

Search for $D^0 - \bar{D}^0$ mixing in the Dalitz plot analysis of $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

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The resonant substructure in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ decays is described by a combination of ten quasi two-body intermediate states which include both CP -even and CP -odd eigenstates and one doubly Cabibbo suppressed channel. We present a formalism that connects the variation in D^0 decay time over the Dalitz plot with the mixing parameters, x and y , that describe off-shell and on-shell $D^0 - \bar{D}^0$ mixing. We analyze the CLEO II.V data sample and find the parameters x and y are consistent with zero. We limit $(-4.5 < x < 9.3)\%$ and $(-6.4 < y < 3.6)\%$ at the 95% confidence level.

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The CLEO Collaboration has studied the decay to $K_S^0 \pi^+ \pi^-$ of particles tagged at production as D^0 mesons. The data were obtained at the Cornell Electron Storage Ring. These decays are believed to proceed through two-body intermediate states. Previous studies [1,2] parametrized the $K_S^0 \pi^+ \pi^-$ Dalitz-plot distribution with ten intermediate two-body channels and determined values for the relative amplitudes and phases. The purpose of the present study is to extend the analysis to include in the Dalitz-plot distribution the decays $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ where the \bar{D}^0 has arisen via the time evolution of the state which was tagged as a D^0 at production ($D^0 - \bar{D}^0$ mixing). By measuring the time evolution of the Dalitz plot one can measure, or constrain the values of the standard mixing parameters x and y . This method enables the measurement of x and y separately and for the first time offers a way to measure the sign of x .

Studies of the evolution of a K^0 or B^0 into the respective antiparticle, a \bar{K}^0 or \bar{B}^0 , have guided the form and content

of the standard model and permitted useful estimates of the masses of the charm [3] and top quark [4] prior to their direct observation. A D^0 can evolve into a \bar{D}^0 through on-shell intermediate states, such as $K^+ K^-$ with mass, $m_{K^+ K^-} = m_{D^0}$, or through off-shell intermediate states, such as those that might be present due to new physics. This evolution through the former (latter) states is parametrized by the dimensionless variables $-iy$ (x) defined in Eq. (23).

Many predictions for x in the $D^0 \rightarrow \bar{D}^0$ amplitude have been made [5]. Several nonstandard models predict $|x| > 0.01$. Contributions to x at this level could result from the presence of new particles with masses as high as 100–1000 TeV [6]. The standard model short-distance contribution to x is determined by the box diagram in which two virtual quarks and two virtual W bosons are exchanged. The magnitude of x is determined by the mass and Cabibbo-Kobayashi-Maskawa [7] couplings of the virtual quarks. From the Wolfenstein parametrization [8] where

$\lambda \equiv \sin^2 \theta_C \approx 0.05$, contributions involving b quarks ($\sim \lambda^6$) can be neglected relative to those with d and s quarks ($\sim \lambda^2$). The most prominent remaining amplitude is proportional to $(m_s^2 - m_d^2)/m_W^2$. The near degeneracy on the W mass scale of the d and s quarks results in a particularly effective suppression by the GIM [9] mechanism. A simple estimate of x is obtained by comparing with the Kaon sector;

$$\frac{\Delta M_{D^0}}{\Delta M_{K^0}} = \frac{f_{D^0}(m_s^2 - m_d^2)m_{D^0}}{f_{K^0}(m_c^2 - m_u^2)m_{K^0}}. \quad (1)$$

Assuming $f_{D^0} \approx f_{K^0}$ and taking $m_u = 5$ MeV, $m_d = 9$ MeV, $m_s = 60-170$ MeV, $m_c = 1.2$ GeV and $\Delta M_{K^0} = (3.48 \pm 0.01) \times 10^{-15}$ GeV, and $x = (\Delta M_{D^0}/\Gamma) = 6.31 \times 10^{11} \times \Delta M_{D^0}$ yields, $x = 2 \times 10^{-5} - 2 \times 10^{-4}$. Short-distance contributions to y are expected to be less than x . Both are beyond current experimental sensitivity. Long-distance effects are expected to be larger but are difficult to estimate due to the large number of resonances near the D^0 pole. It is likely that x and y contribute similarly to mixing in the standard model. Decisive signatures of new physics include $|y| \ll |x|$ or type II or type III CP violation [10]. In order to assess the origin of a $D^0 - \bar{D}^0$ mixing signal, the values of both x and y must be measured.

