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## Consistency of New Meson-Nucleon Elastic Scattering Data with a Previously Conjectured Universal Curve\*

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We show that important new large- $t \pi \bar{p}$  data at  $p_L = 13.8$  and 22.6 GeV/c are in good agreement with a universal curve suggested last year.

Recently a detailed experimental study<sup>1</sup> of elastic pion-proton scattering was made at large energies  $(p_L = 13.8 \text{ and } 22.6 \text{ GeV}/c)$  over a substantial part of the forward scattering region  $[|t| \leq 5 (\text{GeV}/c)^2]$ in order "to determine if the shapes and magnitudes of the cross sections are approaching limiting values as the momentum increases."<sup>1</sup> In this note we will show that these new data are in close agreement with an apparently universal curve for meson-nucleon scattering which was found last year in a study<sup>2</sup> of the high-energy  $(p_L \geq 5 \text{ GeV}/c)$ elastic data then available. At that time it was shown that existing forward and backward data fell on a simple curve if cross sections normalized to unity at t=0,

$$f = \frac{d\sigma}{dt} / \left(\frac{d\sigma}{dt}\right)_{t=0} , \qquad (1)$$

were plotted versus the dimensionless variable

$$\tau = -bt(s+t)/s, \qquad (2)$$

where b(s) is the slope of the forward peak  $[|t| \le 0.5 (\text{GeV}/c)^2]$  appropriate to the reaction and energy. The angular regions which fell on the universal curve were defined by  $|t| \le 3 (\text{GeV}/c)^2$  in the forward region and  $|u| \le 1 (\text{GeV}/c)^2$  in the backward region. The quadratic character of the variable  $\tau$  reflects the backward peak onto the forward peak. The universal character of the curve was expected to become even more evident at higher energies. If this curve is valid, a large body of existing data has been reduced to a determination of two quantities of obvious geometrical (optical) significance, b and  $\sigma_t$  (which fixes  $d\sigma/dt|_{t=0}$  via the optical theorem, assuming the real part of the forward amplitude is small).

The recent high-energy forward-region data of Cornillon  $et al.^1$  give strong additional support to

the universality of the curve. Figure 1 shows a plot of their  $\pi^- p$  data at  $p_L = 13.8$  and 22.6 GeV/c in the manner described above compared with the conjectured curve of Fig. 1 in Ref. 2. The agreement for values of  $|t| \leq 3$  (GeV/c)<sup>2</sup> over six decades is striking. The points not on the curve at large  $\tau$  are beyond the boundary of the curve's validity at  $t \cong 3$  (GeV/c)<sup>2</sup>.

In order to plot the data in Fig. 1 we used<sup>3</sup>  $\sigma_T$  = 26 mb at  $p_L$  = 13.8 GeV/c and  $\sigma_T$  = 25 mb at  $p_L$  = 22.6 GeV/c. In both cases the slope parameter was taken to be 7.5 (GeV/c)<sup>-2</sup>, consistent with the data.

The disappearance of the dip at  $t \approx -0.8$   $(\text{GeV}/c)^2$ and the appearance of a marked change in slope are in good agreement with the piecewise exponential character of the universal curve which has a break at  $\tau \approx 5$ .

In addition Cornillon *et al.* noted that the data between 1 < -t < 3 (GeV/c)<sup>2</sup> cannot be simply fitted with a Regge parametrization. The conjectured curve of Ref. 2 provides a simple parametrization of meson-nucleon data and is apparently applicable where naive Regge theory is not. The authors feel that the data are displaying a geometrical character which (considering that the regularity is only observed in the forward and backward regions) may be understood within the framework of an optical model.

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FIG. 1. A plot of new  $\pi^{-}p$  data taken from Ref. 1. The solid line is a reproduction of the previously conjectured universal curve shown in Fig. 1 of Ref. 2.

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