Collider effects of unparticle interactions in multiphoton signals

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A new model of physics, with a hidden conformal sector which manifests itself as an unparticle coupling to standard model particles effectively through higher dimensional operators, predicts strong collider signals due to unparticle self-interactions. We perform a complete analysis of the most spectacular of these signals at the hadron collider, $p p(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$ and $\gamma \gamma gg$. These processes can go through the three-point unparticle self-interactions as well as through some s and t channel diagrams with one and/or two unparticle exchanges. We study the contributions of individual diagrams classified with respect to the number of unparticle exchanges and discuss their effect on the cross sections at the Tevatron and the LHC. We also restrict the Tevatron bound on the unknown coefficient of the three-point unparticle correlator. With the availability of data from the Tevatron, and the advent of the data emerging from the LHC, these interactions can provide a clear and strong indication of unparticle physics and distinguish this model from other beyond the standard model scenarios.

I. INTRODUCTION

The Large Hadron Collider (LHC) at CERN, once functional, will attempt to discover the last piece of the standard model (SM) puzzle (the Higgs boson, responsible for electroweak breaking) as well as hopefully provide signals of physics beyond the standard model (BSM). The main process responsible for producing a Higgs boson at the LHC is gluon fusion, and a light boson produced in such fashion is then expected to decay into two photons. Such a decay is supposed to be weak, as Higgs interact only weakly and in the SM the process occurs at one-loop level only.

In a BSM scenario, a new scalar field which is singlet under the SM gauge group can mix with the Higgs boson but also couple to photons and gluons directly through higher dimensional operators with a cutoff scale $\Lambda_{\mathcal{U}}$.
Such a model has been proposed by Georgi [1] hased on Such a model has been proposed by Georgi [[1](#page-17-0)], based on the hypothesis that there could be an exact scale-invariant hidden sector at a high energy scale. Below $\Lambda_{\mathcal{U}}$, the model
emerges as interpolating fields with general popintegral emerges as interpolating fields with general nonintegral scaling dimension $d_{\mathcal{U}}$, which behave like a $d_{\mathcal{U}}$ number of invisible massless particles—hence the term unparticle (U) used by Georgi. An unparticle does not possess a fixed invariant mass squared, but has a continuum mass spectrum, as a consequence of scale invariance

$$
\rho(p^2) = A_{d\mu}\theta(p^0)\theta(p^2)(p^2)^{d\mu-2},\tag{1}
$$

with $A_{d\mu}$ the normalization factor. The production of unparticles at low energies is described by an effective field

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theory and can give rise to peculiar energy distributions because of the nonintegral values of $d_{\mathcal{U}}$.

While the concept dates only to 2007 [[1\]](#page-17-0), there have been over 120 studies so far for implications of unparticle physics topics as varied as on neutrino physics [\[2](#page-17-1)] cosmology [\[3\]](#page-17-2), rare processes in the standard model [\[4](#page-17-3)], effects on precision measurements [[5](#page-17-4)], as well as specific low energy signals for the detection of unparticles [[6](#page-17-5)]. The peculiarities of unparticle physics have motivated numerous studies of their implications at the colliders [\[7](#page-17-6)[,8](#page-17-7)]. Recently, it has been pointed out [[9](#page-17-8)[,10\]](#page-17-9) that among collider signals, unparticle self-interactions give rise to spectacular effects in gluon fusion processes. (Note also the more recent study on unparticle self-interactions [[11](#page-17-10)]). In particular, while the interactions $gg \to \mathcal{U} \to \gamma \gamma$ lead to enhanced signals in the Higgs boson decay channels, the three-point selfinteractions $gg \to U \to UU \to \gamma \gamma \gamma \gamma$ are practically background free and may provide an unsuppressed and extremely promising signal for unparticle discovery. The unusual feature here is that the production of additional unparticles with high p_T in the final states does not suppress the production rate, unlike the production of known particles [\[9](#page-17-8)]. There is encouraging data from the L3 Collaboration on $\gamma\gamma$ interaction, which exceeds the prediction of the standard model by about 1 order of magnitude at the highest transverse momentum data [\[12\]](#page-17-11), and gluon fusion might show similar enhancements. Motivated by these considerations, in the present paper we extend the calculation in [[9](#page-17-8)], and we present a complete evaluation of the relevant diagrams, in a comparative fashion, for the processes $p p(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$ and $\gamma \gamma gg$ at both the Tevatron and the LHC. We restrict our analysis to the hadron colliders: the LHC because of the large center-of-mass energy, and the Tevatron, because it operates now and could pro-

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duce visible signals of physics BSM. A similar analysis is possible for ILC, but for our purposes, it is beyond the scope of this work. We also update the Tevatron bound on the three-point unparticle self-interaction discussed in [[9\]](#page-17-8), based on the complete evaluation of the cross section.

We proceed as follows: in Sec. [II](#page-1-0) we describe briefly the unparticle model features, concentrating on the ones relevant for our considerations. In Sec. III we present the numerical investigation of processes generated by unparticle self-interactions in $\gamma \gamma \gamma \gamma$ and $\gamma \gamma gg$ at both the Tevatron and the LHC. We compare the results obtained from production subprocesses, grouped by number of unparticles in intermediate states, and by channels. There are basically only two important unknown parameters, namely, the scaling dimension $d_{\mathcal{U}}$ and the cutoff scale $\Lambda_{\mathcal{U}}$. We restrict a third parameter emerging from the three-point restrict a third parameter, emerging from the three-point unparticle correlation function from the Tevatron data. We discuss the results obtained and conclude in Sec. IV. In the Appendix we give the complete list of relevant diagrams for our calculation.