Previous attempts to measure x and y include: the measurement of the wrong sign semileptonic branching ratio $D^0 \rightarrow K \ell \nu$ [11] which is sensitive to the mixing rate $R_M = [(x^2 + y^2)/2]$; decay rates to CP eigenstates $D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$ [12,13] which are sensitive to y ; and the wrong sign $D^0 \rightarrow K^+ \pi^-$ [14-16] hadronic branching ratio which measures $x'^2 = (y \sin \delta_{K\pi} + x \cos \delta_{K\pi})^2$ and $y' = y \cos \delta_{K\pi} - x \sin \delta_{K\pi}$. Here, $\delta_{K\pi}$, which has yet to be measured experimentally, is the relative strong phase between D^0 and \bar{D}^0 to $K^+ \pi^-$. In this study we utilize the fact that the values of x and y can also be determined from the distribution of the $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ Dalitz plot if one measures that distribution as a function of the D^0 decay time. We show that x and y can be separately determined. This is the first demonstration of possible sensitivity to the sign of x . Predictions of the sign of x are sensitive to the details of the treatment of long-distance effects within the standard model as well as the nature of potential new physics contributions.

The time evolution of the $D^0 - \bar{D}^0$ system is described by the Schrödinger equation

$$i \frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}, \quad (2)$$

where the \mathbf{M} and $\mathbf{\Gamma}$ matrices are Hermitian, and CPT invariance requires $M_{11} = M_{22} \equiv M$ and $\Gamma_{11} = \Gamma_{22} \equiv \Gamma$. The off-diagonal elements of these matrices describe the dispersive or long distance and absorptive or short-distance contributions to $D^0 - \bar{D}^0$ mixing.

The two eigenstates D_1 and D_2 of the effective Hamiltonian matrix $(\mathbf{M} - \frac{i}{2} \mathbf{\Gamma})$ are given by

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle, \quad p^2 + q^2 = 1. \quad (3)$$

The corresponding eigenvalues are

$$\lambda_{1,2} \equiv m_{1,2} - \frac{i}{2} \Gamma_{1,2} = \left(M - \frac{i}{2} \Gamma \right) \pm \frac{q}{p} \left(M_{12} - \frac{i}{2} \Gamma_{12} \right), \quad (4)$$

where $m_{1,2}, \Gamma_{1,2}$ are the masses and decay widths and

$$\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{i}{2} \Gamma_{12}^*}{M_{12} - \frac{i}{2} \Gamma_{12}}}. \quad (5)$$

The proper time evolution of the eigenstates of Eq. (2) is

$$|D_{1,2}(t)\rangle = e_{1,2}(t)|D_{1,2}\rangle, \quad e_{1,2}(t) = e^{[-i(m_{1,2} - i\Gamma_{1,2}/2)t]}. \quad (6)$$

A state that is prepared as a flavor eigenstate $|D^0\rangle$ or $|\bar{D}^0\rangle$ at $t = 0$ will evolve according to

$$|D^0(t)\rangle = \frac{1}{2p} [p(e_1(t) + e_2(t))|D^0\rangle + q(e_1(t) - e_2(t))|\bar{D}^0\rangle], \quad (7)$$

$$|\bar{D}^0(t)\rangle = \frac{1}{2q} [p(e_1(t) - e_2(t))|D^0\rangle + q(e_1(t) + e_2(t))|\bar{D}^0\rangle]. \quad (8)$$

