Heavy baryon production and decay

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The branching ratio $B(\Lambda_c \rightarrow pK^- \pi^+)$ normalizes the production and decay of charmed and bottom baryons. At present, this crucial branching ratio is extracted dominantly from $\overline{B} \rightarrow$ baryons analyses. This paper questions several of the underlying assumptions and predicts sizable $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ transitions, which were traditionally neglected. It predicts $B(\Lambda_c \rightarrow pK^- \pi^+)$ to be larger (0.07±0.02) than the world average. Some consequences are briefly mentioned. Several techniques to measure $B(\Lambda_c \rightarrow pK^- \pi^+)$ are outlined with existing or soon available data samples. By equating two recent CLEO results, an appendix obtains $B(D^0 \rightarrow K^- \pi^+) = 0.035 \pm 0.002$, which is somewhat smaller than the current world average. [S0556-2821(98)05319-3]

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I. MOTIVATION

Decays of heavy baryons allow novel tests of heavy quark effective theory (HQET) [1,2]. For instance, the structure of the $1/m_c$ corrections is known for the semileptonic transition $\Lambda_b \rightarrow \Lambda_c l \nu$ [3]. That structure is theoretically simpler than the much studied $\overline{B} \rightarrow D^{(*)} l \nu$ one because the light degrees of freedom of the heavy baryon are spinless and isospinless, while those of the heavy meson are not. Heavy baryon decays allow one to refine¹ the extraction of the fundamental Cabibbo-Kobayashi-Maskawa (CKM) parameters [3,5,6] and could show *CP* violating effects [6]. Detailed studies of heavy baryons are thus important.

The mode $\Lambda_c \rightarrow pK^-\pi^+$ plays a central role in those investigations, because of its sizable branching ratio and observability. Currently, most other Λ_c branching ratios are normalized with respect to $B(\Lambda_c \rightarrow pK^-\pi^+)$. The branching fractions of other weakly decaying charmed baryons (Ξ_c, Ω_c) can also be tied to $B(\Lambda_c \rightarrow pK^-\pi^+)$. The importance of the $\Lambda_c \rightarrow pK^-\pi^+$ process is not limited to the charm sector but extends to the *b* sector. Decay products of beautiful baryons will normally involve charmed baryons. Even bottom mesons decay non-negligibly into $\Lambda_c, \Xi_c, \Omega_c$ baryons.

The 1996 edition of the Particle Data Group (PDG) quotes [7] $B(\Lambda_c \rightarrow pK^-\pi^+) = 0.044 \pm 0.006$, which is dominated by $\overline{B} \rightarrow$ baryons analyses. The "traditional" interpretation of the most accurate and recent $B \rightarrow \Lambda_c X$ data [8] leads to a value of $B(\Lambda_c \rightarrow pK^-\pi^+) = 0.027 \pm 0.005$. Those "traditional" analyses have made simplifying assumptions which may not hold as discussed below. This paper obtains a significantly larger

$$B(\Lambda_c \rightarrow pK^-\pi^+) = 0.07 \pm 0.02,$$

by combining existing data with theory.²

Section II discusses the derivation of this sizably larger branching ratio. Section III reviews the traditional extraction of $B(\Lambda_c \rightarrow pK^-\pi^+)$ from $\overline{B} \rightarrow$ baryons analyses, and reviews the various employed assumptions. While the $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ transitions were neglected, a straightforward theoretical Dalitz plot analysis shows that they probably are sizable [11]. Here $N^{(\prime)}$ denotes a nucleon. This paper predicts that

$$B(\bar{B} \to D^{(*)}N\bar{N}'X) \sim \text{few\%}, \qquad (1.1)$$

and demonstrates that the assumption of neglecting $\overline{B} \rightarrow \Xi_c X, \Omega_c X$ cannot be justified. Finally, the so-called "model-independent" determination of [12,7]

$$B(\overline{B} \rightarrow \text{baryons}) = 0.068 \pm 0.006 \tag{1.2}$$

is questionable as it neglected the $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ processes. The latter part of Sec. III suggests several methods to search for and observe $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ in existing data samples. The observation would put into further doubt the conventional $\overline{B} \rightarrow$ baryons model. It would necessitate a serious rethinking of how to accurately determine absolute branching ratios of heavy baryons. The goal of Sec. IV is therefore to sketch several methods that are able to determine absolute Λ_c branching ratios from existing or soon available data samples. Some implications of the significantly larger predicted $B(\Lambda_c \rightarrow pK^-\pi^+)$ are discussed in Sec. V. Section VI concludes.

¹The model-independent determination of $|V_{cb}|$ from inclusive semileptonic $\overline{B} \rightarrow X l \nu$ transitions involves corrections dependent on $\overline{\Lambda} \equiv m_B - m_b$ [4]. While $\overline{\Lambda}$ is poorly known at present, it could be determined more accurately from the $\Lambda_b \rightarrow \Lambda_c l \nu$ process [3]. The theoretical input could thus be better controlled.

²The results of this paper were made available to the PDG last year, and influenced substantially the revision in the 1997 and 1998 PDG world-wide-web editions [9]. The PDG now cites a current world average of $B(\Lambda_c \rightarrow pK^- \pi^+)=0.050\pm 0.013$, and emphasizes that this value is model-dependent [10].

II.
$$B(\Lambda_c \rightarrow pK^-\pi^+)$$

The 1996 Particle Data Group value is [7]

$$B(\Lambda_c \to pK^-\pi^+) = 0.044 \pm 0.006.$$
 (2.1)

It is dominated by $B \rightarrow$ baryons analyses, which the next section critically reviews. The recent and more accurate CLEO result [8] would imply a much reduced

$$B(\Lambda_c \to pK^-\pi^+) = 0.027 \pm 0.005,$$
 (2.2)

if one were allowed to use the conventional $B \rightarrow$ baryons analysis.

This paper argues to use instead

$$B(\Lambda_c \to pK^-\pi^+) = 0.07 \pm 0.02,$$
 (2.3)

which is obtained from [13]

$$B(\Lambda_c \to pK^- \pi^+) = \frac{B(\Lambda_c \to pK^- \pi^+)}{B(\Lambda_c \to \Lambda X l\nu)} \frac{B(\Lambda_c \to \Lambda X l\nu)}{B(\Lambda_c \to X_s l\nu)} \frac{\Gamma(\Lambda_c \to X_s l\nu)}{\Gamma(D^0 \to X_s l\nu)} \frac{B(D^0 \to X l\nu)}{\left(1 + \left|\frac{V_{cd}}{V_{cs}}\right|^2\right)} \frac{\tau(\Lambda_c)}{\tau(D^0)}.$$
(2.4)

The various factors will be discussed in turn. Experiment informs us about [13]

$$\frac{B(\Lambda_c \to pK^-\pi^+)}{B(\Lambda_c \to \Lambda X l \nu)} = 1.93 \pm 0.10 \pm 0.33.$$

