Implications of a massless neutralino for neutrino physics

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(Received 13 December 2002; revised manuscript received 1 August 2003; published 28 October 2003)

We consider the phenomenological implications of a soft supersymmetry (SUSY) breaking term $\tilde{B}N$ at the TeV scale [here \tilde{B} is the U(1)_Y gaugino and N is the right-handed neutrino field]. In models with a massless (or nearly massless) neutralino, such a term will give rise through the seesaw mechanism to new contributions to the mass matrix of the light neutrinos. We treat the massless neutralino as an (almost) sterile neutrino and find that its mass depends on the square of the soft SUSY breaking scale, with interesting consequences for neutrino physics. We also show that, although it requires finetuning, a massless neutralino in the minimal supersymmetric standard model or next-to-minimal supersymmetric standard model is not experimentally excluded. The implications of this scenario for neutrino physics are discussed.

DOI: 10.1103/PhysRevD.68.073004

PACS number(s): 14.60.Pq, 12.60.Jv

I. INTRODUCTION

The atmospheric neutrino data [1] give convincing evidence of nonzero neutrino masses. These data also imply maximal or close to maximal mixing of muon and tau neutrinos. Furthermore, the solar neutrino data [2] can also be naturally explained by a nonzero mass splitting and mixing between the electron and muon neutrino. Recent data favor large mixing in this sector as well.

The questions which arise then are what is the physics behind the neutrino masses and mixing patterns? What is the mechanism of neutrino mass generation? Why is the lepton mixing large, in contrast to the small mixing in the quark sector? These are among the most challenging problems of fundamental physics today.

Many mechanisms for neutrino mass generation have been suggested so far. Among these, the seesaw mechanism [3] seems to be the simplest and most natural. In this context, large neutrino mixing can appear due to large mixing in the charged lepton mass matrix [4] or in the Dirac mass matrix of neutrinos [5]. It can also appear from large mixing or very strong hierarchy in the Majorana mass matrix of the righthanded neutrinos [6]. Large mixing in the lepton sector can also be obtained by radiative corrections due to renormalization group effects in schemes with quasidegenerate neutrinos [7]. Also, noncanonical (type II) seesaw models are good candidates for generating large mixing in the neutrino sector [8].

Models with three light neutrinos can explain the solar and atmospheric neutrino oscillation data, and also the results of all laboratory neutrino experiments, with the exception of the Liquid Scintillator Neutrino Detector (LSND) [9]. The explanation of the LSND experimental results requires either a fourth light neutrino [10,11] (which, to satisfy the constraints coming from Z physics, has to be sterile), or violation of CPT in the neutrino sector [12]. In this later case, the neutrino and antineutrino masses can be different, thus providing an elegant solution to the LSND question. However, violation of CPT may be hard to accommodate theoretically. In the sterile neutrino case, one of the problems is that there is no compelling reason for the existence of such a particle. Also, even if the sterile neutrino is introduced by hand, it is hard to find a reason why it is so light, with mass of the order 1 eV, as required to explain LSND.

In this work we propose a scenario in which the sterile neutrino is an essentially massless (mass of order eV or less) *B*-ino. It can be shown that, in the framework of the general minimal supersymmetric standard model (MSSM), such a massless neutralino is still allowed experimentally. In order to couple this neutralino to the neutrino sector, we consider a new soft supersymmetry (SUSY) breaking term of the form $c\tilde{B}N$, where *N* is the right-handed neutrino and *c* is a soft SUSY breaking mass parameter. This coupling will give the *B*-ino mass through the seesaw mechanism: $m_{\nu_0} \sim c^2/M_M$, thereby relating the mass of the sterile neutrino to the soft SUSY breaking scale. Moreover, the seesaw induced couplings of this *B*-ino with the three SM neutrinos naturally leads to large mixing between the three active families.

The paper is organized as follows. In Sec. II we show how a massless neutralino can become the sterile neutrino. We also discuss the connection between the neutrino mass and the SUSY breaking scale, and how large mixing arises naturally in this model. In Sec. III we formulate and review the conditions under which the lightest neutralino can be massless [both in MSSM and in next-to-minimal supersymmetric standard model (NMSSM)], and satisfy all the existing experimental constraints. A new U(1)_R symmetry is introduced in order to allow the *B*-ino-neutrino (or singlino-neutrino, in NMSSM) couplings, while forbidding all the usual *R*-parity violating (RPV) terms. In Sec. IV we consider the implications of our model for neutrino phenomenology in somewhat more detail. Conclusions are summarized in Sec. V.

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II. SEESAW MECHANISM AND THE MASSLESS NEUTRALINO

In this section we will assume the existence of a massless neutralino, leaving the justification for this assumption for later. This neutralino can be thought of as a superposition of higgsino and gaugino states. In the next section we will see that in the MSSM it has to be mostly *B*-ino in order to satisfy the existing experimental constraints.

