Supersymmetry and an extra vectorlike generation

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Within the framework of supersymmetry, the particle content is extended in a way that each Higgs doublet is in a full generation. Namely, in addition to ordinary three generations, there is an extra vectorlike generation, and it is the extra slepton $SU(2)_L$ doublets that are taken to be the two Higgs doublets. *R*-parity violating interactions contain ordinary Yukawa interactions. Breaking of supersymmetry and gauge symmetry are analyzed. Fermion and boson spectra are calculated. Phenomenological constraints and relevant new physics at Large Hadron Collider are discussed.

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I. INTRODUCTION

The main stream spirit of the physics beyond the standard model (SM) is like the following. SM gauge interactions unify at a high scale ($\sim 10^{16}$ GeV) [1]. Supersymmetry (SUSY) [2] is then a must to stabilize the SM Higgs mass. The minimal SUSY extension of SM (MSSM), which necessarily involves two Higgs doublets, reinforces the idea of the grand unification theory (GUT) because of LEP data [3]. Further assuming *R*-parity conservation, the dark matter (DM) is provided [4].

However, things can be different. Before verification of SUSY GUT, other ideas should be pursued whenever they have reasonable points. In this Large Hadron Collider (LHC) era, discoverable ideas besides MSSM are of particular interests.

In this paper, we still use weak scale SUSY to extend the SM. Our consideration is as follows: The SUSY SM needs two Higgs doublets in order to provide masses to both upand down-type quarks. Fermions in each doublet cause anomaly. In MSSM, anomalies of the two doublets would cancel each other. The two Higgs doublets would be vectorlike matter in MSSM. They are very different from the three generation chiral matter in which the anomaly of each generation automatically vanishes. To treat the Higgs and the matter on equal footing, we introduce additional fields associated with each Higgs doublet, making them one generation leptons and quarks alike, the anomaly due to each SU(2) Higgsino cancels those of the new introduced. In such an extension, for example, the downtype Higgs is in the same position as a lepton doublet in a full matter generation. Immediately we find that except for the lepton and baryon numbers, the down-type Higgs and its associated fields can be identified as another full matter generation, that is the fourth generation.

The fourth chiral generation may have been generally disfavored because of the Z^0 decays, which show three generation light neutrinos only. There were many discussions about the fourth generation [5–8]. Ref. [7] introduced the fourth generation and identified its slepton as the Higgs. The partial role of sleptons in electroweak symmetry breaking (EWSB) was discussed previously [9]. Different from Ref. [7], we take the weak scale being a low energy one, therefore we still have two Higgs doublets. As we will see, when introducing SUSY, the fourth generation neutrino is automatically heavy because of the existence of the generation associated with the up-type Higgs.

The extra generations in this model are vectorlike. There are quite a few studies of vectorlike fermionic generations [5,10,11]. Vectorlike fermions may have interesting physical implications [12,13]. Within SUSY, Ref. [11] studied one mirror generation case. We introduce a vectorlike generation pair, which contains the two Higgs doublets required for EWSB.

This paper is organized as follows: In Sec. II, the model is constructed. SUSY breaking, EWSB, and particle spectra are presented. In Sec. III, phenomenological constraints are discussed. LHC phenomenology is given in Sec. IV. We summarize the model and further discuss its other aspects in the final section.

II. MODEL

In this paper, we consider a SUSY SM with a vectorlike generation. The particle contents are given below. In addition to the fourth generation superfields, L_4 , E_4^c , Q_4 , U_4^c , D_4^c , the up-type Higgs H_u and its associated matter (E_H^c , Q_H , U_H^c , D_H^c), which compose an anomaly free chiral generation, are introduced. Their quantum numbers under $SU(2)_L \times U(1)_Y \times SU(3)_c$ and the global baryon number are

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$$\begin{split} & L_m(2, -1, 1, 0), \qquad E_m^c(1, 2, 1, 0), \qquad Q_m(2, \frac{1}{3}, 3, \frac{1}{3}), \\ & U_m^c(1, -\frac{4}{3}, \overline{3}, -\frac{1}{3}), \qquad D_m^c(1, \frac{2}{3}, \overline{3}, -\frac{1}{3}), \qquad H_u(2, 1, 1, 0), \\ & E_H^c(1, -2, 1, 0), \qquad Q_H(2, -\frac{1}{3}, \overline{3}, -\frac{1}{3}), \qquad U_H^c(1, \frac{4}{3}, 3, \frac{1}{3}), \\ & D_H^c(1, -\frac{2}{3}, 3, \frac{1}{3}), \end{split}$$

where m = 1 - 4. In fact, the up-type Higgs family is in the antiparticle representation compared to particles in the other four ordinary generations. It will be massive after combining with one of the ordinary families.

The superpotential is written as follows: Instead of the R-parity, baryon number conservation is assumed,

$$\mathcal{W} = \mu_{m}L_{m}H_{u} + \mu_{m}^{e}E_{m}^{c}E_{H}^{c} + \mu_{m}^{Q}Q_{m}Q_{H} + \mu_{m}^{U}U_{m}^{c}U_{H}^{c} + \mu_{m}^{D}D_{m}^{c}D_{H}^{c} + \lambda_{lmn}L_{l}L_{m}E_{n}^{c} + \lambda_{lmn}^{\prime}Q_{l}L_{m}D_{n}^{c} + y_{mn}Q_{m}H_{u}U_{n}^{c} + y_{m}^{\prime}Q_{H}L_{m}U_{H}^{c} + \tilde{y}_{m}E_{H}^{c}D_{m}^{c}U_{H}^{c} + \tilde{y}_{mn}E_{m}^{c}D_{H}^{c}U_{n}^{c},$$
(1)

where μ_m 's are mass parameters, $\lambda^{(l)}$, $y^{(l)}$ and $\tilde{y}^{(l)}$'s coefficients. Note, l, m, n = 1-4. By redefining the down-type

Higgs and the other fourth generation fields,

$$H_{d} \equiv \frac{\mu_{m}}{\mu} L_{m}, \qquad E_{4}^{c} \equiv \frac{\mu_{m}^{e}}{\mu^{e}} E_{m}^{c}, \qquad Q_{4} \equiv \frac{\mu_{m}^{O}}{\mu^{O}} Q_{m},$$

$$U_{4}^{c} \equiv \frac{\mu_{m}^{U}}{\mu^{U}} U_{m}^{c}, \qquad D_{4}^{c} \equiv \frac{\mu_{m}^{D}}{\mu^{D}} D_{m}^{c},$$
(2)

where

$$\mu \equiv \sqrt{\sum_{m=1}^{4} |\mu_{m}|^{2}}, \qquad \mu^{e} \equiv \sqrt{\sum_{m=1}^{4} |\mu_{m}^{e}|^{2}},$$
$$\mu^{Q} \equiv \sqrt{\sum_{m=1}^{4} |\mu_{m}^{Q}|^{2}}, \qquad \mu^{U} \equiv \sqrt{\sum_{m=1}^{4} |\mu_{m}^{U}|^{2}}, \qquad (3)$$
$$\mu^{D} \equiv \sqrt{\sum_{m=1}^{4} |\mu_{m}^{D}|^{2}},$$

