

# Axial-vector meson emitting weak nonleptonic decays of bottom baryons

Arvind Sharma\*

*Department of Physics, College of Engineering and Management, Kapurthala-144601, India*

R. C. Verma†

*Department of Physics, Punjabi University, Patiala-147002, India*

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We investigate the two-body weak nonleptonic decays of  $\Lambda_b^0$ ,  $\Xi_b^0$ , and  $\Xi_b^-$  into the octet baryons ( $J^P = 1/2^+$ ) and axial-vector mesons ( $J^P = 1^+$ ) employing the factorization scheme and obtain their branching ratios and asymmetry parameters.

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## I. INTRODUCTION

The nonleptonic weak decays of hadrons provide insight into the interplay of strong with weak interactions. Theoretically, most of the attention has been paid to understand the weak decays of the heavy flavor mesons. Although the experimental data [1–5] and theoretical predictions [6–13] on the nonleptonic decays of charm baryons have become available in the past decade, the data on bottom baryons has merely begun. Some attempts have already been made [14–16] to study the weak hadronic decays of bottom baryons emitting  $s$ -wave mesons mainly. Recently, the lifetime and masses of  $\Lambda_b^0$ ,  $\Xi_b^0$ , and  $\Xi_b^-$  have been measured. These bottom baryons, being heavy, can emit  $p$ -wave axial-vector mesons also [17]. One particular decay,  $\Lambda_b^0 \rightarrow \Lambda_c^+ a_1^-$ , has already been seen but its branching ratio has not yet been measured. In light of these developments, we here present theoretical estimates for weak nonleptonic decays of  $\Lambda_b^0$ ,  $\Xi_b^0$ , and  $\Xi_b^-$  into the octet baryons ( $J^P = 1/2^+$ ) and axial-vector mesons ( $J^P = 1^+$ ). Employing the factorization scheme in the nonrelativistic quark model (NRQM) and the heavy quark effective theory (HQET) considerations, we estimate the branching ratios and asymmetry parameters for  $\Lambda_b^0$ ,  $\Xi_b^0$ , and  $\Xi_b^-$  decays.

The layout of this paper is as follows. Section II describes the meson spectroscopy. Section III deals with basic methodology including the weak Hamiltonian, kinematics, form factors, and decay constants involved in the weak decays. In the last section, discussion of results and conclusions are given.

## II. MESON SPECTROSCOPY

Both types of axial-vector mesons,  $^3P_1 (J^{PC} = 1^{++})$  and  $^1P_1 (J^{PC} = 1^{+-})$ , behave well with respect to the quark model  $q\bar{q}$  assignments. Strange and charmed states made up of different flavors are given by a mixture of  $^3P_1$  and  $^1P_1$  states, since there is no quantum number forbidding such mixing. In contrast, diagonal  $^3P_1$  and  $^1P_1$  states have

opposite  $C$ -parity and cannot mix. Experimentally [1], the following nonstrange and uncharmed mesons have been observed:

- (i) for  $^3P_1$  multiplet, isovector  $a_1(1.260)$  and three isoscalars  $f_1(1.285)$ ,  $f'_1(1.510)$ , and  $\chi_{c1}(3.510)$ . Numbers given in the brackets indicate mass (in GeV) of the respective mesons.
- (ii) for  $^1P_1$  multiplet, isovector  $b_1(1.235)$  and three isoscalars  $h_1(1.170)$ ,  $h'_1(1.380)$ , and  $h_{c1}(3.525)$ . Spin and parity of the  $h_{c1}(3.525)$  remains to be confirmed.

In the present analysis, mixing of the isoscalar states of ( $1^{++}$ ) mesons is defined as

$$\begin{aligned} f_1(1.285) &= \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}) \cos\phi_A + (s\bar{s}) \sin\phi_A, \\ f'_1(1.510) &= \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}) \sin\phi_A - (s\bar{s}) \cos\phi_A. \end{aligned} \quad (1)$$

$$\chi_{c1}(3.510) = (c\bar{c}),$$

where

$$\phi_A = \theta(\text{ideal}) - \theta_A(\text{physical}).$$

Similarly, mixing of the two isoscalar mesons  $h_1(1.170)$  and  $h'_1(1.380)$  is defined as