Let us consider scenarios under which mixing between this state and the three SM neutrinos can arise. The first possibility is direct mixing: the higgsino states can couple to the neutrinos through bilinear RPV couplings μ_i ; we will not study this scenario here. We shall consider the more interesting case when the mixing with the three SM neutrinos is obtained through coupling of the massless neutralino to the right-handed neutrino and the seesaw mechanism.

We take the right-handed neutrino fields N_i to be singlets under the SU(2)_L×U(1)_Y gauge group. Then they can couple only with the *B*-ino component of the massless neutralino, and to SU(2)_L×U(1)_Y singlet components of the neutralino, if present. The corresponding bilinear couplings to the *B*-ino:

$$\tilde{B}N_i$$
 (1)

have dimension three, and are therefore soft SUSY breaking terms [13]. The coefficients with which these terms appear in the Lagrangian (let us call them c_i) will have dimensions of mass, and their magnitude is expected to be of the order of SUSY breaking scale, that is, $\mathcal{O}(\text{TeV})$.

The Lagrangian for the neutrino sector of our model will then be

$$L = (m_D)_{ij} \bar{\nu}_i N_j + (M_M)_{ij} N_i N_j + c_i N_i \chi_0 + \text{H.c.}, \quad (2)$$

where m_D and M_M are the Dirac and Majorana mass matrices for the three SM neutrinos, and χ_0 is the massless neutralino. We treat the massless neutralino as an (almost) sterile neutrino. Upon decoupling the heavy neutrino states (through the seesaw approximation) the mass matrix for the remaining four light neutrinos takes the form

$$M_{\nu} = \begin{pmatrix} c M_{M}^{-1} c^{T} & c M_{M}^{-1} m_{D}^{T} \\ m_{D} M_{M}^{-1} c^{T} & m_{D} M_{M}^{-1} m_{D}^{T} \end{pmatrix},$$
(3)

where the first line corresponds to the sterile neutrino.

For simplicity of presentation let us assume in the following that the right-handed neutrino mass matrix is diagonal and proportional to the identity matrix: $(M_M)_{ij} = m_M \delta_{ij}$. It can easily be seen then that the 4-neutrino mass matrix above has a zero eigenvalue, two eigenvalues of order m_D^2/m_M , and one eigenvalue of order $(c^2 + m_D^2)/m_M$. The first three eigenvectors can be identified with the three SM neutrino mass eigenstates. The fourth eigenvector (which is mostly χ_0) can be identified with the sterile neutrino.

Note that, since the magnitude of the *c* terms is of the order of soft SUSY breaking scale, they are naturally about ten times larger than the Dirac mass terms appearing in m_D

[which are of the order of the electroweak breaking scale, i.e., $\mathcal{O}(100 \text{ GeV})$]. This means that the mass of the sterile neutrino will be about two orders of magnitude above the mass of the heavier SM neutrino, which, to account for the atmospheric neutrino data, has to be of the order of 5 $\times 10^{-2}$ eV. This makes the mass of the sterile neutrino of eV size, which is the right value to explain the LSND experiment results. Moreover, we will show in Sec. IV that Eq. (3) predicts the right value of mixing between the sterile and active neutrinos as well.

Notwithstanding the LSND experiment, the mass matrix in Eq. (3) with $|c| \ge |m_D|$ naturally gives large mixing between the three light neutrinos. To see this we can decouple the sterile neutrino from the other three by using the seesaw approximation, and the mass matrix becomes

$$M_{\nu}' = \frac{1}{m_M} \begin{pmatrix} cc^T & 0 \\ 0 & (m_D m_D^T)_{ij} - \frac{(cm_D^T)_i (cm_D^T)_j}{cc^T} \end{pmatrix}.$$
 (4)

From this expression it can be seen that even if m_D is diagonal, we get off-diagonal entries of the same magnitude as the diagonal elements in the three SM neutrino mass matrix. This means that at least one mixing angle is large. Of course, in order to obtain the specific pattern of two large mixing angles and a small one, further conditions must be imposed. We will study this further in Sec. IV.

We end this section with some comments. Above, we have assumed that the sterile neutrino is a massless neutralino. This does not necessarily have to be so. What is needed for the above seesaw scenario to work is a massless fermion, which is (or contains among its components) a singlet under the $SU(2)_L \times U(1)_Y$ gauge group. Then, this fermion can couple with the right-handed neutrinos through the soft SUSY breaking terms (1), and the mechanism presented above works. In the next section we will actually consider the case when the sterile neutrino is the NMSSM singlino. Some other SUSY particles (like a Goldstino, which has the advantage of being naturally massless) can also play this role.

