# Measurement of electron-neutrino electron elastic scattering

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The cross section for the elastic scattering reaction  $\nu_e + e^- \rightarrow \nu_e + e^-$  was measured by the Liquid Scintillator Neutrino Detector using a  $\mu^+$  decay-at-rest  $\nu_e$  beam at the Los Alamos Neutron Science Center. The standard model of electroweak physics predicts a large destructive interference between the charge current and neutral current channels for this reaction. The measured cross section,  $\sigma_{\nu_e e^-} = [10.1 \pm 1.1(\text{stat}) \pm 1.0(\text{syst})] \times E_{\nu_e} (\text{MeV}) \times 10^{-45} \text{ cm}^2$ , agrees well with standard model expectations. The measured value of the interference parameter,  $I = -1.01 \pm 0.13(\text{stat}) \pm 0.12(\text{syst})$ , is in good agreement with the standard model expectation of  $I^{SM} = -1.09$ . Limits are placed on neutrino flavor-changing neutral currents. An upper limit on the muon-neutrino magnetic moment of  $6.8 \times 10^{-10} \mu_{Bohr}$  is obtained using the  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  fluxes from  $\pi^+$  and  $\mu^+$  decay.

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### I. INTRODUCTION

Neutrino-electron elastic scattering is a simple, purely leptonic weak process that can provide precise tests of the standard model (SM) of electroweak interactions. Measurements of the reactions  $\nu_{\mu} + e^- \rightarrow \nu_{\mu} + e^-$  and  $\bar{\nu}_{\mu} + e^- \rightarrow \bar{\nu}_{\mu}$  $+ e^-$  have been used to determine the vector and axial vector electron-Z couplings,  $g_V$  and  $g_A$  [1–3]. These reactions proceed solely via the neutral current (NC) channel. In contrast, the reaction  $\nu_e + e^- \rightarrow \nu_e + e^-$  proceeds via both the charged current (CC) and neutral current channels. This reaction is of interest primarily because it is one of the few reactions for which the SM predicts a large destructive interference between these two channels. In this paper, we report a measurement of this reaction that is in good agreement with the SM and with the previous measurement [4].

The differential cross sections for  $\nu_{\mu}$  scattering on electrons can be written

$$\frac{d\sigma^{\nu_{\mu}}}{dy} = \sigma_0 [g_L^2 + g_R^2 (1-y)^2]$$
(1)

for  $E_{\nu} \ge m_e$ , where  $\sigma_0 = G_F^2 s/4\pi$ ,  $s = 2m_e E_{\nu}$ ,  $y = E_e/E_{\nu}$ ,  $g_L = g_V + g_A$  and  $g_R = g_V - g_A$ . In the SM,  $g_V = -\frac{1}{2} + 2\sin^2\theta_W$  and  $g_A = -\frac{1}{2}$ . The total cross section is then

$$\sigma^{\nu_{\mu}} = \sigma_0 \left( g_L^2 + \frac{g_R^2}{3} \right). \tag{2}$$

For  $\overline{\nu}_{\mu}$  scattering on electrons  $g_L$  and  $g_R$  are interchanged so that

$$\sigma^{\bar{\nu}_{\mu}} = \sigma_0 \left( g_R^2 + \frac{g_L^2}{3} \right). \tag{3}$$

For scattering of  $\nu_e$  on electrons the presence of the CC diagram results in a differential cross section of

$$\frac{d\sigma^{\nu_e}}{dy} = \sigma_0[(g_L + 2)^2 + g_R^2(1 - y)^2]$$
(4)

and a total cross section

$$\sigma^{\nu_e} = \sigma_0 \bigg[ (g_L + 2)^2 + \frac{g_R^2}{3} \bigg].$$
 (5)

To make explicit the interference of the NC and CC, we rewrite this as

$$\sigma^{\nu_e} = \sigma^{CC} + \sigma^I + \sigma^{NC}, \tag{6}$$

where  $\sigma^{CC} = 4\sigma_0$ ,  $\sigma^{NC} = \sigma_0(g_L^2 + g_R^2/3)$  and  $\sigma^I = 2I\sigma_0$ . In the SM  $I = 2g_L = -2 + 4\sin^2\theta_W$  and  $\sigma^{NC} = \sigma_0(1 - 4\sin^2\theta_W + \frac{16}{3}\sin^4\theta_W)$ . Assuming  $\sin^2\theta_W = 0.23$ , we get I = -1.1. Thus there is a substantial negative interference between the NC and CC terms. Including radiation correction [5] and retain-

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ing terms in the mass of the electron in the cross section formula, we obtain  $I^{SM} = -1.09$  and  $\sigma^{NC} = 0.37\sigma_0$ .

The measured value of the interference term can be used to set limits on neutrino flavor-changing neutral currents (FCNC) [6]. Such currents would not be detectable in neutrino experiments which measure a pure NC process since the flavor of the outgoing neutrino is not observed. The interference term, however, depends on the interference of the CC with the flavor conserving part of the NC.

Neutrino-electron elastic scattering can also be used to measure certain intrinsic electromagnetic properties of the neutrino. Neutrinos with magnetic moments will scatter electromagnetically on electrons. For electrons with recoil energy greater than T, the cross section for single-photon exchange dipole scattering is given by

$$\sigma^{EM}(E_{\nu}) = f^2 \pi r_0^2 [T/E_{\nu} - \ln(T/E_{\nu}) - 1], \qquad (7)$$

where  $r_0$  is the classical electron radius ( $r_0 = 2.82 \times 10^{-13}$  cm) and *f* is the ratio of the neutrino magnetic moment to the electron Bohr magneton. The present experiment can set upper limits on both the  $\nu_e$  magnetic moment and the  $\nu_{\mu}$  magnetic moment because it observes scattering of  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  as well as  $\nu_e$  on electrons. However, only the upper limit obtained on the  $\nu_{\mu}$  magnetic moment is competitive with previous laboratory limits [1,4].

