

Muon anomalous $g-2$ and gauged $L_\mu-L_\tau$ models

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In this paper we study the Z' contribution to $g-2$ of the muon anomalous magnetic dipole moment in gauged $U(1)_{L_\mu-L_\tau}$ models. Here L_i are the lepton numbers. We find that there are three classes of models which can produce a large value of $g-2$ to account for the possible discrepancy between the experimental data and the standard model prediction. The three classes are as follows: (a) Models with an exact $U(1)_{L_\mu-L_\tau}$. In these models, Z' is massless. The new gauge interaction coupling $ea/\cos\theta_W$ is constrained to be $0.8 \times 10^{-3} < |a| < 2.24 \times 10^{-3}$. (b) Models with broken $U(1)_{L_\mu-L_\tau}$ and the breaking scale is not related to electroweak symmetry breaking scale. The Z' gauge boson is massive. The allowed range of the coupling and the Z' mass are constrained, but Z' mass can be large. (c) The $U(1)_{L_\mu-L_\tau}$ is broken and the breaking scale is related to the electroweak scale. In this case the Z' mass is constrained to be ~ 1.2 GeV. We find that there are interesting experimental signatures in $\mu^+\mu^- \rightarrow \mu^+\mu^-, \tau^+\tau^-$ in these models.

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I. INTRODUCTION

Recently an experiment at Brookhaven National Lab (BNL) [1] has measured the muon anomalous magnetic dipole moment with $a_\mu^{\text{exp}} = (g-2)/2 = (11\,659\,202 \pm 14 \pm 6) \times 10^{-10}$. This value differs from the standard model (SM) prediction in Refs. [2,3] by 2.6σ :

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (42.6 \pm 16.5) \times 10^{-10}. \quad (1)$$

At present the experimental errors are still too large to claim a real deviation. There are also uncertainties from theoretical calculations, in particular contributions from hadrons at loop levels are not well determined [4]. Improvements from both experimental measurements and theoretical calculations are needed. If this difference is true, it is an indication of new physics beyond the SM. Many authors have discussed possible implications for new physics beyond the SM [5]. Some interesting constraints have been obtained. In this paper we study the implications of a large Δa_μ on models with gauged $L_\mu-L_\tau$. Here L_i is the i lepton number.

$L_\mu-L_\tau$ gauge models are some of the simplest models beyond the SM which contain an additional Z' boson. Without enlarging the fermion contents in the SM, there are only three types of $U(1)$ symmetries which can be gauged from anomaly cancellation requirement. These symmetries are

$$(i) \ U(1)_{L_e-L_\mu}; \quad (ii) \ U(1)_{L_e-L_\tau}; \quad (iii) \ U(1)_{L_\mu-L_\tau}. \quad (2)$$

Some experimental consequences of these models have been studied in Refs. [6,7]. There are stringent constraints on the parameters of models based on (i) and (ii) because the Z' couple to electrons. It is difficult to generate a large enough value for Δa_μ in Eq. (1). On the other hand, for models based on (iii) there are limited data available to constrain relevant parameters. It is possible to have a large Δa_μ .

In $U(1)_{L_\mu-L_\tau}$ models, only the second and third generations of leptons are affected, whereas all other SM particles are not. The transformation properties of leptons under the $SU(3)_C \times SU(2)_L \times U(1)_Y$ SM gauge group and the $U(1)_{L_\mu-L_\tau}$ gauge group are

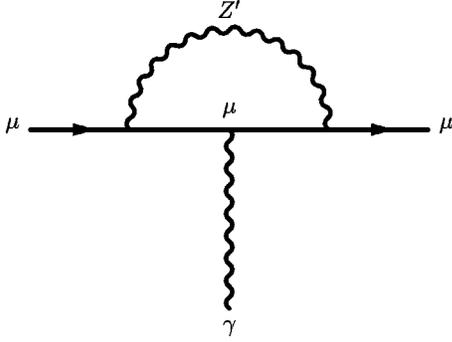
$$\begin{aligned} L_L^e &: (1,2,-1)(0) & e_R &: (1,1,-2)(0) \\ L_L^\mu &: (1,2,-1)(2a) & \mu_R &: (1,1,-2)(2a) \\ L_L^\tau &: (1,2,-1)(-2a) & \tau_R &: (1,1,-2)(-2a) \end{aligned} \quad (3)$$