Because both the initial state Λ_c and the $c \rightarrow sl\nu$ transition have zero isospin, the resulting final states are isospinless. Isospin symmetry gives

$$\Gamma(\Lambda_c \to n\bar{K}^0 l\nu) = \Gamma(\Lambda_c \to pK^- l\nu),$$

$$\Gamma(\Lambda_c \to \Sigma^+ \pi^- l\nu) = \Gamma(\Lambda_c \to \Sigma^- \pi^+ l\nu)$$

$$= \Gamma(\Lambda_c \to \Sigma^0 [\to \Lambda X] \pi^0 l\nu),$$

and once applied to the ratio $f \equiv B(\Lambda_c \rightarrow \Lambda X l \nu) / B(\Lambda_c \rightarrow X_s l \nu)$ yields

$$f = 1 \left/ \left(1 + 2 \frac{\Gamma(\Lambda_c \to \Sigma^+ \pi^- l\nu)}{\Gamma(\Lambda_c \to \Lambda X l\nu)} + 2 \frac{\Gamma(\Lambda_c \to p K^- l\nu)}{\Gamma(\Lambda_c \to \Lambda X l\nu)} \right).$$
(2.5)

The underlying expectation is that the Cabibbo-allowed semileptonic transition $\Lambda_c \rightarrow X_s l \nu$ consists almost entirely of $\Lambda X l \nu$, $\Sigma \pi l \nu$, and $N \overline{K} l \nu$. Further, the exclusive $\Lambda_c \rightarrow \Lambda l \nu$ transition is predicted to dominate (almost saturate) Λ_c $\rightarrow X_s l \nu$, in analogy to what has been observed in $D \rightarrow X_s l \nu$ processes. Cabibbo-allowed semileptonic D decays are basically saturated by the exclusive $\overline{K} l \nu$ and $\overline{K}^* l \nu$ modes and no evidence for resonant $\overline{K}^{**} l \nu$ or non-resonant $\overline{K} n \pi l \nu$ ($n \ge 1$) activity has been found [16]. Because the $\overline{K}^{(*)}$ analogue in the baryon sector is the Λ hyperon, the observed Ddecay pattern indicates a value close to 1 for f. Theoretical studies of invariant hadronic mass spectra in $\Lambda_c \rightarrow X_s l \nu$ transitions come to the same conclusion [14]. We thus estimate $f=0.9\pm0.1$. Fortunately, f can be determined experimentally in the future via the right-hand side of Eq. (2.5).

The ratio $r \equiv \Gamma(\Lambda_c \rightarrow X_s l \nu) / \Gamma(D^0 \rightarrow X_s l \nu)$ has been estimated [15]

$r = 1.3 \pm 0.2$.

The prediction for r to be larger than 1 follows from the operator-product-expansion formalism. The inclusive semileptonic Λ_c and D^0 decay rates involve the same leading terms, but differ in the $\mathcal{O}(1/m_c^2)$ corrections [15]. The most significant difference occurs in the average value of the spin energy. That value vanishes for the Λ_c , while it decreases $\Gamma(D \rightarrow X_s l \nu)$. That explains why r is expected to be larger than 1.

CLEO [16] gives the most precise $B(D^0 \rightarrow Xe\nu) = 0.0664 \pm 0.0018 \pm 0.0029$ measurement to date and the lifetime ratio is taken from the PDG [7]. Equation (2.4) expresses the branching ratio of $\Lambda_c \rightarrow pK^-\pi^+$ in terms of Cabibbo favored transitions, because the $c \rightarrow d$ transitions of Λ_c suffer from large Pauli interference enhancements [17] that are difficult to quantify. Those enhancements are absent for the semi-leptonic D^0 decays. While phase-space effects for the dominant exclusive transitions will change the ratio

$$\Gamma(D^0 \rightarrow X_d l \nu) / \Gamma(D^0 \rightarrow X_s l \nu)$$

away from the naive estimate $|V_{cd}/V_{cs}|^2$, the expected change will have negligible effect on the determination for $B(\Lambda_c \rightarrow pK^-\pi^+)$ with present accuracy. Equation (2.3) is obtained by combining the above.

III. BARYON PRODUCTION IN B DECAYS

Because the dominant extractions of $B(\Lambda_c \rightarrow pK^-\pi^+)$ [7,8] involve $\overline{B} \rightarrow$ baryons analyses, it is worthwhile to review the various traditional assumptions made [18,12]. At the present level of accuracy, it is safe to neglect the $b \rightarrow u$ baryon producing transitions to obtain (see Fig. 1)

$$B(\overline{B} \rightarrow \text{baryons}) = B(\overline{B} \rightarrow N_c X) + B(\overline{B} \rightarrow D^{(*)} N \overline{N}' X).$$
(3.1)

Here N_c denotes any weakly decaying charmed baryon $(\Lambda_c, \Xi_c, \Omega_c)$, D denotes charmed mesons and $N^{(\prime)}$ stands for a nucleon. The $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ processes were tradition-



FIG. 1. Graph depicting baryon production in \overline{B} decays.

ally neglected, because of arguments based on phase space suppression [18,12]. One assumed that

$$B(\overline{B} \rightarrow \text{baryons}) = B(\overline{B} \rightarrow N_c X).$$
 (3.2)

Since at the time neither Ξ_c nor Ω_c production in \overline{B} decays were observed, they were neglected. One thus obtained

$$B(\bar{B} \rightarrow \text{baryons}) = B(\bar{B} \rightarrow \Lambda_c X).$$
 (3.3)

This report distinguishes flavor-specific branching fractions- $B(\overline{B} \rightarrow TX)$ and $B(\overline{B} \rightarrow \overline{T}X)$ -from the flavor-blind yield per *B* decay

$$Y_T \equiv B(\bar{B} \to TX) + B(\bar{B} \to \bar{T}X), \qquad (3.4)$$

where \overline{B} represents a weighted average of B^- and \overline{B}^0 . From flavor-specific and flavor-blind light baryon production in Bmeson decays $[B \rightarrow p, p\overline{p}, \Lambda, \Lambda \overline{p}, \Lambda \overline{\Lambda}]$, one deduced that [12]

$$B(\bar{B} \to \text{baryons}) = 0.068 \pm 0.006.$$
 (3.5)

The $B(\overline{B} \to \Lambda_c X)B(\Lambda_c \to pK^-\pi^+)$ measurement was then used to obtain $B(\Lambda_c \to pK^-\pi^+)$ by substituting $B(\overline{B} \to \Lambda_c X)$ by the "measured" $B(\overline{B} \to baryons)$ [Eq. (3.5)]. The most accurate measurement to date is [8]

$$Y_{\Lambda_c} \times B(\Lambda_c \to pK^-\pi^+) = (1.81 \pm 0.22 \pm 0.24) \times 10^{-3},$$
(3.6)

from which Eq. (2.2) is obtained. That summarizes the traditional understanding of baryon production in *B* meson decays and the conventional determination of $B(\Lambda_c \rightarrow pK^-\pi^+)$.

