Higgs boson production: A comparison of parton showers and resummation

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The search for the Higgs boson(s) is one of the major priorities at the upgraded Fermilab Tevatron and at the CERN Large Hadron Collider (LHC). Monte Carlo (MC) event generators are heavily utilized to extract and interpret the Higgs signal, which depends on the details of the soft-gluon emission from the initial state partons in hadronic collisions. Thus, it is crucial to establish the reliability of the MC event generators used by the experimentalists. In this paper, the MC based parton shower formalism is compared to that of an analytic resummation calculation. Theoretical input, predictions and, where they exist, data for the transverse momentum distribution of Higgs bosons, Z^0 bosons, and photon pairs are compared for the Tevatron and the LHC. This comparison is useful in understanding the strengths and the weaknesses of the different theoretical

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approaches, and in testing their reliability.

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I. INTRODUCTION

To reveal the dynamics of electroweak symmetry breaking, a new generation of hadron colliders will search for the Higgs boson(s). The potential of the upgraded Fermilab Tevatron, the 2 TeV center of mass energy proton-antiproton collider starting operation within a year, was analyzed in Ref. [1]. Later in this decade, two experimental collaborations (ATLAS and CMS) will join the search at the CERN Large Hadron Collider (LHC) with 14 TeV proton-proton collisions. An extraction of the Higgs signal at the LHC requires not only precise knowledge of the signal and background invariant mass distributions, but also an accurate prediction of the corresponding transverse momentum (p_T) distributions. In general, the determination of the signal requires a detailed event modeling, an understanding of the detector resolution, kinematical acceptance and efficiency, all of which depend on the p_T distribution. The shape of this distribution in the low to moderate p_T region can dictate the details of both the experimental triggering and the analysis strategies for the Higgs boson search. It can also be used to devise an improved search strategy and to enhance the statistical significance of the signal over the background [2,3]. In the $gg \rightarrow HX \rightarrow \gamma \gamma X$ mode at the LHC, for example, the shape of the signal and the background p_T distribution of the photon pairs is different (cf. Refs. [4,5]), with the signal being harder. This difference can be utilized to increase the signal to background ratio. Furthermore, since vertex pointing with the photons is not possible in the CMS barrel, the

shape of the p_T distribution affects the precision of the determination of the event vertex from which the Higgs boson (decaying into two photons) originated.¹ Thus, for a successful, high precision extraction of the Higgs signal, the theoretical calculation must be capable of reproducing the expected transverse momentum distribution.

To reliably predict the p_T distribution of Higgs bosons at the LHC, especially for the low to medium p_T region where the bulk of the rate is, the effects of the multiple soft-gluon emission have to be included. One approach which achieves this is parton showering [6]. Parton shower Monte Carlo programs such as PYTHIA [7], HERWIG [8] and ISAJET [9] are commonly used by experimentalists, both as a way of comparing experimental data to theoretical predictions and also as a means of simulating experimental signatures in kinematic regimes for which there are no experimental data yet (such as for the LHC). The final output of these Monte Carlo programs consists of the 4-momenta of a set of final state particles. This output can either be compared to reconstructed experimental quantities or, when coupled with a simulation of a detector response, can be directly compared to raw data taken by the experiment and/or passed through the same reconstruction procedures as the raw data. In this way, the parton shower programs can be more useful to experimentalists than analytic calculations. Indeed, almost all of the physics plots by the ATLAS Collaboration [10] involve comparisons to PYTHIA version 5.7.

Predictions of the Higgs boson p_T can also be obtained

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¹The vertex with the most activity is chosen as the vertex from which the Higgs particle has originated. If the Higgs boson is typically produced at a relatively high value of p_T , then this choice is correct a large fraction of the time.

utilizing an analytic resummation formalism, which sums contributions of $\alpha_S^n \ln^m(m_H/p_T)$ (where m_H is the Higgs boson mass and $m \le 2n-1$) up to all orders in the strong coupling α_S . In the recent literature, most calculations of this kind are either based on, or originate from, the low p_T factorization formalism [11] (for the latest review see Ref. [12]). This formalism resums the effects of the multiple soft-gluon emission while also systematically including the fixed order QCD corrections. It is possible to smoothly match the resummed result to the fixed order one in the intermediate to high p_T region, thus obtaining a prediction for the full p_T distribution [13]. In this paper, we use this formalism as an analytic "benchmark" to calculate the p_T distributions of Higgs bosons at the LHC and of Z^0 bosons and photon pairs produced in hadron collisions.

For many physical quantities, the predictions from parton shower Monte Carlo programs should be nearly as precise as those from analytic theoretical calculations. It is expected that both Monte Carlo and analytic calculations should accurately describe the effects of the emission of multiple soft gluons from the incoming partons, an all orders problem in QCD. The initial state solf-gluon emission affects the kinematics of the final state partons. This may have an impact on the signatures of physics processes at both the trigger and analysis levels and thus it is important to understand the reliability of such predictions. The best method for testing the reliability is a direct comparison of the predictions to experimental data. If no experimental data are available for certain predictions, then some understanding of the reliability may be gained from a comparison of the predictions from the two different methods.

