Production of electron neutrinos at nuclear power reactors and the prospects for neutrino physics

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High flux of electron neutrinos(ν_e) is produced at nuclear power reactors through the decays of nuclei activated by neutron capture. Realistic simulation studies on the neutron transport and capture at the reactor core were performed. The production of ⁵¹Cr and ⁵⁵Fe give rise to monoenergetic ν_e 's at Q-values of 753 keV and 231 keV and fluxes of 8.3×10^{-4} and $3.0 \times 10^{-4} \nu_e$ /fission, respectively. Using data from a germanium detector at the Kuo-Sheng Power Plant, we derived direct limits on the ν_e magnetic moment and the radiative lifetime of $\mu_{\nu} < 1.3 \times 10^{-8} \mu_B$ and $\tau_{\nu}/m_{\nu} > 0.11$ s/eV at 90% confidence level (CL), respectively. Indirect bounds on τ_{ν}/m_{ν}^3 were also inferred. The ν_e -flux can be enhanced by loading selected isotopes to the reactor core, and the potential applications and achievable statistical accuracies were examined. These include accurate cross-section measurements, studies of mixing angle θ_{13} and monitoring of plutonium production.

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I. INTRODUCTION

Results from recent neutrino experiments provide strong evidence for neutrino oscillations due to finite neutrino masses and mixings [1,2]. Their physical origin and experimental consequences are not fully understood. Studies on neutrino properties and interactions can shed light on these fundamental questions and constrain theoretical models necessary for the interpretation of future precision data. It is therefore motivated to explore alternative neutrino sources and new neutrino detection channels.

The theme of this paper is to study the production of electron neutrinos (ν_e) from nuclear power reactors. Fluxes derived from the "Standard Reactor" configuration were used to obtain direct limits on the neutrino properties from data taken at the Kuo-Sheng Power Plant. The hypothetical "Loaded Reactor" scenario was also studied, where selected materials were inserted to the core to substantially enhance the ν_e -flux. The detection channels and the achievable physics potentials in ideal experiments were investigated.

II. STANDARD POWER REACTOR

A. Evaluation of Electron Neutrino Fluxes

Production of electron antineutrinos($\bar{\nu}_e$) due to β -decays of fission products at power reactors is a well-

studied process. There are standard parametrizations for the reactor $\bar{\nu}_{e}$ spectra [3]. The typical fission rate at the reactor core with a thermal power of P_{th} in GW is 0.3×10^{20} P_{th}s⁻¹, while an average about $6\bar{\nu}_{e}$ /fission are emitted. The modeling of the $\bar{\nu}_{e}$ energy spectra above 3 MeV is consistent with measurements at the <5% level [4], while the low energy portion is subjected to much bigger uncertainties [5]. In a realistically achievable setting at a location 10 m from a core with P_{th} = 4.5 GW, the $\bar{\nu}_{e}$ -flux is 6.4 × 10^{13} cm⁻² s⁻¹.

Nuclear reactors also produce ν_e via (a) electron capture or inverse beta decay of the fission products and (b) neutron activation on the fuel rods and the construction materials at the reactor core. There were unpublished studies [6] on the reactor ν_e -fluxes from early reactor experiments, indicating that they would not contribute to the background in the measurements with $\bar{\nu}_e$. We extended these studies with realistic simulations, and focused on the potentials of using them as sources to study neutrino physics.

Primary fission daughters are predominantly neutronrich and go through β^- -decays to reach stability. Direct feeding to isotopes which decay by β^+ -emissions or electron capture(EC) is extremely weak, at the $\sim 10^{-8}$ /fission level [7]. The leading components for the ²³⁵U and ²³⁹Pu fissions with relative contributions r_f, fission yields Y_f and branching ratio BR for ν_e -emissions are shown in Table Ia. The average ν_e -yield per fission Y_{ν} is therefore Y_{ν} = r_f · Y_f · BR. In addition, stable fission products can undergo

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TABLE I. The leading ν_e -yields per fission ($Y_{\nu} = r_f \cdot Y_f \cdot BR$) from (a) direct feeding of daughters (Z,N) and (b) neutron capture on stable isotope (Z,N-1) at equilibrium conditions.

