

Promising process to distinguish supersymmetric models with large $\tan\beta$ from the standard model: $B \rightarrow X_s \mu^+ \mu^-$

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It is shown that in supersymmetric models the large supersymmetric contributions to $B \rightarrow X_s \mu^+ \mu^-$ come from the Feynman diagrams which consist of exchanging neutral Higgs boson loops and are proportional to $m_b m_\mu \tan^3 \beta / m_h^2$ when $\tan\beta$ is large and the mass of the lightest neutral Higgs boson m_h is not too large (say, less than 150 GeV). Numerical results show that the branching ratios of $B \rightarrow X_s \mu^+ \mu^-$ can be enhanced by more than 100% compared to the standard model (SM) and the backward-forward asymmetry of the lepton is significantly different from that in the SM when $\tan\beta \geq 30$. [S0556-2821(98)50123-3]

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It is widely believed that supersymmetry (SUSY) is one of the most promising candidates for physics beyond the standard model (SM) since it offers a scheme to embed the SM in a more fundamental theory in which many theoretical problems such as gauge hierarchy, origin of mass, and Yukawa couplings can be answered. One direct way to search for SUSY is to discover SUSY particles at colliders. But, unfortunately, so far no SUSY particles have been found. Another way is to search for its effect through indirect methods. In most SUSY models (SUSYMs) R parity is conserved so that SUSY contributions to an observable appear at the loop level. Therefore, it has been realized for a long time that rare processes can be used as a good probe for searches of SUSY, since in these processes the contributions of SUSY and SM arise at the same order in perturbation theory. The $B \rightarrow X_s l^+ l^-$ ($l = e, \mu, \tau$) process, one of rare processes, in SUSYMs has been extensively studied [1–5]. The effects of large $\tan\beta$ have been noticed in recent papers [4,5]. There is a top-squark–chargino loop diagram which gives a large contribution to C_7 when $\tan\beta$ is large [6]. This leads to that in the minimal supergravity model ($mSUGRA$) there are regions in the parameter space where the branching ratio of $b \rightarrow sl^+ l^-$ ($l = e, \mu$) is enhanced by about 50% compared to the SM [5]. However, the contributions from exchanging neutral Higgs bosons (NHBs) are ignored in these previous analyses. Recently, the contributions of NHBs in SUSYMs have been taken into account. Because the contributions to $b \rightarrow s\tau^+ \tau^-$ coming from the chargino-top-squark loop diagram are proportional to $m_b m_\tau \tan^3 \beta / m_h^2$ ($h = h^0, A^0$) when $\tan\beta$ is large, the branching ratio of $b \rightarrow s\tau^+ \tau^-$ can be enhanced by about 200% compared to the SM [7].

From experimental points of view, the observation of $B \rightarrow X_s l^+ l^-$ ($l = e, \mu$) is more easily accessible than that of $B \rightarrow X_s \tau^+ \tau^-$. The inclusive decay $B \rightarrow X_s \gamma$ has been observed by CLEO. In the meantime, experiments at $e^+ e^-$ and hadron colliders are closing in on the observation of $B \rightarrow K^* l^+ l^-$ ($l = e, \mu$) [8]. The B factories presently under

