription is about half of that obtained by Blümlein et $al.$ (BBG) $[33,53]$ $[33,53]$ in fixed-x bins. This may be due in part to our HT parametrization being too restrictive. On the other hand, the BBG parton distributions have been fitted with $cut0$ kinematic cuts and then extrapolated to smaller x and Q^2 before extracting the HT terms. This extrapolation may underestimate the d quark distribution at large x , similar to our result in Fig. $3(a)$, therefore leading to an overestimate of the HT terms.

We emphasize, however, that our main finding here is not the magnitude of the higher twist correction per se, but the fact that very stable fits to *leading twist* PDFs for the u and d quarks can be obtained by the inclusion of both the target mass and higher twist corrections.

D. Final fit results

We conclude this section with the presentation in Fig. [5](#page-9-0) of the final fit results for the cut3 set of constraints, which we refer to as ''CTEQ6X.'' One can see the significant reduction in the d PDF at large values of x that was discussed previously, with the vertical lines again indicating the approximate limits of the fit constraints. As shown in Fig. [1](#page-5-0), the proton DIS data extend to $x = 0.9$, and consequently the u distribution is well constrained up to that limit. The d distribution, however, is constrained only up to $x = 0.8$, reflecting the maximum extent of the deuterium data. The error bands on the PDFs correspond to $\Delta \chi = 1$ and include systematic and statistical experimental uncertainties, but exclude the theoretical uncertainties discussed above.

One of the goals of this investigation was to examine the extent to which the errors on the PDFs would be affected by the addition of the new data made accessible by relaxing the selection criteria applied to the DIS data. This is shown in Fig. [6](#page-9-1) where the relative errors on the u and d PDFs are

FIG. 5 (color online). Results of the CTEQ6X fit with expanded kinematics (cut3) and inclusion of TMC, HT, and nuclear corrections, normalized to the CTEQ6.1 PDFs. The vertical lines show the approximate values of x above which PDFs are not directly constrained by data. The error bands correspond to $\Delta \chi = 1$.

shown, normalized to the relative errors from the reference fit. These ratios are shown for the cut0 through cut3 kinematic cuts. For cut0 and cut1, the errors typically increase because the amount of new DIS data is not sufficient to compensate for the added 3 free parameters that describe the phenomenological higher twist contributions. For cut2 and cut3, there is a substantial reduction in the uncertainty of these PDFs due to the increased data, with the cut3 errors reduced by 10–20% for $x \le 0.6$, and by up to 40–60% at larger x. However, it must be stressed that

FIG. 6 (color online). Relative PDF errors for u and d quarks normalized to the relative errors in the reference fit.

these errors only reflect the uncertainties due to propagating the experimental errors. In particular, uncertainties associated with nuclear corrections are not shown; these will be discussed in more detail in a subsequent analysis [\[77\]](#page-13-12).

As a consistency check of the new fits, in Fig. [7](#page-10-0) we show the ratio $F_2^d/2F_2^p$ computed from the new PDFs and compare them to data at $Q^2 = 6$, 12, and 20 GeV² [\[78\]](#page-13-13) using several models for the nuclear corrections, as in Fig. [3\(b\)](#page-7-0). The fit with no nuclear corrections is clearly disfavored, while all three nuclear correction model curves show a χ^2 which is improved to some degree. The nuclear density model correction has difficulty in reproducing the Q^2 dependence of the data, especially at high x . The WBA nuclear smearing model, on the other hand, is strongly Q^2 dependent at large x and rises more steeply than the density model as $x \to 1$ when $Q^2 \ge 10 \text{ GeV}^2$. The addition of offshell corrections has very little effect on the fit: essentially, the d-quark PDF shifts to compensate the inclusion of the off-shell corrections, and the PDFs obtained with these two models provide an estimate of the uncertainty due to the model dependence of the nuclear corrections. A detailed comparison to data over a wider range of Q^2 would help to clarify the nature of the Q^2 dependence of the nuclear corrections, as also emphasized recently by Arrington et al. [[78](#page-13-13)].