In the absence of experimental data for Higgs boson production, we can gauge the reliability of calculations for this process by comparing them to each other. We also compare predictions from the different formalisms to data for processes which are similar to Higgs boson production at the LHC. In this way we can perform a genuine "reality check" of the various theoretical predictions. Production of a light, neutral Higgs boson at the LHC in the standard model (SM) and its supersymmetric extensions proceeds via the partonic subprocess gg (through heavy fermion loop) $\rightarrow HX$. One of the major backgrounds for a light Higgs boson, in the mass range of 100 GeV $\leq m_H \leq 150$ GeV, is diphoton production, a sizable contribution to which comes from the same, gginitial state. Since the major part of the soft-gluon radiation is initiated from the incoming partons, the structures of the resummed corrections are similar for Higgs boson and diphoton production. Because the latter is measurable at the Fermilab Tevatron, diphoton production provides an exceptional opportunity to test the different theoretical models. Z^0 boson production can also be a good testing ground for the soft-gluon corrections to Higgs boson production. The treatment of the fixed order and resummed QCD corrections for Z^0 boson production is theoretically well understood and implemented at next-to-next-to-leading order [13]. Furthermore, just as in the diphoton case, predictions can also be tested against Tevatron data. The Z^0 data have the advantage that sufficient statistics exist in the run 1 data from Collider Detector at Fermilab (CDF) and D0 to allow for detailed comparisons to the theoretical predictions.

II. LOW p_T FACTORIZATION

In this section the low transverse momentum factorization formalism and its matching to the usual factorization are reviewed. The problem arises as follows. When calculating fixed order QCD corrections to the p_T distribution of the Higgs boson produced in the inclusive process $pp \rightarrow HX$, the standard QCD factorization theorem is invoked:

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$$\frac{d\sigma}{dp_T^2} = f_{j_1/p}(m_H) \otimes \frac{d\hat{\sigma}_{j_1j_2}}{dp_T^2}(m_H, p_T) \otimes f_{j_2/p}(m_H), \quad (1)$$

which is a convolution in the partonic momentum fractions, and is derived under the usual assumption $p_T \gg m_H$.² When $p_T \ll m_H$ occurs, as a result of soft and soft+collinear emission of gluons from the initial state, the theorem fails. The ratio of the two very different physical scales in the partonic cross section $\hat{\sigma}_{j_1 j_2}$ produces large logarithms of the form $\ln(m_H/p_T)$, which are not absorbed by the parton distribution functions $f_{j/p}$, unlike the ones originating from purely collinear parton emission. These logarithms are enhanced by a $1/p_T^2$ pre-factor at low p_T . (The same factor suppresses them for large p_T .) As a result, the Higgs p_T distribution calculated using the conventional hadronic factorization theorem is un-physical in the low p_T region.

To resolve this problem, the differential cross section is split into a part which contains all the logarithmic terms (W) and into a regular term (Y):

$$\frac{d\sigma}{dp_T^2} = W(m_H, p_T) + Y(m_H, p_T).$$
(2)

Since *Y* does not contain logarithms of p_T , it can be calculated using the usual factorization. The *W* term has to be evaluated differently, keeping in mind that failure of the standard factorization occurs because it neglects the transverse motion of the incoming partons in the hard scattering. As has been proved [11], *W* has a simple form in the Fourier conjugate, that is the transverse position (\vec{b}) space,

$$\widetilde{W}(m_H,b) = \mathcal{C}_{j_1/h_1}(m_H,b)e^{-\mathcal{S}(m_H,b_*)}\mathcal{C}_{j_2/h_2}(m_H,b), \quad (3)$$

with the Sudakov exponent defined as

²Here and henceforth, summation on double partonic indices (e.g. j_i) is implied. Also, since we are focusing on the transverse momentum, longitudinal partonic momentum fractions are either kept implicit or, when applicable, integrated over.

$$S(m_H, b_*) = \int_{C_0^2/b_*^2}^{m_H^2} \frac{d\mu^2}{\mu^2} \bigg[A(\alpha_S(\mu)) \ln\bigg(\frac{m_H^2}{\mu^2}\bigg) + B(\alpha_S(\mu)) \bigg],$$
(4)

which resums the large logarithmic terms.³ The partonic recoil against soft gluons, as well as the intrinsic partonic transverse momentum, is included in the generalized parton distributions

$$\mathcal{C}_{j/h}(m_H, b, x) = [C_{ja}(m_H, b_*) \otimes f_{a/h}(m_H)](x)$$
$$\times \mathcal{F}_{a/h}(m_H, b, x), \tag{5}$$

where the convolution is evaluated over the partonic momentum fraction x. The A and B functions, and the Wilson coefficients C_{ja} , are free of logarithms and safely calculable perturbatively as expansions in the strong coupling:

$$A(\alpha_S) = \sum_{n=1}^{\infty} \left(\frac{\alpha_S}{\pi}\right)^n A^{(n)}, \quad \text{etc.}$$
(6)

The process independent non-perturbative functions $\mathcal{F}_{a/h}$, describing long distance transverse physics, are extracted from low-energy experiments [14].