$$\begin{aligned} h_1(1.170) &= \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}) \cos\phi_{A'} + (s\bar{s}) \sin\phi_{A'}, \\ h'_1(1.380) &= \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}) \sin\phi_{A'} - (s\bar{s}) \cos\phi_{A'}. \end{aligned} \quad (2)$$

$$h_{c1}(3.525) = (c\bar{c}).$$

Proximity of  $a_1(1.260)$  and  $f_1(1.285)$  and to lesser extent that of  $b_1(1.235)$  and  $h_1(1.170)$  indicates the ideal mixing for both  $1^{++}$  and  $1^{+-}$  nonets, i.e.,

$$\phi_A = \phi_{A'} = 0^\circ. \quad (3)$$

States involving a strange quark of  $A(J^{PC} = 1^{++})$  and  $B(J^{PC} = 1^{+-})$  mesons mix to generate the physical states in the following manner:

\*arvindkamalsharma@gmail.com  
†rcverma@gmail.com

$$\begin{aligned} K_1(1.270) &= K_{1A} \sin\theta_1 + K_{1B} \cos\theta_1, \\ \underline{K}_1(1.400) &= K_{1A} \cos\theta_1 - K_{1B} \sin\theta_1, \end{aligned} \quad (4)$$

where  $K_{1A}$  and  $K_{1B}$  denote the strange partners of  $a_1(1.260)$  and  $b_1(1.235)$ , respectively. The Particle Data Group [1] assumes that the mixing is maximal, i.e.,  $\theta_1 = 45^\circ$ , whereas  $\tau \rightarrow K_1(1.270)/K_1(1.400) + \nu_\tau$  data yields  $\theta_1 = \pm 37^\circ$  and  $\theta_1 = \pm 58^\circ$  [18]. However, the study of  $D \rightarrow K_1(1.270)\pi$ ,  $K_1(1.400)\pi$  decays rules out positive mixing-angle solutions. Therefore, both negative mixing-angle solutions are allowed by experiment as discussed in detail in Ref. [19]. But  $D \rightarrow K_1^-(1.400)\pi^+$  is very suppressed for  $\theta_1 = -37^\circ$  and favors the other solution  $\theta_1 = -58^\circ$  [19]. Hence, we take  $\theta_1 = -58^\circ$  in our analysis.

The mixing of charmed and strange charmed states is given by

$$\begin{aligned} D_1(2.422) &= D_{1A} \sin\theta_{D_1} + D_{1B} \cos\theta_{D_1}, \\ \underline{D}_1(2.427) &= D_{1A} \cos\theta_{D_1} - D_{1B} \sin\theta_{D_1}, \end{aligned} \quad (5)$$

and

$$\begin{aligned} D_{s1}(2.460) &= D_{s1A} \sin\theta_{D_{s1}} + D_{s1B} \cos\theta_{D_{s1}}, \\ \underline{D}_{s1}(2.536) &= D_{s1A} \cos\theta_{D_{s1}} - D_{s1B} \sin\theta_{D_{s1}}. \end{aligned} \quad (6)$$

However, in the heavy quark limit, the physical mass eigenstates with  $J^P = 1^+$  are  $P_1^{3/2}$  and  $P_1^{1/2}$  rather than  ${}^3P_1$  and  ${}^1P_1$  states as the heavy quark spin  $S_Q$  decouples from the other degrees of freedom so that  $S_Q$  and the total angular momentum of the light antiquark are separately good quantum numbers. Therefore, we can write

$$\begin{aligned} |P_1^{1/2}\rangle &= -\sqrt{\frac{1}{3}}|{}^1P_1\rangle + \sqrt{\frac{2}{3}}|{}^3P_1\rangle, \\ |P_1^{3/2}\rangle &= \sqrt{\frac{2}{3}}|{}^1P_1\rangle + \sqrt{\frac{1}{3}}|{}^3P_1\rangle. \end{aligned} \quad (7)$$

Hence, the states  $D_1(2.422)$  and  $D_{1-}(2.427)$  can be identified with  $P_1^{1/2}$  and  $P_1^{3/2}$ , respectively. However, beyond the heavy quark limit, there is a mixing between  $P_1^{1/2}$  and  $P_1^{3/2}$ , denoted by

$$\begin{aligned} D_1(2.422) &= D_1^{1/2} \cos\theta_2 + D_1^{3/2} \sin\theta_2, \\ \underline{D}_1(2.427) &= -D_1^{1/2} \sin\theta_2 + D_1^{3/2} \cos\theta_2. \end{aligned} \quad (8)$$

