Study of Inclusive γ and π^0 Production in 12.4-GeV/c pp Interactions

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From an exposure of the Argonne National Laboratory 12-foot bubble chamber to a beam of 12.4-GeV/c protons we have obtained a 3649-event sample of the reaction $pp \rightarrow \gamma + anything$, where we observe photon conversions into e^+e^- pairs in the liquid hydrogen. We find that the invariant cross section for this reaction does not separate in its x and P_{\perp} dependence at our energy. By setting upper bounds on the cross sections for inclusive η and Σ^0 production, we show that π^0 decay is the dominant source of photons and therefore measure the cross section for inclusive π^0 production to be $\sigma(\pi^0) = (31.5 \pm 2.6)$ mb. Comparison with the inclusive π^+ and π^- cross sections at 12.0 GeV/c shows that the relation $2\sigma(\pi^0) = \sigma(\pi^+) + \sigma(\pi^-)$ is well satisfied. We confirm earlier indications that the average number of π^0 's per inelastic pp interaction is approximately independent of the number of associated charged particles produced.

The description of pion production in pp interactions requires, in general, three independent isotopic spin amplitudes. Thus π^0 production cannot be derived from π^+ and π^- data in a model-independent way. We report here an experiment which measures π^0 production by means of the inclusive photon reaction, where the dominant source of photons is from the decay of π^{0} 's. These results were obtained from the first exposure of the Argonne National Laboratory 12-foot bubble chamber,¹ to a 12.4-GeV/c proton beam extracted from the Zero-Gradient Synchrotron (ZGS).

We have analyzed the V^0 topology events in which a neutral particle converts or decays into two charged particles in the liquid hydrogen. The film was double-scanned for all V^{0} events which might be associated with a beam proton interaction. The two charged tracks from the V^{0} 's, and the vertices of all beam interactions to which they might point, were then measured on the Argonne POLLY III CRT measuring machine.² The primary interaction tracks were not measured. After remeasurements were completed, all events reconstructed by the geometry program TVGP were processed through the kinematics routine SQUAW, in which threeconstraint pointing tests were made. After applying appropriate selections,³ we find 3649 threeconstraint e^+e^- pairs. The small number (5% of all γ 's) of ambiguities between pair production and strange-particle decays were resolved on a statistical basis.4

The initial weight for each γ event was the inverse of the probability that it converts within the chosen fiducial volume, using the momentum-dependent pair-production cross section as given by quantum electrodynamics⁵ and requiring a minimum photon length of 12 cm. The average weight so obtained is 11.3 and the average photon detection efficiency calculated from this weight only is 10.5%.

The double scan efficiency for finding and correctly associating the γ events was ~96%, but is somewhat lower (~92%) for large ($\geq 45^{\circ}$) laboratory angles. Since the laboratory and center-ofmass production angles are one-to-one related, independent of the photon momentum, we have corrected the data for scan efficiency in six equal bins of $\cos\theta_{\star}^{*}$.

Due to the falloff of the pair-production cross section at small γ momentum,⁵ special attention has to be given to low-energy γ 's. The correction due to this effect is based on the forward-backward symmetry in the pp center of mass. We vary the lab momentum P_{γ}^{lab} and compare the weighted numbers of events in the forward and backward centerof-mass hemispheres, after eliminating those which fall under the P_{γ}^{lab} curve (region A of Fig. 1) as well as those which fall under its reflection into the forward hemisphere (region B of Fig. 1). For $P_{\gamma}^{\text{lab}} \ge 90 \text{ MeV}/c$, we find the two hemispheres to be equally populated with weighted events. We therefore eliminate all events with $P_{\gamma}^{\text{lab}} \le 90 \text{ MeV}/c$

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FIG. 1. $P_{\gamma}^{\text{lab}} \leq 90 \text{ MeV}/c$ region and its reflection in the Peyrou plot.

and $P_L^* \leq 0.0$ (region A). To correct for these events, we double the weights for all events which lie in the reflection of A, namely region B. We then have a fully corrected sample of events in the folded distributions $|P_L^*|$, |x|, etc., except for the small region (C in Fig. 1) bounded by $P_{\perp} \leqslant 35$ MeV/c and $0 \le P_L^* \le 17 MeV/c$. Those events found in region C have been included in the distributions, with doubled weights. Since region C is a small fraction of the populated phase space (35 events), we have not attempted to make any further corrections for the loss of very-low-momentum photons. After folding in corrections due to scanning efficiency, unbiased reconstruction failures, the cut on probability of $\chi^2,\,$ and the requirement that $P_{\gamma}^{\text{lab}} \ge 90 \text{ MeV}/c$, the over-all average weight factor is 18.7, and the corresponding average total detection efficiency is 6.9%.

The cross-section normalization was obtained from a count of the beam tracks entering the fiducial volume and corresponds to 1.05 events/ μ b. All cross sections in this paper include an 8% systematic error due to cross section normalization (~ 5%), the redistribution of track reconstruction failures (~ 4%), and scanning efficiency (~ 5%). These errors have been quadratically added to the statistical errors.