construction will collect some 10^7 – 10^8 B mesons per year which can be used to obtain good precision on low branching fraction modes. Therefore, it is meaningful to pay attention to the process $B \rightarrow X_s l^+ l^-$ ($l = e, \mu$). As pointed above, the contributions of NHBs are proportional to the mass of a lepton and $\tan^3 \beta$. For $B \rightarrow X_s e^+ e^-$, the contributions can be safely neglected due to the smallness of m_e , no matter how large $\tan\beta$ is [of course, in the theoretically allowed range, say, in a SUSY grand unified theory (GUT), $\tan\beta \leq 50$]. However, for $b \rightarrow s\mu^+ \mu^-$, $m_\mu \tan\beta$ can be as large as m_τ as long as $\tan\beta \geq 17$. Thus one can expect that for $b \rightarrow s\mu^+ \mu^-$, in addition to the enhancement coming from the possible change of the sign of C_7 [the value of C_7 is fixed by the measurement of $b \rightarrow s\gamma$ with a branching ratio of $(2.32 \pm 0.57 \pm 0.35) \times 10^{-4}$ and 95% C.L. bounds of $1 \times 10^{-4} < X_{br}(B \rightarrow X_s \gamma) < 4.2 \times 10^{-4}$ [9]], an even more significant enhancement coming from exchanging NHBs arises in SUSYMs with large $\tan\beta$. In the Rapid Communication, we calculate the invariant mass distribution and backward-forward asymmetry of dilepton angular distribution for $B \rightarrow X_s \mu^+ \mu^-$ in SUSYMs. Our results show that the branching ratio of $B \rightarrow X_s \mu^+ \mu^-$ is enhanced by at least 100% compared to the SM and the back-forward asymmetry is more sensitive to $\tan\beta$ than the invariant mass distribution when $\tan\beta$ is larger than 30 and masses of Higgs bosons, stops and charginos are in the reasonable range (i.e., all constraints from phenomenology are satisfied). Note that the invariant mass distribution of $B \rightarrow X_s \mu^+ \mu^-$ in a two Higgs doublet model with large $\tan\beta$ is not enhanced compared to the SM. Therefore, the rare process $B \rightarrow X_s \mu^+ \mu^-$ provides a good opportunity to distinguish SUSYMs with large $\tan\beta$ from the SM and it is possible that the first distinct signals of SUSY could come from deviations from the SM in the inclusive decay $B \rightarrow X_s \mu^+ \mu^-$.

Inclusive decay rates of $B \rightarrow X_s \mu^+ \mu^-$ can be calculated in the $1/m_Q$ expansion and it has been shown that the leading order term turns to be the decay of a free b quark and corrections stem from the $1/m_Q^2$ order and are small about a few percent [10]. Therefore in what follows we limit our analyses to the leading order term, i.e., the decay $b \rightarrow s\mu^+ \mu^-$.

There are several classes of new contributions in SUSYMs and the dominant ones are arising from chargino–

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($\widetilde{\chi^-}$)up-type squark loop and charged Higgs boson (H^\pm)-up-type quark loop. Because of small generation mixing of squarks coming from phenomenological constraints on $K^0-\bar{K}^0$ and $D^0-\bar{D}^0$, the contributions from gluino-down-type squark loop and neutralino-down-type squark loop are much smaller than the dominant ones and are neglected in the following.

The effective Hamiltonian relevant to the $b \rightarrow s \mu^+ \mu^-$ process is

$$H_{eff} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left(\sum_{i=1}^{10} C_i(\mu) O_i(\mu) + \sum_{i=1}^{10} C_{Q_i}(\mu) Q_i(\mu) \right), \quad (1)$$

where O_i ($i=1, 2, \dots, 10$) are given in Ref. [11], and Q_i 's come from exchanging neutral Higgs bosons and have been given in Ref. [13]. The coefficients $C_i(m_w)$ in SUSYMs have been calculated [1,3]. We calculate the coefficients $C_{Q_i}(m_w)$ in SUSYMs and the results are