II. UNPARTICLE FORMULATION

In this section, we summarize the basic features of unparticle physics. In order to be relevant, unparticles must interact with SM fields, although the detailed dynamics of the interactions are not known. These interactions are parametrized in the effective Lagrangian approach as interactions between a new physics operator \mathcal{O}_U with dimension $d_{\mathcal{U}}$ and the standard model operator \mathcal{O}_{SM} with dimension d_{SM}

$$
\mathcal{L} = \lambda_{d_{\rm SM}} \Lambda_{\mathcal{U}}^{4-d_{\rm U}-d_{\rm SM}} \mathcal{O}_{\mathcal{U}} \mathcal{O}_{\rm SM}
$$
 (2)

with $\lambda_{d_{SM}}$ a coupling constant of order 1. From scale invariance considerations, the phase space for the unparticle operator is a continuous spectral density

$$
d\text{LISP}_{d_{\mathcal{U}}} = A_{d_{\mathcal{U}}} \theta(p^0) \theta(p^2) (p^2)^{d_{\mathcal{U}} - 2} \frac{d^4 p}{(2\pi)^4} \tag{3}
$$

where $A_{d_{1}}$ is the normalization factor

$$
A_{du} = \frac{16\pi^{5/2}}{(2\pi)^{2d}u} \frac{\Gamma(d_{\mathcal{U}} + \frac{1}{2})}{\Gamma(d_{\mathcal{U}} - 1)\Gamma(2d_{\mathcal{U}})}.
$$
 (4)

Unparticle operators interact with the SM fields through the exchange of heavy particles of mass M. Integrating out the heavy fields produces a series of effective operators describing unparticle interactions with the SM fields at low energy [[1](#page-17-0)]. The operators describing the interactions for various unparticle spins are [[1](#page-17-0)[,7\]](#page-17-6)

$$
\text{Spin 0: } \lambda_0' \frac{1}{\Lambda_{\mathcal{U}}^{d_U - 1}} \bar{f} f \mathcal{O}, \lambda_0'' \frac{1}{\Lambda_{\mathcal{U}}^{d_U - 1}} \bar{f} i \gamma^5 f \mathcal{O},
$$
\n
$$
\lambda_0 \frac{1}{\Lambda_{\mathcal{U}}^{d_U}} G_{\alpha \beta} G^{\alpha \beta} \mathcal{O}, \cdots
$$
\n
$$
\text{Spin 1: } \lambda_1 \frac{1}{\Lambda_{\mathcal{U}}^{d_U - 1}} \bar{f} \gamma_{\mu} f \mathcal{O}^{\mu}, \lambda_1' \frac{1}{\Lambda_{\mathcal{U}}^{d_U - 1}} \bar{f} \gamma_{\mu} \gamma_5 f \mathcal{O}^{\mu}, \cdots
$$
\n
$$
\text{Spin 2: } -\frac{1}{4} \lambda_2' \frac{1}{\Lambda_{\mathcal{U}}^{d_U}} \bar{\psi} i (\gamma_{\mu} \vec{\mathbf{D}}_{\nu} + \gamma_{\nu} \vec{\mathbf{D}}_{\mu}) \psi \mathcal{O}^{\mu \nu},
$$
\n
$$
\lambda_2 \frac{1}{\Lambda_{\mathcal{U}}^{d_U}} G_{\mu \alpha} G^{\alpha}_{\nu} \mathcal{O}^{\mu \nu}, \cdots
$$

For the spin-0 case, the interaction of U with a fermion pair is suppressed if there is a γ_5 in the vertex and we neglect such terms. Note also that, unlike the above form, in our study this vertex is defined with a Higgs coupling such that the prefactor becomes $e\lambda_0'v/\Lambda_d^{d_u}$ where v is the Higgs vacuum expectation value and e is the proton charge. Higgs vacuum expectation value and e is the proton charge. Otherwise, one needs to introduce two cutoff scales.

A couple of remarks about the above list of interactions are in order here. The list of course is not complete as it stands. We only include the dominant dimension 3 and 4 operators in each spin case. For example there are would be operators like $\lambda_0'''(G_{\alpha\beta}G^{\alpha\beta})^2O/\Lambda_U^{d_U+4}$ which couples 4
SM gauge bosons with the unparticle but such interactions SM gauge bosons with the unparticle, but such interactions are suppressed with the power of $\Lambda_{\mathcal{U}}$. However, there is a dimension 2 term for spin-0 case which is interesting. This dimension 2 term for spin-0 case which is interesting. This term is of the form $HHO/\Lambda_U^{d_U-2}$ and becomes rather
problematic when the Higgs fields get a vacuum expectaproblematic when the Higgs fields get a vacuum expectation value, since such a term breaks conformal invariance due to a shifted conformal fixed point [[13](#page-17-12)]. The scale defined by the above term needs to be smaller than Λ \mathcal{U}
and preferably they are well separated to have a wide and preferably they are well separated to have a wide enough conformal window. Thus, in order to see unparticle signals the energy scale of any experiment should be higher than the conformal breaking scale. Otherwise, the unparticle sector turns into a conventional one. In fact, there are ways to include nonconformal effects through modifying the unparticle propagator [\[13,](#page-17-12)[14\]](#page-17-13). As far as our study at the LHC is concerned, in the kinematical region we are working such effects will be suppressed and we simply set the corresponding coupling constant at zero. Another point is about the convention used in the unparticle-fermion-fermion vertex. In the spin-0 case as an example, the coupling constant is defined as $e\lambda_0'v$ but
this is only for practical purposes since it allows to make this is only for practical purposes since it allows to make comparison easier with the composite lepton and quark theories available in the literature (see [[15](#page-17-14),[16](#page-17-15)] for details).