(a)	Series	(Z,N	I) Y	_f (Z, N)	Q(M	leV)	BR(%)	Y_{ν}
	²³⁵ U	⁸⁶ R	b 1	$.4e^{-5}$	0.:	53	0.0	05	$4.3e^{-10}$
	$(r_{\rm f} = 0.62)$	⁸⁷ S	r <	$< 1e^{-5}$	0.2	2	0.3		$< 1.9e^{-8}$
		104 R	h	$7e^{-8}$	1.	15	0.4	5	$2.0e^{-10}$
		128	[1	$.2e^{-8}$	1.	26	6		$4.3e^{-10}$
	²³⁹ Pu	128	[1	$.7e^{-6}$	1.	26	6		$2.6e^{-8}$
	$(r_f = 0.26)$	^{110}A	g 1	.3e ⁻⁵	0.	88	0.3		$1.0e^{-8}$
_									
(b)	Series (Z,N)	$Y_f(A$	-1) σ	$r_{n\gamma}(b)$	Q(M	eV) I	3R(%) Y_{ν}
	²³⁵ U ¹	⁰⁴ Rh	3.20	e^{-2}	146	1.1	5	0.45	$9.0e^{-5}$
	$(r_f = 0.62)$	^{128}I	1.20	e^{-3}	6.2	1.2	6	6	$4.3e^{-5}$
	1	²² Sb	1.20	e^{-4}	6.2	1.6	2	2.2	$1.6e^{-6}$
	1	¹⁰ Ag	3e	-4	89	0.8	8	0.3	$5.6e^{-7}$
	²³⁹ Pu	^{128}I	5.20	e^{-3}	6.2	1.2	6	6	$8.2e^{-5}$
	$(r_f = 0.26)^{-1}$	⁰⁴ Rh	6.80	e^{-2}	146	1.1	5	0.45	$8.0e^{-5}$
	1	¹⁰ Ag	1.10	e^{-2}	89	0.8	8	0.3	$8.9e^{-6}$
	1	²² Sb	4.30	e^{-4}	6.2	1.6	2	2.2	$2.6e^{-6}$

 (n,γ) capture to unstable states which decay by $\nu_{\rm e}$ -emissions. The equilibrium yield of the major components [7] are shown in Table Ib. The leading contribution is from 103 Rh $(n, \gamma)^{104}$ Rh, where the yield summed over all four fissile isotopes is $Y_{\nu} = 2.1 \times 10^{-4} \nu_{\rm e}/{\rm fission}$. However, under realistic settings in reactor operation, the time to reach equilibrium is of the order of 10 years, such that the contribution to $\nu_{\rm e}$ -emissions by this channel is also small $(Y_{\nu} \sim 10^{-5})$.

A complete "MCNP" neutron transport simulation [8] was performed to study the effect of neutron capture on the reactor core materials, which include the fuel elements, cooling water, control rod structures and construction materials. While the layout is generic for most nuclear power reactors, the exact dimensions and material compositions were derived from the $P_{th} = 2.9$ GW Core#1 of the Kuo-Sheng(KS) Nuclear Power Station in Taiwan, where a neutrino laboratory [9] has been built. The reactor core materials and their mass compositions are summarized in Table IIa. A homogeneous distribution of these materials inside a stainless steel containment vessel of inner radius 225 cm, height 2750 cm, and thickness 22 cm was adopted. This approximation is commonly used and has been demonstrated to be valid in reactor design studies [10]. Standard parametrizations of the "Watt" fission neutron spectra [8,10] were adopted as input:

$$\phi_{\rm n} \propto \exp(-E/a)\sinh(\sqrt{bE})$$
 (1)

where (a,b) depend on the fission elements. The emitted neutron spectra for the fissile isotopes are depicted in Fig. 1. There are on average 2.5 neutrons generated per fission with energy distribution peaked at ~ 1 MeV. The

TABLE II. The compositions for (a) the construction materials inside the reactor core and of the containment vessel used in the neutron capture studies, and (b) the three isotopes responsible for ν_{e} -emissions.

(a)	Functions	Materials	Weig	ht (kg)	
	UO ₂ Fuel Elements:	Total	11(0000	
	Fission Isotopes:	²³⁵ U	1	376	
		²³⁸ U	98	8688	
		²³⁹ Pu		431	
		²⁴¹ Pu		84	
	Non-Fuel Materials insic	le			
	Containment Vessel:	Total	125000		
	Fuel Container	Zr-Alloy	67500		
	Cooling	Water	42	2500	
	Control Rod Assembly	at			
	complete insertion:	B_4C		479	
		Stainless Steel	14	100	
	Containment Vessel:	Stainless Steel	910	0000	
(h)	Materials	Compositions (%)			
(0)		50Cr	54E2	58 NI:	
	Stainless Steel SUS304	0.95	12 12	63	
	Zr-2 alloy	0.95	0.006	0.034	

neutrons are scattered in the core and eventually absorbed by either the (n,fission) processes with the fuel elements or the (n,γ) or other interactions with the core materials.