III. MASSLESS NEUTRALINO

In this section we will explore the possibility that supersymmetry allows the existence of a nearly massless neutralino. For the MSSM and the NMSSM, we show that a massless neutralino can be obtained by a finetuning of the soft breaking parameters. While we do not provide a reason for such a tuning, we do verify that the resulting massless neutralino is not yet excluded by experiment. By extending the visible sector particle content beyond that of the MSSM or NMSSM, it may be possible to achieve TeV scale visible sector SUSY breaking in a phenomenologically viable way. In such a case the lightest neutralino can be the Goldstino and thus naturally massless, up to supergravity corrections of order TeV²/ $M_{\text{Planck}} \sim 10^{-4}$ eV. This is an interesting direction for further study.

In this section we will explore the possibility that supersymmetry allows the existence of a massless neutralino. Note that we will not try to give a reason why there should be such a particle (at this point, we do not know), but we will just simply verify that the existence of a massless neutralino is compatible with the experimental results from SUSY

$$M_{ij} = \begin{pmatrix} -M_1 & 0 \\ 0 & -M_2 \\ -m_z \cos\beta\sin\theta_w & m_z\cos\beta\cos\theta_w \\ m_z \sin\beta\sin\theta_w & -m_z\sin\beta\cos\theta_w \end{pmatrix}$$

where M_1 and M_2 are the soft SUSY breaking mass terms for the U(1)_Y and SU(2)_w gaugino fields, m_z is the mass of the Z boson, tan $\beta \equiv v_1/v_2$, and μ is the Higgs boson mixing term.

The existence of a massless neutralino requires that the determinant of the mass matrix in Eq. (5) be zero:

$$\Delta_0 \equiv \mu m_z^2 \sin 2\beta (M_1 \cos^2 \theta_w + M_2 \sin^2 \theta_w) - \mu^2 M_1 M_2 = 0.$$
(6)

Most studies of the MSSM have been performed with the assumption of universal gaugino masses, where M_1 and M_2 are related by the Grand Unified Theory (GUT) relation:

$$M_2 = \frac{5}{3} \tan^2 \theta_W M_1. \tag{7}$$

In this framework, Eq. (6) requires that

$$\mu M_2 = \frac{m_z^2}{r} \sin 2\beta (r \cos^2 \theta_w + \sin^2 \theta_w) \tag{8}$$

with $r=M_1/M_2\approx 0.5$, which implies either that both μ and M_2 are of order m_z , or one of these parameters is much smaller than m_z . However, since μ and m_2 are responsible for the masses of the other neutralinos, as well as for the masses of the charginos, this can bring us into conflict with direct searches for these particles at LEP. A detailed analysis [15] shows that a massless neutralino is excluded in the MSSM with the GUT relation (7), except for a narrow region in the parameter space, where tan $\beta \approx 1$. However, this value for tan β is excluded from other considerations.

searches. We shall consider two SUSY models, first the MSSM, and then the NMSSM, which contains an extra singlet.

A. MSSM case

In the MSSM we have the following mass matrix for neutralinos:

$$\begin{array}{c} -m_z \cos\beta\sin\theta_w & m_z \sin\beta\sin\theta_w \\ m_z \cos\beta\cos\theta_w & -m_z \sin\beta\cos\theta_w \\ 0 & -\mu \\ -\mu & 0 \end{array} \right), \tag{5}$$

In the search for a massless neutralino we are therefore led to give up the assumption of universal gaugino masses. Then, values for the M_1 parameter

$$M_1 = \frac{M_2 m_z^2 \sin 2\beta \sin^2 \theta_w}{\mu M_2 - m_z^2 \sin 2\beta \cos^2 \theta_w} \simeq \frac{m_z^2}{\mu} \sin 2\beta \sin^2 \theta_w \quad (9)$$

of order of a few GeV (or even smaller, for large $\tan \beta$), can satisfy Eq. (6). M_2 and μ can be chosen sufficiently large to satisfy the constraints coming from Z decay to $\chi^+\chi^-$ and $\chi_i^0\chi_j^0$, with *i* and *j* not 1 at the same time. One more constraint we have to consider comes from the massless neutralino, which will give contribution to the invisible Z width. The current experimental [16] value

$$\Gamma_7^{inv} = 499.0 \pm 1.5 \text{ MeV}$$
 (10)

requires that the branching ratio of Z to the massless neutralino pair be smaller than about 0.3%:

$$Br(Z \to \chi_1^0 \chi_1^0) < 3 \times 10^{-3}.$$
 (11)

In order to figure out this branching ratio, we need to evaluate the particle content of the lightest neutralino and its interactions. If we define the mass eigenstates of the neutralino matrix by