We also place limits on anomalous contributions to the Lorentz and Dirac structure of the scattering amplitude, which would be manifested as changes in the electromagnetic form factors [7] and, in particular, as an effective neutrino charge radius [8]. The weak NC coupling,  $g_V$ , would shift to  $g_V+2\delta$  where  $\delta = (\sqrt{2}\pi\alpha/3G_F)\langle r^2 \rangle = (2.39 \times 10^{30} \text{ cm}^{-2})\langle r^2 \rangle$  and  $\langle r^2 \rangle$  is the effective mean squared charge radius of the neutrino. As defined,  $\langle r^2 \rangle$  is gauge dependent and not necessarily positive. It provides a procedure, however, for parametrizing certain not-standard contributions to neutrino scattering. Our measurement of  $g_V$  in elastic scattering provides a limit on internal electromagnetic structure at the level of  $10^{-16}$  cm.

The interference of the NC (Z exchange) and CC (W exchange) terms can be studied in several other reactions, including  $\nu_{\mu}N \rightarrow \nu_{\mu}\mu^{+}\mu^{-}N$ ,  $\bar{\nu}_{e}e^{-} \rightarrow \bar{\nu}_{e}e^{-}$  and  $e^{+}e^{-} \rightarrow \gamma \nu \bar{\nu}$ . Neutrino trident production,  $\nu_{\mu}N \rightarrow \nu_{\mu}\mu^{+}\mu^{-}N$ , was first clearly observed by the CHARM II experiment, but this experiment was not sensitive enough to demonstrate destructive interference [9]. CCFR saw destructive interference and was able to rule out a pure W exchange interaction [10]. A more recent measurement by the NuTeV experiment, however, could not distinguish between W exchange alone and the SM [11]. Further, they note that earlier analyses of trident production did not consider diffractive sources. The cross section for  $\bar{\nu}_{e} + e^{-} \rightarrow \bar{\nu}_{e} + e^{-}$  was measured in a reactor experiment and found to be in agreement with the SM but also consistent, within errors, with a CC interaction [12].

The reaction  $e^+e^- \rightarrow \gamma \nu \overline{\nu}$  has been extensively studied at the CERN  $e^+e^-$  collider LEP [13]. Near the  $Z^0$ , the NC term dominates and the interference term is small. At higher energies the interference term can contribute as much as

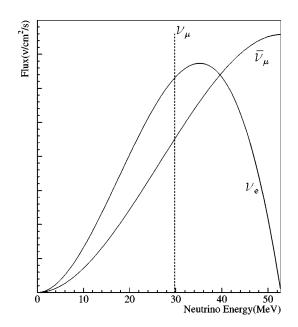


FIG. 1. Flux shape of neutrinos from pion and muon decay at rest.

25%, but is also sensitive to the event selection criteria used. The LEP2 measurements agree well with the SM and have been used to set limits on various possible new physics processes, but we are not aware of any explicit measurements of the interference term.

## **II. THE NEUTRINO SOURCE**

The data reported here were obtained between 1994 and 1998 by the Liquid Scintillator Neutrino Detector (LSND) at the Los Alamos Neutron Science Center (LANSCE) using neutrinos produced at the A6 proton beam stop. The neutrino source is described in detail elsewhere [14]. In 1994 and 1995 the beam stop consisted of a 30 cm water target surrounded by steel shielding and followed by a copper beam dump. The high-intensity 798 MeV proton beam from the linear accelerator generated a large pion flux from the water target. The flux of  $\nu_e$  used for the measurements reported here arise from the decay at rest (DAR) of stopped  $\pi^+$  and  $\mu^+$ . This decay chain yields almost equal intensities of  $\nu_e$ ,  $\bar{\nu}_{\mu}$  and  $\nu_{\mu}$  with the well-determined energy spectra shown in Fig. 1.

After the 1995 run the beam stop was substantially modified for accelerator production of tritium (APT) tests. The most significant change for the analysis presented in this paper was the replacement of the water target by tungsten and other materials with high atomic number. This resulted in reduced  $\pi^+$  production and a lower DAR neutrino flux, largely due to the change in the neutron to proton ratio in the target.

The corresponding decay chain for  $\pi^-$  and  $\mu^-$  is highly suppressed due to three factors. First, production of  $\pi^-$  is smaller than for  $\pi^+$ . Second,  $\pi^-$  which stop are absorbed by nuclear interactions. Finally, most  $\mu^-$  which stop are absorbed before they can decay. These stopped  $\mu^-$  arise from  $\pi^-$  which decay in flight (DIF).

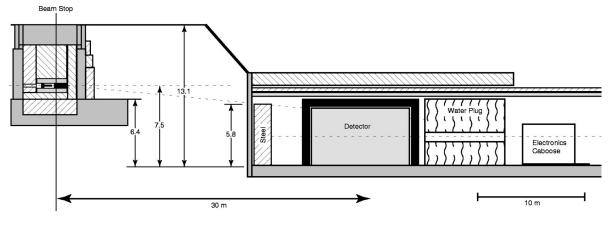


FIG. 2. Detector enclosure and target area configuration, elevation view.

The LANSCE beam dump has been used as the neutrino source for previous experiments [15–17]. A calibration experiment [18] measured the rate of stopped  $\mu^+$  from a lowintensity proton beam incident on an instrumented beam stop. The rate of stopped  $\mu^+$  per incident proton was measured as a function of several variables and used to fine-tune a beam dump simulation program [19]. The simulation program can then be used to calculate the flux for any particular beam dump configuration. The calibration experiment determined the DAR flux to  $\pm 7\%$  for the proton energies and beam stop configurations used at LANSCE. This uncertainty provides the largest source of systematic error for the cross sections presented here. The LANSCE proton beam typically had a current of 800  $\mu$ A at the beam stop. For 1994 and 1995 the energy was approximately 770 MeV at the beam stop due to energy loss in upstream targets. The integrated beam current was 5904 C in 1994 and 7081 C in 1995. The calculated ratio of stopped  $\mu^+$  per proton was 0.090 and 0.084 for 1994 and 1995, respectively, with the lower ratio for 1995 arising because the water target was out for 32% of the 1995 data. Upstream targets contributed 1.4% to the DAR flux in 1994 and 1995. The DAR  $\nu_{e}$  flux averaged over the LSND detector was then  $3.08 \times 10^{13}$  cm<sup>-2</sup> for 1994 and  $3.45 \times 10^{13}$  cm<sup>-2</sup> for 1995.