An important constraint is that an equilibrium chain reaction must be sustained to provide stable power generation. This is achieved by regulating the fraction of the control rod assembly (ξ) inserted into the fuel bundles. This constraint is parametrized by K_{eff} defined as the ratio of neutron-induced fission to starting fission rates. The variation of K_{eff} versus ξ is depicted in Fig. 2. The equi-



FIG. 1. The energy spectra for emitted neutrons from the fissile isotopes 235 U, 238 U and 239 Pu. The spectra for 241 Pu is approximated to be that from 239 Pu.



FIG. 2. The variations of the K_{eff} parameter and the neutrino yield Y_{ν} from ⁵¹Cr, as functions of control rod fraction ξ .

librium conditions require $K_{eff} = 1.0$, and the distributions of the per-fission neutron capture yield (Y_n) are given in Table III. Only 0.35% of the neutrons escape from the containment vessel, justifying that detailed treatment exterior to the vessel is not necessary.

Stainless steel "SUS304" and "Zr-2 alloy" are the typical construction materials at reactor cores, used in the containment vessel and control rod assembly, as well as in fuel-element containers, respectively. These materials contain ⁵⁰Cr, ⁵⁴Fe and ⁵⁸Ni with compositions given in Table IIb. Upon activation by the (n,γ) reactions, these isotopes produce ⁵¹Cr, ⁵⁵Fe and ⁵⁹Ni that will subsequently

decay by EC and ν_{e} -emissions. Their properties (isotopic abundance IA, (n, γ) cross-sections $\sigma_{n\gamma}$, half-life $\tau_{\frac{1}{2}}$, EC Qvalue and branching ratio BR) and ν_{e} -yield ($Y_{\nu} = Y_{n} \cdot$ BR) are given in Table IV. The variation of Y_{ν} in ⁵¹Cr with ξ is displayed in Fig. 2. The half-life of ⁵⁹Ni is too long and thus not relevant for ν_{e} -emissions. The dominant reactor ν_{e} sources are therefore ⁵¹Cr and ⁵⁵Fe, with total yields of $Y_{\nu} = 8.3 \times 10^{-4}$ and $3.0 \times 10^{-4} \nu_{e}$ /fission, implying ν_{e} -fluxes of $7.5 \times 10^{16} \text{s}^{-1}$ and $2.7 \times 10^{16} \text{s}^{-1}$, respectively, at a 2.9 GW reactor. The total strength corresponds to a 2.7 MCi source.

To demonstrate the validity of the simulation procedures and results, a series of cross-checks were made. As depicted in Fig. 2, the control rod fraction is $\xi = 8\%$ at critical condition $K_{eff} = 1$. The relative fission yields of the four fissile elements are given in Table III. The neutron energy spectrum averaged over the reactor core volume is depicted in Fig. 3. The integrated flux is $7.6 \times$ 10^{13} cm⁻² s⁻¹, with 26\%, 52\% and 22\% in the thermal (<1 eV), epithermal (1 eV to 1 MeV) and fast (>1 MeV) ranges, respectively. The maximal flux at the center of the reactor core is about 2.5 times the average value.

Comparisons were made between these results with industry-standard calculations and actual reactor operation data. Agreement to within 10% was achieved. In particular, the important neutron capture process ²³⁸U(n, γ) leads to the accumulation of ²³⁹Pu via β -decays of ²³⁹U. The yield of Y_n = 0.59 per fission agrees with the results from an independent study [11]. These consistency requirements

Channel	Isotope	Weight (kg)	Y _n
(n,fission) on	²³⁸ U	98688	0.057
fuel element	²³⁵ U	1376	0.62
	²³⁹ Pu	431	0.26
	²⁴¹ Pu	84	0.068
	ΣY_n (fission) =		1.0
(n,γ) at	²³⁸ U	98688	0.59
Core Region	Water	42519	0.25
	$^{10}\mathbf{B}$	5.4	0.28
	⁵⁰ Cr	9.0	0.00067
	⁵⁴ Fe	26.6	0.00018
	⁵⁸ Ni	57.6	0.0010
(n,γ) at	⁵⁰ Cr	8650	0.00016
Stainless Steel	⁵⁴ Fe	38200	0.00012
Containment Vessel	⁵⁸ Ni	57300	0.00026
Other capture channels:			
[mainly (n, γ) on other isotopes]			0.37
External to Containment Vessel			0.009
	$\Sigma Y_n(total) =$		2.5

TABLE III. The neutron capture yields Y_n of the major channels at $K_{eff} = 1$. The average number of neutron emitted per fission is $\Sigma Y_n = 2.5$.