The propagators for the unparticles were suggested to be [\[8\]](#page-17-7)

$$
\Delta_F(p^2) = \frac{A_{d_{\mathcal{U}}}}{2\sin\pi d_{\mathcal{U}}} \frac{i}{(|p^2| + i0^+)^{2-d_{\mathcal{U}}}} e^{i\phi} \tag{5}
$$

for the scalar, and

$$
[\Delta_F(p^2)]_{\mu\nu} = \frac{A_{d_u}}{2\sin\pi d_u} \frac{i}{(|p^2| + i0^+)^{2-d_u}} e^{i\phi} \pi_{\mu\nu}(p)
$$
\n(6)

and

$$
\left[\Delta_F(p^2)\right]_{\mu\nu,\rho\sigma} = \frac{A_{d_u}}{2\sin\pi d_u}
$$

$$
\times \frac{i}{(\vert p^2 \vert + i0^{\dagger})^{2-d_u}} e^{i\phi} T_{\mu\nu,\rho\sigma}(p) \quad (7)
$$

for the spin-1 and spin-2 unparticle, respectively. The phase is defined as $\phi = \text{Arg} [(-p^2)^{du}]$. Thus, it is nonzero only in the s-channel where p^2 is nositive while ϕ is only in the s-channel where p^2 is positive while ϕ is identical to zero in the t - and u - channels. Of course, the $+i0^+$ piece is only relevant in the s channel. Here $\pi_{\mu\nu}$ = $-g_{\mu\nu}+\frac{p_\mu p_\nu}{p^2}$ and $T_{\mu\nu,\rho\sigma} = \frac{1}{2} \{\pi_{\mu\rho}(p)\pi_{\nu\sigma}(p) +$ $\pi_{\mu\sigma}(p)\pi_{\nu\rho}(p) - \frac{2}{3}\pi_{\mu\nu}(p)\pi_{\rho\sigma}(p)$.
For a scalar operator, unitarity req

For a scalar operator, unitarity requires as a lower bound, $d_{\mathcal{U}} \geq 1$. While no upper bound exists, supersymmetric examples suggest values of $d_U < 2$ [[17](#page-17-16)]. For vector unparticle operators $d_U > 3$ and for symmetric and antisymmetric tensor operators $d_u > 2$ and $d_u > 4$ respectively [\[18](#page-17-17)[,19\]](#page-17-18). The cross section is dependent on $d_{\mathcal{U}}$ as $1/\Lambda^{2d_{\mathcal{U}}}$
and it becomes much smaller for the values of $d_{\mathcal{U}}$ larger and it becomes much smaller for the values of $d_{\mathcal{U}}$ larger than 3. For this reason in this work we only consider the scalar unparticle effects.

A scalar unparticle couples to the standard model sector through

$$
\mathcal{L}_{\mathcal{U}} = -\frac{\lambda_g}{4} \frac{\mathcal{U}}{\Lambda^{d_{\mathcal{U}}}} G^A_{\mu\nu} G^{A\mu\nu} - \frac{\lambda_\gamma}{4} \frac{\mathcal{U}}{\Lambda^{d_{\mathcal{U}}}} F_{\mu\nu} F^{\mu\nu}.
$$
 (8)

The Feynman rules for the scalar and tensor unparticle operators coupling to the gg and $\gamma\gamma$ are, respectively,

$$
\mathcal{O}: 4i\lambda_{g,\gamma}^0 \frac{\mathcal{U}}{\Lambda^{d_u}}(-p_1 \cdot p_2 g^{\mu\nu} + p_1^{\nu} p^{\mu})
$$

$$
\mathcal{O}^{\mu\nu}: \lambda_{g,\gamma}^2 \frac{\mathcal{U}_{\rho\sigma}}{\Lambda^{d_u}} \big[K^{\mu\nu\rho\sigma} + K^{\mu\nu\sigma\rho}\big]
$$

$$
(9)
$$

where $K^{\mu\nu\rho\sigma} = -g^{\mu\nu} p_1^{\rho} p_2^{\sigma} - g^{\rho\mu} g^{\sigma\nu} p_1 \cdot p_2 + g^{\sigma\mu} p_1^{\nu} p_2^{\rho}$, and λ^0 , λ^2 are the scalar and tensor coupling constants constants.

Evaluation of the processes $p p(\bar{p}) \rightarrow \gamma \gamma g g$, $\gamma \gamma \gamma \gamma$ require evaluation of both the two-point correlation function [\[1,](#page-17-0)[8](#page-17-7)]:

$$
\langle 0|\mathcal{O}_U(x)\mathcal{O}_U^\dagger(0)|0\rangle = \int \frac{d^4P}{(2\pi)^4} e^{-iPx} \rho_U(P^2) \qquad (10)
$$

as well as the three-point interaction [\[9](#page-17-8)]:

$$
\langle 0|\mathcal{O}_U(x)\mathcal{O}_U(y)\mathcal{O}_U^{\dagger}(0)|0\rangle = \frac{C_d'}{(|x-y||x||y|)^{du}}.\tag{11}
$$

The latter yields, in momentum space, using the two-point

correlation function,

$$
\langle 0|\mathcal{O}_{\mathcal{U}}(p_1)\mathcal{O}_{\mathcal{U}}(p_2)\mathcal{O}_{\mathcal{U}}^{\dagger}(p_1 + p_2)|0\rangle
$$

\n
$$
= C_d \int \frac{d^4q}{(2\pi)^4} \{[-q^2 - i\epsilon][-(p_1 - q)^2 - i\epsilon] \times [-(p_2 + q)^2 - i\epsilon][(du/2) - 2] \times [-(p_2 + q)^2 - i\epsilon][(du/2) - 2] \times [-(q_2 + q)^2 - i\epsilon][(dq/2) - 2] \times [-(q_2 + q)^2 - i\epsilon
$$

where $n = 6(1 - d_{11}/4)$ and

$$
F_y\left(\frac{p_1^2}{s}, \frac{p_2^2}{s}\right) = \frac{\Gamma(n-2)}{16\pi^2[\Gamma(\frac{n}{3})]^3} \int_0^1 dx_1 dx_2 dx_3 (x_1 x_2 x_3)^{(n/3)-1} \times \delta(x_1 + x_2 + x_3 - 1) \left(\frac{1}{\Delta}\right)^{n-2} \tag{13}
$$

with $\Delta = x_1 x_2 p_1^2 / s + x_1 x_3 p_2^2 / s + x_2 x_3$ and $s = (p_1 + p_2)^2$ As a check we reproduced Fig. 2 in [9] where $\frac{2}{1}/s + x_1x_3p_2^2$
eck we repro $(p_1 + p_2)^2$. As a check, we reproduced Fig. 2 in [\[9](#page-17-8)] where F is plotted as a function of its one argument and got F_y is plotted as a function of its one argument and got complete agreement.