where the numbers in the first and the second brackets indicate the transformation properties under the SM gauge group and the $U(1)_{L_\mu-L_\tau}$ group, respectively. The numbers in the second bracket will be indicated as Y' . The covariant derivative in terms of the photon field A_μ , the Z_μ field, and the Z'_μ field is given as

$$D_\mu = \partial_\mu + ieQA_\mu + i\frac{e}{s_W c_W}(I_3 - s_W^2 Q)Z_\mu + i\frac{e}{c_W}\frac{Y'}{2}Z'_\mu, \quad (4)$$

where $s_W = \sin\theta_W$, $c_W = \cos\theta_W$. We have normalized the Z' coupling to the $U(1)_Y$ charge coupling e/c_W .

The $U(1)_{L_\mu-L_\tau}$ may be an exact symmetry or a broken one at some scale which may or may not be related to the electroweak breaking scale. One can classify three types of models based on $U(1)_{L_\mu-L_\tau}$ as: (a) $U(1)_{L_\mu-L_\tau}$ is an exact symmetry; (b) $U(1)_{L_\mu-L_\tau}$ is broken and the breaking scale is not related to the electroweak scale; and (c) $U(1)_{L_\mu-L_\tau}$ is broken and the breaking scale is related to the electroweak scale. In all these cases Δa_μ receives contribution from Z' exchange at one loop level. In case (c), there is in general $Z-Z'$ mixing. Electroweak precision tests from various experiments constrain the mixing severely. We will concentrate

FIG. 1. Feynman diagram which generates a nonzero Δa_μ .

on models where the Z - Z' mixing is naturally zero at tree level, such that the related constraints are automatically satisfied.

II. THE MUON MAGNETIC DIPOLE MOMENT IN $U(1)_{L_\mu-L_\tau}$ MODELS

A. Δa_μ in case (a)

In this case, there is no need to introduce other new particles. It is the simplest $U(1)_{L_\mu-L_\tau}$ model. Z' couplings to μ and τ are given by

$$L = \frac{ea}{c_W} (\bar{\mu} \gamma^\mu \mu - \bar{\tau} \gamma^\mu \tau) Z'_\mu. \quad (5)$$

The Feynman diagram which generates a nonzero Δa_μ is shown in Fig. 1. The contribution to Δa_μ is given by

$$\Delta a_\mu = a_\mu^{\text{SM}+\text{new}} - a_\mu^{\text{SM}} = \frac{\alpha_{\text{em}}}{2\pi} \frac{a^2}{c_W^2}. \quad (6)$$

The 2σ range consistent with Eq. (1) is determined to be

$$0.8 \times 10^{-3} < |a| < 2.24 \times 10^{-3}. \quad (7)$$

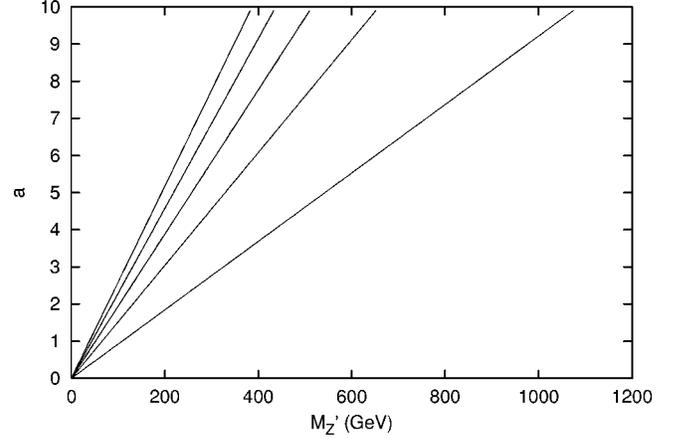
The τ also receives the same amount of correction to the anomalous magnetic dipole moment.

With a nonzero value for a , all processes involving μ and τ will be affected. However, because the coupling parameter a is small, the effects are all small.

