

## Continuum charged $D^*$ spin alignment at $\sqrt{s}=10.5$ GeV

G. Brandenburg, R. A. Briere, A. Ershov, Y. S. Gao, D. Y.-J. Kim, R. Wilson, and H. Yamamoto  
*Harvard University, Cambridge, Massachusetts 02138*

T. E. Browder, Y. Li, and J. L. Rodriguez  
*University of Hawaii at Manoa, Honolulu, Hawaii 96822*

T. Bergfeld, B. I. Eisenstein, J. Ernst, G. E. Gladding, G. D. Gollin, R. M. Hans, E. Johnson, I. Karliner, M. A. Marsh,  
M. Palmer, M. Selen, and J. J. Thaler  
*University of Illinois, Urbana-Champaign, Illinois 61801*

K. W. Edwards  
*Carleton University, Ottawa, Ontario, Canada K1S 5B6  
and the Institute of Particle Physics, Canada*

A. Bellerive, R. Janicek, D. B. MacFarlane, and P. M. Patel  
*McGill University, Montréal, Québec, Canada H3A 2T8  
and the Institute of Particle Physics, Canada*

A. J. Sadoff  
*Ithaca College, Ithaca, New York 14850*

R. Ammar, P. Baringer, A. Bean, D. Besson, D. Coppage, C. Darling, R. Davis, S. Kotov, I. Kravchenko, N. Kwak,  
and L. Zhou  
*University of Kansas, Lawrence, Kansas 66045*

S. Anderson, Y. Kubota, S. J. Lee, J. J. O'Neill, R. Poling, T. Riehle, and A. Smith  
*University of Minnesota, Minneapolis, Minnesota 55455*

M. S. Alam, S. B. Athar, Z. Ling, A. H. Mahmood, S. Timm, and F. Wappler  
*State University of New York at Albany, Albany, New York 12222*

A. Anastassov, J. E. Duboscq, D. Fujino,\* K. K. Gan, T. Hart, K. Honscheid, H. Kagan, R. Kass, J. Lee, M. B. Spencer,  
M. Sung, A. Undrus,† A. Wolf, and M. M. Zoeller  
*Ohio State University, Columbus, Ohio 43210*

B. Nemati, S. J. Richichi, W. R. Ross, H. Severini, and P. Skubic  
*University of Oklahoma, Norman, Oklahoma 73019*

M. Bishai, J. Fast, J. W. Hinson, N. Menon, D. H. Miller, E. I. Shibata, I. P. J. Shipsey, and M. Yurko  
*Purdue University, West Lafayette, Indiana 47907*

S. Glenn, Y. Kwon,‡ A. L. Lyon, S. Roberts, and E. H. Thorndike  
*University of Rochester, Rochester, New York 14627*

C. P. Jessop, K. Lingel, H. Marsiske, M. L. Perl, V. Savinov, D. Ugolini, and X. Zhou  
*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94309*

T. E. Coan, V. Fadeyev, I. Korolkov, Y. Maravin, I. Narsky, V. Shelkov, J. Staeck, R. Stroynowski, I. Volobouev,  
and J. Ye  
*Southern Methodist University, Dallas, Texas 75275*

M. Artuso, F. Azfar, A. Efimov, M. Goldberg, D. He, S. Kopp, G. C. Moneti, R. Mountain, S. Schuh, T. Skwarnicki,  
S. Stone, G. Viehhauser, J. C. Wang, and X. Xing  
*Syracuse University, Syracuse, New York 13244*

J. Bartelt, S. E. Csorna, V. Jain,§ K. W. McLean, and S. Marka  
*Vanderbilt University, Nashville, Tennessee 37235*

R. Godang, K. Kinoshita, I. C. Lai, P. Pomianowski, and S. Schrenk  
*Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061*

G. Bonvicini, D. Cinabro, R. Greene, L. P. Perera, and G. J. Zhou  
*Wayne State University, Detroit, Michigan 48202*

M. Chadha, S. Chan, G. Eigen, J. S. Miller, M. Schmidtler, J. Urheim, A. J. Weinstein, and F. Würthwein  
*California Institute of Technology, Pasadena, California 91125*

D. W. Bliss, G. Masek, H. P. Paar, S. Prell, and V. Sharma  
*University of California, San Diego, La Jolla, California 92093*

D. M. Asner, J. Gronberg, T. S. Hill, D. J. Lange, R. J. Morrison, H. N. Nelson, T. K. Nelson, and D. Roberts  
*University of California, Santa Barbara, California 93106*

B. H. Behrens, W. T. Ford, A. Gritsan, J. Roy, and J. G. Smith  
*University of Colorado, Boulder, Colorado 80309-0390*

J. P. Alexander, R. Baker, C. Bebek, B. E. Berger, K. Berkelman, K. Bloom, V. Boisvert, D. G. Cassel, D. S. Crowcroft, M. Dickson, S. von Dombrowski, P. S. Drell, K. M. Ecklund, R. Ehrlich, A. D. Foland, P. Gaidarev, L. Gibbons, B. Gittelman, S. W. Gray, D. L. Hartill, B. K. Heltsley, P. I. Hopman, J. Kandaswamy, P. C. Kim, D. L. Kreinick, T. Lee, Y. Liu, N. B. Mistry, C. R. Ng, E. Nordberg, M. Ogg,<sup>||</sup> J. R. Patterson, D. Peterson, D. Riley, A. Soffer, B. Valant-Spaight, and C. Ward  
*Cornell University, Ithaca, New York 14853*