In all the analyses that follow we take $\lambda_{g,\gamma}^{0} = 1$ and $\lambda_{g,\gamma}^{0} = 1$ and $\lambda'_0 = \sqrt{2\pi}/e$ since the couplings are expected to be of order 1 from the naturalness requirement, and we reduce order 1 from the naturalness requirement, and we reduce the number of free parameters by setting them at unity (please note that λ'_0 is introduced differently than the other
for the reason mentioned earlier). We also restrict our for the reason mentioned earlier). We also restrict our considerations to the scalar unparticle, as it was shown that the vector and tensor give smaller contributions $[8]$ $[8]$ ¹

III. NUMERICAL ANALYSIS

The complete set of Feynman diagrams for the subprocesses gg, $q\bar{q} \rightarrow U \dots \rightarrow \gamma \gamma \gamma \gamma$ and for the subprocesses $gg, q\bar{q} \rightarrow U... \rightarrow \gamma \gamma gg$ are given in the Appendix. There are quite a number of diagrams contributing to the processes, requiring some automatization to do calculation. We generated our results using the software FeynArts and FormCalc [\[20\]](#page-17-19) and the Vegas Monte Carlo program for the four-body phase space integration as well as for the numerical evaluation of the function F_y . In order to avoid collinear singularities, we employ angular cuts as well as cuts on the transverse energies of the final photons and gluons. We require the final photons and gluons to have at least 30 GeV transverse energy and their ejection directions make at least 10 degrees with the beamline in the forward and backward directions. Since the unparticle model has unconventional features, the vertices and propagators of the software FeynArts and FormCalc required some modifications. The hadronization is done by using the LHAPDF version 5.3 [\[21\]](#page-17-20) with the parton distribution functions of CTEQ6LL. We neglect the masses of the light quarks in the proton while calculating the con-

¹Note that the vector unparticle does couple only to $q\bar{q}$ while
e tensor couples to both $q\bar{q}$ and $q\bar{q}$. the tensor couples to both $q\bar{q}$ and gg.

tributions from the quark pair. We also neglect the contributions from the SM diagrams but include the SM background separately. In fact, the SM backgrounds for $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ and the signals $p p \rightarrow \gamma \gamma g g$ go only through quark subprocesses at partonic level. Under the same conditions, we estimated the background cross sections as follows: at the Tevatron, 2.6×10^{-5} pb and 0.3 pb for $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ and $p\bar{p} \rightarrow \gamma \gamma gg$, respectively; at the LHC, 7.7 \times 10⁻⁵ pb (for $pp \rightarrow \gamma \gamma \gamma \gamma$) and 0.8 pb (for $pp \rightarrow$ $\gamma\gamma gg$).

In order to keep track of various contributions and make comparisons, we group the graphs according to the partonic constituents (gg or $q\bar{q}$), the number of unparticles present in the intermediate states, and whether they proceed through the s or the t channel. We follow the same path in the numerical evaluation of each contribution, which we discuss in the following subsections.

The existence of more than one external gluon requires extra care. To preserve the gauge invariance one either needs to include the ghost contributions or perform the gluon polarization sum for only the transversal polarization. We follow the second path by introducing appropriate projection operators for the transverse polarization states of the gluon. Since one can still do the sum conventionally for one of the gluons, in the $gg \rightarrow \gamma \gamma \gamma \gamma$ and $gg \rightarrow \gamma \gamma gg$ subprocesses, we need a single and three projection operators, respectively, when summation over the gluon polarizations is performed (for more details, see [[22](#page-17-21)]).

A. The multiphoton processes at the Tevatron

While the LHC seems to be still besieged by technical problems, it is worthwhile to explore signals coming from the physics of the largest currently running energy collider facility, the Tevatron at Fermilab. The Tevatron has accumulated yet unexplored data, and can still be expected to yield signals for physics beyond the standard model. With this in mind, we begin the exploration of unparticle interactions in the multiphoton signals at the Tevatron, specifically looking at the signals $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ and $p\bar{p} \rightarrow \gamma \gamma gg$. The center-of-mass energy $\sqrt{s} = 1.96$ GeV for the Tevatron is used throughout Tevatron is used throughout.

1. The process $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ at the Tevatron

We explore first the dependence of the total cross section on the value of the parameter $\Lambda_{\mathcal{U}}$. Figure [1](#page-4-0) shows the variation of the cross section with the unparticle energy variation of the cross section with the unparticle energy scale for three values of $d_{\mathcal{U}}$ (1.1, 1.5 and 1.9). As expected, the cross section is the largest for the smallest $d_{\mathcal{U}}$. Within each panel, we plot separately contributions from the two partonic channels (gg and $q\bar{q}$) and momentum transfer channels $(s \text{ and } t)$, and present separate contributions coming from one, two and three unparticle exchange. One of the processes, the s-channel contribution coming from the exchange of three unparticles as intermediate states in gg and $q\bar{q}$, was calculated in [\[9](#page-17-8)]. Clearly, as can be seen from all three graphs in Fig. [1](#page-4-0), this process is subdominant for all values of $\Lambda_{\mathcal{U}}$. As expected, the pro-
cesses with the least number of unparticles dominate as we cesses with the least number of unparticles dominate, as we must include in the evaluation 1 order of the energy scale proceeding through the s channel are suppressed compared Λ _U for every unparticle exchanged. In addition, processes to the t-channel, and the gg partonic contributions are much smaller at the Tevatron than the $q\bar{q}$ ones. We take $C_d = 1$ for our evaluations; however later we will use the known information on the Tevatron data to restrict C_d and discuss its effect to the maximal cross section. Looking at all the contributions, the cross section is dominated by the $q\bar{q}$ partonic contribution with one unparticle exchange proceeding through the t-channel, and could reach as much as around 1 fb. The cross section is very sensitive to the values of the d_U parameter, and is maximal for smaller $d_{\mathcal{U}}$.

