QCD and SUSY QCD corrections to the three-body decay of the charged Higgs boson

Xiao-Jun Bi, Yuan-Ben Dai, and Xiao-Yuan Qi

Institute of Theoretical Physics, Academia Sinica, P.O. Box 2735, Beijing 100080, People's Republic of China

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The $O(\alpha_s)$ QCD corrections to the three-body decay width of the charged Higgs boson $\Gamma(H^+ \rightarrow W^+ b\bar{b})$ are discussed in the MSSM. Our calculations indicate that the standard QCD corrections to the three-body decay mode raise the width by about 12% and the supersymmetric QCD corrections (due to $\tilde{g}, \tilde{t}, \tilde{b}$ exchanges) can be comparable to or even larger than the standard QCD corrections in some regions of the supersymmetric parameter space. This is mainly due to the effect of large left-right mixing of the top squark (\tilde{t}). It could significantly affect the phenomenology of the H^+ search.

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I. INTRODUCTION

Despite the great success of the standard model (SM) in elementary particle physics, one important aspect, the Higgs mechanism, of the model has not yet been experimentally verified, and there is plenty of room for extensions. The SM possesses the minimal Higgs structure of one doublet and only one neutral physical Higgs boson is left after spontaneous symmetry breaking (SSB). One of the most interesting versions of the extended SM is the minimal supersymmetric standard model (MSSM) which demands two Higgs doublets and predicts a charged Higgs pair (H^{\pm}) [1]. The search for the charged Higgs boson will give bounds on the parameter space of new physics models. Several groups have analyzed their experimental data and give lower bounds on the charged Higgs boson mass [2,3].

The top quark decay provides a promising laboratory to look for the Higgs boson because the top quark-Higgs Yukawa coupling is large. The H^{\pm} search strategy in topquark decays has been based on the distinctive features of the channels $t \rightarrow bH^+ \rightarrow b(\tau^+ \nu, c\bar{s})$, compared with the standard model decay $t \rightarrow bW^+ \rightarrow b(l\nu, \tau\nu, q'\bar{q})$, which assumes that the dominant decay channels of the charged Higgs boson below the $t\bar{b}$ the threshold are $H^+ \rightarrow \tau^+ \nu$ and $H^+ \rightarrow c\bar{s}$ [4]. Recently, another important three-body decay channel of the Higgs boson $H^+ \rightarrow \bar{b}bW^+$ has been proposed by Ma *et al.* [5]. They found that the above three-body channel is dominant for $H^+ \ge 140$ GeV and $\tan \beta \le 1$ while the $\tau^+ \nu$ mode dominates at large $\tan \beta$. The $c\bar{s}$ mode is relatively small at all $\tan \beta$ for $H^+ \ge 140$ GeV. This can significantly affect the signature for top quark products.

Accurate predictions of charged Higgs boson width including $\mathcal{O}(\alpha_s)$ corrections to the above processes are important to the phenomenology of the H^+ search. The one-loop effects (strong and electroweak) on the decay $t \rightarrow H^+ b$ and $t \rightarrow bW^+$ have been discussed in detail in Refs. [6] and [7], respectively. The leading QCD corrections to the process $H^+ \rightarrow c\bar{s}$ is taken into account by substituting the quark mass parameters by the running masses at the H^+ mass scale [8] which changes the charm quark mass from 1.5 to 1 GeV and considerably reduces the width of the $H^+ \rightarrow c\bar{s}$ process. Correspondingly, the leading QCD corrections to the above three-body decay channel should also be taken into account, which, so far as we know, is absent in the literatures. In this paper, we present the calculations of the QCD and supersymmetric (SUSY) QCD corrections to the width of the three-body decay $H^+ \rightarrow \overline{b}bW^+$ within the MSSM. We also calculate the one-loop corrections from charged Higgs particle which may be important for small tan β .

The paper is organized as follows. In Sec. II, we present most of the formulas in our calculations and show some important analytical results. We also discuss the arrangement of the ultraviolet and infrared divergences. Some relevant formulas are given in Appendixes A and B. In Sec. III, numerical results and discussions are presented.

II. ANALYSIS AND FORMULAS

We shall perform the calculations mainly in the MSSM. The related pieces of Lagrangian are given in Appendix A. For simplicity, we neglect terms directly proportional to m_b but of course keep those terms which are singular in the vanishing mass limit $[\sim \ln(m_b)]$. In the final results after we include real gluon emission, such singularities are cancelled out. As a result of taking $m_b=0$ in the MSSM, only the left-handed bottom squark (\tilde{b}_L) enters our calculations while the left-right handed mixing of the top squark $(\tilde{t}_L, \tilde{t}_R)$ is included in the calculations.

First we define several quantities and symbols

$$G = \frac{g^2 m_t}{2m_W} \cot \beta |V_{tb}|^2, \qquad (1)$$

$$A_1 = \overline{u}(p_2) \not\in P_L v(p_1), \tag{2}$$

$$A_2 = \overline{u}(p_2) \not p_3 P_L v(p_1) p_2 \cdot \boldsymbol{\epsilon}, \tag{3}$$

$$A_3 = \overline{u}(p_2) \not p_3 P_L v(p_1) p_1 \cdot \boldsymbol{\epsilon}, \tag{4}$$

where $\cot \beta = v_1/v_2$ is the ratio of the vaccum expectation values of the two Higgs boson doublets, V_{tb} is the Cabibbo-Kobayashi-Maskawa (CKM) matrix element, ϵ is the polarization vector of W^+ boson, and p_1, p_2, p_3 are the fourvector momenta of \overline{b} , b, and W^+ , respectively.