We parametrize the $K_S^0 \pi^+ \pi^-$ Dalitz plot following the methodology described in Refs. [17,18] using the same sign convention as Refs. [1,2,19]. Now, however, we generalize to the case where the time-dependent state is a mixture of D^0 and \bar{D}^0 so the Dalitz-plot distribution depends also on x and y . We express the amplitude for D^0 to decay via the j th quasi-two-body state as $a_j e^{i\delta_j} \mathcal{A}_k^j$ where $\mathcal{A}_k^j = \mathcal{A}_k^j(m_{K_S^0 \pi^-}^2, m_{\pi^+ \pi^-}^2)$ is the Breit-Wigner amplitude for resonance j with spin k described in Ref. [18]. We denote the CP conjugate amplitudes for \bar{D}^0 as $\bar{\mathcal{A}}_k^j = \bar{\mathcal{A}}_k^j(m_{K_S^0 \pi^+}^2, m_{\pi^+ \pi^-}^2)$.

We begin our search for $D^0 - \bar{D}^0$ mixing in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ from the results of our standard fit in Ref. [1] which clearly observed the ten modes [$K^{*-} \pi^+$, $K_0^*(1430)^- \pi^+$, $K_2^*(1430)^- \pi^+$, $K^*(1680)^- \pi^+$, $K_S^0 \rho$, $K_S^0 \omega$, $K_S^0 f_0(980)$, $K_S^0 f_2(1270)$, $K_S^0 f_0(1370)$, and the ‘‘wrong sign’’ $K^{*+} \pi^-$] plus a small nonresonant component.

The decay rate to $K_S^0 \pi^+ \pi^-$ with $(m_{K_S^0 \pi^-}^2, m_{\pi^+ \pi^-}^2)$ at time t of a particle tagged as $|D^0\rangle$ at $t = 0$ is

$$d\Gamma(m_{K\pi}^2, m_{\pi\pi}^2, t) = \frac{1}{256\pi^3 M^3} |\mathcal{M}|^2 dm_{K\pi}^2 dm_{\pi\pi}^2, \quad (9)$$

where the matrix element is defined as $\mathcal{M} = \langle f | \mathcal{H} | i \rangle$. We

evaluate $|\mathcal{M}|^2$ where $|i\rangle$ is given by Eq. (7), and $\langle f| = \langle K_S^0 \pi^+ \pi^- (m_{K_S^0 \pi^-}^2, m_{\pi^+ \pi^-}^2) |$.

The decay channels can be collected into those which are CP even or CP odd (with amplitudes A_+ or A_-) and to those which are D^0 or \bar{D}^0 flavor eigenstates (with amplitudes A_f or \bar{A}_f);

$$\langle f | \mathcal{H} | D_{+,-} \rangle = \sum a_j e^{i\delta_j} \mathcal{A}_{k=\text{even,odd}}^j = p A_{+,-} \quad (10)$$

$$\langle \bar{f} | \mathcal{H} | D_{+,-} \rangle = \sum a_j e^{i\delta_j} \bar{\mathcal{A}}_{k=\text{even,odd}}^j = q \bar{A}_{+,-} \quad (11)$$

$$\langle f | \mathcal{H} | D_f^0 \rangle = \sum a_j e^{i\delta_j} \mathcal{A}_k^j = A_f \quad (12)$$

$$\langle \bar{f} | \mathcal{H} | \bar{D}_f^0 \rangle = \sum \bar{a}_j e^{i\delta_j} \bar{\mathcal{A}}_k^j = \bar{A}_f. \quad (13)$$

Dalitz-plot analyses are sensitive only to relative phases and amplitudes. As in Ref. [1], we fix $a_\rho = 1$, $\delta_\rho = 0$ and assume $a_j = \bar{a}_j$, $\delta_j = \bar{\delta}_j$. In Ref. [2], we considered CP violation more generally and allowed $a_j \neq \bar{a}_j$, $\delta_j \neq \bar{\delta}_j$.