TABLE IV. The ν_e sources and their yields Y_n , Y_{ν} (both in 10^{-4}) at the reactor core.

Isotope	IA(%)	$\sigma_{n\gamma}(b)$	$ au_{1/2}$	Q(keV)	BR(%)	Y _n	Y_{ν}
¹⁰³ Rh	4.6 ^a	146	41.8 s	1145	0.45	30 ^b	0.14 ^b
⁵⁰ Cr	4.35	15.8	27.7 d	753	100	8.3	8.3
⁵⁴ Fe	5.85	2.3	2.73 у	231	100	3.0	3.0
⁵⁸ Ni	68.1	4.6	7.6e ⁴ y	1073	100	13.0	—

^afission yield

^baveraged over 18 months reactor period



FIG. 3. Energy spectrum of neutron at the reactor core, derived from MCNP simulations.

posed constraints to possible systematic effects. The leading uncertainties are expected to arise from the modeling of the reactor core compositions, and were estimated to be <20%.

The process ²³⁸U(n, γ) generates two $\bar{\nu}_{e}$'s from β -decays of ²³⁹U. Adding to the $6\bar{\nu}_{e}$ /fission from the fission fragments, the total $\bar{\nu}_{e}$ -yield is therefore $Y_{\bar{\nu}} = 7.2\bar{\nu}_{e}$ /fission, such that $Y_{\nu}/Y_{\bar{\nu}} \sim 1.6 \times 10^{-4}$. In particular, the ν_{e} -e to $\bar{\nu}_{e}$ -e event rate ratio at the electron recoil energy range of 300 to 750 keV is $\sim 2 \times 10^{-4}$, too small to account for the factor of 2 excess over the standard model values in the measured $\bar{\nu}_{e}$ -e rates recently reported by the MUNU experiment[12].

B. Studies of Intrinsic Neutrino Properties

A high-purity germanium detector has collected data with a trigger threshold of 5 keV at a distance of 28 m from the core at KS Plant. Background at the range of 1/ (kg-keV-day) was achieved [13], comparable with those from underground Dark Matter experiments. These unique low energy data provide an opportunity to study directly the possible anomalous effects from reactor ν_e . Previous reactor experiments were sensitive only to processes above the MeV range. While the sensitivities are not competitive to those from reactor $\bar{\nu}_e$ [12,13], the studies provide direct probes on the ν_e properties without assuming CPT invariance, and cover possible anomalous matter effects which may differentiate ν_e from $\bar{\nu}_e$.

The anomalous coupling of neutrinos with photons are consequences of finite neutrino masses and electromagnetic form factors [14]. The manifestations include neutrino magnetic moments (μ_{ν}) and radiative decays (Γ_{ν}) . The searches of μ_{ν} are usually performed in neutrinoelectron scattering experiments $\nu_{l_1} + e^- \rightarrow \nu_{l_2} + e^-$. Both diagonal and transition moments are allowed, corresponding to the cases where $l_1 = l_2$ and $l_1 \neq l_2$, respectively. The experimental observable is the kinetic energy of the recoil electrons (T). A finite neutrino magnetic moment (μ_l) , usually expressed in units of the Bohr magneton

$$\mu_{\rm B} = \frac{\rm e}{2\rm m_e}; \quad \rm e^2 = 4\pi\alpha_{\rm em} \tag{2}$$

will contribute to a differential cross-section term given by [3]:

$$\left(\frac{\mathrm{d}\sigma}{\mathrm{d}T}\right)_{\mu} = \frac{\pi\alpha_{\mathrm{em}}^{2}\mu_{\mathrm{l}}^{2}}{\mathrm{m}_{\mathrm{e}}^{2}} \left[\frac{1-\mathrm{T}/\mathrm{E}_{\nu}}{\mathrm{T}}\right]$$
(3)

where α_{em} is the fine-structure constant, E_{ν} is the neutrino energy and the natural unit with $\hbar = c = 1$ is adopted. The quantity μ_l is an effective parameter which can be expressed as[15]:

$$\mu_1^2 = \sum_j \left| \sum_k U_{lk} \cdot \mu_{jk} \right|^2, \tag{4}$$

where U is the mixing matrix and μ_{jk} are the coupling constants between the mass eigenstates ν_j and ν_k with the photon. Experimental signatures of μ_l from reactor neutrino experiments are therefore an excess of events between reactor ON/OFF periods with an 1/T distribution.