M. Athanas, P. Avery, C. D. Jones, M. Lohner, S. Patton, C. Prescott, J. Yelton, and J. Zheng  
*University of Florida, Gainesville, Florida 32611*

(CLEO Collaboration)

(Received 26 February 1998; published 29 July 1998)

A measurement of the spin alignment of charged  $D^*$  mesons produced in continuum  $e^+e^- \rightarrow c\bar{c}$  events at  $\sqrt{s} = 10.5$  GeV is presented. This study using  $4.72 \text{ fb}^{-1}$  of CLEO II data shows that there is little evidence of any  $D^*$  spin alignment. [S0556-2821(98)01317-4]

PACS number(s): 13.65.+i, 13.60.Le, 13.87.Fh

## I. INTRODUCTION

There have been numerous theoretical [1–7] and experimental [8–15] studies of the fragmentation of heavy quarks. The energy distribution and flavor dependence of heavy quark hadronization have been modeled by fragmentation functions. The role that spin plays in the hadronization process is still being investigated and is not well understood at this time [16–22]. To increase the understanding of this role, a precise measurement of the probabilities of a meson being directly produced in each of the available spin states is needed.

At CLEO, the fragmentation of charm quarks can be analyzed by making measurements of primary hadrons containing charm quarks from continuum  $e^+e^-$  annihilations.

CLEO has previously published results of charmed meson energy distributions [8] as well as the spin alignment of charged  $D^*$  mesons [18]. In this paper an updated measurement of the charged  $D^*$  spin alignment using the entire CLEO II data set is presented.

## II. POLARIZATION, ALIGNMENT, AND $P_V$

According to the quark model, a meson is composed of two spin  $\frac{1}{2}$  valence quarks that can combine to form four spin states in the absence of orbital angular momentum, i.e. four  $S$ -wave states. Writing these in the basis of total angular momentum,  $J$ , and its  $z$ -component,  $J_z$ , they are the vector states  $|1,1\rangle$ ,  $|1,0\rangle$ ,  $|1,-1\rangle$ , and the pseudoscalar state  $|0,0\rangle$ , where the  $z$ -direction can be arbitrarily chosen. The probability of an  $S$ -wave meson being produced in a vector state is often described by the ratio  $P_V$  defined as

$$P_V = \frac{V}{V+P} \quad (1)$$

\*Permanent address: Lawrence Livermore National Laboratory, Livermore, CA 94551.

†Permanent address: BINP, RU-630090 Novosibirsk, Russia.

‡Permanent address: Yonsei University, Seoul 120-749, Korea.

§Permanent address: Brookhaven National Laboratory, Upton, NY 11973.

||Permanent address: University of Texas, Austin, TX 78712.

where  $P$  and  $V$  are the respective probabilities of the meson being created in the pseudoscalar and vector states.

The helicity formalism is useful in the context of describing the angular distributions and correlations in the production and decay of particles with non-zero spin. For a particle with momentum  $\vec{p}$ , the helicity is defined as

$$\lambda = \frac{\vec{J} \cdot \vec{p}}{|\vec{p}|}, \quad (2)$$

which in the case of a spin-1 particle is just the  $z$ -component of the spin when the  $z$ -direction has been chosen as the flight direction of the meson. The helicity density matrix is often used to organize information about the spin of a particle. The diagonal elements of this matrix  $\rho_{\lambda\lambda}$ , with  $\sum_{\lambda} \rho_{\lambda\lambda} = 1$ , represent the probability that the particle has helicity  $\lambda$ .

Simple statistical expectations are that all helicity states of a spin  $J$  particle are equally populated, but production and fragmentation dynamics can lead to either polarized or aligned particles. A system of particles is polarized if there is a net angular momentum, i.e.  $\rho_{\lambda\lambda} \neq \rho_{-\lambda-\lambda}$  for some helicity  $\lambda$ , and it is aligned if there is a nonuniform population of states, but  $\rho_{\lambda\lambda} = \rho_{-\lambda-\lambda}$  for all  $\lambda$ . Since the production and fragmentation processes in this analysis conserve parity and the Cornell Electron Storage Ring (CESR) beams are unpolarized, it is expected that the  $D^*$  mesons from  $e^+e^- \rightarrow \gamma^* \rightarrow c\bar{c}$  are unpolarized, but it is possible for the  $D^*$  mesons to be aligned.

To measure the spin alignment of a vector meson, the angular distribution of its decay products is analyzed, but because the angular distributions of the  $\lambda=1$  and  $\lambda=-1$  states are degenerate, the values of  $\rho_{11}$  and  $\rho_{-1-1}$  cannot be distinguished and only one variable, e.g.  $\rho_{00} = 1 - \rho_{11} - \rho_{-1-1}$ , is accessible. From the definition above, the vector meson is aligned if  $\rho_{00}$  differs from  $1/3$ . For the case of a vector meson decaying to two pseudoscalar mesons, the angular distribution can be written

$$W(\cos \theta) = \frac{3}{4} [(1 - \rho_{00}) + (3\rho_{00} - 1)\cos^2 \theta] \quad (3)$$

where  $\theta$  is defined as the angle of a daughter pseudoscalar in the parent vector meson rest frame, with respect to the direction of motion of the parent vector meson in the rest frame of the production process. In our case, the production rest frame of a  $D^*$  directly produced in charm fragmentation from  $e^+e^-$  annihilation coincides with the laboratory frame.