Collecting terms with similar time dependence we find

$$\begin{aligned} \langle f | \mathcal{H} | D^0(t) \rangle &= \frac{1}{2p} (\langle f | \mathcal{H} | D_1(t) \rangle + \langle f | \mathcal{H} | D_2(t) \rangle) \\ &= \frac{1}{2p} (\langle f | \mathcal{H} | (pD^0 + q\bar{D}^0) e_1(t) + \langle f | \mathcal{H} | (pD^0 - q\bar{D}^0) e_2(t) \rangle) \\ &= \frac{1}{2p} ([p(A_f + A_+) + q(\bar{A}_f + \bar{A}_+)] e_1(t) + [p(A_f + A_-) - q(\bar{A}_f + \bar{A}_-)] e_2(t)) \\ &= \frac{1}{2} [(1 + \chi_f) A_f + (1 + \chi_+) A_+] e_1(t) + \frac{1}{2} [(1 - \chi_f) A_f + (1 - \chi_-) A_-] e_2(t) \\ &\equiv e_1(t) A_1 + e_2(t) A_2 \end{aligned} \quad (14)$$

$$\begin{aligned} \langle \bar{f} | \mathcal{H} | \bar{D}^0(t) \rangle &= \frac{1}{2q} (\langle \bar{f} | \mathcal{H} | D_1(t) \rangle - \langle \bar{f} | \mathcal{H} | D_2(t) \rangle) \\ &= \frac{1}{2} [(\chi_f^{-1} + 1) \bar{A}_f + (\chi_+^{-1} + 1) \bar{A}_+] e_1(t) - \frac{1}{2} [(\chi_f^{-1} - 1) \bar{A}_f + (\chi_-^{-1} - 1) \bar{A}_-] e_2(t) \\ &\equiv e_1(t) \bar{A}_1 + e_2(t) \bar{A}_2, \end{aligned} \quad (15)$$

for D^0 and \bar{D}^0 , respectively. Similar to Ref. [20],

$$\chi_f = \frac{q \bar{A}_f}{p A_f} = \left| \frac{\bar{A}_f}{A_f} \right| \frac{1 - \epsilon}{1 + \epsilon} e^{i(\delta + \phi)}, \quad (16)$$

$$\chi_{\bar{f}} = \frac{q \bar{A}_{\bar{f}}}{p A_{\bar{f}}} = \left| \frac{\bar{A}_{\bar{f}}}{A_{\bar{f}}} \right| \frac{1 - \epsilon}{1 + \epsilon} e^{-i(\delta - \phi)}, \quad (17)$$

$$\chi_\pm = \pm \frac{q \bar{A}_\pm}{p A_\pm} = \pm \frac{1 - \epsilon}{1 + \epsilon} e^{\pm i\phi}, \quad (18)$$

where δ is the relative strong phase between D^0 and \bar{D}^0 to $K_S^0 \pi^+ \pi^-$, and in the limit of CP conservation, the real CP -violating parameters, ϵ and ϕ , are zero. Squaring the amplitude and factoring out the time dependence yields

$$\begin{aligned} |\mathcal{M}|^2 &= |e_1(t)|^2 |A_1|^2 + |e_2(t)|^2 |A_2|^2 \\ &\quad + 2\Re[e_1(t) e_2^*(t) A_1 A_2^*]. \end{aligned} \quad (19)$$

$$\begin{aligned} |\bar{\mathcal{M}}|^2 &= |e_1(t)|^2 |\bar{A}_1|^2 + |e_2(t)|^2 |\bar{A}_2|^2 \\ &\quad + 2\Re[e_1(t) e_2^*(t) \bar{A}_1 \bar{A}_2^*]. \end{aligned} \quad (20)$$