In Fig. [2](#page-5-0) we show the dependence of the total cross section at the Tevatron on the d_{11} parameter for two fixed values of the unparticle scale $\Lambda_{\mathcal{U}} = 1$, 3 TeV. As each unparticle intermediate state contributes to the amplitude a unparticle intermediate state contributes to the amplitude a factor of $\frac{1}{\Lambda_u^{2d}u}$, the drop in cross section with increasing Λ_u is expected. The $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ cross section at $\sqrt{s} =$
1.96 TeV is dominated again by the $q\bar{q}$ partonic contribu-1.96 TeV is dominated again by the $q\bar{q}$ partonic contribution with one unparticle exchange proceeding through the *t*-channel, and for $\Lambda_{\mathcal{U}} = 1$ TeV, $d_{\mathcal{U}} = 1.1$, we recover the maximal (≈ 1 fb) value for the cross section. As a commaximal (\approx 1 fb) value for the cross section. As a common feature of both parameter investigations, the cross section for the process $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ is completely dominated by one set of diagrams only, the t channel $g\bar{g}$ with one unparticle exchange. We should also note that the diagrams with two $\mathcal U$ exchange in the *t*-channel, given in the Appendix, are proportional the mass of the quarks and we neglect them. This is also true for the subprocess $q\bar{q} \rightarrow$ $\gamma\gamma gg.$

2. The process $p\bar{p} \rightarrow \gamma \gamma gg$ at the Tevatron

We perform the same analysis for the process $p\bar{p} \rightarrow$ $\gamma \gamma gg$ at the Tevatron. Unlike the four-photon signal, this involves two jets which would be affected by background signals and whose identification requires further studies. The Feynman diagrams corresponding to this process are given in the Appendix. As before, the relevant parameters are $d_{\mathcal{U}}$ and $\Lambda_{\mathcal{U}}$ and we use the settings as in the four-
photon case. In Fig. 3 we show the dependence of the total photon case. In Fig. [3](#page-6-0) we show the dependence of the total cross section on energy scale of the unparticle, for three values of $d_{\mathcal{U}}$ (1.1, 1.5 and 1.9); and in Fig. [4](#page-7-0) we give the corresponding dependence on the d_U parameter, for two values of $\Lambda_{\mathcal{U}} = 1$, 3 TeV. The cross section in this case is
dominated by two contributions: the partonic contributions dominated by two contributions: the partonic contributions from $q\bar{q}$ and gg containing the minimal number of unparticles as intermediate states (one in this case), and without s-channel suppression (both *t*-channels). The cross section is further enhanced here with respect to $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$ by the presence of two powers of the strong coupling constant

 α_s replacing the electroweak one α_w , and could reach about 100 fb for the $\Lambda_{\mathcal{U}} = 1$ TeV, $d_{\mathcal{U}} = 1.1$ case.
Figure 4 shows that the maximal value for the cross section Figure [4](#page-7-0) shows that the maximal value for the cross section decreases by 2 orders of magnitudes when we increase $\Lambda_{\mathcal{U}}$
from 1 to 3 TeV. It is interesting to note that while the gg from 1 to 3 TeV. It is interesting to note that while the gg contribution is suppressed at the Tevatron for hadron production, and in unparticle-mediated $p\bar{p} \rightarrow \gamma \gamma \gamma \gamma$, it is very strong for the process $p\bar{p} \rightarrow \gamma \gamma gg$, while all the other subprocesses are subdominant.

B. The multiphoton processes at the LHC

We turn our attention to the four-photon production and two photon plus two gluon at the LHC and discuss these

FIG. 1 (color online). The $p\bar{p} \to \gamma\gamma\gamma\gamma$ cross section at $\sqrt{s} = 1.96$ TeV as a function of $\Lambda_{\mathcal{U}}$ for $C_d = 1$ and $d\mathcal{U} = 1.1$, $d\mathcal{U} = 1.5$
and $d\mathcal{U} = 1.9$. The individual contributions from the *a a* a and $d_U = 1.9$. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of unparticles exchanged.

two channels separately. We take throughout the center-ofmass energy $\sqrt{s} = 14$ TeV. We expect our signals to be significantly enhanced here and even more relevant comsignificantly enhanced here, and even more relevant compared to the Tevatron results if the unparticle scale Λ u
turns out to be large turns out to be large.

1. The process $pp \rightarrow \gamma \gamma \gamma \gamma$ at the LHC

At the LHC, $pp \rightarrow \gamma \gamma \gamma \gamma$ can proceed through gg and $q\bar{q}$ at the partonic level. At $\sqrt{s} = 14$ TeV the gluonic
components of the proton dominate, so one would expect components of the proton dominate, so one would expect the cross section to be dominated by the gg contribution. This is true only for a very small part of the parameter space, $\Lambda_{\mathcal{U}}$ < 1.2 TeV, and the result is dependent of the value of $d_{\mathcal{U}}$. (For instance for $d_{\mathcal{U}} = 1.5$ the $q\bar{q}$ contribuvalue of $d_{\mathcal{U}}$. (For instance, for $d_{\mathcal{U}} = 1.5$, the $q\bar{q}$ contribution dominates over the whole parameter space, whereas for $d_{11} = 1.1$ and 1.9 there is small region of the parameter space where the gg contribution is slightly larger.) The reason is that the $q\bar{q}$ partonic cross section can proceed through a single unparticle, while the gg requires at least two. The energy scale suppression associated with each unparticle overwhelms the advantage from the partonic distribution function of gluons versus quarks in the proton, and the correlation between the number of unparticles in a graph and the size of its contribution to the cross section dominates the cross section (see Fig. [5\)](#page-8-0). Here as before there is also an indication of s-channel suppression, thus the smallest contribution will be given by the process with three unparticles going through the s channel, with (in that instance) gg contribution dominating the $q\bar{q}$ one.