By using the variable

$$\alpha = \frac{3\rho_{00} - 1}{1 - \rho_{00}}, \quad (4)$$

the angular distribution can be expressed as

$$W(\cos \theta) = N(1 + \alpha \cos^2 \theta) \quad (5)$$

where  $N$  is a normalization factor equal to  $3/(6 + 2\alpha)$ . The value of  $\alpha$  can range between  $-1$  and  $+\infty$ , where the angu-

lar distribution would be isotropic if  $\alpha=0$ , proportional to  $\sin^2 \theta$  if  $\alpha=-1$  and proportional to  $\cos^2 \theta$  if  $\alpha=\infty$ .

Whereas the naive statistical expectation is that all four  $S$ -wave meson states are created in equal proportions, i.e.  $\rho_{\lambda\lambda} = \frac{1}{3}$  ( $\alpha=0$ ) and  $P_V=0.75$ , there are other models that have been presented where the alignment and  $P_V$  vary as a function of momentum [23,24]. Heavy quark symmetry predicts that vector mesons containing a single heavy quark are produced unaligned, but there have been suggestions that the value of  $P_V$  may depend upon the mass difference of the vector and pseudoscalar mesons [3,25]. It has also been suggested that  $P_V$  is directly related to the spin alignment [26], and in the previous CLEO  $D^*$  spin alignment analysis, a value for  $P_V$  was calculated using this relationship [18]. However, the validity of the statistical model was assumed when deriving this relationship. We feel that a determination of  $P_V$  for  $D^*$  mesons warrants an independent measurement which is the topic of a current CLEO analysis. The results of the  $P_V$  analysis will be presented in a future paper.

### III. DETECTOR AND EVENT SELECTION

The CLEO II detector is a general purpose charged and neutral particle detector and is described in detail elsewhere [27]. The data set used in this analysis consists of  $3.11 \text{ fb}^{-1}$  of data collected at the  $Y(4S)$  resonance and  $1.61 \text{ fb}^{-1}$  of data collected about 60 MeV below the resonance. This corresponds to approximately  $5 \times 10^6$  continuum  $c\bar{c}$  events.

The  $D^{*+}$  in this analysis is required to decay through the channel  $D^{*+} \rightarrow D^0 \pi^+$  with the  $D^0$  decaying either through the mode  $D^0 \rightarrow K^- \pi^+$  or  $D^0 \rightarrow K^- \pi^+ \pi^0$  (inclusion of charge conjugate modes is implied throughout this paper). The  $\pi^+$  in the  $D^{*+}$  decay is kinematically limited to having a momentum less than 456 MeV/ $c$  in the laboratory frame of reference, and is referred to as the ‘‘slow’’ pion.

All tracks used in this analysis are required to have an impact parameter within 5 mm of the interaction point in the plane transverse to the beam pipe and within 50 mm in the direction of the beam pipe. Tracks are also required to have a momentum less than 6 GeV/ $c$  and an rms residual less than 1 mm for their hits. Particle identification is not used since there is no appreciable gain for this particular analysis and it introduces the possibility of additional systematic errors. For a pair of photons to be considered as a candidate  $\pi^0$ , they must have an energy of at least 100 MeV, be within the barrel region of the detector where support structures do not adversely affect shower measurement ( $|\cos \theta_{detector}| < 0.71$ ), have a shower shape in the crystal calorimeters consistent with that of a photon, and have  $|\cos \theta_{\gamma}| < 0.9$ , where  $\theta_{\gamma}$  is the decay angle of the photon in the  $\pi^0$  rest frame, with respect to the  $\pi^0$  direction of motion in the laboratory frame. In addition, the reconstructed  $\pi^0$  must have an invariant mass within 20 MeV/ $c^2$  of the neutral pion mass.

For the  $D^0 \rightarrow K^- \pi^+$  mode, the  $D^0$  is reconstructed by taking all possible pairs of oppositely charged tracks in an event, assigning the kaon mass to one and the pion mass to the other (or vice versa), adding their four-momenta, and then calculating the invariant mass. The  $D^{*+}$  is recon-

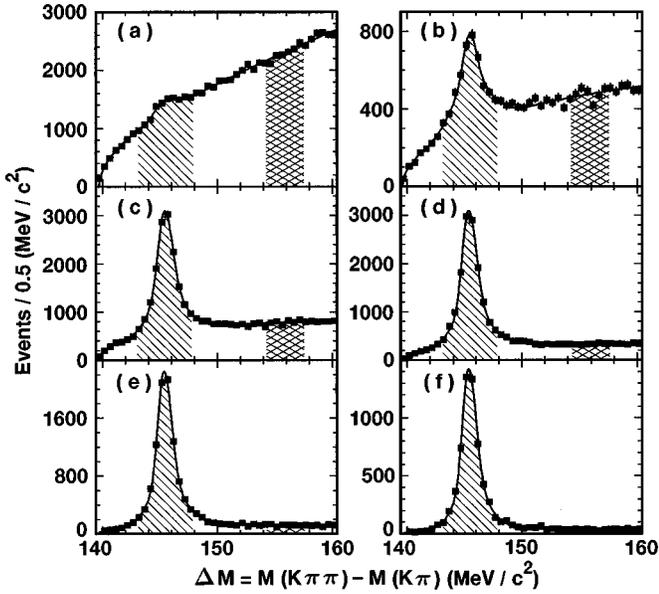


FIG. 1.  $D^* - D$  mass difference for the  $D^0 \rightarrow K\pi$  decay mode for the six  $x^+$  ranges (a)  $0.25 < x^+ < 0.45$ , (b)  $0.45 < x^+ < 0.55$ , (c)  $0.55 < x^+ < 0.65$ , (d)  $0.65 < x^+ < 0.75$ , (e)  $0.75 < x^+ < 0.85$ , (f)  $0.85 < x^+ < 1.0$ . The solid squares are the data points and the solid line is the fitting function as described in Sec. IV. The hatched area is the signal region while the crosshatched region is the sideband.

structured by adding the four-momentum of a candidate slow  $\pi^+$  in the event to the four-momentum of the candidate  $D^0$ . The mass difference,  $\Delta M$ , between the candidate  $D^0$  and  $D^{*+}$  is required to be within  $2.5 \text{ MeV}/c^2$  of the world-average mass difference of  $145.42 \text{ MeV}/c^2$  [28].