A. Critique

In contrast, our picture of baryon yields in *B* meson decays is more involved, and $B(\Lambda_c \rightarrow pK^-\pi^+)$ is significantly larger than currently believed. First, are the $\overline{B} \rightarrow D^{(*)}N\overline{N'}X$ transitions really negligible? A straightforward theoretical Dalitz plot analysis of the quark subprocess indicates that they probably are sizable. Simple accounting of the various baryon yields leads independently to the same conclusion. Thus, the traditional assumption [Eq. (3.2)] is probably not justified. Second, is it permissible to neglect Ξ_c , Ω_c production in \overline{B} meson decays [Eq. (3.3)]? Clearly not, since \overline{B}



FIG. 2. Graph responsible for the two-body \overline{B} -modes, $\overline{B} \rightarrow \{\Lambda_c, \Sigma_c\}\{\overline{p}, \overline{\Delta}\}.$

 $\rightarrow \Xi_c$ has been observed [22–24], and $B(\bar{B} \rightarrow \Xi_c X, \Omega_c X)$ has been predicted [11] to be a sizable fraction with respect to $B(\bar{B} \rightarrow \Lambda_c X)$.

Third, the inclusive $B(\overline{B} \rightarrow \text{baryons})$ determination [Eq. (3.5)] assumed Eq. (3.2). Because that assumption is probably not justified, the result [Eq. (3.5)] inferred from flavor-specific light baryon yields is questionable. Instead of the traditional extraction of $B(\Lambda_c \rightarrow pK^-\pi^+)$, the measurement [Eq. (3.6)] is used to determine the flavor-blind Λ_c yield in *B* decays:

$$Y_{\Lambda_c} = (0.026 \pm 0.005) \ \frac{0.07}{B(\Lambda_c \to pK^- \pi^+)}. \tag{3.7}$$

Only about 2.6% of all \overline{B} decays are seen in modes involving $\stackrel{(-)}{\Lambda}_c$, in contrast to conventional belief [12,18,7,19]. Before constructing a consistent view of baryon production in *B* decays, two apparently puzzling observations are reviewed:

(a) The momentum spectrum of produced Λ_c in \overline{B} decays is very soft [8].

(b) The two-body modes $\overline{B} \rightarrow \{\Lambda_c, \Sigma_c\}\{\overline{p}, \overline{\Delta}\}\)$, shown in Fig. 2, have not been observed. Only tight upper limits at the 10^{-3} level exist [7,20].

B. Previous attempt to solve the puzzles

To resolve these puzzles it was hypothesized that baryon production in *B* decays is governed by the $b \rightarrow c \bar{c} s$ transition (see Fig. 3) [21]. The $\bar{\Lambda}_c$ momentum spectrum is soft because the $\bar{\Lambda}_c$'s are produced in association with the heavy $\Xi_c^{(r)}$, where superscript "r" denotes resonance. The twobody modes $\bar{B} \rightarrow \{\Lambda_c, \Sigma_c\}\{\bar{p}, \bar{\Delta}\}$ are naturally absent. Further, this mechanism gives rise to "wrong-sign" $b \rightarrow \bar{\Lambda}_c$ transitions in contrast to the conventional "right-sign" $b \rightarrow \Lambda_c$ processes. Finally, it followed that Ξ_c production in \bar{B} decays is large and not negligible as commonly assumed.

Subsequently, CLEO found evidence for a large Ξ_c yield [23,22]



FIG. 3. Graph governing $\overline{B} \rightarrow \Xi_c^{(r)} \overline{\Lambda}_c X$ transitions.

$$Y_{\Xi} = 0.039 \pm 0.015. \tag{3.8}$$

That same analysis measured the "wrong-sign" to "rightsign" Λ_c production in *B* meson decays to be small [22]

$$r_{\Lambda_c} = \frac{B(\bar{B} \to \bar{\Lambda}_c X)}{B(\bar{B} \to \Lambda_c X)} = 0.20 \pm 0.14.$$
(3.9)

This result indicated that the $\overline{B} \rightarrow \Xi_c^{(r)} \overline{\Lambda}_c X$ processes are not dominant, and refuted the hypothesis that baryon production in *B* decays is dominated by the $b \rightarrow c \overline{c} s$ transition.

The flavor-specific Ξ_c and Ω_c production in *B* meson decays can be correlated to the much more accurately measured flavor-specific Λ_c yields [11]. For a full list of predictions, please consult Ref. [11]. One prediction is that

$$\frac{Y_{\Xi_c}}{Y_{\Lambda_c}} = 0.38 \pm 0.10, \tag{3.10}$$

and once combined with Eq. (3.7) predicts that

$$Y_{\Xi_c} = (0.010 \pm 0.003) \frac{0.07}{B(\Lambda_c \to pK^- \pi^+)} = 0.010 \pm 0.004.$$

The much larger central value quoted by CLEO (3.8) indicates that the absolute branching ratio scale of Ξ_c decays is in truth much larger than assumed. Theoretical support can be obtained from a recent paper of Voloshin [17]. Because of the above reasons, the CLEO collaboration now cites [24]

$$Y_{\Xi} = 0.020 \pm 0.010.$$

There remains little doubt that Ξ_c production is sizable in \overline{B} decays. Thus the determination of $B(\Lambda_c \rightarrow pK^-\pi^+)$ from previous $\overline{B} \rightarrow$ baryons analyses is questionable.

C. Towards a consistent view of baryon production in *B* decays

Puzzles (a) and (b) can be explained by noting that a straightforward Dalitz plot for the dominant $b \rightarrow c \bar{u} d$ transition predicts the cd invariant mass to be very large [11]. (The predicted invariant cd mass distribution follows from the V-A nature of the $b \rightarrow c \bar{u} d$ process.) If the cd forms a charmed baryon (Fig. 1), then in general this baryon will be significantly more massive than a Λ_c or Σ_c , which explains puzzle (b). Further, such very massive cdq objects or highly excited charmed baryon resonances would be seen usually as $\Lambda_c n \pi$ ($n \ge 1$). That explains naturally the observed soft Λ_c momentum spectrum [puzzle (a)].

Analogously the invariant cs mass in $b \rightarrow csc$ transitions is predicted to be very high. The Ξ_c^r produced in \overline{B} $\rightarrow \Xi_c^{(r)} \overline{\Lambda}_c X$ processes could be seen significantly as $\Lambda_c \overline{K} X [\Lambda D X]$ which would lead to $\overline{B} \rightarrow \Lambda_c \overline{\Lambda}_c \overline{K} X [\Lambda D \overline{\Lambda}_c X]$ transitions. Such transitions could comprise a non-negligible fraction of the inclusive Λ_c production in \overline{B} decays and



FIG. 4. Baryon production in \overline{B} decays, wherein the virtual W hadronizes into a baryon-antibaryon pair.

could show up as $\Lambda_c \overline{\Lambda}$ correlations in single *B* decays.³

While the theoretical Dalitz plot argument predicts the initially produced charmed baryons (via $b \rightarrow c$) to be highly excited, this is not expected of their pair produced antibaryons (via $b \rightarrow \overline{u}$ or $b \rightarrow \overline{c}$). The V-A nature of the interaction favors smaller energies for the \overline{u} or \overline{c} antiquark in the rest-frame of the decaying b. Since the spectator antiquark \overline{q}_s of the $\overline{B}(\equiv b\overline{q}_s)$ meson involves only a modest Fermi momentum, the invariant mass of the $\overline{u}\overline{q}_s$ or $\overline{c}\overline{q}_s$ system is also expected to be modest.