Likewise for strange axial-vector charmed mesons,

$$\begin{aligned} D_{s1}(2.460) &= D_{s1}^{1/2} \cos\theta_3 + D_{s1}^{3/2} \sin\theta_3, \\ \underline{D}_{s1}(2.536) &= -D_{s1}^{1/2} \sin\theta_3 + D_{s1}^{3/2} \cos\theta_3. \end{aligned} \quad (9)$$

The mixing angle  $\theta_2 = (5.7 \pm 2.4)^\circ$  is obtained by Belle through a detailed  $B \rightarrow D^* \pi \pi$  analysis [20], while  $\theta_3 \approx 7^\circ$  is determined from the quark potential model [21,22].

### III. METHODOLOGY

#### A. Weak Hamiltonian

For bottom changing  $\Delta b = 1$  decays involving  $b \rightarrow c$  transition, QCD modified weak Hamiltonian is given below:

$$\begin{aligned} H_W &= \frac{G_F}{\sqrt{2}} \{ V_{cb} V_{ud}^* [a_1(\bar{c}b)(\bar{d}u) + a_2(\bar{d}b)(\bar{c}u)] \\ &\quad + V_{cb} V_{cs}^* [a_1(\bar{c}b)(\bar{s}c) + a_2(\bar{s}b)(\bar{c}c)] \\ &\quad + V_{cb} V_{us}^* [a_1(\bar{c}b)(\bar{s}u) + a_2(\bar{s}b)(\bar{c}u)] \\ &\quad + V_{cb} V_{cd}^* [a_1(\bar{c}b)(\bar{d}c) + a_2(\bar{d}b)(\bar{c}c)] \}, \end{aligned} \quad (10)$$

where  $(\bar{q}_i q_j) \equiv \bar{q}_i \gamma_\mu (1 - \gamma_5) q_j$  denotes the weak  $V-A$  current. We follow the convention of the large  $N_c$  limit to fix QCD coefficients  $a_1 \approx c_1$  and  $a_2 \approx c_2$ , where [23]

$$\begin{aligned} c_1(\mu) &= 1.26, & c_2(\mu) &= -0.51 & \text{at } \mu \approx m_c^2, \\ c_1(\mu) &= 1.12, & c_2(\mu) &= -0.26 & \text{at } \mu \approx m_b^2. \end{aligned} \quad (11)$$

#### B. Kinematics

Following the standard procedure for baryon decays [6,24], the matrix element for the  $B_i(1/2^+) \rightarrow B_f(1/2^+) + A_k(1^+)$  decay process can be written as

$$\begin{aligned} \langle B_f(p_f) A_k(q) | H_W | B_i(p_i) \rangle \\ = i \bar{u}_{B_f}(p_f) \varepsilon^{*\mu} (A_1 \gamma_\mu \gamma_5 + A_2 p_{f\mu} \gamma_5 + B_1 \gamma_\mu + B_2 p_{f\mu}) \\ \times u_{B_i}(p_i), \end{aligned}$$

where  $\varepsilon^\mu$  is the polarization vector of the axial-vector meson  $A_k$ . Here  $A_i$ 's and  $B_i$ 's denote the parity conserving (PC) and parity violating (PV) amplitudes, respectively. The decay width is given by

$$\begin{aligned} \Gamma &= \frac{q_\mu}{8\pi} \frac{E_f + m_f}{m_i} \left[ 2(|S|^2 + |P_2|^2) \right. \\ &\quad \left. + \frac{E_A^2}{m_A^2} (|S + D|^2 + |P_1|^2) \right], \end{aligned} \quad (12)$$

and asymmetry parameter is

$$\alpha = \frac{4m_A^2 \text{Re}(S * P_2) + 2E_A^2 \text{Re}(S + D) * P_1}{2m_A^2 (|S|^2 + |P_2|^2) + E_A^2 (|S + D|^2 + |P_1|^2)}, \quad (13)$$

with

$$\begin{aligned} S &= -A_1, \\ P_1 &= -\frac{q_\mu}{E_A} \left( \frac{m_i + m_f}{E_f + m_f} B_1 + m_i B_2 \right), \\ P_2 &= \frac{q_\mu}{E_f + m_f} B_1, \\ D &= -\frac{q_\mu^2}{E_A(E_f + m_f)} (A_1 - m_i A_2), \end{aligned} \quad (14)$$