The 18-month reactor cycle suggests that the optimal $\nu_{\rm e}$'s are from ⁵¹Cr, where the half-life is $\tau_{\frac{1}{2}} = 27.7$ days. The equilibrium flux at 28 m is 7.3×10^8 cm⁻² s⁻¹. With the actual reactor OFF period denoted by t = 0 to t = 67 days, the background-measuring OFF* period was taken to be from t = 30 to 101 days, during which the average residual $\nu_{\rm e}$ -flux was 37% of the steady-state ON-level. The ON periods included data prior to reactor OFF and starting from t = 101 days. A total of 3458/1445 hours of data from the ON/OFF* periods were used in the analysis reported in this article.

The focus in the μ_{ν} -search was on the T = 10 - 100 keV range for the enhanced signal rates and robustness in the control of systematic uncertainties. The ν_{e} -e scattering rates due to μ_{ν} at the sensitivity level being explored are much larger (factor of 20 at 10 keV) than the Standard Model rates from $\bar{\nu}_{e}$, such that the uncertainties in the irreducible background can be neglected [5]. Similar event selection and analysis procedures as Ref. [13] were adopted. Neutrino-induced events inside the Ge target would manifest as "lone-events" uncorrelated with the cosmic-ray veto panels and the NaI(Tl) anti-Compton scintillators. Additional pulse shape analysis further suppressed background due to electronic noise and the delayed "cascade" events. No excess of lone-events was observed in the $ON - OFF^*$ residual spectrum. A limit of

$$\mu_{\nu} < 1.3 \times 10^{-8} \mu_{\rm B}$$

at 90% confidence level (CL) was derived. The residual plot and the best-fit regions are displayed in Fig. 4(a).

The neutrino-photon couplings probed by ν -e scatterings can also give rise to neutrino radiative decays: $\nu_j \rightarrow \nu_k + \gamma$ between mass eigenstates ν_j and ν_k with masses m_j and m_k , respectively. The decay rates Γ_{jk} and half-lives τ_{jk} are related to μ_{jk} via [16]

$$\frac{1}{\tau_{jk}} = \Gamma_{jk} = \frac{\mu_{jk}^2}{8\pi} \frac{(m_j^2 - m_k^2)^3}{m_j^3}.$$
 (5)

Results from oscillation experiments [2,17] indicate that $\nu_{\rm e}$ is predominantly a linear combination of mass eigenstates ν_1 and ν_2 with mixing angle θ_{12} given by $\sin^2\theta_{12} \sim 0.27$. The mass differences between the mass eigenstates are $\Delta m_{12}^2 \sim 8 \times 10^{-5} \text{ eV}^2$ and $\Delta m_{23}^2 \sim 2 \times 10^{-3} \text{ eV}^2$. Both "normal" (nor.: $m_3 \gg m_2 > m_1$) and "inverted" (inv.: $m_2 > m_1 \gg m_3$) mass hierarchies are allowed. The $\nu_1 \rightarrow \nu_3$ and $\nu_2 \rightarrow \nu_3$ decays are allowed only in the inverted mass hierarchy, while $\nu_2 \rightarrow \nu_1$ is possible in both hierarchies. Adopting these as input, the μ_{ν} limit can be translated via Eq. (5) to indirect bounds of

$$\begin{aligned} \frac{\tau_{13}}{m_1^3} (\text{inv.:} \nu_1 \to \nu_2) &> 1 \times 10^{23} \text{ s/eV}^3 \\ \frac{\tau_{23}}{m_2^3} (\text{inv.:} \nu_2 \to \nu_3) &> 4 \times 10^{22} \text{ s/eV}^3 \\ \frac{\tau_{21}}{m_2^3} (\text{nor.} + \text{inv.:} \nu_2 \to \nu_1) &> 6 \times 10^{26} \text{ s/eV}^3 \end{aligned}$$

at 90% CL. These limits are sensitive to the bare neutrinophoton couplings and are therefore valid for neutrino radiative decays of in vacuum.

It is also of interest to perform a direct search of $\nu_e \rightarrow \nu_X + \gamma$ the signature of which is a step-function convoluted with detector efficiencies where the end-point is at $E_{\nu} = 753$ keV for ν_e 's from ⁵¹Cr[18]. As shown in Fig. 4(b), no excess of uncorrelated lone-events was observed in the residual spectrum from the ON – OFF* data. A limit of

$$\tau_{\nu}/m_{\nu} > 0.11 \text{ s/eV}$$

for ν_e at 90% CL was derived. This implies

$$\frac{\tau_1}{m_1} > 0.08 \text{ s/eV}$$

 $\frac{\tau_2}{m_2} > 0.03 \text{ s/eV}$

in the mass eigenstate basis. These direct radiative decay limits apply to all the kinematically allowed decay channels and cover possible anomalous neutrino radiative decay mechanisms in matter, since the decay vertices are within the active detector volume. In particular, the matter-induced radiative decay rates can be enhanced by a huge factor($\sim 10^{23}$) [19] in the minimally-extended model.