The very massive cdq produced in $b \rightarrow cd\bar{u}$ transitions could be seen sizably as $D^{(*)}NX$. The \bar{B} meson could be seen therefore in $\bar{B} \rightarrow D^{(*)}N\bar{N}'X$ processes, in contrast to prevailing belief. Figure 4 shows another $\bar{B} \rightarrow D^{(*)}N\bar{N}'X$ amplitude where the virtual $W^- \rightarrow \bar{u}d$ hadronizes into a light baryon antibaryon pair.⁴ Sizable $\bar{B} \rightarrow D^{(*)}N\bar{N}'X$ processes would invalidate the assumption that baryon production involves, in general, weakly-decaying charmed baryons (3.2). The current determinations of $B(\Lambda_c \rightarrow pK^-\pi^+)$ from \bar{B} \rightarrow baryons analyses would have to be modified.

Another reason why the $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ processes were neglected is the tight upper limit [18]

$$B(\bar{B} \rightarrow D^{*+} p \bar{p} X) < 0.4\%.$$
(3.11)

Our scenario survives, however, because of flavor correlations [11]. Consider the very massive cdq object. It could be seen as a $D^{(*)+}$, which would normally not be produced in association with a p, because

$$cdq \rightarrow (c\overline{d})(ddq) = D^{(*)+}\{n, \Delta^{0,-}, \ldots\}$$

If a *p* is required in the final state, it is more readily correlated with a $D^{(*)0}$ from cdq decays. The virtual $W^- \rightarrow \bar{u}d$ normally hadronizes as $\bar{u}d \rightarrow \bar{p}n, \ldots$ and may thus survive the constraint of Eq. (3.11). This paper predicts that

$$B(\overline{B} \to D^{(*)}N\overline{N}'X) \sim \text{few\%}, \qquad (3.12)$$

³If $\Lambda_c \overline{\Lambda}_c$ production in *B* decays turns out to be sizable, then the statement of Ref. [18] that their $B(\Lambda_c \rightarrow pK^- \pi^+)$ measurement should be considered strictly as a lower limit has to be modified.

⁴The size of this amplitude can be estimated from baryon production measurements at e^+e^- colliders at c.m. energies \sqrt{s} that satisfy $2m_p < \sqrt{s} < m_B - m_D$.

from $B(\overline{B} \rightarrow D^{(*)}N\overline{N'}X) = B(\overline{B} \rightarrow \text{baryons}) - B(\overline{B} \rightarrow N_cX)$. First we discuss what can be inferred about inclusive baryon production in *B* decays, and then we determine $B(\overline{B} \rightarrow N_cX)$ [11]. Prediction (3.12) follows.

D. $B(\overline{B} \rightarrow \text{baryons})$

The "accepted" value [7,12],

$$B(\bar{B} \to \text{baryons}) = 0.068 \pm 0.006,$$
 (3.13)

is obtained from flavor-specific, light baryon yields,

$$\overset{(\sim)}{B} \rightarrow p, p\bar{p}, \Lambda, p\bar{\Lambda}, \Lambda\bar{\Lambda},$$
 (3.14)

under the assumption that baryon production always involves an N_c [Eq. (3.2)]. The assumption probably does not hold, raising the question about the accurate value for $B(\bar{B} \rightarrow baryons)$. Model-independent lower limits can be derived from the light baryon measurements⁵

$$B(B \to \text{baryons}) \\ \ge \operatorname{Max} \left\{ \frac{Y_p}{2}, \frac{Y_{\text{direct } p} + Y_{\Lambda}}{2}, Y_p - B(\overline{B} \to p\overline{p}X) \right\} \\ = \operatorname{Max} \{ 0.040 \pm 0.002, \ 0.0475 \\ \pm 0.0035, \ 0.055 \pm 0.005 \}.$$
(3.15)

Here the flavor-blind yield is defined in Eq. (3.4), and the values summarized in Ref. [7] were used.

Isospin arguments [25] could be used to determine $B(\overline{B} \rightarrow baryons)$. Consider the dominant baryon producing transition $b \rightarrow c \overline{u} d$. The $\overline{B} \rightarrow N$ transition can proceed in several ways, some of which violate isospin even after the weak decay of the \overline{B} (such as the $\overline{B} \rightarrow N_c \rightarrow N$ cascades). Thus, we focus instead on the light antibaryon yield in \overline{B} meson decays, $\overline{B} \rightarrow \overline{N}'$. Because this \overline{N}' "contains" the \overline{u} from the $b \rightarrow c \overline{u} d$ transition and the other antiquarks forming the \overline{N}' are as likely to be a \overline{d} as a \overline{u} , we expect more \overline{p} than \overline{n} production. Suppose that the ratio of $\overline{p}/\overline{n}$ production falls within the range

$$1 < \frac{B(\bar{B} \to \bar{p}X)}{B(\bar{B} \to \bar{n}X)} < 3.$$
(3.16)

That range combined with the measurement of [12]

$$B(\bar{B} \to \bar{p}X) = 0.048 \pm 0.004$$
, yields (3.17)

$$0.097 \pm 0.009 > B(\bar{B} \rightarrow \text{baryons}) > 0.065 \pm 0.006.$$
 (3.18)

In summary, the inclusive baryon yield is in excess of 0.05 [Eq. (3.15)], and probably somewhere in the 0.06–0.10 range. Studies of neutron yields in *B* decays offer one model-independent way to determine $B(\overline{B} \rightarrow \text{baryons})$.

E. N_c production in \overline{B} decays

Once the value of $B(\overline{B} \rightarrow N_c X)$ is established, the $\overline{B} \rightarrow D^{(*)}N\overline{N'}X$ fraction can be determined. The $B(\overline{B} \rightarrow N_c X)$ is determined in two steps:

$$B(\overline{B} \to N_c X) = B(\overline{B} \to \Lambda_c X) + [B(\overline{B} \to \Xi_c X) + B(\overline{B} \to \Omega_c X)].$$
(3.19)

The flavor-specific $B(\overline{B} \to \Lambda_c X)$ is taken from experiment [8,22], whereas $B(\overline{B} \to \Xi_c X)$ and $B(\overline{B} \to \Omega_c X)$ are correlated⁶ to the observed Λ_c yields [11] and therefore are predictions dependent on $B(\Lambda_c \to pK^-\pi^+)$,

$$B(\bar{B} \to N_c X) = (0.032 \pm 0.006) \frac{0.07}{B(\Lambda_c \to p K^- \pi^+)}$$

= 0.032 \pm 0.011. (3.20)

The last equation follows by inserting 0.07 ± 0.02 for $B(\Lambda_c \rightarrow pK^-\pi^+)$. Since the inclusive baryon yield is at the 0.06–0.1 level and $B(\bar{B} \rightarrow N_c X)$ is given by Eq. (3.20), we predict that probably

$$B(\overline{B} \to D^{(*)}N\overline{N}'X) \sim \text{few\%}.$$
(3.21)

Our prediction gets additional support from the theoretical Dalitz plot argument outlined above [11]. Table I summarizes this section. The existing data samples are sufficiently large to search for and observe sizable $\bar{B} \rightarrow D^{(*)}N\bar{N}'X$ processes.