and

$$|q_\mu| = \frac{1}{2m_i} \sqrt{[m_i^2 - (m_f - m_A)^2][m_i^2 - (m_f + m_A)^2]},$$

where  $q_\mu = (p_i - p_f)_\mu$  is the four momentum of the axial-vector meson in the rest frame of the parent particle,  $m_i$  and  $m_f$  are the masses of the initial and final baryons, and  $m_A$  is the emitted meson mass.  $E_A$  and  $E_f$  are the energies of the axial-vector meson and the daughter baryon, respectively.

In general, weak hadronic decays of the baryons obtain contributions from  $W$ -emission and  $W$ -exchange diagrams, which are usually calculated as factorizable and pole diagrams. Though for weak hadronic decays of hyperons and charm baryons,  $W$ -exchange effects are comparable to the factorization terms, we expect pole terms to be relatively small for the bottom baryon decays due to the large bottom baryon masses. Therefore, to obtain the preliminary estimate of the branching ratios of the decays considered here, we include the factorizable contributions only. In the standard factorization scheme [6], the separable combination of decay amplitudes for  $B_i(1/2^+) \rightarrow B_f(1/2^+) + A_k(1^+)$  is given by

$$\langle A_k(q) | A_\mu | 0 \rangle \langle B_f(p_f) | V^\mu - A^\mu | B_i(p_i) \rangle \quad (15)$$

apart from the scale factors. The first factor is written as

$$\langle A_k(q) | (\bar{q}_1 q_2) | 0 \rangle = f_A m_A \varepsilon_\mu^*, \quad (16)$$

where  $f_A$  is the decay constant of the emitted axial-vector meson  $A_k$ . Matrix elements of the weak currents between baryon states are

$$\begin{aligned} \langle B_f(p_f) | V_\mu | B_i(p_i) \rangle &= \bar{u}_f(p_f) \left[ f_1 \gamma_\mu - \frac{f_2}{m_i} i \sigma_{\mu\nu} q^\nu \right. \\ &\quad \left. + \frac{f_3}{m_i} q_\mu \right] u_i(p_i) \end{aligned} \quad (17)$$

and

$$\begin{aligned} \langle B_f(p_f) | A_\mu | B(p_i) \rangle &= \bar{u}_f(p_f) \left[ g_1 \gamma_\mu \gamma_5 - \frac{g_2}{m_i} i \sigma_{\mu\nu} q^\nu \gamma_5 \right. \\ &\quad \left. + \frac{g_3}{m_i} q_\mu \gamma_5 \right] u_i(p_i). \end{aligned} \quad (18)$$

The factorizable amplitudes are thus given by

$$\begin{aligned} A_1^{\text{fac}} &= -\frac{G_F}{\sqrt{2}} F_C f_A c_k m_A \left[ g_1^{B_i, B_f}(m_A^2) - g_2^{B_i, B_f}(m_A^2) \frac{m_i - m_f}{m_i} \right], \\ A_2^{\text{fac}} &= \frac{G_F}{\sqrt{2}} F_C f_A c_k m_A [2g_2^{B_i, B_f}(m_A^2)/m_i], \\ B_1^{\text{fac}} &= \frac{G_F}{\sqrt{2}} F_C f_A c_k m_A \left[ f_1^{B_i, B_f}(m_A^2) + f_2^{B_i, B_f}(m_A^2) \frac{m_i + m_f}{m_i} \right] \\ B_2^{\text{fac}} &= -\frac{G_F}{\sqrt{2}} F_C f_A c_k m_A [2f_2^{B_i, B_f}(m_A^2)/m_i], \end{aligned} \quad (19)$$

where  $F_C$  contains appropriate Cabibbo-Kobayashi-Maskawa factors and Clebsch-Gordan coefficients.