Previous accelerator experiments provided the other direct "laboratory" limits on the $\nu_{\rm e}$ magnetic moments and radiative decay rates: $\mu_{\nu} < 1.1 \times 10^{-9} \mu_{\rm B}$ [20] and $\tau_{\nu}/m_{\nu} > 6.4$ s/eV [21], both at 90% CL. The new limits from reactor $\nu_{\rm e}$ are complementary to these more stringent results, since they probe parameter space with lower neutrino energy and denser target density which may favor anomalous matter effects. Astrophysical arguments [22] placed bounds which are orders of magnitude stronger [1], but there are model dependence and implicit assump-



FIG. 4 (color online). Residual plots for neutrino (a) magnetic moment and (b) radiative decay searches with the reactor ⁵¹Cr ν_e -source.



FIG. 5 (color online). Summary of the results on neutrino radiative lifetimes for ν_1 and ν_2 from reactor ν_e and solar neutrinos experiments, denoted by r and s, respectively. The superscripts (I,D) correspond to indirect bounds and direct limits, while the subscript "12" is attributed to decays driven by Δm_{12}^2 , and so on. The upper bound (m_{up}) on m_{ν} is due to limits from direct mass measurements, while the lower bounds m_{lo}^{nor} and m_{lo}^{inv} are valid for the normal and inverted hierarchies, respectively. The indirect bounds r_{13}^{I} and s_{23}^{I} are valid for inverted hierarchies. All modes are valid for decays in vacuum, while r^{D} applies also for decays in matter. Bounds for ν_1 and ν_2 can be represented by the same bands in this scale.

tions on the neutrino properties involved [14]. Limits were also derived from solar neutrinos, through the absence of spectral distortion in the Super-Kamiokande spectra: $\mu_{\nu} < 1.1 \times 10^{-10} \mu_{\rm B}$ [15,23], and the observational limits of solar X- and γ -rays: $\tau_{\nu}/m_{\nu} > 7 \times 10^9$ s/eV [24], both at 90% CL. However, the compositions of the mass eigenstates being probed are different from those due to $\nu_{\rm e}$ flavor eigenstate at the production site studied by the reactor and accelerator-based experiments, such that the interpretations of the limits are not identical.

The limits for the radiative decay lifetimes for mass eigenstates ν_1 and ν_2 from reactor and solar neutrino experiments are summarized and depicted in Fig. 5, using the latest results from the neutrino experiments [2,17] as input. The notations are defined in the figure caption. Several characteristic features can be identified. The solar neutrino experiments lead to tighter limits than those from reactor ν_e 's. The indirect bounds inferred from ν_e -e scatterings are much more stringent than the direct approaches, but only apply to decays in vacuum. Among the various approaches, only the direct limit with reactor ν_e reported in this article covers decays in both vacuum and matter.

III. LOADED POWER REACTOR

A. Enhancement of Neutrino Flux

Using the simulation software discussed above, we investigated the merits of inserting selected materials to the reactor core to enhance the ν_e -flux. A convenient proce-

TABLE V. The (n,γ) and ν_e -yields for selected materials loaded to the reactor core, at $K_{eff} = 1$ and $\xi = 0\%$.

Isotope	IA(%)	$\sigma_{n\gamma}(b)$	$ au_{1/2}$	Q(keV)	BR(%)	$\Delta(\%)$	$\mathbf{Y}_{\mathbf{n}}$	Y_{ν}
⁵⁰ Cr(n) ⁵⁰ Cr(p)	4.35 100	15.8	27.7 d	753	100	14.3 5.4	0.056 0.31	0.056 0.31
⁶³ Cu(n) ⁶³ Cu(p)	69.2 100	4.5	12.7 h	1675	61	16.3 14.8	0.20 0.25	0.12 0.15
$^{151}Eu(n)$ $^{151}Eu(p)$	47.8 100	2800	9.3 h	1920	27	0.073 0.035	0.092 0.095	0.025 0.027

dure is to load them to the unfilled rods or to replace part of the UO_2 fuel elements or control rod assembly during reactor outage. Though such a scenario involves difficulties with reactor operation regulations and requires further radiation safety studies, it is nevertheless technically feasible and ready—and costs much less than the various accelerator neutrino factories projects, which involve conventional neutrino beam upgrades [25], muon storage rings [26] and beta beams [27]. It is therefore of interest to explore the physics potentials and achievable sensitivities.