F. $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$ search

Here we list a few suggestions to search for $\overline{B} \rightarrow D^{(*)}N\overline{N}'X$. At the Y(4S) one could look for non-trivial angular correlations between a $D^{(*)}$ and a light baryon or antibaryon N. If the $D^{(*)}$ comes from one \overline{B} and the N from the other B, then they should be distributed almost isotropically [26]. On the other hand, observing a nontrivial angular correlation would indicate single \overline{B} parentage. It is likely, however, that either the $D^{(*)}$ or the N or both are soft, in which case the angular correlations are largely lost. Thus we recommend to search for the triple correlation $l^+D^{(*)}N$ on the Y(4S) [11]. The l^+ and the $D^{(*)}$ cannot originate from a single B meson, because of their flavors. Either the N and the

⁵Neutron yields have not been measured yet. The lower limits are obtained by neglecting them.

⁶This paper does not use the direct Ξ_c measurement in \overline{B} decays, because of the very large uncertainties involved (see above). Instead, the uncertainties are drastically reduced by correlating the predicted Ξ_c and Ω_c yields to the better measured Λ_c yield.

Assumptions	Comments
$\overline{B(\bar{B}\to D^{(*)}N\bar{N}'X)} = 0$	Could be \sim few %. Theoretical Dalitz plot allows for
	sizable $\overline{B} \rightarrow D^{(*)} N \overline{N}' X$.
$B(\overline{B} \to \Xi_c X, \Omega_c X) = 0$	$\bar{B} \rightarrow \Xi_c X$ large
$B(\overline{B} \rightarrow \text{baryons}) = 0.068 \pm 0.006$	Value questionable, because derived under the assumption that $B(\overline{B} \rightarrow D^{(*)}N\overline{N'}X) = 0$. Instead, this paper determines <i>model-independent lower limits</i> from existing light baryon yields.

TABLE I. The conventional determination of $B(\Lambda_c \rightarrow pK^-\pi^+)$ involves $\bar{B} \rightarrow$ baryons analyses with the assumptions tabulated here.

lepton share *B* parentage or the *N* and the $D^{(*)}$ originate from the same \overline{B} . While the latter interpretation is our coveted signal, the former is very unlikely. The former interpretation would indicate semileptonic *B* decay in conjunction with baryon/antibaryon production⁷

$$B \to \bar{N}_c N' l^+ \nu, \qquad (3.22)$$

which is expected theoretically to be tiny, and for which tight upper limits already exist [7,27].

Bottom hadrons produced at Z^0 factories are boosted and hadronize generally in opposing hemispheres. After selecting a *b*-enriched event, one could search, in a single *b*-hemisphere, for the predicted few percent (detached) $D^{(*)}\overline{N}$ correlation.⁸

At either e^+e^- or hadron colliders, one may attempt to reconstruct the $\overline{B} \rightarrow D^{(*)}N\overline{N'}\pi$'s modes. The existence of a n can be inferred in analogy to methods developed for ν or K_L reconstruction. Sizable $\overline{B} \rightarrow D^{(*)}N\overline{N'}X$ processes would further question the traditional $B(\Lambda_c \rightarrow pK^-\pi^+)$ determinations. The next section outlines briefly some methods that allow the determination of $B(\Lambda_c \rightarrow pK^-\pi^+)$ from existing or soon available data samples.

IV. ON DETERMINING $B(\Lambda_c \rightarrow f)$

This section lists a few methods that allow the determination of $B(\Lambda_c \rightarrow f)$, where f denotes an exclusive $(pK^-\pi^+, \Lambda\pi, \ldots)$ or semi-inclusive $(\Lambda X, pX, \ldots)$ Λ_c -mode.

A. Method (a)

At e^+e^- or $p\bar{p}$ colliders, produce $\Lambda_c\bar{\Lambda}_c$ pairs at threshold. Fully reconstruct one of the charmed baryons. Then one determines $B(\Lambda_c \rightarrow f)$, by measuring the probability for the remaining Λ_c to be seen in f [28].

B. Method (b)

At fixed target experiments, the production asymmetry can be used to determine $B(\Lambda_c \rightarrow f)$ [29]. Since the total produced number of charm quarks equals that of anticharm quarks, one obtains

$$N(\Lambda_c) - N(\bar{\Lambda}_c) + N(\Xi_c, \Omega_c) - N(\bar{\Xi}\Xi_c, \bar{\Omega}_c)$$
$$= N(\bar{D}) - N(D) + N(\bar{D}_s) - N(D_s), \qquad (4.1)$$

where *N* denotes the total produced number. In the lack of a Ξ_c, Ω_c production asymmetry, the coveted absolute $B(\Lambda_c \rightarrow f)$ is obtained via

$$B(\Lambda_c \to f) = \frac{N(f) - N(\bar{f})}{N(\bar{D}) - N(D) + N(\bar{D}_s) - N(D_s)}.$$
 (4.2)

If a Ξ_c , Ω_c production asymmetry is observed, it can be incorporated to determine $B(\Lambda_c \rightarrow f)$.

The method looks promising, and its feasibility is being studied by the Fermilab experiments FOCUS/E831 and SELEX/E781. This approach is applicable to other fixed target experiments as well.

C. Method (c)

The probability that a leading s-quark jet hadronizes as a hyperon [$P(s \rightarrow \text{hyperon})$] can be experimentally measured. The relevant (diquark) parameters in current simulation models could then be tuned to agree with the measurements. The simulation model then predicts the probability for charmed baryon production [$P(c \rightarrow N_c)$], with uncertainties typically at the (10–20)% level. Since the charm production cross section is known, reconstructing final states of Λ_c (f) permits the extraction of $B(\Lambda_c \rightarrow f)$.

⁷A sufficiently large lepton momentum removes any background from $\overline{B} \rightarrow \Xi_c \overline{\Lambda}_c X$, where one of the charmed baryons decays semileptonically and either one contributes the *N*.

⁸The small (~0.5%) background from $\bar{\Lambda}_b \rightarrow \bar{N}_c [\rightarrow \bar{N}X] D^{(*)}KX \Rightarrow \bar{N}D^{(*)}$ processes can be significantly reduced by (a) flavortagging, which enriches *b* over \bar{b} content, (b) enhancing B^- parentage via vertex charge, which reduces the *b*-baryon background thereby making even the (detached) $D^{(*)}N$ correlations a convincing signal.

D. Method (d)

At an $\Upsilon(4S)$ factory, reconstruct a \bar{c} -hadron $[D^{(*)-}, \bar{D}^0, \bar{\Lambda}_c]$ with sufficiently high momentum from the continuum to remove the $B\bar{B} \rightarrow \bar{c}X$ background. [No momentum cut is required when the data is taken at the continuum below the $\Upsilon(4S)$ resonance.] The "opposite" hemisphere contains in general a *c*-hadron. Determine the number of events that an antiproton is made in the "opposite" hemisphere $N[\bar{c}\bar{p}]$. This \bar{p} cannot be a decay product of the *c*-hadron and indicates *c*-baryon production in the "opposite" hemisphere. The observation of Λ_c modes *f* in the "opposite" hemisphere allows the measurement of $N[\bar{c}\bar{p}f]$ and of

$$B(\Lambda_c \to f) \approx \frac{N[\bar{c}\bar{p}f]}{N[\bar{c}\bar{p}]}.$$
(4.3)

A few corrections and comments must be made before this method becomes promising.