The  $D^0$  is spinless and the decay products have an isotropic angular distribution. However, because of the jet-like nature of continuum events, the background from random track combinations tends to have  $\cos \phi_K \approx -1$ , where  $\phi_K$  is the decay angle of the  $K^-$  in the  $D^0$  rest frame, relative to the  $D^0$  motion in the laboratory frame. A requirement that  $\cos \phi_K \geq -0.9$  is added to improve the signal-to-background ratio.

For the  $D^0 \rightarrow K^- \pi^+ \pi^0$  mode, the four-momentum of a candidate  $\pi^0$  is added to the four-momenta of two oppositely charged tracks to form candidate  $D^0$ 's in the event. Mass difference and kaon decay angle requirements are the same as described above.

#### IV. FITTING

To test models that predict that the alignment varies as a function of the momentum of the  $D^{*+}$ , the data are broken up into six  $x^+$  bins in the range 0.25–1.0, where  $x^+$  is a Lorentz-invariant variable defined as

$$x^+ \equiv \frac{P(D^*) + E(D^*)}{P_{max}(D^*) + E_{max}(D^*)}, \quad (6)$$

where  $E_{max} = E_{beam}$ ,  $P_{max} = \sqrt{E_{beam}^2 - M_{D^{*+}}^2}$  and  $M_{D^{*+}}$  is the world-average value for the mass of a  $D^{*+}$ .

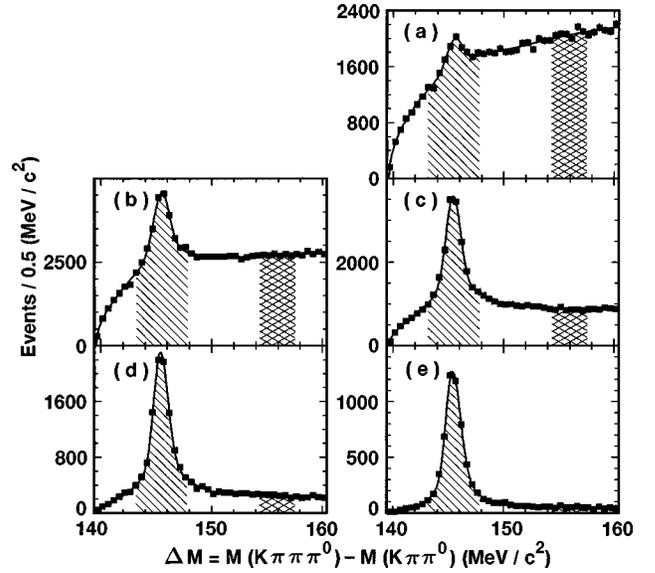


FIG. 2.  $D^* - D$  mass difference for the  $D^0 \rightarrow K\pi\pi^0$  decay mode for the five  $x^+$  ranges (a)  $0.45 < x^+ < 0.55$ , (b)  $0.55 < x^+ < 0.65$ , (c)  $0.65 < x^+ < 0.75$ , (d)  $0.75 < x^+ < 0.85$ , (e)  $0.85 < x^+ < 1.0$ . The solid squares are the data points and the solid line is the fitting function as described in Sec. IV. The hatched area is the signal region while the crosshatched region is the sideband.

For each  $x^+$  range, a sideband subtraction is performed. The sideband region is from  $9 \text{ MeV}/c^2$  to  $12 \text{ MeV}/c^2$  above the mean of the  $\Delta M$  peak and the ratio for the sideband subtraction is determined by fitting the data with a bifurcated double Gaussian for the signal plus a background function  $A + B(\Delta M)^{1/2} + C(\Delta M)^{3/2}$  and integrating the background shape for the signal and sideband regions. The fits used to determine the sideband ratios are shown in Figs. 1 and 2.

The sideband-subtracted  $M(K\pi)$  data are fit for each  $x^+$  bin with a double Gaussian for the signal region plus a first-order polynomial background.<sup>1</sup> Each of these  $x^+$  bins is broken up into five equal  $\cos \theta$  bins, where  $\theta$  is the angle defined in Sec. II. In order to reduce variance in the fitted parameters, the width and ratio of areas of the double Gaussian fit to the invariant mass distribution are fixed to the values obtained when fitting the mass peak in that momentum range for the entire  $\cos \theta$  spectrum.

#### V. EFFICIENCIES

It is important to understand the relative efficiencies of detecting a  $D^{*+}$  in the various  $\cos \theta$  bins. In the lowest momentum bins, for example, the efficiency decreases as  $\cos \theta$  approaches 1 because of the increased difficulty in measuring the track of a slow pion that is emitted in the direction opposite the  $D^*$  direction in the laboratory frame.

<sup>1</sup>The highest  $x^+$  bin is fit with a second order polynomial for the background since the background is not well represented by a straight line.

