# **Constraining the absolute neutrino mass scale and Majorana** *CP* **violating phases** by future  $0\nu\beta\beta$  decay experiments

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Assuming that neutrinos are Majorana particles, in a three-generation framework, current and future neutrino oscillation experiments can determine six out of the nine parameters which fully describe the structure of the neutrino mass matrix. We try to clarify the interplay among the remaining parameters, the absolute neutrino mass scale and two *CP* violating Majorana phases, and how they can be accessed by future neutrinoless double beta ( $0\nu\beta\beta$ ) decay experiments, for the normal as well as for the inverted order of the neutrino mass spectrum. Assuming the oscillation parameters to be in the range presently allowed by atmospheric, solar, reactor, and accelerator neutrino experiments, we quantitatively estimate the bounds on  $m<sub>0</sub>$ , the lightest neutrino mass, that can be inferred if the next generation  $0\nu\beta\beta$  decay experiments can probe the effective Majorana mass ( $m_{ee}$ ) down to  $\sim$  1 meV. In this context we conclude that in the case that neutrinos are Majorana particles, (a) if  $m_0 \ge 300$  meV, i.e., within the range directly attainable by future laboratory experiments as well as astrophysical observations, then  $m_{ee} \gtrsim 30$  meV must be observed, (b) if  $m_0 < 300$  meV, results from future  $0 \nu \beta \beta$  decay experiments combined with stringent bounds on the neutrino oscillation parameters, especially the solar ones, will place much stronger limits on the allowed values of  $m<sub>0</sub>$  than these direct experiments. For instance, if a positive signal is observed around  $m_{ee} = 10 \text{ meV}$ , we estimate  $3 \le m_0/\text{meV} \le 65$  at 95% C.L.; on the other hand, if no signal is observed down to  $m_{ee} = 10$  meV, then  $m_0 \le 55$  meV at 95% C.L.

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## **I. INTRODUCTION**

During the last few years, a significant amount of information on the size of the neutrino oscillation parameters has been gathered. Most of what we currently know about these parameters relies on evidence of neutrino flavor transformation that has been collected by experimental observations of solar  $[1]$  as well as of atmospheric neutrinos  $[2]$ . The evidence coming from solar neutrino data has been strengthened by the recent neutral current measurement at the Sudbury Neutrino Observatory  $(SNO)$   $[3]$  while that from atmospheric neutrinos has also been strongly supported by the K2K accelerator based neutrino oscillation experiment [4]. Furthermore, the negative results of reactor experiments  $[5]$ also impose stringent limits on some oscillation parameters.

Assuming that only three active neutrinos participate in oscillations in nature, independent of whether neutrinos are Dirac or Majorana particles, current and future neutrino oscillation experiments can determine at the most six out of the nine parameters which completely describe the neutrino mass matrix: i.e., two mass-squared differences  $(\Delta m_{12}^2, \Delta m_{23}^2)$ , three mixing angles  $(\theta_{12}, \theta_{13}, \theta_{23})$ , and one  $CP$  violating phase  $(\delta)$ , which parametrize the Maki-Nakagawa-Sakata (MNS) [6] leptonic mixing matrix. See, for instance, Refs.  $[7,8]$  for recent discussions on the determination of these *oscillation* parameters.

However, if neutrinos are of the Majorana type, there remain three nonoscillation parameters, which cannot be accessed by oscillation experiments. They are the absolute neutrino mass scale, which can be taken as the lightest neutrino mass, and two extra  $CP$  violating Majorana phases  $|9-11|$ . It is well known that neutrinoless double beta  $(0\nu\beta\beta)$  decay experiments can shed light on these nonoscillation parameters.

 $0\nu\beta\beta$  decay is a process that can occur if and only if neutrinos are Majorana particles [12]. A positive signal of  $0\nu\beta\beta$  decay always implies a nonzero electron neutrino mass  $[13]$  even if it is not induced by the exchange of a light neutrino but by some other mechanism such as the one in supersymmetry models with broken  $R$  parity [14]. In this work, we assume the simplest possibility to be true, that the  $0\nu\beta\beta$  decay process is induced only by the exchange of a light neutrino.

The relationship between the signals in  $0\nu\beta\beta$  decay experiments and oscillation phenomena has been abundantly discussed in the literature; see, for example, Ref.  $[15]$ . So far, a large amount of effort has been made to constrain the oscillation parameters from the observation or nonobservation of  $0\nu\beta\beta$  decay, as well as to predict the possible range of the effective Majorana mass in  $0\nu\beta\beta$  decay experiments,  $m_{ee}$ , from the allowed range of oscillation parameters [15].

In this paper, we take a different point of view. We examine how well we can constrain the three nonoscillation parameters by future  $0\nu\beta\beta$  decay experiments, considering that the oscillation parameters will soon be precisely deter-

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mined (or constrained) by current and future oscillation experiments. We discuss the interplay among these parameters and the observable signal in future  $0\nu\beta\beta$  decay experiments for the normal as well as for the inverted ordering of the neutrino mass spectrum. In particular, presuming the oscillation parameters to be in the range presently allowed by the atmospheric, solar, and reactor neutrino experiments, we examine what can be concluded about these parameters in the case of either a positive or a negative signal obtained in future  $0\nu\beta\beta$  decay experiments [16].

So far, no convincing signal of  $0\nu\beta\beta$  decay has been observed, rather only an upper bound on *mee* ,

$$
m_{ee} < 350 \, \text{meV}, \tag{1}
$$

which comes from the result of the Heidelberg-Moscow Collaboration  $[17]$ , exists. Recently, an experimental indication of the occurrence of  $0\nu\beta\beta$  decay has been announced [18] but since this result seems to be controversial  $[19]$  we do not discuss it in this work.

There are many proposals for future  $0\nu\beta\beta$  decay experiments to go beyond the bound given in Eq.  $(1)$ ; these include GENIUS [20], CUORE [21], EXO [22], MAJORANA [23], and NOON  $[24]$ . It is expected that in the initial phase of the proposed GENIUS experiment  $[20]$  the sensitivity to  $m_{ee}$  can be as low as  $\sim$ 10 meV, going down to  $\sim$ 2 meV if the 10 ton version of the experiment is implemented. In this work, we will try to be optimistic and consider that future experiments will eventually inspect  $m_{ee}$  down to  $\sim$  1 meV.

