

# SUSY electroweaklike corrections to top pair production in photon-photon collisions

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We study the one-loop contributions of the gaugino-Higgsino sector to the process of top-quark pair production via  $\gamma\gamma$  fusion at the NLC in framework of the minimal supersymmetric standard model. We find that the corrections to  $\gamma\gamma \rightarrow t\bar{t}$  and  $e^+e^- \rightarrow \gamma\gamma \rightarrow t\bar{t}$  are found to be significant and can approach a few percent and one percent, respectively. Furthermore, the dependences of the corrections on the supersymmetric parameters are also investigated. The corrections are not sensitive to  $M_{SU(2)}$  (or  $|\mu|$ ) when  $M_{SU(2)} \gg |\mu|$  (or  $|\mu| \gg M_{SU(2)}$ ) and are weakly dependent on the  $\tan\beta$  with  $M_Q$  (or  $|\mu|$ ) being large enough. However, they are sensitive to the c.m.s. energy of the incoming photons.

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## I. INTRODUCTION

The direct discovery of the top quark was presented in 1995 by the Collider Detector at Fermilab (CDF) and D0 experiments at the Fermilab Tevatron [1]. This is considered to be a remarkable success for the standard model (SM), since the present value of the top quark mass determined by the Particle Data Group (PDG) average is  $173.8 \pm 5.2$  GeV from the direct observation of top events [2], which coincides with the indirect determination from the available precise data of electroweak experiments. But the SM has still some theoretical problems, such as the hierarchy problem, the necessity of fine-tuning, and the nonoccurrence of gauge coupling unification at high energies. The supersymmetric (SUSY) models can solve these problems by presenting an additional symmetry. Among all the extensions of the SM, the minimal supersymmetric standard model (MSSM) [3] is the most attractive one at present, since it is the simplest case of the SUSY models.

Because of the strong Yukawa couplings of the top quark, the SUSY electroweak radiative corrections in the top-quark pair production process are especially interesting. People believe that an accurate measurement of top quark pair production at the present and future colliders should be effective in measuring the physical effects induced by the virtual supersymmetric particles and can afford us much information about the MSSM. Any deviation of the cross section of top-quark pair production from the SM predictions, including QCD and electroweak radiative corrections, would give a hint of new physics beyond the SM. Therefore testing this process to make the indirect search for virtual SUSY particles is an attractive theme at present and future colliders.

In previous studies, many works were concentrated on the top-quark pair production at the  $e^+e^-$  and hadron colliders, such as the CERN  $e^+e^-$  collider LEP2, CERN Large Hadron Collider (LHC), and Tevatron. In Ref. [4], the SUSY QCD and SUSY electroweaklike (EW-like) corrections at  $pp$  colliders are presented. Recently, Hollik and Schappacher calculated the MSSM radiative one-loop corrections to top-quark pair production via  $e^+e^-$  collisions at LEP2 energies and found the relative difference between the pre-

dictions of the MSSM and the SM is typically below 10% [5].

The future Next Linear Collider (NLC) is designed to give the facilities for both  $e^+e^-$  and  $\gamma\gamma$  collisions at the energy of 500–2000 GeV with a luminosity of the order  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$  [6]. A large number of top quark and other particle pairs can be produced at this machine operating in  $\gamma\gamma$  collision mode with an agreeable production rate [7]. The events would be much cleaner than those produced at  $pp$  and  $p\bar{p}$  colliders. It has been also found that the  $t\bar{t}$  production rate in  $\gamma\gamma$  collisions is much larger than that from the direct  $e^+e^- \rightarrow t\bar{t}$  production both with and without considering the threshold QCD effect of top quark pair at center-of-mass energies of the electron-positron system around 1 TeV [8]. Thus the process  $\gamma\gamma \rightarrow t\bar{t}$  has a large potential for studying top quark physics directly.

The next-to-leading order QCD corrections in the SM and MSSM for this process both for polarized and unpolarized photon-photon collisions have been discussed in detail in Ref. [9]. There it was shown that the QCD corrections in both the SM QCD and the MSSM QCD are about 10% and of the order  $-10^{-2}$ , respectively. Denner, Dittmaier, and Strobel calculated the corrections to the process  $\gamma\gamma \rightarrow t\bar{t}$  in the electroweak standard model and found that the correction reduction for unpolarized or equally polarized photons can reach almost 10% close to threshold [10]. In Ref. [11], Li *et al.* calculated the  $O(\alpha m_t^2/m_W^2)$  Yukawa corrections from Higgs sector to top-quark pair production via photon-photon collision in the SM, the general two-Higgs-doublet model (2HDM) as well as the MSSM. They found that the correction to the cross section is about a few percent in the SM, but the correction can be more significant ( $>10\%$ ) in the MSSM. Therefore the SUSY loop contributions have considerable effects. In this paper, we study the possible effects from the additional EW-like one-loop corrections through the virtual presence of charginos, neutralinos and squarks at the NLC. We provide explicit analytical expressions for the form factors which parametrize the one-loop corrections of  $\gamma\gamma \rightarrow t\bar{t}$  subprocess, and present numerical results both for the subprocess and process  $e^+e^- \rightarrow \gamma\gamma \rightarrow t\bar{t}$  at the NLC.

The paper is organized as follows: In Sec. II, the theory about the chargino or neutralino is introduced, and the relative Feynman rules used in the calculation are listed. In Sec. III, we discuss the tree level and one-loop EW-like correction cross section, respectively, and give the explicit analytical formulas for them. In Sec. IV, the numerical results and discussions are described. Finally, we give a short summary. In the Appendixes, the form factors used in the cross section calculations are listed in detail.

## II. LAGRANGIAN AND FEYNMAN RULES

We denote the process of the top-quark pair production via  $\gamma\gamma$  fusion as

$$\gamma(p_3)\gamma(p_4) \rightarrow \bar{t}(p_1)t(p_2), \quad (2.1)$$

where  $p_{1,2}$  and  $p_{3,4}$  represent the four-momenta of the outgoing top quark pair and the incoming photons, respectively. In this work, we consider one-loop corrections of the gaugino-Higgsino sector in the MSSM to this process. At the one-loop EW-like correction order, the vertex  $\gamma\bar{t}t$  is modified by the virtual exchange of two charginos  $\tilde{\chi}_{i=1,2}^{\pm}$  and four neutralinos  $\tilde{\chi}_{i=1-4}^0$ , which are respectively combinations of charged gaugino and Higgsino (for charginos), and neutral gaugino, Higgsino, photino and  $z$ -ino (for neutralinos). The mass eigenstates  $\tilde{\chi}_{1,2,3,4}^0$ ,  $\tilde{\chi}_{1,2}^{\pm}$  for the charginos and neutralinos are respectively obtained by diagonalizing the mass matrices  $X$  and  $Y$  in four component representation [3,12]. The chargino mass term in Lagrangian has the form

$$\mathcal{L}_m = -\frac{1}{2}(\psi^+ \psi^-) \begin{pmatrix} 0 & X^T \\ X & 0 \end{pmatrix} \begin{pmatrix} \psi^+ \\ \psi^- \end{pmatrix}, \quad (2.2)$$

with a  $2 \times 2$   $X$  defined in Ref. [3]. The two masses of chargino  $m_{\tilde{\chi}_{1,2}^{\pm}}$  extracted from the diagonal elements of matrix  $X$  are worked out as

$$\begin{aligned} M_{\pm}^2 = & \frac{1}{2}\{M_{SU(2)}^2 + \mu^2 + 2m_W^2 \pm [(M_{SU(2)}^2 - \mu^2)^2 \\ & + 4m_W^4 \cos^2 2\beta + 4m_W^2(M_{SU(2)}^2 + \mu^2 \\ & + 2M_{SU(2)}\mu \sin 2\beta)]^{1/2}\}. \end{aligned} \quad (2.3)$$

As to the neutralino sector, the mass term in Lagrangian has the form as

$$\mathcal{L}_m = -\frac{1}{2}(\psi^0)^T Y \psi^0 + \text{H.c.} \quad (2.4)$$

The definition of the  $4 \times 4$  matrix  $Y$  can also be found in [3,12].

Since we do not take the  $CP$  violation into account, all the possible  $CP$  phases [12] are assumed to be zero. The physical masses of neutralinos are obtained by utilizing the transformation matrix  $N$  to diagonalize the  $4 \times 4$  mass matrix  $Y$ . The detailed steps to work out  $N$  and the diagonal matrix  $Y_D$  are described in Ref. [12]. The above equations show that the chargino and neutralino masses are related to the MSSM

parameters  $M_{SU(2)}$ ,  $M_{U(1)}$ ,  $\mu$  and  $\tan\beta$ . In our work we adopt the assumption that the  $SU(2) \times U(1)$  theory is embedded in grand unified theory (GUT), so we have the following relation:

$$M_{U(1)} = \frac{5s_W^2}{3c_W^2} M_{SU(2)}. \quad (2.5)$$

In the MSSM, each quark has two scalar partners called squarks:  $\tilde{q}_L$  and  $\tilde{q}_R$ . Without considering  $CP$  phases, the mass matrix of scalar quark takes the following form [13]:

$$-\mathcal{L}_m = (\tilde{q}_L^* \tilde{q}_R^*) \begin{pmatrix} m_{\tilde{q}_L}^2 & a_q m_q \\ a_q m_q & m_{\tilde{q}_R}^2 \end{pmatrix} \begin{pmatrix} \tilde{q}_L \\ \tilde{q}_R \end{pmatrix}. \quad (2.6)$$

The expressions of the masses for the squark current eigenstates are listed in Appendix A, Eqs. (A1)–(A3). Then the masses of  $\tilde{q}_1$  and  $\tilde{q}_2$  read

$$(m_{\tilde{q}_1}^2, m_{\tilde{q}_2}^2) = \frac{1}{2}\{m_{\tilde{q}_L}^2 + m_{\tilde{q}_R}^2 \mp [(m_{\tilde{q}_L}^2 - m_{\tilde{q}_R}^2)^2 + 4a_q^2 m_q^2]^{1/2}\}. \quad (2.7)$$

The Feynman rules for the couplings of  $t - \tilde{b}_{L,R} - \tilde{\chi}_{1,2}^+$  and  $t - \tilde{t}_{L,R} - \tilde{\chi}_{1,2,3,4}^0$  are presented in Ref. [3]. The squark mixing angles  $\theta_b$ ,  $\theta_t$  and phases  $\phi_b$ ,  $\phi_t$  enter in the couplings when the weak eigenstates  $\tilde{q}_L, \tilde{q}_R$  above are transformed into the mass eigenstates  $\tilde{q}_1, \tilde{q}_2$ . In this paper we denote the vertices in squark mass eigenstate basis as

$$\bar{t} - \tilde{b}_i - \tilde{\chi}_j^+ : \quad V_{tb\tilde{\chi}_j^+}^{(1)} P_L + V_{tb\tilde{\chi}_j^+}^{(2)} P_R, \quad (2.8a)$$

$$\bar{t} - \tilde{b}_i - \tilde{\chi}_j^+ : \quad -V_{tb\tilde{\chi}_j^+}^{(2)*} P_L - V_{tb\tilde{\chi}_j^+}^{(1)*} P_R, \quad (2.8b)$$

$$\bar{t} - \tilde{t}_i - \tilde{\chi}_j^0 : \quad V_{ti\tilde{\chi}_j^0}^{(1)} P_L + V_{ti\tilde{\chi}_j^0}^{(2)} P_R, \quad (2.8c)$$

$$\bar{t} - \tilde{t}_i - \tilde{\chi}_j^0 : \quad -V_{ti\tilde{\chi}_j^0}^{(2)*} P_L - V_{ti\tilde{\chi}_j^0}^{(1)*} P_R, \quad (2.8d)$$

respectively, where  $P_{L,R} = \frac{1}{2}(1 \mp \gamma_5)$  and the explicit expressions of the notations defined in Eqs. (2.8a)–(2.8d) are listed in Eqs. (A4)–(A11) in Appendix A.

For the Feynman rules of the Higgs-quark-quark, Higgs-squark-squark, Higgs-chargino-chargino and  $Z(\gamma)$ -chargino-chargino, one can refer to Ref. [3]. The couplings of Higgs( $B$ )– $\tilde{\chi}_k^+ - \tilde{\chi}_k^+$  have a general form as

$$V_{B\tilde{\chi}_k^+\tilde{\chi}_k^+} = V_{B\tilde{\chi}_k^+\tilde{\chi}_k^+}^s + V_{B\tilde{\chi}_k^+\tilde{\chi}_k^+}^{ps} \gamma_5 (B = h^0, H^0, A^0, G^0). \quad (2.9)$$

The notations defined above which appear in the form factors are explicitly expressed in Eqs. (A12)–(A15) of Appendix A.