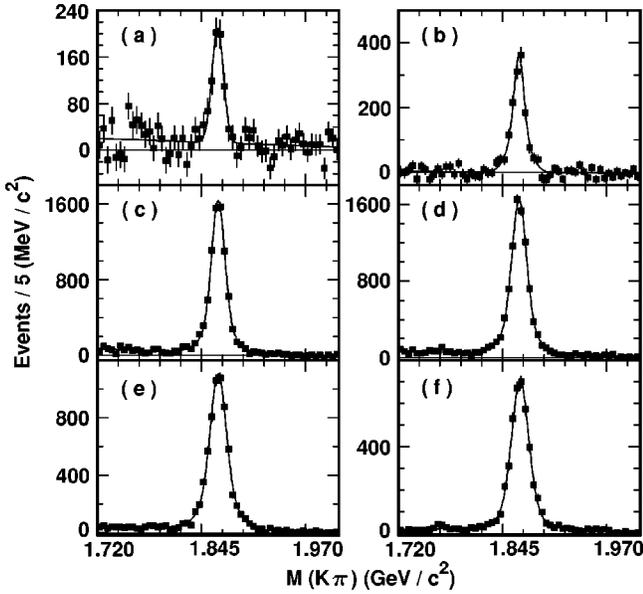


FIG. 3.  $M(K\pi)$  after sideband subtraction for the six  $x^+$  ranges (a)  $0.25 < x^+ < 0.45$ , (b)  $0.45 < x^+ < 0.55$ , (c)  $0.55 < x^+ < 0.65$ , (d)  $0.65 < x^+ < 0.75$ , (e)  $0.75 < x^+ < 0.85$ , (f)  $0.85 < x^+ < 1.0$ . The solid squares are the data points and the solid line is the fitting function as described in Sec. IV.

Detection efficiency as a function of  $x^+$  and  $\cos \theta$  was estimated by analyzing Monte Carlo events with a GEANT-based detector simulation.

Monte Carlo events were generated using the Lund JETSET 7.3 program, where the  $e^+e^-$  annihilation was required to result in a  $c\bar{c}$  pair with one of the charm quarks hadronizing to a  $D^{*+}$  that decays to  $D^0\pi^+$  with  $D^0$

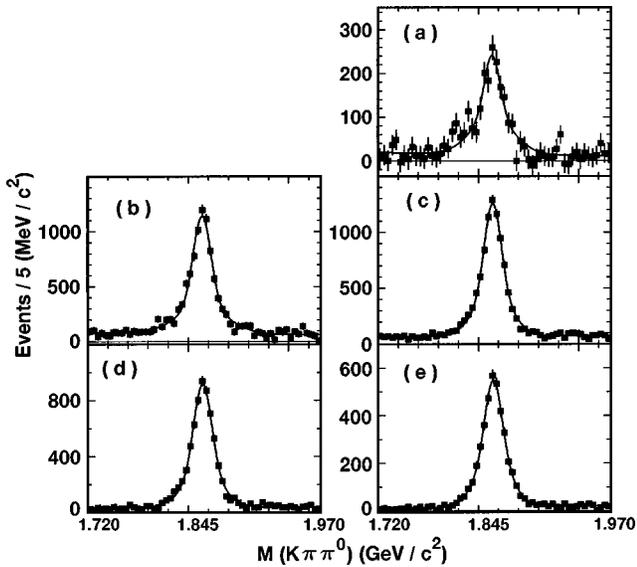


FIG. 4.  $M(K\pi\pi^0)$  after sideband subtraction for the five  $x^+$  ranges (a)  $0.45 < x^+ < 0.55$ , (b)  $0.55 < x^+ < 0.65$ , (c)  $0.65 < x^+ < 0.75$ , (d)  $0.75 < x^+ < 0.85$ , (e)  $0.85 < x^+ < 1.0$ . The solid squares are the data points and the solid line is the fitting function as described in Sec. IV.

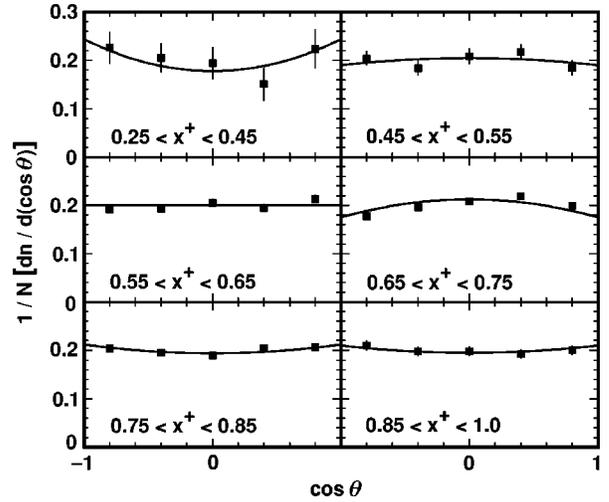


FIG. 5. Normalized  $\cos \theta$  distributions in the six  $x^+$  ranges for the  $D^0 \rightarrow K^- \pi^+$  and  $D^0 \rightarrow K^- \pi^+ \pi^0$  decay modes combined. The solid squares are the efficiency-corrected yields for each  $\cos \theta$  bin in the specified  $x^+$  range. These distributions are fit with the function  $W(\cos \theta) = 0.4N(1 + \alpha \cos^2 \theta)$ , where the factor of 0.4 is the bin width and  $N = 3/(6 + 2\alpha)$ .

$\rightarrow K^- \pi^+(\pi^0)$ , while no constraints were placed on the other charm quark. The  $D^*$  mesons were produced such that their decay to  $D^0\pi^+$  had an isotropic angular distribution in the rest frame of the  $D^{*+}$ .