FIG. 1. Tree-level diagram for the three-body decay of the charged Higgs boson $H^+ \rightarrow W^+ b \overline{b}$.

The tree-level amplitude due to Fig. 1 is

$$M_0 = G \frac{m_t}{p_t^2 - m_t^2} A_1, \qquad (5)$$

with $p_t \equiv p_2 + p_3$ and the corresponding width [5] is

$$\frac{d\Gamma_0}{ds_{\bar{b}}ds_b} = \frac{1}{256\pi^3 m_{H^+}^3} \left(\frac{3g^4 m_t^4 \cot^2 \beta}{4m_W^4 (m_t^2 - s_{\bar{b}})^2} \right) [m_W^2 (s_W - 2m_b^2) + (s_{\bar{b}} - m_b^2 - m_W^2) (s_b - m_b^2 - m_W^2)], \quad (6)$$

where $s_{\bar{b}}$, s_b , and s_W are the four-momentum squared transferred to the corresponding particles by H^+ [9].

The one-loop QCD and SUSY-QCD corrections to the process arise from the diagrams of Figs. 2 and 3, which involve virtual gluon and gluino exchanges. The self-energy corrections of external legs make no contribution to the width and we do not depict these diagrams. The amplitudes for those diagrams in Figs. 2 and 3 are

$$M_{a}^{(g,\tilde{g})} = G \frac{\alpha_{s}}{3\pi} \frac{1}{(p_{t}^{2} - m_{t}^{2})^{2}} F_{1}^{(g,\tilde{g})} A_{1},$$
(7)

$$M_{b}^{(g,\tilde{g})} = G \frac{\alpha_{s}}{3\pi} \frac{1}{(p_{t}^{2} - m_{t}^{2})} [F_{2}^{(g,\tilde{g})}A_{1} + F_{3}^{(g,\tilde{g})}A_{2}], \qquad (8)$$

$$M_{c}^{(g,\tilde{g})} = G \frac{\alpha_{s}}{3\pi} \frac{1}{(p_{t}^{2} - m_{t}^{2})} [F_{4}^{(g,\tilde{g})} A_{1}], \qquad (9)$$

$$M_{d}^{(g,\tilde{g})} = G \frac{\alpha_{s}}{3\pi} [F_{5}^{(g,\tilde{g})} A_{1} + F_{6}^{(g,\tilde{g})} A_{2} + F_{7}^{(g,\tilde{g})} A_{3}],$$



FIG. 2. Diagrams relevant for the calculation of the $\mathcal{O}(\alpha_s)$ QCD corrections to the width of the three-body decay $H^+ \rightarrow W^+ b\bar{b}$.

where the indices g and \tilde{g} refer to the gluon and gluino corrections. $F_1^{(g,\tilde{g})} - F_7^{(g,\tilde{g})}$ are functions of various kinematic invariants, which include the two-point, three-point, and four-point functions as defined in Ref. [10]. We give the explicit forms of $F_1^{(g,\tilde{g})} - F_7^{(g,\tilde{g})}$ in Appendix B. It can be seen from above that the amplitudes for the loop diagrams in Fig. 3 have the same structures as their counterparts in Fig. 2. Now we turn to the mass and wave-function renormalization due to Figs. 4(a) and 4(b). The self-energy parts can be written in the form

$$-i\Sigma^{(g)} = \frac{-i\alpha_s}{3\pi} \{ \not p [1 - 2B_0(p^2, m_q^2, \lambda^2) - 2B_1(p^2, m_q^2, \lambda^2)] + [4B_0(p^2, m_q^2, \lambda^2) - 2]m_q \},$$
(11)

$$\Sigma_{L}^{(g)}(p^{2})P_{L} + \Sigma_{R}^{(g)}(p^{2})P_{R}$$

$$= \frac{\alpha_{s}}{3\pi} \{ 2[\cos^{2}\theta P_{L} + \sin^{2}\theta P_{R}]B_{1}(p^{2}, m_{\tilde{g}}^{2}, m_{\tilde{q}_{1}}^{2}) + 2[\sin^{2}\theta P_{L} + \cos^{2}\theta P_{R}]B_{1}(p^{2}, m_{\tilde{g}}^{2}, m_{\tilde{q}_{2}}^{2}) \}, \qquad (13)$$

$$\Sigma_{s}^{(\tilde{g})}(p^{2}) = \frac{\alpha_{s}}{3\pi} \{ m_{\tilde{g}} \sin 2\theta [B_{0}(p^{2}, m_{\tilde{g}}^{2}, m_{\tilde{q}_{1}}^{2}) - B_{0}(p^{2}, m_{\tilde{g}^{2}}, m_{\tilde{q}_{2}}^{2})] \},$$
(14)

where we have introduced a gluon mass λ to regularize the infrared divergences and θ is the mixing angle of left-right handed top-squark defined in Appendix A.