For Higgs-quark-quark and Higgs-squark-squark couplings, we denote

$$H^0 - t - t: \quad V_{H^0 tt} = \frac{-ig m_t \sin \alpha}{2 m_W \sin \beta}, \quad (2.10a)$$

$$h^0 - t - t: \quad V_{h^0 tt} = \frac{-ig m_t \cos \alpha}{2 m_W \sin \beta}, \quad (2.10b)$$

$$A^0 - t - t: \quad V_{A^0 tt} \gamma_5 = \frac{-g m_t \cot \beta}{2 m_W} \gamma_5. \quad (2.10c)$$

$$G^0 - t - t: \quad V_{G^0 tt} \gamma_5 = \frac{-g m_t}{2 m_W} \gamma_5, \quad (2.10d)$$

The couplings of  $H^0(h^0) - \tilde{q}_i - \tilde{q}_i$  ( $i=1,2, q=t,b$ ) are

$$\begin{aligned} V_{H^0 \tilde{t}_1 \tilde{t}_1} &= \frac{-ig m_Z \cos(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \cos^2 \theta_{\tilde{t}} \right. \\ &\quad \left. + \frac{2}{3} \sin^2 \theta_W \sin^2 \theta_{\tilde{t}} \right] - \frac{ig m_t^2 \sin \alpha}{m_W \sin \beta} \\ &\quad + \frac{ig m_t}{2 m_W \sin \beta} (A_t \sin \alpha + \mu \cos \alpha) \sin \theta_{\tilde{t}} \cos \theta_{\tilde{t}}, \end{aligned} \quad (2.11a)$$

$$\begin{aligned} V_{H^0 \tilde{t}_2 \tilde{t}_2} &= \frac{-ig m_Z \cos(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \sin^2 \theta_{\tilde{t}} \right. \\ &\quad \left. + \frac{2}{3} \sin^2 \theta_W \cos^2 \theta_{\tilde{t}} \right] - \frac{ig m_t^2 \sin \alpha}{m_W \sin \beta} \\ &\quad - \frac{ig m_t}{2 m_W \sin \beta} (A_t \sin \alpha + \mu \cos \alpha) \sin \theta_{\tilde{t}} \cos \theta_{\tilde{t}}, \end{aligned} \quad (2.11b)$$

$$\begin{aligned} V_{H^0 \tilde{b}_1 \tilde{b}_1} &= \frac{ig m_Z \cos(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{1}{3} \sin^2 \theta_W \right) \cos^2 \theta_{\tilde{b}} \right. \\ &\quad \left. + \frac{1}{3} \sin^2 \theta_W \sin^2 \theta_{\tilde{b}} \right] - \frac{ig m_b^2 \cos \alpha}{m_W \cos \beta} \\ &\quad + \frac{ig m_b}{2 m_W \cos \beta} (A_b \cos \alpha + \mu \sin \alpha) \sin \theta_{\tilde{b}} \cos \theta_{\tilde{b}}, \end{aligned} \quad (2.11c)$$

$$\begin{aligned} V_{H^0 \tilde{b}_2 \tilde{b}_2} &= \frac{ig m_Z \cos(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{1}{3} \sin^2 \theta_W \right) \sin^2 \theta_{\tilde{b}} \right. \\ &\quad \left. + \frac{1}{3} \sin^2 \theta_W \cos^2 \theta_{\tilde{b}} \right] - \frac{ig m_b^2 \cos \alpha}{m_W \cos \beta} \\ &\quad - \frac{ig m_b}{2 m_W \cos \beta} (A_b \cos \alpha + \mu \sin \alpha) \sin \theta_{\tilde{b}} \cos \theta_{\tilde{b}}, \end{aligned} \quad (2.11d)$$

$$\begin{aligned} V_{h^0 \tilde{t}_1 \tilde{t}_1} &= \frac{ig m_Z \sin(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \cos^2 \theta_{\tilde{t}} \right. \\ &\quad \left. + \frac{2}{3} \sin^2 \theta_W \sin^2 \theta_{\tilde{t}} \right] - \frac{ig m_t^2 \cos \alpha}{m_W \sin \beta} \\ &\quad + \frac{ig m_t}{2 m_W \sin \beta} (A_t \cos \alpha - \mu \sin \alpha) \sin \theta_{\tilde{t}} \cos \theta_{\tilde{t}}, \end{aligned} \quad (2.11e)$$

$$\begin{aligned} V_{h^0 \tilde{t}_2 \tilde{t}_2} &= \frac{ig m_Z \sin(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \sin^2 \theta_{\tilde{t}} \right. \\ &\quad \left. + \frac{2}{3} \sin^2 \theta_W \cos^2 \theta_{\tilde{t}} \right] - \frac{ig m_t^2 \cos \alpha}{m_W \sin \beta} \\ &\quad - \frac{ig m_t}{2 m_W \sin \beta} (A_t \cos \alpha - \mu \sin \alpha) \sin \theta_{\tilde{t}} \cos \theta_{\tilde{t}}, \end{aligned} \quad (2.11f)$$

$$\begin{aligned} V_{h^0 \tilde{b}_1 \tilde{b}_1} &= \frac{-ig m_Z \sin(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{1}{3} \sin^2 \theta_W \right) \cos^2 \theta_{\tilde{b}} \right. \\ &\quad \left. + \frac{1}{3} \sin^2 \theta_W \sin^2 \theta_{\tilde{b}} \right] + \frac{ig m_b^2 \sin \alpha}{m_W \cos \beta} \\ &\quad - \frac{ig m_b}{2 m_W \cos \beta} (A_b \sin \alpha - \mu \cos \alpha) \sin \theta_{\tilde{b}} \cos \theta_{\tilde{b}}, \end{aligned} \quad (2.11g)$$

$$\begin{aligned} V_{h^0 \tilde{b}_2 \tilde{b}_2} &= \frac{-ig m_Z \sin(\alpha + \beta)}{\cos \theta_W} \left[ \left( \frac{1}{2} - \frac{1}{3} \sin^2 \theta_W \right) \sin^2 \theta_{\tilde{b}} \right. \\ &\quad \left. + \frac{1}{3} \sin^2 \theta_W \cos^2 \theta_{\tilde{b}} \right] + \frac{ig m_b^2 \sin \alpha}{m_W \cos \beta} \\ &\quad + \frac{ig m_b}{2 m_W \cos \beta} (A_b \sin \alpha - \mu \cos \alpha) \sin \theta_{\tilde{b}} \cos \theta_{\tilde{b}}, \end{aligned} \quad (2.11h)$$

respectively.

### III. CALCULATIONS

In the calculation, we take the 't Hooft gauge and adopt the dimensional reduction (DR) scheme [14], which is commonly used in the calculations of the MSSM radiative corrections as it preserves supersymmetry at least at one-loop order, to eliminate the ultraviolet divergences in the virtual loop corrections. We choose the on-mass-shell (OMS) scheme [15] for doing renormalization.

#### A. The tree-level formulas and notations

In the process of top-quark pair production via photon-photon collision, the Mandelstam variables  $\hat{s}$ ,  $\hat{t}$  and  $\hat{u}$  are defined as  $\hat{s}=(p_1+p_2)^2$ ,  $\hat{t}=(p_1-p_3)^2$ ,  $\hat{u}=(p_1-p_4)^2$ . The

corresponding Lorentz invariant matrix element at the lowest order for the reaction  $\gamma\gamma \rightarrow t\bar{t}$  is written as

$$\mathcal{M}_0 = \mathcal{M}_t + \mathcal{M}_{\bar{t}}, \quad (3.1a)$$

where

$$\mathcal{M}_t = \left[ \bar{u}(p_3)(-ie\gamma_\mu) \frac{i}{\hat{t} - m_t} (-ie\gamma_\nu) v(p_4) \epsilon^\mu(p_1) \epsilon^\nu(p_2) \right], \quad (3.1b)$$

$$\mathcal{M}_{\bar{t}} = \left[ \bar{u}(p_3)(-ie\gamma_\nu) \frac{i}{\hat{t} - m_t} (-ie\gamma_\mu) v(p_4) \epsilon^\nu(p_2) \epsilon^\mu(p_1) \right]. \quad (3.1c)$$

The corresponding differential cross section is obtained by

$$\frac{d\hat{\sigma}_0(\hat{t}, \hat{s})}{d\hat{t}} = \frac{N_c}{16\pi^2 \hat{s}} \overline{\sum_{spins}} |\mathcal{M}_0|^2, \quad (3.1d)$$

where the summation with a bar overhead means the sum of the spins of final states and the average of the spins of initial photons. After integration over  $\hat{t}$ , the total Born cross section with unpolarized incoming photons is worked out as

$$\hat{\sigma}_0(\hat{s}) = \frac{32\pi\alpha^2}{27\hat{s}} \left[ 2\hat{\beta}(\hat{\beta}^2 - 2) + (3 - \hat{\beta}^4) \ln \frac{1 + \hat{\beta}}{1 - \hat{\beta}} \right], \quad (3.1e)$$

where the kinematic factor is defined as

$$\hat{\beta} = \sqrt{1 - 4m_t^2/\hat{s}}. \quad (3.1f)$$

The total cross section including the leading one-loop corrections in the frame of the MSSM is

$$\hat{\sigma} = \hat{\sigma}_0 + \delta\hat{\sigma}^{1-loop}, \quad (3.1g)$$

where  $\delta\hat{\sigma}^{1-loop}$  represents the interference term between tree level and one-loop correction amplitudes.

## B. Self-energies

The top quark wave function corrections  $\delta Z_{tt}$ 's are determined in terms of the one-particle irreducible two-point function  $i\Gamma(p^2)$  for top quarks in the dimensional reduction (DR) mass basis. It should be written as [16]

$$\begin{aligned} \Gamma_{tt}(p^2) = & (\not{p} - m_t) + [\not{p} P_L \Sigma_{tt}^L(p^2) + \not{p} P_R \Sigma_{tt}^R(p^2) \\ & + P_L \Sigma_{tt}^{S,L}(p^2) + P_R \Sigma_{tt}^{S,R}(p^2)]. \end{aligned} \quad (3.2a)$$

With the Feynman rules of the interactions of top-quark–bottom-squark–chargino and top-quark–top-squark–neutralino, the corresponding unrenormalized chargino self-energies read [see Fig. 1(f)]

$$\Sigma_{tt}^{S,L}(p^2) = \frac{1}{16\pi^2} \sum_{j=1,2} \left( \sum_{i=1,4} m_{\tilde{\chi}_i^0} V_{\tilde{t}_j \tilde{\chi}_i^0}^{(1)} V_{\tilde{t}_j \tilde{\chi}_i^0}^{(2)*} B_0[-p, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}] + \sum_{i=1,2} m_{\tilde{\chi}_i^+} V_{\tilde{t}_j \tilde{\chi}_i^+}^{(1)} V_{\tilde{t}_j \tilde{\chi}_i^+}^{(2)*} B_0[-p, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] \right), \quad (3.2b)$$

$$\Sigma_{tt}^{S,R}(p^2) = \frac{1}{16\pi^2} \sum_{j=1,2} \left( \sum_{i=1,4} m_{\tilde{\chi}_i^0} V_{\tilde{t}_j \tilde{\chi}_i^0}^{(2)} V_{\tilde{t}_j \tilde{\chi}_i^0}^{(1)*} B_0[-p, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}] + \sum_{i=1,2} m_{\tilde{\chi}_i^+} V_{\tilde{t}_j \tilde{\chi}_i^+}^{(2)} V_{\tilde{t}_j \tilde{\chi}_i^+}^{(1)*} B_0[-p, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] \right), \quad (3.2c)$$

$$\Sigma_{tt}^L(p^2) = -\frac{1}{16\pi^2} \sum_{j=1,2} \left( \sum_{i=1,4} |V_{\tilde{t}_j \tilde{\chi}_i^0}^{(2)}|^2 B_1[-p, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}] + \sum_{i=1,2} |V_{\tilde{t}_j \tilde{\chi}_i^+}^{(2)}|^2 B_1[-p, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] \right), \quad (3.2d)$$

$$\Sigma_{tt}^R(p^2) = -\frac{1}{16\pi^2} \sum_{j=1,2} \left( \sum_{i=1,4} |V_{\tilde{t}_j \tilde{\chi}_i^0}^{(1)}|^2 B_1[-p, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}] + \sum_{i=1,2} |V_{\tilde{t}_j \tilde{\chi}_i^+}^{(1)}|^2 B_1[-p, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] \right). \quad (3.2e)$$

Imposing the on-shell renormalization conditions given in Refs. [15,16], one can obtain the renormalization constants for the renormalized top quark self-energies as [9]

$$\delta\Sigma_{tt}(p^2) = C_L \not{P}_L + C_R \not{P}_R - C_S^- P_L - C_S^+ P_R. \quad (3.2f)$$

The  $\gamma\gamma$  and  $\gamma Z^0$  self-energies with only quark and squark one loops were presented in Ref. [17]. We can see that the

self-energies of  $\gamma\gamma$  and  $\gamma Z^0$  have no contribution to the relevant counterterms of the  $\gamma tt$  vertex. The renormalization constant for the  $\Gamma_{\gamma tt}^\mu$  vertex is written in the form

$$\delta\Gamma_{\gamma tt}^\mu = -ie\gamma^\mu [C^L P_L + C^R P_R], \quad (3.2g)$$

where

$$\begin{aligned} C_L &= \frac{1}{2} (\delta Z_{tt}^L + \delta Z_{tt}^{L\dagger}), \\ C_R &= \frac{1}{2} (\delta Z_{tt}^R + \delta Z_{tt}^{R\dagger}), \\ C_S^- &= \frac{m_t}{2} (\delta Z_{tt}^L + \delta Z_{tt}^{R\dagger}) + \delta m_t, \\ C_S^+ &= \frac{m_t}{2} (\delta Z_{tt}^R + \delta Z_{tt}^{L\dagger}) + \delta m_t, \end{aligned} \quad (3.2h)$$

$$\begin{aligned} \delta m_t &= \frac{1}{2} \widetilde{\text{Re}} [m_t \Sigma_{tt}^L(m_t^2) + m_t \Sigma_{tt}^R(m_t^2) + \Sigma_{tt}^{S,L}(m_t^2) \\ &\quad + \Sigma_{tt}^{S,R}(m_t^2)], \end{aligned} \quad (3.2i)$$

$$\begin{aligned} \delta Z_{tt}^L &= -\widetilde{\text{Re}} \Sigma_{tt}^L(m_t^2) - \frac{1}{m_t} \widetilde{\text{Re}} [\Sigma_{tt}^{S,R}(m_t^2) - \Sigma_{tt}^{S,L}(m_t^2)] \\ &\quad - m_t \frac{\partial}{\partial p^2} \widetilde{\text{Re}} \{m_t \Sigma_{tt}^L(p^2) + m_t \Sigma_{tt}^R(p^2) + \Sigma_{tt}^{S,L}(p^2) \\ &\quad + \Sigma_{tt}^{S,R}(p^2)\}|_{p^2=m_t^2}, \end{aligned} \quad (3.2j)$$

$$\begin{aligned} \delta Z_{tt}^R &= -\widetilde{\text{Re}} \Sigma_{tt}^R(m_t^2) - m_t \frac{\partial}{\partial p^2} \widetilde{\text{Re}} \{m_t \Sigma_{tt}^L(p^2) + m_t \Sigma_{tt}^R(p^2) \\ &\quad + \Sigma_{tt}^{S,L}(p^2) + \Sigma_{tt}^{S,R}(p^2)\}|_{p^2=m_t^2}, \end{aligned} \quad (3.2k)$$

where  $\widetilde{\text{Re}}$  takes the real part of the loop integrals. It ensures reality of the renormalized Lagrangian.