## VI. RESULTS

The fits of the sideband subtracted  $M(K\pi)$  and  $M(K\pi\pi^0)$  distributions for all scaled momentum ranges are

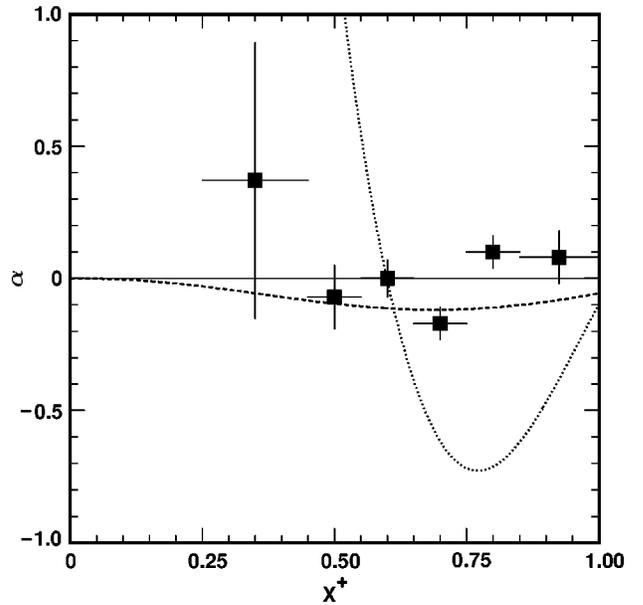


FIG. 6. The values of  $\alpha$  for each momentum bin are represented by the solid squares. Errors shown are the statistical and systematic errors added in quadrature. The solid line represents the statistical model. The dotted line represents the function predicted by Suzuki [23]. The dashed line is the function of Cheung and Yuan [24].

TABLE I. Values of  $\alpha$  for different momentum ranges. The first error given is statistical; the second is systematic. The last column is the confidence level of the fit for the combined values of  $\alpha$ .

$x^+$	$D^0 \rightarrow K^- \pi^+$		$D^0 \rightarrow K^- \pi^+ \pi^0$		Combined $\alpha$	Confidence level (%)
	Events	$\alpha$	Events	$\alpha$		
0.25–0.45	687±62	0.37±0.35			0.37±0.35±0.38	90
0.45–0.55	1472±58	−0.14±0.13	1830±171	0.09±0.24	−0.07±0.11±0.05	43
0.55–0.65	7640±125	0.14±0.08	8305±290	−0.18±0.08	0.00±0.05±0.05	11
0.65–0.75	8432±116	−0.13±0.06	8355±165	−0.22±0.06	−0.17±0.04±0.04	1
0.75–0.85	6264±97	0.14±0.08	6339±118	0.05±0.08	0.10±0.05±0.02	73
0.85–1.0	3828±83	0.17±0.12	3740±91	−0.02±0.11	0.08±0.08±0.07	90

shown in Figs. 3 and 4.<sup>2</sup> The efficiency-corrected angular distributions for both decay modes were combined in each  $x^+$  bin with a weighted average and are shown in Fig. 5, where they have each been normalized to unit area and fit with Eq. (5).

The values of  $\alpha$  resulting from these fits as well as the fits for each of the two decay modes treated separately are listed in Table I. Figure 6 shows the combined results for  $\alpha$  plotted as a function of momentum as well as the theoretical curves suggested by Suzuki [23] and Cheung and Yuan [24]. Table II lists the values of  $\rho_{00}$  as calculated from the measurement of  $\alpha$  for each scaled momentum bin. Averaging the  $\cos \theta$  distributions over all momenta and then fitting gives a value  $\bar{\alpha} = -0.028 \pm 0.026$ , corresponding to  $\bar{\rho}_{00} = 0.327 \pm 0.006$ .

Similar analyses have been done by the HRS, TPC, SLD and OPAL Collaborations [16,17,21,20], as well as by CLEO using a previous data set [18]. The average values of  $\alpha$  and  $\rho_{00}$  in each study are presented in Table III.

## VII. SYSTEMATIC ERROR

Many possible sources of absolute systematic uncertainty, such as the overall track-finding efficiency, do not have a significant effect on this analysis because the extraction of  $\alpha$  in each momentum range involves only relative comparisons of the same measured quantity, namely the yield of the  $D^0$  decays, in the different bins of  $\cos \theta$ . The remaining sources

TABLE II. Values of  $\rho_{00}$  for different momentum ranges. The first error given is statistical; the second is systematic.

$x^+$	$\rho_{00}$
0.25–0.25	0.40±0.07±0.07
0.45–0.55	0.31±0.03±0.01
0.55–0.65	0.33±0.01±0.01
0.65–0.75	0.30±0.01±0.01
0.75–0.85	0.35±0.01±0.01
0.85–1.0	0.35±0.02±0.01

<sup>2</sup>Only the highest five momentum bins were used for the  $D^0 \rightarrow K \pi \pi^0$  mode due to the small number of signal events and low signal-to-noise ratio in the lowest  $x^+$  range.

of uncertainty will therefore be related to extracting the yield and the efficiency as a function of  $\cos \theta$ . The effects of the various sources of systematic error are shown in Fig. 7 while the methods used to determine these errors are described below.