(10)

We shall use the on-shell renormalization scheme throughout the paper [11]. From Eqs. (11) and (12), we can easily derive the mass counterterms δm ,

$$\delta m_q^{(g)} = \frac{\alpha_s}{3\pi} m_q [2B_0(m_q^2, m_q^2, 0) - 2B_1(m_q^2, m_q^2, 0) - 1],$$
(15)

$$\begin{split} & \delta m_q^{(\tilde{g})} = \frac{\alpha_s}{3\pi} m_q \bigg\{ B_1(m_q^2, m_{\tilde{g}}^2, m_{\tilde{q}_1}^2) + B_1(m_q^2, m_{\tilde{g}}^2, m_{\tilde{q}_2}^2) \\ & + \frac{m_{\tilde{g}}}{m_q} \sin 2\,\theta [B_0(m_q^2, m_{\tilde{g}}^2, m_{\tilde{q}_1}^2) \\ & - B_0(m_q^2, m_{\tilde{g}}^2, m_{\tilde{q}_2}^2)] \bigg\}, \end{split}$$
(16)

and the wave-function renormalization constants

$$\delta Z_q^{(g)} = \frac{\alpha_s}{3\pi} \{ 1 - 2B_0(m_q^2, m_q^2, \lambda^2) - 2B_1(m_q^2, m_q^2, \lambda^2) + 4m_q^2 [DB_0(m_q^2, m_q^2, \lambda^2) - DB_1(m_q^2, m_q^2, \lambda^2)] \},$$
(17)

$$\delta Z_L^{(\tilde{g})} = \Sigma_L^{(\tilde{g})} + m_q^2 (\dot{\Sigma}_L^{(\tilde{g})} + \dot{\Sigma}_R^{(\tilde{g})}) + 2m_q \dot{\Sigma}_s^{(\tilde{g})}, \tag{18}$$

$$\delta Z_R^{(\tilde{g})} = \Sigma_R^{(\tilde{g})} + m_q^2 (\dot{\Sigma}_L^{(\tilde{g})} + \dot{\Sigma}_R^{(\tilde{g})}) + 2m_q \dot{\Sigma}_s^{(\tilde{g})}, \qquad (19)$$

with $\dot{X} = dX/dp^2$. In the above expressions we denote $B_X(X=0,1)$ as the two point functions and DB_X as the derivative of B_X with respect to the momentum squared. We give the related two point, three point, and four point functions in Appendix B.

The counterterms for the coupling coefficients of the Higgs-top-bottom vertex and top-bottom- W^+ boson vertex are

$$\delta_{htb}^{(g)} = -\frac{\delta m_t^{(g)}}{m_t} + \frac{1}{2} (\delta Z_t^{(g)} + \delta Z_b^{(g)}), \qquad (20)$$

$$\delta_{tbW}^{(g)} = \frac{1}{2} (\delta Z_t^{(g)} + \delta Z_b^{(g)}), \qquad (21)$$

$$\delta_{htb}^{(\tilde{g})} = -\frac{\delta m_t^{(g)}}{m_t} + \frac{1}{2} (\delta Z_{t_R}^{(\tilde{g})} + \delta Z_{b_L}^{(\tilde{g})}), \qquad (22)$$

$$\delta_{tbW}^{(\tilde{g})} = \frac{1}{2} (\delta Z_{t_L}^{(\tilde{g})} + \delta Z_{b_L}^{(\tilde{g})}).$$
(23)

The amplitudes of the diagrams containing above counterterms will cancel out the ultraviolet divergences contained in the amplitudes for Figs. 2(b),2(c) and Figs. 3(b),3(c) completely.



FIG. 3. Diagrams relevant for the calculation of the $\mathcal{O}(\alpha_s)$ gluino corrections to the width of the three-body decay $H^+ \rightarrow W^+ b \bar{b}$.

To remove the ultraviolet divergence of the amplitude for Fig. 3(a), we introduce the following counterterm which corresponds to Fig. 4(c):

$$i\left[p(\delta Z_{t_L}^{(\tilde{g})}P_L + \delta Z_{t_R}^{(\tilde{g})}P_R) - m_t \frac{\delta Z_{t_L}^{(\tilde{g})} + \delta Z_{t_R}^{(\tilde{g})}}{2} + \delta m_t^{(\tilde{g})}\right].$$
(24)

There is another way to get the same results. If we only subtract δm from the self-energy function Σ at the mass shell, the remaining ultraviolet divergences will disappear automatically after we add all the amplitudes for loop diagrams (including the self-energy diagrams of the external legs) and the mass counterterms related with the H^+tb vertex. The $\mathcal{O}(\alpha_s)$ contributions to the three-body decay width are given by the interference terms between higher order amplitudes and tree-level amplitude: i.e.,



FIG. 4. Diagrams relevant for wave-function and mass renormalization in the calculations of the $\mathcal{O}(\alpha_s)$ QCD and SUSY-QCD corrections to the width of the three-body decay $H^+ \rightarrow W^+ b\bar{b}$.



FIG. 5. Diagrams for real-gluon emission $H^+ \rightarrow W^+ b \bar{b} g$.

$$\delta\Gamma = \int_{\text{phase space}} 2 \operatorname{Re}\left(\sum_{\epsilon,c,\sigma} M^{(\alpha_s)} M_0^*\right), \quad (25)$$

where ϵ represents the *W*-boson polarization and c, σ represent the color and spin of *b* and \overline{b} , respectively.