The 1996–1998 data was obtained with the APT beam stop. There were no upstream targets for almost all of the data taking. The integrated beam current was 3789 C in 1996, 7181 C in 1997 and 3155 C in 1998. The calculated ratio of stopped  $\mu^+$  per incident proton was 0.069, 0.068, and 0.067 respectively in 1996, 1997 and 1998. The DAR  $\nu_e$  flux average over the LSND detector was  $1.32 \times 10^{13}$  cm<sup>-2</sup> for 1996,  $2.73 \times 10^{13}$  cm<sup>-2</sup> for 1997 and  $1.18 \times 10^{13}$  cm<sup>-2</sup> for 1998. For the full data sample used in this paper the  $\nu_e$  flux is  $11.76 \times 10^{13}$  cm<sup>-2</sup>.

## **III. THE LSND DETECTOR**

The detector is located 29.8 m downstream of the proton beam stop at an angle of  $12^{\circ}$  to the proton beam. Figure 2 shows a side-view of the setup. Approximately 2000 g/cm<sup>2</sup> of shielding above the detector attenuates the hadronic component of cosmic rays to a negligible level. The detector is also well shielded from the beam stop so that beamassociated neutrons are attenuated to a negligible level. Enclosing the detector, except on the bottom, is a highly efficient liquid scintillator veto shield which is essential to reduce contributions from the cosmic ray muon background to a low level. Reference [14] provides a detailed description of the detector, veto, and data acquisition system which we briefly review here.

The detector is an approximately cylindrical tank containing 167 tons of liquid scintillator and viewed by 1220 uniformly spaced 8 in. Hamamatsu photomultiplier tubes (PMT) covering 25% of the surface inside the tank wall. When the deposited energy in the tank exceeds a threshold of approximately 4 MeV electron-equivalent energy and there are fewer than 4 PMT hits in the veto shield, the digitized time and pulse height of each of these PMTs (and of each of the 292 veto shield PMTs) are recorded. A veto, imposed for 15.2  $\mu$ s following the firing of >5 veto PMTs, substantially reduces  $(10^{-3})$  the large number of background events arising from the decay of cosmic ray muons that stop in the detector. Activity in the detector or veto shield during the 51.2  $\mu$ s preceding a primary trigger is also recorded provided there are >17 detector PMT hits or >5 veto PMT hits. This activity information is used in the analysis to reject events arising from muon decay. Data after the primary event are recorded for 1 ms with a threshold of 21 PMTs (approximately 0.7 MeV electron-equivalent energy). This low threshold is used for the detection of 2.2 MeV  $\gamma$  from neutron capture on free protons. In the present analysis this information is used to help identify events induced by cosmic ray neutrons. The detector operates without reference to the beam spill, but the state of the beam is recorded with the event. Approximately 94% of the data is taken between beam spills. This allows an accurate measurement and subtraction of cosmic ray background surviving the event selection criteria.

Most triggers due to electrons from stopped muon decays (Michel electrons) are identified by a preceding activity produced by the decay muon. Occasionally, however, the muon will not satisfy the activity threshold of >17 detector PMT hits or >5 veto PMT hits. For several LSND analyses, including the present one, it is desirable to further reduce the number of unidentified Michel electrons. Therefore, for data recorded after 1994 all PMT information was recorded for a period of 6  $\mu$ s (2.7 muon lifetimes) preceding certain primary events. This "lookback" information was recorded for primary events with >300 PMT hits and no activity within the past 35  $\mu$ s (20  $\mu$ s) for 1995 data (1996–1998 data). For the present analysis this "lookback" information is used to further reduce the cosmic ray muon background.

The detector scintillator consists of mineral oil (CH<sub>2</sub>) in which is dissolved a small concentration (0.031 g/l) of b-PBD [20]. This mixture allows the separation of Čerenkov light and scintillation light and produces about 33 photoelectrons per MeV of electron energy deposited in the oil. The combination of the two sources of light provides direction information for relativistic particles and makes particle identification (PID) possible. Note that the oil consists almost entirely of carbon and hydrogen. Isotopically the carbon is 1.1%  $^{13}$ C and 98.9%  $^{12}$ C.

The veto shield encloses the detector on all sides except the bottom. Additional counters were placed below the veto shield before the 1994 run to reduce cosmic ray background entering through the bottom support structure. These counters around the bottom support structure are referred to as bottom counters. More bottom counters were added after the 1995 run. The main veto shield [21] consists of a 15-cm layer of liquid scintillator in an external tank and 15 cm of lead shot in an internal tank. This combination of active and passive shielding tags cosmic ray muons that stop in the lead shot. A veto inefficiency <10<sup>-5</sup> is achieved with this detector for incident charged particles.

## **IV. ANALYSIS TECHNIQUES**

Each event is reconstructed using the hit time and pulse height of all hit PMTs in the detector [14]. The present analysis relies on the reconstructed energy, position, direction, and two PID parameters,  $\chi'_{tot}$  and  $\alpha$ , as described later in this section. The particle direction is determined from the Čerenkov cone. The parameters  $\chi'_{tot}$  and  $\alpha$  are used to distinguish electron events from events arising from interactions of cosmic ray neutrons in the detector. Fortunately, it is possible to directly measure the response of the detector to electrons and neutrons in the energy range of interest for this analysis by using copious control data samples. We also use a Monte Carlo simulation, LSNDMC [22], to simulate events in the detector using GEANT.

The response of the detector to electrons was determined from a large, essentially pure sample of electrons (and positrons) from the decay of stopped cosmic ray  $\mu^{\pm}$  in the detector. The known energy spectra for electrons from muon decay was used to determine the absolute energy calibration, including its small variation over the volume of the detector. The energy resolution was determined from the shape of the electron energy spectrum and was found to be 6.6% at the 52.8 MeV end point. The position and direction resolution obtained from the LSNDMC simulation are 27 cm and 17°, respectively, for electrons from  $\nu e$  elastic scattering in the energy region above 18 MeV. The accuracy of the direction measurement is discussed more in Sec. VI since the measurement of the angular distribution of electrons is crucial for the analysis presented in this paper. Electrons from  $\nu e$  elastic scattering are sharply peaked along the incident neutrino direction, while electrons from other neutrino processes have a broad angular distribution that peaks in the backward direction.