### C. Renormalized one-loop corrections

The renormalized one-loop matrix element involves the contributions from all the self-energy, vertex, box, triangle and quartic interaction one-loop diagrams and their relevant counterterms. The Feynman diagrams for the process (2.1) are depicted in Fig. 1, where (a) is for the tree level and (b)–(f) are EW-like one-loop diagrams contributing to the cross section in the frame of the MSSM. Specifically, Fig. 1(b.1–4) are the vertex diagrams, Fig. 1(c.1–3) are the box diagrams, Fig. 1(d.1–2) are the quartic interactions, Fig. 1(e.1–2) are the triangle sectors, and Fig. 1(f) is the self-energy diagram. Below we denote them by the upper indexes of  $v$ ,  $b$ ,  $q$ ,  $tr$  and  $self$ , respectively. The relevant Feynman rules are shown in Sec. II [3]. In the calculation, some of the  $s$ -channel Feynman diagrams involving quark loops with the exchanging of  $\gamma$  or  $Z^0$  boson in Fig. 1(e.2) can be neglected, as the consequence of Furry theorem. This is because Furry theorem forbids the production of the spin-one components of the  $Z^0$  and  $\gamma$ , and the contribution from the spin-zero component of the  $Z^0$  vector boson coupling with a pair of chargino is very small and neglectable. The calculation also shows the  $\gamma$  and  $Z^0$  exchanging  $s$ -channel diagrams in Fig. 1(d.2) and Fig. 1(e.1) with a squark loop have no contribution to the cross section, in which the contribution from each of the  $\gamma$  and  $Z^0$  exchanging  $s$ -channel diagrams in Fig. 1(e.1) is canceled out by the corresponding one with exchanging incoming photons. Including all the diagrams appearing in Fig. 1, the renormalized matrix elements for  $t\bar{t}$  pair production in  $\gamma\gamma$  collision is written as

$$\begin{aligned} \delta \mathcal{M}_{1-loop} &= \mathcal{M}^v + \mathcal{M}^b + \mathcal{M}^q + \mathcal{M}^{tr} + \mathcal{M}^{self} \\ &= \mathcal{M}^{v,\hat{t}} + \mathcal{M}^{v,\hat{u}} + \mathcal{M}^{b,\hat{t}} + \mathcal{M}^{b,\hat{u}} + \mathcal{M}^q + \mathcal{M}^{tr,\hat{t}} + \mathcal{M}^{tr,\hat{u}} + \mathcal{M}^{self,\hat{t}} + \mathcal{M}^{self,\hat{u}} \\ &= \epsilon^\mu(p_3) \epsilon^\nu(p_4) \bar{u}(p_1) \{ f_1 \gamma_\mu \gamma_\nu + f_2 \gamma_\nu \gamma_\mu + f_3 \gamma_\mu p_{1\nu} + f_4 \gamma_\mu p_{2\nu} + f_5 \gamma_\nu p_{1\mu} + f_6 \gamma_\nu p_{2\mu} + f_7 p_{1\mu} p_{1\nu} + f_8 p_{1\mu} p_{2\nu} \\ &\quad + f_9 p_{1\nu} p_{2\mu} + f_{10} p_{2\mu} p_{2\nu} + f_{11} \not{p}_3 \gamma_\mu \gamma_\nu + f_{12} \not{p}_3 \gamma_\nu \gamma_\mu + f_{13} \not{p}_3 \gamma_\mu p_{1\nu} + f_{14} \not{p}_3 \gamma_\mu p_{2\nu} + f_{15} \not{p}_3 \gamma_\nu p_{1\mu} + f_{16} \not{p}_3 \gamma_\nu p_{2\mu} \\ &\quad + f_{17} \not{p}_3 p_{1\mu} p_{1\nu} + f_{18} \not{p}_3 p_{1\mu} p_{2\nu} + f_{19} \not{p}_3 p_{1\nu} p_{2\mu} + f_{20} \not{p}_3 p_{2\mu} p_{2\nu} + f_{21} \gamma_5 \epsilon_{\mu\nu\alpha\beta} \not{p}_1^\alpha \not{p}_3^\beta + f_{22} \gamma_5 \epsilon_{\mu\nu\alpha\beta} \not{p}_2^\alpha \not{p}_3^\beta \} v(p_2), \end{aligned} \quad (3.3a)$$

with form factors

$$f_i = f_i^v + f_i^b + f_i^q + f_i^{tr} + f_i^{self} \quad (i=1-22). \quad (3.3b)$$

Here we have divided each matrix element  $\mathcal{M}^v$ ,  $\mathcal{M}^b$ ,  $\mathcal{M}^{tr}$  and  $\mathcal{M}^{self}$  into  $t$ -channel and  $u$ -channel parts. For each of the corresponding form factors we have

$$f_i^k = f_i^{k,\hat{t}} + f_i^{k,\hat{u}} \quad (k=v,b,tr,self, \quad i=1-22). \quad (3.3c)$$

The vertex, box and triangle diagrams with exchanging photons (i.e.,  $u$ -channel) are not shown in Fig. 1. The amplitude parts from the  $u$ -channel vertex, box and quartic interaction corrections can be obtained from the  $t$  channels by doing exchanges as below:

$$\mathcal{M}^{j,\hat{u}} = \mathcal{M}^{j,\hat{t}}(t \rightarrow u, p_3 \leftrightarrow p_4, \mu \leftrightarrow \nu) \quad (j=v,b,tr,s). \quad (3.3d)$$

Then we list only the explicit  $t$ -channel form factors in

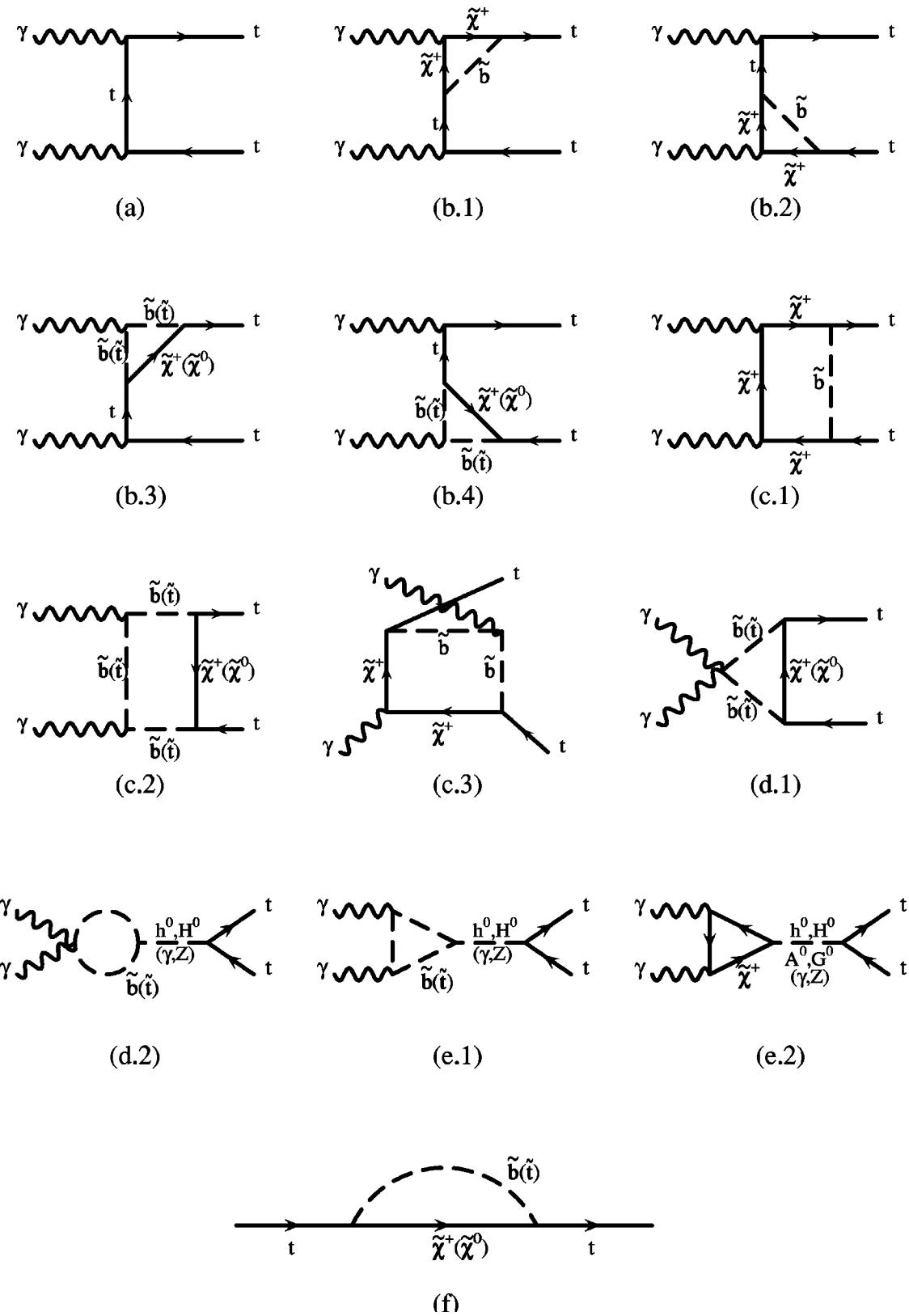


FIG. 1. The Feynman diagrams at tree level and EW-like one-loop diagrams in the MSSM for subprocess  $\gamma\gamma \rightarrow t\bar{t}$ . (a) Tree level diagram; (b) vertex diagrams; (c) box diagrams; (d) quartic coupling diagram; (e) triangle diagrams, and (f) self-energy diagrams. The  $\tilde{t}$  and  $\tilde{b}$  that appear in diagrams have two physical particle eigenstates, while  $\tilde{\chi}^0$  have four mass eigenstates, and  $\tilde{\chi}^\pm$  have two. The diagrams with exchanging incoming photons are not shown in the figures except for (d).

Appendix B. Now we can obtain the one-loop corrections to the cross section from the chargino and neutralino sectors for this subprocess in unpolarized photon collisions:

$$\delta\hat{\sigma}^{1-loop}(\hat{s}) = \frac{N_c}{16\pi\hat{s}^2} \int_{\hat{t}^-}^{\hat{t}^+} d\hat{t} 2 \operatorname{Re} \sum_{spins} (\mathcal{M}_0^\dagger \cdot \delta\mathcal{M}_{1-loop}), \quad (3.3e)$$

where  $\hat{t}^\pm = (m_t^2 - \frac{1}{2}\hat{s}) \pm \frac{1}{2}\hat{s}\beta$ . The cross section of the top-quark pair production via photon-photon fusion at the  $e^+e^-$  linear collider, can be obtained by folding the cross section of the subprocess  $\hat{\sigma}(\gamma\gamma \rightarrow t\bar{t})$  with the photon luminosity [18,19].

#### IV. NUMERICAL RESULTS AND DISCUSSIONS

The SUSY EW-like corrections to top-quark pair production process are strongly related to the fundamental MSSM parameters through the electroweak couplings involving top-quark, squark and chargino (neutralino), i.e.,  $V_{tb\tilde{\chi}^+}$  and  $V_{t\tilde{b}\tilde{\chi}^0}$  as expressed in Eqs. (2.8a)–(2.8d). For our numerical calculation of squark sector, we take  $M_Q$ ,  $\theta_t$  and  $\theta_b$  as input parameters, and we set  $\theta_b=0$ , and  $\theta_t$  approaches  $\pi/4$ , so that the masses of top squark pair split remarkably, while the split of the sbottom masses is minimized. From Eq. (2.7) and relevant expressions, we can see that the parameter  $M_Q$  is strongly related to the masses of top and bottom squarks, therefore it would affect the MSSM correction quantitatively in some regions of the parameter space.

As stated in Sec. II, the correction should also depend on the fundamental MSSM parameters  $\tan\beta$ ,  $M_{SU(2)}$  and  $\mu$  through gaugino and Higgsino couplings. Note that these parameters take part in the EW-like corrections not only through the chargino and neutralino mass spectra, but also through the couplings including their transformation matrices  $U$ ,  $V$  and  $N$ .

We take some of the general constants as  $m_t=175$  GeV,  $m_Z=91.187$  GeV,  $m_b=4.5$  GeV,  $\sin^2\theta_W=0.2315$ , and  $\alpha=1/128$ . And we adopt the following set of input parameters by default, in case the parameter is not set as the independent variable of the figure and no special declaration has been presented on them:

$$\sqrt{\hat{s}}=500 \text{ or } 1000 \text{ GeV}, \quad \tan\beta=4 \text{ or } 40,$$

$$M_Q=M_{SU(2)}=\mu=200 \text{ GeV}, \quad (4.1)$$

$$\theta_t=44.325^\circ, \quad \theta_b=0.$$

We use the analytical formulas for the masses of the MSSM Higgs bosons (including two-loop leading-log corrections and squark mixing effects) given in Refs. [20,21]:

$$m_{h^0,H^0}^2 = \frac{1}{2} [\operatorname{Tr} M^2 \mp \sqrt{(\operatorname{Tr} M^2)^2 - 4 \det M^2}], \quad (4.2a)$$

where

$$\operatorname{Tr} M^2 = M_{11}^2 + M_{22}^2, \quad \det M^2 = M_{11}^2 M_{22}^2 - (M_{12}^2)^2, \quad (4.2b)$$

with

$$\begin{aligned} M_{12}^2 &= 2v^2 [\sin\beta \cos\beta (\lambda_3 + \lambda_4) + \lambda_6 \cos^2\beta + \lambda_7 \sin^2\beta] \\ &\quad - m_{A^0}^2 \sin\beta \cos\beta, \\ M_{11}^2 &= 2v^2 [\lambda_1 \cos^2\beta + 2\lambda_6 \cos\beta \sin\beta + \lambda_5 \sin^2\beta] \\ &\quad + m_{A^0}^2 \sin^2\beta, \\ M_{22}^2 &= 2v^2 [\lambda_2 \sin^2\beta + 2\lambda_7 \cos\beta \sin\beta + \lambda_5 \cos^2\beta] \\ &\quad + m_{A^0}^2 \cos^2\beta, \end{aligned} \quad (4.2c)$$

where  $v=174.1$  GeV. The mixing angle  $\alpha$  is determined by

$$\sin 2\alpha = \frac{2M_{12}^2}{\sqrt{(\operatorname{Tr} M^2)^2 - 4 \det M^2}}. \quad (4.2d)$$

One can find the explicit expressions of  $\lambda_i (i=1, \dots, 7)$  in Ref. [20]. In this work, we take  $m_{A^0}=150$  GeV.