B. Δa_μ in case (b)

The simplest model for case (b) can be realized by just introducing a SM singlet scalar S but transforms nontrivially under $U(1)_{L_\mu-L_\tau}$, $S: (1,1,0)(a)$. In this case when S develops a nonzero vacuum expectation value v_S , the Z' boson becomes massive with $m_{Z'}^2 = e^2 a^2 v_S^2 / 2c_W^2$. In this model, there is no Z and Z' mixing at tree level. The Z' couplings to μ and τ are the same as that in Eq. (5). One obtains a nonzero Δa_μ through the same diagram in Fig. 1 for case (a), but with a nonzero Z' mass. We have

$$\Delta a_\mu = \frac{\alpha_{\text{em}}}{2\pi} \frac{a^2}{c_W^2} \int_0^1 dx \frac{2m_\mu^2 x^2 (1-x)}{x^2 m_\mu^2 + (1-x)m_{Z'}^2}. \quad (8)$$

FIG. 2. Δa_μ on the a vs $m_{Z'}$ plane in case (b). The lines from left to right are for Δa_μ away from its central value at $+2\sigma$, $+1\sigma$, 0 , -1σ , and -2σ , respectively.

Requiring the new contribution to produce the value in Eq. (1), the allowed values of a and $m_{Z'}^2$ are constrained. The results are shown in Fig. 2. We see that there is a large allowed region where a large value of Δa_μ can be produced.

In the limit $m_{Z'}^2 \gg m_\mu^2$,

$$\Delta a_\mu = \frac{\alpha_{\text{em}}}{2\pi} \frac{a^2}{c_W^2} \frac{2}{3} \frac{m_\mu^2}{m_{Z'}^2}. \quad (9)$$

To produce the value in eq. (1), one obtains $9.2 \times 10^{-3} < a/m_{Z'} (\text{GeV}) < 25.8 \times 10^{-3}$. The breaking scale v_S of the $U(1)_{L_\mu-L_\tau}$ is of order ~ 200 (GeV). Changing m_μ to m_τ in Eq. (8), one obtains the tauon $g-2$. We note that for large enough $m_{Z'}$, only the parameter $a/m_{Z'}$ is constrained from Δa_μ . Of course one should not let a to be arbitrarily large, because a large a will invalidate perturbation calculations carried out here. We will limit a such that $\alpha_{\text{em}} a^2 \leq 1$. The effects of Z' on $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$, $\tau^+ \tau^-$ turn out to be quite dramatic in this case and will be discussed in the next section.

C. Δa_μ in case (c)

There are many ways to realize case (c). Here we study the effect on Δa_μ in the model discussed in Ref. [7]. In this model there are two more SM Higgs doublets $\phi_{2,3}$ in addition to the usual SM doublet ϕ_1 . The Higgs doublets SM gauge group and the $U(1)_{L_\mu-L_\tau}$ quantum numbers are

$$\phi_1: (1,2,1)(0); \quad \phi_2: (1,2,1)(4a); \quad \phi_3: (1,2,1)(-4a). \quad (10)$$

Because $\phi_{2,3}$ transform nontrivially under the SM and $U(1)_{L_\mu-L_\tau}$, in general after symmetry breaking there are Z and Z' mixing. This mixing can be eliminated by applying an unbroken discrete symmetry

$$A_\mu \rightarrow A_\mu; \quad Z_\mu \rightarrow Z_\mu; \quad Z'_\mu \rightarrow -Z'_\mu;$$

$$L_L^\mu(\mu_R) \leftrightarrow L_L^\tau(\tau_R); \quad \phi_2 \leftrightarrow \phi_3; \quad (11)$$

$$\langle \phi_2 \rangle = v_2 = \langle \phi_3 \rangle = v_3.$$

The Z' mass in this model is given by

$$m_{Z'}^2 = 8 \frac{e^2}{c_W^2} a^2 v_2^2. \quad (12)$$

The Yukawa couplings of the $\phi_{2,3}$, consistent with the discrete symmetry, are given by

$$L_{\text{Yuk}} = \lambda (\bar{L}_L^\mu \mu_R \phi_1 + \bar{L}_L^\tau \tau_R \phi_1) + \lambda' (\bar{L}_L^\mu \tau_R \phi_2 + \bar{L}_L^\tau \mu_R \phi_3). \quad (13)$$

The above Yukawa coupling produces a nondiagonal mass matrix for μ and τ . In the mass eigenstate bases, Z' couplings to μ , τ , and their associated neutrinos are given by

$$L = \frac{ea}{\cos\theta_W} [\bar{\mu} \gamma^\mu \tau + \bar{\tau} \gamma^\mu \mu] Z'_\mu + \frac{ea}{2\cos\theta_W} [\bar{\nu}_\mu \gamma^\mu (1 - \gamma_5) \nu_\tau + \bar{\nu}_\tau \gamma^\mu (1 - \gamma_5) \nu_\mu] Z'_\mu. \quad (14)$$