While the existence of an "opposite" hemisphere \overline{p} indicates *c*-baryon production, one must correct for the fraction of the time the \overline{cp} -correlation occurs with *c*-meson production. That correction can be determined by measuring the *c*-meson yield in the "opposite" hemisphere, $N[\overline{cp}D_{(s)}]$. The probability that \overline{cp} opposite hemisphere events contain *c*-baryons can thus be determined and is given by 1 $-N[\overline{cp}D_{(s)}]/N[\overline{cp}]$. While the dominant fraction is Λ_c 's, one may wish to correct for the much smaller Ξ_c , Ω_c yields.⁹

It appears that this method may not yet be feasible, because of the poor statistics for the various triple correlations $[\bar{c}\bar{p}f,\bar{c}\bar{p}D_{(s)},\bar{c}\bar{p}\{\Xi_c,\Omega_c\}]$. It is thus important to note that much larger statistics are involved in "single" hemisphere $\bar{p}f,\bar{p}D_{(s)},\bar{p}\{\Xi_c,\Omega_c\}$ events. The existence of a \bar{c} -hadron (normally) in the other hemisphere can be inferred from the reconstructed *c*-hadron [31]. Thus, the poor statistics of the triple correlations can be avoided, and $B(\Lambda_c \rightarrow f)$ can be measured [31].¹⁰

E. Method (e)

This method requires a superb vertex detector. After selecting a *b*-sample, the sample of fragmentation \overline{p} 's, which originate from the interaction point and are close to the *b*-jet, indicate *b*-baryon production. (Below we discuss how to correct for *b*-meson production in association with such \overline{p} 's.) Observe also negative leptons l^- with high p_T and significant impact parameter, which normally are primary decay products of *b*-decays. The produced number of such $\bar{p}l^-$ correlations $N[\bar{p}l^-]$ is proportional to

$$N[\bar{p}l^{-}] \sim P(\ldots \to \bar{p}) P(b \to \Lambda_{b})$$
$$\times B(\Lambda_{b} \to \Lambda_{c} X l \nu), \qquad (4.4)$$

where we assumed that semileptonic Λ_b decays are almost always accompanied by a Λ_c , apart from tiny Λ_b $\rightarrow \{\Xi_c K X, D^{(*)} N X, \ldots\} l \nu$ and $b \rightarrow u$ processes. The tiny processes are at most at the 10% level of inclusive semileptonic Λ_b decays, as can be inferred from an analogy to semileptonic \overline{B} -decay measurements [32,33]. Ratios of specific Λ_c decay rates can thus be determined

$$\frac{\Gamma(\Lambda_c \to f')}{\Gamma(\Lambda_c \to f)} = \frac{N[\bar{p}l^- f']}{N[\bar{p}l^- f]},$$
(4.5)

where $f, f' = pK\pi, \Lambda n\pi, \Lambda X, pX, \ldots$. Information concerning semi-inclusive Λ_c decay rates can thus be obtained. Even absolute Λ_c branching ratios can be determined via

$$B(\Lambda_c \to f) \approx \frac{N[pl^-f]}{N[\bar{p}l^-]}.$$
(4.6)

One must correct for the fraction of the time the *b*-jet nearby the fragmentation \overline{p} gives rise to a *b*-meson (rather than a *b*-baryon). The correction factor can be obtained in several ways:

- (1) Measure the probability that $\overline{p}l^-$ events involve (detached) charmed mesons, which together with the $l^$ point to the *b*-decay vertex.
- (2) Select a charged B^- sample by using vertex charge and vertex mass. Study the fraction of the time this B^- sample involves a nearby fragmentation $p^{(-)}$.
- (3) In the *b*-enriched sample with one fragmentation p, observe an additional fragmentation p also from the interaction point and nearby the *b*-jet. Since baryon number is conserved, it is likely a *b*-meson was produced. (The possibility of more than one nearby baryon-antibaryon pair production may not be negligible, however.) Because isospin symmetry allows one to determine the production ratio of fragmentation neutrons versus protons, the fraction of the time *b*-mesons are made can be inferred.

It may prove useful to introduce stringent cuts on the fragmentation \overline{p} , so as to reduce the *b*-meson fraction.

F. Method (f)

If it were possible to theoretically relate $\Gamma(\Lambda_b \rightarrow \Lambda J/\psi)$ to $\Gamma(\bar{B} \rightarrow \bar{K}^{(*)}J/\psi)$ then the observed $\Lambda J/\psi$ sample of fully

⁹The Ξ_c and Ω_c yields can be measured. Rates of specific Ξ_c and Ω_c modes are related to specific Λ_c -modes by the SU(3)-flavor symmetry [30]. The rates of those specific modes are normally measured well with respect to the calibrating modes. Thus, the fraction of Λ_c , Ξ_c , Ω_c in \overline{cp} events can be determined.

¹⁰This $B(\Lambda_c \rightarrow f)$ measurement neglects long range $c\bar{c}$ production correlations, which are expected to be small. They can be accounted for in triple correlation studies.

reconstructed Λ_b decays permits the determination of $P(b \rightarrow \Lambda_b)$. Once $P(b \rightarrow \Lambda_b)$ is known, then the $\Lambda_c[\rightarrow f]l^-$ sample yields $B(\Lambda_c \rightarrow f)$.

G. Conclusion

Those are then some suggestions to determine $B(\Lambda_c \rightarrow f)$. Undoubtedly, many possible variations and improvements will become obvious to the dedicated experimenter. Appendix A sketches a determination of $B(\Lambda_b \rightarrow X l \nu)$ and $|V_{cb}|$ with a reduced dependence on $B(\Lambda_c \rightarrow f)$.

V. IMPLICATIONS

If $B(\Lambda_c \rightarrow pK^-\pi^+)$ turns out to be larger than the current world average, as we predict, then there will be many ramifications. Some of them are:

Since $B(\Lambda_c \rightarrow pK^-\pi^+)$ normalizes most heavy baryon productions and decays, the heavy baryon decay tables listed in Ref. [7] will have to be recalibrated accordingly.

The $\Lambda_b: \overline{B}: \overline{B}_s$ production fractions will be affected. The Λ_b fraction will be reduced sizably from current estimates while the \overline{B} and \overline{B}_s fractions will increase. The measured Λ_b branching ratios thus increase sizably, while the $B_{(s)}$ ones decrease.

The number of charms per *b*-decay decreases on two counts. First, the Ξ_c yield in \overline{B} decays is predicted to be sizably lower than its measured central value. Second, the $B(\Lambda_c \rightarrow pK^-\pi^+)$ is larger than expected, resulting into a lower Λ_c yield in *b* decays than presently believed. Quantitative estimates can be found in Refs. [11,34].

The charmless yield in *B*-meson decays is larger than a recent indirect extraction [19]. CLEO [19] measured the flavor-specific charm yields in *B* decays in a way that removes the large systematic uncertainty¹¹ due to $B(D^0 \rightarrow K^- \pi^+)$. That beautiful analysis then assumed that the inclusive baryon yield in \overline{B} decays is saturated by weakly decaying charmed baryon production (N_c) , resulting in $B(b \rightarrow \text{no open } c) = 0.04 \pm 0.04$. In contrast, this note questions the validity of the assumption and uses $B(\overline{B} \rightarrow N_c X) = 0.032 \pm 0.011$, which implies a larger $B(b \rightarrow \text{no open } c) = 0.07 \pm 0.04$. Table II summarizes both viewpoints.