the superpotential is

$$\mathcal{W} = \mu H_{d}H_{u} + \mu^{e}E_{4}^{c}E_{H}^{c} + \mu^{Q}Q_{4}Q_{H} + \mu^{U}U_{4}^{c}U_{H}^{c} + \mu^{D}D_{4}^{c}D_{H}^{c} + y_{ij}^{l}L_{i}H_{d}E_{j}^{c} + y_{ij}^{d}Q_{i}H_{d}D_{j}^{c} + y_{ij}^{u}Q_{i}H_{u}U_{j}^{c} + \lambda_{ijk}L_{i}L_{j}E_{i}^{c} + \lambda_{ijk}L_{i}L_{j}E_{i}^{c} + y_{ij}^{e}Q_{4}L_{i}D_{j}^{c} + y_{ij}^{Q}Q_{4}H_{d}D_{i}^{c} + \lambda_{ij}^{D}Q_{i}L_{j}D_{4}^{c} + y_{i}^{D}Q_{i}H_{d}D_{4}^{c} + \lambda_{i}^{Q}Q_{4}L_{i}D_{4}^{c} + y_{i}^{Q}Q_{4}H_{d}D_{i}^{c} + \lambda_{ij}^{D}Q_{i}L_{j}D_{4}^{c} + y_{i}^{D}Q_{i}H_{d}D_{4}^{c} + \lambda_{i}^{Q}Q_{4}L_{i}D_{4}^{c} + y_{i}^{Q}Q_{4}H_{u}D_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + y_{i}^{Q}Q_{4}H_{u}U_{4}^{c} + \lambda_{i}^{Q}Q_{4}H_{u}U_{4}^{c} +$$

where field decomposition have been generally written as follows with i being 1–3:

$$L_{m} = c_{mi}L_{i} + c_{m4}H_{d}, \qquad E_{m}^{c} = c_{mi}^{e}E_{i}^{c} + c_{m4}^{e}E_{4}^{c}, \qquad Q_{m} = c_{mi}^{Q}Q_{i} + c_{m4}^{Q}Q_{4},$$
$$U_{m}^{c} = c_{mi}^{U}U_{i}^{c} + c_{m4}^{U}U_{4}^{c}, \qquad D_{m}^{c} = c_{mi}^{D}D_{i}^{c} + c_{m4}^{D}D_{4}^{c}, \qquad (5)$$

and the coefficients are

$$y_{ij}^{l} = 2\lambda_{lmn}c_{li}c_{m4}c_{nj}^{e}, \qquad y_{ij}^{d} = \lambda_{lmn}^{\prime}c_{li}^{Q}c_{m4}c_{nj}^{D}, \qquad y_{ij}^{u} = y_{mn}c_{mi}^{Q}c_{nj}^{U}, \qquad \lambda_{ijk} = \lambda_{lmn}c_{li}c_{mj}c_{nk}^{e}, \\ \lambda_{ijk}^{\prime} = \lambda_{lmn}^{\prime}c_{li}^{Q}c_{mj}c_{nk}^{D}, \qquad \lambda_{ij}^{E} = \lambda_{lmn}c_{li}c_{mj}c_{n4}^{e}, \qquad y_{i}^{E} = 2\lambda_{lmn}c_{li}c_{m4}c_{n4}^{e}, \qquad \lambda_{ij}^{Q} = \lambda_{lmn}^{\prime}c_{l4}^{Q}c_{mi}c_{nj}^{D}, \\ y_{i}^{Q\prime} = \lambda_{lmn}^{\prime}c_{l4}^{Q}c_{m4}c_{ni}^{D}, \qquad \lambda_{ij}^{D} = \lambda_{lmn}^{\prime}c_{li}^{Q}c_{mj}c_{n4}^{D}, \qquad y_{i}^{D} = \lambda_{lmn}^{\prime}c_{li}^{Q}c_{m4}c_{n4}^{D}, \qquad \lambda_{ij}^{QD} = \lambda_{lmn}^{\prime}c_{l4}^{Q}c_{mi}c_{n4}^{D}, \\ y^{QD} = \lambda_{lmn}^{\prime}c_{l4}^{Q}c_{m4}c_{n4}^{D}, \qquad y_{i}^{U} = y_{mn}c_{mi}^{Q}c_{n4}^{U}, \qquad y_{i}^{Q} = y_{mn}c_{m4}^{Q}c_{ni}^{U}, \qquad y^{QU} = y_{mn}c_{m4}^{Q}c_{n4}^{U}, \\ \lambda_{i}^{\prime} = y_{m}^{\prime}c_{mi}, \qquad y = y_{m}^{\prime}c_{m4}, \qquad \tilde{\lambda}_{i} = \tilde{y}_{m}c_{mi}^{e}c_{ni}^{U}, \qquad \tilde{\lambda}^{EU} = \tilde{y}_{mn}c_{m4}^{e}c_{n4}^{U}. \end{cases}$$

From the superpotential (4), we see that because of Dirac mass terms of up-type Higgs and the four generations, one of the four generation, namely, the fourth generation (H_d , E_4^c , Q_4 , U_4^c , D_4^c), is always heavy, which is identified as the one containing the down-type Higgs. The fourth generation neutrino together with the "neutrino" in H_u consists of Higgsinos. After the mass terms, the next five terms in Eq. (4) are ordinary Yukawa interactions and trilinear lepton number (*R*-parity) violating terms, where *i*,

j, *k* stand for three light generations. The other terms in (4) are new, which involve extra generations. Many of these new terms violate lepton numbers. Note that by taking $\mu^{e,Q,U,D} \gg \mu \sim \mathcal{O}$ (TeV), we obtain MSSM as a low energy effective theory.

A. SUSY breaking

Soft SUSY breaking mass terms should be included into the Lagrangian. In addition to gaugino masses, they include mass-squared terms of scalars and $B\mu$ -type terms corresponding to those μ terms in superpotential (1),

$$-\mathcal{L} \supset M^{2}\tilde{L}_{m}^{\dagger}\tilde{L}_{m} + M_{h}^{2}h_{u}^{\dagger}h_{u} + M_{E}^{2}\tilde{E}_{m}^{c\dagger}\tilde{E}_{m}^{c} + M_{Q}^{2}\tilde{Q}_{m}^{\dagger}\tilde{Q}_{m}$$

$$+ M_{U}^{2}\tilde{U}_{m}^{c\dagger}\tilde{U}_{m}^{c} + M_{D}^{2}\tilde{D}_{m}^{c\dagger}\tilde{D}_{m}^{c} + M_{EH}^{2}\tilde{E}_{H}^{c\ast}\tilde{E}_{H}^{c}$$

$$+ M_{QH}^{2}\tilde{Q}_{H}^{\dagger}\tilde{Q}_{H} + M_{UH}^{2}\tilde{U}_{H}^{c\ast}\tilde{U}_{H}^{c} + M_{DH}^{2}\tilde{D}_{H}^{c\ast}\tilde{D}_{H}^{c}$$

$$+ (B\mu_{m}\tilde{L}_{m}h_{u} + B^{e}\mu_{m}^{e}\tilde{E}_{m}^{c}\tilde{E}_{H}^{c} + B^{Q}\mu_{m}^{Q}\tilde{Q}_{m}\tilde{Q}_{H}$$

$$+ B^{U}\mu_{m}^{U}\tilde{U}_{m}^{c}\tilde{U}_{H}^{c} + B^{D}\mu_{m}^{D}\tilde{D}_{m}^{c}\tilde{D}_{H}^{c} + \text{H.c.}), \qquad (7)$$

where tildes stand for scalars. We have assumed universality of the mass-squared terms and the alignment of the *B* terms, namely, the mass parameters $B^{e,Q,U,D}$ do not depend on the subscript *m*. In terms of three light generations of Eq. (4), universality of these soft mass terms is easily seen,

$$-\mathcal{L} \supset M^{2}\tilde{L}_{i}^{\dagger}\tilde{L}_{i} + M^{2}h_{d}^{\dagger}h_{d} + M_{h}^{2}h_{u}^{\dagger}h_{u} + M_{E}^{2}\tilde{E}_{m}^{c\dagger}\tilde{E}_{m}^{c} + M_{Q}^{2}\tilde{Q}_{m}^{\dagger}\tilde{Q}_{m} + M_{U}^{2}\tilde{U}_{m}^{c\dagger}\tilde{U}_{m}^{c} + M_{D}^{2}\tilde{D}_{m}^{c\dagger}\tilde{D}_{m}^{c} + M_{EH}^{2}\tilde{E}_{H}^{c\ast}\tilde{E}_{H}^{c} + M_{QH}^{2}\tilde{Q}_{H}^{\dagger}\tilde{Q}_{H} + M_{UH}^{2}\tilde{U}_{H}^{c\ast}\tilde{U}_{H}^{c} + M_{DH}^{2}\tilde{D}_{H}^{c\ast}\tilde{D}_{H}^{c} + (B\mu h_{d}h_{u} + B^{e}\mu^{e}\tilde{E}_{4}^{c}\tilde{E}_{H}^{c} + B^{Q}\mu^{Q}\tilde{Q}_{4}\tilde{Q}_{H} + B^{U}\mu^{U}\tilde{U}_{4}^{c}\tilde{U}_{H}^{c} + B^{D}\mu^{D}\tilde{D}_{4}^{c}\tilde{D}_{H}^{c} + H.c.).$$
(8)