The matching of the low and the high p_T regions is achieved via the *Y* piece. To correct the behavior of the resummed piece in the intermediate and high p_T regions, it is defined as the difference of the cross section calculated by the standard factorization formula at a fixed order *n* of perturbation theory and its $p_T \ll m_H$ asymptote.⁴ The resummed cross section, to order α_s^n , then reads as

$$\frac{d\sigma}{dp_T^2} = W(m_H, p_T) + \frac{d\sigma^{(n)}}{dp_T^2} - \frac{d\sigma^{(n)}}{dp_T^2} \bigg|_{p_T \ll m_H}.$$
 (7)

At low p_T , the logarithms are large and the asymptotic part dominates the fixed order p_T distribution. The last two terms in Eq. (7) nearly cancel, and W is a good approximation to the cross section. At high p_T the logarithms are small, and the expansion of the resummed term cancels the p_T singular terms (up to higher orders in α_S), and the cross section reduces to the fixed order perturbative result. After matching the resummed and fixed order cross sections in such a manner, it is expected that the normalization of the resummed cross section reproduces the fixed order total rate, since when expanded and integrated over p_T it deviates from the fixed order result only in higher order terms. For further details of the low p_T factorization formalism and its application to Higgs boson production we refer to the recent literature [5,16].

III. PARTON SHOWERING AND RESUMMATION

For technical reasons, the initial state parton shower proceeds by a *backwards* evolution, starting at the large (negative) Q^2 scale of the hard scatter and then considering emissions at lower and lower (negative) virtualities, corresponding to earlier points on the cascade (and earlier points in time), until a scale corresponding to the factorization scale is reached. The transverse momentum of the initial state is built up from the whole series of splittings and boosts. The showering process is independent of the hard scattering process being considered (as long as one does not introduce any matrix element corrections), and depends only on the initial state partons and the hard scale of the process.

Parton showering utilizes the fact that the leading order singularities of cross sections factorize in the collinear limit. This is expressed as

$$\lim_{p_b \parallel p_g} |\mathcal{M}_{n+1}|^2 = \frac{2\pi\alpha_S}{p_b \cdot p_g} P_{a \to bg}(z) |\mathcal{M}_n|^2, \tag{8}$$

where \mathcal{M}_{n+1} is the invariant amplitude for the process producing *n* partons and a gluon, α_S is the strong coupling constant, p_b and p_g are the 4-momenta of the daughters of parton *a*, and $P_{a \to bg}(z)$ is the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution kernel associated with the $a \to bg$ splitting. These leading order collinear singularities can be factorized into a Sudakov form factor

$$S_{\text{shower}}(Q) = \int_{Q_0^2}^{Q^2} \frac{d\mu^2}{\mu^2} \frac{\alpha_s(\mu)}{2\pi} \int_0^1 dz \, P_{a \to bg}(z), \qquad (9)$$

which is interpreted as the probability $\mathcal{P}=\exp(-S_{\text{shower}})$ of the partonic evolution from scale Q_0 to Q with no resolvable branchings. This probability can be used to determine the scale for the first emission and hence for the whole cascade. The formalism can be extended to soft singularities as well by using angular ordering. In this approach, the choice of the hard scattering is based on the use of evolved parton distributions, which means that the inclusive effects of initial-state radiation are already included. What remains is, therefore, to construct the exclusive showers.

Parton showering resums primarily the leading logarithms which are universal, that is process independent, and depend only on the given initial state. In this lies one of the strengths of Monte Carlo programs, since parton showering can be incorporated into a wide variety of physical processes. An analytic calculation, in comparison, can resum all logarithms. For example, the low p_T factorization formalism sums all of the logarithms with m_H/p_T in their arguments. As discussed earlier, all of the "dangerous logarithms" are included in the Sudakov exponent (4). The A and B functions in Eq. (4) contain an infinite number of coefficients, with the $A^{(n)}$ coefficients being universal, while the $B^{(n)}$'s are process dependent, with the exception of $B^{(1)}$. In practice, the number of towers of logarithms included in the analytic Sudakov exponent depends on the level to which a fixed order calculation was performed for a given process. Generally, if a next-to-next-to-leading order calculation is available, then

³To prevent evaluation of the Sudakov exponent in the nonperturbative region, the impact parameter $b = |\vec{b}|$ is replaced by $b_* = b/\sqrt{1 + (b/b_{\text{max}})^2}$. The choice of $C_0 = 2e^{-\gamma_E}$, where γ_E is the Euler constant, is customary.

⁴The expression for the *Y* term for Higgs boson production can be found elsewhere [15].



FIG. 1. The $Z^0 p_T$ distribution (at low p_T) from CDF for run 1 compared to predictions from ResBos (curve) and from PYTHIA (histograms). The two PYTHIA predictions use the default (rms) value for the non-perturbative k_T (0.44 GeV) and the value that gives the best agreement with the shape of the data (2.15 GeV). The normalization of the resummed prediction was rescaled upwards by 8.4%. The PYTHIA prediction was rescaled by a factor of 1.4 for the shape comparison. (Including only soft-gluon QCD corrections, PYTHIA does not contain the QCD K factor.)

 $B^{(2)}$ can be extracted and incorporated. Extraction of higher coefficients requires knowledge of even higher order QCD corrections. So far, only the $A^{(1)}$, $A^{(2)}$ and $B^{(1)}$ coefficients are known for Higgs boson production but the calculation of $B^{(2)}$ is in progress [17]. If we try to interpret parton showering in the same language, then we can say that the Monte Carlo Sudakov exponent always contains a term analogous to $A^{(1)}$. It was shown in Ref. [18] that a term equivalent to $B^{(1)}$ is also included in the (HERWIG) shower algorithm, and a suitable modification of the Altarelli-Parisi splitting function, or equivalently the strong coupling constant α_S , also effectively approximates the $A^{(2)}$ coefficient.⁵

In contrast with the shower Monte Carlo programs analytic resummation calculations integrate over the kinematics of the soft-gluon emission, with the result that they are limited in their predictive power to inclusive final states. While the Monte Carlo program maintains an exact treatment of the branching kinematics, in the original low p_T factorization formalism no kinematic penalty is paid for the emission of the soft gluons, although an approximate treatment of this can be incorporated into its numerical implementations, such as ResBos [5,13]. Neither the parton showering process nor the analytic resummation translate smoothly into kinematic configurations where one hard parton is emitted at large p_T . In the Monte Carlo matrix element corrections and in the analytic resummation calculation, matching is necessary. This matching is standard procedure for resummed calculations, and matrix element corrections are becoming increasingly common in Monte Carlo programs [19–21].