### C. Form factors and decay constants

Determination of the baryonic form factors in the quark model is not straightforward due to their having three-quark structure, and several corrections, like  $q^2$  dependence of the form factors and hard gluon QCD contributions. Moreover, the form factors for baryon-baryon transitions are expected to satisfy the constraints imposed by the heavy quark symmetry. Charm changing baryon-baryon transition form factors have been evaluated by Perez-Marcial *et al.* [25] in the nonrelativistic quark model (NRQM). We extend their analysis to calculate bottom changing baryon-baryon transition form factors which are given in column 2 of Table I. However, it has been pointed out by Cheng and Tseng [26] that the relations between form factors at zero recoil, which are given by the heavy quark symmetry, are not respected by baryon-baryon form factors obtained in the nonrelativistic quark model. In order to improve the quark model calculations, in consistency with the features of the heavy quark symmetry, they have calculated the  $1/M$  corrections to form factors using the heavy quark effective theory (HQET) considerations. We have employed their formalism to recalculate the heavy-heavy and heavy-light transition form factors using our phase convention. The calculated form factors are given in column 3 of Table I. In light of the large  $1/M$  corrections, the results obtained in NRQM may not be reliable. Therefore, considering the theoretical uncertainties in the evaluation of the form factors, which would obviously affect the branching ratios, we have calculated the branching ratios in both of these models.

Let us now turn to the decay constants of the axial-vector mesons. The decay constant of the  $J^{\text{PC}} = 1^{+-}$  axial-vector mesons is suppressed due to the  $C$ -parity behavior. Under charge conjugation, the two types of axial-vector mesons transform as

$$\begin{aligned} M_b^a(1^{++}) &\rightarrow +M_b^a(1^{++}) \\ M_b^a(1^{+-}) &\rightarrow -M_b^a(1^{+-}) \quad (a, b = 1, 2, 3), \end{aligned} \quad (20)$$

where  $M_b^a$  denotes meson  $3 \times 3$  matrix elements in SU(3) flavor symmetry. Since the weak axial-vector current transforms as  $(A_\mu)_b^a \rightarrow +(A_\mu)_a^b$  under charge conjugation, only the  $(1^{++})$  state can be produced through the axial-vector current in the SU(3) symmetry limit [18].

To determine the decay constant of  $K_1(1.270)$ , we use the following formula:

$$\Gamma(\tau \rightarrow K_1 \nu_\tau) = \frac{G_F^2}{16\pi} |V_{us}|^2 f_{K_1}^2 \frac{(m_\tau^2 + 2m_{K_1}^2)(m_\tau^2 - m_{K_1}^2)^2}{m_\tau^3}, \quad (21)$$

which gives  $f_{K_1(1.270)} = 0.175 \pm 0.019$  GeV. The decay constant of  $K_1(1.400)$  can be simply related to  $K_1(1.270)$

TABLE I. Baryon to baryon form factors at  $q^2 = 0$ .

Decay	Using NRQM [25]				Based on HQET considerations [26]			
	$f_1$	$f_2$	$g_1$	$g_2$	$f_1$	$f_2$	$g_1$	$g_2$
$\Lambda_b^0 \rightarrow \Lambda_c^+$	0.310	0.170	0.530	-0.044	0.547	0.103	0.592	0.013
$\Lambda_b^0 \rightarrow n$	0.067	-0.110	-0.098	0.019	-0.045	-0.024	-0.090	-0.020
$\Lambda_b^0 \rightarrow \Lambda$	-0.058	0.130	0.120	-0.021	0.061	0.025	0.100	0.013
$\Xi_b^0 \rightarrow \Xi_c^+$	0.330	0.150	0.540	-0.041	0.554	0.129	0.590	0.019
$\Xi_b^0 \rightarrow \Lambda$	-0.018	0.036	0.040	-0.007	0.020	0.012	0.039	0.012
$\Xi_b^0 \rightarrow \Sigma^0$	-0.029	0.070	0.081	-0.014	0.043	0.028	0.080	0.026
$\Xi_b^0 \rightarrow \Xi^0$	0.039	-0.130	-0.160	0.024	-0.083	-0.041	-0.130	-0.024
$\Xi_b^- \rightarrow \Xi_c^0$	0.330	0.150	0.530	-0.041	0.554	0.129	0.590	0.019
$\Xi_b^- \rightarrow \Sigma^-$	-0.039	0.092	0.110	-0.018	0.063	0.040	0.113	0.037
$\Xi_b^- \rightarrow \Xi^-$	0.037	-0.120	-0.150	0.024	-0.084	-0.041	-0.131	-0.025