Those are then some of the consequences of our view of heavy baryon production and decay.

TABLE II. Open charm production in \overline{B} decays. The last row lists the charmless yield which is obtained via $B(b \rightarrow \text{no open } c) = 1 - B(b \rightarrow \text{open } c)$.

$\overline{B}[\equiv b\overline{q}] \rightarrow \text{open } c$	CLEO [19] (This paper)
$ar{B}{ ightarrow}D^0, D^+$	0.87 ± 0.04
$\bar{B} \rightarrow D_s^+$	0.02 ± 0.01
$\bar{B} \rightarrow N_c [\equiv \Lambda_c, \Xi_c, \Omega_c]$	$0.065 \pm 0.015 \ (0.032 \pm 0.011)$
$\overline{B} \rightarrow$ no open c	$0.04 \pm 0.04 \ (0.07 \pm 0.04)$

VI. CONCLUSIONS

Because the $\Lambda_c \rightarrow pK^-\pi^+$ process normalizes heavy baryon production and decay, its absolute branching ratio must be known to the highest accuracy achievable. Analyses of baryon production in *B* meson decays dominate the traditional $B(\Lambda_c \rightarrow pK^-\pi^+)$ "measurements,"

$$B(\Lambda_c \to pK^-\pi^+) = \begin{cases} 0.044 \pm 0.006 \ [7],\\ 0.027 \pm 0.005 \ [8]. \end{cases}$$
(6.1)

Those analyses however made several questionable assumptions, summarized in Table I. Instead, a considerably larger $B(\Lambda_c \rightarrow pK^-\pi^+)$ emerges [13,11,35],

$$B(\Lambda_c \rightarrow pK^-\pi^+) = 0.07 \pm 0.02,$$

by combining theory and available experimental data on semileptonic charm transitions.

This confusing state of affairs can be clarified by searching for and observing the traditionally overlooked \overline{B} $\rightarrow D^{(*)}N\overline{N}'X$ processes. We predict those $\overline{B}\rightarrow D^{(*)}N\overline{N}'X$ processes to constitute a sizable fraction of all $\overline{B}\rightarrow$ baryons transitions. They should be observable in existing data samples. If this is borne out, then $B(\Lambda_c \rightarrow pK^-\pi^+)$ must be determined afresh. That can be accomplished in a variety of methods, some of which Sec. IV briefly outlined. A considerably larger $B(\Lambda_c \rightarrow pK^-\pi^+)$ than currently accepted will have ramifications, such as:

The heavy baryon decay tables will have to be recalibrated.

The $b \rightarrow \Lambda_b$ production fraction decreases.

The measured number of charm per *b*-decay decreases.

The \overline{B} \rightarrow baryons transitions are more involved than currently modeled.

More theoretical and experimental investigations are highly welcome, as it will improve our understanding of heavy baryon production and decay.

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¹¹That study enables Appendix B to point out a complementary method for determining $B(D^0 \rightarrow K^- \pi^+)$, which does not involve the soft pion from $D^{*+} \rightarrow \pi^+ D^0$ transitions. The result is $B(D^0 \rightarrow K^- \pi^+) = 0.035 \pm 0.002$, by equating two CLEO measurements for Y_D .

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APPENDIX A: ON DETERMINING $B(\Lambda_b \rightarrow X l \nu)$ AND $|V_{cb}|$ WITH A REDUCED $B(\Lambda_c \rightarrow f)$ UNCERTAINTY

At present there exists a discrepancy between theory and experiment concerning the lifetime ratio $\tau(\Lambda_b)/\tau(B_d)$ [7]. The most plausible explanation is an enhanced nonleptonic Λ_b rate, without a corresponding enhancement in the semileptonic Λ_b rate. This Appendix discusses one way to determine the semileptonic Λ_b rate and branching ratio, thereby probing the underlying cause of the lifetime discrepancy. Building on the discussion presented in method (e) of Sec. IV, one notes that the produced number of l^-f events is proportional to

$$N[l^{-}f] \sim P(\ldots \rightarrow b)P(b \rightarrow \Lambda_{b})$$
$$\times B(\Lambda_{b} \rightarrow \Lambda_{c}Xl\nu)B(\Lambda_{c} \rightarrow f), \qquad (A1)$$

where it is understood that the various backgrounds have been corrected for. In addition, the direct production of Λ_c baryons can be studied as well. To remove the large $b \rightarrow \Lambda_c$ background, it may prove advantageous to focus on the high momentum $\Lambda_c \rightarrow f$ sample,

$$N[f] \sim P(\ldots \to c) P(c \to \Lambda_c) B(\Lambda_c \to f).$$
 (A2)

The production ratio $P(\ldots \rightarrow b)/P(\ldots \rightarrow c)$ is well known, and HQET can in principle determine the ratio¹²

$$\frac{P(b \to \Lambda_b)}{P(c \to \Lambda_c)} = 1 + \mathcal{O}(1/m_Q).$$
(A3)

The semileptonic Λ_b -branching ratio can thus be determined

$$B(\Lambda_b \to X l\nu) \approx B(\Lambda_b \to \Lambda_c X l\nu) \sim \frac{N[l^- f]}{N[f]}.$$
 (A4)

Even the CKM parameter $|V_{cb}|$ can be extracted by measuring the *exclusive* $\Lambda_b \rightarrow \Lambda_c l\nu$ branching ratio, $B(\Lambda_b \rightarrow \Lambda_c l\nu)$. That measurement combined with $\tau(\Lambda_b)$ determines $\Gamma(\Lambda_b \rightarrow \Lambda_c l\nu)$. HQET [3,2] and lattice studies [36] inform on the relevant form factors, so that $|V_{cb}|$ can be determined from that $\Lambda_b \rightarrow \Lambda_c l\nu$ measurement.

APPENDIX B: ON THE $B(D^0 \rightarrow K^- \pi^+)$ VALUE

Not only does $B(D^0 \rightarrow K^- \pi^+)$ calibrate most other D^0 decays, but the D^+ and D_s^+ calibration modes $[D^+]$

 $\rightarrow K^- \pi^+ \pi^+$ and $D_s^+ \rightarrow \phi \pi^+$] are tied to it as well [7]. The $D^0 \rightarrow K^- \pi^+$ process normalizes charmed meson production and decay, in analogy to the role of the $\Lambda_c \rightarrow p K^- \pi^+$ transition for charmed baryon studies. This Appendix introduces one more method for determining $B(D^0 \rightarrow K^- \pi^+)$, which yields

$$B(D^0 \to K^- \pi^+) = 0.035 \pm 0.002.$$
 (B1)

There exist now two CLEO measurements of D production in flavor-blind B decays,

$$Y_D \equiv B(\bar{B} \to DX) + B(\bar{B} \to \bar{D}X). \tag{B2}$$

The first is a high statistics measurement of inclusive *D* and \overline{D} production in *B* decays, which is inversely proportional to $B(D^0 \rightarrow K^- \pi^+)$ [24],

$$Y_D = (0.876 \pm 0.037) \left[\frac{0.0388}{B(D^0 \to K^- \pi^+)} \right].$$
(B3)

The second is not sensitive to $B(D^0 \rightarrow K^- \pi^+)$,

$$Y_D = 0.96 \pm 0.05,$$
 (B4)

and was deduced from Ref. [19] as discussed below. Equating the two and solving for $B(D^0 \rightarrow K^- \pi^+)$ yields Eq. (B1). This value agrees with the one obtained in Refs. [11,37,38], and is somewhat below the world average [39], $B(D^0 \rightarrow K^- \pi^+) = 0.0388 \pm 0.0010$.