 $\chi_i^0 = N_{ij}\psi_j \quad \text{where} \quad \psi_j = \{\tilde{B}, \tilde{W}^3, \tilde{h}^0, \tilde{h}'^0\}, \qquad (12)$

then

$$N_{1i} = \left(1, \frac{m_z^2 \sin 2\beta \sin 2\theta_W/2}{m_z^2 \sin 2\beta \cos^2 \theta_W - \mu M_2}, -\frac{m_z M_2 \sin \beta \sin \theta_W}{m_z^2 \sin 2\beta \cos^2 \theta_W - \mu M_2}, \frac{m_z M_2 \cos \beta \sin \theta_W}{m_z^2 \sin 2\beta \cos^2 \theta_W - \mu M_2}\right)$$
(13)

up to a normalization constant. If $\mu \gg m_z$, that normalization constant is 1, and the massless neutralino is mostly *B*-ino. The interaction Lagrangian with the *Z* boson in terms of physical states is the following [14]:

$$\mathcal{L}_{Z\chi_i\chi_j} = \left(\frac{g}{2\cos\theta_w}\right) Z_\mu \bar{\chi}_i \gamma^\mu (O_{ij}^L P_L + O_{ij}^R, P_R) \chi_j, \quad (14)$$

where

$$O_{ij}^{L} = \frac{1}{2} (-N_{i3}N_{j3}^{*} + N_{i4}N_{j4}^{*}), \quad O_{ij}^{R} = -O_{ij}^{L*}.$$
(15)

Therefore, for the massless neutralino we have

$$O_{11}^{L} \simeq \frac{1}{2} \frac{m_Z^2}{\mu^2} \sin^2 \theta_W \cos 2\beta.$$
 (16)

Equation (11) requires that $O_{11}^L \le 1/30$; we see that this can be easily satisfied for values of μ of order 500 GeV. (Note also that although in the limit $\tan \beta \approx 1$ the massless neutralino is decoupled from Z boson, this is not a necessary condition.)

One must also consider cosmological constraints on the existence of a light neutralino. From constraints on the neutralino relic abundance, recent analyses [18] infer a lower limit of 6 to 18 GeV on the neutralino mass. However, these analyses are valid for neutralinos with mass in the GeV range. Superlight neutralinos (mass of order eV) will not annihilate before decoupling, and therefore different limits apply. Since the annihilation cross section to e^+e^- is sup-

pressed by the small coupling to Z (and the large selectron mass), our neutralino will behave very much as a sterile neutrino. Recent cosmological data impose an upper limit on a sterile neutrino mass of around 1.4 eV [19], which we assume to be also valid for the neutralino considered in this section.

So far we have shown that a massless neutralino is consistent with experimental constraints¹ (if we give up the assumption of gaugino mass universality at GUT scale). This massless state, however, does not appear naturally in the theory; finetuning of order 1 eV/ 100 GeV $\approx 10^{-11}$ is necessary to satisfy Eq. (6). Moreover, we have to impose this finetuning on the complete theory; for example, if Eq. (6) holds at tree level, it will be broken by loop corrections, and the neutralino will acquire GeV size mass. For these reasons, this model is not very compelling theoretically; however, it is experimentally allowed.

B. NMSSM case

In the event we want to keep the GUT relation (7), it is possible to get a massless neutralino in the framework of NMSSM. Let us consider NMSSM with the following terms in the superpotential:

$$W = \lambda \varepsilon_{ii} H_1^i H_2^j S - \frac{1}{3} \kappa S^3, \qquad (17)$$

where i, j = 1, 2, ϵ_{ij} is the antisymmetric tensor, H_1 and H_2 are the standard Higgs boson doublets, and *S* is the MSSM Higgs boson singlet. (The first term replaces the usual SUSY μ term.) In this case the neutralino mass matrix becomes

	$-M_1$	0	$-m_z \cos\beta\sin\theta_w$	$m_z \sin \beta \sin \theta_w$	0
$M_{ij} \equiv$	0	$-M_2$	$m_z \cos \beta \cos \theta_w$	$-m_z \sin\beta\cos\theta_w$	0
	$-m_z \cos\beta\sin\theta_w$	$m_z \cos \beta \cos \theta_w$	0	λx	$\lambda v \sin \beta$
	$m_z \sin \beta \sin \theta_w$	$-m_z \sin\beta\cos\theta_w a$	λx	0	$\lambda v \cos \beta$
	0	0	$\lambda v \sin \beta$	$\lambda v \cos \beta$	$-2\kappa x$