Numerically soft masses *M*'s, *B*'s and gaugino masses are assumed to be O(100) GeV.

Soft trilinear terms corresponding to Eq. (1) are

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$$\mathcal{L} \supset \bar{\lambda}_{lmn} \tilde{L}_l \tilde{L}_m \tilde{E}_n^c + \bar{\lambda}'_{lmn} \tilde{Q}_l \tilde{L}_m \tilde{D}_n^c + \bar{y}_{mn} \tilde{Q}_m h_u \tilde{U}_n^c$$

$$+ \bar{y}'_m \tilde{Q}_H \tilde{L}_m \tilde{U}_H^c + \bar{\tilde{y}}_m \tilde{E}_H^c \tilde{D}_m^c \tilde{U}_H^c + \bar{\tilde{y}}_{mn} \tilde{E}_m^c \tilde{D}_H^c \tilde{U}_n^c$$

$$+ \text{H.c.},$$

$$(9)$$

. . .

where the following coupling alignment will be assumed,

$$\bar{\lambda}_{lmn}^{(l)} = \lambda_{lmn}^{(l)} m_0, \qquad \bar{y}_{mn} = y_{mn} m_0, \qquad \bar{y}_m' = y_m' m_0$$
(10)

with m_0 being the order of soft masses $\sim \mathcal{O}(100)$ GeV.

B. EWSB

Let us look at gauge symmetry breaking. From the Lagrangian, the scalar potential can be written down straightforwardly. To get EWSB, one needs a negative determinant of the Higgs mass-squared matrix, namely,

$$(M^2 + \mu^2)(M_h^2 + \mu^2) < |B\mu|^2$$
(11)

with the ordinary condition $M^2 + M_h^2 + 2\mu^2 + 2B\mu > 0$. This requirement can be realized when the renormalization group is considered. M_h^2 will become negative at the weak scale, due to the large top quark Yukawa coupling. Therefore, everything of EWSB here will be the same as that in MSSM. The MSSM analysis of EWSB applies here. EWSB in this model occurs at the weak scale.

In addition to $B\mu$, other $B\mu$ terms in Eqs. (7) and (8) might complicate the gauge symmetry breaking analysis. The experience from MSSM shows that if a $B\mu$ term is large enough, gauge symmetry breaking always occurs. The new $B^{Q,U,D} \mu^{Q,U,D}$ terms could result in color symmetry breaking, and the $B^e \mu^e$ term could cause purely $U(1)_Y$ symmetry breaking. Such unwanted gauge symmetry breaking should be avoided. To be concrete, besides Eq. (11), correct EWSB also requires

$$(M_X^2 + \mu^{X2})(M_{XH}^2 + \mu^{X2}) > |B^X \mu^X|^2 \quad \text{for } X = e, Q, U, D.$$
(12)

Then the remaining analysis of EWSB is identical to that of MSSM with same Higgs and Higgsino spectra. Equation (12) can be satisfied easily. Careful thinking of EWSB conditions Eqs. (11) and (12), we see that if $\mu < \mu^X$, EWSB occurs naturally. This point will be discussed later. The fact that pure U(1)_Y breaking does not occur can be simply due to a large enough μ^e compared to μ .

In the scalar potential, quartic terms are determined by SUSY gauge interactions. From the point of view of quartic terms, the larger the coefficients of certain quartic terms, the more difficult the gauge symmetry breaking is. Therefore, EWSB is easier to be obtained compared to that of the color symmetry. Traditional $SU(2)_L \times U(1)_Y$ breaking via Higgs doublet fields contains the quartic term

$$V \supset \frac{g^2 + g'^2}{8} (h_u^{\dagger} h_u - h_d^{\dagger} h_d)^2 + \dots \dots$$
(13)

Whereas for purely $U(1)_Y$ symmetry breaking, the relevant quartic term is

$$V \supset \frac{g^{\prime 2}}{2} (\tilde{E}_H^{c*} \tilde{E}_H^c - \tilde{E}_4^{c*} \tilde{E}_4^c)^2 + \dots \dots$$
(14)

Because $g'^2/2$ is comparable to $(g^2 + g'^2)/8$ numerically at the weak scale, pure U(1)_Y symmetry breaking is not really favored.

C. Fermion spectra

We write down relevant matter superfields in $SU(2)_L$ components explicitly,

$$L_i = \begin{pmatrix} L_i^0 \\ L_i^- \end{pmatrix}, \qquad Q_m = \begin{pmatrix} Q_m^t \\ Q_m^b \end{pmatrix} \text{ and } Q_H = \begin{pmatrix} Q_H^b \\ Q_H^t \end{pmatrix}.$$

Because fourth generation doublet leptons have been taken as Higgsinos, and EWSB is the same as that in MSSM, gauginos and Higgsinos are identical to those in MSSM. In the following we first look at the lepton spectrum. As we have seen, the first three generation sneutrinos do not obtain vacuum expectation values. $SU(2)_L$ doublet leptons, therefore, do not mix with the down-type Higgsino and chargino. Lepton masses are due to ordinary Yukawa couplings and Yukawa couplings between $SU(2)_L$ doublet leptons with the fourth generation singlet lepton, as well as the μ^e term,

$$\mathcal{L} \supset -(e_i^-, e_H^c) \mathcal{M}^l \begin{pmatrix} e_j^c \\ e_4^c \end{pmatrix}, \tag{15}$$

where small letters denote fermionic components, the 4×4 charged lepton mass matrix is given as

$$\mathcal{M}^{l} = \begin{pmatrix} m_{ij}^{l} & m_{i4}^{l} \\ 0 & \mu^{e} \end{pmatrix}, \tag{16}$$

where $m_{ij}^l \equiv y_{ij}^l \frac{v}{\sqrt{2}} \cos\beta$, $m_{i4}^l \equiv y_i^E \frac{v}{\sqrt{2}} \cos\beta$. Consider typically the third and fourth generation case, namely, that of *i*, *j* being 3, taking $\frac{|m'_{33}||m'_{34}|}{|\mu^{\epsilon}|^2 - |m'_{33}|^2 + |m'_{34}|^2} \ll 1$, lepton masses are obtained,

$$m_{\tau} \simeq \sqrt{|m_{33}^l|^2 - |m_{33}^l||m_{34}^l|}, \qquad M_l \simeq |\mu^e|.$$
 (17)

The unitary matrix diagonalizing $\mathcal{M}^{l}\mathcal{M}^{l\dagger}$ is then

$$\begin{pmatrix} 1 & -(1 + \frac{|m_{33}^l|}{|m_{34}^l|})\frac{m_{44}^{l*}}{\mu^{e^*}} \\ \frac{m_{34}^l}{\mu^{e}} & 1 \end{pmatrix} + \mathcal{O}\left(\frac{m_{\tau}}{\mu^{e}}\right)^2.$$
(18)

This implies that there is an

$$\mathcal{O}\left(\frac{m_{\tau}}{\mu^{e}}\right)^{2}$$

unitarity deviation among the three generation leptons.