With the appropriate input from higher order cross sec-



FIG. 2. The $Z^0 p_T$ distribution (for the full range of p_T) from CDF for run 1 compared to predictions from ResBos (curve) and from PYTHIA (histogram). The normalization of the resummed prediction was rescaled upwards by 8.4%. The PYTHIA prediction was rescaled by a factor of 1.4 for the shape comparison.

tions, a resummation calculation has the corresponding higher order normalization and scale dependence. The normalization and scale dependence for the Monte Carlo program, though, remains that of a leading order calculation. The parton showering process redistributes the events in phase space, but does not change the total cross section (for example, for the production of a Higgs boson).⁶

One quantity which is expected to be well described by both calculations is the transverse momentum of the final state electroweak boson in a subprocess such as $q\bar{q}$ $\rightarrow W^{\pm}X$, $Z^{0}X$ or $gg \rightarrow HX$, where most of the p_{T} is provided by initial state parton emission. The parton showering supplies the same sort of transverse kick as the resummed softgluon emission in the analytic calculation. Indeed, similar Sudakov form factors appear in both approaches. The correspondence between the Sudakov form factors of resummation and Monte Carlo approaches embodies many subtleties, relating to both the arguments of the Sudakov factors as well as the impact of sub-leading logarithms [22].

At a point in its evolution, typically corresponding to the virtuality of a few GeV², the parton shower is cut off and the effects of gluon emission at softer scales must be parametrized and inserted by hand. This is similar to the somewhat arbitrary division between perturbative and non-perturbative regions in the resummation calculation. The parametrization is typically expressed in a Gaussian form, similar to that used for the non-perturbative k_T in a resummation program [14]. In general, the value for the non-perturbative $\langle k_T \rangle$ needed in a Monte Carlo program will depend on the particular kinematics and initial state being investigated. A value of the

⁵This is rigorously true only for the high x or $\sqrt{\tau}$ region.

⁶Technically, one could add the branching for $q \rightarrow q +$ Higgs boson in the shower, which would somewhat increase the Higgs boson cross section. However, the main contribution to the higher order *K* factor comes from the virtual corrections and the "Higgs bremsstrahlung" contribution is negligible.



FIG. 3. A comparison of the PYTHIA predictions for diphoton production at the Tevatron for the two different subprocesses, $q\bar{q}$ and gg. The same cuts are applied to PYTHIA as in the CDF diphoton analysis.

average non-perturbative k_T of greater than 1 GeV, for example, does not imply that there is an anomalous intrinsic k_T associated with the parton size. Rather, this amount of $\langle k_T \rangle$ needs to be supplied to provide what is missing in the truncated parton shower. If the shower is cut off at a higher virtuality, more of the "non-perturbative" k_T will be needed.

IV. Z⁰ BOSON PRODUCTION AT THE TEVATRON

From a theoretical viewpoint, Z^0 boson production at the Tevatron is one of the highest precision testing grounds for the effects of multiple soft-gluon emission. The fully differential fixed order cross section has been calculated up to $\mathcal{O}(\alpha_s^2)$, and the $A^{(1,2)}$, $B^{(1,2)}$, and $C^{(1)}$ resummed coefficients are known for this process, and have been numerically implemented [13]. Since the $\mathcal{O}(\alpha_s^2)$ corrections are relatively small (the order of a percent), the contribution of $B^{(2)}$ is almost negligible. Thus, nominally the same perturbative physics is implemented in the shower Monte Carlo programs as in the resummation calculation. Any differences between their predictions can be ascribed to the small differences in the implementation of the perturbative physics and to the different non-perturbative physics they contain. Experimentally, the 4-momentum of a Z^0 boson, and thus its p_T , can be measured with great precision in the e^+e^- decay mode. Resolution effects are relatively minor and are easily corrected. Thus, the $Z^0 p_T$ distribution is an excellent probe of the effects of the soft-gluon emission.

The resolution corrected p_T distribution (in the low p_T region) for Z^0 bosons from the CDF experiment [23] is shown in Fig. 1, compared to both the resummed prediction



FIG. 4. A comparison of the PYTHIA predictions for diphoton production at the Tevatron for the two different subprocesses, gg (top) and $q\bar{q}$ (bottom), for two recent versions of PYTHIA. The same cuts are applied to PYTHIA as in the CDF diphoton analysis.

of ResBos and to two predictions from PYTHIA version 6.125. One PYTHIA prediction uses the default value of intrinsic $k_T^{\text{rms}} = 0.44$ GeV (dashed histogram)⁷, and the second a value of 2.15 GeV (solid histogram), per incoming parton.⁸ The latter value was found to give the best agreement for PYTHIA with the data, and a similar conclusion has been reached in comparisons of the CDF $Z^0 p_T$ data with HERWIG [24]. All of the predictions use the CTEQ4M parton distributions [25]. The shift between the two PYTHIA predictions at low p_T is clearly evident. As might have been expected, the high p_T region (above 10 GeV) is unaffected by the value of the non-perturbative k_T . Much of the k_T "given" to the incoming partons at their lowest virtuality, Q_0 , is reduced at the hard scatter due to the number of gluon branchings preceding the collision. The emitted gluons carry off a sizable fraction of the original non-perturbative k_T [26]. This point will be investigated in more detail later for the case of Higgs boson production.