Our numerical results are presented in the figures. In Figs. 2(a) and 2(b), the correction  $\Delta\sigma$  and the relative correction  $\delta=\Delta\sigma/\sigma_0$  of the process (2.1) depending on the c.m.s. energy  $\sqrt{\hat{s}}$  are plotted, respectively. From our analyses, we expect that for the curves of  $\tan\beta=4$  in Figs. 2(a) and 2(b), there should be some spikes or turning points at  $\sqrt{\hat{s}} \sim 2m_{\tilde{b}_1}=403$  GeV,  $2m_{\tilde{b}_2}=415$  GeV,  $2m_{\tilde{\chi}_2^+}=546$  GeV, and  $2m_{\tilde{t}_2}=628$  GeV due to the resonance effects. But we see in both figures that the first two resonance points merge each other in the curves of  $\tan\beta=4$  because they are too near. For  $\tan\beta=40$ , there are only two obvious resonance points that can be seen on the curve in Fig. 2(a) in the vicinities of  $\sqrt{\hat{s}} \sim 2m_{\tilde{b}_1} \sim 2m_{\tilde{b}_2} \sim 410$  GeV and  $\sqrt{\hat{s}}=2m_{\tilde{\chi}_2^+}=531$  GeV, while only one obvious resonance peak can be seen on the curve of  $\tan\beta=40$  at  $\sqrt{\hat{s}}=2m_{\tilde{\chi}_2^+}=531$  GeV in Fig. 2(b).

In Figs. 3–6 we depicted the dependences of the relative radiative correction on the fundamental supersymmetric input parameters  $M_Q$ ,  $M_{SU(2)}$  and  $|\mu|$ , respectively. In each figure we take four data sets for discussion: (1)  $\tan\beta=4$ ,  $\sqrt{\hat{s}}=500$  GeV; (2)  $\tan\beta=40$ ,  $\sqrt{\hat{s}}=500$  GeV; (3)  $\tan\beta=4$ ,  $\sqrt{\hat{s}}=1$  TeV; (4)  $\tan\beta=40$ ,  $\sqrt{\hat{s}}=1$  TeV. From Fig. 3 one can see the absolute value of the relative correction becomes generally larger when  $\sqrt{\hat{s}}$  goes higher. The same feature is also shown in Fig. 2. Figure 3 presents that the absolute value of the relative correction goes down to a smaller constant with  $M_Q$  increasing. Since  $M_Q$  is related to the masses of squarks  $\tilde{t}_{1,2}$  and  $\tilde{b}_{1,2}$  as stated in Eq. (2.7), it can be easily understood as the feature of the decoupling effect. We can conclude that the smaller  $M_Q$  is, the more significant the correction can be. We can read from Fig. 3 that the relative correction can reach  $-2\%$  when  $M_Q$  is about 150 GeV, and for large  $M_Q$  with the same  $\sqrt{\hat{s}}$  the parameter  $\tan\beta$  tends to make little difference on the relative correction. In Fig. 4, the corrections as the function of  $M_{SU(2)}$  are plotted with the four data sets. The grooves around 230 GeV on the two curves for  $\sqrt{\hat{s}}=500$  GeV and the small heaves in the vicinity

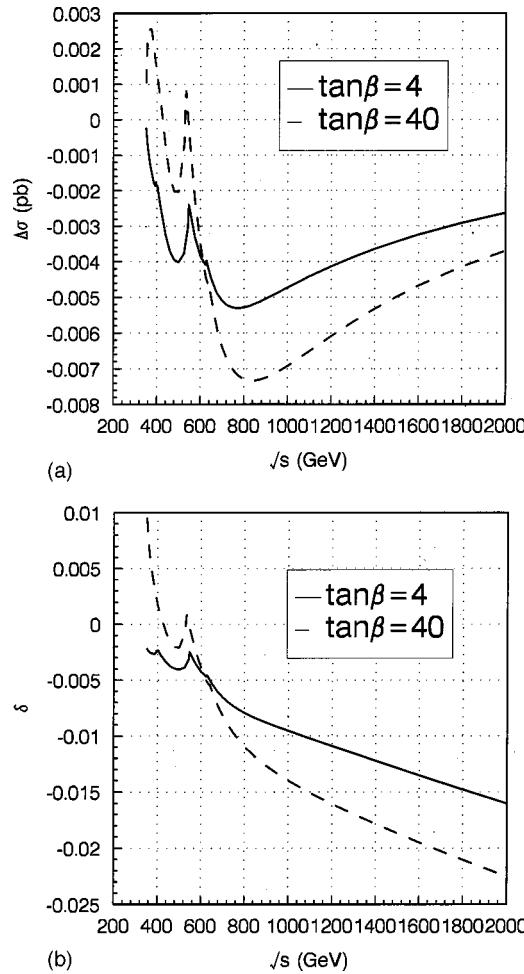


FIG. 2. The corrections as the functions of c.m.s. energy  $\sqrt{s}$  for subprocess  $\gamma\gamma \rightarrow t\bar{t}$ . (a) The absolute corrections; (b) the relative corrections. The solid line is for  $\tan\beta=4$  and the dashed line is for  $\tan\beta=40$ .

of 450 GeV on the two curves of  $\sqrt{s}=1$  TeV, are all because of the resonance effect:  $\sqrt{\hat{s}} \sim 2m_{\tilde{\chi}_2^+}$ . When  $M_{SU(2)}$  is large, all of the four curves become very plain because of the decoupling effect. In Fig. 5, there are two peaks at the position about  $\mu \sim 470$  GeV on the curves of  $\sqrt{s}=1$  TeV due to the resonance effect, but the resonance effects around the region  $\mu \sim 230$  GeV on the curves with  $\sqrt{s}=500$  GeV are not clear. And we can see that the correction is no longer sensitive to  $\tan\beta$  and  $\mu$  when  $\mu$  gets larger than 600 GeV. This is because the parameter  $\tan\beta$  and  $\mu$  are not only related to the masses of sparticles, but also involved in some vertices which are concerned in our calculation. Both Fig. 4 and Fig. 5 show that the higher the c.m.s. energy  $\sqrt{s}$  is, the larger the relative corrections to subprocess are.

Figure 6 shows the cross section of the parent process  $e^+e^- \rightarrow \gamma\gamma \rightarrow t\bar{t}$  including one-loop EW-like corrections as the function of c.m.s energy of incoming electron-positron pair. In Fig. 7, the relative corrections for  $\tan\beta=4$  and  $\tan\beta=40$  are plotted, respectively. It is clear that the absolute value of the relative correction becomes larger with the increasing of the  $e^+e^-$  c.m.s energy. The reduction of the

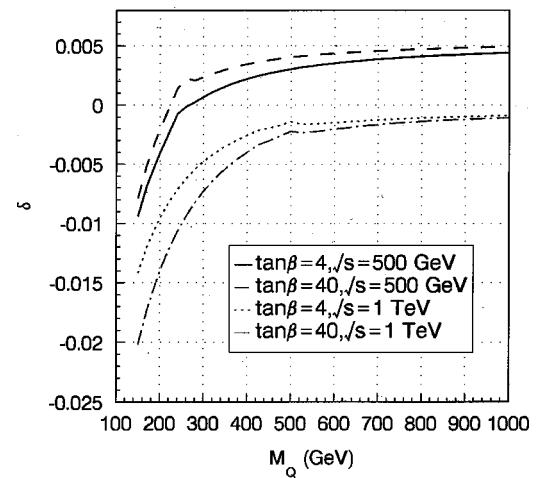


FIG. 3. The relative corrections as the functions of  $M_Q$  for subprocess  $\gamma\gamma \rightarrow t\bar{t}$ . The solid line is for  $\tan\beta=4$ ,  $\sqrt{s}=500$  GeV, the dashed line is for  $\tan\beta=40$ ,  $\sqrt{s}=500$  GeV, the dotted line is for  $\tan\beta=4$ ,  $\sqrt{s}=1$  TeV, and the dash-dotted line is for  $\tan\beta=40$ ,  $\sqrt{s}=1$  TeV.

cross section of the parent process due to the one-loop EW-like correction can approach one percent.

## V. SUMMARY

In this work we have studied the complete one-loop radiative corrections from the gaugino-Higgsino sector in the process  $\gamma\gamma \rightarrow t\bar{t}$  in the frame of the MSSM at the NLC. This process has great importance at the future NLC operating in photon-photon collision mode. From the numerical calculation with several typical sets of input parameters, we find that the EW-like corrections from the chargino or neutralino sector can be a few percent for subprocess and can approach one percent for the parent process. These corrections are smaller than the QCD corrections, but are comparable to the

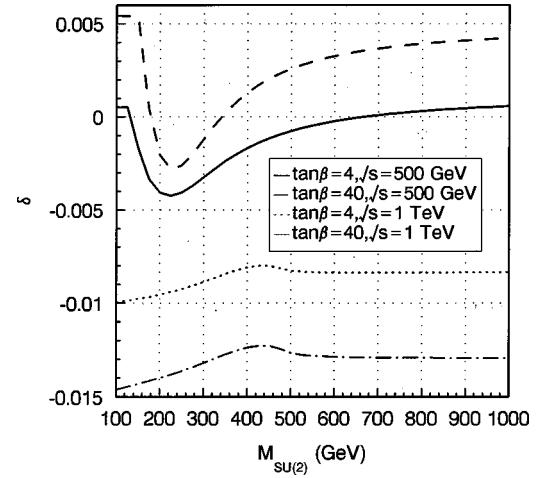


FIG. 4. The relative corrections as the functions of  $M_{SU(2)}$  for subprocess  $\gamma\gamma \rightarrow t\bar{t}$ . The solid line is for  $\tan\beta=4$ ,  $\sqrt{s}=500$  GeV, the dashed line is for  $\tan\beta=40$ ,  $\sqrt{s}=500$  GeV, the dotted line is for  $\tan\beta=4$ ,  $\sqrt{s}=1$  TeV, and the dash-dotted line is for  $\tan\beta=40$ ,  $\sqrt{s}=1$  TeV.

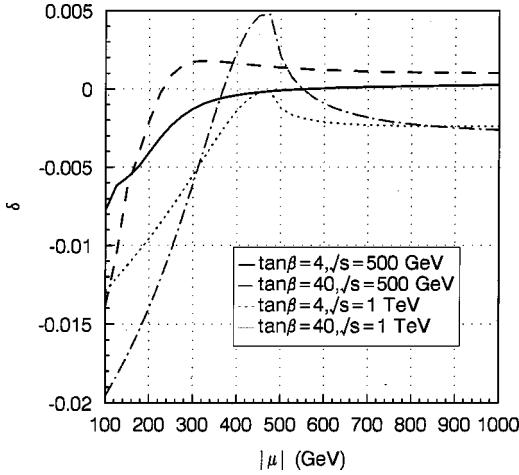


FIG. 5. The relative corrections as the functions of  $\mu$  for subprocess  $\gamma\gamma \rightarrow t\bar{t}$ . The solid line is for  $\tan \beta=4$ ,  $\sqrt{s}=500$  GeV, the dashed line is for  $\tan \beta=40$ ,  $\sqrt{s}=500$  GeV, the dotted line is for  $\tan \beta=4$ ,  $\sqrt{s}=1$  TeV, and the dash-dotted line is for  $\tan \beta=40$ ,  $\sqrt{s}=1$  TeV.

electroweak correction part from the Higgs sector in the MSSM. Therefore the correction from chargino or neutralino sector is also significant and unneglectable. We investigated also the dependences of the corrections on the supersymmetric parameters. With the variation of the parameters  $M_Q$ ,  $M_{SU(2)}$  and  $|\mu|$ , we can see some physical features, such as the decoupling effects, threshold effects and the resonance effects, where the relative correction can be significantly enhanced or diminished. We conclude that the EW-like one-loop correction to Born cross section is strongly dependent on the c.m.s. energy and the related MSSM parameters in some cases. We find that the correction is not sensitive to  $M_{SU(2)}$  (or  $|\mu|$ ) when  $M_{SU(2)} \gg |\mu|$  (or  $|\mu| \gg M_{SU(2)}$ ). The correction is weakly dependent on the ratio of the vacuum expectation values  $\tan \beta$ , when  $M_Q$  (or  $|\mu|$ ) is large enough. But it is related to the c.m. energy of the incoming photons obviously.

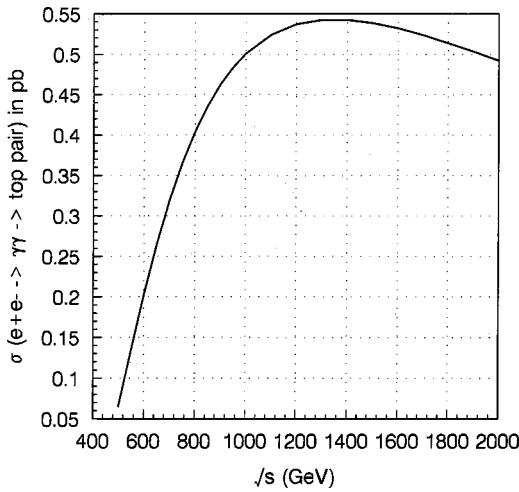


FIG. 6. The cross section including the contributions of one-loop EW-like corrections for the parent process as the function of  $e^+e^-$  energy  $\sqrt{s}$ .