The Monte Carlo contribution to the systematic error was accounted for by including the error in the Monte Carlo efficiencies in the calculations of the yields. To investigate the systematic error associated with the fitting function, the analysis was done using a single Gaussian rather than a double Gaussian to fit the signal peaks. Likewise, to investigate the systematic error associated with the choice of range for the sideband subtraction, the analysis was done using a sideband region from 6 MeV/ $c^2$  to 9 MeV/ $c^2$  above the nominal  $D^* - D$  mass difference rather than from 9 MeV/ $c^2$  to 12 MeV/ $c^2$  above the nominal value. The effect of the mass difference requirement was investigated by constraining the mass difference to be within 1.25 MeV/ $c^2$  of the

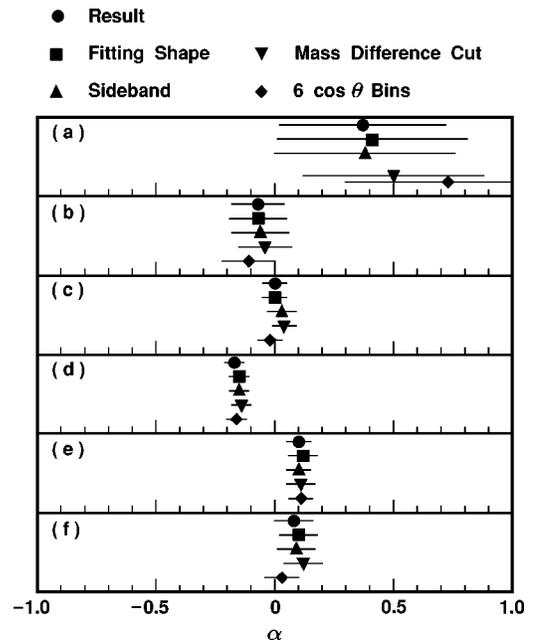


FIG. 7. The results from the systematic error studies for the six  $x^+$  bins (a)  $0.25 < x^+ < 0.45$ , (b)  $0.45 < x^+ < 0.55$ , (c)  $0.55 < x^+ < 0.65$ , (d)  $0.65 < x^+ < 0.75$ , (e)  $0.75 < x^+ < 0.85$ , (f)  $0.85 < x^+ < 1.0$ . The different symbols represent the resulting values of  $\alpha$  using the modifications in the analysis procedure as described in Sec. VII.

TABLE III. Results for  $\bar{\alpha}$  and  $\bar{\rho}_{00}$  found by various collaborations.

Collaboration	$\sqrt{s}$ (GeV)	$\bar{\alpha}$	$\bar{\rho}_{00}$
HRS	29	$0.18 \pm 0.08$	$0.371 \pm 0.016$
TPC	29	$-0.14 \pm 0.17 \pm 0.03$	$0.301 \pm 0.042 \pm 0.007$
SLD	91	$0.019 \pm 0.378 \pm 0.582$	$0.34 \pm 0.08 \pm 0.13$
OPAL	91	$0.33 \pm 0.11$	$0.40 \pm 0.02$
CLEO I.5	10.5	$0.08 \pm 0.07 \pm 0.04$	$0.351 \pm 0.015 \pm 0.008$
<b>CLEO II</b>	<b>10.5</b>	<b><math>-0.028 \pm 0.026</math></b>	<b><math>0.327 \pm 0.006</math></b>

Particle Data Group (PDG) value rather than  $2.5 \text{ MeV}/c^2$ . The systematic effects of the  $\cos \theta$  binning were studied by using six equal  $\cos \theta$  bins rather than five. The differences between the resulting values of  $\alpha$  and the central value were all summed in quadrature as an estimate of the systematic error and are included in the error bars shown in Fig. 6.

A small linear component in the angular distribution can easily be seen in Fig. 5 for the range  $0.65 < x^+ < 0.75$ . This is most likely due to a slight inaccuracy in the efficiency correction from the Monte Carlo sample. The data in Fig. 5 were fit with a straight line added to Eq. (4) as a check and the difference in the fitted values of  $\alpha$  was negligible.

### VIII. INTERPRETATION OF RESULTS

We have measured the spin alignment of all  $D^*$  mesons produced in  $e^+e^- \rightarrow q\bar{q}$  interactions at  $\sqrt{s}=10.5$  GeV. Although the details of the analysis ensure that the measured  $D^*$  does not come from a decaying  $B$  meson, we cannot determine any other details about the production hierarchy. From a theoretical standpoint, we are particularly interested in the  $D^*$  mesons that are produced directly in the  $e^+e^-$  collision, but we cannot distinguish these from secondary  $D^*$ 's resulting from decays of charm mesons with  $L > 0$  [29–31].

The most prominent excited charm mesons, which are commonly referred to as  $D^{**}$  mesons, consist of a charm quark and a light anti-quark with relative orbital angular momentum  $L=1$ . They are categorized into four states with spin-parity  $J^P=0^+, 1^+, 1^+,$  and  $2^+$ . A  $0^+$  state decay to  $D^*\pi$  is forbidden due to spin-parity conservation while other  $D^*$  modes are expected to be suppressed. When a  $2^+$  state decays through a  $D^*$  channel, it can only produce a  $D^*$  meson with a helicity of  $\pm 1$  in the  $2^+$  rest frame, while the  $1^+$  states only decay through  $D^*$  channels and favor a helicity of 0 in the  $1^+$  rest frame. From the measurements available [32,33], we estimate that 16–20 % of  $D^*$  mesons observed at CLEO could be daughters of a  $D^{**}$  meson, not

including the contribution from  $D_s^{**}$  mesons.