V. d/u RATIO

According to spin-flavor SU(6) symmetry with no flavor-dependent interactions between quarks, one would expect $d/u = 1/2$ for all x. Empirically, the d/u ratio of course deviates strongly from this naive expectation, and its $x \rightarrow 1$ behavior is a particularly sensitive indicator of the dynamics responsible for the symmetry breaking. If the interaction between the two valence quarks that are spectators to the hard collision is mediated by a spin-dependent color-magnetic force, such as from single gluon exchange (which also accounts for the mass splitting between the nucleon and Δ [[79](#page-13-14)]), the two-quark state with spin 0 will be energetically favored relative to that with spin 1. A dominant scalar ''diquark'' component of the proton would then lead to a suppression of the d quark distribution and a vanishing d/u ratio as $x \to 1$ [[80](#page-13-15)]. On the other hand, if the dominant scattering process involves scattering from quarks with the same helicity as that of the proton, as would be expected from perturbative QCD, then this mechanism of SU(6) breaking would lead to $d/u \rightarrow 1/5$ in the $x \rightarrow 1$ limit [\[81\]](#page-13-16). The approach of the PDFs to the $x = 1$ limiting values may also reveal the role played by quark orbital angular momentum in the nucleon [\[82\]](#page-13-17).

In this section, we explore in more details what the new fits can tell us about the large-x behavior of the d/u ratio. We discuss the sensitivity of our d/u fits to nuclear corrections, and review future experiments which can more directly constrain the d distribution as $x \to 1$.

FIG. 7 (color online). Ratio of deuteron to proton F_2 structure functions computed from the cut3 PDFs at $Q^2 = 6$, 12 and 20 GeV² for various nuclear correction models, as in Fig. [3.](#page-7-2) Data points are taken from the compilation of SLAC, BCDMS, and NMC data in Ref. [\[78\]](#page-13-13), with $W^2 < 3$ GeV² data denoted by open circles.

A. Effect of nuclear corrections on d/u

The ratio of the d to u distributions is shown in Fig. [8](#page-10-1) for the CTEQ6.1, reference, and CTEQ6X fits, together with predictions from various models for the limiting behavior as $x \rightarrow 1$. The rapid falloff at high values of x for the CTEQ6X PDFs (with cut3) suggests that our results favor a lower d/u value that is more consistent with the model of scalar diquark dominance of the proton wave function than with models that predict large d/u asymptotic values. In fact, relative to the standard PDF fits which assume no nuclear corrections in the deuteron, the extracted d/u ratio is reduced at $x \ge 0.6$, as evident already from Fig. [3.](#page-7-2)

We should note, however, that since our fitting region is restricted to $x \le 0.8$ for the d-quark distribution, the fits can only extrapolate the behavior of the d/u ratio at $0.8 \leq$ $x \leq 1$. Furthermore, since similar parametric forms are used for both the u and d distributions, the d/u ratio is constrained to approach 0 or infinity at the point $x = 1$. Nevertheless, in the absence of a dramatically large upturn in d/u beyond $x \sim 0.8$, the fits in the constrained region suggest a trend of the ratio towards a small limiting value.

This result is qualitatively different from the fit of Yang and Bodek [\[34\]](#page-12-27), in which the ratio of deuteron to proton and neutron F_2 structure functions was fitted with d/u constrained to approach the limit $1/5$ at $x = 1$ [[81\]](#page-13-16). However, the neutron structure function in that analysis was extracted assuming the nuclear density model [\[36\]](#page-12-29) for the nuclear corrections in the deuteron. As discussed in Sec. II B, the extrapolation of the density model to the deuteron suffers from ambiguities associated with defining physically meaningful nuclear densities for the deuteron [\[37\]](#page-12-30), and even for large nuclei, the model should not be considered quantitative at very large $x (x \ge 0.6-0.7)$ [[36\]](#page-12-29).

In contrast to the nuclear density model, where the nuclear correction is assumed to be independent of the bound nucleon structure, the size of the nuclear correction within the nuclear smearing approach depends also on the shape of the bound nucleon structure function through the convolution in Eq. (2) (2) . Functions with harder x distributions produce ratios F_2^d/F_2^N which have greater depletion at intermediate and large x, and a delayed onset of the Fermi motion rise as $x \rightarrow 1$. This was observed in the quark model calculation of Ref. [\[30\]](#page-12-23), which also illustrates the importance of the Q^2 dependence of the data at large x. Since the determination of the model parameters in [\[30\]](#page-12-23) involved fitting to the large-x proton and deuteron data without including target mass and higher twist corrections,

FIG. 8 (color online). (a) d/u quark distribution ratio for the reference, CTEQ6.1 and CTEQ6X (cut3) fits. (b) Ratio of the reference and CTEQ6X (cut3) to the CTEQ6.1 d/u ratios. In both panels, the dotted lines indicate the region where the PDFs are not directly constrained by DIS data.

the resulting distributions were generally harder than the empirical PDFs, leading to a ratio F_2^d/F_2^N in which the Fermi motion rise does not appear until $x \ge 0.8$. Incorporating the finite- Q^2 corrections in the fits would result in softer distributions and consequently an earlier rise of F_2^d/F_2^N due to Fermi motion at $x \sim 0.6$.
It is clear that obtaining a precise behavior