There are very stringent constraints on this model. First, $a/m_{Z'}$ is restricted from the expression of the Z' mass formula in Eq. (12) since v_2 have to be less than $\sqrt{v_1^2 + v_2^2 + v_3^2} = 246$ GeV which determines the W boson mass. We have

$$\frac{a^2}{m_{Z'}^2} > \frac{1}{32 \tan^2 \theta_W m_W^2}. \quad (15)$$

Second, there is a new contribution to $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ by exchanging Z' with

$$R \equiv \frac{\Gamma(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau(\bar{\nu}_\tau \nu_\mu))}{\Gamma(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)_{\text{SM}}} = 1 + \xi g_1(z) + 2\xi^2 g_2(z),$$

$$\Delta a_\mu = \frac{\alpha_{\text{em}}}{2\pi} \frac{a^2}{c_W^2} 2m_\mu \int_0^1 dx \frac{x(1-x) \{ 2(m_\tau - m_\mu) + m_\mu x \} - \frac{1}{2} \left(\frac{m_\tau - m_\mu}{m_{Z'}} \right)^2 x^2 (m_\tau - m_\mu + x m_\mu)}{x^2 m_\mu^2 + (1-x)m_{Z'}^2 + x(m_\tau^2 - m_\mu^2)}. \quad (17)$$

In the limit $m_{Z'} \gg m_\tau$,

$$\Delta a_\mu = \frac{\alpha_{\text{em}}}{2\pi} \frac{a^2}{c_W^2} \frac{2m_\mu m_\tau}{m_{Z'}^2}. \quad (18)$$

The above constraints are so restrictive that within the experimentally allowed value for $R-1$ and the constraint of Eq. (15), it is not possible to produce Δa_μ given in Eq. (1). This simple model is ruled out.

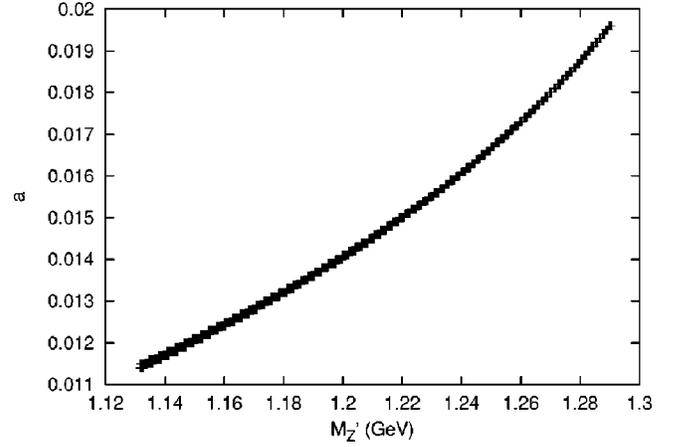


FIG. 3. The allowed region on the a vs $m_{Z'}$ plane with Δa_μ and R varying in their 2σ allowed ranges for case (c).

$$g_1(z) = -\frac{1}{3z^4} [z(12 - 12z - 5z^2) + 6(2 - 3z + z^3) \log|1 - z|], \quad (16)$$

$$g_2(z) = \frac{1}{z^4} [z(6 - 3z + z^2) + 6(1 - z) \log|1 - z|],$$

where $z = m_\tau^2/m_{Z'}^2$, and $\xi = 2\sqrt{2}\pi\alpha_{\text{em}}/(G_F m_{Z'}^2)(a^2/c_W^2)$. The factor of 2 in front of $g_2(z)$ comes from the fact that $\tau^- \rightarrow \mu^- \bar{\nu}_\tau \nu_\mu$ is not distinguished from $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ in experiments, and we need to sum over these two modes.

Experimentally the SM prediction is very close to the observation for $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$. The new contribution must be smaller than the experimental error [8] on R , $\Delta R = 0.004(1\sigma)$. This provides a very tight constraint on the allowed parameters.