There are no tracking devices in the LSND detector. Thus, event positions must be determined solely from the PMT information. The reconstruction process determines an event position by minimizing a function  $\chi_r$  which is based on the time of each PMT hit corrected for the travel time of light from the assumed event position to the PMT [14]. The procedure used in several previous analyses systematically shifted event positions away from the center of the detector and thus effectively reduced the fiducial volume [23]. The reconstruction procedure has been analyzed in detail and an improved reconstruction procedure was developed which reduces this systematic shift and provides substantially better position resolution. This procedure also provides results which agree well with positions obtained from the event likelihood procedure described in Ref. [24]. In the analysis presented in this paper, a fiducial cut is imposed by requiring D>35 cm, where D is the distance between the reconstructed event position and the surface tangent to the faces of the PMTs. Events near the bottom of the detector (y <-120 cm) are also removed, as discussed in Sec. V.

The particle identification procedure is designed to separate particles with velocities well above Čerenkov threshold from particles below Čerenkov threshold. The procedure makes use of the four parameters defined in Ref. [14]. Briefly,  $\chi_r$  and  $\chi_a$  are the quantities minimized for the determination of the event position and direction,  $\chi_t$  is the fraction of PMT hits that occur more than 12 ns after the fitted event time and  $\chi_{tot}$  is proportional to the product of  $\chi_r$ ,  $\chi_a$ and  $\chi_t$ .

Several previous LSND analyses [23,25,26] have used  $\chi_{tot}$  for particle identification. The distribution of  $\chi_{tot}$  for electrons, however, has a small variation with electron energy and with the position of the event. Therefore, in this paper, we used a modified variable,  $\chi'_{tot}$ , with a mean of zero and sigma of one, independent of the electron energy and position. We also used the variable,  $\alpha$ , which is based on the event likelihood procedures discussed in Ref. [24]. It is similar to the parameter  $\rho$  discussed there, which is based on the ratio of Cerenkov to scintillator light. The parameter  $\alpha$  varies from 0 to 1 and peaks at one for electrons and at 0.3 for neutrons. The combination  $\chi_{\alpha} = \chi'_{tot} + 10(1-\alpha)$  provides better separation of electrons and neutrons than  $\chi'_{tot}$  by itself.

Figure 3(a) shows the  $\chi'_{tot}$  distribution for electrons from stopping  $\mu$  decay and for cosmic ray neutrons with electron equivalent energies in the  $18 < E_e < 50$  MeV range. Neutrons, after thermalizing, undergo a capture reaction,  $n+p \rightarrow d$  $+\gamma$ . The 2.2 MeV  $\gamma$ 's are used to select a clean sample of neutron events. For a neutron  $E_e$  is the equivalent electron energy corresponding to the observed total charge. Figure 3(b) shows the  $\chi_{\alpha}$  distribution for the same events. In the present analysis we eliminate most cosmic ray neutron background by requiring  $\chi_{\alpha} < 4.0$ . We note that a modest particle

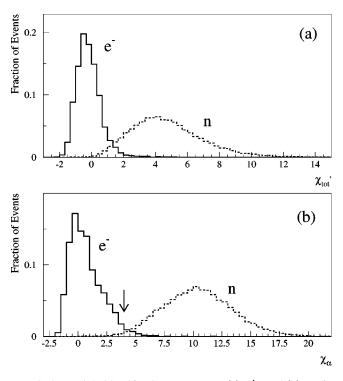


FIG. 3. Particle identification parameters (a)  $\chi'_{tot}$  and (b)  $\chi_{\alpha}$  for electrons and neutrons. In the present analysis we require  $\chi_{\alpha} < 4.0$  as indicated by the arrow in (b).

identification requirement was imposed in the initial data processing that created the samples analyzed here. The effect of this requirement is also included in the analysis.

Beam-off data taken between beam spills play a crucial role in the analysis of this experiment. Most event selection criteria are designed to reduce the cosmic ray background while retaining high acceptance for the neutrino process of interest. Cosmic ray background which remains after all selection criteria have been applied is well measured with the beam-off data and subtracted using the duty ratio, the ratio of beam-on time to beam-off time. The subtraction was performed separately for each year's data using the measured duty ratio for that year. The ratio averaged over the data full sample was 0.0632. Beam-on and beam-off data have been compared to determine if there are any differences other than those arising from neutrino interactions. Any differences are small and the 1.1% uncertainty in the duty ratio introduces a negligible effect in the present analysis.

The beam-off subtraction procedure is illustrated in Fig. 4 for the y distribution of the sample of inclusive electron events discussed in the next section. Figure 4(a) shows the y distribution for beam-on events and for beam-off events corrected by the duty ratio. The beam-off background is largest at low y due to the absence of a veto below the detector. Figure 4(b) compares the y distribution of the beam-excess events with that expected from neutrino processes. The agreement is excellent.

### V. INCLUSIVE ELECTRON SAMPLE

Beam-associated electrons below 52 MeV in LSND arise from four major neutrino processes:

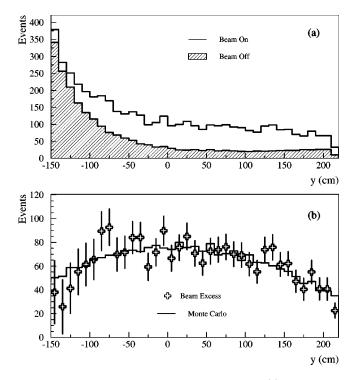


FIG. 4. The *y* distribution of inclusive electrons (a) for beam-on events and for beam-off events corrected by the duty ratio (cross hatched), and (b) beam-excess events compared with Monte Carlo expectations (solid line).