For the down-type quark spectrum, introduction of additional two generations makes the full down quark mass matrix \mathcal{M}^d being a 5 × 5 one,

$$\mathcal{L} \supset -(q_i^b, q_4^b, d_H^c) \mathcal{M}^d \begin{pmatrix} d_j^c \\ d_4^c \\ q_H^c \end{pmatrix},$$
(19)

and

$$\mathcal{M}^{d} = \begin{pmatrix} m_{ij}^{d} & m_{i4}^{d} & 0\\ m_{4j}^{d} & m_{44}^{d} & -\mu^{Q}\\ 0 & -\mu^{D} & 0 \end{pmatrix},$$
(20)

where $m_{ij}^d \equiv y_{ij}^d \frac{v}{\sqrt{2}} \cos\beta$, $m_{i4}^d \equiv y_i^D \frac{v}{\sqrt{2}} \cos\beta$, $m_{4i}^d \equiv y_i^{Q'} \frac{v}{\sqrt{2}} \cos\beta$, $m_{44}^d \equiv y^{QD} \frac{v}{\sqrt{2}} \cos\beta$. The 3 × 3 submatrix m_{ij}^d is the ordinary down quark mass matrix, which is now not necessarily unitary. Focusing on its unitarity de-

viation due to extra generations, we consider the sub-mass matrix of the third generation and extra generations, that is \mathcal{M}^d with *i* and *j* being 3. It is natural to take $|\mu^Q| \sim |\mu^D| \gg |m_{4j}^d|$, $|m_{44}^d|$, $|m_{ij}^d|$, $|m_{i4}^d|$. To the first order of m_{mn}^d/μ^D with *m* and *n* being 3 and 4, the absolute mass eigenvalues are then $|\mu^Q|$, $|\mu^D|$ and $|m_{33}^d|$, respectively. The mass matrix is diagonalized by unitary matrices U^d and V^d ,

$$U^{d\dagger} \mathcal{M}^{d} V^{d} = \begin{pmatrix} m_{b} & 0 & 0\\ 0 & \mu^{Q} & 0\\ 0 & 0 & \mu^{D} \end{pmatrix},$$
(21)

where

$$U^{d} = \begin{pmatrix} 1 & 0 & -\frac{m_{34}^{2}}{\mu^{D}} \\ 0 & 1 & -\frac{|m_{34}^{d}|^{2}}{\mu^{D}m_{44}^{d*}} \\ -\frac{m_{34}^{d*}}{\mu^{D*}} & \frac{\mu^{D}m_{44}^{d*}}{|\mu^{D}|^{2} - |\mu^{Q}|^{2}} & 1 \end{pmatrix} + \mathcal{O}\left(\frac{m_{b}}{\mu^{D}}\right)^{2}, \quad (22)$$

and

$$V^{d} = \begin{pmatrix} 1 & -\frac{m_{43}^{d*}}{\mu^{Q^{*}}} & 0\\ 0 & \frac{|m_{43}^{d}|^{2}}{\mu^{Q^{*}}m_{44}^{d}} & 1\\ \frac{m_{43}^{d}}{\mu^{Q}} & 1 & \frac{\mu^{Q^{*}}m_{44}^{d}}{|\mu^{Q}|^{2} - |\mu^{D}|^{2}} \end{pmatrix} + \mathcal{O}\left(\frac{m_{b}}{\mu^{D}}\right)^{2}.$$
 (23)

Therefore, there is generally an

$$\mathcal{O}\left(\frac{m_b}{\mu^D}\right)^2$$

contribution to unitarity deviation of the Cabbibo-Kobayashi-Maskawa (CKM) matrix.

Similarly, the up-type quark mass matrix \mathcal{M}^u is given in the following:

$$\mathcal{L} \supset -(q_i^t, q_4^t, u_H^c) \mathcal{M}^u \begin{pmatrix} u_j^c \\ u_4^c \\ q_H^b \end{pmatrix},$$
(24)

and

$$\mathcal{M}^{u} = \begin{pmatrix} m_{ij}^{u} & m_{i4}^{u} & 0\\ m_{4j}^{u} & m_{44}^{u} & \mu^{Q}\\ 0 & \mu^{U} & -m_{H}^{u} \end{pmatrix},$$
(25)

where $m_{ij}^{u} \equiv -y_{ij}^{u} \frac{v}{\sqrt{2}} \sin\beta$, $m_{i4}^{u} \equiv -y_{i}^{U} \frac{v}{\sqrt{2}} \sin\beta$, $m_{4j}^{u} \equiv -y_{j}^{Q} \frac{v}{\sqrt{2}} \sin\beta$, $m_{44}^{u} \equiv -y^{QU} \frac{v}{\sqrt{2}} \sin\beta$, and $m_{H}^{u} \equiv y \frac{v}{\sqrt{2}} \cos\beta$. Taking that $|\mu^{Q}| \sim |\mu^{U}| \gg |m_{4j}^{u}|$, $|m_{44}^{u}|$, $|m_{ij}^{u}|$, $|m_{i4}^{u}|$, $|m_{H}^{u}|$, the absolute mass eigenvalues are $|\mu^{Q}|$, $|\mu^{U}|$, and $|m_{33}^{u}|$, respectively. The diagonalizing matrices to Eq. (25) are U^{u} and V^{u} ,

$$U^{u\dagger} \mathcal{M}^{u} V^{u} = \begin{pmatrix} m_{t} & 0 & 0\\ 0 & \mu^{Q} & 0\\ 0 & 0 & \mu^{U} \end{pmatrix}, \qquad (26)$$

where

$$U^{u} = \begin{pmatrix} 1 & 0 & \frac{m_{34}^{u}}{\mu^{U}} \\ 0 & 1 & \frac{|m_{H}^{u}|^{2} + |m_{34}^{u}|^{2}}{\mu^{0^{s}} m_{H}^{u} - \mu^{U} m_{44}^{us}} \\ -\frac{m_{34}^{u^{s}}}{\mu^{U^{s}}} & \frac{\mu^{U} m_{44}^{u^{s}} - m_{H}^{u} \mu^{Q^{s}}}{|\mu^{Q}|^{2} - |\mu^{U}|^{2} - |m_{H}^{u}|^{2}} & 1 \end{pmatrix} + \mathcal{O}\left(\frac{m_{t}}{\mu^{U}}\right)^{2}, \tag{27}$$

and

$$V^{u} = \begin{pmatrix} 1 & \frac{m_{43}^{u}}{\mu^{Q^{*}}} & 0 \\ 0 & \frac{|m_{H}^{u}|^{2} + |m_{43}^{u}|^{2}}{\mu^{U}m_{H}^{u^{*}} - \mu^{Q^{*}}m_{44}^{u}} & 1 \\ -\frac{m_{43}^{u}}{\mu^{Q}} & 1 & \frac{\mu^{Q^{*}}m_{44}^{u} - m_{H}^{u^{*}}\mu^{U}}{|\mu^{U}|^{2} - |\mu^{Q}|^{2} - |m_{H}^{u}|^{2}} \end{pmatrix} + \mathcal{O}\left(\frac{m_{t}}{\mu^{U}}\right)^{2}.$$
(28)

The contribution to unitarity deviation of the CKM matrix can be as large as $(m_t/\mu^U)^2$.