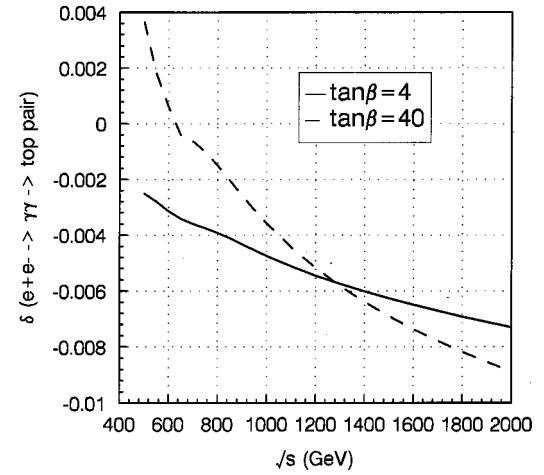


FIG. 7. The relative correction for the parent process as the function of  $e^+e^-$  energy  $\sqrt{s}$ . The solid line is for  $\tan \beta=4$  and the dashed line is for  $\tan \beta=40$ .

## ACKNOWLEDGMENTS

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## APPENDIX A: SOME EXPRESSIONS DEFINED IN LAGRANGIAN

In the Lagrangian shown in Eq. (2.6), we denote  $\tilde{q}_L$  and  $\tilde{q}_R$  as the current eigenstates. For the up-type scalar quarks, we have

$$\begin{aligned} m_{\tilde{q}_L}^2 &= \tilde{M}_Q^2 + m_q^2 + m_Z^2 \left( \frac{1}{2} - Q_q s_W^2 \right) \cos 2\beta, \\ m_{\tilde{q}_R}^2 &= \tilde{M}_U^2 + m_q^2 + Q_q m_Z^2 s_W^2 \cos 2\beta, \\ a_q &= \mu \cot \beta + A_q \tilde{M}. \end{aligned} \quad (\text{A1})$$

For the down-type scalar quarks,

$$\begin{aligned} m_{\tilde{q}_L}^2 &= \tilde{M}_Q^2 + m_q^2 - m_Z^2 \left( \frac{1}{2} + Q_q s_W^2 \right) \cos 2\beta, \\ m_{\tilde{q}_R}^2 &= \tilde{M}_D^2 + m_q^2 + Q_q m_Z^2 s_W^2 \cos 2\beta, \\ a_q &= \mu \tan \beta + A_q \tilde{M}, \end{aligned} \quad (\text{A2})$$

where  $Q_q = \frac{2}{3}$  (for up-type),  $-\frac{1}{3}$  (for down-type) is the charge of the scalar quark,  $\tilde{M}_Q^2$ ,  $\tilde{M}_U^2$  and  $\tilde{M}_D^2$  are the self-supersymmetry-breaking mass terms for the left-handed and right-handed scalar quarks, and  $s_W = \sin \theta_W$ ,  $c_W = \cos \theta_W$ . As an assumption at Planck scale, we choose  $\tilde{M}_Q = \tilde{M}_U = \tilde{M}_D = \tilde{M}$ . Since  $CP$  effects are not considered, the value  $a_q$  is real. When  $\tilde{q}_L$  and  $\tilde{q}_R$  are mixed, they give the mass eigenstates  $\tilde{q}_1$  and  $\tilde{q}_2$ . The mass eigenstates  $\tilde{q}_1$  and  $\tilde{q}_2$  are expressed in terms of the current eigenstates  $\tilde{q}_L$ ,  $\tilde{q}_R$  as

$$\begin{aligned}\tilde{q}_1 &= \tilde{q}_L \cos \theta_q - \tilde{q}_R \sin \theta_q, \\ \tilde{q}_2 &= \tilde{q}_L \sin \theta_q + \tilde{q}_R \cos \theta_q,\end{aligned}$$

with

$$\tan 2\theta_q = \frac{2a_q m_q}{m_{\tilde{q}_L}^2 - m_{\tilde{q}_R}^2}. \quad (\text{A3})$$

The explicit expressions for the notations used in Eqs. (2.8a)–(2.8d) are listed as below:

$$V_{tb_1\tilde{\chi}_j^+}^{(1)} = \frac{ig m_t}{\sqrt{2} m_w \sin \beta} V_{j2}^* \cos \theta_{\tilde{b}}, \quad (\text{A4})$$

$$V_{tb_1\tilde{\chi}_j^+}^{(2)} = -ig \left( U_{j1} \cos \theta_{\tilde{b}} + \frac{m_b}{\sqrt{2} m_w \cos \beta} U_{j2} \sin \theta_{\tilde{b}} \right), \quad (\text{A5})$$

$$V_{tb_2\tilde{\chi}_j^+}^{(1)} = \frac{ig m_t}{\sqrt{2} m_w \sin \beta} V_{j2}^* \sin \theta_{\tilde{b}}, \quad (\text{A6})$$

$$V_{tb_2\tilde{\chi}_j^+}^{(2)} = -ig \left( U_{j1} \sin \theta_{\tilde{b}} - \frac{m_b}{\sqrt{2} m_w \cos \beta} U_{j2} \cos \theta_{\tilde{b}} \right), \quad (\text{A7})$$

$$V_{t\tilde{t}_1\tilde{\chi}_j^0}^{(1)} = -ig \sqrt{2} \left( \frac{m_t}{2 m_w \sin \beta} N_{j4}^* \cos \theta_{\tilde{t}} + \frac{2}{3} \tan \theta_w N_{j1}^* \sin \theta_{\tilde{t}} \right), \quad (\text{A8})$$

$$\begin{aligned}V_{t\tilde{t}_1\tilde{\chi}_j^0}^{(2)} &= -ig \sqrt{2} \left( \left( \frac{1}{6} \tan \theta_w N_{j1} + \frac{1}{2} N_{j2} \right) \cos \theta_{\tilde{t}} \right. \\ &\quad \left. - \frac{m_t}{2 m_w \sin \beta} N_{j4} \sin \theta_{\tilde{t}} \right), \quad (\text{A9})\end{aligned}$$

$$V_{t\tilde{t}_2\tilde{\chi}_j^0}^{(1)} = -ig \sqrt{2} \left( \frac{m_t}{2 m_w \sin \beta} N_{j4}^* \sin \theta_{\tilde{t}} - \frac{2}{3} \tan \theta_w N_{j1}^* \cos \theta_{\tilde{t}} \right), \quad (\text{A10})$$

$$\begin{aligned}V_{t\tilde{t}_2\tilde{\chi}_j^0}^{(2)} &= -ig \sqrt{2} \left( \left( \frac{1}{6} \tan \theta_w N_{j1} + \frac{1}{2} N_{j2} \right) \sin \theta_{\tilde{t}} \right. \\ &\quad \left. + \frac{m_t}{2 m_w \sin \beta} N_{j4} \cos \theta_{\tilde{t}} \right), \quad (\text{A11})\end{aligned}$$

The shorted notations defined in Eq. (2.9), are explicitly expressed below:

$$V_{H^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s = \frac{-ig}{\sqrt{2}} [\cos \alpha \operatorname{Re}(V_{k,1} U_{k,2}) + \sin \alpha \operatorname{Re}(V_{k,2} U_{k,1})], \quad (\text{A12})$$

$$V_{h^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s = \frac{ig}{\sqrt{2}} [\sin \alpha \operatorname{Re}(V_{k,1} U_{k,2}) - \cos \alpha \operatorname{Re}(V_{k,2} U_{k,1})], \quad (\text{A13})$$

$$V_{A^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^{ps} = \frac{g}{\sqrt{2}} [\sin \beta \operatorname{Re}(V_{k,1} U_{k,2}) + \cos \beta \operatorname{Re}(V_{k,2} U_{k,1})], \quad (\text{A14})$$

$$V_{G^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^{ps} = \frac{-g}{\sqrt{2}} [\cos \beta \operatorname{Re}(V_{k,1} U_{k,2}) - \sin \beta \operatorname{Re}(V_{k,2} U_{k,1})]. \quad (\text{A15})$$

## APPENDIX B: FORM FACTORS

In this appendix we list all the form factors for the one-loop correction diagrams by using some abbreviations for the following expressions:

$$\bar{B}_0^{1,k} = B_0[-p_1 - p_2, m_{\tilde{b}_k}, m_{\tilde{b}_k}] - \Delta, \quad \bar{B}_0^{2,k} = \bar{B}_0^{1,k}(m_{\tilde{b}_k} \rightarrow m_{\tilde{t}_k}),$$

$$\bar{B}_0^{3,i,j} = B_0[p_3 - p_1, m_{\tilde{\chi}_i^0}, m_{\tilde{\chi}_j^0}] - \Delta, \quad \bar{B}_1^{3,i,j} = B_0[p_3 - p_1, m_{\tilde{\chi}_i^0}, m_{\tilde{\chi}_j^0}] + \frac{\Delta}{2},$$

$$\bar{B}_0^{4,i,j} = B_0[p_3 - p_1, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] - \Delta, \quad \bar{B}_1^{4,i,j} = B_0[p_3 - p_1, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}] + \frac{\Delta}{2},$$

$$C_0^{1,i,j}, C_{ab}^{1,i,j} = C_0, C_{ab}[-p_1, p_1 + p_2, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}, m_{\tilde{b}_j}],$$

$$C_0^{2,i,j}, C_{ab}^{2,i,j} = C_0, C_{ab}[-p_1, p_1 + p_2, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}, m_{\tilde{t}_j}],$$

$$C_0^{3,k}, C_{ab}^{3,k} = C_0, C_{ab}[-p_3, p_1 + p_2, m_{\tilde{\chi}_k^+}, m_{\tilde{\chi}_k^+}, m_{\tilde{\chi}_k^+}],$$

$$C_0^{4,k}, C_{ab}^{4,k} = C_0, C_{ab}[p_3, -p_1 - p_2, m_{\tilde{b}_k}, m_{\tilde{b}_k}, m_{\tilde{b}_k}],$$

$$C_0^{5,k}, C_{ab}^{5,k} = C_0, C_{ab}[p_3, -p_1 - p_2, m_{\tilde{t}_k}, m_{\tilde{t}_k}, m_{\tilde{t}_k}],$$

$$C_0^{6,i,j}, C_{ab}^{6,i,j}(k_1, k_2) = C_0, C_{ab}[-k_1, k_1 + k_2, m_{\tilde{b}_j}, m_{\tilde{\chi}_i^+}, m_{\tilde{\chi}_i^+}],$$

$$C_0^{7,i,j}, C_{ab}^{7,i,j}(k_1, k_2) = C_0, C_{ab}[-k_1, k_1 + k_2, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}, m_{\tilde{b}_j}],$$

$$C_0^{8,i,j}, C_{ab}^{8,i,j}(k_1, k_2) = C_0, C_{ab}[-k_1, k_1 + k_2, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}, m_{\tilde{t}_j}],$$

$$D_0^{1,i,j}, D_{ab}^{1,i,j}, D_{abc}^{1,i,j} = D_0, D_{ab}, D_{abc}[p_1, -p_3, -p_4, m_{\tilde{b}_j}, m_{\tilde{\chi}_i^+}, m_{\tilde{\chi}_i^+}, m_{\tilde{\chi}_i^+}],$$

$$D_0^{2,i,j}, D_{ab}^{2,i,j}, D_{abc}^{2,i,j} = D_0, D_{ab}, D_{abc}[-p_1, p_3, p_4, m_{\tilde{\chi}_i^+}, m_{\tilde{b}_j}, m_{\tilde{b}_j}],$$

$$D_0^{3,i,j}, D_{ab}^{3,i,j}, D_{abc}^{3,i,j} = D_0, D_{ab}, D_{abc}[-p_1, p_3, p_4, m_{\tilde{\chi}_i^0}, m_{\tilde{t}_j}, m_{\tilde{t}_j}, m_{\tilde{t}_j}],$$

$$D_0^{4,i,j}, D_{ab}^{4,i,j}, D_{abc}^{4,i,j} = D_0, D_{ab}, D_{abc}[-p_3, p_1, -p_4, m_{\tilde{b}_j}, m_{\tilde{b}_j}, m_{\tilde{\chi}_i^+}, m_{\tilde{\chi}_i^+}],$$

$$A_t = \frac{i}{\hat{t} - m_t^2}, \quad A_u = \frac{i}{\hat{u} - m_t^2},$$

$$A_h = \frac{i}{\hat{s} - m_h^2}, \quad A_H = \frac{i}{\hat{s} - m_H^2},$$

$$A_A = \frac{i}{\hat{s} - m_A^2}, \quad A_G = \frac{i}{\hat{s} - m_Z^2},$$

$$F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} = -|V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(1)}|^2 - |V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(2)}|^2, \quad F_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} = -V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(1)*} V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(2)} - V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(2)*} V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+}^{(1)},$$

and

$$G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} = -|V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(1)}|^2 - |V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(2)}|^2, \quad G_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} = -V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(1)*} V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(2)} - V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(2)*} V_{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0}^{(1)}.$$