Finally there is a constraint from Δa_μ . The Feynman diagram generating a nonzero Δa_μ is similar to Fig. 1 with the replacement of μ by τ for the fermion in the loop. We have

The above problem, however, can be easily overcome by lifting the constraint from Eq. (15). This can be achieved by introducing a SM singlet S for case (b). The introduction of this singlet scalar does not cause Z - Z' mixing and does not change the Z' couplings to μ, τ and their associated neutrinos, but will introduce a new contribution to the Z' mass. The new Z' mass is given by

$$m_{Z'}^2 = 8 \frac{e^2 a^2}{c_W^2} v_2^2 + \frac{1}{2} \frac{e^2 a^2}{c_W^2} v_S^2. \quad (19)$$

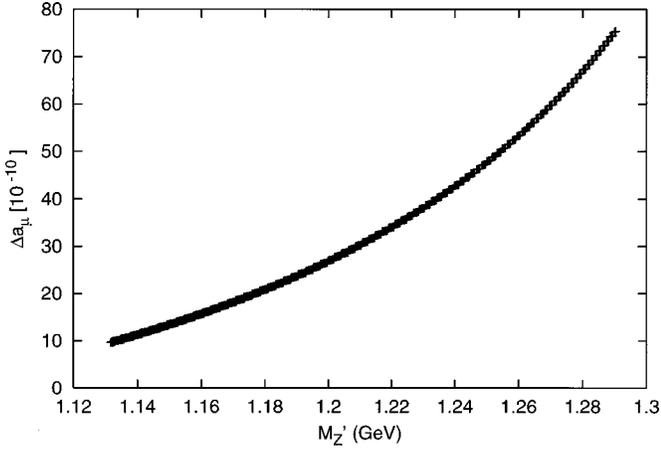


FIG. 4. Δa_μ in terms of $m_{Z'}$ for the allowed parameters in the R constraints in case (c).

Because v_S is not fixed, the constraint on $a/m_{Z'}$ from Eq. (15) is no longer applicable.

In this modified model, it is possible to obtain a large enough value for Δa_μ in Eq. (1). However, the allowed parameter space is still very restrictive. The results are shown in Figs. 3 and 4. In Fig. 3 we show the allowed region of a and $m_{Z'}$, and in Fig. 4 we show the allowed Δa_μ as a function of $m_{Z'}$. To produce a large enough Δa_μ to account for the value in Eq. (1), the Z' mass is forced to be around 1.2 GeV. Note that the region $m_{Z'} < 0.5$ GeV is ruled out by the nonobservation of two body decay mode $\tau \rightarrow \mu Z'$ [7].

The τ anomalous magnetic dipole moment also receives a similar correction. In the heavy Z' limit, $\Delta a_\tau = \Delta a_\mu$. This model also has interesting signatures at muon colliders which will be discussed in the following section.

III. $\mu^+ \mu^- \rightarrow \mu^+ \mu^-, \tau^+ \tau^-$ IN $U(1)_{L_\mu-L_\tau}$ MODELS

In this section we study experimental signatures of the $U(1)_{L_\mu-L_\tau}$ models at a muon collider using the processes $\mu^+ \mu^- \rightarrow \mu^+ \mu^-, \tau^+ \tau^-$. The Feynman diagrams which contribute to these processes are shown in Figs. 5 and 6. For cases (a) and (b) there are two new diagrams for $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ besides the SM ones, but there is only one new diagram for $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ shown in Fig. 5. For case (c), there is no contribution from Z' exchange for $\mu^+ \mu^-$

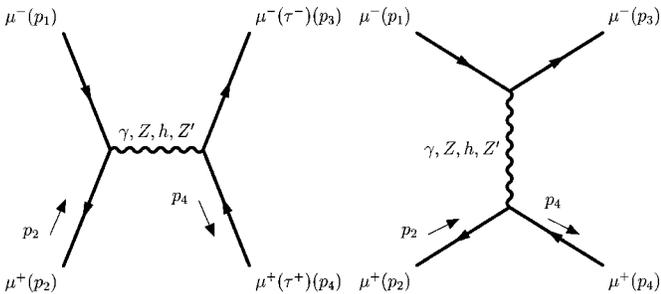


FIG. 5. Feynman diagrams for processes $\mu^+ \mu^- \rightarrow \mu^+ \mu^- (\tau^+ \tau^-)$ in case (b).

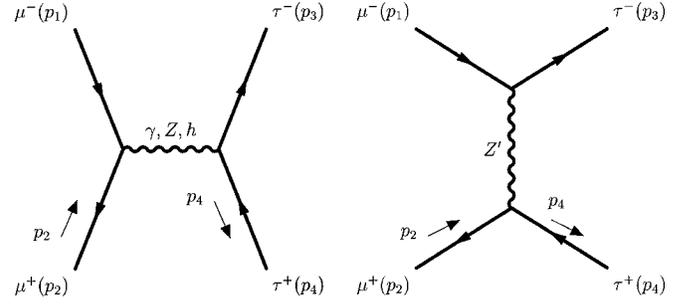


FIG. 6. Feynman diagrams for process $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ in case (c).