D. Boson spectra

Boson masses are more complicated than the fermion case because of soft terms as well as SUSY kinetic terms. Higgs bosons, and therefore gauge bosons, in this model have exactly the same spectra as those in MSSM. So we will only consider slepton and squark masses.

SUSY kinetic terms contribute sfermion masses in the same manner like that in MSSM,

$$V \supset m_Z^2 \cos 2\beta (I_3 - \sin^2 \theta_W Q) f^* f, \qquad (29)$$

where θ_W is the Weinberg angle, and the field f denotes \tilde{L}_i , \tilde{Q}_m , \tilde{Q}_H , \tilde{E}_{Ri} , \tilde{E}_4 , \tilde{E}_H , \tilde{U}^c_m , \tilde{D}^c_m , \tilde{D}^c_H , \tilde{U}^c_H . Trilinear terms in Eqs. (9) and (10) contribute

$$\mathcal{L} \supset -m_0(m_{im}^l \tilde{L}_i^- \tilde{E}_m^c + m_{mn}^d \tilde{Q}_m^b \tilde{D}_n^c + m_{mn}^u \tilde{Q}_m^t \tilde{U}_n^c + m_H^u \tilde{Q}_B^b \tilde{U}_H^c + \text{H.c.}).$$
(30)

The superpotential, which involves μ terms and Yukawa interactions, contributes

$$\mathcal{L} \supset -[|\mu|^{2}(h_{d}^{\dagger}h_{d} + h_{u}^{\dagger}h_{u}) + |\mu^{e}|^{2}(\tilde{E}_{4}^{c*}\tilde{E}_{4}^{c} + \tilde{E}_{H}^{c*}\tilde{E}_{H}^{c}) + |\mu^{Q}|^{2}(\tilde{Q}_{4}^{\dagger}\tilde{Q}_{4} + \tilde{Q}_{H}^{\dagger}\tilde{Q}_{H}) + |\mu^{U}|^{2}(\tilde{U}_{4}^{c*}\tilde{U}_{4}^{c} + \tilde{U}_{H}^{c*}\tilde{U}_{H}^{c}) + |\mu^{D}|^{2}(\tilde{D}_{4}^{c*}\tilde{D}_{4}^{c} + \tilde{D}_{H}^{c*}\tilde{D}_{H}^{c}) + |m_{H}^{u}|^{2}(\tilde{U}_{H}^{c*}\tilde{U}_{H}^{c} + \tilde{Q}_{H}^{b*}\tilde{Q}_{H}^{b}) + \tilde{E}^{c*}m^{l\dagger}m^{l}\tilde{E}^{c} + \tilde{D}^{c*}m^{d\dagger}m^{d}\tilde{D}^{c} + \tilde{U}^{c*}m^{u\dagger}m^{u}\tilde{U}^{c} + \tilde{L}m^{l}m^{l\dagger}\tilde{L}^{*} + \tilde{Q}^{b}m^{d}m^{d\dagger}\tilde{Q}^{b*} + \tilde{Q}^{t}m^{u}m^{u\dagger}\tilde{Q}^{t*} - (\mu\tan\beta\tilde{L}m^{l}\tilde{E}^{c} + \mu\tan\beta\tilde{Q}^{b}m^{d}\tilde{D}^{c} + \mu\cot\beta\tilde{Q}^{t}m^{u}\tilde{U}^{c} + \mu\tan\beta m_{H}^{u}\tilde{Q}_{H}^{d}\tilde{U}_{H}^{c} + \mu^{e*}m_{l4}^{l}\tilde{L}_{i}^{-}\tilde{E}_{H}^{c*} + \mu^{D*}m_{m4}^{d}\tilde{Q}_{m}^{b}\tilde{D}_{H}^{c*} + \mu^{U*}m_{m4}^{u}\tilde{Q}_{m}^{t}\tilde{U}_{H}^{c*} + \mu^{Q*}m_{H}^{u}\tilde{Q}_{4}^{t*}\tilde{U}_{H}^{c*} - \mu^{Q*}m_{4m}^{d}\tilde{Q}_{H}^{t*}\tilde{D}_{m}^{c} + \mu^{Q*}m_{4m}^{u}\tilde{Q}_{H}^{b*}\tilde{U}_{m}^{c} + \mu^{U*}m_{H}^{u}\tilde{Q}_{H}^{b}\tilde{U}_{4}^{c*} + \text{H.c.}] \right],$$

$$(31)$$

where $m^{l,d,u}$ are matrices with elements defined before.

Together with $B\mu$ terms given in Eq. (8), full masssquared matrices of sfermions are obtained. In the Appendix, the charged slepton, up squark, and down squark mass-squared matrices will be given explicitly.

III. PHENOMENOLOGICAL CONSTRAINTS

The direct experimental search of extra generation particles at LEP requires that they should be heavier than 100 GeV, and direct search of extra generation quarks at Tevatron requires they are heavier than 270 GeV [14]. This result can be simply satisfied if μ^X 's are larger than 100 GeV or 270 GeV. Note that we do not have extra neutrinos which, in this model, consist of Higgsinos.

The electroweak precision measurement generally has constraints on extra matters [8]. Current constraints are [14]

$$S = -0.10 \pm 0.10, \qquad T = -0.08 \pm 0.11,$$

$$U = 0.15 \pm 0.11. \qquad (32)$$

For one extra chiral generation, oblique parameters S, T, Ustill allow the existence of the fourth generation [8] provided that there is certain mass splitting in extra $SU(2)_L$ doublets. In our case, the vectorlike generation contributes to the parameters in the way of $1/\mu^{X2}$ as expected from the decoupling theorem [13]. Typically,

$$S \simeq T \simeq \left(\frac{m_t}{\mu^X}\right)^2.$$
 (33)

The effect of the extra generation can be small enough $\leq (m_t/\mu^X)^2 \simeq (1-10)\%$ if we take $\mu^X \simeq 500$ GeV-1 TeV.

Important constraints come from the unitarity of the 3 × 3 CKM quark mixing matrix of three chiral generations [14]. This unitarity is consistent with current data within experimental errors. In this model, extra generations mix with ordinary three chiral generations, which necessarily break the unitarity of the CKM mixing matrix. As we have observed following Eqs. (20) and (25), unitarity violation is about $(m_{i4}^{d(u)}/\mu^{D(U)})^2$. This μ^X dependence is generally expected in the case of extra vectorlike generations.

Hierarchical or small mixing masses $m_{i4}^{d(u)}$ can easily make the CKM matrix approximately unitary within errors. For an example, $(m_{14}^{d(u)}/\mu^X)^2 \le 10^{-3}$. Assuming only the third generation mixes with extra generations, the constraint is still loose, $(m_{34}^{d(u)}/\mu^{D(U)})^2 \le 0.39$. The quantity $m_{34}^{d(u)}$ is at most about m_t . This gives that the parameter $\mu^{D,U} \ge$ 280 GeV.

From Eqs. (22), (23), (27), and (28), it can be seen that there are new phases in fermion mixing matrices. However, these new matrix elements are of order of $(m_t/\mu^X)^2$ at most. So new *CP* violation effects are generally suppressed.

One of the characteristic properties of the superpotential in this model is that there are many μ parameters. In the following analysis, we prefer to take all the μ parameters approximately equal. They are expected having common origin. On the other hand, by taking $|\mu| \ll |\mu^X|$, such as $|\mu| = 100 \text{ GeV}$ and $|\mu^X| = 500 \text{ GeV}$, this model will have MSSM as its low energy effective theory. In order to make this model distinct, considering above discussed constraints, we will take $|\mu|$ close to $|\mu^X|$, and

$$|\mu^X| \sim 500 \text{ GeV.}$$
 (34)

We bear in mind that for correct EWSB, it maybe necessary to require that $|\mu|$ is a kind of smaller than $|\mu^e|$, and $|\mu|$ cannot be too large. Of course, values of soft masses and $B\mu$'s are also important to EWSB. They can affect the choice of values of μ parameters.