The one-particle-irreducible (1PI) correction to the vertex  $\gamma tt$  stemming from squark, chargino and neutralino can be written in terms of the form factors

$$\begin{aligned} \Delta\Gamma_{\gamma tt}^\mu(k_1, k_2) = & g_1(k_1, k_2)k_1^\mu\gamma_5\mathbf{k}_1 + g_2(k_1, k_2)k_2^\mu\gamma_5\mathbf{k}_1 + g_3(k_1, k_2)k_1^\mu\gamma_5\mathbf{k}_2 + g_4(k_1, k_2)k_2^\mu\gamma_5\mathbf{k}_2 + g_5(k_1, k_2)k_1^\mu\gamma_5 \\ & + g_6(k_1, k_2)k_2^\mu\gamma_5 + g_7(k_1, k_2)\gamma_5\gamma^\mu\mathbf{k}_1\mathbf{k}_2 + g_8(k_1, k_2)\gamma_5\gamma^\mu\mathbf{k}_1 + g_9(k_1, k_2)\gamma_5\gamma^\mu\mathbf{k}_2 + g_{10}(k_1, k_2)\gamma_5\gamma^\mu \\ & + g_{11}(k_1, k_2)k_1^\mu\mathbf{k}_1 + g_{12}(k_1, k_2)k_2^\mu\mathbf{k}_1 + g_{13}(k_1, k_2)k_1^\mu\mathbf{k}_2 + g_{14}(k_1, k_2)k_2^\mu\mathbf{k}_2 + g_{15}(k_1, k_2)k_1^\mu + g_{16}(k_1, k_2)k_2^\mu \\ & + g_{17}(k_1, k_2)\gamma^\mu\mathbf{k}_1\mathbf{k}_2 + g_{18}(k_1, k_2)\gamma^\mu\mathbf{k}_1 + g_{19}(k_1, k_2)\gamma^\mu\mathbf{k}_2 + g_{20}(k_1, k_2)\gamma^\mu, \end{aligned}$$

where  $k_1$  and  $k_2$  are the four-momenta of the lightest top quark pair and along their outgoing directions, respectively. In the equation above, the form factors of the Lorentz invariant structures including  $\gamma_5$  do not contribute to the cross sections of our subprocess. Therefore we shall list only the explicit expressions of the form factors  $g_i$  ( $i=11-20$ ). The form factors  $g_i$  ( $i=11-20$ ) are expressed as follows:

$$\begin{aligned} g_{11}(k_1, k_2) = & \frac{ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} (C_{11}^{6,i,j} - C_{12}^{6,i,j} + C_{21}^{6,i,j} + C_{22}^{6,i,j} - 2C_{23}^{6,i,j})(k_1, k_2) - \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} (C_{11}^{7,i,j} - C_{12}^{7,i,j} \\ & + 2C_{21}^{7,i,j} + 2C_{22}^{7,i,j} - 4C_{23}^{7,i,j})(k_1, k_2) - \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} (C_{11}^{8,i,j} - C_{12}^{8,i,j} + 2C_{21}^{8,i,j} + 2C_{22}^{8,i,j} - 4C_{23}^{8,i,j})(k_1, k_2), \end{aligned}$$

$$\begin{aligned}
g_{12}(k_1, k_2) &= \frac{ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_{22}^{6,i,j} - C_{23}^{6,i,j})(k_1, k_2) + \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_{11}^{7,i,j} - C_{12}^{7,i,j} + 2C_{22}^{7,i,j} + 2C_{23}^{7,i,j})(k_1, k_2) \\
&\quad + \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} (C_{11}^{8,i,j} - C_{12}^{8,i,j} + 2C_{22}^{8,i,j} + 2C_{23}^{8,i,j})(k_1, k_2), \\
g_{13}(k_1, k_2) &= \frac{-ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_0^{6,i,j} + C_{11}^{6,i,j} - C_{22}^{6,i,j} + C_{23}^{6,i,j})(k_1, k_2) + \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_{12}^{7,i,j} - 2C_{22}^{7,i,j} + 2C_{23}^{7,i,j}) \\
&\quad \times (k_1, k_2) + \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} (C_{12}^{8,i,j} - 2C_{22}^{8,i,j} + 2C_{23}^{8,i,j})(k_1, k_2), \\
g_{14}(k_1, k_2) &= \frac{ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_{12}^{6,i,j} + C_{22}^{6,i,j})(k_1, k_2) - \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_{12}^{7,i,j} + 2C_{22}^{7,i,j})(k_1, k_2) \\
&\quad - \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} (C_{12}^{8,i,j} + 2C_{22}^{8,i,j})(k_1, k_2), \\
g_{15}(k_1, k_2) &= \frac{ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (C_0^{6,i,j} + C_{11}^{6,i,j} - C_{12}^{6,i,j})(k_1, k_2) + \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (C_0^{7,i,j} + 2C_{11}^{7,i,j}) \\
&\quad - 2C_{12}^{7,i,j})(k_1, k_2) + \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_2^{\tilde{t}_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (C_0^{8,i,j} + 2C_{11}^{8,i,j} - 2C_{12}^{8,i,j})(k_1, k_2), \\
g_{16}(k_1, k_2) &= \frac{-ie}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} C_{12}^{6,i,j}(k_1, k_2) - \frac{ie}{32\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (C_0^{7,i,j} + 2C_{12}^{7,i,j})(k_1, k_2) \\
&\quad - \frac{ie}{32\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_2^{\tilde{t}_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (C_0^{8,i,j} + 2C_{12}^{8,i,j})(k_1, k_2), \\
g_{17}(k_1, k_2) &= \frac{ie}{32\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (C_0^{6,i,j} + C_{11}^{6,i,j})(k_1, k_2), \\
g_{18}(k_1, k_2) &= g_{19}(k_1, k_2) = \frac{-ie}{32\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} C_0^{6,i,j}(k_1, k_2), \\
g_{20}(k_1, k_2) &= \frac{-ie}{32\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (\epsilon - 2) C_{24}^{6,i,j} + (k_1 \cdot k_1) (C_{11}^{6,i,j} - C_{12}^{6,i,j} + C_{21}^{6,i,j} + C_{22}^{6,i,j} - 2C_{23}^{6,i,j}) + 2(k_1 \cdot k_2) (C_{22}^{6,i,j} - C_{23}^{6,i,j}) \\
&\quad + (k_2 \cdot k_2) (C_{12}^{6,i,j} + C_{22}^{6,i,j}) - m_{\tilde{\chi}_i^+}^2 C_0^{6,i,j}(k_1, k_2) + \frac{ie}{16\pi^2} Q_b \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} C_{24}^{7,i,j}(k_1, k_2) \\
&\quad + \frac{ie}{16\pi^2} Q_t \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} C_{24}^{8,i,j}(k_1, k_2).
\end{aligned}$$

Then the form factors in the renormalized amplitude of the  $t$ -channel vertex diagrams in the process  $\gamma\gamma \rightarrow t\bar{t}$  can be written as

$$f_i^{v,\hat{t}} = 0 \quad (i=2,3,6,7,9,10,12,13,16-22),$$

$$f_1^{v,\hat{t}} = 2ieQ_t(p_1 \cdot p_3)A_t\{m_t[g_{17}(p_1, p_3 - p_1) + g_{17}(p_1 - p_3, p_2)] - g_{18}(p_1 - p_3, p_2) - g_{19}(p_1, p_3 - p_1)\},$$

$$f_4^{v,\hat{t}} = 2ieQ_t(p_1 \cdot p_3)A_t[g_{12}(p_1 - p_3, p_2) - g_{11}(p_1 - p_3, p_2)],$$

$$\begin{aligned} f_5^{v,\hat{t}} = & -2ieQ_t A_t \{ ie[C^+ + C^-] + m_t^2 [g_{11}(p_1, p_3 - p_1) - g_{12}(p_1, p_3 - p_1) - g_{13}(p_1, p_3 - p_1) + g_{14}(p_1, p_3 - p_1) \\ & - g_{17}(p_1, p_3 - p_1) + g_{17}(p_1 - p_3, p_2)] + (p_1 \cdot p_3)[g_{13}(p_1, p_3 - p_1) - g_{14}(p_1, p_3 - p_1) + 2g_{17}(p_1, p_3 - p_1)] \\ & + m_t [g_{15}(p_1, p_3 - p_1) - g_{16}(p_1, p_3 - p_1) + g_{18}(p_1, p_3 - p_1) - g_{18}(p_1 - p_3, p_2) - g_{19}(p_1, p_3 - p_1) \\ & - g_{19}(p_1 - p_3, p_2)] + g_{20}(p_1, p_3 - p_1) + g_{20}(p_1 - p_3, p_2)\}, \end{aligned}$$

$$\begin{aligned} f_8^{v,\hat{t}} = & 2f_{14}^{v,\hat{t}} = 2ieQ_t A_t \{ m_t [g_{11}(p_1 - p_3, p_2) - g_{12}(p_1 - p_3, p_2) - g_{13}(p_1 - p_3, p_2) + g_{14}(p_1 - p_3, p_2) \\ & - 2g_{17}(p_1 - p_3, p_2)] + g_{15}(p_1 - p_3, p_2) - g_{16}(p_1 - p_3, p_2) + 2g_{18}(p_1 - p_3, p_2)\}, \end{aligned}$$

$$\begin{aligned} f_{11}^{v,\hat{t}} = & -ieQ_t A_t \{ ie(C^+ + C^-) + m_t^2 [g_{17}(p_1, p_3 - p_1) + g_{17}(p_1 - p_3, p_2)] - m_t [g_{18}(p_1, p_3 - p_1) \\ & + g_{18}(p_1 - p_3, p_2) + g_{19}(p_1, p_3 - p_1) + g_{19}(p_1 - p_3, p_2)] + g_{20}(p_1, p_3 - p_1) + g_{20}(p_1 - p_3, p_2)\}, \end{aligned}$$

$$f_{15}^{v,\hat{t}} = f_{14}^{v,\hat{t}} [g_i(p_1 - p_3, p_2) \rightarrow g_i(p_1, p_3 - p_1)].$$

The form factors from the renormalized amplitude of  $t$ -channel box diagrams [Fig. 1(c)] are expressed as

$$\begin{aligned} f_1^{b,\hat{t}} = & \frac{-ie^2}{32\pi^2} \sum_{i=1,2} \sum_{j=1,2} (F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{13}^{1,i,j} + D_{25}^{1,i,j} - D_{23}^{1,i,j}) + 2p_1 \cdot p_3 (D_{11}^{1,i,j} + D_{12}^{1,i,j} + D_{23}^{1,i,j} + D_{24}^{1,i,j} - D_{25}^{1,i,j} - D_{26}^{1,i,j} \\ & - 2D_{13}^{1,i,j}) + 2p_2 \cdot p_3 (D_{23}^{1,i,j} - D_{13}^{1,i,j} - D_{26}^{1,i,j}) + m_t^2 (2D_{13}^{1,i,j} + 2D_{25}^{1,i,j} - 2D_{11}^{1,i,j} - 2D_{23}^{1,i,j} - D_0^{1,i,j} - D_{21}^{1,i,j}) + 2D_{27}^{1,i,j} + m_{\tilde{\chi}_i^+}^2 D_0^{1,i,j}] \\ & + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} \{2p_1 \cdot p_2 m_t (D_{13}^{1,i,j} + D_{35}^{1,i,j} + 2D_{25}^{1,i,j} - D_{23}^{1,i,j} - D_{37}^{1,i,j}) + 2p_1 \cdot p_3 m_t (D_{11}^{1,i,j} + D_{12}^{1,i,j} + D_{21}^{1,i,j} + D_{23}^{1,i,j} + D_{34}^{1,i,j} + D_{37}^{1,i,j} \\ & + 2D_{24}^{1,i,j} - 3D_{25}^{1,i,j} - D_{26}^{1,i,j} - D_{310}^{1,i,j} - D_{35}^{1,i,j} - 2D_{13}^{1,i,j}) + 2p_2 \cdot p_3 m_t (D_{23}^{1,i,j} + D_{37}^{1,i,j} - D_{13}^{1,i,j} - D_{25}^{1,i,j} - D_{26}^{1,i,j} - D_{310}^{1,i,j}) \\ & + m_t m_{\tilde{\chi}_i^+}^2 (D_0^{1,i,j} + D_{11}^{1,i,j}) + m_t [4D_{27}^{1,i,j} + (4 - \epsilon) D_{311}^{1,i,j}] + m_t^3 (2D_{13}^{1,i,j} + 2D_{35}^{1,i,j} + 4D_{25}^{1,i,j} - 3D_{11}^{1,i,j} - 3D_{21}^{1,i,j} - 2D_{23}^{1,i,j} - 2D_{37}^{1,i,j} \\ & - D_0^{1,i,j} - D_{31}^{1,i,j})\}) - \frac{ie^2 Q_b^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} (F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t D_{311}^{2,i,j} - F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{27}^{2,i,j}) - \frac{ie^2 Q_t^2}{16\pi^2} \sum_{i=1,4} \sum_{j=1,2} (G_1^{\tilde{t}b_j \tilde{\chi}_i^0} m_t D_{311}^{3,i,j} \\ & - G_2^{\tilde{t}b_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} D_{27}^{3,i,j}) - \frac{ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{27}^{4,i,j} + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t (D_{27}^{4,i,j} + D_{312}^{4,i,j})], \end{aligned}$$

$$\begin{aligned} f_2^{b,\hat{t}} = & \frac{ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t (D_{27}^{1,i,j} + D_{311}^{1,i,j}) + F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{27}^{1,i,j}] - \frac{ie^2 Q_b^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} (F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t D_{311}^{2,i,j} - F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{27}^{2,i,j}) \\ & - \frac{ie^2 Q_t^2}{16\pi^2} \sum_{i=1,4} \sum_{j=1,2} (G_1^{\tilde{t}b_j \tilde{\chi}_i^0} m_t D_{311}^{3,i,j} - G_2^{\tilde{t}b_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} D_{27}^{3,i,j}) - \frac{-ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{27}^{4,i,j} + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t (D_{27}^{4,i,j} + D_{312}^{4,i,j})], \end{aligned}$$