The absolute neutrino mass scale is also independently constrained by tritium decay experiments, which can directly measure the electron neutrino mass, obtaining the upper bound  $[25]$ 

$$
m_{\nu_e} < 2200 \text{ meV.}
$$

The proposed KATRIN experiment aims to stretch the current sensitivity down to  $\sim$  340 meV [26]. We also take this into consideration in our discussion.

This paper is organized as follows. In Sec. II, we describe the theoretical framework on which we base our work. We first discuss in Sec. III the dependence of the  $0\nu\beta\beta$  signal on the lightest neutrino mass, and second in Sec. IV we discuss how the dependence of  $m_{ee}$  on  $m_0$  is related to the two  $CP$ phases  $\alpha_1$  and  $\alpha_3$ . In Sec. V we discuss how  $m_{ee}^{\text{min}}$ , the minimum possible value of  $m_{ee}$ , depends on  $m_0$  and  $\theta_{13}$ . Finally, in Sec. VI, we discuss how the upper as well as the lower bounds on  $m_0$  depend on the solar neutrino oscillation parameters. Section VII is devoted to our discussion and conclusions.

#### **II. THE FORMALISM**

In this section we discuss the theoretical framework we will rely upon in this work.

### **A. Mixing and mass scheme**

We consider mixing among three neutrino flavors as

$$
\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = U \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix},
$$
 (3)

where  $v_{\alpha}$  ( $\alpha=e,\mu,\tau$ ) and  $v_i$  ( $i=1,2,3$ ) are the weak and mass eigenstates, respectively, and  $U$  is the MNS  $\lceil 6 \rceil$  mixing matrix, which can be parametrized as

$$
\begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23}-c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23}-s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix},
$$
\n
$$
(4)
$$

where  $s_{ij}$  and  $c_{ij}$ , correspond to the sine and cosine of  $\theta_{i,j}$ . We define the neutrino mass-squared differences as  $\Delta m_{ij}^2$  $\equiv m_j^2 - m_i^2$ , where  $\Delta m_{\odot}^2 = \Delta m_{12}^2$  is relevant for solutions to the solar neutrino problem, and  $\Delta m_{\text{atm}}^2 = |\Delta m_{23}^2| \approx |\Delta m_{13}^2|$  is relevant for atmospheric neutrino observations.

Current atmospheric neutrino data  $[2]$  indicate that

$$
\Delta m_{\text{atm}}^2 = |\Delta m_{23}^2| \approx (2 - 4) \times 10^{-3} \text{ eV}^2,
$$
  

$$
\sin^2 2 \theta_{23} \approx 0.9 - 1,
$$
 (5)

which combined with nuclear reactor results  $[5]$  imply

$$
\sin^2 \theta_{13} \le 0.02,\tag{6}
$$

while the various solar neutrino experiment results strongly suggest that the so-called large mixing angle (LMA) Mikheyev-Smirnov-Wolfenstein (MSW) solution with parameters in the range  $\lceil 1,3,27 \rceil$ 

$$
\Delta m_{\odot}^2 = \Delta m_{12}^2 \approx (2 - 40) \times 10^{-5} \text{ eV}^2,
$$
  
\n
$$
\tan^2 \theta_{12} \approx 0.2 - 0.8,
$$
 (7)

will prevail as the explanation to the solar neutrino problem. We will admit throughout this paper that the actual values of these parameters will be confirmed within the above ranges by future neutrino oscillation experiments. In addition to further constraining the oscillation parameters given in Eqs.  $(5)$ – $(7)$ , it is expected that these experiments can also probe the  $\mathcal{CP}$  violating phase  $\delta$  and determine the neutrino mass spectrum (sign of  $\Delta m_{23}^2$ ) [7].



FIG. 1. Mass ordering considered in this work.

In this work, we denote the lightest neutrino mass by  $m_0$ . Then, using  $\Delta m_{\odot}^2$  and  $\Delta m_{\text{atm}}^2$  as defined above, we can describe the two possible mass spectra as follows:

(a) normal mass ordering:

$$
m_1 \equiv m_0,
$$
  
\n
$$
m_2 \equiv \sqrt{m_0^2 + \Delta m_{\odot}^2},
$$
  
\n
$$
m_3 \equiv \sqrt{m_0^2 + \Delta m_{\odot}^2 + \Delta m_{\text{atm}}^2};
$$
\n(8)

(b) inverted mass ordering:

$$
m_1 \equiv \sqrt{m_0^2 - \Delta m_{\odot}^2 + \Delta m_{\text{atm}}^2},
$$
  
\n
$$
m_2 \equiv \sqrt{m_0^2 + \Delta m_{\text{atm}}^2},
$$
  
\n
$$
m_3 \equiv m_0.
$$
\n(9)

In this manner  $\Delta m_{12}^2 = \Delta m_{\odot}^2$  for both mass orderings and  $\Delta m_{23}^2 = \pm \Delta m_{\text{atm}}^2$  where the  $+ (-)$  sign indicates normal (inverted) mass ordering. In Fig. 1, a schematic picture of the mass ordering we consider here is shown.

## **B.** Effective Majorana mass and  $0\nu\beta\beta$

Assuming that the  $0\nu\beta\beta$  decay process occurs through the exchange of a light ( $m_v$ <10 MeV) neutrino, the theoretically expected half-life of the  $0\nu\beta\beta$  decay,  $T_{1/2}^{0\nu}$ , is given by  $[28]$ 

$$
[T_{1/2}^{0\nu}]^{-1} = G^{0\nu} |M_{0\nu}|^2 m_{ee}^2, \qquad (10)
$$

where  $G^{0\nu}$  denotes the exact calculable phase space integral,  $M_{0\nu}$  consists of the sum of the Gamow-Teller and the Fermi nuclear matrix elements defined as in Ref.  $[28]$ , and  $m_{ee}$  is the effective Majorana mass defined in Eq.  $(11)$  below.