The above results still contain infrared divergences which are cancelled out by the infrared divergences in real gluon emission given by Fig. 5. In our calculations of the real gluon emission contributions, we closely follow the procedure discussed in Ref. [10] where an energy cutoff ΔE is adopted to distinguish soft and hard gluon. The soft gluon contribution is calculated by soft gluon approximation and the hard gluon contribution is calculated by Monte Carlo methods [12,13]. The contributions of soft gluon emission of Figs. 5(a),5(b) are

$$\frac{d\Gamma^{(a)}}{ds_b d\bar{s}_b} = -\frac{\alpha_s}{3\pi^2} I_{11} \frac{d\Gamma_0}{ds_b ds_{\bar{b}}},\tag{26}$$

$$\frac{d\Gamma^{(b)}}{ds_b d\bar{s}_b} = -\frac{\alpha_s}{3\pi^2} I_{22} \frac{d\Gamma_0}{ds_b d\bar{s}_b},\tag{27}$$

respectively, while that of the interference term between Figs. 5(a) and 5(b) is

$$\frac{d\Gamma^{(\text{inter})}}{ds_b d\bar{s}_b} = \frac{2\alpha_s}{3\pi^2} I_{12} \frac{d\Gamma_0}{ds_b d\bar{s}_b},\tag{28}$$

where

$$I_{ij} = \int_{|\mathbf{k}| \le \Delta E} \frac{d^3k}{2\omega_k} \frac{2p_i p_j}{(p_i k)(p_j k)},\tag{29}$$

with $\omega_k = \sqrt{\mathbf{k}^2 + \lambda^2}$ and ΔE the cutoff parameter. The explicit form of I_{ij} is given in Ref. [10]. The infrared divergence terms contained in Eqs. (26), (27) are the same



FIG. 6. Diagrams relevant for the charged Higgs corrections to the width of the three-body decay $H^+ \rightarrow W^+ b \bar{b}$.

$$-\frac{2\alpha_s}{3\pi}\ln\frac{4\Delta E^2}{\lambda^2}\frac{d\Gamma_0}{ds_b d\bar{s}_b}.$$
(30)

The infrared divergence terms contained in Eq. (28) is

$$\frac{4\alpha_s}{3\pi} \ln \frac{2p_1 p_2}{m_b^2} \ln \frac{4\Delta E^2}{\lambda^2} \frac{d\Gamma_0}{ds_b d\bar{s}_b}.$$
(31)

The infrared divergences in Eqs. (26), (27) will cancel out the the infrared divergences contained in $\delta Z_b^{(g)}$ and that in Eq. (28) will cancel out the infrared divergence coming from the contribution of the box diagram in Fig. 2. This can be seen from the analytical form of $\delta Z_b^{(g)}$

$$\delta Z_b^{(g)} = \frac{\alpha_s}{3\pi} \bigg[-\bigg(\frac{1}{\epsilon} + \ln 4\pi - \gamma_E\bigg) - 2\ln\frac{\lambda^2}{m_b^2} - \ln\frac{\mu^2}{m_b^2} - 4\bigg],\tag{32}$$

where $D=4-2\epsilon$ is the space-time dimension, γ_E the Euler's constant, and μ the 't Hooft mass parameter in the dimensional regularization scheme. The divergent part of the amplitude for the box diagram is contained in the following integral:

$$M^{\rm IR} = G \frac{\alpha_s}{3\pi} (2\pi\mu)^{4-D} \int \frac{d^D k}{i\pi^2} \\ \times \frac{\bar{u}(p_2) 2m_t \not{p}_1 \not{\epsilon} \not{p}_2 P_L v(p_1)}{(k^2 - \lambda^2) [(p_2 - k)^2 - m_b^2] [(p_1 + k)^2 - m_b^2](p_t^2 - m_t^2)} \\ = G \frac{\alpha_s}{3\pi} \frac{-4m_t p_1 \cdot p_2 \bar{u}(p_2) \not{\epsilon} P_L v(p_1)}{p_t^2 - m_t^2} \\ \times C_0 [m_b^2, m_b^2, (p_1 + p_2)^2, m_b^2, \lambda^2, m_b^2].$$
(33)

The analytical expression of C_0 can be found in Ref. [14]. We can thus easily obtain the infrared part contained in the contribution due to the box diagram in Fig. 2:

$$\frac{d\Gamma(\text{box})}{ds_b ds_{\bar{b}}} \sim \frac{-4\alpha_s}{3\pi} \ln \frac{m_b^2}{2p_1 \cdot p_2} \ln \frac{\lambda^2}{2p_1 \cdot p_2} \frac{d\Gamma_0}{ds_b ds_{\bar{b}}}.$$
 (34)



FIG. 7. Comparison of the tree-level width with those including the standard QCD or gluino corrections . The parameters taken in gluino corrections are $(m_{\tilde{t}_1}, m_{\tilde{g}}, \mu, A) = (200, 400, -300, 200)$.

It is evident that all the infrared divergences are cancelled out completely.

At last, we consider the charged Higgs boson loop corrections to the width because we are interested in the large $\cot \beta$ region where the coupling of charged Higgs boson to top quark and bottom quark is large. The corresponding diagrams are shown in Fig. 6. The substraction procedure is standard [11]. We will discuss the numerical result for it in the next section.



FIG. 8. Contour lines of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ for $(m_{H^+}, m_{\tilde{g}}, m_{t_L}) = (150,400,280)$ GeV and $\tan \beta = 1$ in the A- μ plane.



FIG. 9. Contour lines of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ for $(m_{H^+}, m_{\tilde{g}}, \mu) = (150, 420, 300)$ GeV and $\tan \beta = 1$ in the $A - m_{\tilde{t}_1}$ plane.

III. NUMERICAL CALCULATIONS AND DISCUSSIONS

We now turn to the numerical evaluation of the corrected width. We have tested the results in a number of ways. We found that the results are reliable since they do not depend on the choice of the 't Hooft mass parameters μ in the dimensional-regularization scheme and the fictitious gluon mass λ . We also choose different energy cutoffs in the calculation of soft gluon emission and find the results are independent of it to a satisfactory precision. The cancellation of ln m_b is examined too.