Although the favored helicities of  $D^{**}$ 's from the decays of  $2^+$  and  $1^+$  charm states partially cancel, it is probable that these  $D^{**}$ 's are aligned in their production rest frame, i.e. the rest frame of the parent  $D^{**}$ . It is expected that any effect would be most noticeable for the highest  $x^+$  bins which have the largest correlation between the  $D^*$  4-momentum in the laboratory frame and the  $D^*$  4-momentum in the  $D^{**}$  rest frame. If the 4-momenta in the two reference frames are uncorrelated, as tends to be the case for the lower  $x^+$  bins, any alignment of  $D^*$ 's from  $D^{**}$ 's would not be noticeable in the laboratory frame.

Because of the current lack of information about the production and decay of  $P$ -wave charm meson states, we can only state that  $D^{**}$  decays could have a significant effect on this  $D^*$  spin alignment measurement in at least some of the  $x^+$  bins.

### IX. CONCLUSION

This analysis is the most precise measurement of the spin alignment of  $D^{*+}$  mesons to date. The data, without any corrections for  $D^{**}$  effects on the measurements, agree well with the statistical model expectation that the  $J_z=0$  state has a  $\frac{1}{3}$  probability of being populated.

### ACKNOWLEDGMENTS

We gratefully acknowledge the effort of the CESR staff in providing us with excellent luminosity and running conditions. J.P.A., J.R.P., and I.P.J.S. thank the NYI program of the NSF, M.S. thanks the PFF program of the NSF, K.K.G., M.S., H.N.N., T.S., and H.Y. thank the OJI program of the DOE, J.R.P., K.H., M.S. and V.S. thank the A.P. Sloan Foundation, M.S. thanks Research Corporation, and S.D. thanks the Swiss National Science Foundation for support. This work was supported by the National Science Foundation, the U.S. Department of Energy, and the Natural Sciences and Engineering Research Council of Canada.

[1] C. Peterson *et al.*, Phys. Rev. D **27**, 105 (1983).

[2] M. Suzuki, Phys. Lett. **71B**, 139 (1977).

[3] A. F. Falk and M. E. Peskin, Phys. Rev. D **49**, 3320 (1994).

[4] M. Cacciari and M. Greco, Phys. Rev. D **55**, 7134 (1997).

[5] J. D. Bjorken, Phys. Rev. D **17**, 171 (1978).

[6] X. Artru and G. Mennessier, Nucl. Phys. **B70**, 93 (1974).

[7] M. G. Bowler, Z. Phys. C **11**, 169 (1981).

[8] CLEO Collaboration, D. Bortoletto *et al.*, Phys. Rev. D **37**, 1719 (1988).

- [9] ARGUS Collaboration, H. Albrecht *et al.*, *Z. Phys. C* **52**, 353 (1991).
- [10] OPAL Collaboration, R. Akers *et al.*, *Z. Phys. C* **67**, 27 (1995).
- [11] DELCO Collaboration, H. Yamamoto *et al.*, *Phys. Rev. Lett.* **54**, 522 (1985).
- [12] HRS Collaboration, M. Derrick *et al.*, *Phys. Lett.* **146B**, 261 (1984).
- [13] TPC Collaboration, H. Aihara *et al.*, *Phys. Rev. D* **34**, 1945 (1986).
- [14] TASSO Collaboration, M. Althoff *et al.*, *Phys. Lett.* **126B**, 493 (1983).
- [15] JADE Collaboration, W. Bartel *et al.*, *Phys. Lett.* **161B**, 197 (1985).
- [16] HRS Collaboration, S. Abachi *et al.*, *Phys. Lett. B* **199**, 585 (1987).
- [17] TPC Collaboration, S. Aihara *et al.*, *Phys. Rev. D* **43**, 29 (1991).
- [18] CLEO Collaboration, Y. Kubota *et al.*, *Phys. Rev. D* **44**, 593 (1991).
- [19] ALEPH Collaboration, D. Decamp *et al.*, *Phys. Lett. B* **266**, 218 (1991).
- [20] OPAL Collaboration, K. Ackerstaff *et al.*, *Z. Phys. C* **74**, 437 (1997).
- [21] SLD Collaboration, K. Abe *et al.*, presented at International Europhysics Conference on High-Energy Physics (HEP97), Jerusalem, Israel, 1997, Report No. SLAC-PUB 7574.
- [22] ALEPH Collaboration, D. Buskulic *et al.*, *Z. Phys. C* **62**, 1 (1994).
- [23] M. Suzuki, *Phys. Rev. D* **33**, 676 (1986).
- [24] K. Cheung and T. C. Yuan, *Phys. Rev. D* **50**, 3181 (1994).
- [25] K. Cheung, presented at the 1995 PASCOS/Hopkins Workshop, Johns Hopkins University, Baltimore, Maryland, 1995, hep-ph/9505365.
- [26] J. F. Donoghue, *Phys. Rev. D* **19**, 2806 (1979).
- [27] CLEO Collaboration, Y. Kubota *et al.*, *Nucl. Instrum. Methods Phys. Res. A* **320**, 66 (1992).
- [28] Particle Data Group, R. M. Barnett *et al.*, *Phys. Rev. D* **54**, 1 (1996).
- [29] ARGUS Collaboration, H. Albrecht *et al.*, *Phys. Rev. Lett.* **56**, 549 (1986).
- [30] CLEO Collaboration, P. Avery *et al.*, *Phys. Rev. D* **41**, 744 (1990).
- [31] OPAL Collaboration, K. Ackerstaff *et al.*, *Z. Phys. C* **76**, 425 (1997).
- [32] CLEO Collaboration, P. Avery *et al.*, *Phys. Lett. B* **331**, 236 (1994).
- [33] CLEO Collaboration, T. Bergfeld *et al.*, *Phys. Lett. B* **340**, 194 (1994).