in SU(3) limit as  $f_{K_1(1.400)}/f_{K_1(1.270)} = \cot\theta_1$ . A small value around 0.011 GeV for the decay constant of  $K_{1B}$  may arise through SU(3) breaking, which yields

$$f_{\underline{K}_1(1.400)} = f_{K_{1A}} \cos\theta_1 - f_{K_{1B}} \sin\theta_1 = -0.087 \text{ GeV}, \tag{22}$$

for  $\theta_1 = -58^\circ$  [22]. Similarly, the decay constant of  $a_1(1.260)$  can be obtained from  $B(\tau \rightarrow a_1 \nu_\tau)$ . However, this branching ratio is not given by Particle Data Group [1], although the data on  $\tau \rightarrow a_1 \nu_\tau \rightarrow \rho \pi \nu_\tau$  have been reported by various experiments. We take  $f_{a_1} = 0.203 \pm 0.018$  GeV from the analysis given by Bloch *et al.* [27]. For the decay constant of  $f_1(1.285)$ , we assume  $f_{f_1} \approx f_{a_1}$ .

The decay constants

$$\begin{aligned} f_{D_{1A}} &= -0.127 \text{ GeV}, & f_{D_{1B}} &= 0.045 \text{ GeV}, \\ f_{D_{s1A}} &= -0.121 \text{ GeV}, & f_{D_{s1B}} &= 0.038 \text{ GeV} \end{aligned} \tag{23}$$

have been taken from [22] and determine  $f_{\chi_{c1}} \approx -0.160$  GeV [22].

#### IV. DISCUSSION OF RESULTS AND CONCLUSIONS

Substituting various quantities in the decay amplitudes given in Eq. (19), and using Eqs. (12) and (13), we now compute the branching ratios and asymmetry parameters

TABLE II. Branching ratio and asymmetry for  $\Lambda_b^0$  decays.

Decay	Branching ratio (%)	Asymmetry “ $\alpha$ ”	Branching ratio (%)	Asymmetry “ $\alpha$ ”
	Using the form factors obtained in column 2 of Table I		Using the form factors obtained in column 3 of Table I	
$\Delta C = 1, \Delta S = 0$				
$\Lambda_b^0 \rightarrow \Lambda_c^+ a_1^-$	0.58	-0.53	0.90	-0.73
$\Lambda_b^0 \rightarrow n D_1^0$	$1.4 \times 10^{-3}$	0.74	$9.2 \times 10^{-4}$	-0.31
$\Lambda_b^0 \rightarrow n D_{-1}^0$	$4.9 \times 10^{-5}$	0.74	$3.1 \times 10^{-5}$	-0.31
$\Delta C = 0, \Delta S = -1$				
$\Lambda_b^0 \rightarrow \Lambda_c^+ D_{s1}^-$	0.33	-0.084	0.42	-0.24
$\Lambda_b^0 \rightarrow \Lambda_c^+ D_{-s1}^-$	0.016	-0.064	0.021	-0.22
$\Lambda_b^0 \rightarrow \Lambda \chi_{c1}$	$7.0 \times 10^{-3}$	0.49	$3.7 \times 10^{-3}$	0.001
$\Delta C = 1, \Delta S = -1$				
$\Lambda_b^0 \rightarrow \Lambda_c^+ K_1^-$	0.024	-0.51	0.037	-0.71
$\Lambda_b^0 \rightarrow \Lambda_c^+ K_{-1}^-$	$7.9 \times 10^{-3}$	-0.46	0.012	-0.66
$\Lambda_b^0 \rightarrow \Lambda D_1^0$	$1.0 \times 10^{-4}$	0.62	$6.1 \times 10^{-5}$	-0.31
$\Lambda_b^0 \rightarrow \Lambda D_{-1}^0$	$3.5 \times 10^{-6}$	0.62	$2.1 \times 10^{-6}$	-0.31
$\Delta C = 0, \Delta S = 0$				
$\Lambda_b^0 \rightarrow \Lambda_c^+ D_1^-$	0.019	-0.092	0.025	-0.26
$\Lambda_b^0 \rightarrow \Lambda_c^+ D_{-1}^-$	$6.7 \times 10^{-4}$	-0.093	$8.5 \times 10^{-4}$	-0.26
$\Lambda_b^0 \rightarrow n \chi_{c1}$	$2.7 \times 10^{-4}$	0.58	$1.6 \times 10^{-4}$	-0.003

TABLE III. Branching ratio and asymmetry for  $\Xi_b^0$  decays.