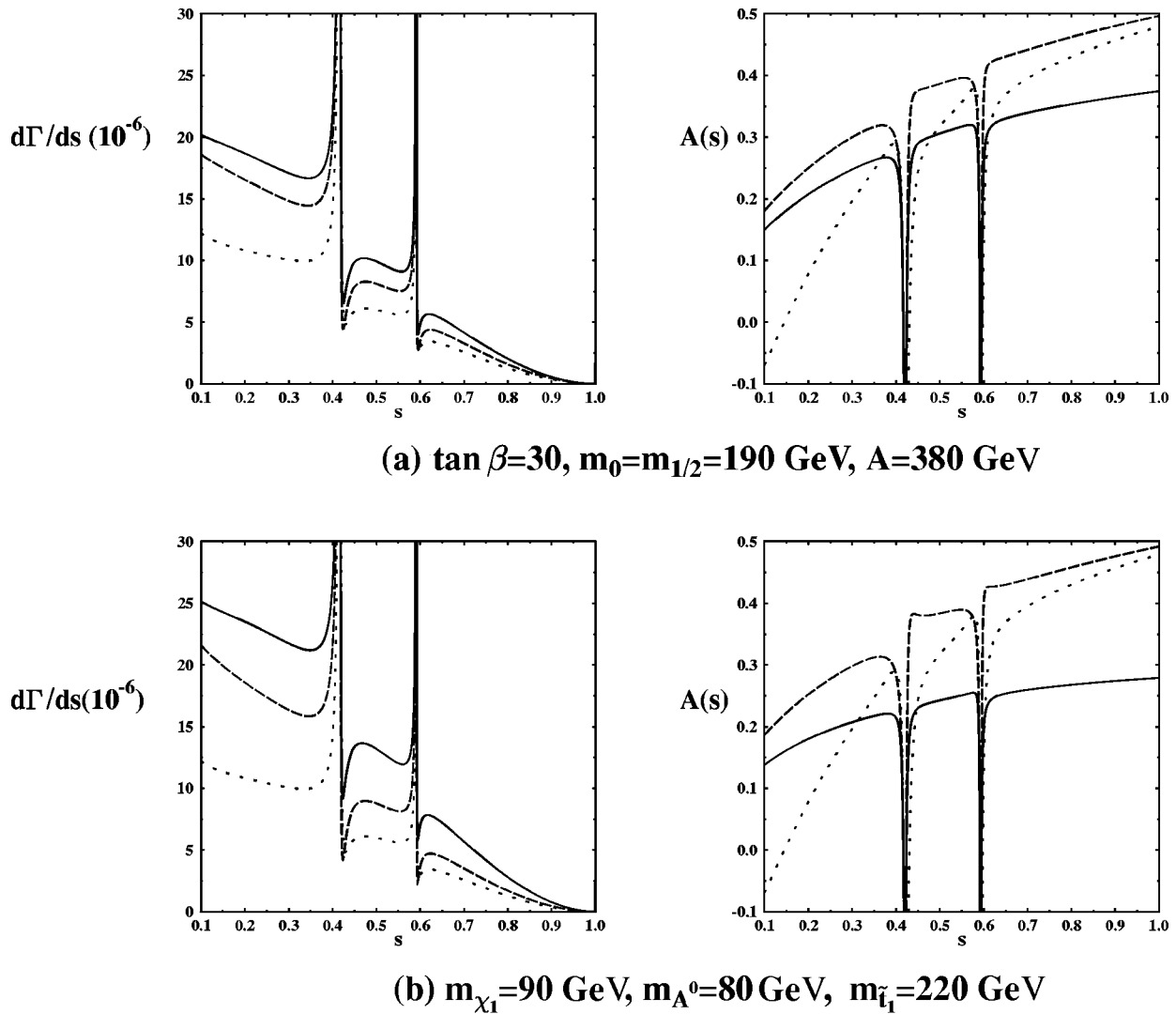
$$\begin{aligned} C_{Q_1}(m_w) &= \frac{m_b m_\mu}{4m_{h^0}^2 \sin^2 \theta_W} \tan^2 \beta \left\{ (\sin^2 \alpha + h \cos^2 \alpha) \left[\frac{1}{x_{Wt}} [f_1(x_{Ht}) - f_1(x_{Wt})] + \sqrt{2} \sum_{i=1}^2 \frac{m_{\chi_i} U_{i2}}{m_W \cos \beta} \right. \right. \\ &\quad \times \left[-V_{i1} f_1(x_{\chi_i \tilde{q}}) + \sum_{k=1}^2 \Lambda(i, k) T_{k1} f_1(x_{\chi_i \tilde{t}_k}) \right] + \left(1 + \frac{m_{H^\pm}^2}{m_W^2} \right) f_2(x_{Ht}, x_{Wt}) \left. \right] - \frac{m_{h^0}^2}{m_W^2} f_2(x_{Ht}, x_{Wt}) \\ &\quad \left. + 2 \sum_{ii'=1}^2 [B_1(i, i') \Gamma_1(i, i') + A_1(i, i') \Gamma_2(i, i')] \right\}, \\ C_{Q_2}(m_w) &= -\frac{m_b m_\mu}{4m_{A^0}^2 \sin^2 \theta_W} \tan^2 \beta \left(\frac{1}{x_{Wt}} [f_1(x_{Ht}) - f_1(x_{Wt})] + 2f_2(x_{Ht}, x_{Wt}) + \sqrt{2} \sum_{i=1}^2 \frac{m_{\chi_i} U_{i2}}{m_W \cos \beta} \right. \\ &\quad \left. \times \left[-V_{i1} f_1(x_{\chi_i \tilde{q}}) + \sum_{k=1}^2 \Lambda(i, k) T_{k1} f_1(x_{\chi_i \tilde{t}_k}) \right] + 2 \sum_{ii'=1}^2 [-U_{i'2} V_{i1} \Gamma_1(i, i') + U_{i2}^* V_{i'1}^* \Gamma_2(i, i')] \right), \quad (2) \end{aligned}$$