The whole analysis will depend on m_{H^+} , $\tan \beta, \mu, A$ $(=A_t), m_{\tilde{g}}, m_{\tilde{t}_L}(=m_{\tilde{b}_L})$, and $m_{\tilde{t}_R}$. For simplicity, we have assumed $m_{\tilde{t}_L} = m_{\tilde{t}_R}$ in the calculations. We take $|V_{tb}| = 1$,



FIG. 10. Contour lines of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ for $(m_{H^+}, m_{\tilde{g}}, A) = (150, 420, 300)$ GeV and $\tan \beta = 1$ in the $\mu - m_{\tilde{t}_L}$ plane.



FIG. 11. Contour lines of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ for $(m_{H^+}, \mu, m_{\tilde{t}_1}, A) = (150, -300, 280, 300)$ GeV in the tan $\beta - m_{\tilde{g}}$ plane.

 $m_t = 180$ GeV, $m_b = 4.8$ GeV, $m_W = 80.4$ GeV, $\sin^2 \theta_W = 0.23$, $\alpha = 1/128$, $\alpha_s = \alpha_s(150 \text{ GeV}) = 0.113$, and $m_Z = 91.2$ GeV. The SUSY parameters are constained to satisfy the lighter top squark $m_{\tilde{t}_1} \ge 90$ GeV.

The effects of the standard QCD and SUSY-QCD corrections of Eqs. (8), (9), (10), and (11) can be seen in Fig. 7, in which we take $(m_{\tilde{t}_L}, m_{\tilde{g}}, \mu, A) = (200, 400, -300, 200)$ GeV. The results show the QCD corrctions raise the width by about 12%. The gluino corrections can raise the width by about 9% if we take the parameters listed above.

In Fig. 8, we show the contour lines of



FIG. 12. The ratio of the three-body decay width including the standard QCD corrections to the width of the two-body decay $(H^+ \rightarrow c\bar{s}, \tau^+ \nu)$ for $m_{H^+} = 150$ GeV.



FIG. 13. The ratio of the gluino corrections to the three-body decay width to the width of the two-body decay $(H^+ \rightarrow \tau^+ \nu)$ for $(m_{H^+}, m_{\tilde{t}_t}, m_{\tilde{g}}, \mu, A) = (150, 200, 400, -300, 200)$ GeV.

 $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ in the $A-\mu$ plane for $\tan \beta = 1$ and $(m_{H^+}, m_{\tilde{g}}, m_{\tilde{b}_L} = m_{\tilde{t}_L}) = (150,400,280)$ GeV. This correction has a strong dependence on μ . It changes sign near $\mu \sim 0$ GeV. We can see for the chosen values of masses it can reach about 12% when A is near ± 450 GeV and μ is near ± 450 GeV.

In Fig. 9, we show the dependence of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$



FIG. 14. The ratio of the the three-body decay width including the standard QCD and charged Higgs boson corrections to the width of the two-body decay $(H^+ \rightarrow \tau^+ \nu)$ for $m_{H^+} = 150$ GeV.

as a function of A and $m_{\tilde{t}_L}$ for $\tan \beta = 1$ and $(m_{H^+}, m_{\tilde{g}}, \mu) = (150,420,300)$ GeV. We can see the gluino correction can be about 15% when A is negative and $m_{\tilde{t}_I}$ is about 100 GeV.

In Fig. 10 we show a contour plot of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ in the μ - $m_{\tilde{t}_L}$ plane for $\tan \beta = 1$ and $(m_{H^+}, m_{\tilde{g}}, A) = (150,420,300)$ GeV. We find the corrections can reach 20% when $\mu = -500-400$ and $m_{\tilde{t}_I}$ is about 100 GeV.

In Fig. 11 we show a contour plot of $\delta\Gamma(\text{gluino})/\Gamma(\text{tree})$ in the $\tan\beta - m_{\tilde{g}}$ plane for $(m_{H^+}, \mu, m_{\tilde{t}_L}, A) = (150, -300, 280, 300)$ GeV. Divided by $\tan\beta = 1.1$, the left part of the graph is similar to the right part. The correction rises when $\tan\beta$ deviates from $\tan\beta = 1.1$. Given a $\tan\beta$, the corrections increase up to about $m_{\tilde{g}} = 650$ GeV and then decrease as $m_{\tilde{g}}$ increases.

The reason for the large contribution of $\delta\Gamma(\text{gluino})$ is mainly because the vertex correction part of the gluinoexchange corrections is proportional to the $H^+\tilde{t}\tilde{b}$ coupling which can be enlarged greatly if the \tilde{t} -mixing parameters A and μ are large.

In Fig. 12, we show the ratio of the three-body decay width including the standard QCD corrections to the width of the two-body decay $(H^+ \rightarrow c\bar{s}, \tau^+ \nu)$, in which we can clearly see the corrected three-body decay rises sharply with increasing m_{H^+} . It can reach more than 8 times the size of the two-body decay in the given area.

In Fig. 13, we show the ratio of $\delta\Gamma^{(g)}$, the corrections due to gluino exchanges, to the width of the two-body decay $(H^+ \rightarrow \tau^+ \nu)$, in which we take $(m_{\tilde{t}_L}, m_{\tilde{g}}, \mu, A) = (200, 400, -300, 200)$ GeV. These curves indicate that the ratio tends to be smaller when tan β increases while it can be large when tan β is less than 1.

Finally, we have calculated the dominant terms from the Higgs boson loop corrections in Fig. 6. We find the Higgs boson corrections are relatively small, which can lower the width by about $0.6\% \cot^2\beta$ when $m_{H^+} = 140$ GeV, and the ratio of the Higgs boson corrections to the tree-level contribution decreases when m_{H^+} increases. Therefore, the Higgs boson corrections can be neglected if tan β is not too small.