Decay	Branching ratio (%)	Asymmetry “ $\alpha$ ”	Branching ratio (%)	Asymmetry “ $\alpha$ ”
	Using the form factors obtained in column 2 of Table I		Using the form factors obtained in column 3 of Table I	
$\Delta C = 1, \Delta S = 0$				
$\Xi_b^0 \rightarrow \Xi_c^+ a_1^-$	0.63	-0.57	0.93	-0.73
$\Xi_b^0 \rightarrow \Lambda D_1^0$	$2.4 \times 10^{-4}$	0.58	$1.8 \times 10^{-4}$	-0.32
$\Xi_b^0 \rightarrow \Lambda D_{-1}^0$	$8.3 \times 10^{-6}$	0.58	$6.3 \times 10^{-6}$	-0.32
$\Xi_b^0 \rightarrow \Sigma^0 D_1^0$	$9.5 \times 10^{-4}$	0.52	$7.7 \times 10^{-4}$	-0.33
$\Xi_b^0 \rightarrow \Sigma^0 D_{-1}^0$	$3.2 \times 10^{-5}$	0.52	$2.7 \times 10^{-5}$	-0.33
$\Delta C = 0, \Delta S = -1$				
$\Xi_b^0 \rightarrow \Xi_c^+ D_{s1}^-$	0.35	-0.12	0.44	-0.24
$\Xi_b^0 \rightarrow \Xi_c^+ D_{-s1}^-$	0.018	-0.096	0.022	-0.22
$\Xi_b^0 \rightarrow \Xi^0 \chi_{c1}$	0.012	0.39	$7.0 \times 10^{-3}$	0.0008
$\Delta C = 1, \Delta S = -1$				
$\Xi_b^0 \rightarrow \Xi_c^+ K_1^-$	0.026	-0.55	0.039	-0.71
$\Xi_b^0 \rightarrow \Xi_c^+ K_{-1}^-$	$8.4 \times 10^{-3}$	-0.50	0.012	-0.66
$\Xi_b^0 \rightarrow \Xi^0 D_1^0$	$1.7 \times 10^{-4}$	0.44	$1.1 \times 10^{-4}$	-0.32
$\Xi_b^0 \rightarrow \Xi^0 D_{-1}^0$	$5.9 \times 10^{-6}$	0.44	$3.9 \times 10^{-6}$	-0.32
$\Delta C = 0, \Delta S = 0$				
$\Xi_b^0 \rightarrow \Xi_c^+ D_1^-$	0.021	-0.13	0.026	-0.25
$\Xi_b^0 \rightarrow \Xi_c^+ D_{-1}^-$	$7.1 \times 10^{-4}$	-0.13	$8.9 \times 10^{-4}$	-0.25
$\Xi_b^0 \rightarrow \Lambda \chi_{c1}$	$4.9 \times 10^{-5}$	0.47	$3.2 \times 10^{-5}$	-0.015
$\Xi_b^0 \rightarrow \Sigma^0 \chi_{c1}$	$1.9 \times 10^{-4}$	0.43	$1.3 \times 10^{-4}$	-0.007

 TABLE IV. Branching ratio and asymmetry for  $\Xi_b^-$  decays.