The time-dependent terms are given explicitly by

$$\begin{aligned} |e_{1,2}(t)|^2 &= \exp(2\Im(\lambda_{1,2})t) = \exp(-\Gamma_{1,2}t) \\ &= \exp(-\Gamma(1 \pm y)t), \end{aligned} \quad (21)$$

$$\begin{aligned} e_1(t) e_2(t)^* &= \exp(-i\lambda_1 t) \exp(+i\lambda_2 t) \\ &= \exp(-\Gamma(1 + ix)t), \end{aligned} \quad (22)$$

where

$$\Gamma = \frac{\Gamma_1 + \Gamma_2}{2}, \quad x = \frac{m_1 - m_2}{\Gamma}, \quad y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}. \quad (23)$$

Experimentally, y modifies the lifetime of certain contributions to the Dalitz plot while x introduces a sinusoidal rate variation.

This analysis uses an integrated luminosity of 9.0 fb^{-1} of e^+e^- collisions at $\sqrt{s} \approx 10 \text{ GeV}$ provided by the Cornell Electron Storage Ring (CESR). The data were taken with the CLEO II.V detector [21]. The event selection is identical to that used in our previous study of $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ [1,2] which did not consider $D^0 - \bar{D}^0$ mixing. We reconstruct candidates for the decay sequence $D^{*+} \rightarrow \pi_S^+ D^0$, $D^0 \rightarrow K_S^0 \pi^+ \pi^-$. The charge of the slow pion (π_S^+ or π_S^-) identifies the initial charm state as either D^0 or \bar{D}^0 .

The detector resolution in the Dalitz-plot parameters $m_{K\pi}^2$ and $m_{\pi\pi}^2$ is small relative to the intrinsic widths of intermediate resonances; the exception is the decay channel $D^0 \rightarrow K_S^0 \omega, \omega \rightarrow \pi^+ \pi^-$. We reconstruct the D^0 decay time t as described in Ref. [14].

The uncertainty in t , σ_t , is typically 200 fs or $0.5/\Gamma$ and cannot be neglected. We fit the unbinned decay time distribution by analytically convolving the exponentials in each term in Eqs. (19) and (20) by resolution functions similar to, but slightly modified from, that used in Refs. [12,22]. We use one function assuming the event is signal and another assuming the event is background. For the signal events the resolution function is the sum of two Gaussians. One Gaussian is designed to represent the effect of mistakes in the calculation of the event-by-event proper time error σ_t which are common to all events—for example, imperfect material description of the detector during track fitting. The width of this Gaussian is $\sigma_t \times S_{\text{sig}}$ where σ_t is the calculated error for that event and S_{sig} is a scale factor to be determined by the fit.

For the other Gaussian, the measured proper time errors are ignored and the width $\sigma_{\text{mis sig}}$ and the normalization $f_{\text{mis sig}}$ are fit for directly. This Gaussian models the “MIS-measured SIGNAL” proper time resolution when the measured σ_t is *not* correct, as would be the case for hard multiple scattering of one or more of the D meson daughters. The sum of these two components to the likelihood is normalized by the total signal fraction f_{sig} . Note that if we understand our detector well, we will find that the scale factor used in the first Gaussian is close to unity and the fraction of the signal in the second Gaussian is near zero.

The treatment of the background is similar to that of the signal. The total background likelihood is normalized by the background fraction, which is $(1 - f_{\text{sig}})$. We consider two types of background: background with zero lifetime and background with nonzero lifetime τ_{BG} normalized by $f_{\tau_{\text{BG}}}$. We constrain both backgrounds to have the same resolution function. The model for the resolution function is two Gaussians, with core width σ_{BG} , misreconstructed width $\sigma_{\text{mis BG}}$ and the background fraction $f_{\text{mis BG}}$ in the wider Gaussian.

We perform an unbinned maximum likelihood fit to the Dalitz plot which minimizes the function \mathcal{F} given below

$$\mathcal{F} = \sum_{D^0} -2 \ln \mathcal{L} + \sum_{\bar{D}^0} -2 \ln \bar{\mathcal{L}}, \quad (24)$$

where \mathcal{L} and $\bar{\mathcal{L}}$ are defined as in Ref. [2] using \mathcal{M} and $\bar{\mathcal{M}}$ as defined in Eqs. (19) and (20) convolved with the resolution function described above. Simplified Monte Carlo studies indicate that our fit procedure is unbiased and the statistical errors as determined by the fit are accurate.