In Fig. 14, we show the ratio of $\Gamma_0 + \delta \Gamma^{(g)} + \delta \Gamma^{(H^+)}$ (the width including the standard QCD and charged Higgs corrections) to the width of the two-body decay $(H^+ \rightarrow \tau^+ \nu)$. If we measure the three channels $H^+ \rightarrow \tau^+ \nu$, $H^+ \rightarrow c\bar{s}$, and $H^+ \rightarrow W^+ b\bar{b}$ simultaneously and obtain $\tan \beta$ of the two-Higgs doublet model of type II from $\Gamma_{c\bar{s}}/\Gamma_{\tau^+\nu}$, we can check the validity of the two-Higgs doublet model of type II without supersymmetry by comparing the experimental data for $\Gamma_3/\Gamma_{\tau^+\nu}$ with theoretical results similar to those in Fig. 14.

In summary, we have performed complete calculations of the $\mathcal{O}(\alpha_s)$ standard QCD and SUSY-QCD corrections to the width of $H^+ \rightarrow b\bar{b}W^+$. We have found that the QCD corrections raise the width by about 12% and the SUSY-QCD corrections can be comparable to or even larger than the standard QCD corrections and change signs as μ varies. This provides an effective way to distinguish the two-Higgs doublet model of type II from the MSSM.

APPENDIX A

In this appendix we list some relevant pieces of the SUSY Lagrangian. The charged Higgs boson coupling to top and bottom quarks is given by

$$\mathcal{L} = \frac{gV_{tb}}{\sqrt{2}m_W} H^+ [m_t \cot\beta \bar{t} P_L b + m_b \tan\beta \bar{b} P_R t] + \text{H.c.},$$
(A1)

where $P_{L,R} = \frac{1}{2}(1 \mp \gamma_5)$ are the chiral projector operators, cot $\beta = v_1/v_2$ is the ratio of the vaccum expectation values of the two Higgs doublets and V_{tb} is the CKM matrix element.

The squark couplings to the charged Higgs boson, gluino, and W^+ boson are given by

$$\mathcal{L}_{\tilde{t}\tilde{b}H} = \frac{-g}{\sqrt{2}m_{W}} \bigg[(m_{W}^{2}\sin 2\beta - m_{t}^{2}\cot\beta - m_{b}^{2}\tan\beta) Z_{1j}^{b} Z_{1i}^{t} - \frac{2m_{t}m_{b}}{\sin 2\beta} Z_{2j}^{b} Z_{2i}^{t}, + m_{t}(A_{t}^{*}\cot\beta - \mu) Z_{2i}^{t} Z_{1j}^{b} + m_{b}(A_{b}\tan\beta - \mu^{*}) Z_{2j}^{b} Z_{1i}^{t} \bigg] V_{tb}^{*} \tilde{t}_{i} \tilde{b}_{j}^{*} H^{-} + \text{H.c.},$$
(A2)

$$\mathcal{L}_{\tilde{t}t\tilde{g}} = g_s \sqrt{2} \tilde{t}_i^* T^a \bar{\tilde{g}}^a [-Z_{1i}^{t*} P_L + Z_{2i}^{t*} P_R] t + \text{H.c.},$$
(A3)

$$\mathcal{L}_{\tilde{b}b\tilde{g}} = g_s \sqrt{2} \tilde{b}_i^* T^a \overline{\tilde{g}}^a [-Z_{1i}^{b*} P_L + Z_{2i}^{b*} P_R] b + \text{H.c.},$$
(A4)

$$\mathcal{L}_{\tilde{b}\tilde{t}W} = \frac{-g}{\sqrt{2}} Z_{1i}^{b} Z_{1j}^{t} V_{tb} (\tilde{b}_{i}^{*} \overleftrightarrow{\partial}^{\mu} \tilde{t}_{j}) W_{\mu}^{-} + \text{H.c.}, \qquad (A5)$$

respectively, in which g_s is the QCD coupling constant, g is the EW coupling constant, and T^a is the matrices of the SU(3) generators in the three representation:

$$Z^{t} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$
(A6)

and Z^b are orthogonal matrices which diagonalize the mass matrices $M_{\tilde{t}}^2$ and $M_{\tilde{b}}^2$ of the squarks:

$$M_{\tilde{t}}^{2} = \begin{pmatrix} m_{\tilde{t}_{L}}^{2} + m_{t}^{2} + 0.35(m_{Z}^{2}\cos 2\beta) & -m_{t}(A_{t} + \mu \cot \beta) \\ -m_{t}(A_{t} + \mu \cot \beta) & m_{\tilde{t}_{R}}^{2} + m_{t}^{2} + 0.15(m_{Z}^{2}\cos 2\beta) \end{pmatrix},$$
 (A7)

$$M_{\tilde{b}}^{2} = \begin{pmatrix} m_{\tilde{b}_{L}}^{2} + m_{b}^{2} - 0.42(m_{Z}^{2}\cos 2\beta) & -m_{b}(A_{b} + \mu \tan \beta) \\ -m_{b}(A_{b} + \mu \tan \beta) & m_{\tilde{b}_{R}}^{2} + m_{b}^{2} - 0.08(m_{Z}^{2}\cos 2\beta) \end{pmatrix},$$
 (A8)

when we neglect the mass of bottom-quark, the last mass matrix reduces to

$$M_{\tilde{b}}^{2} = \begin{pmatrix} m_{\tilde{b}_{L}}^{2} - 0.42(m_{Z}^{2}\cos 2\beta) \\ m_{\tilde{b}_{R}}^{2} - 0.08(m_{Z}^{2}\cos 2\beta) \end{pmatrix}.$$
 (A9)