<sup>12</sup>C(ν<sub>e</sub>, e<sup>-</sup>)<sup>12</sup>N<sub>g.s.</sub>, <sup>12</sup>C(ν<sub>e</sub>, e<sup>-</sup>)<sup>12</sup>N\*, <sup>13</sup>C(ν<sub>e</sub>, e<sup>-</sup>)<sup>13</sup>X and νe elastic scattering. We distinguish transitions to the ground states (<sup>12</sup>N<sub>g.s.</sub>) and excited states (<sup>12</sup>N\*) of nitrogen because the ground state has a clear signature from its β-decay. In this section we describe the selection criteria used to obtain a clean sample of inclusive electron events arising from neutrino interactions in the detector. The next section describes how the angular distribution of these electrons is used to obtain a νe elastic sample and, in addition, to determine the background due to other neutrino processes remaining in that sample.

The selection criteria and corresponding efficiencies for electrons from  $\nu e$  elastic scattering are shown in Table I. A lower limit on the electron energy of 18.0 MeV eliminates the large cosmic ray background from  ${}^{12}B\beta$ -decay as well as most 15.1 MeV gamma rays from the NC excitation of carbon. The <sup>12</sup>B nuclei arise from the absorption of stopped  $\mu^$ on <sup>12</sup>C nuclei in the detector. The requirement y > -120 cm removes a small region at the bottom of the detector for which the cosmic ray background is relatively high, as shown in Fig. 4(a). The reconstructed electron position is also required to be a distance D>35 cm from the surface tangent to the faces of the PMTs. There are  $2.72 \times 10^{31}$  electrons within this fiducial volume. We show in the next section that we are able to make a good measurement of the direction for electrons within this fiducial volume. The fiducial volume efficiency, defined to be the ratio of the number of events reconstructed within the fiducial volume to the actual number within this volume, was determined to be  $0.918 \pm 0.055$ . This efficiency is less than one because there

TABLE I. The electron selection criteria and corresponding efficiencies for the reaction  $\nu_e + e \rightarrow \nu_e + e$ .

Quantity	Criteria	Efficiency
Fiducial volume	D>35 cm,	$0.918 \pm 0.055$
	y > -120  cm	
Electron energy	$18 < E_e < 50 \text{ MeV}$	$0.442 \pm 0.010$
Particle ID	$\chi_{lpha} < 4$	$0.940 \pm 0.018$
In-time veto	<4 PMTs	$0.988 \pm 0.010$
Past activity	See text	$0.635 \pm 0.012$
Future activity	$\Delta t_f > 8.8 \ \mu s$	$0.991 \pm 0.003$
Future beta	See Text	$0.997 \pm 0.003$
Lookback	likelihood	$0.994 \pm 0.004$
DAQ and tape dead time	_	$0.958 \pm 0.010$
Direction	$\cos \theta > 0.9$	$0.832 \pm 0.020$
Total		$0.187 \pm 0.014$

is a systematic shift of reconstructed event positions away from the center of the detector as discussed in Sec. IV.

Several selection criteria are designed to further reject cosmic ray induced events. Events with more than three veto PMT hits or any bottom counter coincidence during the 500 ns event window are eliminated. The past activity cut is designed to reject most electron events arising from cosmic ray muons which stop in the detector and decay. This background has a time dependence given by the 2.2  $\mu$ s muon lifetime. The past activity selection criteria reject all events

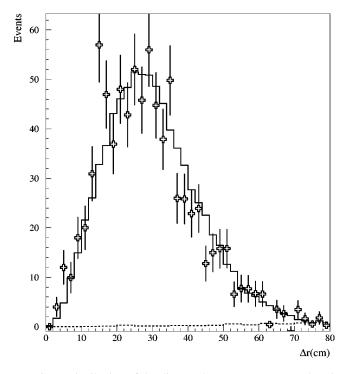


FIG. 5. Distribution of the distance between reconstructed positions of  $e^-$  and  $e^+$  for beam-excess events in the  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$  sample compared with Monte Carlo expectations (solid line). The calculated accidental contribution is shown by the dashed line.

TABLE II. Criteria to select  $e^+$  from N<sub>g.s.</sub> beta decay and corresponding efficiencies for the reaction  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$ .

Quantity	Criteria	Efficiency
$\beta$ decay time	52 $\mu$ s <t<60 ms<="" td=""><td><math>0.974 \pm 0.002</math></td></t<60>	$0.974 \pm 0.002$
Spatial correlation	$\Delta r < 0.7 \text{ m}$	$0.992 \pm 0.008$
PMT threshold	>100 for 1994,	$0.860 \pm 0.011$
	>75 after 1994	
Fiducial volume	D > 0 cm	$0.986 \pm 0.010$
Trigger veto	$>15.1 \ \mu s$	$0.760 \pm 0.010$
Intime veto	<4 PMTs	$0.988 \pm 0.010$
DAQ dead time		$0.977 \pm 0.010$
Total		$0.601 \pm 0.015$

with activity within the past 20  $\mu$ s with >5 veto PMT hits or >17 detector PMT hits. We also reject any event with a past activity within 51  $\mu$ s with >5 veto PMT hits and >500 detector PMT hits. A small (0.5%) loss of efficiency arises from a cut (made during initial data processing) on past activities that are spatially correlated with the primary event, within 30  $\mu$ s of the primary event and have >4 veto PMT hits.

Muons which are misidentified as electrons are removed by requiring that there be no future activity consistent with a Michel electron. Any event with a future activity with fewer than 4 veto PMT hits and more than 50 detector PMT hits within 8.8  $\mu$ s is rejected.

Electrons from the reaction  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$  can be

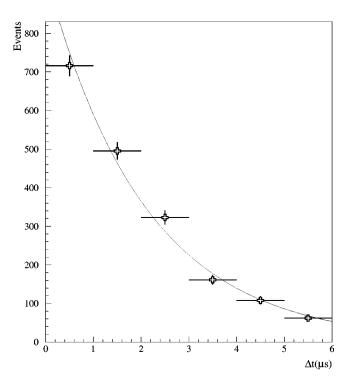


FIG. 6. The distribution of time between the primary and the veto signal for beam-off events rejected using the "lookback" information compared with a curve corresponding to the muon life-time.