The world average is dominated by studies involving the soft π^+ in $D^{*+} \rightarrow \pi^+ D^0$ decays, which require the accurate modeling of the tails of the soft pion momentum spectrum. Because such accurate modeling may prove more difficult than presently appreciated [38], measurements of $B(D^0 \rightarrow K^- \pi^+)$ insensitive to such soft π^+ 's should also be pursued. Such methods were discussed in the literature [11,38,19]. This appendix introduces yet another one.

Equation (B4) is obtained via

$$Y_D = D_l \times (1 + r_D) \times L. \tag{B5}$$

Here theory delivers [19]

$$L \equiv B(\overline{B} \rightarrow DXl\nu) / B(\overline{B} \rightarrow Xl\nu) = 0.97 \pm 0.02,$$

while the other quantities were measured [19]:

$$D_{l} \equiv \frac{B(\bar{B} \rightarrow DX)}{B(\bar{B} \rightarrow DX l\nu)/B(\bar{B} \rightarrow X l\nu)} = 0.901 \pm 0.037,$$
$$r_{D} \equiv B(\bar{B} \rightarrow \bar{D}X)/B(\bar{B} \rightarrow DX) = 0.100 \pm 0.031.$$

Note that several uncertainties cancel in the $D_l \times (1+r_D)$ combination [40], so that CLEO can determine $Y_D[B(D^0 \rightarrow K^- \pi^+)]$ with a smaller error than given in Eq. (B4) [Eq. (B1)].

¹²It would be useful to calculate the momentum dependence of this ratio.

- [1] N. Isgur and M. B. Wise, Nucl. Phys. B348, 276 (1991).
- [2] M. Neubert, Phys. Rep. 245, 259 (1994).
- [3] H. Georgi, B. Grinstein, and M. B. Wise, Phys. Lett. B 252, 456 (1990).
- [4] For a recent review, see for instance, I. Bigi, M. Shifman, and N. Uraltsev, Annu. Rev. Nucl. Part. Sci. 47, 591 (1997).
- [5] R. Springer (private communication).
- [6] I. Dunietz, Z. Phys. C 56, 129 (1992).
- [7] Particle Data Group, R. M. Barnett *et al.*, Phys. Rev. D 54, 1 (1996).
- [8] CLEO Collaboration, M. M. Zoeller, Ph.D. thesis, State University of New York, Albany, 1994.
- [9] P. Burchat (for the PDG) (private communication).
- [10] Particle data group www site, http://PDG.LBL.GOV.
- [11] I. Dunietz, Fermilab report, FERMILAB-PUB-96-104-T, 1996 (hep-ph/9606247).
- [12] ARGUS Collaboration, H. Albrecht *et al.*, Z. Phys. C 56, 1 (1992).
- [13] CLEO Collaboration, T. Bergfeld *et al.*, Phys. Lett. B **323**, 219 (1994).
- [14] A. Dighe and I. Dunietz (unpublished).
- [15] I. I. Bigi, N. G. Uraltsev, and A. I. Vainshtein, Phys. Lett. B 293, 430 (1992); 297, 477(E) (1993); A. V. Manohar and M. B. Wise, Phys. Rev. D 49, 1310 (1994); I. I. Bigi, UND-HEP-95-BIG02, hep-ph/9508408, 1995.
- [16] CLEO Collaboration, Y. Kubota *et al.*, Phys. Rev. D 54, 2994 (1996).
- [17] M. B. Voloshin, Phys. Lett. B 385, 369 (1996).
- [18] CLEO Collaboration, G. Crawford *et al.*, Phys. Rev. D 45, 752 (1992).
- [19] CLEO Collaboration, T. E. Coan *et al.*, Phys. Rev. Lett. **80**, 1150 (1998).
- [20] ARGUS Collaboration, M. Paulini, *Electroweak Interactions and Unified Theories*, Proceedings of the XXVIIIth Recontre de Moriond, Les Arcs, France, 1993, edited by J. Trân Thanh Vân (Editions Frontières, Gif-sur-Yvette, France, 1993), p. 253.

- [21] I. Dunietz, P. S. Cooper, A. F. Falk, and M. B. Wise, Phys. Rev. Lett. 73, 1075 (1994).
- [22] CLEO Collaboration, D. Cinabro *et al.*, Cornell report, CLEO CONF 94-8, 1994.
- [23] T. E. Browder, K. Honscheid, and D. Pedrini, Annu. Rev. Nucl. Part. Sci. 46, 395 (1996).
- [24] CLEO Collaboration, L. Gibbons *et al.*, Phys. Rev. D 56, 3783 (1997).
- [25] M. Peshkin and J. L. Rosner, Nucl. Phys. B122, 144 (1977).
- [26] CLEO Collaboration, P. L. Tipton, Ph.D. thesis, University of Rochester Report UR 984, 1987; CLEO Collaboration, M. S. Alam *et al.*, Phys. Rev. Lett. **58**, 1814 (1987).
- [27] CLEO Collaboration, G. Bonvicini *et al.*, Phys. Rev. D 57, 6604 (1998).
- [28] Mark II Collaboration, G. S. Abrams *et al.*, Phys. Rev. Lett. 44, 10 (1980).
- [29] H. W. K. Cheung (private communication).
- [30] A. Datta, I. Dunietz, and P. J. O'Donnell (in preparation).
- [31] I. Dunietz and J. L. Lewis (in preparation).
- [32] ALEPH Collaboration, D. Buskulic *et al.*, Z. Phys. C 73, 601 (1997).
- [33] N. Isgur (in progress).
- [34] I. Dunietz, J. Incandela, F. D. Snider, and H. Yamamoto, Eur. Phys. J. C1, 211 (1998).
- [35] I. Dunietz, Proceedings of the 2nd International Conference on B Physics and CP Violation, Honolulu, HI, 1997, FERMILAB-CONF-97-230-T, hep-ph/9708252.
- [36] UKQCD Collaboration, K. C. Bowler *et al.*, Phys. Rev. D 57, 6948 (1998).
- [37] I. Dunietz, J. Incandela, F. D. Snider, K. Tesima, and I. Watanabe, FERMILAB-PUB-96-026-T, hep-ph/9606327, 1996.
- [38] I. Dunietz, J. Incandela, and F. D. Snider, Nucl. Phys. B (Proc. Suppl.) 55A, 145 (1997).
- [39] J. D. Richman, in *ICHEP 96*, Proceedings of the 28th International Conference on High Energy Physics, Warsaw, Poland, 1996, edited by Z. Ajduk and A. Wroblewski (World Scientific, Singapore, 1997), hep-ex/9701014.
- [40] We thank E. Thorndike for discussions on this point.