It is known that the evaluation of the nuclear matrix elements suffers from a large uncertainty depending on the method used in the calculations. As we can see in Table II of Ref. [28], the evaluated half-lives for a given nucleus and a given value of  $m_{ee}$  typically vary within a factor of  $\sim 10$ comparing the largest and smallest predicted values. This implies a factor of  $\sim$  3 difference between the minimum and maximum values of  $m_{ee}$  when extracting it from the results of  $0\nu\beta\beta$  decay experiments, which in fact directly measure or constrain not  $m_{ee}$  but the value of  $T_{1/2}^{0\nu}$ . This is clear from Eq. (10). In Sec. VI, we will consider for our estimations a somewhat optimistic uncertainty of a factor  $\sim$  2 instead of 3, assuming future improvements in the evaluation of the nuclear matrix elements.

The effective Majorana mass  $m_{ee}$  is given by

$$
m_{ee} = |m_1 U_{e1}^2 + m_2 U_{e2}^2 + m_3 U_{e3}^2|,
$$
  
=  $|m_1 c_{12}^2 c_{13}^2 e^{2i\alpha_1} + m_2 s_{12}^2 c_{13}^2 + m_3 s_{13}^2 e^{2i\alpha_3}|,$  (11)

where we have chosen to attach the *CP* violating phases to the first and third elements. Note that  $\alpha_1$  and  $\alpha_3$  must be understood as the relative phases of  $U_{e1}$  and  $U_{e3}$  with respect to that of  $U_{e2}$ . The ranges of these phases are

$$
0 \le \alpha_1 \le \pi, \ 0 \le \alpha_3 \le \pi. \tag{12}
$$

As is known, the value of  $m_{ee}$  can be perceived as the norm of the sum of three vectors  $\vec{m}_{ee}^{(1)}$ ,  $\vec{m}_{ee}^{(2)}$ , and  $\vec{m}_{ee}^{(3)}$  in the complex plane whose absolute values are given by

$$
m_{ee}^{(1)} \equiv |\vec{m}_{ee}^{(1)}| \equiv |U_{e1}^2| m_1 = m_1 c_{12}^2 c_{13}^2,
$$
  
\n
$$
m_{ee}^{(2)} \equiv |\vec{m}_{ee}^{(2)}| \equiv |U_{e2}^2| m_2 = m_2 s_{12}^2 c_{13}^2,
$$
  
\n
$$
m_{ee}^{(3)} \equiv |\vec{m}_{ee}^{(3)}| \equiv |U_{e3}^2| m_3 = m_3 s_{13}^2.
$$
\n(13)

Explicitly,  $m_{ee}$  is expressed as

$$
m_{ee}^{2} = [m_{ee}^{(1)} \cos 2\alpha_{1} + m_{ee}^{(2)} + m_{ee}^{(3)} \cos 2\alpha_{3}]^{2} + [m_{ee}^{(1)} \sin 2\alpha_{1} + m_{ee}^{(3)} \sin 2\alpha_{3}]^{2}
$$
  
\n
$$
= [m_{ee}^{(1)}]^{2} + [m_{ee}^{(2)}]^{2} + [m_{ee}^{(3)}]^{2} + 2\{m_{ee}^{(1)}m_{ee}^{(2)} \cos 2\alpha_{1} + m_{ee}^{(2)}m_{ee}^{(3)} \cos 2\alpha_{3} + m_{ee}^{(1)}m_{ee}^{(3)} \cos[2(\alpha_{1} - \alpha_{3})]\}
$$
  
\n
$$
= m_{1}^{2}c_{12}^{4}c_{13}^{4} + m_{2}^{2}s_{12}^{4}c_{13}^{4} + m_{3}^{2}s_{13}^{4} + 2\{m_{1}m_{2}c_{12}^{2}s_{12}^{2}c_{13}^{2} \cos 2\alpha_{1} + m_{2}m_{3}s_{12}^{2}c_{13}^{2}s_{13}^{2} \cos 2\alpha_{3} + m_{1}m_{3}c_{12}^{2}c_{13}^{2}s_{13}^{2} \cos[2(\alpha_{1} - \alpha_{3})]\}.
$$
  
\n(14)

We can clearly see from Eq.  $(14)$  that  $m_{ee}$  is invariant under the transformation

which allows us to further restrict the range of  $(\alpha_1, \alpha_3)$ , without loss of generality, to

$$
(\alpha_1, \alpha_3) \rightarrow (\pi - \alpha_1, \pi - \alpha_3), \tag{15}
$$

$$
0 \le \alpha_1 \le \pi, \ 0 \le \alpha_3 \le \pi/2. \tag{16}
$$

We note that  $\alpha_1$  and/or  $\alpha_3$  different from 0 and  $\pi/2$  imply *CP* violation.

The maximum possible value of  $m_{ee}$ , denoted by  $m_{ee}^{\text{max}}$ , is given by

$$
m_{ee}^{\text{max}} = m_{ee}^{(1)} + m_{ee}^{(2)} + m_{ee}^{(3)}
$$
  
=  $(m_1 c_{12}^2 + m_2 s_{12}^2) c_{13}^2 + m_3 s_{13}^2,$  (17)

which occurs for  $\alpha_1 = \alpha_3 = 0$ . On the other hand, the minimum possible value of  $m_{ee}$  is zero only when the three vectors  $\vec{m}_{ee}^{(i)}$  ( $i=1,2,3$ ) can form a triangle. This can occur when the condition

$$
m_{ee}^{(i)} < \sum_{j \neq i} m_{ee}^{(j)} \quad (i = 1, 2, 3)
$$
 (18)

is satisfied. When these three vectors cannot form a closed triangle, which includes the case when one of them is null, the minimum value is given by twice the length of the largest vector minus the sum of the norm of all three vectors,

$$
m_{ee}^{\min} = 2 \max \{ m_{ee}^{(1)}, m_{ee}^{(2)}, m_{ee}^{(3)} \}
$$

$$
- [m_{ee}^{(1)} + m_{ee}^{(2)} + m_{ee}^{(3)}].
$$
 (19)

The values of  $(\alpha_1, \alpha_3)$  that lead to such a minimum are  $(\alpha_1, \alpha_3) = (\pi/2,0), (\pi/2, \pi/2)$ , or  $(0,\pi/2)$  when, respectively,  $m_{ee}^{(1)}$ ,  $m_{ee}^{(2)}$ , or  $m_{ee}^{(3)}$  is the largest contribution.