where the definitions of the functions f_i , Γ_i ($i=1, 2$), A_1 , B_1 , Λ and the meaning of the matrices U , V , T have been given in [7] and we have omitted less important terms because they are numerically negligible compared to those given in Eq. (2) when $\tan \beta \geq 20$.

From Eq. (2), we see that, for large $\tan \beta$ (≥ 20), the coefficients C_{Q_i} are proportional to $m_b m_\mu / m_h \tan^3 \beta$ ($h = h^0, A^0$). One factor of $\tan \beta$ comes from the chargino-up-type squark loop and $\tan^2 \beta$ from exchanging the neutral Higgs bosons (note that in the large $\tan \beta$ approximation, $\cos^{-1} \beta \approx \tan \beta$). Therefore, C_{Q_i} can compete with C_i and even overwhelm C_i as long as $\tan \beta$ is large enough. We remark that the chirality structure of the Q_i ($i=1, 2$) operators allows a large $\tan \beta$ enhancement for the C_{Q_i} ($i=1, 2$) coefficients, as happened for the magnetic moment operator O_7 , and there is no such large $\tan \beta$ enhancement for the C_i ($i=8, 9$) coefficients due to the different chirality structure of the O_i ($i=8, 9$) operators. Incorporating the QCD corrections to the coefficients C_i and C_{Q_i} in the standard way, we calculate these coefficients at $\mu = m_b$.

The differential branching ratio and the forward-backward asymmetry of the dimuon angular distribution for $B \rightarrow X_s \mu^+ \mu^-$ can be obtained from [7] with substituting m_μ for m_τ . The numerical results of the invariant mass distribu-

tion and backward-forward asymmetry are shown in Fig. 1(a) for the MSUGRA model and Fig. 1(b) for the MSSM with a typical choice of masses of sparticles and Higgs bosons, respectively. The MSUGRA parameters ($m_0, m_{1/2}, A$) = (190, 190, 380) GeV, Higgs mass mixing parameter $\mu < 0$ and $\tan \beta = 30$ have been chosen in Fig. 1(a). In the computations of sparticle mass spectra and mixings, we neglect the Yukawa couplings of the first two generations. The chosen values of masses of relevant sparticles and Higgs bosons in MSSM are given in the figure captions. The constraints from the CERN e^+e^- collider LEP and $b \rightarrow s \gamma$ [7,12] have been imposed in our numerical calculations. One can see from Fig. 1 that a large enhancement of the differential branching ratio $d\Gamma/ds$ shows up and the enhancement can reach 100% compared to SM when $\tan \beta = 30$. The backward-forward is significantly different from that in SM. The predictions without including the contributions of exchanging NHBs are also shown in Fig. 1 in order to compare. It is evident from the figure that the contributions of exchanging NHBs to the differential branching ratio are the same order of magnitude as supersymmetric contributions without including exchanging NHBs in the low s region ($s \leq 0.4$) and larger than those in the high s region ($s > 0.4$). There are regions in the parameter space where the contributions of NHBs alone make a large enhancement of the dif-