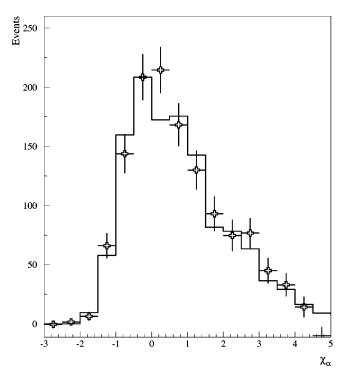


FIG. 7. The  $\chi_{\alpha}$  distribution of the beam-excess inclusive electron sample. The histogram shows the  $\chi_{\alpha}$  distribution of Michel electrons weighted and normalized to the same area.

identified by the positron from the  $\beta$ -decay of the  ${}^{12}N_{g.s.}$ . Figure 5 shows the distance between the reconstructed electron and positron positions. Table II shows the  $\beta$  selection criteria and corresponding efficiencies. Reference [25] discusses in detail the measurement of the reaction  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$ . For the  $\nu_e e$  analysis we reject events with an identified  $\beta$ .

Cosmic ray muons which fire <6 veto PMTs ( $10^{-3}$  probability) and stop in the iron walls of the detector will not register as past activities. Some of the decay electrons will radiate photons which will enter the detector and be reconstructed as electrons within the fiducial volume. In previous analyses we simply relied on the beam-off subtraction procedure to remove this background. Here we use the 'lookback' information described in Sec. III to reject events from this source. This results in slightly smaller statistical errors in the final beam-excess sample.

For primary events with >300 PMT hits and no activity within the past 35  $\mu$ s (20  $\mu$ s) for 1995 data (1996–1998 data), we recorded all PMT information for the 6  $\mu$ s interval preceding the event. Muons with <6 veto PMT hits will appear in this ''lookback'' interval as a cluster of veto PMT hits spatially correlated with the primary event. The distribution of time between the veto signals and the primary event should be consistent with the muon lifetime, and the distributions of veto PMT hits and veto pulse height should be consistent with that measured for muons producing <6 veto PMT hits. We developed a likelihood procedure based on these distributions which allowed us to reduce the beam-off background by 15% with only a 0.6% loss of efficiency for

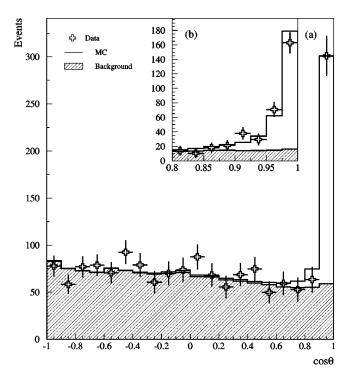


FIG. 8. The observed  $\cos \theta$  distribution of the beam-excess inclusive electron sample (a) for all angles and (b) for  $\cos \theta > 0.8$ . The solid line shows a fit to the data by the method explained in the text. The hatched histogram shows the estimated background level from neutrino reactions other than  $\nu e$  elastic scattering.

neutrino events [27]. Figure 6 shows the time between the veto signal and the primary for rejected events.

The acceptances for the past activity, the future activity, the ''lookback'' and the in-time veto cuts are obtained by applying these cuts to a large sample of random events triggered with the laser used for detector calibration. These laser events are spread uniformly through the run and thus average over the small variation in run conditions. The acceptance for the 15.1  $\mu$ s trigger veto is included in the past activity efficiency.

A sample of Michel electrons was analyzed to obtain the acceptance of electrons for the PID cut. Figure 7 compares the  $\chi_{\alpha}$  distribution of the inclusive electron sample with a weighted Michel electron sample. The agreement is excellent. To eliminate any energy dependence, the Michel electrons are given weights as a function of energy so that the weighted spectrum agrees with the energy spectrum of  $\nu_e e$  elastic scattering. The acceptance, however, is very insensitive to the assumed energy spectrum. The beam-excess distribution shown in Fig. 7 is obtained by subtracting the beam-off distribution from the beam-on distribution as discussed in Sec. III.

### VI. ELASTIC ELECTRON SAMPLE

Figure 8 shows the observed distribution in  $\cos \theta$  for the beam-excess inclusive electron sample, where  $\theta$  is the angle between the reconstructed electron direction and the incident neutrino direction. The large forward peak arises from  $\nu e$  elastic scattering. Figure 9 shows the expected distributions

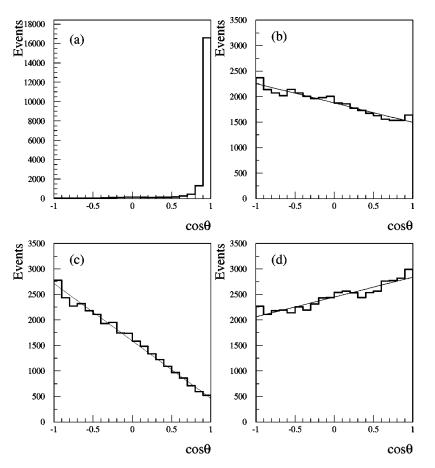


FIG. 9. The expected distributions of  $\cos \theta$  for (a)  $\nu e^-$  elastic scattering, (b)  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$ , (c)  ${}^{12}C(\nu_e, e^-){}^{12}N^*$ , and (d)  ${}^{13}C(\nu_e, e^-){}^{13}X$ . Straight line fits are shown in (b), (c) and (d).

in  $\cos \theta$  for the primary sources of electrons in the sample: *ve* elastic scattering,  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$ ,  ${}^{12}C(\nu_e, e^-){}^{12}N^*$ , and  ${}^{13}C(\nu_e, e^-){}^{13}X$ . These distributions have been obtained with the LSNDMC simulation package [22] and thus include the angular smearing due to experimental effects. Before smearing, the expected distribution for all processes other than  $\nu e$  elastic scattering varies gradually with  $\cos \theta$ , and a function of the form  $A + B \cos \theta$  provides a good fit to the distribution. As seen in Fig. 9, there is only a small deviation from linearity after experimental smearing. Most ve elastic events satisfy the selection criteria  $\cos \theta > 0.9$ . The background from neutrino carbon scattering under the elastic peak (cos  $\theta > 0.9$ ) is obtained by fitting the observed distribution in Fig. 8 to the sum of a term with the shape expected for ve elastic scattering shown in Fig. 9 and a background term which differs slightly from the form  $A + B \cos \theta$  due to the experimental smearing. From the fit we calculate a background of 59 $\pm$ 5 events with cos  $\theta$ >0.9. Measurements of  $\nu_e C$  scattering, including angular distributions for  ${}^{12}C(\nu_e, e^-){}^{12}N_{g.s.}$  and  ${}^{12}C(\nu_e, e^-){}^{12}N^*$ , will be reported in a separate paper [28].