#### **C. Some useful extreme limits**

To help the comprehension of our discussion in the following sections, let us review here the approximate expressions for  $m_{ee}^{\text{max}}$  and  $m_{ee}^{\text{min}}$  for the two extreme cases of the absolute neutrino mass scale: vanishing  $m_0$  and very large  $m_0$  compared to  $\sqrt{\Delta m_{\text{atm}}^2}$ . The neutrino oscillation parameters are assumed to lie in the ranges given in Eqs.  $(5)$ – $(7)$ . *(i) Vanishing m<sub>0</sub> limit.* For normal mass ordering we have

$$
m_{ee}^{\min}, m_{ee}^{\max} \simeq m_{ee}^{(2)} \mp m_{ee}^{(3)}
$$
  

$$
\simeq \sqrt{\Delta m_{\odot}^2 s_{12}^2 c_{13}^2} \mp \sqrt{\Delta m_{\text{atm}}^2 s_{13}^2}, \tag{20}
$$

where the  $- (+)$  sign corresponds to  $m_{ee}^{\text{min}}$  ( $m_{ee}^{\text{max}}$ ).

For inverted mass ordering we have

$$
m_{ee}^{\min} \simeq m_{ee}^{(1)} - m_{ee}^{(2)} \simeq \sqrt{\Delta m_{\text{atm}}^2} \cos 2\,\theta_{12} c_{13}^2, \tag{21}
$$

$$
m_{ee}^{\text{max}} \simeq m_{ee}^{(1)} + m_{ee}^{(2)} \simeq \sqrt{\Delta m_{\text{atm}}^2} c_{13}^2. \tag{22}
$$

*(ii) Large*  $m_0$  ( $\gg \sqrt{\Delta m_{\text{atm}}^2}$ *) limit*. For normal as well as for inverted mass ordering,

$$
m_{ee}^{\min} \simeq m_{ee}^{(1)} - m_{ee}^{(2)} - m_{ee}^{(3)}
$$
  

$$
\simeq m_0 (c_{13}^2 \cos 2\theta_{12} - s_{13}^2), \tag{23}
$$

$$
m_{ee}^{\max} \simeq m_{ee}^{(1)} + m_{ee}^{(2)} + m_{ee}^{(3)} \simeq m_0.
$$
 (24)



FIG. 2. Maximum and minimum possible values of *mee* as a function of  $m_0$  indicated by the thick solid curves for  $\sin^2\theta_{13}=0$  $(left$  panels) and  $0.02$  (right panels) for normal (upper panels) as well as for inverted (lower panels) mass ordering. We have fixed the other mixing parameters as  $\Delta m_{12}^2 = 5 \times 10^{-5} \text{ eV}^2$ ,  $\tan^2 \theta_{12} = 0.35$ , and  $|\Delta m_{23}^2| = 3 \times 10^{-3} \text{ eV}^2$ . The individual contributions of  $m_{ee}^{(1)}$ ,  $m_{ee}^{(2)}$ , and  $m_{ee}^{(3)}$  are also shown by dashed, dotted, and dash-dotted curves, respectively.

# **III. DEPENDENCE ON THE LIGHTEST NEUTRINO MASS**

In this section we examine how the effective Majorana mass  $m_{ee}$  depends on the lightest neutrino mass  $m_0$ , and clarify the importance of each of the individual contributions  $m_{ee}^{(1)}$ ,  $m_{ee}^{(2)}$ , and  $m_{ee}^{(3)}$  to  $m_{ee}$ . We present in Fig. 2 for normal (upper panels) as well as inverted (lower panels) mass ordering the maximum and minimum values of  $m_{ee}$  as a function of  $m_0$  for vanishing  $\theta_{13}$  (left panels) and  $\sin^2 \theta_{13} = 0.02$  (right panels). In the same plots we also show the individual contributions of  $m_{ee}^{(1)}$ ,  $m_{ee}^{(2)}$ , and  $m_{ee}^{(3)}$  by dashed, dotted, and dash-dotted lines, respectively.

Let us first discuss the case of normal mass ordering. As we can see from the plots in the upper panels of Fig. 2, for smaller values of  $m_0$ ,  $m_{ee}^{(2)}$  is the dominant contribution, whereas for larger values of  $m_0$ ,  $m_{ee}^{(1)}$  dominates over the other contributions. For the typical values of the oscillation parameters allowed by the solar, atmospheric neutrino, and reactor data,  $m_{ee}^{(3)}$  is almost always the smallest contribution to  $m_{ee}$ , being subdominant in  $m_{ee}$ , and it can only be important when there is a large cancellation between  $m_{ee}^{(1)}$  and  $m_{ee}^{(2)}$  .

It is clear that a strong cancellation in  $m_{ee}$  can occur if at least two of  $m_{ee}^{(1)}$ ,  $m_{ee}^{(2)}$ , and  $m_{ee}^{(3)}$  are comparable in magnitude. Just by comparing their magnitudes in the plots in Fig. 2, we can easily see for which values of  $m_0$  a strong cancellation in  $m_{ee}$  can occur. For the case if  $\theta_{13}=0$ ,  $m_{ee}$  can be zero only at one particular value of  $m_0$  [see Fig. 2(a)],



FIG. 3. Isocontour plots of  $m_{ee}$  for  $\sin^2\theta_{13}=0$  for normal mass ordering in the  $\alpha_1$ - $m_0$  plane. We have fixed the other relevant mixing parameters as  $(\Delta m_{12}^2, \tan^2 \theta_{12}) = (2 \times 10^{-5} \text{ eV}^2, 0.2)$  in (a), (5)  $\times 10^{-5}$  eV<sup>2</sup>, 0.35) in (b),  $(5\times10^{-5}$  eV<sup>2</sup>, 0.5), in (c), and (4  $\times 10^{-4}$  eV<sup>2</sup>, 0.6) in (d).

whereas for the case if  $\theta_{13} \neq 0$  *m<sub>ee</sub>* can be zero for some range of  $m_0$  [see Fig. 2(b)]. See Sec. V for more detailed discussion of the dependence of  $m_{ee}^{\text{min}}$  on  $m_0$  and  $\theta_{13}$ .