In the resummed calculation it has been shown that, in addition to the perturbative physics (Sudakov-Wilson coefficients, C_{ja}), the choice of the non-perturbative parameters affects the shape of the distribution in the lowest p_T region

⁷For a Gaussian distribution, $k_T^{\text{rms}} = 1.13 \langle k_T \rangle$.

⁸A previous publication [19] indicated the need for a substantially larger non-perturbative $\langle k_T \rangle$, of the order of 4 GeV, for the case of W^{\pm} production at the Tevatron. The data used in the comparison, however, were not corrected for resolution smearing, a fairly large effect for the case of $W \rightarrow e \nu$ production and decay.



FIG. 5. A comparison of the PYTHIA and ResBos predictions for diphoton production at the Tevatron for the two different subprocesses, gg (left) and $q\bar{q}$ (right). The same cuts are applied to PYTHIA and ResBos as in the CDF diphoton analysis. The bottom figures show the same in logarithmic scale.

and the location of the peak [13]. In order to qualitatively compare this effect to the smearing applied in the Monte Carlo programs, it is possible to bring the resummation formula to a form where the non-perturbative function acts as a Gaussian type smearing term. This, using the Ladinsky-Yuan parametrization [27] of the non-perturbative function, leads to an rms value of 2.5 GeV for the effective k_T smearing parameter for Z^0 production at the Tevatron. This is in agreement with the PYTHIA and HERWIG results: to describe well the Z^0 production data at the Tevatron, 2–2.5 GeV nonperturbative k_T is needed in these implementations. The resummed curve agrees with the shape of the data well, which is a non-trivial result, since the resummation calculation does not contain any free parameters which are fitted to the $Z^0 p_T$ distribution. Even with the optimal non-perturbative k_T^{rms} =2.15 GeV, there is slight shape difference between the shower Monte Carlo program and the data. This might be partially due to the lack of the $B^{(2)}$ coefficient in the shower Monte Carlo programs. This is supported by the fact that, if the $B^{(2)}$ coefficient was not included in the resummed prediction, the result would be an increase in the height of the peak and a decrease in the rate between 10 and 20 GeV, leading to a better agreement with the best PYTHIA prediction [12].

The Z^0 p_T distribution is shown over a wider p_T range in Fig. 2. The PYTHIA and ResBos predictions both describe the data well. Note especially the agreement of PYTHIA with the data at high p_T , made possible by explicit matrix element



FIG. 6. A comparison of the PYTHIA predictions for diphoton production at the LHC for the two different subprocesses, $q\bar{q}$ and gg. Similar cuts are applied to the diphoton kinematics as those used by ATLAS and CMS.

corrections (from the subprocesses $q\bar{q} \rightarrow Z^0 g$ and $gq \rightarrow Z^0 q$) to the Z^0 production process.⁹

V. DIPHOTON PRODUCTION

Most of the experience that we have for comparisons of data to resummation calculations or Monte Carlo programs is based on Drell-Yan pair production, that is mostly on $q\bar{q}$ initial states. It is important then to examine diphoton production at the Tevatron, where a large fraction of the contribution at low mass is due to gg scattering. The prediction for the diphoton p_T distribution at the Tevatron, from PYTHIA (version 6.122), is shown in Fig. 3, using the experimental cuts applied in the CDF analysis [28]. About half of the diphoton cross section at the Tevatron is due to the gg subprocess, and the diphoton p_T distribution is noticeably broader for the gg subprocess than for the $q\bar{q}$ subprocess.

A comparison of the p_T distributions for the two diphoton

⁹Slightly different techniques are used for the matrix element corrections by PYTHIA [19] and by HERWIG [20]. In PYTHIA, the parton shower probability distribution is applied over the whole phase space and the exact matrix element corrections are applied only to the branching closest to the hard scatter. In HERWIG, the corrections are generated separately for the regions of phase space unpopulated by HERWIG (the ''dead zone'') and the populated region. In the dead zone, the radiation is generated according to a distribution using the first order matrix element calculation, while the algorithm for the already populated region applies matrix element corrections whenever a branching is capable of being ''the hardest so far.''



FIG. 7. A comparison of the PYTHIA predictions for diphoton production at the LHC for the two different subprocesses, gg (top) and $q\bar{q}$ (bottom), for two recent versions of PYTHIA. Similar cuts are applied to the diphoton kinematics as are used by ATLAS and CMS.