The determinant of this mass matrix is

$$\Delta = -2\kappa x \Delta_0 + \lambda^2 v^2 (m_z^2 (M_1 \cos^2 \theta_w + M_2 \sin^2 \beta_w) - \mu M_1 M_2 \sin 2\beta),$$
(18)

where v = 174 GeV, x is the vacuum expectation value (VEV) of S field, and we define μ to be λx . We assume in the following that we are in a region of the parameter space where $\mu M_1 M_2 \ge m_z^2 (M_1 \cos^2 \theta_W + M_2 \sin^2 \theta_W) \simeq 0.6 m_z^2 M_2$; we also assume that $\tan \beta$ is large. Then $\Delta_0 \simeq -\mu^2 M_1 M_2$, and

$$\kappa = \lambda \frac{1}{2} \left(\frac{\lambda v}{\mu} \right)^2 \frac{0.6m_z^2 M_2 - 0.5\mu M_2^2 \sin 2\beta}{-\mu M_1 M_2}$$
(19)

will provide a massless neutralino. The particle content of this neutralino is given by

$$N_{1i} = \left(\lambda \frac{v m_z}{\mu M_1} \cos 2\beta \sin \theta_W, -\lambda \frac{v m_z}{\mu M_2} \cos 2\beta \cos \theta_W, -\lambda \frac{v}{\mu} \frac{0.6m_z^2 \sin \beta - \mu M_1 \cos \beta}{\mu M_1}, -\lambda \frac{v}{\mu} \frac{0.6m_z^2 \cos \beta - \mu M_1 \sin \beta}{\mu M_1}, -\lambda \frac{v}{\mu} \frac{0.6m_z^2 \cos \beta - \mu M_1 \sin \beta}{\mu M_1}, 1\right),$$
(20)

¹For a similar analysis, including additional constraints, see, for example, Ref. [17].

that is, in the limit when $\lambda v/\mu \ll 1$, it is mostly singlino. The coupling to the Z is given by

$$O_{11}^{L} \approx \left(\frac{\lambda v}{\mu}\right)^{2} \frac{(\mu M_{1})^{2} - (0.6m_{z}^{2})^{2}}{(\mu M_{1})^{2}} \approx \left(\frac{\lambda v}{\mu}\right)^{2}$$
(21)

and with μ of order 500 GeV and $\lambda \approx 0.3$, the constraint coming from the invisible Z width is satisfied again. (Note that this implies that κ is quite small as well.)

C. The c terms

We have seen that bilinear terms (1) which couple the *B*-ino (or, in the NMSSM case, the singlino) and the right-handed neutrino are allowed by the requirement that supersymmetry is softly broken. However, these terms break usual *R* parity, which may not be desirable. In order to forbid the usual RPV terms, we can introduce a new $U(1)_R$ symmetry. Let us then consider the following generation independent assignment of $U(1)_R$ charges to the MSSM and right-handed neutrino superfields:

$$Q(3,2,1/6): q \quad D^{c}(\overline{3},1,1/3):2-2q-u$$
$$U^{c}(\overline{3},1,-2/3): u \quad L(1,2,-1/2):-2+q+u$$

$$Q \quad (3,2,1/6): \qquad q$$

$$U^{c} \quad (\overline{3},1,-2/3): \qquad u$$

$$N \quad (1,1,0): \qquad \frac{10}{3}$$

$$H_{d} \quad (1,2,-1/2): \qquad -\frac{2}{3}+q+u$$

$$\theta: \qquad \qquad 1$$

and in this case only the (23) couplings are allowed from general the RPV term.

IV. IMPLICATIONS FOR NEUTRINO SECTOR

In this section we will consider the implications of a sterile neutrino coming from supersymmetry for neutrino physics.

A. LSND result and massless neutralino

As was mentioned briefly in Sec. II, a massless neutralino seems ideally suited to explain the LSND experiment results. Since the magnitude of c couplings is given by the SUSY breaking scale, we can expect the mass of the fourth neutrino to be of order $c^2/m_D^2 \approx 100$ times larger than the mass of the heaviest SM neutrino. This puts it in the eV range, which is the right value needed to account for the LSND result.

$$N(1,1,0): 2 \quad E^{c}(1,1,1):4-2q-2u$$

$$H_{d}(1,2,-1/2):q+u \quad H_{u}(1,2,1/2):2-q-u$$

$$\theta: \quad 1, \qquad (22)$$

where the $SU(3)_c \times SU(2)_L \times U(1)_Y$ quantum numbers of the particles are given in the brackets, and θ is the Grassmann coordinate. We choose the $U(1)_R$ charge of the Grassmann coordinate θ to be unity. It is easy to check that this charge assignment forbids the usual *R*-parity breaking terms and allows all MSSM Yukawa couplings as well as the righthanded neutrino $\tilde{B}N$ coupling and the Higgs boson mixing μ term. In our $U(1)_R$ charge approach we assume that the right-handed neutrino fields have $U(1)_R$ charge equal to -1. This means that the corresponding mass terms are generated though a heavy field VEV ($\geq 10^{14}$ GeV). This field also breaks the $U(1)_R$ symmetry at the high scale.