In the case of inverted mass ordering, the situation changes significantly. Here  $m_{ee}^{(1)} > m_{ee}^{(2)} \ge m_{ee}^{(3)}$  and  $m_{ee}^{\min} \ne 0$ always must satisfy the condition

$$
m_{ee}^{\min} \gtrsim \sqrt{\Delta m_{\text{atm}}^2} \cos 2\theta_{12} \sim 10 \text{ meV},\tag{25}
$$

for any value of  $m_0$  for current allowed parameters from solar and atmospheric neutrino data and no complete cancellation in  $m_{ee}$  is expected as we can see clearly from the plots in the lower panels of Fig. 2. Therefore, if no positive signal of  $0\nu\beta\beta$  is observed down to  $\sim$  10 meV, inverted mass ordering can be excluded as long as neutrinos are Majorana particles.

# **IV. DEPENDENCE ON THE LIGHTEST NEUTRINO MASS AND** *CP* **PHASES**

Let us next discuss how the  $m_{ee}$  dependence on  $m_0$  is related to the two *CP* phases  $\alpha_1$  and  $\alpha_3$ . We present in Fig. 3 isocontour plots of  $m_{ee}$  in the  $m_0$ - $\alpha_1$  plane for vanishing  $\theta_{13}$ , for normal mass ordering, for some values of the solar parameters taken within the allowed ranges given in Eq.  $(7)$ . Note that, in this particular case, there is no dependence on the phase  $\alpha_3$  in our choice of parametrization, which is clear from Eq.  $(11)$ .

First we note that in the plots isocontours are symmetric with respect to  $\alpha_1 / \pi = 0.5$ . Second we note that if  $m_{ee}$  is smaller than a certain value  $m_{ee}^{\text{crit}}$  the isocontours are closed, which means that the possible values of both  $m_0$  and  $\alpha_1$  are bounded to some limited range, which does not include zero.



FIG. 4. Same as Fig. 3(b) but for  $\sin^2\theta_{13} = 0.01$  (left panels) and 0.02 (right panels), for  $\alpha_3=0$  (upper panels),  $\pi/4$  (middle panels), and  $\pi/2$  (lower panels). The dashed vertical lines mark  $\alpha_1 / \pi$  $= 0.5.$ 

The critical value of  $m_{ee}$  under which the contour is a closed one is given by

$$
m_{ee}^{\text{crit}} \simeq m_{ee}^{(2)} = \sqrt{\Delta m_{\odot}^2} s_{12}^2 \simeq (1 - 10) \text{ meV}; \qquad (26)
$$

this dependence is illustrated in Fig. 3. If a positive  $0\nu\beta\beta$ signal is not observed down to these values, this will imply either that  $m_0$  as well as the *CP* phase  $\alpha_1$  are bounded to the limited range within the closed contours shown in Fig. 3 or that neutrinos are not Majorana type particles.

We show in Fig. 4 the same information as in Fig.  $3(b)$ but for  $\sin^2\theta_{13} = 0.01$  (left panels) and 0.02 (right panels) for three different values of  $\alpha_3=0,\pi/4$ , and  $\pi/2$  in the upper, middle, and lower panels, respectively. As we can see from these plots the qualitative behaviors of the contours are very similar to those in Fig. 3(b). This is due to the fact that  $m_{ee}^{(3)}$ , which is the only term that carries the contributions of  $\sin^2\theta_{13}$  and  $\alpha_3$ , is subdominant compared to the other two elements in  $m_{ee}$ . The effect of a nonzero  $\alpha_3$  is to cause some displacement of the position of the symmetry line of the plots from around  $\alpha_1 / \pi = 0.5$  to somewhat smaller values.

Let us here mention the case where  $m_0$  can be independently measured by another experiment such as the KATRIN  $[26]$  tritium decay one. In this case, it is possible to constrain the *CP* phase  $\alpha_1$  by comparing the measured values of  $m_{ee}$ and  $m_0$  provided that  $m_0 \geq 340$  meV, the maximum sensitivity of KATRIN. If a  $0\nu\beta\beta$  decay experiment measures  $m_{ee}$ significantly smaller than  $m_0$  measured by KATRIN, this would imply a nonzero  $CP$  phase  $\alpha_1$ . This is because, for the  $m_0$  values relevant for KATRIN,  $m_{ee} \sim m_0$  if  $\alpha_1 \approx 0$ , but  $m_{ee}$  can be as small as  $\sim 0.1 \times m_0$  if  $\alpha_1 \sim \pi/2$  and if the largest allowed value of  $\theta_{12}$  from the current LMA allowed



FIG. 5. Same as Fig. 3 but for inverted mass ordering. Here we have fixed the atmospheric mass scale to  $\Delta m_{23}^2 = -5 \times 10^{-3} \text{ eV}^2$  in (a), to  $\Delta m_{23}^2 = -3 \times 10^{-3} \text{ eV}^2$  in (b) and (c), and to  $\Delta m_{23}^2 = -1.3$  $\times 10^{-3}$  eV<sup>2</sup> in (d).

region is realized [see Eqs.  $(23)$  and  $(24)$ ]. However, it would still be difficult to say something definite about the value of  $\alpha_1$  for  $10 \le m_0$ /meV $\le$ 340.

Our plots in Figs. 3 and 4 are in agreement with the conclusion presented in Ref.  $[29]$ , that is, either a positive or a negative result in a  $0\nu\beta\beta$  decay experiment can constrain  $m_0$  and  $\alpha_1$  but, since the possible values of  $\alpha_1$  will always include  $\pi/2$ , a nonzero value of  $\alpha_1$  cannot be interpreted as evidence of *CP* violation, even if a positive signal of  $0\nu\beta\beta$ decay is observed. Unfortunately, to be able to say anything more definite on the *CP* phase, independent precise information on  $m_0$  is unavoidable. Moreover, nothing can be concluded about the value of  $\alpha_3$ .