$$b \rightarrow s \mu^+ \mu^-$$

FIG. 1. $d\Gamma/ds$ and $A(s)$ for the case $\mu < 0$ and $\tan \beta = 30$ (a) $m_{1/2} = m_0 = 190$ GeV, $A = 380$ GeV in the MSUGRA and (b) $\theta_{\tilde{\tau}} = -40^\circ$, $m_{\chi_2} = 200$ GeV, $m_{\chi_1} = 90$ GeV, $m_{\tilde{q}} = 350$ GeV, $m_{\tilde{\tau}_1} = 220$ GeV, $m_{\tilde{\tau}_2} = 450$ GeV, $m_{A^0} = 80$ GeV, $m_{\tilde{\nu}} = 160$ GeV in the MSSM. The solid, dashed, and dotted lines represent the predictions of the SUSYMs, the SUSYMs without including contributions of NHBs and SM, respectively.

ferential branching ratio. For example, for a set of values of parameters ($\theta_{\tilde{\tau}} = -20^\circ$, $m_{\chi_2} = 220$ GeV, $m_{\chi_1} = 100$ GeV, $m_{\tilde{q}} = 430$ GeV, $m_{\tilde{\tau}_1} = 250$ GeV, $m_{\tilde{\tau}_2} = 500$ GeV, $m_{A^0} = 80$ GeV, $m_{\tilde{\nu}} = 160$ GeV, and $\tan \beta = 30$), the enhancement of $d\Gamma/ds$ coming from NHBs is about 80% compared to SM.

We would like to make some remarks.

(i) The large enhancement of the invariant mass distribution of $B \rightarrow X_s \mu^+ \mu^-$ compared to the SM is of a common feature of SUSYMs with large $\tan \beta$ in some region of the parameter space. Figure 2 shows the results for $\tan \beta = 30$. For larger $\tan \beta$, for example, $\tan \beta = 45$, the enhancement can reach 200%. The enhancement exists as long as the masses of the Higgs bosons h^0 and A^0 (actually of all Higgs bosons due to correlations among Higgs bosons masses) and

the chargino $\tilde{\chi}_1$, are small¹ (say, less than 200 GeV), and the mass splitting of top squarks is large enough (say, ≥ 100 GeV). The latter condition is necessary because if all the squark masses are degenerate ($m_{\tilde{\tau}_1} = m_{\tilde{\tau}_2} = \tilde{m}$), the large contributions arising from the chargino-squark loop exactly cancel due to the Glaskov-Iliopoulos-Maiani (GIM) mechanism [6]. In order to illustrate this point, we show the C_{Q_i} as a

¹Note that although the charged Higgs contribution is very dangerous for $b \rightarrow s \gamma$ when charged Higgs boson is light, sparticle contribution at large $\tan \beta$ overwhelms the W and Higgs contributions due to the light chargino and the large mass splitting of top squarks.