In the NMSSM case, when the massless neutralino is mostly singlino, the relevant coupling with the right-handed neutrino is

$$c_i \tilde{S} N_i$$
. (23)

This coupling also breaks usual *R* parity. But we can choose the following $U(1)_R$ charge assignments:

$$D^{c} \quad (3,1,1/3): \quad \frac{8}{3} - 2q - u$$

$$L \quad (1,2,-1/2): \quad -\frac{10}{3} + q + u$$

$$E^{c} \quad (1,1,1): \quad 6 - 2q - 2u$$

$$u \quad H_{u} \quad (1,2,1/2): \quad 2 - q - u$$

$$S \quad -\frac{2}{3}$$
(24)

Moreover, LSND data [9] and constraints from short baseline experiments [20,21] require that the admixture of ν_e and ν_{μ} in the fourth neutrino (let us call it ν_0) has to be of the order of 0.1. In terms of the elements of the rotation matrix $U_{\alpha i}$ (α stands for $\chi_1^0, \nu_e, \nu_{\mu}, \nu_{\tau}$) which diagonalizes the $(M_{\nu})_{\alpha\beta}4\times4$ mass matrix (3), we need $U_{e0}, U_{\mu 0}$ ~0.12-0.14. On the other hand, as long as $M_{\nu}(\chi_1^0, \nu_i)$ $\leq M_{\nu}(\chi_1^0, \chi_1^0)$ we can employ the seesaw approximation to decouple the fourth neutrino from the other three, and we will have

$$U_{i0} \simeq \frac{M_{\nu}(\chi_1^0, \nu_i)}{M_{\nu}(\chi_1^0, \chi_1^0)} \simeq \frac{m_D}{c} \simeq \frac{1}{10},$$

which fits nicely the experimental requirements.

For the purpose of illustration, we present here a particular realization of this situation. We can work in a basis where the Majorana mass matrix is diagonal; let us even assume that it is proportional to the identity matrix: $M_M = I_{3\times 3}m_M$. Moreover, let us assume that there is no hierarchy between the soft SUSY breaking parameters: $c_1 = c_2 = c_3 = c$. For the Dirac mass matrix, take a symmetric form

$$m_D = \begin{pmatrix} m_1 & a_3 & a_2 \\ a_3 & m_2 & a_1 \\ a_2 & a_1 & m_3 \end{pmatrix}$$
(25)

and see what constraints the LSND result imposes on the elements of this matrix.

First, we need $U_{e0} \approx U_{\mu 0}$; since in the seesaw approximation $U_{i0} = M_{\nu}(\chi_1^0, \nu_i)/M_{\nu}(\chi_1^0, \chi_1^0)$, this implies $\Sigma_i(m_D)_{i1} = \Sigma_i(m_D)_{i2}$, or

$$m_1 + a_2 + a_3 = m_2 + a_1 + a_3. \tag{26}$$

Moreover, from atmospheric oscillation results and the CHOOZ constraints on $\bar{\nu}_e$ disappearance [22] ($\theta_{23} \approx 45^\circ, \theta_{13}$ small), we know that $|U_{\mu3}| \approx |U_{\tau3}| \approx 1/\sqrt{2}$ and $|U_{e3}| \approx 0$, which implies $|U_{03}| \approx 0$, too. From the orthogonality of the rotation matrix $\Sigma_i U_{i0} U_{i3} = 0$, we then get $|U_{\mu0}| \approx |U_{\tau0}|$, or

$$m_2 + a_1 + a_3 = m_3 + a_1 + a_2. \tag{27}$$

After decoupling the sterile neutrino, the effective mass matrix for the three SM neutrinos will be

$$(M_{\nu}')_{ij} = \frac{(m_D m_D^I)_{ij}}{m_M} - \frac{(M_{\nu})_{i0}(M_{\nu})_{0j}}{(M_{\nu})_{00}}.$$
 (28)

Since the determinant of this matrix is zero, there are three possible textures which will explain the observed neutrino mass splitting and mixings (see, for example, Ref. [23]). We shall try to obtain the hierarchical form, where $(m_{\nu_1}, m_{\nu_2}, m_{\nu_3}) = (0, \delta, M)$, with $\delta \ll M$. Then the mass matrix should look like Eq. (32). Requiring that $|(M'_{\nu})_{12}| \simeq |(M'_{\nu})_{13}| \simeq 0$ we get the following equations:

$$m_2 = m_3, \quad a_1 = 2m_1 - m_3.$$
 (29)