In the following, we give a numerical illustration. μ parameters can have the following values:

$$\mu = 300 \text{ GeV}, \qquad \mu^e = 400 \text{ GeV}, \mu^{Q,U,D} = 500 \text{ GeV}.$$
(35)

Correct EWSB happens if we take

$$B\mu = -(260 \text{ GeV})^2, \qquad M^2 = (219 \text{ GeV})^2,$$

 $M_h^2 = -(243 \text{ GeV})^2, \qquad B^X \mu^X = -(200 \text{ GeV})^2, \quad (36)$
 $M_X^2 = M_{XH}^2 = (200 \text{ GeV})^2.$

Note that we have taken M_h^2 negative. This is expected due to the large top quark Yukawa coupling [2]. It is straightforward to see that this set of parameters results in consistent EWSB, and it fixes that $\tan\beta = 2$ and results in the Higgs spectrum

$$m_h^2 \simeq (124 \text{ GeV})^2, \qquad m_{H^0}^2 \simeq (420 \text{ GeV})^2,$$

 $m_A^2 \simeq (413 \text{ GeV})^2, \qquad m_{H^\pm}^2 \simeq (424 \text{ GeV})^2,$ (37)

where the quantum correction to m_h^2 has been included.

IV. LHC PHENOMENOLOGY

This model can be tested at LHC. In addition to the (super) particle content of MSSM, it predicts following vectorlike particles: one lepton singlet (E_4^c, E_H^c) , one quark doublet (Q_4, Q_H) , one up-type quark singlet (U_4^c, U_H^c) and one down-type quark singlet (D_4^c, D_H^c) , but there is no extra doublet leptons, which are already identified as the Higgs doublets.

Let us look at fermions. Because the effect of EWSB is much smaller than μ parameters, these new Weyl fermions form several Dirac fermions with masses $|\mu^X| \sim$ 500 GeV,

$$\Psi_{e} \equiv \begin{pmatrix} e_{H}^{c} \\ \bar{e}_{4}^{c} \end{pmatrix}, \qquad \Psi_{Q} \equiv \begin{pmatrix} q_{4} \\ \bar{q}_{H} \end{pmatrix},
\Psi_{u} \equiv \begin{pmatrix} u_{4}^{c} \\ u_{H} \end{pmatrix}, \qquad \Psi_{d} \equiv \begin{pmatrix} d_{4}^{c} \\ d_{H} \end{pmatrix}.$$
(38)

Note that in this case, mass splitting in the $SU(2)_L$ doublet q_4 or q_H is also negligible. Considering gauge kinetic terms, the Lagrangian describing these pseudo-Dirac fermions can be written as

$$\mathcal{L} \supset \sum_{X} (\bar{\Psi}_{X} \gamma_{\mu} D^{\mu} \Psi_{X} + \mu^{X} \bar{\Psi}_{X} \Psi_{X}), \qquad (39)$$

where the covariant derivative is self-evident.

Decay signals of these new particles can be easily identified. From trilinear Yukawa interactions given in Eq. (4), it is seen that they decay into SM first three generation matters. Ψ_e can decay into e_i and a neutral Higgs, the decay rate is

$$\Gamma(\Psi_e \to e_i h^0) \simeq \frac{1}{16\pi} |y_i^E|^2 |\mu^e| \left(1 - \frac{m_h^2}{|\mu^e|^2}\right)^2.$$
(40)

Alternative to the Higgs, scalar neutrinos can be also the decay product, which is expected at least heavier than the lighter neutral Higgs. Similarly, new quarks Ψ_u and Ψ_d decay into ordinary quarks and the Higgs,

$$\Psi_u \to u(c, t)h^0, \qquad \Psi_d \to d(s, b)h^0$$
(41)

with decay rates

$$\Gamma(\Psi_{u(d)} \to u_i(d_i)h^0) \simeq \frac{1}{16\pi} |y_i^{4(D)}|^2 |\mu^{U(D)}| \left(1 - \frac{m_h^2}{|\mu^{U(D)}|^2}\right)^2.$$
(42)

And decays of new quarks q_4 and q_H have following results:

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$$\Gamma(\Psi_q^{d(u)} \to d_i^c(u_i^c)h^0) \simeq \frac{1}{16\pi} |y_i^{Q'(Q)}|^2 |\mu^Q| \left(1 - \frac{m_h^2}{|\mu^Q|^2}\right)^2.$$
(43)

Taking relevant Yukawa coefficients y_i 's $\sim 10^{-1} - 10^{-2}$, decay rates in Eqs. (40)–(43) are $\Gamma \sim 5-500$ MeV.

Taking EWSB into consideration, Ψ_X mixes with SM fermions. The 5 × 5 generalized CKM matrix is derived from Eqs. (22) and (27),

$$V \equiv U^{u^{\dagger}} U^{d} \simeq \begin{pmatrix} 1 & 0 & -\frac{m_{44}^{d}}{\mu^{D}} - \frac{m_{34}^{u}}{\mu^{U}} \\ 0 & 1 & \frac{|m_{34}^{d}|^{2}}{\mu^{D}m_{44}^{d*}} + \frac{\mu^{U^{*}}m_{44}^{u} - m_{H}^{u^{*}}\mu^{D}}{|\mu^{Q}|^{2} - |\mu^{U}|^{2} - |m_{H}^{u}|^{2}} \\ \frac{m_{34}^{u^{*}}}{\mu^{D^{*}}} + \frac{m_{34}^{d^{*}}}{\mu^{D^{*}}} & \frac{|m_{H}^{u}|^{2} + |m_{44}^{u}|^{2}}{\mu^{Q}m_{H}^{u^{*}} - \mu^{U^{*}}m_{44}^{u}} & 1 \end{pmatrix}.$$
(44)

Note that $\mathcal{O}(m/\mu^X)^2$ terms have been omitted. We see that decays $\Psi_d \to \bar{t}W^+$ and $\Psi_u \to \bar{b}W^-$ occur via the SU(2)_L gauge interaction at the level of $\mathcal{O}(m/\mu^X)$,

$$\Gamma(\Psi_{d} \to \bar{t}W^{+}) \simeq \frac{G_{F}m_{W}^{2}|\mu^{D}||V_{35}|^{2}}{8\sqrt{2}\pi} \left\{ 1 + \left(\frac{m_{W}}{\mu^{D}}\right)^{4} + \left(\frac{m_{t}}{\mu^{D}}\right)^{4} - 2\left[\left(\frac{m_{W}}{\mu^{D}}\right)^{2} + \left(\frac{m_{W}}{\mu^{D}}\right)^{2}\left(\frac{m_{t}}{\mu^{D}}\right)^{2} + \left(\frac{m_{t}}{\mu^{D}}\right)^{2}\right] \right\}^{1/2} \\
\times \left\{ \left[1 - \left(\frac{m_{t}}{\mu^{D}}\right)^{2}\right]^{2} + \left(\frac{m_{W}}{\mu^{D}}\right)^{2} \left[1 + \left(\frac{m_{t}}{\mu^{D}}\right)^{2}\right] - 2\left(\frac{m_{W}}{\mu^{D}}\right)^{4} \right\}, \tag{45}$$

$$\Gamma(\Psi_{u} \to \bar{b}W^{-}) \simeq \frac{G_{F}m_{W}^{2}|\mu^{U}||V_{53}|^{2}}{8\sqrt{2}\pi} \left[1 - \left(\frac{m_{W}}{\mu^{U}}\right)^{2}\right]^{2} \left[1 + 2\left(\frac{m_{W}}{\mu^{U}}\right)^{2} \right], \tag{45}$$

where the phase space factors were given in Ref. [15]. Taking $m/\mu^X \sim 1/3$, these Γ 's are about 1 GeV.