The candidate isotopes are those with good IA, $\sigma_{n\gamma}$ and BR as well as convenient lifetimes for the activated nuclei. In order to sustain the fission chain reactions (that is, having $K_{eff} = 1$), the control rod fraction ξ in the core should be reduced and there is a maximum amount of the neutron-absorbing materials that can be inserted. This amount as a fraction of the fuel-element mass is denoted by Δ . Several selected materials and their maximal Δ , Y_n and Y_{ν} at $K_{eff} = 1$ and $\xi = 0$ in both natural(n) and pure(p) IA form are given in Table V. The optimal choice is ${}^{50}Cr(p)$. To illustrate how the allowed amount of control rods and source materials would relate to the reactor operation, the variations of K_{eff} and Y_{ν} versus Δ are plotted in Figs. 6(a) and 6(b), at two configurations where the control rod fractions are (a) $\xi = 4\%$ and (b) $\xi = 0\%$, respectively. Criticality condition Keff=1 requires a maximum load of ⁵⁰Cr(p) corresponding to $\Delta = 5.4\%$ when the control rods are completely retrieved ($\xi = 0\%$). This gives rise to a neutrino yield of $Y_{\nu} = 0.31 \nu_e$ /fission, and therefore a $Y_{\nu}/Y_{\bar{\nu}}$ ratio of 0.04. As shown in Table II, the total weight of nonfuel materials inside the containment vessel is 1.14 times that of the fuel elements. Therefore, such loading of ${}^{50}Cr(p)$ is only a small addition of materials to the reactor core. In the case of a $P_{th} = 4.5$ GW reactor, this maximal loading implies 8900 kg of ⁵⁰Cr(p). A total of 4.2×10^{19} of ν_e 's per second are emitted from the core, equivalent to the activity of a 1.1 GCi source. The ν_{e} -flux at 10 m is 3.3×10^{12} cm⁻² s⁻¹.

B. Detection and Potential Applications

In order to detect such neutrinos, detection mechanisms common to both ν_e and $\bar{\nu}_e$ such as neutrino-electron scatterings are not appropriate. Instead, flavor-specific



FIG. 6. The variation of the K_{eff} parameter and the neutrino yield Y_{ν} from ⁵⁰Cr(p) as a function of loading fraction Δ , at control rod fraction (a) $\xi = 4\%$ and (b) $\xi = 0\%$.

charged-current interactions ($\nu_e NCC$) would be ideal. Solar ν_e has been observed by $\nu_e NCC$ in radio-chemical experiments on ³⁷Cl and ⁷¹Ga, with calibration measurements using ⁵¹Cr ν_e -sources performed for ⁷¹Ga [28]. Detection of the low energy solar neutrinos has been a central topic in neutrino physics. There are many detection schemes and intense research program towards counter experiments with $\nu_e NCC$ [29], using isotopes such as ¹⁰⁰Mo, ¹¹⁵In, ¹⁷⁶Yb. The $\nu_e NCC$ rates for the various isotopes in their natural abundance at a ⁵¹Cr ν_e -flux of 3.3×10^{12} cm⁻² s⁻¹ are summarized in Table VI. Also

TABLE VI. Expected $\nu_e \text{NCC}$ rates per ton-year at a reactor ⁵¹Cr ν_e -flux of $3.3 \times 10^{12} \text{ cm}^{-2} \text{s}^{-1}(\text{R}_{\text{core}})$, at the standard solar model ⁷Be flux(R_o), and due to a 1 MCi ⁵¹Cr source(R_{src}).

Target	IA(%)	Threshold(keV)	R _{core}	R_{\odot}	R _{src} ^a
⁷¹ Ga	39.9	236	2100	3.8	58
¹⁰⁰ Mo	9.63	168	2300	3.9	64
¹¹⁵ In	95.7	118	11000	19	300
¹⁷⁶ Yb	12.7	301	3700	7.4	100

^afor four half-lives of data taking

listed for comparison are the rates from the standard solar model ⁷Be ν_e -flux and from a 1 MCi ⁵¹Cr source inside a spherical detector of 1 m diameter. More than 10⁴ ν_e NCC events or 1% statistical accuracy can be achieved by 1 tonyear of data with an indium target. Calculations of the ν_e -flux depends on the amount of loaded materials and the well-modeled reactor neutron spectra, so that a few % uncertainties should be possible. Similar accuracies can be expected on the ν_e NCC cross-section measurements. This would provide important calibration data to complement the solar neutrino program.