Decay	Branching ratio (%)	Asymmetry “ $\alpha$ ”	Branching ratio (%)	Asymmetry “ $\alpha$ ”
	Using the form factors obtained in column 2 of Table I		Using the form factors obtained in column 3 of Table I	
$\Delta C = 1, \Delta S = 0$				
$\Xi_b^- \rightarrow \Xi_c^0 a_1^-$	0.63	-0.57	0.93	-0.73
$\Xi_b^- \rightarrow \Sigma^- D_1^0$	$1.9 \times 10^{-3}$	0.52	$1.6 \times 10^{-3}$	-0.33
$\Xi_b^- \rightarrow \Sigma^- D_{-1}^0$	$6.6 \times 10^{-5}$	0.52	$5.4 \times 10^{-5}$	-0.33
$\Delta C = 0, \Delta S = -1$				
$\Xi_b^- \rightarrow \Xi_c^0 D_{s1}^-$	0.35	-0.12	0.44	-0.24
$\Xi_b^- \rightarrow \Xi_c^0 D_{-s1}^-$	0.018	-0.096	0.022	-0.22
$\Xi_b^- \rightarrow \Xi^- \chi_{c1}$	0.013	0.38	$7.0 \times 10^{-3}$	0.002
$\Delta C = 1, \Delta S = -1$				
$\Xi_b^- \rightarrow \Xi_c^0 K_1^-$	0.026	-0.55	0.039	-0.71
$\Xi_b^- \rightarrow \Xi_c^0 K_{-1}^-$	$8.5 \times 10^{-3}$	-0.50	0.012	-0.66
$\Xi_b^- \rightarrow \Xi^- D_1^0$	$1.8 \times 10^{-4}$	0.43	$1.2 \times 10^{-4}$	-0.32
$\Xi_b^- \rightarrow \Xi^- D_{-1}^0$	$6.0 \times 10^{-6}$	0.43	$3.9 \times 10^{-6}$	-0.32
$\Delta C = 0, \Delta S = 0$				
$\Xi_b^- \rightarrow \Xi_c^0 D_1^-$	0.021	-0.13	0.026	-0.25
$\Xi_b^- \rightarrow \Xi_c^0 D_{-1}^-$	$7.1 \times 10^{-4}$	-0.13	$8.9 \times 10^{-4}$	-0.25
$\Xi_b^- \rightarrow \Sigma^- \chi_{c1}$	$3.9 \times 10^{-4}$	0.43	$2.7 \times 10^{-4}$	-0.007

for  $\Lambda_b^0$ ,  $\Xi_b^0$ , and  $\Xi_b^-$  decays. Results are given in Tables II, III, and IV. We conclude the following:

- (1) The decays  $\Lambda_b^0 \rightarrow \Lambda_c^+ a_1^- / \Lambda_c^+ D_{s1}^-$ ,  $\Xi_b^0 \rightarrow \Xi_c^+ a_1^- / \Xi_c^+ D_{s1}^-$ , and  $\Xi_b^- \rightarrow \Xi_c^0 a_1^- / \Xi_c^0 D_{s1}^-$  are the dominant ones having branching ratios in the range 0.33%–0.95% in both models. These branching ratios may interest the experimentalists for their search. In addition, the decays  $\Lambda_b^0 \rightarrow \Lambda_c^+ D_{s1}^- / \Lambda_c^+ K_1^- / \Lambda_c^+ D_1^-$ ,  $\Xi_b^0 \rightarrow \Xi_c^+ D_{s1}^- / \Xi_c^+ K_1^- / \Xi_c^+ D_1^- / \Xi^0 \chi_{c1}$ , and  $\Xi_b^- \rightarrow \Xi_c^0 D_{s1}^- / \Xi_c^0 K_1^- / \Xi_c^0 D_1^- / \Xi^- \chi_{c1}$  are also dominant having next order branching ratios in the range 0.01%–0.04%.
  - (2) The decays involving the  $b_1^-$  meson in the final state are forbidden in the isospin limit. However, the isospin symmetry breaking may generate  $\Lambda_b^0 \rightarrow \Lambda_c^+ b_1^-$ ,  $\Xi_b^0 \rightarrow \Xi_c^+ b_1^-$ , and  $\Xi_b^- \rightarrow \Xi_c^0 b_1^-$  decays, which in our analysis are found to have branching ratios of the order of  $10^{-6}$ %.
  - (3) Though for weak hadronic decays of the hyperons and charm baryons, pole contributions are comparable to the factorization terms, we expect pole
- terms to be relatively small for the bottom baryon decays due to the large bottom baryon masses.
- (4) Determination of the baryonic form factors is not reliable for several reasons, like complications due to three-quark dynamics,  $q^2$  dependence, and hard gluon QCD contributions. The form factors obtained in the quark model for baryon-baryon transitions are also expected to satisfy the relations given by the heavy quark symmetry. It has been observed that the form factors given by NRQM [25] do not respect such relations and large  $1/M$  corrections have been obtained using the HQET considerations [26]. Therefore, considering the theoretical uncertainties in the evaluation of the form factors, we have obtained the preliminary estimates of branching ratios in both of these models.
  - (5) Predicted branching ratios are of the same order in both models, however, asymmetry parameters of some of the decays show change in sign, observation of which would clarify the situation.

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