All above decays are fast enough that they occur inside detectors. With the invariant mass method, decayed new fermions will be reconstructed.

These new quarks can be produced at LHC via gluon fusion processes $gg \rightarrow Q_4 Q_H$, $U_4^c U_H^c$, $D_4^c D_H^c$. The production mechanism is essentially the same as that of the top quark [16] with an estimated cross section ~ hundreds fbby taking $\mu^X \sim 500$ GeV and $\sqrt{s} = 14$ TeV.

For the new lepton, the Drell-Yan process is the main production mechanism, $pp \rightarrow \gamma Z \rightarrow e^c e^c_H$. The cross section is estimated to be few fb, which means a few tens events in one year [17]. Considering the detector efficiency, new lepton observation maybe challenging at LHC. However, once they are produced, their decay signals are easy to be identified.

V. SUMMARY AND DISCUSSION

Within the framework of SUSY, we have extended the matter content in a way that each Higgs doublets is in a full generation. Namely, in addition to ordinary three generations, there is an extra vectorlike generation, and it is the extra slepton $SU(2)_L$ doublets that are taken as two Higgs doublets. *R*-parity violating interactions contain ordinary Yukawa interactions. SUSY and gauge symmetry breaking have been analyzed. Fermion and boson spectra have been

calculated. Phenomenological constraints and relevant LHC physics have been discussed.

Finally, we discuss some aspects of this model. We are motivated by trying to naturally understand the Higgs. Within SUSY, Higgs can be considered as certain slepton doublets. Thus, they are nothing special compared to three ordinary generations, the anomaly cancels within each generation. It might be amusing to note that the first generation composes the ordinary matter, the second generation provides fermion mixing, the third gives *CP* violation, and the fourth and fifth (the vector one) give out EWSB because they contain Higgs doublets.

Like in traditional *R*-parity violating models, baryon number conservation is required. While the requirement of any first principle global symmetry is a drawback compared to SM, it is possible to consider baryon number conservation as a result of the so-called discrete gauge symmetry [18].

R-parity violation implies that neutralinos cannot be DM. Of course, the TeV particle theory does not necessarily provide DM, there are many alternative scenarios, like the axion, the sterile neutrino, or even the modified gravity. Nevertheless, the thermally produced weakly interacting massive particle (WIMP) is one of the most attractive. To this model, it is still possible to introduce additional matter playing the role of WIMP. We note that a recent DM proposal by Arkani-Hamed *et al.* [19] can be directly combined with our model. Their proposal is an

effort to explain all recent DM experiments [20], WIMP DM lies in a new sector.

Neutrino masses can be generated. This model has lepton number violation, which contributes neutrino masses [21]. Although the original superpotential (1) is simple, its expression in terms of ordinary three light generations given in Eq. (4) is complicated. There are many new lepton number violating sources. All of them involve the vector-like extra generation, which is heavier than soft SUSY breaking masses. Therefore, except for the ordinary *R*-parity violating terms with couplings λ_{ijk} and λ'_{ijk} , the new lepton number violating terms are less stringent constrained at low energies. The full phenomenological analysis of lepton number violation is rather involved, and will be considered in a separate work. Furthermore, the seesaw mechanism can be introduced to get the fully realistic neutrino mass pattern.

It seems that we have lost GUT. In MSSM, running gauge coupling constants meet together at the energy $\sim 3 \times 10^{16}$ GeV. This is regarded as a result of GUT. By adding new matter, which is charged under the SM, gauge coupling unification would be lost generally. However, if the new matter composes complete representations of GUT, gauge coupling unification is still kept at least to the one-loop level [22]. Compared to MSSM, the new matter contents we have added in this model are $(E_4^c, Q_4,$ U_4^c , D_4^c) and $(E_H^c$, Q_H , U_H^c , D_H^c). They do not compose complete representations of GUT. Giving up GUT while keeping SUSY sounds bizarre. However, GUT relation of gauge coupling constants maybe finally restored after additional matter, that is DM, is included. This SUSY model has already introduced the new matter $\mathbf{5} \oplus \mathbf{\overline{5}}$ and $\mathbf{10} \oplus \mathbf{\overline{10}}$ in SU(5) representation. Gauge couplings still do not reach their Landau poles in the GUT energy scale [10,22].

We have ignored the mixing of first two chiral generations with the vector generation. Detailed consideration of such possibly small mixing may give interesting observable phenomena [12].

SUSY breaking and its mediation to our sector should be considered systematically. This is closely related to EWSB and LHC phenomenology.

All above discussed aspects deserve further and separate studies.

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APPENDIX: SCALAR MASS-SQUARED MATRICES

In writing sfermion mass matrices, for simplicity and without losing generality, we will omit the first two generations. Neglecting the mixing between (1, 2) generations and (3, 4) generations, the first two generation sfermion themselves are the same as those in MSSM. The charged slepton mass-squared matrix is \tilde{M}_{l}^{2} ,

$$\mathcal{L} \supset (\tilde{L}_{3}^{-*}, \tilde{E}_{3}^{c}, \tilde{E}_{4}^{c}, \tilde{E}_{H}^{c*}) \tilde{\mathcal{M}}_{l}^{2} \begin{pmatrix} \tilde{L}_{3}^{-} \\ \tilde{E}_{3}^{c*} \\ \tilde{E}_{4}^{c} \\ \tilde{E}_{H}^{c} \end{pmatrix},$$
(A1)

where $4 \times 4 \ \tilde{\mathcal{M}}_l^2$ is given by the following matrix elements:

$$\begin{split} & (\tilde{\mathcal{M}}_{l}^{2})_{11} = M^{2} + \left(\frac{m_{Z}^{2}}{2} - m_{W}^{2}\right) \cos 2\beta + m_{\tau}^{2} + |m_{34}^{l}|^{2}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{12} = (m_{0} - \mu \tan\beta)m_{\tau}^{*}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{13} = (m_{0} - \mu \tan\beta)m_{34}^{l*}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{21} = (m_{0} - \mu \tan\beta)m_{\tau}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{22} = M_{E}^{2} - (m_{Z}^{2} - m_{W}^{2})\cos 2\beta + m_{\tau}^{2} + |m_{43}^{l}|^{2}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{22} = m_{\tau}m_{34}^{l*} + m_{43}m_{44}^{l*}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{24} = 0, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{31} = (m_{0} - \mu \tan\beta)m_{34}^{l}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{32} = m_{\tau}^{*}m_{34}^{l} + m_{43}^{l*}m_{44}^{l}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{33} = |\mu^{e}|^{2} + M_{E}^{2} - (m_{Z}^{2} - m_{W}^{2})\cos 2\beta \\ & + |m_{44}^{l}|^{2} + |m_{34}^{l}|^{2}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{34} = B^{e}\mu^{e}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{41} = \mu^{e^{*}}m_{34}^{l}, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{42} = 0, \\ & (\tilde{\mathcal{M}}_{l}^{2})_{43} = B^{e^{*}}\mu^{e^{*}}, \end{split}$$

$$(\tilde{\mathcal{M}}_l^2)_{44} = |\mu^e|^2 + M_{EH}^2 + (m_Z^2 - m_W^2)\cos 2\beta.$$
(A2)