Then

$$M'_{\nu} = \frac{1}{m_M} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 2(m_1 - m_3)^2 & -2(m_1 - m_3)^2 \\ 0 & -2(m_1 - m_3)^2 & 2(m_1 - m_3)^2 \end{pmatrix}$$
(30)

leads to maximal mixing for the atmospheric neutrinos, with the corresponding mass scale given by $M=4(m_1 - m_3)^2/m_M$. The θ_{13} angle is also zero. However, this texture does not explain the solar oscillations. To account for these, we need corrections of order δ/M to texture (30), where δ is the mass scale responsible for solar oscillations. We are therefore led to consider corrections of order δ/M to Eqs. (26), (27), and (29). It turns out that, when θ_{13} is chosen to be zero, Eq. (27) and the first one of Eqs. (29) are protected by the requirement that $\theta_{23}=45^\circ$. Breaking relation (26) will give a mass to the second neutrino state, which can account for the splitting necessary for solar neutrino oscillations. An interesting note is that if the second relation in Eq. (29) remains unchanged, then the solar mixing angle will be given by $\tan^2 \theta_{12} = 0.5$, which is very close to the best fit value for solar neutrino oscillations.

With these choices, the following neutrino Dirac mass matrix is obtained:

$$m_{D} = \begin{pmatrix} m_{1} & m_{1} + \frac{\delta}{\sqrt{2}} & m_{1} + \frac{\delta}{\sqrt{2}} \\ m_{3} & 2m_{1} - m_{3} \\ m_{3} & m_{3} \end{pmatrix}$$

(the matrix being symmetric). This texture gives rise the following neutrino masses:

$$\{m_{\nu_0}, m_{\nu_1}, m_{\nu_2}, m_{\nu_3}\} = \left\{3\frac{c^2 + 3m_1^2}{m_M}, 0, \delta\right. \\ + \mathcal{O}\left(\delta\frac{m_1^2}{c^2}\right), 4\frac{(m_1 - m_3)^2}{M_M}\right\}$$

and the 4-neutrino mixing matrix will be

 $U_{\alpha i}$

$$= \begin{pmatrix} \frac{c^2}{c^2 + 3m_1^2} & 0 & 0 & 0\\ \frac{m_1 + \sqrt{2}/3\sqrt{\delta m_M}}{c} & \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} & 0\\ \frac{m_1 + \sqrt{2}/6\sqrt{\delta m_M}}{c} & \sqrt{\frac{1}{6}} & -\sqrt{\frac{1}{3}} & -\frac{1}{\sqrt{2}}\\ \frac{m_1 + \sqrt{2}/6\sqrt{\delta m_M}}{c} & \sqrt{\frac{1}{6}} & -\sqrt{\frac{1}{3}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

(with corrections of order m_1/c). Here m_1 can be taken to be arbitrary (as long as it is smaller than c), and m_3 to be fixed by the mass of the third neutrino: $m_3 = \pm \sqrt{M_M m_{\nu_3}}/2 + m_1$.

We have obtained the hierarchical structure for neutrino masses. Taking $m_{\nu_3} = M \approx 5 \times 10^{-2}$ eV and $m_{\nu_2} = \delta \approx 7 \times 10^{-3}$ eV, the splitting between ν_3 and ν_2 accounts for atmospheric neutrino oscillations, while the splitting between ν_2 and ν_1 accounts for the solar neutrinos. The atmospheric mixing angle is 45°, the solar angle is large ($\approx 35^{\circ}$), and the θ_{13} angle is zero. Choosing c = 1 TeV for $m_M = 2.4 \times 10^{15}$ GeV, and $m_1 = 0.08c$, we obtain the mass of the fourth neutrino $m_{\nu_0} \approx 1.3$ eV, and the elements of the rotation matrix

$$U_{e0} \simeq 0.14, \ U_{\mu 0} = U_{\tau 0} \simeq 0.11,$$

which implies $\sin^2 2\theta_{LSND} = 1.2 \times 10^{-3}$, and can therefore account for the LSND results, while at the same time satisfying the cosmological constraints on a sterile neutrino mass [24].