Our standard fit to the data, described above, is referred to as fit A. Fit B is identical to fit A except CP conservation ($\epsilon = 0, \phi = 0$) is assumed. The D^0 and \bar{D}^0 subsamples are

TABLE I. Results of the Dalitz plot vs decay time fit of the $D^0 \rightarrow K_S^0 \pi^+ \pi^-$. Fit A allows both $D^0 - \bar{D}^0$ mixing and CP violation. Fit B is the CP -conserving fit, $\epsilon = 0$ and $\phi = 0$. Fit C1 (C2) is the fit to the D^0 (\bar{D}^0) subsample. The errors shown for fit A and fit B are statistical, experimental systematic and modeling systematic, respectively, and the 95% confidence intervals *include* systematic uncertainty. The errors for fit C1 and fit C2 are statistical only.

Parameter	Best fit	1-Dimensional 95% C.L.
Fit A		
Most general fit		
x (%)	$2.3^{+3.5}_{-3.4} \pm 0.4 \pm 0.4$	(-4.5:9.3)
y (%)	$-1.5^{+2.5}_{-2.4} \pm 0.8 \pm 0.4$	(-6.4:3.6)
ϵ (%)	$1.1 \pm 0.7 \pm 0.4 \pm 0.2$	(-0.4:2.4)
ϕ (°)	$5.7 \pm 2.8 \pm 0.4 \pm 1.2$	(-0.3:11.7)
Fit B		
CP -conserving fit		
x (%)	$1.8^{+3.4}_{-3.2} \pm 0.4 \pm 0.4$	(-4.7:8.6)
y (%)	$-1.4^{+2.5}_{-2.4} \pm 0.8 \pm 0.4$	(-6.3:3.7)
Fit C1		
D^0 subsample		
x (%)	$3.3^{+5.0}_{-4.8}$	(-6.1:13.5)
y (%)	$-2.8^{+3.6}_{-3.7}$	(-10.2:4.2)
Fit C2		
\bar{D}^0 subsample		
x (%)	$0.6^{+5.7}_{-8.6}$	(-16.0:11.5)
y (%)	$-0.3^{+6.9}_{-3.1}$	(-6.6:13.0)

fit independently in fit C1 and fit C2, respectively. Fit C1 and fit C2 are identical to fit B.

Fit A has 35 free parameters; ten resonances and the nonresonant contribution correspond to ten relative amplitudes and ten relative phases, signal fraction and mis-tag fraction, four signal decay time parameters, five background decay time parameters, two mixing parameters and two CP -violating parameters. The results for x , y , ϵ , and ϕ are in Table I and are consistent with the absence of both $D^0 - \bar{D}^0$ mixing and CP violation. The one-dimensional, 95% confidence intervals are determined by an increase in negative log likelihood ($-2 \ln \mathcal{L}$) of 3.84 units. All other fit variables are allowed to vary to distinct, best-fit values. The amplitude and phase, a_j and δ_j , for all fits in Table I, are consistent with our “no mixing” result [1]. The projection of the results of fit A onto the D^0 decay time is shown in Fig. 1.

We find the parameters describing the signal decay time, $f_{\text{sig}} = (97.1 \pm 0.8)\%$, $\tau_{\text{sig}} = 402 \pm 8$ fs, $S_{\text{sig}} = 1.13 \pm 0.02$, $\sigma_{\text{mis sig}} = 730 \pm 149$ fs, $(1 - f_{\text{mis sig}}) = (96.9 \pm 1.5)\%$ and the parameters describing the background time, $f_{\tau_{\text{BG}}} = (100^{+0}_{-89})\%$, $\tau_{\text{bg}} = 95 \pm 75$ fs, $(1 - f_{\text{mis BG}}) = (86 \pm 11)\%$, $\sigma_{\text{BG}} = 194 \pm 40$ fs, $\sigma_{\text{mis BG}} = 1116 \pm 307$ fs. The scale factor S_{sig} , although not consistent with unity, is comparable to results from other CLEO lifetime analyses which include Refs. [12,14,22].