subprocesses $(q\bar{q},gg)$ in two recent versions of PYTHIA, 5.7 and 6.1, is shown in Fig. 4. There seems to be little difference in the p_T distributions between the two versions for both subprocesses. As will be shown later, this is not true for the case of Higgs boson production. In Fig. 5 are shown the ResBos predictions for diphoton production at the Tevatron from $q\bar{q}$ and gg scattering compared to the PYTHIA predictions. The gg subprocess predictions in ResBos agree well with those from PYTHIA while the $q\bar{q}$ p_T distribution is noticeably broader in ResBos. The latter behavior is due to the presence of the Y piece in ResBos at moderate p_T , that is the matching of the $q\bar{q}$ cross section to the fixed order $q\bar{q}$ $\rightarrow \gamma \gamma g$ at high p_T . The corresponding matrix element correction is not implemented in PYTHIA. The PYTHIA and Res-Bos predictions for $gg \rightarrow \gamma \gamma$ agree in the moderate p_T region, even though the ResBos prediction has the Y piece present and is matched to the matrix element piece gg $\rightarrow \gamma \gamma g$ at high p_T , while there is no such matrix element correction for PYTHIA. This demonstrates the smallness of the Y piece for the gg subprocess, which is the same conclusion that was reached in Ref. [3]. One way to understand this is recalling that the gg parton-parton luminosity falls very steeply with increasing partonic center of mass energy, $\sqrt{\hat{s}}$. This falloff tends to suppress the size of the Y piece since the production of the diphoton pair at higher p_T requires larger values of the longitudinal momentum fractions.

Comparisons of the diphoton data measured by both the CDF [28] and D0 [29] experiments indicate a disagreement of the observed diphoton p_T distribution with the NLO QCD predictions [30]. In particular, the p_T distribution in the data



FIG. 8. A comparison of the PYTHIA and ResBos predictions for diphoton production at the LHC for the two different subprocesses, gg (left) and $q\bar{q}$ (right). Similar cuts are applied to PYTHIA and ResBos as in the ATLAS and CMS diphoton analyses. The bottom figures show the same in logarithmic scale.

is noticeably broader than that predicted by fixed order QCD calculations, but in agreement with the predictions of ResBos [31]. The transverse distributions of the diphoton pair are particularly sensitive to the effects of soft-gluon radiation. The p_T distribution, for example, is a delta function calculated at leading order, and is strongly smeared by the all orders Sudakov factor. Given the small size of the diphoton cross section at the Tevatron, the comparisons for run 1 are statistically limited. A more precise comparison between theory and experiment will be possible with the 2 fb^{-1} or greater data sample that is expected for CDF and D0 in run 2 and at the LHC. The Monte Carlo prediction for the diphoton production cross section, as a function of the diphoton p_T and using cuts appropriate to ATLAS and CMS, is shown in Fig. 6. As at the Tevatron, about half of the cross section is due to gg scattering and the diphoton p_T distribution from gg scattering is noticeably broader than that from $q\bar{q}$ production.

In Fig. 7 is shown a comparison of the diphoton p_T distribution at the LHC for two different versions of PYTHIA, for the two different subprocesses. Note that the p_T distribution in PYTHIA version 5.7 is somewhat broader than that in version 6.122 for the case of gg scattering. The effective diphoton mass range being considered here is lower than the 150 GeV Higgs boson mass that will be considered in the next section. As will be seen, the differences in soft-gluon emission between the two versions of PYTHIA are larger in that case. In Fig. 8 are shown the ResBos predictions for diphoton production at the LHC from $q\bar{q}$ and gg scattering compared to the PYTHIA predictions. Again, the gg subprocess in ResBos agrees well with PYTHIA, while the $q\bar{q}$ p_T



FIG. 9. A comparison of predictions for the Higgs p_T distribution at the LHC from ResBos and from two recent versions of PYTHIA. The ResBos and PYTHIA predictions have been normalized to the same area. The bottom figure shows the same in logarithmic scale.

distribution is noticeably broader in ResBos, for the reasons cited previously.

VI. HIGGS BOSON PRODUCTION

A comparison of the SM Higgs p_T distribution at the LHC, for a Higgs boson mass of 150 GeV, is shown in Fig. 9, for ResBos and the two recent versions of PYTHIA. As before, PYTHIA has been rescaled by a factor of 1.7, to agree with the normalization of ResBos to allow for a better shape comparison. There are a number of features of interest. First, the peak of the resummed distribution has moved to p_T ≈ 11 GeV (compared to about 3 GeV for Z⁰ boson production at the Tevatron). This is partially due to the larger mass (150 GeV compared to 90 GeV), but is primarily because of the larger color factors associated with initial state gluons $(C_A=3)$ rather than quarks $(C_F=4/3)$, and also because of the larger phase space for initial state gluon emission at the LHC. Second, and more importantly, there is a substantial disagreement for the shape of the Higgs p_T distribution between ResBos and PYTHIA 5.7, and between the two versions of PYTHIA. An understanding of the reasons for these differences is critical, as the shape of the transverse momentum distribution for the Higgs boson in the low to moderate p_T region can dictate the details of both the experimental triggering and the analysis strategies for the Higgs boson search. As noted before, most of the studies for Higgs boson production by CMS and ATLAS have been based on PYTHIA 5.7. For the CMS detector, the higher p_T activity associated with Higgs boson production in version 5.7 allows for a more precise determination of the event vertex from which the Higgs boson (decaying into two photons) originates. Vertex



FIG. 10. A comparison of predictions for the Higgs p_T distribution at the Tevatron from ResBos and from two recent versions of PYTHIA. The ResBos and PYTHIA predictions have been normalized to the same area. The bottom figure shows the same in logarithmic scale.

pointing with the photons is not possible in the CMS barrel and the large number of interactions occurring with high intensity running will mean a substantial probability that at least one of the interactions will have more activity than the Higgs vertex, thus leading to the assignment of the Higgs boson decay to the wrong vertex, and therefore a noticeable degradation of the $\gamma\gamma$ effective mass resolution.