$$\begin{aligned} f_3^{b,\hat{t}} = & \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{25}^{1,i,j} + D_{35}^{1,i,j} + D_{39}^{1,i,j} - D_{26}^{1,i,j} - D_{37}^{1,i,j} - D_{310}^{1,i,j} - D_{37}^{1,i,j}) + 2p_1 \cdot p_3 (D_{24}^{1,i,j} + D_{26}^{1,i,j} + D_{34}^{1,i,j} + D_{37}^{1,i,j} \\ & + D_{38}^{1,i,j} - D_{22}^{1,i,j} - D_{25}^{1,i,j} - D_{35}^{1,i,j} - D_{36}^{1,i,j} - D_{39}^{1,i,j}) + 2p_2 \cdot p_3 (D_{26}^{1,i,j} + D_{37}^{1,i,j} + D_{38}^{1,i,j} - D_{25}^{1,i,j} - D_{310}^{1,i,j} - D_{39}^{1,i,j}) + m_t^2 (D_{12}^{1,i,j} + D_{34}^{1,i,j} \\ & + 2D_{24}^{1,i,j} + 2D_{25}^{1,i,j} + 2D_{35}^{1,i,j} + 2D_{39}^{1,i,j} - D_{11}^{1,i,j} - D_{31}^{1,i,j} - 2D_{21}^{1,i,j} - 2D_{26}^{1,i,j} - 2D_{310}^{1,i,j} - 2D_{37}^{1,i,j}) + m_{\tilde{\chi}_i^+}^2 (D_{11}^{1,i,j} - D_{12}^{1,i,j}) + (4 - \epsilon) \\ & \times (D_{311}^{1,i,j} - D_{312}^{1,i,j})] - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} (D_{311}^{2,i,j} - D_{312}^{2,i,j}) - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j \tilde{\chi}_i^0} (D_{311}^{3,i,j} - D_{312}^{3,i,j}) \end{aligned}$$

$$\begin{aligned}
f_4^{b,\hat{t}} = & \frac{-ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} (D_{312}^{4,i,j} - D_{311}^{4,i,j}), \\
f_5^{b,\hat{t}} = & \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{23}^{1,i,j} + D_{37}^{1,i,j} + D_{39}^{1,i,j} - D_{26}^{1,i,j} - D_{310}^{1,i,j} - D_{33}^{1,i,j}) + 2p_1 \cdot p_3 (2D_{26}^{1,i,j} + 2D_{310}^{1,i,j} + D_{25}^{1,i,j} + D_{33}^{1,i,j} \\
& + D_{38}^{1,i,j} - 2D_{23}^{1,i,j} - 2D_{39}^{1,i,j} - D_{22}^{1,i,j} - D_{36}^{1,i,j} - D_{37}^{1,i,j}) + 2p_2 \cdot p_3 (D_{26}^{1,i,j} + D_{33}^{1,i,j} + D_{38}^{1,i,j} - 2D_{39}^{1,i,j} - D_{23}^{1,i,j}) + m_t^2 (D_{12}^{1,i,j} + D_{34}^{1,i,j} \\
& + 2D_{23}^{1,i,j} + 2D_{24}^{1,i,j} + 2D_{37}^{1,i,j} + 2D_{39}^{1,i,j} - D_{13}^{1,i,j} - D_{35}^{1,i,j} - 2D_{25}^{1,i,j} - 2D_{26}^{1,i,j} - 2D_{310}^{1,i,j} - 2D_{33}^{1,i,j}) + m_{\tilde{\chi}_i^+}^2 (D_{13}^{1,i,j} - D_{12}^{1,i,j}) \\
& + (6-\epsilon) D_{313}^{1,i,j} - 2D_{27}^{1,i,j} - (4-\epsilon) D_{312}^{1,i,j}] + \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} (D_{27}^{2,i,j} + D_{312}^{2,i,j}) + \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j \tilde{\chi}_i^0} (D_{27}^{3,i,j} + D_{312}^{3,i,j}) \\
& + \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} D_{311}^{4,i,j}, \\
f_5^{b,\hat{t}} = & \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} \{2F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_t m_{\tilde{\chi}_i^+} (D_0^{1,i,j} + D_{11}^{1,i,j} - D_{13}^{1,i,j}) + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_2 \cdot p_3 (D_{25}^{1,i,j} - D_{26}^{1,i,j}) + m_t^2 (D_0^{1,i,j} + D_{21}^{1,i,j} + 2D_{11}^{1,i,j} \\
& - 2D_{13}^{1,i,j} - 2D_{25}^{1,i,j}) + m_{\tilde{\chi}_i^+}^2 D_0^{1,i,j} + 2(D_{313}^{1,i,j} - D_{311}^{1,i,j})]\} - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} (D_{27}^{2,i,j} + D_{311}^{2,i,j} - D_{313}^{2,i,j}) \\
& - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j \tilde{\chi}_i^0} (D_{27}^{3,i,j} + D_{311}^{3,i,j} - D_{313}^{3,i,j}) - \frac{ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} \{2F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_t m_{\tilde{\chi}_i^+} (D_{13}^{4,i,j} - D_{12}^{4,i,j}) \\
& + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (2D_{39}^{4,i,j} - D_{33}^{4,i,j} - D_{38}^{4,i,j}) + 2p_1 \cdot p_3 (2D_{26}^{4,i,j} + 2D_{310}^{4,i,j} + D_{33}^{4,i,j} + D_{38}^{4,i,j} - 2D_{39}^{4,i,j} - D_{22}^{4,i,j} - D_{23}^{4,i,j} - D_{36}^{4,i,j} \\
& - D_{37}^{4,i,j}) + 2p_2 \cdot p_3 (D_{310}^{4,i,j} + D_{33}^{4,i,j} - D_{37}^{4,i,j} - D_{39}^{4,i,j}) + m_t^2 (D_{13}^{4,i,j} + D_{32}^{4,i,j} + 4D_{39}^{4,i,j} - 3D_{38}^{4,i,j} - D_{12}^{4,i,j} - 2D_{33}^{4,i,j}) + m_{\tilde{\chi}_i^+}^2 (D_{13}^{4,i,j} \\
& - D_{12}^{4,i,j}) + (4-\epsilon) (D_{313}^{4,i,j} - D_{312}^{4,i,j})]\}, \\
f_6^{b,\hat{t}} = & \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} \{-2F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_t m_{\tilde{\chi}_i^+} D_{13}^{1,i,j} + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{33}^{1,i,j} - D_{37}^{1,i,j}) + 2p_1 \cdot p_3 (D_{23}^{1,i,j} + D_{37}^{1,i,j} + D_{39}^{1,i,j} - D_{25}^{1,i,j} - D_{310}^{1,i,j} \\
& - D_{33}^{1,i,j}) + 2p_2 \cdot p_3 (D_{39}^{1,i,j} - D_{33}^{1,i,j}) + m_t^2 (D_{35}^{1,i,j} + 2D_{33}^{1,i,j} - D_{13}^{1,i,j} - 2D_{37}^{1,i,j}) - m_{\tilde{\chi}_i^+}^2 D_{13}^{1,i,j} - (4-\epsilon) D_{313}^{1,i,j}]\} \\
& + \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j \tilde{\chi}_i^+} D_{313}^{2,i,j} + \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j \tilde{\chi}_i^0} D_{313}^{3,i,j} - \frac{ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} \{2F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_t m_{\tilde{\chi}_i^+} D_{13}^{4,i,j} \\
& + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{39}^{4,i,j} - D_{33}^{4,i,j}) + 2p_1 \cdot p_3 (D_{26}^{4,i,j} + D_{310}^{4,i,j} + D_{33}^{4,i,j} - D_{23}^{4,i,j} - D_{37}^{4,i,j} - D_{39}^{4,i,j}) + 2p_2 \cdot p_3 (D_{33}^{4,i,j} - D_{37}^{4,i,j}) \\
& + m_t^2 (D_{13}^{4,i,j} + 2D_{39}^{4,i,j} - D_{38}^{4,i,j} - 2D_{33}^{4,i,j}) + m_{\tilde{\chi}_i^+}^2 D_{13}^{4,i,j} + (4-\epsilon) D_{313}^{4,i,j}\}], \\
f_7^{b,\hat{t}} = & \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{11}^{1,i,j} + D_{21}^{1,i,j} + D_{26}^{1,i,j} - D_{12}^{1,i,j} - D_{24}^{1,i,j} - D_{25}^{1,i,j}) + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t (2D_{21}^{1,i,j} + D_{11}^{1,i,j} + D_{26}^{1,i,j} + D_{310}^{1,i,j} \\
& + D_{31}^{1,i,j} - 2D_{24}^{1,i,j} - D_{12}^{1,i,j} - D_{25}^{1,i,j} - D_{34}^{1,i,j} - D_{35}^{1,i,j})] - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{11}^{2,i,j} + D_{21}^{2,i,j} + D_{26}^{2,i,j} - D_{12}^{2,i,j} - D_{24}^{2,i,j} \\
& - D_{25}^{2,i,j}) + F_1^{\tilde{t}b_j \tilde{\chi}_i^+} m_t (D_{24}^{2,i,j} + D_{34}^{2,i,j} + D_{35}^{2,i,j} - D_{21}^{2,i,j} - D_{310}^{2,i,j} - D_{31}^{2,i,j})] - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} [G_2^{\tilde{t}b_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (D_{11}^{3,i,j} + D_{21}^{3,i,j} + D_{26}^{3,i,j} \\
& + D_{31}^{3,i,j})]
\end{aligned}$$

$$\begin{aligned}
& -D_{12}^{3,i,j} - D_{24}^{3,i,j} - D_{25}^{3,i,j}) + G_1^{\tilde{t}_j \tilde{\chi}_i^0} m_t (D_{24}^{3,i,j} + D_{34}^{3,i,j} + D_{35}^{3,i,j} - D_{21}^{3,i,j} - D_{310}^{3,i,j} - D_{31}^{3,i,j})] - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{24}^{4,i,j}) \\
& + D_{26}^{4,i,j} - D_{22}^{4,i,j} - D_{25}^{4,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{24}^{4,i,j} + D_{26}^{4,i,j} + D_{36}^{4,i,j} + D_{38}^{4,i,j} - D_{22}^{4,i,j} - D_{25}^{4,i,j} - D_{310}^{4,i,j} - D_{32}^{4,i,j})], \\
f_8^{b,\hat{t}} &= \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (-D_{12}^{1,i,j} + D_{26}^{1,i,j} - D_{24}^{1,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{26}^{1,i,j} + D_{310}^{1,i,j} - 2D_{24}^{1,i,j} - D_{12}^{1,i,j} - D_{34}^{1,i,j})] \\
& - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{13}^{2,i,j} + D_{26}^{2,i,j} - D_0^{2,i,j} - D_{11}^{2,i,j} - D_{12}^{2,i,j} - D_{24}^{2,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{11}^{2,i,j} + D_{21}^{2,i,j} + D_{24}^{2,i,j} + D_{34}^{2,i,j} \\
& - D_{25}^{2,i,j} - D_{310}^{2,i,j})] - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} [G_2^{\tilde{t}_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (D_{13}^{3,i,j} + D_{26}^{3,i,j} - D_0^{3,i,j} - D_{11}^{3,i,j} - D_{12}^{3,i,j} - D_{24}^{3,i,j}) + G_1^{\tilde{t}_j \tilde{\chi}_i^0} m_t (D_{11}^{3,i,j} + D_{21}^{3,i,j} \\
& + D_{24}^{3,i,j} + D_{34}^{3,i,j} - D_{25}^{3,i,j} - D_{310}^{3,i,j})] - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{24}^{4,i,j} - D_{25}^{4,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{24}^{4,i,j} + D_{36}^{4,i,j} - D_{25}^{4,i,j} - D_{310}^{4,i,j})], \\
f_9^{b,\hat{t}} &= \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{26}^{1,i,j} - D_{25}^{1,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{26}^{1,i,j} + D_{310}^{1,i,j} - D_{25}^{1,i,j} - D_{35}^{1,i,j})] \\
& - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{26}^{2,i,j} - D_{25}^{2,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{35}^{2,i,j} - D_{310}^{2,i,j})] - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} [G_2^{\tilde{t}_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (D_{26}^{3,i,j} - D_{25}^{3,i,j}) \\
& + G_1^{\tilde{t}_j \tilde{\chi}_i^0} m_t (D_{35}^{3,i,j} - D_{310}^{3,i,j})] - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{26}^{4,i,j} - D_{25}^{4,i,j}) + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{26}^{4,i,j} + D_{38}^{4,i,j} - D_{25}^{4,i,j} - D_{310}^{4,i,j})], \\
f_{10}^{b,\hat{t}} &= \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{26}^{1,i,j} + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{26}^{1,i,j} + D_{310}^{1,i,j})] - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} (D_{13}^{2,i,j} + D_{26}^{2,i,j}) \\
& - F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{25}^{2,i,j} + D_{310}^{2,i,j})] - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} [G_2^{\tilde{t}_j \tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} (D_{13}^{3,i,j} + D_{26}^{3,i,j}) - G_1^{\tilde{t}_j \tilde{\chi}_i^0} m_t (D_{25}^{3,i,j} + D_{310}^{3,i,j})] \\
& + \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} D_{25}^{4,i,j} + F_1^{\tilde{t}_j \tilde{\chi}_i^+} m_t (D_{25}^{4,i,j} + D_{310}^{4,i,j})], \\
f_{11}^{b,\hat{t}} &= \frac{-ie^2}{32\pi^2} \sum_{i=1,2} \sum_{j=1,2} \{2F_2^{\tilde{t}_j \tilde{\chi}_i^+} m_t m_{\tilde{\chi}_i^+} D_0^{1,i,j} + F_1^{\tilde{t}_j \tilde{\chi}_i^+} [2p_1 \cdot p_2 (D_{25}^{1,i,j} + D_{37}^{1,i,j} + D_{39}^{1,i,j} - D_{26}^{1,i,j} - D_{310}^{1,i,j} - D_{33}^{1,i,j}) + 2p_1 \cdot p_3 (D_{33}^{1,i,j} \\
& + D_{38}^{1,i,j} + 2D_{26}^{1,i,j} + 2D_{310}^{1,i,j} - D_{22}^{1,i,j} - D_{23}^{1,i,j} - D_{36}^{1,i,j} - D_{37}^{1,i,j} - 2D_{39}^{1,i,j}) + 2p_2 \cdot p_3 (D_{33}^{1,i,j} + D_{38}^{1,i,j} - 2D_{39}^{1,i,j}) + m_t^2 (2D_{24}^{1,i,j} \\
& + 2D_{37}^{1,i,j} + 2D_{39}^{1,i,j} + D_0^{1,i,j} + D_{12}^{1,i,j} + D_{34}^{1,i,j} - 2D_{26}^{1,i,j} - 2D_{310}^{1,i,j} - 2D_{33}^{1,i,j} - D_{13}^{1,i,j} - D_{21}^{1,i,j} - D_{35}^{1,i,j}) + m_{\tilde{\chi}_i^+}^2 (D_0^{1,i,j} + D_{13}^{1,i,j} - D_{12}^{1,i,j}) \\
& + (4-\epsilon) (D_{313}^{1,i,j} - D_{312}^{1,i,j})]\} + \frac{-ie^2 Q_b^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (D_{313}^{2,i,j} - D_{312}^{2,i,j}) + \frac{-ie^2 Q_t^2}{16\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} (D_{313}^{3,i,j} - D_{312}^{3,i,j}) \\
& + \frac{-ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (D_{313}^{4,i,j} - D_{311}^{4,i,j}), \\
f_{12}^{b,\hat{t}} &= \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (D_{27}^{1,i,j} + D_{312}^{1,i,j} - D_{313}^{1,i,j}) + \frac{-ie^2 Q_b^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (D_{313}^{2,i,j} - D_{312}^{2,i,j}) \\
& + \frac{-ie^2 Q_t^2}{16\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}_j \tilde{\chi}_i^0} (D_{313}^{3,i,j} - D_{312}^{3,i,j}) + \frac{-ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}_j \tilde{\chi}_i^+} (D_{313}^{4,i,j} - D_{27}^{4,i,j} - D_{311}^{4,i,j}),
\end{aligned}$$