In Fig. [6](#page-9-0) we recover the expected Λ_u suppression (3
ders of magnitude going from $\Lambda_u = 1$ TeV to $\Lambda_u =$ orders of magnitude going from $\Lambda_{\mathcal{U}} = 1$ TeV to Λ
3 TeV). We also note that the total relative contribu 3 TeV). We also note that the total relative contribution
coming from different channels is changing: at $\Lambda_{d} =$ coming from different channels is changing: at Λ_{γ} Coming from different channels is changing. at $N_{\mathcal{U}}$ –
1 TeV mainly gg s and t channels with two unparticle
exchanges dominate and the gg t-channel with one unexchanges dominate, and the $q\bar{q}$ *t*-channel with one unparticle exchange contributes significantly, while at $\Lambda_{\mathcal{U}} =$ particle exchange contributes significantly, while at $N\mathcal{U} = 3$ TeV the cross section is dominated by the one-unparticle $q\bar{q}$ t-channel. This is indeed expected since larger values of $q\bar{q}$ t-channel. This is indeed expected since larger values of exchanges. The cross section in $pp \rightarrow \gamma \gamma \gamma \gamma$ can reach
about 10 fb for $\Lambda_{ac} = 1$ TeV and $d_{ac} = 1$ 1 (Again to be $\Lambda_{\mathcal{U}}$ suppress further the channels with many unparticle about 10 fb, for $\Lambda_{\mathcal{U}} = 1$ TeV and $d_{\mathcal{U}} = 1.1$. (Again to be expected as the suppression associated with each unparexpected, as the suppression associated with each unparticle is inversely proportional to $\Lambda_{\mathcal{U}}^{d_{\mathcal{U}}}$.)

2. The process $pp \rightarrow \gamma \gamma gg$ at the LHC

Finally, in Figs. [7](#page-10-0) and [8](#page-11-0) we show the dependence of the $pp \rightarrow \gamma \gamma gg$ cross section with the energy scale $\Lambda_{\mathcal{U}}$ and d_{α} parameter respectively at the LHC. The cross sections $d_{\mathcal{U}}$ parameter, respectively, at the LHC. The cross sections obtained in this case are the largest shown in this analysis, and can reach a spectacular 20–25 pb for the most advanta-

FIG. 2 (color online). The $p\bar{p} \to \gamma \gamma \gamma \gamma$ cross section at $\sqrt{s} = 1.96$ TeV as a function of $d\mu$ for $C_d = 1$ and $\Lambda \mu = 1$ TeV and $\Lambda \mu = 3$ TeV. The individual contributions from the *gg* and $q\bar{q}$ subprocesses -unparticles exchanged. $\Lambda_{\mathcal{U}} = 3$ TeV. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of

geous parameter point $\Lambda_{\mathcal{U}} = 1$ TeV and $d_{\mathcal{U}} = 1.1$. The cross sections are dominated by the *g g* t-channel partonic cross sections are dominated by the $gg t$ -channel partonic contribution with only one unparticle in the process, although perhaps slightly less so for $d_U = 1.9$. Increasing $\Lambda_{\mathcal{U}}$ from 1 to 3 TeV decreases the cross section
again by 2 orders of magnitude. It also slightly reorders the again by 2 orders of magnitude. It also slightly reorders the relative contributions coming from different channels, but not significantly.

C. The Tevatron bound on C_d

So far we set the three-point unparticle coupling constant C_d as unity. However, this parameter is practically

FIG. 3 (color online). The $p\bar{p} \to \gamma \gamma gg$ cross section at $\sqrt{s} = 1.96$ TeV as a function of $\Lambda_{\mathcal{U}}$ for $C_d = 1$ and $d\mathcal{U} = 1.1$, $d\mathcal{U} = 1.5$
and $d\mathcal{U} = 1.9$ The individual contributions from the *a g* and and $d_U = 1.9$. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of unparticles exchanged.

FIG. 4 (color online). The $p\bar{p} \to \gamma \gamma gg$ cross section at $\sqrt{s} = 1.96$ TeV as a function of $d\mu$ for $C_d = 1$ and $\Lambda \mu = 1$ TeV and $\Lambda \mu = 3$ TeV. The individual contributions from the *gg* and $q\bar{q}$ subprocesses are -unparticles exchanged. $\Lambda_{\mathcal{U}} = 3$ TeV. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of

unconstrained. In Ref. [[9\]](#page-17-8) an upper bound is obtained from the contribution of the three-point interactions using the multiphoton events in the Tevatron data with integrated luminosity $\mathcal{L} = 0.83$ fb⁻¹. Based on our results in previous subsections, we recalculate here the upper bound on C_d by including all contributions to multiphoton signal. The standard model predicts negligible background events, and no signal event is observed above the standard model prediction. Then at 95% CL the bound is [[9\]](#page-17-8)

$$
\mathcal{L} \times \sigma_{p\bar{p}\to 4\gamma} \le 3.04 \tag{14}
$$

where the right-hand side is the number of qualified events in the data. Here $\sigma_{p\bar{p}\to 4\gamma} \equiv \sigma_{p\bar{p}\to 4\gamma}^{q\bar{q}} + \sigma_{p\bar{p}\to 4\gamma}^{gg}$. Writing the total cross section as a sum of terms grouped in powers of C_d , we replace the cross section $\sigma_{p\bar{p}\to 4\gamma}$ in the left-hand side of the above expression by an quadratic equation

$$
\sigma_{p\bar{p}\to 4\gamma}^{UUU} C_d^2 + \sigma_{p\bar{p}\to 4\gamma}^{\text{mix}} C_d + \left(\sigma_{p\bar{p}\to 4\gamma}^{No-UUU} - \frac{3.04}{\mathcal{L}}\right) \le 0. \tag{15}
$$