The down quark mass-squared matrix is $\tilde{\mathcal{M}}_d^2$,

$$\mathcal{L} \supset (\tilde{Q}_{3}^{b*}, \tilde{D}_{3}^{c}, \tilde{D}_{4}^{c}, \tilde{D}_{H}^{c*}, \tilde{Q}_{4}^{b*}, \tilde{Q}_{H}^{t}) \tilde{\mathcal{M}}_{d}^{2} \begin{pmatrix} \tilde{Q}_{3}^{b} \\ \tilde{D}_{3}^{c*} \\ \tilde{D}_{4}^{c*} \\ \tilde{D}_{H}^{c} \\ \tilde{Q}_{4}^{b} \\ \tilde{Q}_{H}^{t*} \end{pmatrix}, \quad (A3)$$

where $\tilde{\mathcal{M}}_d^2$ is

$$\begin{split} (\tilde{\mathcal{M}}_{d}^{2})_{11} &= M_{Q}^{2} - \frac{m_{Z}^{2} + 2m_{W}^{2}}{6} \cos 2\beta + m_{b}^{2} + |m_{34}^{d}|^{2}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{12} = (m_{0} - \mu \tan\beta)m_{b}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{13} = (m_{0} - \mu \tan\beta)m_{34}^{*}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{14} &= \mu^{D}m_{34}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{15} = m_{b}^{*}m_{43}^{*} + m_{34}^{*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{16} = 0, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{21} = (m_{0} - \mu \tan\beta)m_{b}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{22} &= M_{D}^{2} - \frac{m_{Z}^{2} - m_{W}^{2}}{3} \cos 2\beta + m_{b}^{2} + |m_{43}^{4}|^{2}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{23} = m_{b}m_{34}^{*} + m_{43}^{*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{24} = 0, \\ (\tilde{\mathcal{M}}_{d}^{2})_{25} &= (m_{0} - \mu \tan\beta)m_{43}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{26} = \mu^{Q*}m_{43}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{31} = (m_{0} - \mu \tan\beta)m_{34}^{*}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{32} &= m_{b}^{*}m_{34}^{*} + m_{43}^{*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{33} = |\mu^{D}|^{2} + M_{D}^{2} - \frac{m_{Z}^{2} - m_{W}^{2}}{3} \cos 2\beta + |m_{34}^{*}|^{2} + |m_{44}^{*}|^{2}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{34} = B^{D}\mu^{D}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{35} &= (m_{0} - \mu \tan\beta)m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{36} = \mu^{Q*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{41} = \mu^{D*}m_{34}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{42} = 0, \\ (\tilde{\mathcal{M}}_{d}^{2})_{35} &= (m_{0} - \mu \tan\beta)m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{36} = \mu^{Q*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{41} = \mu^{D*}m_{34}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{42} = 0, \\ (\tilde{\mathcal{M}}_{d}^{2})_{43} &= B^{D*}\mu^{D*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{44} = |\mu^{D}|^{2} + M_{DH}^{2} + \frac{m_{Z}^{2} - m_{W}^{2}}{3} \cos 2\beta, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{45} = \mu^{D*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{46} = 0, \\ (\tilde{\mathcal{M}}_{d}^{2})_{51} &= m_{b}m_{43}^{*} + m_{34}^{*}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{52} = (m_{0} - \mu \tan\beta)m_{45}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{53} = (m_{0} - \mu \tan\beta)m_{44}^{*}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{54} &= \mu^{D}m_{44}^{*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{55} = |\mu^{Q}|^{2} + M_{Q}^{2} - \frac{m_{Z}^{2} + 2m_{W}^{2}}{6} \cos 2\beta + |m_{44}^{4}|^{2} + |m_{43}^{4}|^{2}, \\ (\tilde{\mathcal{M}}_{d}^{2})_{56} &= -B^{Q*}\mu^{Q*}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{65} = -B^{Q}\mu^{Q}, \qquad (\tilde{\mathcal{M}}_{d}^{2})_{66} = |\mu^{Q}|^{2} + M_{QH}^{2} + \frac{m_{Z}^{2} +$$

The up quark mass-squared matrix is $\tilde{\mathcal{M}}_{u}^{2}$,

$$\mathcal{L} \supset (\tilde{Q}_{3}^{t*}, \tilde{U}_{3}^{c}, \tilde{U}_{4}^{c}, \tilde{U}_{H}^{c*}, \tilde{Q}_{4}^{t*}, \tilde{Q}_{H}^{b}) \tilde{\mathcal{M}}_{u}^{2} \begin{pmatrix} \tilde{Q}_{3}^{t} \\ \tilde{U}_{3}^{c*} \\ \tilde{U}_{4}^{c*} \\ \tilde{U}_{4}^{t} \\ \tilde{Q}_{H}^{t} \end{pmatrix},$$
(A5)

where
$$\tilde{\mathcal{M}}_{u}^{2}$$
 is

$$(\tilde{\mathcal{M}}_{u}^{2})_{11} = M_{Q}^{2} + \frac{4m_{W}^{2} - m_{Z}^{2}}{6} \cos 2\beta + m_{t}^{2} + |m_{34}^{u}|^{2}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{12} = (m_{0} - \mu \cot \beta)m_{t}^{*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{13} = (m_{0} - \mu \cot \beta)m_{t}^{u*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{13} = (m_{0} - \mu \cot \beta)m_{t}^{u*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{14} = \mu^{U}m_{34}^{u*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{15} = m_{t}^{*}m_{43}^{u} + m_{34}^{u}m_{44}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{16} = 0, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{21} = (m_{0} - \mu \cot \beta)m_{t}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{22} = M_{U}^{2} + \frac{2}{3}(m_{Z}^{2} - m_{W}^{2})\cos 2\beta + m_{t}^{2} + |m_{43}^{u}|^{2}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{23} = m_{t}m_{34}^{u*} + m_{43}^{u}m_{44}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{25} = (m_{0} - \mu \cot \beta)m_{43}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{25} = (m_{0} - \mu \cot \beta)m_{43}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{26} = \mu^{Q*}m_{43}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{31} = (m_{0} - \mu \cot \beta)m_{34}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{32} = m_{t}^{*}m_{34}^{u} + m_{43}^{u}m_{44}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{36} = \mu^{Q*}m_{43}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{31} = (m_{0} - \mu \cot \beta)m_{34}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{32} = m_{t}^{*}m_{34}^{u} + m_{43}^{u}m_{44}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{33} = |\mu^{U}|^{2} + M_{U}^{2} + \frac{2}{3}(m_{Z}^{2} - m_{W}^{2})\cos 2\beta + |m_{44}^{u}|^{2}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{41} = \mu^{U*}m_{34}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{34} = B^{U}\mu^{U}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{35} = (m_{0} - \mu \cot \beta)m_{44}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{36} = \mu^{Q*}m_{44}^{u} + \mu^{U}m_{47}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{41} = \mu^{U*}m_{34}^{u}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{42} = 0, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{43} = B^{U*}\mu^{U*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{44} = |\mu^{U}|^{2} + M_{UH}^{2} - \frac{2}{3}(m_{Z}^{2} - m_{W}^{2})\cos 2\beta + |m_{44}^{u}|^{2}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{45} = \mu^{U*}m_{44}^{u} + \mu^{Q}m_{44}^{u*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{55} = |\mu^{Q}|^{2} + M_{Q}^{2} + \frac{4m_{W}^{2} - m_{Z}^{2}}{6}\cos 2\beta + |m_{44}^{u}|^{2} + |m_{43}^{u}|^{2}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{56} = B^{Q*}\mu^{Q*}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{65} = B^{Q}\mu^{Q}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{65} = B^{Q}\mu^{Q}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{65} = B^{Q}\mu^{Q}, \qquad (\tilde{\mathcal{M}}_{u}^{2})_{65} = B^{Q}\mu^{Q}, \qquad (\tilde{\mathcal{M}}_$$

As we have expected, taking the 3–4 mixing mass to be small $m_{34}^{l(u,d)} \rightarrow 0$, the third generation also decouples from the two extra generations.

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