We show in Fig. 5 the same information as in Fig. 3 for inverted mass ordering. Since there is no significant dependence on  $\theta_{13}$  or on  $\alpha_3$  in this case, we show only the curves for vanishing  $\theta_{13}$ . We note from these plots that there is no lower bound for  $m_0$  as long as  $m_{ee} \le 50$  meV, and, moreover,  $\alpha_1$  is less constrained if compared to the case of normal ordering, independently of the values of the other neutrino oscillation parameters.

For the case of normal mass ordering, we have also investigated if the uncertainties in the determination of the solar parameters as well as on  $m_{ee}$  can wash out the determination of a nonzero  $CP$  phase  $\alpha_1$ , expected by the closed contours in Figs. 3 and 4. For four different central values of  $m_{ee}$ , assuming 30% uncertainty in their determination (see Sec. VI for a detailed explanation), we have obtained the region in the  $(\Delta m_{12}^2, \tan^2 \theta_{12})$  plane where  $\alpha_1$  can be constrained to a nonzero value for (i)  $\sin^2\theta_{13} = 0$  and (ii)  $\sin^2\theta_{13} = 0.02$ . This is shown in Fig. 6, where we also have assumed for each point in the  $(\Delta m_{12}^2, \tan^2 \theta_{12})$  plane a 10% uncertainty in the determination of these two parameters. In this plot we have indicated by crosses the set of solar parameters used in Figs.  $3(a) - 3(d)$ .

We observe that for the case of  $\theta_{13}=0$  [see Fig. 6(i)], determination of a nonzero  $\mathbb{CP}$  phase  $\alpha_1$  is possible as long as one can reach the sensitivity  $m_{ee} \leq 5$  meV for the parameter set (d) and  $m_{ee} \leq 1$  meV for sets (b) and (c). On the other hand, in the case where  $\sin^2 \theta_{13} = 0.02$ , as we can see from Fig. 6(ii), a better sensitivity in  $m_{ee}$  is required to establish a nonzero  $\alpha_1$  value for the same parameter set. This is because when  $\theta_{13}$  is nonzero the third element  $m_{ee}^{(3)}$ , which contains another  $CP$  phase  $\alpha_3$ , whose value is assumed to be unknown, comes into play, and this could wash out more efficiently the determination of nonzero  $\alpha_1$  when compared to the case where  $\theta_{13}=0$ .

# **V. DEPENDENCE ON THE LIGHTEST NEUTRINO MASS** AND  $\theta_{13}$

In this and the next sections we focus on the relation among  $m_{ee}$  and some of the yet undetermined mixing parameters. Let us start by discussing the dependence of  $m_{ee}^{\text{min}}$  on  $m_0$  and  $\theta_{13}$ . Here we discuss only the case of normal ordering since the dependence on  $\theta_{13}$  for the inverted case is quite



FIG. 6. Region in the  $(\Delta m_{12}^2, \tan^2 \theta_{12})$  plane where  $\alpha_1$  can be constrained to a nonzero value, indicated by an arrow, for given central values of  $m_{ee}$ =1,2,3 meV, taking into account 30% uncertainty in the determination of  $m_{ee}$  and 10% uncertainty in  $\Delta m_{12}^2$  as well as in tan<sup>2</sup> $\theta_{12}$ . The set of solar parameters used in Figs.  $3(a) - 3(d)$  are indicated by crosses. The allowed region for the LMA MSW solution at  $1\sigma$ ;,  $2\sigma$ ;, and  $3\sigma$  are shown by the shaded area (adapted from Ref.  $[30]$ .



FIG. 7. Isocontour plots of  $m_{ee}^{\text{min}}$  in the  $s_{13}^2$ - $m_0$  plane for different choices of the mixing parameters for normal mass ordering. We note that in the region delimited by thin solid curves  $m_{ee}^{\text{min}}=0$ .

small. We present in Fig. 7, the isocontour plots of  $m_{ee}^{\text{min}}$  in the  $s_{13}^2$ - $m_0$  plane for some different choices of the oscillation parameters.

For vanishing  $\theta_{13}$ , one can have  $m_{ee}^{\text{min}} = 0$  if  $m_{ee}^{(1)} = m_{ee}^{(2)}$ , i.e.,  $m_1 c_{12}^2 = m_2 s_{12}^2$ , which is equivalent to

$$
m_0 = \frac{s_{12}^2}{\sqrt{[\cos 2\theta_{12}]}} \sqrt{\Delta m_\odot^2} \sim 3 \text{ meV},\tag{27}
$$

where we have computed the numerical estimate using the best fitted values of the parameters from the latest solar neutrino data [see Fig. 2(a) and Fig. 7(b)]. Within the current allowed range given in Eq.  $(7)$ , the possible values of  $m_0$  for which we can expect strong cancellation are in the range  $m_0 \approx (0.9-12)$  meV, as we can confirm with the plots in Fig. 7.

For nonzero values of  $\theta_{13}$ , as we can see clearly from Fig. 7,  $m_{ee}^{\text{min}}$  can be zero for some range of  $m_0$ . We can also see that there is a critical value of  $\theta_{13}$  for which  $m_{ee}^{\text{min}}$  is zero with vanishing  $m_0$ . Such a value of  $\theta_{13}$  can be easily estimated by solving  $m_2 c_{13}^2 s_{12}^2 = m_3 s_{13}^2$  with  $m_0 \rightarrow 0$ , which is equivalent to

$$
s_{13}^2 \simeq \sqrt{\frac{\Delta m_{\odot}^2}{\Delta m_{\text{atm}}^2}} s_{12}^2 \sim 0.03
$$
 (28)

for the best fitted parameters from solar as well as atmospheric neutrino data. We note that this is close to the current upper bound on  $s_{13}^2$  allowed by the CHOOZ result [5]. Letting  $\Delta m_{\odot}^2$ ,  $\Delta m_{\text{atm}}^2$ , and  $s_{12}^2$  take any value in the region consistent with the solar and atmospheric neutrino observations given in Eqs. (5) and (7), the range of  $s_{13}^2$  for which strong cancellation can occur is  $s_{13}^2 \approx 0.01 - 0.20$ , which is again consistent with our results in Fig. 7.