$\rightarrow \mu^+ \mu^-$, but there is one for $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ shown in Fig. 6.

In Fig. 7 we show the cross section for $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ in case (b), where each line represents constant Δa_μ . We fixed $\sqrt{s} = 500$ GeV, and a corresponding SM cross section is 451.49 (fb). There are s -channel photon, Z , Z' , and Higgs contributions. It turns out that the Higgs contributions are negligible, if its mass is far from \sqrt{s} . In our calculations we have used Higgs mass close to the experimental lower bound. When \sqrt{s} is close to $m_{Z'}$, there is a resonance, even though we have used a finite width $\Gamma_{Z'}$ calculated in the model with $\Gamma_{Z'} = \Gamma(Z' \rightarrow \nu_{\mu(\tau)} \bar{\nu}_{\mu(\tau)}) + \Gamma(Z' \rightarrow \mu(\tau) \bar{\mu}(\bar{\tau}))$ because it is small. We can clearly see the resonance effects. The cross section can be enhanced quite dramatically compared to the SM. Therefore the muon colliders can clearly show the new Z' effects if case (b) is realized in nature.

In Fig. 8 the cross section for $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ is shown in case (b). Since we neglected the muon mass, the t -channel contribution shows collinear singularity. We imposed angular cuts $|\cos(\theta_{13})| < 0.5$ when obtaining the total cross section. The corresponding cross section for the SM is 1153.7 (fb) for $\sqrt{s} = 500$ GeV. In contrast to the $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ process the cross section does not decrease fast as $m_{Z'}$ increases due to the large t -channel contributions.

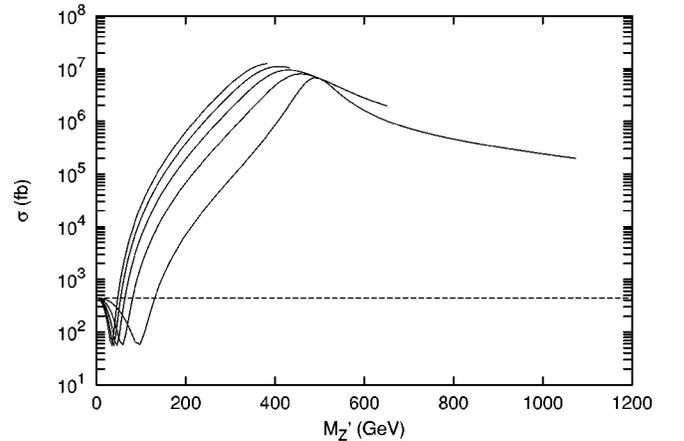


FIG. 7. Cross section for $\mu^+ \mu^- \rightarrow \tau^+ \tau^-$ as a function of $m_{Z'}$ for $\sqrt{s} = 500$ GeV in case (b). The lines from left to right correspond to Δa_μ away from its central value at $+2\sigma$, $+1\sigma$, 0 , -1σ , and -2σ , respectively. The horizontal dashed line is the SM prediction.

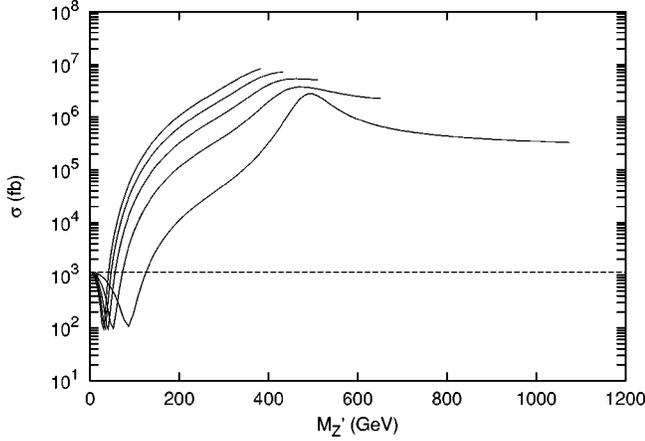


FIG. 8. Cross section for $\mu^+\mu^-\rightarrow\mu^+\mu^-$ as a function of $m_{Z'}$ for $\sqrt{s}=500$ GeV in case (b). The lines from left to right correspond to Δa_μ away from its central value at $+2\sigma$, $+1\sigma$, 0 , -1σ , and -2σ , respectively. The horizontal dashed line is the SM prediction.