$$f_{13}^{b,\hat{t}} = \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{11}^{1,i,j} - D_{12}^{1,i,j}) + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{11}^{1,i,j} + D_{21}^{1,i,j} - D_{12}^{1,i,j} - D_{24}^{1,i,j})],$$

$$f_{14}^{b,\hat{t}} = \frac{ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{12}^{1,i,j} + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{12}^{1,i,j} + D_{24}^{1,i,j})],$$

$$f_{15}^{b,\hat{t}} = \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{13}^{1,i,j} - D_{11}^{1,i,j}) + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{13}^{1,i,j} + D_{25}^{1,i,j} - D_{11}^{1,i,j} - D_{21}^{1,i,j})]$$

$$-\frac{ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{12}^{4,i,j} - D_{13}^{4,i,j}) + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{12}^{4,i,j} + D_{22}^{4,i,j} - D_{13}^{4,i,j} - D_{26}^{4,i,j})],$$

$$f_{16}^{b,\hat{t}} = \frac{-ie^2}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{13}^{1,i,j} + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{13}^{1,i,j} + D_{25}^{1,i,j})) + \frac{ie^2 Q_b}{16\pi^2} \sum_{i=1,2} \sum_{j=1,2} [F_2^{\tilde{t}b_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+}(D_{13}^{4,i,j} + F_1^{\tilde{t}b_j\tilde{\chi}_i^+} m_t(D_{13}^{4,i,j} + D_{26}^{4,i,j}))]$$

$$f_{17}^{b,\hat{t}} = \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{22}^{1,i,j} + D_{25}^{1,i,j} + D_{35}^{1,i,j} + D_{36}^{1,i,j} + D_{39}^{1,i,j} - D_{24}^{1,i,j} - D_{26}^{1,i,j} - D_{34}^{1,i,j} - D_{37}^{1,i,j} - D_{38}^{1,i,j})$$

$$-\frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{24}^{2,i,j} + D_{26}^{2,i,j} + D_{34}^{2,i,j} + D_{37}^{2,i,j} + D_{38}^{2,i,j} - D_{22}^{2,i,j} - D_{25}^{2,i,j} - D_{35}^{2,i,j} - D_{36}^{2,i,j} - D_{39}^{2,i,j})$$

$$-\frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j\tilde{\chi}_i^0} (D_{24}^{3,i,j} + D_{26}^{3,i,j} + D_{34}^{3,i,j} + D_{37}^{3,i,j} + D_{38}^{3,i,j} - D_{22}^{3,i,j} - D_{25}^{3,i,j} - D_{35}^{3,i,j} - D_{36}^{3,i,j} - D_{39}^{3,i,j})$$

$$-\frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{22}^{4,i,j} + D_{25}^{4,i,j} + D_{35}^{4,i,j} + D_{36}^{4,i,j} + D_{39}^{4,i,j} - D_{24}^{4,i,j} - D_{26}^{4,i,j} - D_{34}^{4,i,j} - D_{37}^{4,i,j} - D_{38}^{4,i,j}),$$

$$f_{18}^{b,\hat{t}} = \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{22}^{1,i,j} + D_{23}^{1,i,j} + D_{36}^{1,i,j} + D_{39}^{1,i,j} - D_{25}^{1,i,j} - D_{26}^{1,i,j} - D_{310}^{1,i,j} - D_{38}^{1,i,j}) - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (2D_{26}^{2,i,j} +$$

$$+ D_{13}^{2,i,j} + D_{25}^{2,i,j} + D_{310}^{2,i,j} + D_{38}^{2,i,j} - D_{12}^{2,i,j} - D_{22}^{2,i,j} - D_{23}^{2,i,j} - D_{24}^{2,i,j} - D_{36}^{2,i,j} - D_{39}^{2,i,j}) - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j\tilde{\chi}_i^0} (2D_{26}^{3,i,j} + D_{13}^{3,i,j} +$$

$$+ D_{25}^{3,i,j} + D_{310}^{3,i,j} + D_{38}^{3,i,j} - D_{12}^{3,i,j} - D_{22}^{3,i,j} - D_{23}^{3,i,j} - D_{24}^{3,i,j} - D_{36}^{3,i,j} - D_{39}^{3,i,j}) - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{25}^{4,i,j} + D_{26}^{4,i,j} + D_{310}^{4,i,j} - D_{24}^{4,i,j} - D_{23}^{4,i,j} - D_{34}^{4,i,j} - D_{37}^{4,i,j} - D_{38}^{4,i,j}),$$

$$f_{19}^{b,\hat{t}} = \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{25}^{1,i,j} + D_{310}^{1,i,j} + D_{39}^{1,i,j} - D_{26}^{1,i,j} - D_{37}^{1,i,j} - D_{38}^{1,i,j}) - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{37}^{2,i,j} + D_{38}^{2,i,j} - D_{39}^{2,i,j} - D_{310}^{2,i,j}) - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}b_j\tilde{\chi}_i^0} (D_{37}^{3,i,j} + D_{38}^{3,i,j} - D_{39}^{3,i,j} - D_{310}^{3,i,j}) - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}b_j\tilde{\chi}_i^+} (D_{25}^{4,i,j} + D_{35}^{4,i,j} + D_{39}^{4,i,j} - D_{26}^{4,i,j} - D_{310}^{4,i,j} - D_{37}^{4,i,j}),$$

$$\begin{aligned} f_{20}^{b,\hat{t}} &= \frac{-ie^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} (D_{23}^{1,i,j} + D_{39}^{1,i,j} - D_{26}^{1,i,j} - D_{38}^{1,i,j}) - \frac{ie^2 Q_b^2}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} (D_{26}^{2,i,j} + D_{38}^{2,i,j} - D_{23}^{2,i,j} - D_{39}^{2,i,j}) \\ &\quad - \frac{ie^2 Q_t^2}{8\pi^2} \sum_{i=1,4} \sum_{j=1,2} G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} (D_{26}^{3,i,j} + D_{38}^{3,i,j} - D_{23}^{3,i,j} - D_{39}^{3,i,j}) - \frac{ie^2 Q_b}{8\pi^2} \sum_{i=1,2} \sum_{j=1,2} F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} (D_{25}^{4,i,j} + D_{35}^{4,i,j} - D_{23}^{4,i,j} - D_{37}^{4,i,j}), \\ f_{21,22}^{b,\hat{t}} &= 0. \end{aligned}$$

The form factors in the renormalized amplitude of the quartic interaction diagrams in Fig. 1(d) have the form as

$$\begin{aligned} f_1^q = f_2^q &= \frac{-ie^2}{32\pi^2} \left[ Q_b^2 \sum_{i=1,2} \sum_{j=1,2} (F_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} m_{\tilde{\chi}_i^+} C_0^{1,i,j} - F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} m_t C_{11}^{1,i,j}) + Q_t^2 \sum_{i=1,4} \sum_{j=1,2} (G_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} m_{\tilde{\chi}_i^0} C_0^{2,i,j} - G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} m_t C_{11}^{2,i,j}) \right. \\ &\quad \left. + 2iQ_b^2 \sum_{k=1,2} \bar{B}_0^{1,k} (A_h V_{h^0tt} V_{h^0\tilde{b}_k\tilde{b}_k} + A_H V_{H^0tt} V_{H^0\tilde{b}_k\tilde{b}_k}) + 2iQ_t^2 \sum_{k=1,2} \bar{B}_0^{2,k} (A_h V_{h^0tt} V_{h^0\tilde{k}_k\tilde{k}_k} + A_H V_{H^0tt} V_{H^0\tilde{k}_k\tilde{k}_k}) \right], \\ f_i^q &= 0, \quad (i=3-22). \end{aligned}$$

The form factors in the renormalized amplitude from the  $t$ -channel triangle diagrams depicted in Fig. 1(e) are listed below:

$$\begin{aligned} f_1^{tr,\hat{t}} = f_2^{tr,\hat{t}} &= \frac{e^2}{8\pi^2} \sum_{k=1,2} m_{\tilde{\chi}_k^+} [2p_1 \cdot p_2 C_{22}^{3,k} + (p_1 \cdot p_3 + p_2 \cdot p_3)(C_0^{3,k} - 2C_{23}^{3,k}) + \epsilon \bar{C}_{24}^{3,k} + 2m_t^2 C_{22}^{3,k} - m_{\tilde{\chi}_k^+}^2 C_0^{3,k}] (A_h V_{h^0tt} V_{h^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s + A_H V_{H^0tt} V_{H^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s) \\ &\quad + A_H V_{H^0tt} V_{H^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s - \left[ \frac{e^2 Q_b^2}{8\pi^2} \sum_{k=1,2} \bar{C}_{24}^{4,k} (A_h V_{h^0tt} V_{h^0\tilde{b}_k\tilde{b}_k} + A_H V_{H^0tt} V_{H^0\tilde{b}_k\tilde{b}_k}) + (Q_b, \tilde{b}, C^{4,k} \rightarrow Q_t, \tilde{t}, C^{5,k}) \right], \\ f_7^{tr,\hat{t}} = f_8^{tr,\hat{t}} = f_9^{tr,\hat{t}} = f_{10}^{tr,\hat{t}} &= -\frac{e^2}{4\pi^2} \sum_{k=1,2} m_{\tilde{\chi}_k^+} (C_0^{3,k} + 4C_{22}^{3,k} - 4C_{23}^{3,k}) (A_h V_{h^0tt} V_{h^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s + A_H V_{H^0tt} V_{H^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^s) \\ &\quad - \left[ \frac{e^2 Q_b^2}{4\pi^2} \sum_{k=1,2} (C_{23}^{4,k} - C_{22}^{4,k}) (A_h V_{h^0tt} V_{h^0\tilde{b}_k\tilde{b}_k} + A_H V_{H^0tt} V_{H^0\tilde{b}_k\tilde{b}_k}) + (Q_b, \tilde{b}, C^{4,k} \rightarrow Q_t, \tilde{t}, C^{5,k}) \right], \\ f_{21}^{tr,\hat{t}} = f_{22}^{tr,\hat{t}} &= -\frac{ie^2}{4\pi^2} \sum_{k=1,2} m_{\tilde{\chi}_k^+} C_0^{3,k} (A_A V_{A^0tt} V_{A^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^{ps} + A_G V_{G^0tt} V_{G^0\tilde{\chi}_k^+\tilde{\chi}_k^+}^{ps}), \\ f_i^{tr,\hat{t}} &= 0, \quad (i=3-6,11-20), \end{aligned}$$

where  $\bar{C}_{24}^{3,k} = C_{24}^{3,k} - \Delta/4$  and  $\bar{C}_{24}^{4,k} = C_{24}^{4,k} - \Delta/4$ . The form factors in renormalized amplitude of the self-energy corrections  $\mathcal{M}^{s,\hat{t}}$  from Fig. 1(f) in  $t$ -channel are expressed as

$$\begin{aligned} f_i^{s,\hat{t}} &= 0, \quad (i=2-4,6-10,12-22), \\ f_1^{s,\hat{t}} &= \frac{-ie^2 Q_t^2 A_t^2}{16\pi^2} p_1 \cdot p_3 \left\{ 16\pi^2 (C_S^- + C_S^+ - m_t C_L - m_t C_R) + \sum_{i=1,4} \sum_{j=1,2} [m_{\tilde{\chi}_i^0} G_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} \bar{B}_0^{3,i,j} - m_t G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} \bar{B}_1^{3,i,j}] \right. \\ &\quad \left. + \sum_{i=1,2} \sum_{j=1,2} [m_{\tilde{\chi}_i^+} F_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} \bar{B}_0^{4,i,j} - m_t F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} \bar{B}_1^{4,i,j}] \right\}, \\ f_{11}^{s,\hat{t}} &= \frac{ie^2 Q_t^2 A_t^2}{2} \left\{ 16\pi^2 [m_t (C_S^- + C_S^+) + (p_1 \cdot p_3 - m_t^2) (C_L + C_R)] + \sum_{i=1,4} \sum_{j=1,2} [m_t m_{\tilde{\chi}_i^0} G_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} \bar{B}_0^{3,i,j} \right. \\ &\quad \left. + (p_1 \cdot p_3 - m_t^2) G_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^0} \bar{B}_1^{3,i,j}] + \sum_{i=1,2} \sum_{j=1,2} [m_t m_{\tilde{\chi}_i^+} F_2^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} \bar{B}_0^{4,i,j} + (p_1 \cdot p_3 - m_t^2) F_1^{\tilde{t}\tilde{b}_j\tilde{\chi}_i^+} \bar{B}_1^{4,i,j}] \right\}. \end{aligned}$$

In this work we adopted the definitions of two-, three-, four-point one-loop Passarino-Veltman integral functions as shown in Ref. [22] and all the vector and tensor integrals can be deduced in the forms of scalar integrals [23].

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