We observe that if  $s_{13}^2$  is smaller than the critical value given in Eq.  $(28)$ , the value of  $m_0$  can be strongly constrained to some limited range around the value of  $m_0$  given in Eq. (27), provided that future  $0\nu\beta\beta$  experiments can probe an  $m_{ee}$  value as small as  $\sim \sqrt{\Delta m_{\odot}^2 s_{12}^2}$  independent of whether a positive or negative signal of  $0\nu\beta\beta$  is observed.

# **VI. CONSTRAINING** *m***<sup>0</sup> USING SOLAR NEUTRINO DATA**

Finally, let us discuss how we can constrain  $m_0$  using the solar neutrino parameters. Let us first analyze the case where a positive signal of  $0\nu\beta\beta$  is observed. The value of  $m_{ee}$  has to be extracted from the experimentally measured half-life  $T_{1/2}^{0\nu}$  of the decaying parent nucleus by comparison with the theoretical predictions which rely on nuclear matrix element calculations. This means that the experimental value of  $m_{ee}$ has to be expressed as an interval obtained using the maximum and minimum matrix element predictions.

As mentioned in Sec. II B, typically there is a factor of 3 difference among the results of the matrix element evaluations according to different model assumptions [28]. In order to take such large theoretical uncertainty into account in our estimations, we will first assume that the experimentally measured value of  $m_{ee}$  will be extracted using the mean between the minimum and maximum values of the matrix element calculations, and then attach 30% uncertainty around this value, which corresponds to a factor of  $\sim$  2 between the smallest and the largest theoretically allowed  $m_{ee}$  values for a given value of the observed half-life. This is a somewhat optimistic but reasonable assumption. Hopefully, improvements in the understanding of the underlying nuclear physics effects can decrease this uncertainty even further.

In Fig. 8 we show the isocontours of upper  $(m_0^{\text{max}})$  and lower  $(m_0^{\text{min}})$  bounds on  $m_0$  in units of meV in the  $\tan^2 \theta_{12}$ - $\Delta m_{12}^2$  plane for the case where a positive signal of  $0\nu\beta\beta$  is observed with central values  $m_{ee}$ =10, 5, 3, and 1 meV with a 30% uncertainty. In these plots we have used  $\Delta m_{23}^2 = 3 \times 10^{-3} \text{ eV}^2$  and  $\sin^2 \theta_{13} = 0$ . We do not present plots for  $m_{ee}$  > 10 meV, since in these cases the upper and lower bounds can be analytically estimated as we will see below.

When  $m_0 > \sqrt{\Delta m_{\text{atm}}^2}$  the upper bound on  $m_0$  does not depend much on  $\Delta m_{\odot}^2$  but essentially only on  $\theta_{12}$  [see Eq. (23) in Sec. II C]; it is given by

$$
m_0^{\max} \sim \frac{m_{ee}}{\cos 2\,\theta_{12}},\tag{29}
$$

and the lower bound  $m_0^{\text{min}} \sim m_{ee}$ , independent of the solar parameters in the region compatible with the LMA MSW solution to the solar neutrino problem.

We observe that, as can be seen in Fig. 8, as  $m_{ee}$  decreases, the upper bound lines, which mainly depend on  $\tan^2\theta_{12}$ , are shifted to larger values of  $\theta_{12}$ , decreasing  $m_0^{\text{max}}$ for a given set of  $(\tan^2 \theta_{12}, \Delta m_{12}^2)$ . The lower bound lines, on the other hand, depend more on  $\Delta m_{12}^2$  and there are some regions where no lower bound is obtained. For *mee*  $\gtrsim$ 10 meV or  $m_{ee} \lesssim$ 1 meV there is always a lower bound



FIG. 8. Isocontour plots of upper ( $m_0^{\text{max}}$ , solid curves) and lower  $(m_0^{\text{min}})$ , dashed curves) bounds of  $m_0$  in units of meV in the  $\tan^2 \theta_{12}$ - $\Delta m_{12}^2$  plane for the case where a positive signal of  $0\nu\beta\beta$  is observed with central values  $m_{ee}$  = 10 meV (a), 5  $meV$  (b), 3 meV (c), and 1 meV (d). We assume 30% uncertainty in the determination of  $m_{ee}$ . We fix the other mixing parameters as  $\Delta m_{23}^2 = 3$  $\times 10^{-3}$  eV<sup>2</sup> and sin<sup>2</sup> $\theta_{13}$ =0. The allowed region for the LMA MSW solution is the same as in Fig. 6.

found inside the currently allowed LMA MSW region, whereas for  $1 \leq m_{ee}/\text{meV} \leq 10$  this is not true. The appearance of these no-lower-bound bands comes from the fact that in these regions the solar mass scale alone is sufficient to explain the positive signal observed, even for vanishing  $m_0$ .

In Fig. 9 we repeat the same exercise but for  $\sin^2\theta_{13}$ = 0.02. The most significant effect of a nonzero  $\sin^2\theta_{13}$  is the increase of the size of the no-lower-bound band, which can in some cases stretch over the entire LMA allowed region; otherwise the behavior of the upper and lower bound lines is qualitatively similar to the previous case.

Let us next consider the case where no positive signal is observed. In Fig. 10 we present the same information as in Fig. 8 but for the case where no positive signal of  $0\nu\beta\beta$  is



FIG. 9. Same as Fig. 8 but for  $\sin^2\theta_{13} = 0.02$ .