APPENDIX B

In the expressions below, $m_{\tilde{b}} = m_{\tilde{b}_1}$ and $Z_{ij}(i,j=1,2)$ represent the elements of matrix Z^t defined in Appendix A.

$$F_1^{(g)} = -2m_t^3 + 2m_t^3 B_0(0, m_t^2, 0) + 2m_t(m_t^2 + s_{\bar{b}}) B_0(s_{\bar{b}}, m_t^2, 0),$$
(B1)

$$F_{2}^{(g)} = -m_{t} [1 - 2B_{0}(m_{W}^{2}, 0, m_{t}^{2}) + 2(m_{W}^{2} - s_{\bar{b}})C_{0}(m_{W}^{2}, s_{\bar{b}}, m_{b}^{2}, m_{b}^{2}, m_{t}^{2}, 0) + 2(m_{W}^{2} - 2s_{\bar{b}})C_{1}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) + 2(m_{W}^{2} - s_{\bar{b}})C_{2}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) + 4C_{00}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2})],$$
(B2)

$$F_{3}^{(g)} = 4m_{t} \left[C_{1}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) + C_{11}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) + C_{12}(s_{\bar{b}}, m_{W}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) \right],$$
(B3)

$$F_{4}^{(g)} = -2m_{t} [1 - 2B_{0}(m_{H^{+}}^{2}, 0, m_{t}^{2}) - (m_{W}^{2} - s_{b} - s_{W})C_{0}(s_{\bar{b}}, m_{H^{+}}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) - (m_{W}^{2} + s_{\bar{b}} - s_{b} - s_{W})C_{1}(s_{\bar{b}}, m_{H^{+}}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2}) - (m_{W}^{2} - s_{b} - s_{W})C_{2}(s_{\bar{b}}, m_{H^{+}}^{2}, m_{b}^{2}, 0, m_{t}^{2}, m_{b}^{2})],$$
(B4)

$$F_{5}^{(g)} = 2m_{t}C_{0}(m_{W}^{2}, s_{W}, m_{H^{+}}^{2}, m_{t}^{2}, m_{b}^{2}, m_{b}^{2}) - 2m_{t}s_{W}D_{0}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) - 2m_{t}s_{W}D_{1}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) + 2m_{t}(s_{\bar{b}} - s_{b} - s_{W}) \times D_{2}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) - 2m_{t}s_{W}D_{3}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) - 4m_{t}D_{00}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}),$$
(B5)

$$F_{6}^{(g)} = -4m_{t}D_{2}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) - 4m_{t}D_{12}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}) - 4m_{t}D_{22}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, 0, m_{b}^{2}, m_{t}^{2}, m_{b}^{2}),$$
(B6)

$$F_{7}^{(g)} = 4m_t D_2(m_b^2, m_W^2, m_{H^+}^2, m_b^2, s_{\bar{b}}, s_W, 0, m_b^2, m_t^2, m_b^2) + 4m_t D_{23}(m_b^2, m_W^2, m_{H^+}^2, m_b^2, s_{\bar{b}}, s_W, 0, m_b^2, m_t^2, m_b^2),$$
(B7)

$$F_{1}^{(\tilde{g})} = m_{t}B_{0}(0,m_{\tilde{g}}^{2},m_{\tilde{t}_{i}}^{2})(m_{\tilde{g}}^{2}-m_{\tilde{t}_{i}}^{2})(Z_{1i}^{2}+Z_{2i}^{2}) - B_{0}(s_{\bar{b}},m_{\tilde{g}}^{2},m_{\tilde{t}_{i}}^{2})(m_{\tilde{g}}^{2}m_{t}Z_{1i}^{2}+m_{t}s_{\bar{b}}Z_{1i}^{2}-m_{t}m_{\tilde{t}_{i}}^{2}Z_{1i}^{2}-2m_{\tilde{g}}m_{t}^{2}Z_{1i}Z_{2i} - 2m_{\tilde{g}}m_{t}^{2}Z_{1i}Z_{2i} - 2m_{\tilde{g}}m_{t}^{2}Z_{2i} - 2m_{\tilde{g}}m_{t}^$$

$$F_{2}^{(\tilde{g})} = 4m_{t} [C_{00}(m_{b}^{2}, m_{W}^{2}, s_{\bar{b}}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}) Z_{1i}^{2}],$$
(B9)

$$F_{3}^{(\tilde{g})} = 4Z_{1i}[m_{t}C_{12}(m_{b}^{2},m_{W}^{2},s_{\bar{b}},m_{\tilde{g}}^{2},m_{\tilde{b}}^{2},m_{\tilde{t}_{i}}^{2})Z_{1i} + m_{t}C_{22}(m_{b}^{2},m_{W}^{2},s_{\bar{b}},m_{\tilde{g}}^{2},m_{\tilde{t}_{i}}^{2}) + m_{\tilde{g}}C_{0}(m_{W}^{2},s_{\bar{b}},m_{b}^{2},m_{\tilde{b}}^{2},m_{\tilde{t}_{i}}^{2},m_{\tilde{g}}^{2})Z_{2i} + m_{\tilde{g}}C_{1}(m_{b}^{2},m_{W}^{2},s_{\bar{b}},m_{\tilde{g}}^{2},m_{\tilde{t}_{i}}^{2})Z_{2i} + C_{2}(m_{b}^{2},m_{W}^{2},s_{\bar{b}},m_{\tilde{g}}^{2},m_{\tilde{b}}^{2},m_{\tilde{t}_{i}}^{2})(m_{\tilde{g}}Z_{2i} + m_{t}Z_{1i})],$$
(B10)