Figure 10 shows the observed and expected electron energy distributions for beam-excess events with  $\cos \theta > 0.9$ . Figure 11 shows the observed and expected spatial distributions of the same events. Both figures show good agreement with expectations. Table III provides a breakdown of the number of events with  $\cos \theta > 0.9$ , the calculated backgrounds, the acceptance, the neutrino flux and the resulting flux-averaged cross section for  $\nu_e e$  elastic scattering. The dominant sources of systematic error in the cross section are the neutrino flux (7%) discussed in Sec. II, the effective fiducial volume (6%) discussed in Sec. IV, the neutrino background with  $\cos \theta > 0.9$  (3%), particle identification (2%), the energy scale (2%) and the direction determination (2%).

All three types of DAR neutrinos  $(\nu_e, \nu_\mu, \text{ and } \overline{\nu_\mu})$  elastically scatter off electrons in the detector, but the rate is dominated by  $\nu_e e^-$  scattering [29]. The contribution due to DIF  $\nu_{\mu}$  and  $\overline{\nu}_{\mu}$  scattering on electrons is small, approximately 6 events from  $\nu_{\mu}$  scattering and <1 event from  $\bar{\nu}_{\mu}$ scattering. For the  $\nu_e$  electron elastic scattering analysis, events from  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  scattering are background and thus we subtract their contributions, shown in Table III, from the observed elastic scattering signal. Other experiments have measured cross sections for both  $\nu_{\mu}$  and  $\overline{\nu}_{\mu}$  scattering that are in good agreement with expectations [30]. The numbers in Table III for  $\nu_{\mu}$  and  $\overline{\nu}_{\mu}$  are obtained from the theoretical cross sections rather than the measured ones, although the analysis is insensitive to this choice. We also note that the sum of the contributions from  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  scattering depends only weakly on the value of  $\sin^2 \theta_W$ .

### VII. PHYSICS RESULTS

The measured cross section, with its explicit linear energy dependence, is

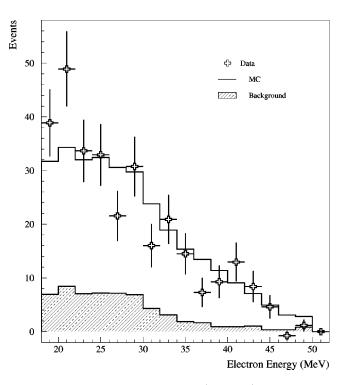


FIG. 10. The observed and expected (solid line) distributions of beam-excess events with  $\cos \theta > 0.9$ . The expected distribution includes the estimated contribution from  $\nu C$  (cross hatched) as well as  $\nu e$  elastic scattering.

$$\sigma_{\nu_e e^-} = [10.1 \pm 1.1(\text{stat}) \pm 1.0(\text{syst})] \times E_{\nu_e}(\text{MeV})$$
$$\times 10^{-45} \text{ cm}^2. \tag{8}$$

This agrees well with the value measured by E225 at Los Alamos [4],

$$\sigma_{\nu_e e^-} = [10.0 \pm 1.5(\text{stat}) \pm 0.9(\text{syst})] \times E_{\nu_e}(\text{MeV})$$
$$\times 10^{-45} \text{ cm}^2 \tag{9}$$

and with SM expectations. The effective electron-Z couplings, including radiative corrections, are  $g_V = -0.0397$  and  $g_A = -0.5064$  in the SM [31]. We then obtain, retaining terms in  $m_e$  in the cross section formula [5,32,33],

$$\sigma_{\nu_e e}^{SM} = 9.3 \times E_{\nu_e} (\text{MeV}) \times 10^{-45} \text{ cm}^2.$$
(10)

The  $\nu_e + e^- \rightarrow \nu_e + e^-$  cross section can be separated into its component parts: CC, NC and interference. Solving for the interference term and substituting the SM calculated values for NC and CC cross sections, the interference term can be written as

 $I = \sigma^{I}/2\sigma_{0}$   $= \frac{\sigma_{exp} - \sigma^{CC} - \sigma^{NC}}{2\sigma_{0}} = \frac{\sigma_{exp} - 4\sigma_{0} - 0.37\sigma_{0}}{2\sigma_{0}}$   $= \frac{\sigma_{exp}}{2\sigma_{0}} - 2.18,$ (11)

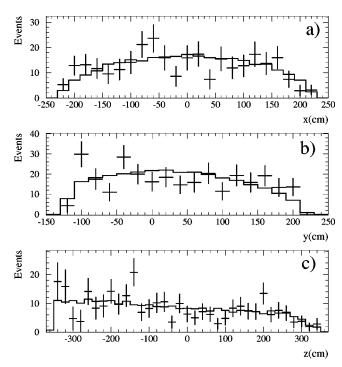


FIG. 11. The spatial distribution of the electron for beam-excess events with  $\cos \theta > 0.9$  compared with expectation (solid line) from  $\nu e$  elastic scattering and  $\nu C$  scattering.

where  $\sigma_0 = (2m_e G_F^2/4\pi) E_{\nu_e} = (4.31 \times 10^{-45})$  cm<sup>2</sup>/MeV  $\times E_{\nu_e}$  and becomes

$$I^{LSND} = -1.01 \pm 0.13 (\text{stat}) \pm 0.12 (\text{syst}).$$
(12)

This compares well with  $I^{E225} = -1.07 \pm 0.17$ (stat)  $\pm 0.11$ (syst) and  $I^{SM} = -1.09$ .