Such monoenergetic $\nu_{\rm e}$ -sources and the detection schemes may find applications in other areas of neutrino physics. We outline two of such applications and derive their achievable statistical accuracies. Discussions on the systematic uncertainties and background of actual experiments are beyond the scope of this work, and will largely depend on the results of the ongoing research efforts to develop realistic $\nu_{\rm e}$ NCC-detectors.

The first potential application is on the study of the mixing angle θ_{13} . The monoenergetic ν_e 's allow simple counting experiments to be performed. The rates between NEAR and FAR detectors can be compared to look for possible deviations from $1/L^2$, L being the core-detector distance. The ν_{e} -flux can be accurately measured by the NEAR detectors, and the oscillation amplitude is precisely known at fixed Δm^2 , E_{ν} and L. Therefore, reactor ν_e experiments are expected to have better systematic control than those with fission $\bar{\nu}_{e}$'s [30] where, because of the continuous energy distribution, the energy dependence in the detector response and the oscillation effects have to be taken into account. Considering both oscillation and luminosity effects, the sensitivities at a given neutrino energy E_{ν} depend on $[\sin^2(\frac{\Delta m^2 L}{E_{\nu}})]/\sqrt{L^2}$. The optimal distance for the *FAR* detector at $\Delta m^2 = 0.002 \text{ eV}^2$ and $E_{\nu} = 747 \text{ keV}$ for the ⁵¹Cr-source is therefore $L_0 = 340$ m. Table VII shows the achievable sensitivities to $\sin^2 2\theta_{13}$ with various detector options in both natural(n) and pure(p) IA located at L₀ from a two-core power plant each with $P_{th} = 4.5$ GW. The source strength of $Y_{\nu} =$ $0.31\nu_{\rm e}$ /fission for maximally-loaded ⁵¹Cr in Table V is adopted. It can be seen that a $\sim 1\%$ sensitivity can be

TABLE VII. Sensitivities to θ_{13} from maximally-loaded reactor core with ⁵¹Cr(p) sources for different detector options. Listed are event rates per 500-ton-year(R₅₀₀) for the *FAR* detector at L₀ = 340 m, their achievable 1σ statistical(σ_{500}) and $\sin^2 2\theta_{13}(\delta(\sin^2 2\theta_{13}))$ accuracies.

Target	IA(%)	R ₅₀₀	$\sigma_{500}(\%)$	$\delta(\sin^2 2\theta_{13})$
¹⁰⁰ Mo(n)	9.63	1900	2.3	0.027
100 Mo(p)	100	20000	0.71	0.0083
$^{115}In(n)$	95.7	9100	1.1	0.012
¹⁷⁶ Yb(n)	12.7	3100	1.8	0.021
¹⁷⁶ Yb(p)	100	24000	0.64	0.0075



FIG. 7. Simulated correlations between the fractional changes of $\nu_{\rm e}$ -yields (ΔY_{ν}) and those of 238 U $(n,\gamma)^{239}$ U rates $(\Delta Y_{n\gamma})$ in the case for a 51 Cr source. Conditions under which the error bars are assigned are explained in the text.

statistically achieved with 5 years of data taking using a 100 ton indium target—a level comparable with those of the other reactor- and accelerator-based projects.

Another possibility is on the monitoring of unwarranted plutonium production during reactor operation—an issue of paramount importance in the control of nuclear proliferation [31]. Plutonium is primarily produced by β -decays following ²³⁸U(n, γ)²³⁹U whose cross-section is overwhelmed at high energy (>1 eV) [7]. In contrast, the

 (n, γ) processes in Table V which give rise to $\nu_{\rm e}$ -emissions are predominantly thermal. The core neutron spectra can be modified without affecting the fission rates through optimizations of the control rod and cooling water fractions, making excessive plutonium production undetectable by monitoring the thermal power output alone. Measurements of the time-variations of the ν_e NCC event rates are effective means to probe changes in the neutron spectra, and therefore to monitor directly the ²³⁹Pu accumulation rates. Illustrated in Fig. 7 are the correlations between the fractional changes of the $\nu_{\rm e}$ -yields (ΔY_{ν}) and those of the 238 U (n, γ) 239 U rates ($\Delta Y_{n\gamma}$) in the case for a ⁵¹Cr source having a strength of $Y_{\nu} = 0.31 \nu_e$ /fission. The uncertainties in ΔY_{ν} correspond to those statistically achieved with 19 days of data using a 10-ton indium detector located at 10 m from the reactor core. Such a measurement is adequate to make a 3σ detection on a 4% reduction of the $\nu_{\rm e}$ -flux, which corresponds to a 10% enhancement of the ²³⁹Pu production rate.

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