In comparison to ResBos, the older version of PYTHIA produces too many Higgs events at moderate p_T . Two changes have been implemented in the newer version 6.1. The first change is that a cut is placed on the combination of z (longitudinal momentum fraction) and Q^2 (partonic virtuality) values in a branching: $\hat{u} = Q^2 - \hat{s}(1-z) < 0$, where \hat{s} refers to the squared invariant mass of the subsystem of the hard scattering plus the shower partons considered to that point. The association with \hat{u} is relevant if the branching is interpreted in terms of a $2 \rightarrow 2$ hard scattering. The corner of emissions that do not respect this requirement occurs when the Q^2 value of the space-like emitting parton is little changed and the z value of the branching is close to unity. This effect is mainly for the hardest emission (largest Q^2). The net result of this requirement is a substantial reduction in the total amount of gluon radiation [32].¹⁰ In the second change, the parameter for the minimum gluon energy emitted

¹⁰Such branchings are kinematically allowed, but since matrix element corrections would assume initial state partons to have $Q^2 = 0$, a non-physical \hat{u} results (and thus no possibility to impose matrix element corrections). The correct behavior is beyond the predictive power of leading logarithm Monte Carlo programs.



FIG. 11. A comparison of predictions for the Higgs p_T distribution at the LHC from ResBos, a recent version of PYTHIA, and HERWIG. All predictions have been normalized to the same area. The bottom figure shows the same in logarithmic scale.

in space-like showers is modified by an extra factor roughly corresponding to the $1/\gamma$ factor for the boost to the hard subprocess frame [32]. The effect of this change is to increase the amount of gluon radiation. Thus, the two effects are in opposite directions but with the first effect being dominant. In principle, this problem could affect the p_T distribution for all PYTHIA processes. In practice, it affects only gg initial states, due to the enhanced probability for branching in such an initial state.

The newer version of PYTHIA agrees well with ResBos at low to moderate p_T , but falls below the resummed prediction at high p_T . The agreement of the predictions of PYTHIA 6.1 with those of ResBos, in the low to moderate p_T region, gives some credence that the changes made in PYTHIA move in the right direction. The disagreement at high p_T can be easily understood: ResBos switches to the next-to-leading order Higgs boson+jet matrix element at high p_T , while the default PYTHIA can generate the Higgs p_T distribution only by initial state gluon radiation, using the Higgs boson mass squared as the maximum virtuality. High p_T Higgs boson production is another example where a $2 \rightarrow 1$ Monte Carlo calculation with parton showering cannot completely reproduce the exact matrix element calculation, without the use of matrix element corrections. The high p_T region is better reproduced if the maximum virtuality Q_{max}^2 is set equal to the squared partonic center of mass energy, s, rather than m_H^2 . This is equivalent to applying the parton shower to all of phase space. However, this has the consequence of depleting the low p_T region, as "too much" showering causes events to migrate out of the peak. The appropriate scale to use in PYTHIA (or any Monte Carlo program) depends on the p_T range to be probed. If matrix element information is used to



FIG. 12. A comparison of predictions for the Higgs p_T distribution at the LHC from ResBos, two recent versions of PYTHIA, and HERWIG. All predictions have their absolute normalizations. The bottom figure shows the same in logarithmic scale.

constrain the behavior, the correct high p_T cross section can be obtained while still using the lower scale for showering. Thus, the incorporation of matrix element corrections to Higgs boson production (involving the processes $gq \rightarrow qH, q\bar{q} \rightarrow gH, gg \rightarrow gH$) is the next logical project for the Monte Carlo experts, in order to accurately describe the high p_T region, and is already in progress [26,33].

A comparison of the two versions of PYTHIA and of Res-Bos is also shown in Fig. 10 for the case of Higgs boson production at the Tevatron with center-of-mass energy of 2.0 TeV (for a hypothetical SM Higgs boson mass of 100 GeV).¹¹ The same qualitative features are observed as at the LHC: the newer version of PYTHIA agrees better with ResBos in describing the low p_T shape, and there is a falloff at high p_T unless the larger virtuality is used for the parton showers. The default (rms) value of the non-perturbative k_T (0.44 GeV) was used for the PYTHIA predictions for Higgs boson production.

VII. COMPARISON WITH HERWIG

The variation between versions 5.7 and 6.1 of PYTHIA gives an indication of the uncertainties due to the types of

¹¹As an exercise, events for an 80 GeV *W* boson and an 80 GeV Higgs boson were generated at the Tevatron using PYTHIA 5.7 [34]. A comparison of the distribution of values of \hat{u} and the virtuality *Q* for the two processes indicates a greater tendency for the Higgs virtuality to be near the maximum value and for there to be a larger number of Higgs events with positive \hat{u} .



FIG. 13. Top: a comparison of the PYTHIA predictions for the p_T distribution of a 100 GeV Higgs boson at the Tevatron using the default (rms) non-perturbative k_T (0.44 GeV) and a larger value (4 GeV), at the initial scale Q_0 and at the hard scatter scale. Also shown is the ResBos prediction. Bottom: the vector sum of the intrinsic k_T ($k_{T1}+k_{T2}$) for the two initial state partons at the initial scale Q_0 and at the hard scatter scale, for the two values of primordial k_T .

choices that can be made in Monte Carlo programs. The prescription that \hat{u} be negative for all branchings is a choice rather than an absolute requirement. Perhaps the better agreement of version 6.1 with ResBos is an indication that the adoption of the \hat{u} restrictions was correct. Of course, there may be other changes to PYTHIA which would also lead to better agreement with ResBos for this variable.