In Fig. 9 we show the cross section of $\mu^+\mu^-\rightarrow\tau^+\tau^-$ as a function of $m_{Z'}$ for case (c) for the parameters that satisfy the Δa_μ constraint. Assuming the design luminosity 50 (fb^{-1}) per year, we expect about 1000 deficit in the number of $\tau^+\tau^-$ production events compared to the SM prediction. We also note that this is also in contrast to case (b) where $m_{Z'}$ can be large and the cross section can be highly enhanced compared to the SM case. Therefore we can see that the muon colliders can easily discriminate the three different realizations of Z' models as well as the SM.

IV. DISCUSSIONS AND CONCLUSIONS

In this paper we have shown that the gauged $U(1)_{L_\mu-L_\tau}$ models may contribute significantly to the anomalous muon magnetic dipole moment. It is possible to produce a large enough value to account for the discrepancy between in SM prediction in Refs. [2,3] and experimental measurement from BNL. The relevant parameters are tightly constrained. The Z' gauge boson mass can vary from zero to large mass depending on how the $U(1)_{L_\mu-L_\tau}$ model manifests itself in nature. We have discussed three different cases. We find that in all cases there are allowed parameters within which a large enough muon anomalous magnetic dipole moment given in Eq. (1) can be generated. In case (a) the Z' coupling parameter a is restricted to be in the range $0.8\times 10^{-3}<|a|<2.24\times 10^{-3}$. In case (b), the constraints on a and $m_{Z'}$ are corre-

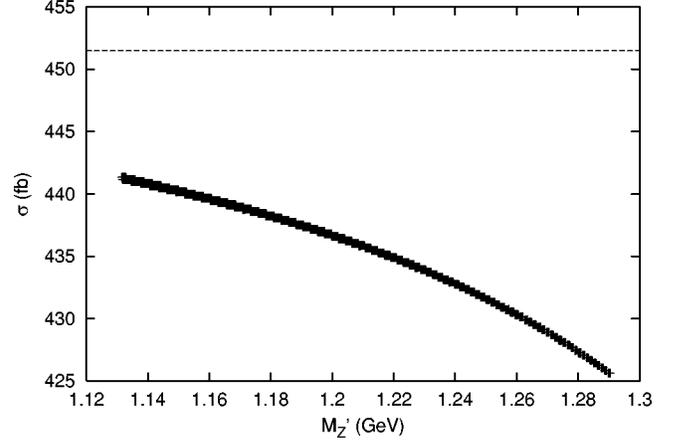


FIG. 9. Cross section for $\mu^+\mu^-\rightarrow\tau^+\tau^-$ as a function of $m_{Z'}$ for $\sqrt{s}=500$ GeV in case (c). The horizontal dashed line is the SM prediction.

lated. In the heavy Z' limit, $a/m_{Z'}$ is restricted to be in the range $9.2\times 10^{-3}<a/m_{Z'}(\text{GeV})<25.8\times 10^{-3}$. In case (c), the constraints on the a and $m_{Z'}$ are even more restrictive. The allowed Z' mass is restricted to be around 1.2 GeV.

In all the models discussed, the electron anomalous magnetic dipole moment is not affected by Z' exchange because no Z - Z' mixing was introduced. If there were Z - Z' mixing, Δa_e would also be affected. The τ magnetic dipole moment is constrained. We find that in case (a), $\Delta a_\tau = \Delta a_\mu$; in case (b), in the limit of large Z' mass $\Delta a_\tau \approx (m_\tau/m_\mu)^2 \Delta a_\mu$; and in case (c), in the limit of large Z' mass $\Delta a_\tau \approx \Delta a_\mu$.

Within the allowed parameter space, there are also other interesting predictions. We have studied several signatures of these models at muon colliders. At muon colliders there may be large effects for processes $\mu^+\mu^-\rightarrow\mu^+\mu^-$, $\tau^+\tau^-$. It is possible to distinguish the SM from different $U(1)_{L_\mu-L_\tau}$ models. Future muon colliders can provide interesting clues about these models.

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