In the SM

$$\sigma_{\nu_e e}^{SM} = \sigma_0 \bigg[ 1 + 4 \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W \bigg].$$
(13)

Setting  $\sigma_{\nu_e e}^{SM} = \sigma_{exp}$  we obtain

TABLE III. Events, backgrounds and efficiency for  $\cos \theta > 0.9$ . The neutrino flux and the flux averaged cross section for the reaction  $\nu_e + e^- \rightarrow \nu_e + e^-$  are also shown.

Beam-on events	434 events
Beam-off events×duty ratio	133 events
Beam-excess events	301 events
$\nu C$ background	59 events
$\nu_{\mu}e$ background	24 events
$\overline{\nu}_{\mu}e$ background	27 events
$\nu_e e$ elastic	191 events
Efficiency	0.187
$\nu_e$ flux	11.76×10 <sup>13</sup> /cm <sup>2</sup>
$\langle \sigma \rangle$	$(3.19 \pm 0.35 \pm 0.33)$
	$\times 10^{-43} \text{ cm}^2$

$$\sin^2 \theta_W = 0.248 \pm 0.051, \tag{14}$$

where the error combines the statistical and systematic uncertainties. This is in good agreement with other, much more precise measurements of  $\sin^2 \theta_W$ .

Limits on the electron-neutrino charge radius were obtained following closely the notation and procedure of Refs. [4] and [34]. The measured value of  $\sin^2 \theta_W = 0.248 \pm 0.051$ agrees well with the value predicted from high energy collider results,  $\sin^2 \overline{\theta}_W$ . This agreement is used to place limits on the size of the radiative correction ( $\delta = \sin^2 \theta_W$  $-\sin^2 \overline{\theta}_W$ ) to the electron vector coupling constant  $g_V = \overline{g}_V$  $+ 2\delta$  with  $g_V = -\frac{1}{2} + 2\sin^2 \theta_W$  and  $\overline{g}_V = -\frac{1}{2} + 2\sin^2 \overline{\theta}_W$ . The 90% confidence level interval for  $g_V$  (based on 0.159  $<\sin^2 \theta_W < 0.329$ ) is measured to be  $-0.182 < g_V < 0.158$ . The radiative correction  $\delta$  to the vector coupling ( $\overline{g}_V =$ -0.04) is therefore in the range  $-0.142 < 2\delta < 0.198$  at the 90% confidence level. Then using the relation  $\delta$  $= (\sqrt{2}\pi\alpha/3G_F)\langle r^2 \rangle$  we obtain limits on the electronneutrino charge radius:

$$-2.97 \times 10^{-32} < \langle r^2 \rangle < 4.14 \times 10^{-32} \text{ cm}^2.$$
 (15)

A more general interpretation of these results is that they place limits on certain nonstandard contributions to neutrino scattering [31].

It is also possible to search for neutrino flavor-changing neutral currents. If the neutrino emerging from the neutral current differs from the electron-flavor neutrino emerging from the charge current, the two amplitudes will not add coherently. Following Okun [35], we introduce diagonal  $(f_{ee})$  and off-diagonal  $(f_{e\mu} \text{ and } f_{e\tau})$  couplings for neutral-current mixing of neutrino flavors with  $1 = f_{ee}^2 + f_{e\mu}^2 + f_{e\tau}^2$ . Non-zero flavor-changing couplings  $f_{e\mu}$  or  $f_{e\tau}$  would cause the diagonal coupling to be less than unity. Limits on  $1 - f_{ee}$  can be obtained by comparing the measured cross section,  $\sigma_{exp}$ , for  $\nu_e$  electron elastic scattering with the standard model cross section,  $\sigma^{SM}$ . From the relation

$$1 - f_{ee} = \frac{(\sigma_{exp} - \sigma^{SM})}{4\sigma_0 (1 - 2\sin^2 \theta_W)},$$
 (16)

we obtain  $1 - f_{ee} < 0.32$  at 90% confidence level for the allowed region,  $f_{ee} \leq 1$ . Alternatively,  $f_{e\mu}^2 + f_{e\tau}^2 < 0.54$  at 90% confidence level. The E225 experiment at Los Alamos obtained similar limits [4,36].

Limits on the  $\nu_e$  and  $\nu_{\mu}$  magnetic moments are obtained by comparing the observed number of elastic events from  $\nu_e$ ,  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  scattering, 242, with the 229 events expected from the standard model. At 90% confidence level there are then fewer than 55 events due to magnetic scattering. Using the  $\nu_e$ ,  $\nu_{\mu}$  and  $\bar{\nu}_{\mu}$  fluxes, the experimental detection efficiencies and Eq. (7), the cross section for electromagnetic scattering, we obtain

$$\mu_{\nu_e}^2 + 2.4 \mu_{\nu_{\mu}}^2 < 1.1 \times 10^{-18} \mu_{Bohr}^2 \,. \tag{17}$$

Thus  $\mu_{\nu_e} < 1.1 \times 10^{-9} \mu_{Bohr}$  and  $\mu_{\nu_{\mu}} < 6.8 \times 10^{-10} \mu_{Bohr}$  [37]. The limit on the muon-neutrino magnetic moment is slightly more stringent than that given by previous experiments [1,4].

## VIII. CONCLUSIONS

We have measured  $\nu_e e^- \rightarrow \nu_e e^-$  elastic scattering with a sample of  $191\pm 22$  events. The reaction is of interest primarily because it is one of the few reactions for which the SM predicts a large destructive interference between the CC and NC channels. The measured cross section,  $\sigma_{\nu_e e^-} = [10.1 \pm 1.1(\text{stat}) \pm 1.0(\text{syst})] \times E_{\nu_e} (\text{MeV}) \times 10^{-45} \text{ cm}^2$ , is in good agreement with standard model expectations. The measured interference term,  $I^{LSND} = -1.01\pm 0.13(\text{stat}) \pm 0.12(\text{syst})$ , is in good agreement with the SM expectation of  $I^{SM} = -1.09$ . Limits are placed on neutrino flavor-changing neutral currents and on the electron-neutrino charge radius. Finally, we obtain limits on the muon-neutrino magnetic moment that are slightly more stringent than those of previous experiments.

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