The coefficients of various C_d terms are the corresponding cross sections calculated with $C_d = 1$ in the preceding subsections. Note that we cannot extract the $\Lambda_{\mathcal{U}}$ factors from the terms in the left-hand side of Eq. (15) since each from the terms in the left-hand side of Eq. [\(15\)](#page-7-1), since each scales differently with Λ _U. So, the upper bound on C_d can now be computed as the positive root of the above equation from our numerical study. The results are shown in Fig. [9.](#page-11-1) We separately include the results for the three-point interactions for comparison. Note that our cross section values from the three-point interactions are about a factor of 2 greater than the ones given in [\[9](#page-17-8)], which may be due to a different set of cuts used in each case as well as numerical precision in the computation of the function F_v , where we had to keep the number of iterations rather low. It is seen that, in comparison to the bounds from the three-point interactions only, the upper bounds on C_d are significantly reduced when all contributions are included. The deviation is much bigger for smaller values of $d_{\mathcal{U}}$. The order of reduction ranges from an order of magnitude to more than 3 orders of magnitude, depending on the values of d_U and and Λ _U parameters region. For example, the upper bound
on C, becomes around 4 at $d_{a} = 1.1$ and $\Lambda_{a} = 1$ TeV $\Lambda_{\mathcal{U}}$. We obtain much stronger bounds for the smaller $d_{\mathcal{U}}$ on C_d becomes around 4 at $d_u = 1.1$ and $\Lambda_u = 1$ TeV on C_d becomes around 4 at $u\eta = 1.1$ and $N\eta = 1$ TeV
while it can reach 8×10^3 if only the three-point unparticle
interaction cross section is kent. Thus, our earlier choice of interaction cross section is kept. Thus, our earlier choice of $C_d = 1$ turns out to be almost the maximal value at $(d_{\mathcal{U}}, \Lambda_{\mathcal{U}}) = (1.1, 1 \text{ TeV})$ and should be considered con-
servative for any set of bigger $(d_{\mathcal{U}}, \Lambda_{\mathcal{U}})$ values servative for any set of bigger $(d_{\mathcal{U}}, \Lambda_{\mathcal{U}})$ values.
Now what would be the effect of relaxing C

Now, what would be the effect of relaxing $C_d = 1$ and using maximal C_d on the processes $pp(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$ and $pp(\bar{p}) \rightarrow \gamma \gamma gg$ at both colliders? First of all, this would

FIG. 5 (color online). The $p p \to \gamma \gamma \gamma \gamma$ cross section at $\sqrt{s} = 14$ TeV as a function of $\Lambda_{\mathcal{U}}$ for $C_d = 1$ and $d\mathcal{U} = 1.1$, $d\mathcal{U} = 1.5$ and $d\mathcal{U} = 1.9$. The individual contributions from the *a a* and $d\$ $d_U = 1.9$. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of unparticles exchanged.

not change the total cross section significantly, as long as the cross section is dominated by the single unparticle exchange in either the s or t channel. Only if the interference terms between the three-point interactions and the rest of the interactions to the cross section are sizable will there be such enhancement, which is linear in C_d^{\max} . Of course, if we focus on the case of individual contributions enhancement, the three-point unparticle interaction part will receive the largest enhancement since it scales as C_d^{max} while in the rest there will be no change. A more precise analysis would first fit the curves in Fig. [9](#page-11-1) to get an approximate relation for C_d^{max} as a function of $d_{\mathcal{U}}$ when $\Lambda_{\mathcal{U}}$ is fixed.
Then a search for maximal value of the cross section would Then a search for maximal value of the cross section would use these functions to also obtain the relative contributions.

FIG. 6 (color online). The $p p \to \gamma \gamma \gamma \gamma$ cross section at $\sqrt{s} = 14$ TeV as a function of $d_\mathcal{U}$ for $C_d = 1$ and $\Lambda \mathcal{U} = 1$ TeV and Λ
3 TeV. The individual contributions from the *a a* and $a\bar{a}$ subprocesses THO: 0 (Color of other). The $p p \rightarrow \gamma \gamma \gamma \gamma$ closs section at $\sqrt{s} = 14$ TeV as a function of $a_{\mathcal{U}}$ for $C_d = 1$ and $N \mathcal{U} = 1$ TeV and $N \mathcal{U} = 3$ TeV. The individual contributions from the gg and $q\bar{q}$ subproce unparticles exchanged.

We find it unnatural to go to very large C_d values, as the bounds on it most likely will become stronger once some data from the LHC is available. As we did not include this in our evaluations, our obtained total cross section values are more conservative.

IV. SUMMARY AND CONCLUSION

Since the original suggestion of Georgi [[1\]](#page-17-0), and the formulation of unparticle physics, viewed as a conformal theory with exact scale invariance coupled to the standard model at high energies, numerous phenomenological explorations of this idea have been developed.

In the present work, we have presented a contribution to the study of implications of self-interactions of the low energy conformal sector. We concentrated on implications of such couplings on the multiphoton signal at the hadronic colliders, the Tevatron and the LHC. The processes $pp(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$ and $\gamma \gamma gg$ involve exchanges of one, two and three unparticles as intermediate states. The diagrams contributing to such processes involve unparticle exchanges, as well as unparticle and vector boson exchanges. The situation is unusual, and evaluation of these diagrams does not resemble expressions obtained form ordinary perturbation theory, as graphs with one, two or three internal unparticle exchanges contribute to the same subprocess. As every unparticle vertex contains a factor of $\frac{\lambda_{g,\,\gamma}^0}{\Lambda_{\,\mathcal{U}}^{d\,\mathcal{U}}}$ with interaction strength $\alpha_s(\alpha_w)$, the evaluation of the cross section includes a sum over terms with different while every SM particle couples to gluons (photons) cross section includes a sum over terms with different powers of coupling constants and of unparticle energy scale $\Lambda_{\mathcal{U}}$. Although this process is suppressed (in fact
negligible) in the SM and can only proceed here through negligible) in the SM and can only proceed here through (at least one) unparticle exchange, the total cross section is dominated by the diagrams with the minimal number of internal unparticles. We have calculated every contribution to the cross section separately, discriminating between s and t channels, number of internal unparticles, and partonic components. We confirm earlier results for the contribution of the three unparticle exchange and correlation function, but also show that this contribution is subdominant.