It is clear that obtaining a precise behavior of d/u as $x \rightarrow 1$ requires a similarly precise knowledge of the nuclear corrections associated with the use of a deuterium target. While the results will inevitably have some dependence on the nuclear model adopted, our finding of a reduced d-quark distribution will prevail in a wide range of models which incorporate the standard nuclear corrections such as Fermi motion, binding and nucleon off-shell effects. As seen in Fig. [7,](#page-10-0) inclusive DIS data on a deuterium target alone have little discriminatory power, except if the $Q²$ range and precision of the measurements are increased. A more detailed analysis of the correlation between nuclear corrections and the d/u ratio at $x \rightarrow 1$, as well as of the dependence of d/u on the parametric forms, will be presented in a future publication [[77](#page-13-12)].

B. Direct experimental constraints on d/u

To avoid nuclear corrections altogether, one would ideally need data on free nucleon targets which would constrain the d-quark PDF. This suggests weak interaction processes where one can utilize variations of the flavor changing transition $W^+d \rightarrow u$. An example would be the DIS processes $\nu p \rightarrow \mu^- X$ and $\bar{\nu} p \rightarrow \mu^+ X$, which could probe the d and u PDFs, respectively, at large values of x. However, existing data sets for neutrino scattering from hydrogen do not have sufficient statistics to provide information in the $x \rightarrow 1$ region. A new high-statistics experiment on hydrogen, as is being considered by the MINERvA collaboration [[83](#page-13-18)], would be required for such a study.

A further possibility is provided by the W-lepton or W charge asymmetries measured at the Tevatron in $p\bar{p}$ collisions. These are sensitive to the d/u ratio, and data at large values of the lepton or W rapidity can reach x values as high as 0.8. However, this is at the edge of the kinematic coverage and the data there are statistically limited. Nevertheless, new data sets with increased statistics may help provide additional constraints on d/u which are independent of nuclear corrections.

Another method which utilizes the weak interactions to probe the d quark involves parity-violating electron DIS on a hydrogen target [[84](#page-13-19),[85](#page-13-20)]. Here, the asymmetry between left- and right-hand polarized electrons selects the interference between the γ and Z-boson exchange, which depends on the d/u ratio weighted by electroweak charges. Such an experiment is planned at Jefferson Lab, taking advantage of the high luminosity and energy available following the 12 GeV energy upgrade, and with the expected 1% measurements of the asymmetry it would strongly constrain the d/u ratio up to $x \sim 0.8$ [\[84\]](#page-13-19).

While still relying on nuclear targets, a novel idea proposes the use of mirror symmetric nuclei, such as 3He and 3H, in which the nuclear effects mostly cancel. Explicit calculations have confirmed that accurate extraction of F_2^n/F_2^p is possible from measured ratios of ³He to ³H structure functions, with nuclear corrections canceling to within \sim 1% up to $x \approx 0.85$ [[86](#page-13-21)].

Finally, an experimental program is under way to determine the F_2^n structure function from measurements of DIS on a deuterium target with low-momentum spectator protons in the backward center-of-mass hemisphere, which tags DIS on an almost free neutron in the deuteron [[87\]](#page-13-22). Preliminary results have confirmed the feasibility of this method, and future measurements of spectator protons at the 12 GeV energy updated Jefferson Lab, together with 3 He or 3 H spectators on 4 He targets, will be helpful both in determining the d quark at large x and in constraining the nuclear correction models.

VI. CONCLUSION

In this analysis, we have explored the possibility of extending the range of fitted DIS data in both W and Q to lower values than have been traditionally used in global PDF fits, in order to obtain an extension of the covered range of x. The results presented here show that excellent fits can result from such a procedure provided that target mass corrections, higher twist contributions, and nuclear corrections for deuterium targets are all taken into account. The resulting fits show that the leading twist u - and d-quark PDFs are stable with respect to the choices made for implementing the target mass corrections, as long as a flexible higher twist parametrization is employed.

The major new feature of our fits compared to previous global analyses is the stronger suppression of the d-quark distribution at large x. However, the precise amount of suppression is sensitive to the treatment of the nuclear corrections, which are an important source of theoretical uncertainty at $x \sim 1$. Hence, further progress in the determination of the behavior of the large-x PDFs and the d/u ratio requires either a better understanding of the nuclear corrections or the use of data obtained using free nucleons in the initial state, for which we reviewed several experimental possibilities.

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