We discuss our results first in terms of the invariant cross section

$$F(x, P_{\perp}^2, s) = \frac{E^*}{\pi P_{\max}^*} \frac{d^2\sigma}{dx \, dP_{\perp}^2} .$$

We denote by $F_1(x)$ and $F_2(P_{\perp}^2)$ the integrals of $F(x, P_{\perp}^{2})$ over P_{\perp}^{2} and x, respectively.⁶ In Fig. 2 we show $F_1(x)$ and $F_2(P_{\perp}^2)$. Our results on $F_1(x)$ and $2P_{\perp}F_{2}(P_{\perp}^{2})$ (not shown) may be compared with those of Neuhofer et al.," who have studied the reaction $pp \rightarrow \gamma$ + anything at the CERN Intersecting Storage Rings (ISR) at stationary-target-equivalent momenta of 500, 1100, and 1500 GeV/c. They found that the invariant cross section could be represented by the formula $F(x, P_{\perp}^2) \propto F_1(x)F_2(P_{\perp}^2)$, with the x and P_{\perp} dependences $F_1(x) \sim e^{-x/0.083}$ and $P_{\perp}F_2(P_{\perp}^2) \sim \exp(-P_{\perp}/0.162 \,\text{GeV}/c)$ over the ranges $0 \le x \le 0.15$ and $0.1 \le P_{\perp} \le 0.6$ GeV/c, respectively. In our experiment, we obtain $F_1(x) \sim \exp[-|x|/$ (0.126 ± 0.013) for $0 \le |x| \le 0.6$ as shown in Fig. 2, and $P_{\perp}F_2(P_{\perp}^2) \sim \exp[-P_{\perp}/(0.196 \pm 0.020) \, \text{GeV}/c]$ for $0.15 \leq P_{\perp} \leq 1.15 \, \text{GeV}/c$. These slopes are similar to those from the ISR, even though the incident beam momenta differ by two orders of magnitude and the latter data are restricted to small x and P_{\perp} ranges. That the similarities are illusory is illustrated in Fig. 3, where we test separation



FIG. 2. (a) $d\sigma/d|x|$ below, and its invariant counterpart $F_1(|x|)$ above (see text). (b) $d\sigma/dP_1^2$ and $F_2(P_1^2)$.



FIG. 3. (a) $\langle P_{\perp} \rangle$ and $\langle E^* P_{\perp} \rangle / \langle E^* \rangle$ as a function of $|P_L^*|$ (see text).

of variables at our energy by plotting

$$\langle P_{\perp} \rangle = \int \frac{P_{\perp} d^2 \sigma}{d |x| dP_{\perp}^2} dP_{\perp}^2 / \int \frac{d^2 \sigma}{d |x| dP_{\perp}^2} dP_{\perp}^2$$

and

$$\frac{\langle E^*P_{\perp} \rangle}{\langle E^* \rangle} = \frac{\int E^*P_{\perp} \frac{d^2\sigma}{d|x|dP_{\perp}^2} dP_{\perp}^2}{\int E^* \frac{d^2\sigma}{d|x|dP_{\perp}^2} dP_{\perp}^2}$$

as a function of $|P_L^*|$. It is clear that there are correlations between $|P_L^*|$ and $\langle P_\perp \rangle$ in both distributions. This indicates that $F(x, P_\perp^{-2})$ for γ production at 12.4 GeV/c does not separate in its x and P_\perp dependences.

The observed 3649 events of the reaction $pp \rightarrow \gamma$ + anything correspond to an inclusive γ cross section of (63.0±5.1) mb. The most plausible sources of photons other than from π^{0} 's are η and Σ^{0} decays. For the events in which we observe two or more γ 's, or a Λ and a γ associated with the same pp interaction, we form the $\gamma\gamma$ or $\Lambda\gamma$ invariant mass distribution. The π^{0} signal in the $\gamma\gamma$ mass distribution yields a total inclusive π^{0} cross section which is consistent with the one quoted below. No η signal is observed in this distribution. A weak Σ^{0} enhancement is noted above a small background in the $\Lambda\gamma$ mass distributions. We find the following upper limits for the inclusive η and Σ^{0} cross sections at 12.4 GeV/*c*:

$$pp \rightarrow \eta + anything$$
,
 2γ
 $\sigma \leq 0.5 \text{ mb}$ (95% confidence level)

and

$$pp - \Sigma^0$$
 + anything ,
 $\Lambda \gamma$
 $\sigma \leq 1.3 \text{ mb}$ (95% confidence level).

The cross section for non- $\pi^0\gamma$ production is then less than 2.3 mb and has been neglected in obtaining the cross section for inclusive π^0 production:

$$pp \to \pi^0 + \text{anything}$$
, $\sigma(\pi^0) = (31.5 \pm 2.6)$ mb.