We evaluate a contour in the two-dimensional plane of y versus x that contains the true value of x and y at 95%

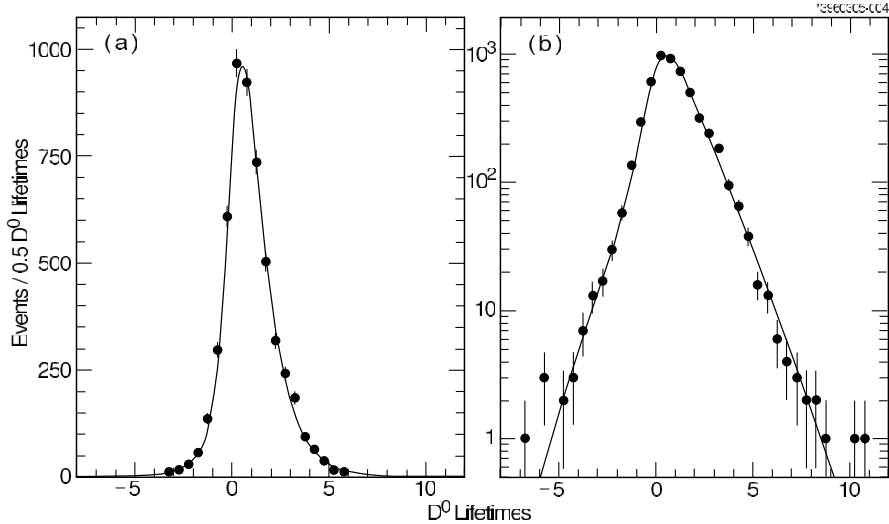


FIG. 1. Projection of the results of fit A onto the D^0 decay time with (a) linear and (b) logarithmic vertical scale.

confidence level (C.L.) without assumption regarding the relative strong phase between D^0 and $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$. We

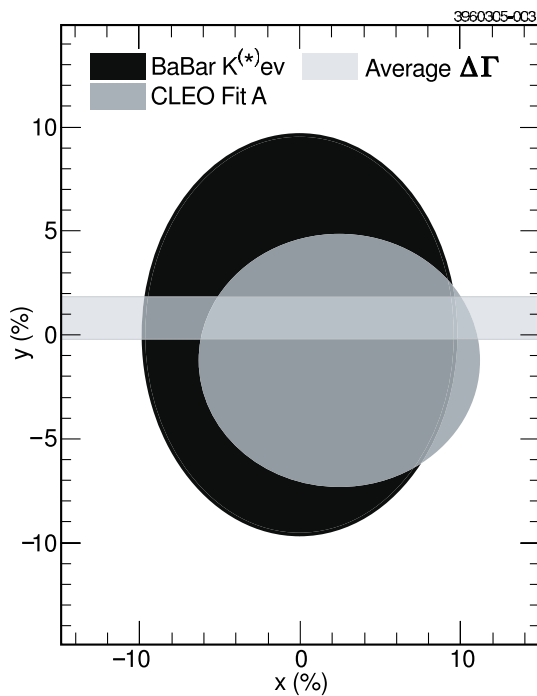


FIG. 2 (color online). Allowed regions in the plane of y versus x . No assumption is made regarding $\delta_{K_S^0 \pi^+ \pi^-}$. The two-dimensional 95% allowed regions from our fit A (light shaded region) is shown. The allowed region for $\Delta\Gamma$ is the average of the y_{CP} [12,13] results. Also shown is the limit from $D^0 \rightarrow K^{(*)} \ell \nu$ from *BABAR* [11]. All results are consistent with the absence of mixing. The limits from *CLEO* [14] and *BABAR* [15] from $D \rightarrow K\pi$ have similar sensitivity to fit A. The 95% allowed regions (not shown) are circles of radius 5.8% and 5.7%, respectively, when assumptions regarding $\delta_{K\pi}$ are removed. The 95% allowed region from *Belle* [16] also from $D \rightarrow K\pi$ is more restrictive—a circle of radius 3.0%.