FIG. 10. Same as Fig. 8 but for the case where no positive signal of  $0\nu\beta\beta$  is observed down to  $m_{ee}$ =10 meV (a), 5 meV (b), 3 meV (c), and  $1 \text{ meV (d)}$ .

observed down to  $m_{ee}$ =10 meV (a), 5 meV (b), 3 meV (c), and  $1 \text{ meV}$  (d). It is assumed that, when no positive signal is observed, for a given bound on the half-life time, the bounds on *mee* are extracted using the smallest nuclear matrix element prediction which leads to the largest  $m_{ee}$  value [see Eq.  $(10)$ ]. We can see that the qualitative behavior of the isocontours for the upper bound is similar to that in Fig. 8 but it is

different for the trend of the lower bound curves. Compared to the case where positive  $0\nu\beta\beta$  signal is obtained, it is more difficult to put a lower bound on  $m_0$ . This can be easily understood from Fig.  $2(a)$ . We note that, unless we can constrain  $m_{ee}$  down to  $\sim$ 3 meV, no lower bound on  $m_0$  is obtained. In Fig. 11 we present the same information as in Fig. 10 but for  $\sin^2\theta_{13} = 0.02$ . Again, the qualitative behavior of



FIG. 11. Same as Fig. 10 but for  $\sin^2\theta_{13}$  $= 0.02.$ 

the isocontours is similar to the case of  $\sin^2 \theta_{13} = 0$ . The difference from the previous case presented in Fig. 10 is that the constraint on  $m_0$  becomes somewhat weaker, leading to larger upper bounds and smaller lower bounds for a given set of  $(\tan^2 \theta_{12}, \Delta m_{12}^2)$ .

Finally, let us also comment on the case of inverted ordering. For this case, we can easily estimate the upper as well as the lower bound from the analytic expressions as well as from the lower panels of Fig. 2. Let us look at Figs.  $2(c)$  and  $2(d)$ . First of all, if inverted ordering is the case, the observed value of  $m_{ee}$  in a  $0 \nu \beta \beta$  decay experiment must be larger than the value given in Eq.  $(25)$ , as already mentioned in Sec. III. If the observed  $m_{ee}$  is smaller than  $\sqrt{\Delta m_{\text{atm}}^2}c_{13}^2$ [see Eq.  $(22)$ ] then there is no lower bound on  $m_0$ , whereas the upper bound is given by the same expression for the case of normal ordering, by Eq.  $(29)$ . If the observed  $m_{ee}$  value is larger than  $\sqrt{\Delta m_{\text{atm}}^2}c_{13}^2$ , then the upper as well as lower bounds are given by the same expression as in the case of normal ordering, which is already discussed in this section.

#### **VII. DISCUSSION AND CONCLUSIONS**

We have studied how the nonoscillation neutrino parameters, which cannot be extracted from the oscillation analysis, the absolute neutrino mass scale and two *CP* violating Majorana phases, can be accessed by the positive or negative signal of future  $0\nu\beta\beta$  decay experiments. We have carried this out by choosing various different sets of mixing parameters which are varied within the parameter region currently allowed by the solar, atmospheric, and reactor neutrino experiments.

In the future, the KATRIN experiment expects to directly inspect  $m_0$  down to  $\sim$ 340 meV [26], while there are several proposed astrophysical measurements on the temperature perturbation in the early universe imprinted in the cosmic microwave background radiation, such as the ones that can be performed by MAP (microwave anisotropy probe)  $[31]$ and Planck [32], which can probe  $m_0$  down to  $\sim$ 300 meV [33], where the expected sensitivity suffers from the uncertainty coming from cosmological parameters. It is expected that future supernova neutrino measurements can probe  $m_0$ down to at most  $\sim$ (2–3) eV [34].

Our analysis permits us to conclude that, if these experiments measure  $m_0 \ge 300$  meV, then either a positive signal of  $0\nu\beta\beta$  decay compatible with  $m_{ee} \ge 30$  meV must be observed in the near future or neutrinos are Dirac particles. This is simply because  $m_{ee}^{\text{min}} \sim m_0 \cos 2\theta_{12}$  [see Eq. (23) in Sec. II C] and cos  $2\theta_{12} \gtrsim 0.1$  from the current allowed LMA parameter region given in Eq.  $(7)$ .

On the other hand, if these experiments do not observe any positive signal of  $m_0 \gtrsim 300$  meV, results from future  $0\nu\beta\beta$  decay experiments combined with more precise values of the neutrino oscillation parameters, especially the solar ones  $(\Delta m_{12}^2, \tan^2 \theta_{12})$ , which can be precisely determined by the KamLAND experiment [8], will place more stringent bounds on  $m_0$  for the Majorana case provided that a sensitivity of  $m_{ee} \leq 30$  meV is achieved. To be more specific, if a positive signal is observed around  $m_{ee} = 10$  meV (assuming a 30% uncertainty on the determination of  $m_{ee}$ ), we estimate  $3 \leq m_0$ /meV  $\leq 65$  at 95% C.L.; on the other hand, if no signal is observed down to  $m_{ee} = 10$  meV, then  $m_0 \le 55$  meV at 95% C.L. Allowing for a more optimistic sensitivity, a positive signal observed around  $m_{ee} = 3$  meV or no signal seen down to 3 meV would mean  $m_0 \le 25$  meV at 95% C.L. These bounds can be improved by a better determination of  $\tan^2\theta_{12}$ ,  $\Delta m_{12}^2$ , and  $\sin^2\theta_{13}$  as can be clearly seen in Figs. 8–11, as well as by a reduction of the uncertainties in the theoretical calculations of the nuclear matrix elements.

We finally conclude that it is possible to constrain the *CP* violating phase  $\alpha_1$  to values around  $\pi/2$  if (1)  $m_0$  is large enough to be detected by KATRIN or by astrophysical observations and future  $0\nu\beta\beta$  decay experiments observe  $m_{ee}$ close to its minimum value or (2) future  $0\nu\beta\beta$  decay experiments can achieve a sensitivity on  $m_{ee} \leq 5$  meV, depending on the values of the solar parameters and on the uncertainty on  $m_{ee}$  (Fig. 6), independently of whether a positive or a negative signal is observed. Unfortunately, nothing can be known about  $\alpha_3$ .

Despite the fact that the parameter region inspected in this work differs from the one considered in Ref.  $\left[29\right]$ , we have found, in agreement with this reference, that evidence for *CP* violation cannot be observed by future  $0\nu\beta\beta$  decay experiments, since the possible values of  $\alpha_1$ , whenever it can be constrained to some nonzero value, always include  $\pi/2$ , unless  $m_0$  can be independently determined by some other experiment.

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