Since there are a variety of choices that can be made in Monte Carlo implementations, it is instructive to compare the predictions for the p_T distribution for Higgs boson production from ResBos and PYTHIA with that from HERWIG version 5.6. The HERWIG prediction, for the Higgs p_T distribution at the LHC, is shown in Fig. 11, along with the PYTHIA and ResBos predictions, all normalized to the Res-Bos prediction.¹² (In all cases, the CTEQ4M parton distribution was used.) The predictions from HERWIG and PYTHIA 6.1 are very similar, with the HERWIG prediction matching the ResBos shape somewhat better at low p_T . It is interesting that HERWIG matches the ResBos prediction so closely without the implementation of any kinematic cuts as in PYTHIA 6.1. Perhaps the reason is related to the treatment of color coherence in the HERWIG parton showering algorithm. For reference, absolutely normalized predictions from ResBos,



FIG. 14. Top: a comparison of the PYTHIA predictions for the p_T distribution of a 150 GeV Higgs boson at the LHC using the default (rms) non-perturbative k_T (0.44 GeV) and a larger value (4 GeV), at the initial scale Q_0 and at the hard scatter scale. Also shown is the ResBos prediction. Bottom: The vector sum of the intrinsic k_T ($k_{T1}+k_{T2}$) for the two initial state partons at the initial scale Q_0 and at the hard scatter scale of the initial scale Q_0 and at the hard scatter scale. Also shown is the ResBos prediction. Bottom: The vector sum of the initial scale Q_0 and at the hard scatter partons at the initial scale Q_0 and at the hard scattering scale, for the two values of primordial k_T .

PYTHIA, and HERWIG for the p_T distribution of a 150 GeV Higgs boson at the LHC are shown in Fig. 12.

VIII. NON-PERTURBATIVE k_T

A question still remains as to the appropriate input value of non-perturbative k_T in the Monte Carlo programs to achieve a better agreement in shape, both at the Tevatron and at the LHC.¹³ In Figs. 13 and 14 are shown comparisons of ResBos and PYTHIA predictions for the Higgs p_T distribution at the Tevatron and the LHC. The PYTHIA prediction (version 6.1 alone) is shown with several values of non-perturbative k_T . Surprisingly, no difference is observed between the predictions with the different values of k_T , with the peak in PYTHIA always being somewhat below that of ResBos. This insensitivity can be understood from the plots at the bottom of the two figures, which show the sum of the nonperturbative partonic initial state k_T 's $(\mathbf{k}_{T1} + \mathbf{k}_{T2})$ at Q_0 and at the hard scatter scale Q. Most of the k_T is radiated away, with this effect being larger (as expected) at the LHC. The large gluon radiation probability from a gg initial state and the greater phase space available at the LHC lead to a stronger degradation of the non-perturbative k_T than was observed with Z^0 production at the Tevatron.

For completeness, a comparison of PYTHIA and ResBos is

¹²The normalization factors (ResBos and Monte Carlo) are 1.68 for both versions of PYTHIA and 1.84 for HERWIG.

¹³This has also been explored for direct photon production in Ref. [35].



FIG. 15. A comparison of the predictions for the p_T distribution for Z^0 production at the LHC from PYTHIA and ResBos, where several values of k_T have been used to make the PYTHIA predictions.

shown in Fig. 15 for Z^0 boson production at the LHC. There are two points that are somewhat surprising. First, there is still a very strong sensitivity to the value of the nonperturbative k_T used in the smearing. Second, the best agreement with ResBos is obtained with the default value (0.44 GeV), in contrast to the 2.15 GeV needed at the Tevatron (cf. Fig. 1). Note again the agreement of PYTHIA with ResBos at the highest values of $Z^0 p_T$ due to the explicit matrix element corrections applied. The sum of the incoming parton k_T distributions, both at the scale Q_0 and at the hard scattering scale, are shown in Fig. 16 for several different starting (rms) values of primordial k_T (per parton). There is substantially less radiation for a $q\bar{q}$ initial state than for a gg initial state (as in the case of the Higgs boson), leading to a noticeable dependence of the $Z^0 p_T$ distribution on the primordial k_T distribution.

IX. CONCLUSIONS

An understanding of the signature for Higgs boson production at either the Tevatron or the LHC depends upon the understanding of the details of the multiple soft-gluon emission from the initial state partons. This soft-gluon radiation

Z production at LHC



FIG. 16. A comparison of the total initial state $k_T (\mathbf{k}_{T1} + \mathbf{k}_{T2})$ distributions for Z^0 production at the LHC from PYTHIA, both at the initial scale Q_0 and at the hard scattering scale, for several (rms) values of the initial state k_T . The mean and rms numbers refer to the values at the hard scattering scale.

can be modeled either in a Monte Carlo program or by an analytic resummation calculation, with various choices possible in both implementations. A comparison of the two approaches helps in understanding their strengths and weaknesses, and their reliability. The data from the Tevatron that either exist now, or will exist in run 2, and from the LHC will be extremely useful to test both methods.

Note added. At the final stage of preparing this manuscript, we became aware of a new paper [36], which studied the *A* and *B* functions for Higgs boson production up to $O(\alpha_S^4)$, and presented an expression for the coefficient $B^{(2)}$.

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