determine the contour around our best-fit values where the $-2 \ln \mathcal{L}$ has increased by 5.99 units. All fit variables other than x and y are allowed to vary to distinct, best-fit values at each point on the contour. The contour for fit A is shown in Fig. 2. On the axes of x and y , these contours fall slightly outside the one-dimensional intervals listed in Table I, as expected. The maximum excursion of the contour of fit A from the origin corresponds to a 95% C.L. limit on the mixing rate of $R_M < 0.63\%$.

We take the sample variance of x , y , ϵ and ϕ from the nominal result compared to the results in the series of fits described below as a measure of the experimental systematic and modeling systematic uncertainty.

We consider systematic uncertainties from experimental sources and from the decay model separately. Our general procedure is to change some aspect of our fit and interpret the change in the values of the mixing and CP -violating parameters in the nonstandard fit relative to our nominal fit as an estimate of the systematic uncertainty. Contributions to the experimental systematic uncertainties arise from our model of the background, the efficiency, the event selection criteria, and biases due to experimental resolution as described in Ref. [1]. Additionally, we vary aspects of the decay time parametrization. To estimate the systematic uncertainty regarding the $u\bar{u}$, $d\bar{d}$, $s\bar{s}$ content of the background, we perform fits where the background is forced to be all zero lifetime and all nonzero lifetime. We consider a single or a triple rather than a double Gaussian to model the decay time resolution of the signal and background. We also vary by $\pm 1\sigma$ the fraction of misreconstructed signal $f_{\text{mis sig}}$. Finally, we set the scale factor for the measured proper time errors S_{sig} to unity. Variation in the event selection criteria are the largest contribution to the experiment systematic error.

Contributions to the theoretical systematic uncertainties arise from our choices for the decay model for

$D^0 \rightarrow K_S^0 \pi^+ \pi^-$ as described in Ref. [1]. We also consider the uncertainty arising from our choice of resonances included in the fit. To study the stability of our results with other choices of resonances, we performed fits which included additional resonances to the ones in our standard fit. We compared the result of our nominal fit to a series of fits where each of the resonances, σ or $f_0(600)$ and $f_0(1500)$ which are CP even, and $\rho(1450)$ and $\rho(1700)$ which are CP odd were included one at a time. In the standard fit we enumerate the nonresonant component with the K^* resonances. We also considered fits where the nonresonant component was considered to be CP even or CP odd. Finally, we consider a fit that includes doubly Cabibbo suppressed contributions from $K_0(1430)$, $K_2(1430)$, and $K^*(1680)$ constrained to have the same amplitude and phase relative to the corresponding Cabibbo favored amplitude as the $K^*(892)$. There is no single dominant contribution to the modeling systematic error.

In conclusion, we have analyzed the time dependence of the three-body decay $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ and exploited the interference between intermediate states to limit the mixing parameters x and y without sign or phase ambiguity. Our data are consistent with an absence of both $D^0 - \bar{D}^0$ mixing and CP violation. The two-dimensional limit in the mixing parameters, x versus y , is similar to previous results obtained from the same data sample [14], when assumptions regarding $\delta_{K\pi}$ are removed. We limit $(-4.5 < x < 9.3)\%$ and $(-6.4 < y < 3.6)\%$, at the 95% C.L. without assumptions regarding CP -violating parameters. We limit the CP -violating parameters $(-0.4 < \epsilon < 2.4)\%$ and $(-0.3 < \phi < 11.7)^\circ$ at the 95% C.L.

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