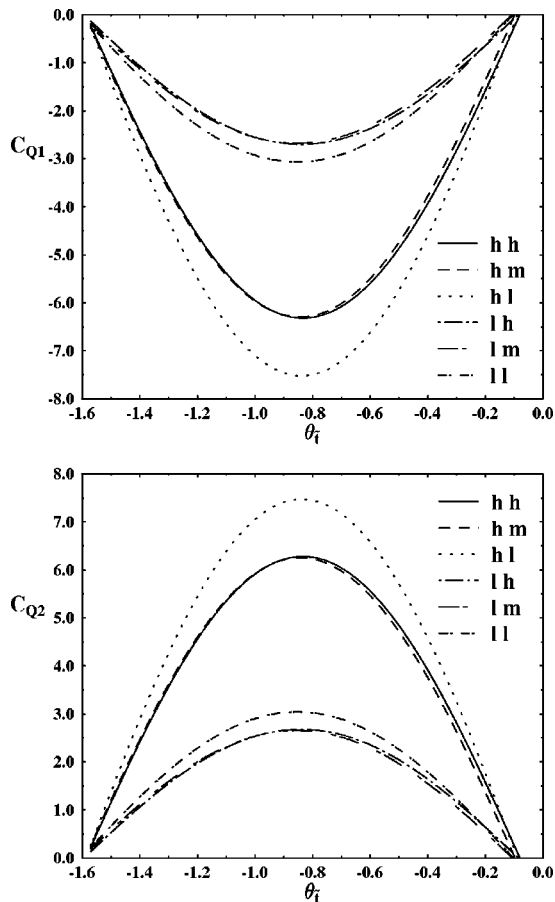


FIG. 2. C_{Q1} and C_{Q2} varying with the mass splitting of the top squark, the mass splitting of chargino, and the top squark mixing angle θ_7 for $\mu < 0$, $\tan \beta = 30$, $m_{\tilde{t}_1} = 150$ GeV, $m_{\tilde{\chi}_1} = 90$ GeV, and $m_{A^0} = 80$ GeV; the characters following the line style indicate the mass splittings: the first character means the mass splitting of the top squark (h represents 300 GeV and l 100 GeV), and the second character means that of chargino (h represents 410 GeV, m 210 GeV, and l 110 GeV).

function of the stop mixing angle θ_7 under the above condition in Fig. 2. As can be seen from the figure, C_{Q_i} is large enough to make an large enhancement of $d\Gamma/ds$ in a wide range of θ_7 (about from $-2\pi/5$ to $-\pi/8$).

(ii) The QCD corrections to coefficients C_i and C_{Q_i} are incorporated in the leading logarithmic approximation in our numerical computations. The one-loop mixing of Q_i with O_7 has been analyzed [13] and leads to about 5% correction to $C_7(m_b)$ when $\tan \beta = 30$. A next-to-leading order (NLO) analysis without including Q_i for $B \rightarrow X_s l^+ l^-$ has been performed, where it is stressed that a scheme independent result can only be obtained by including the leading order (LO) and NLO corrections to C_8^{eff} while retaining only the LO corrections in the remaining Wilson coefficient [14]. Because we did not include the NLO corrections, the theoretical uncertainty due to the renormalization scale μ dependence is about $\pm 20\%$ as μ is varied in the range $1/2 m_b \leq \mu \leq 2m_b$. We expected that a full NLO analysis including Q_i for $B \rightarrow X_s l^+ l^-$ will appear in the near future. As pointed out in Ref. [12], there is a SUSY high scale uncertainty and it is possible that the scale μ dependence is large enough to encompass effectively the uncertainty.

(iii) The following values of parameters have been used in the numerical calculations: $m_t = 175$ GeV, $m_c/m_b = 0.3$, $\eta \equiv \alpha_s(m_b)/\alpha_s(m_w) = 0.548$. We have estimated the uncertainties from the parameters and results are that the m_t dependence is weak and the uncertainties are about ten percent. The error from neglecting the strange quark mass m_s is of order m_s^2/m_b^2 and consequently is very small.

In summary, we have investigated the differential branching ratio and backward-forward asymmetry of lepton for $B \rightarrow X_s \mu^+ \mu^-$ in SUSYMs with large $\tan \beta$. There is a 100% enhancement of the differential branching ratio compared to SM if $\tan \beta \geq 30$ and the masses of Higgs bosons, squarks, and charginos are in the reasonable range. Because there is almost no enhancement till $\tan \beta = 50$ in a two Higgs doublet, one can make the conclusion that the first distinct signals of SUSY could come from the observation of $B \rightarrow X_s \mu^+ \mu^-$.

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