This cross section may be compared with the inclusive π^+ and π^- cross sections⁸ at 12.0 GeV/c: $\sigma(\pi^+) = (42.7 \pm 0.7)$ and $\sigma(\pi^-) = (21.1 \pm 0.4)$ mb. We observe that these cross sections are consistent with the relation

$$\sigma(\pi^{0}) = \frac{1}{2} \left[\sigma(\pi^{-}) + \sigma(\pi^{+}) \right] .$$

Although this equality does not follow from general symmetry arguments alone,⁹ it has been suggested by several authors^{9,10} as a consequence of I=0 *t*-channel exchange dominance in *pp* interactions,¹¹ and has also been derived¹² from a Mueller-Regge point of view by assuming isosinglet, C = +1 dominance in the appropriate Regge exchanges.

From the inclusive π^{0} cross section given above, which is, of course, equal to $\langle n_{\pi^{0}} \rangle \sigma_{in}$, and the total inelastic *pp* cross section of 29.1,¹³ we find

TABLE I. Topological γ and π^0 production cross sections and π^0 multiplicities.

| Topology | $\sigma_{\rm inel}$ (mb) | $\sigma_n(\gamma)$ (mb) | $\sigma_n (\pi^0)$ (mb) | $\langle n_{\pi 0} \rangle$ |
|----------|--------------------------|-------------------------|-------------------------|-----------------------------------|
| 2-prong | 10.4 ±0.6 | 25.5 ± 2.2 | 12.8 ± 1.1 | 1.23 ± 0.13 |
| 4-prong | 14.1 ± 0.6 | 28.8 ± 2.4 | 14.4 ± 1.2 | 1.02 ± 0.10 |
| 6-prong | 4.1 ± 0.3 | 8.6 ± 0.8 | 4.3 ± 0.4 | 1.05 ± 0.13 |
| 8-prong | 0.52 ± 0.10 | 0.94 ± 0.16 | 0.47 ± 0.08 | 0.91 ± 0.23 |
| 10-prong | 0.014 ± 0.010 | 0.01 ± 0.01 | 0.005 ± 0.005 | 0.36 ± 0.36 |
| Total | 29.1 ±2.3 | 63.9 ± 5.1 | 32.0 ±2.6 | $\textbf{1.10} \pm \textbf{0.13}$ |

that the average number of π^{0} 's produced per inelastic collision is $\langle n_{\pi^0} \rangle = 1.08 \pm 0.13$. By examining the dependence of $\langle n_{\pi^0} \rangle$ on the number of associated charged particles, *n*, we may study the correlation between neutral and charged pion production.¹⁴ The topological γ and π^0 production cross sections as well as π^0 multiplicities for this experiment are given in Table I.¹⁵

In Fig. 4 we present $\langle n_{\pi^0} \rangle$ as a function of *n* for this experiment and for experiments at 19 GeV/c,¹⁶ 205 GeV/c,¹⁷ and 303 GeV/c.¹⁸ At low energies, the number of charged particles produced in the final state has little influence on $\langle n_{\pi^0} \rangle$. This is in contrast to high-energy data,¹⁹ which indicate a definite correlation between charged and neutral pion production.

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FIG. 4. The average number of π^{0} 's per inelastic *pp* collision as a function of the number of charged particles produced.

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- ⁴With respect to the line of flight of the V^0 , the transversemomentum distribution of the negative particles from the V^0 peaks at 0.0, 0.1, and 0.2 GeV/*c* for γ , Λ , and K^0 , respectively.
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Proton Compton Scattering at 0.55-to-4.5-GeV Energy and 0.12-to-1.0-(GeV/c)² Momentum Transfer*

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Results are presented on the elastic scattering of photons by protons. The incident photon energy ranged from 0.55 GeV to 4.5 GeV, and the four-momentum transfer t ranged from 0.12 to 1.0 $(\text{GeV}/c)^2$. The data at large angles, $60^\circ < \theta^* < 115^\circ$, are characterized by a pronounced excitation of the $D_{13}(1518)$ resonance, a shoulder in the 1688-MeV mass region, and a precipitous drop thereafter in the cross section as a function of incident energy. The low-t data are characterized by a diffraction slope of 5 $(\text{GeV}/c)^{-2}$. The data are inconsistent with the predictions of the vector-dominance model if the latter is restricted to ρ^0 , ω , and ϕ vector mesons.

I. INTRODUCTION

We report a series of experiments on the elastic scattering of photons by protons conducted at the Cornell and Cambridge Electron Accelerators. The incident photon energy ranged from 0.55 to 4.5 GeV and the four-momentum transfer from 0.12 to 1.0 $(\text{GeV}/c)^2$. The experiments fall into two groups:

(i) "Large-angle" experiments with incident

photon energy <2.5 GeV and the center-of-mass angles in the range $60^{\circ} < \theta^* < 115^{\circ}$. The main motivation here was to search for resonance structure in the differential cross section.

The data exhibit a decrease of two orders of magnitude in the cross section in going from 0.5 to 2.5 GeV in the incident momentum. We were therefore limited by counting rate in extending these large-angle experiments to higher energies. A similar precipitous drop in cross section is