B. Massless neutralino and large mixing

Another interesting question is if it is possible to explain the large mixing among the three SM flavor eigenstates through the coupling to the neutralino. To this purpose, let us assume that the neutrino Dirac mass matrix has a diagonal structure:

$$(m_D)_{\alpha\beta} = m_\alpha \delta_{\alpha\beta}$$

Let us, moreover, assume that $M_{\nu}(\chi^0, \chi^0) = (c_1^2 + c_2^2 + c_3^2)/m_M$ is much larger than the neutrino masses m_{α}^2/m_M . Then, we can decouple the fourth neutrino, and in the seesaw approximation the mass matrix for the three SM neutrinos will become

$$(M_{\nu})'_{\alpha\beta} \simeq \frac{m_{\alpha}m_{\beta}}{m_{M}} \left(\delta_{\alpha\beta} - \frac{c_{\alpha}c_{\beta}}{\bar{c}^{2}} \right)$$

with $\vec{c}^2 = c_1^2 + c_2^2 + c_3^2$. Note that this matrix has zero determinant, but it is not traceless. As a consequence, the only possible diagonal neutrino mass matrices which can be obtained by diagonalization are the hierarchical diag $(0, \delta, M)$ structure and the inverted hierarchy case diag $(M, M + \delta, 0)$. Both of these require that

$$|(M'_{\nu})_{12}| \simeq |(M'_{\nu})_{13}| \simeq 0,$$

$$(M_{\nu})'_{22}| \simeq |(M'_{\nu})_{33}| \simeq |(M'_{\nu})_{23}| \simeq M/2$$

with corrections to these equations of order δ/M . A simple choice which satisfies the above equations is

$$(c_1, c_2, c_3) = (0, c, c); (m_1, m_2, m_3) = (0, \sqrt{Mm_M}, \sqrt{Mm_M}),$$
(31)

which leads to a neutrino mass matrix:

$$M'_{\nu} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & M/2 & -M/2 \\ 0 & -M/2 & M/2 \end{pmatrix}.$$
 (32)

This is the hierarchical case, with $m_{\nu_3} = M$ and the angles $\theta_{23} = 45^\circ$, $\theta_{13} = 0$. Corrections of order δ/M to Eq. (31):

$$(c_1, c_2, c_3) = c \left(\sqrt{\frac{4\delta}{3M}}, 1 - \frac{\delta}{3M}, 1 - \frac{\delta}{3M} \right);$$

$$(m_1, m_2, m_3) = (\sqrt{\delta m_M/3}, \sqrt{M m_M}, \sqrt{M m_M})$$
(33)

will provide a mass δ for ν_2 and make the θ_{12} angle $\simeq 35^\circ$.

Finally, we want to mention that using a sterile neutrino in order to explain large mixing in the active sector is not a new idea (see, for example, Ref. [11]). However, while in Ref.

[11] the couplings of the sterile neutrino with the three SM flavors is introduced in a somewhat *ad hoc* manner, in our model it arises naturally.

V. CONCLUSIONS

In this paper we have addressed two questions. First, is a massless neutralino allowed by experimental data? Second, can such a neutralino couple with the neutrino sector and explain the LSND result, and/or large mixing among the three active neutrino flavors? We answered both questions in the affirmative. By giving up the assumption of universal gaugino masses, we can obtain a massless neutralino in the MSSM. This would require finetuning, but, since its couplings to the Z can be suppressed, it will still satisfy the LEP constraints on the invisible Z width. Conversely, we can obtain a massless neutralino in the framework of the NMSSM, in which case this particle will be mostly a singlino.

The coupling of the massless neutralino with the neutrino sector is achieved through the introduction of new soft SUSY breaking terms of the form $c\tilde{B}N$. Then the neutralino, which is identified with a sterile neutrino, will acquire a mass proportional to the square of the soft SUSY breaking scale $(c^2/M_M \sim eV)$, in contrast with the usual seesaw where the light neutrino mass is proportional to the up quark or charged lepton mass square. This makes it an ideal candidate for explaining the LSND experiment results. Moreover, the seesaw induced mixing of the neutralino with the three neutrinos is also consistent with constraints from short baseline experiments, while large enough to account for LSND. Large mixing among the three active neutrino flavors arises naturally in this model.

The weak point of this model is that finetuning is required to obtain a massless neutralino. A promising candidate for a massless SUSY particle would be a fermion associated with spontaneous SUSY breaking, that is, a visible sector Goldstino. However, this would require some more model building, and we leave it for another paper. Even so, we find the fact that a massless neutralino is experimentally allowed interesting. Also, the fact that one of the light neutrino masses can be connected to the soft SUSY breaking scale is another intriguing feature of this scenario.

ACKNOWLEDGMENTS

We thank K.S. Babu, B. Bajc, Z. Berezhiani, J.L. Chkareuli, P. Kumar, and H.B. Nielsen for useful discussions. I.G., C.M., and S.N. gratefully acknowledge support from the Fermilab Summer Visitor Program and warm hospitality from the Fermilab Theory Group during the initial stages of this project. S.N. also acknowledges the warm hospitality and support of the DESY and CERN Theory Groups during the completion of this work. I.G., C.M., and S.N.'s work is supported in part by the U.S. Department of Energy Grant Numbers DE-FG03-98ER41076 and DE-FG02-01ER45684. The work of J.L. was supported by the U.S. Department of Energy Grant DE-AC02-76CHO3000.

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