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(B14)

$$F_{4}^{(\tilde{g})} = \frac{-2}{m_{t} \cot \beta} [s_{\bar{b}}C_{1}(s_{\bar{b}}, m_{H^{+}}^{2}, m_{b}^{2}, m_{\tilde{g}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2})Z_{1i} + m_{\tilde{g}}m_{t}C_{0}(s_{\bar{b}}, m_{H^{+}}^{2}, m_{b}^{2}, m_{\tilde{g}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2})Z_{2i}][(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta)Z_{1i} + m_{t}(A \cot \beta - \mu)Z_{2i}],$$
(B11)

$$F_{5}^{(\tilde{g})} = \frac{-4}{m_{t} \cot \beta} D_{00}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2}) Z_{1i}[(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta) Z_{1i} + m_{t}(A \cot \beta - \mu) Z_{2i}],$$
(B12)

$$F_{6}^{(\tilde{g})} = \frac{-4}{m_{t} \cot \beta} \{ D_{2}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2}) Z_{1i} [(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta) Z_{1i} + m_{t} (A \cot \beta - \mu) Z_{2i}] + D_{12}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2}) Z_{1i} [(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta) Z_{1i} + m_{t} (A \cot \beta - \mu) Z_{2i}] + D_{22}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2}) Z_{1i} [(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta) Z_{1i} + m_{t} (A \cot \beta - \mu) Z_{2i}] \},$$
(B13)
$$F_{7}^{(\tilde{g})} = \frac{4}{m_{t} \cot \beta} D_{23}(m_{b}^{2}, m_{W}^{2}, m_{H^{+}}^{2}, m_{b}^{2}, s_{\bar{b}}, s_{W}, m_{\tilde{g}}^{2}, m_{\tilde{g}}^{2}, m_{\tilde{b}}^{2}, m_{\tilde{t}_{i}}^{2}, m_{\tilde{b}}^{2}) Z_{1i} [(m_{W}^{2} \sin 2\beta - m_{t}^{2} \cot \beta) Z_{1i} + m_{t} (A \cot \beta - \mu) Z_{2i}] \}.$$

The relevant scalar fuctions are defined as follows:

$$B_0(p_1^2, m_0^2, m_1^2) = (i\pi^2)^{-1} (2\pi\mu)^{4-D} \int d^D q \{ (q^2 - m_0^2) [(q+p_1)^2 - m_1^2] \}^{-1},$$
(B15)

$$C_{0}(p_{1}^{2},p_{12},p_{2}^{2},m_{0}^{2},m_{1}^{2},m_{2}^{2}) = (i\pi^{2})^{-1}(2\pi\mu)^{4-D} \int d^{D}q \{(q^{2}-m_{0}^{2})[(q+p_{1})^{2}-m_{1}^{2}][(q+p_{2})^{2}-m_{2}^{2}]\}^{-1},$$
(B16)

$$D_{0}(p_{1}^{2}, p_{12}, p_{23}, p_{3}^{2}, p_{2}^{2}, p_{13}, m_{0}^{2}, m_{1}^{2}, m_{2}^{2}, m_{3}^{2}) = (i\pi^{2})^{-1}(2\pi\mu)^{4-D} \int d^{D}q \{(q^{2}-m_{0}^{2})[(q+p_{1})^{2}-m_{1}^{2}][(q+p_{2})^{2}-m_{2}^{2}] \\ \times [(q+p_{3})^{2}-m_{3}^{2}]\}^{-1},$$
(B17)

$$DB_0(p_1^2, m_0^2, m_1^2) = \frac{\partial B_0(p_1^2, m_0^2, m_1^2)}{\partial p_1^2},$$
(B18)

in which $p_{ij} = (p_i - p_j)^2$. The definitions of the tensor-integrals and the relevant decompositions are given below

$$T_{\mu_1\dots\mu_p}(p_1,\dots,p_{N-1},m_0,\dots,m_{N-1}) = \frac{(2\pi\mu)^{4-D}}{i\pi^2} \int d^D q \frac{q_{\mu_1}\cdots q_{\mu_n}}{D_0 D_1\cdots D_{N-1}},$$
(B19)

with the denominator factors $D_0 = q^2 - m_0^2$, $D_i = (q + p_i)^2 - m_i^2$ $(i = 1, \dots, N-1)$

$$B_{\mu} = p_{1\mu} B_1,$$
 (B20)

$$C_{\mu} = p_{1\mu}C_1 + p_{2\mu}C_2 = \sum_{i=1}^{2} p_{i\mu}C_i, \qquad (B21)$$

$$C_{\mu\nu} = g_{\mu\nu}C_{00} + p_{1\mu}p_{1\nu}C_{11} + p_{2\mu}p_{2\nu}C_{22} + (p_{1\mu}p_{2\nu} + p_{2\mu}p_{1\nu})C_{12}$$
(B22)

$$=g_{\mu\nu}C_{00} + \sum_{i,j=1}^{2} p_{i\mu}p_{j\nu}C_{ij},$$
(B23)

$$D_{\mu} = \sum_{i=1}^{3} p_{i\mu} D_{i}, \qquad (B24)$$

$$D_{\mu\nu} = g_{\mu\nu} D_{00} + \sum_{i,j=1}^{3} p_{i\mu} p_{j\nu} D_{ij}.$$
(B25)

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