At the Tevatron and the LHC, multiphoton signals coming from unparticle exchanges give rise to significant cross sections, the most spectacular of which could be as large as 20–25 pb, in $pp \rightarrow \gamma \gamma gg$ at the LHC, for the most advantageous parameter point, the minimum $\Lambda_{\mathcal{U}}$ and $d_{\mathcal{U}}$
investigated $(\Lambda_{\mathcal{U}} = 1 \text{ TeV}$ and $d_{\mathcal{U}} = 1 \text{ I})$. We consider investigated (Λ μ = 1 TeV and $d\mu$ = 1.1). We consider
first the case in which C_i the counting from the threefirst the case in which C_d , the coupling from the threeunparticle correlation function is set to one. We then restrict the C_d parameter based on the Tevatron data. This was done previously, assuming the multiphoton pro-

FIG. 7 (color online). The $pp \to \gamma \gamma gg$ cross section at $\sqrt{s} = 14$ TeV as a function of $\Lambda_{\mathcal{U}}$ for $C_d = 1$ and $d_{\mathcal{U}} = 1.1$, $d_{\mathcal{U}} = 1.5$ and $d_{\mathcal{U}} = 1.9$. The individual contributions from the *gg* and $g\bar{$ $d_U = 1.9$. The individual contributions from the gg and $q\bar{q}$ subprocesses are grouped and shown for each channel and number of unparticles exchanged.

cess is dominated entirely by the three-unparticle exchange, where expressions for C_d can be obtained independently of the unparticle scale $\Lambda_{\mathcal{U}}$. In a complete
evaluation terms with different numbers of unparticles evaluation, terms with different numbers of unparticles enter the summation, and the restriction on C_d becomes a restriction on the quadratic roots of a $\Lambda_{\mathcal{U}}$ -dependent equation, rather than a simple inequality. For completeness, we present maximal bounds on C_d for both three-unparticle exchanges, as well as for the total cross section.

In concluding, the main point of our paper is to show that multiphoton signals at the hadron collider are significant if one includes the coupling of SM particles with one or

FIG. 8 (color online). The $p p \to \gamma \gamma g g$ cross section at $\sqrt{s} = 14$ TeV as a function of $d\eta$ for $C_d = 1$ and $\Lambda \eta = 1$ TeV and Λ
3 TeV. The individual contributions from the *a a* and $q\bar{q}$ subprocesses are groune THU. 8 (COIOI OIIIII). The $pp \rightarrow \gamma \gamma gg$ cross section at $\sqrt{s} = 14$ TeV as a function of $a_{\mathcal{U}}$ for $C_d = 1$ and $N\mathcal{U} = 1$ TeV and $N\mathcal{U} = 3$ TeV. The individual contributions from the gg and $q\bar{q}$ subprocesses a unparticles exchanged.

FIG. 9 (color online). The maximal C_d bounds from the Tevatron as a function of d_U for various Λ
function of Λ_d for various d_U on the right panel. The bounds are shown separately when only the FIG. 9 (color online). The maximal C_d bounds from the Tevatron as a function of d_U for various Λ_U on the left panel and as a function of Λ _U for various $d_{\mathcal{U}}$ on the right panel. The bounds are shown separately when only the three-point interactions are considered for comparison $\lambda^0 = 1$ and $\lambda' = \sqrt{2\pi}/e$ are used considered for comparison. $\lambda_{g,\gamma}^0 = 1$ and $\lambda_0' = \sqrt{2\pi}/e$ are used.

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FIG. 10. The Feynman diagrams contributing to the subprocess $gg \rightarrow \gamma \gamma \gamma \gamma$ with the three-point unparticle vertex (panel a), the s -channel (panel b) and the t - and u -channels (panel c).

FIG. 11. The Feynman diagrams contributing to the subprocess $q\bar{q} \to \gamma\gamma\gamma\gamma$ with the three-point unparticle vertex (panel a), the s-channel (panel b) and in the t- and u-channels with two unparticle \mathcal{U}_s exchanged (panel c). The quark $q_{i,j}$ represent all five light quarks and $i = j$.

FIG. 12. The Feynman diagrams contributing to the subprocess $q\bar{q} \to \gamma\gamma\gamma\gamma$ in the t-channel with a single unparticle \mathcal{U}_s exchanged. The corresponding u-channel diagrams are also included.

several unparticles, and if observed, these events would be a strong indication of unparticle physics.

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APPENDIX

In this section we give all the relevant Feynman diagrams for the processes studied. We include only diagrams in which at least one scalar unparticle \mathcal{U}_s contributes. The standard model diagrams are not included.

1. Feynman diagrams for the process $p p(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$

We start first with the $pp(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$ and group the figures into two: one for the gg partonic contribution, and the other for $q\bar{q}$ partonic contributions. Following the numerical estimates, we group further together graphs with the same number of unparticles in the intermediate states, and the processes going through the s and t - u channels together. They are all given in Figs. [10](#page-12-0)–[12.](#page-13-0) In all the diagrams, the wave and the spiral lines represent photon and gluon fields, respectively.

2. Feynman diagrams for the process $p p(\bar{p}) \rightarrow \gamma \gamma g g$

Next we present the Feynman graphs for the process $p p(\bar{p}) \rightarrow \gamma \gamma g g$. The organization of these is the same as for $p p(\bar{p}) \rightarrow \gamma \gamma \gamma \gamma$: we classify contributions from different partonic components first, then further group them according to the number of unparticles and the channel through which they proceed. They are all given in Figs. [13–](#page-14-0) [16.](#page-16-0)

FIG. 13. The Feynman diagrams contributing to the subprocess $gg \rightarrow \gamma \gamma gg$ with the three-point unparticle vertex in the s-channel (panel a), the three-point unparticle vertex in the t-channel (panel b), the s-channel with single unparticle exchange (panel c) and the s-channel with two-unparticle exchange (panel d).

FIG. 14. The Feynman diagrams contributing to the subprocess $gg \to \gamma \gamma gg$ in the t-channel with a single unparticle \mathcal{U}_s exchanged (panel a) and in the t-channel with two unparticles \mathcal{U}_s exchanged (panel b). The corresponding u-channel diagrams are also included.

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FIG. 15. The Feynman diagrams contributing to the subprocess $q\bar{q} \rightarrow \gamma \gamma gg$ with the three-point unparticle vertex (panel a), the s-channel with a single unparticle U_s exchanged (panel b) and the t-channel with two unparticles U_s exchanged (panel c) and in the tand u-channels with two unparticle \mathcal{U}_s exchanged (panel d). The quark $q_{i,j}$ represent all five light quarks and $i = j$.

FIG. 16. The Feynman diagrams contributing to the subprocess $gg \to \gamma \gamma gg$ in the t-channel with a single unparticle U_s exchanged. The corresponding u-channel diagrams are included.

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