Diffractive J/ψ production as a probe of the gluon component in the Pomeron

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We present a study of large $p_T J/\psi$ production in hard diffractive processes by Pomeron exchange at the Fermilab Tevatron. We find that this process $(p\bar{p}\rightarrow p+J/\psi+X)$ can be used to probe the gluon content of the Pomeron and to measure the gluon fraction of the Pomeron. Direct diffractive J/ψ production can also provide another crucial test for the color-octet fragmentation mechanism. Using the *renormalized* Pomeron flux factor $D \approx 1/9$, the single diffractive *J/* ψ production cross section at large p_T (≥ 8 GeV) is found to be of the order of 0.01 nb, and the ratio of single diffractive to nondiffractive J/ψ production is 0.65±0.15% for the gluon fraction $f_g = 0.7 \pm 0.2$. [S0556-2821(98)05409-5]

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In the past few years there has been a renaissance of interest in diffractive scattering. Diffractive processes in hadron collisions are well described by the Regge theory in terms of Pomeron (P) exchange [1,2]. The Pomeron carries quantum numbers of the vacuum, so it is a colorless entity in QCD language, which may lead to ''rapidity gap'' events in experiments. However, the nature of the Pomeron and its reaction with hadrons remains a mystery. In $[3]$, hard diffractive scattering processes were suggested to resolve the quark and gluon content in the Pomeron. That is to say, the Pomeron has a partonic structure, just as hadrons and nuclei. Therefore, various processes may be considered to probe the partonic structure of the Pomeron at high energy colliders $[3-6]$.

On the experimental side, the UA8 collaboration at the CERN Super Proton Synchrotron (S*ppS*) collider has studied diffractive dijet production at \sqrt{s} = 630 GeV [7], which indicates a dominant hard partonic structure of the Pomeron. The H1 and ZEUS Collaborations have studied diffractive deep inelastic scattering (DDIS) and dijet photoproduction in *ep* collisions at \sqrt{s} =300 GeV [8]. From these measurements, the ZEUS Collaboration determined that the gluon fraction of the Pomeron f_g is in the range of $0.3 < f_g < 0.8$, and the H1 Collaboration determined the quark fraction of the Pomeron $f_q \approx 0.2$. The partonic structure of the Pomeron was also studied recently by the Collider Detector at Fermilab (CDF) Collaboration through diffractive *W* production $[9]$ and dijet production $[10]$, which give further evidence for the hard partonic structure of the pomeron. The combination of these two measurements determined the gluon fraction of the Pomeron to be 0.7 ± 0.2 .

In this paper, we will discuss another diffractive process, single diffractive (SD) J/ψ production at large p_T (shown in Fig. 1 :

$$
p + \overline{p} \rightarrow p + J/\psi + X. \tag{1}
$$

By the following calculations, we will show that SD J/ψ production is sensitive to the gluon fraction of the Pomeron. So, the measurement of diffractive J/ψ production at the Fermilab Tevatron would provide a probe of the gluon distribution in the Pomeron. Importantly, at hadron colliders the J/ψ production is of special significance because it has extremely clean signature through its leptonic decay modes. Furthermore, the SD J/ψ production is also interesting to the study of heavy quarkonium production mechanism, which is another hot topic in the past few years.

For a long time, it was believed that the heavy quarkonium production at large p_T dominantly comes from the leading order color-singlet processes [11]. But, as pointed out by Braaten and Yuan $[12]$, the fragmentation contributions may dominate over those from leading-order processes at sufficiently large p_T , although the fragmentation processes are of higher order in strong coupling constant α_s . However, the measurements of large p_T charmonia production from the CDF at the Tevatron show a large excess of direct production (excluding the contribution from b decays and the feeddown from χ_c) both for *J*/ ψ and ψ' [13,14]. The experimental measurement is a factor of 30–50 larger than the theoretical prediction of the color-singlet model even if including the fragmentation contributions. Motivated by this ''surplus'' problem, a new mechanism for heavy quarkonium production at large p_T in hadronic collisions, named as color-octet gluon fragmentation, has been proposed $\lfloor 15 \rfloor$, which is based on the factorization formalism of nonrelativistic quantum chromodynamics $(NRQCD)$ [16]. In the past few years, applications of the NRQCD factorization formalism to $J/\psi(\psi')$ production at various experimental facilities have been studied $[17]$.

FIG. 1. Sketch diagram for the SD J/ψ production by Pomeron exchange at the Tevatron.

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According to the NRQCD factorization formalism, the gluon fragmentation to J/ψ production can be factorized as

$$
D_{g \to J/\psi}(z,\mu^2) = \sum_n d_{g \to n}(z,\mu^2) \langle \mathcal{O}_n^{J/\psi} \rangle, \tag{2}
$$

where *z* is the longitudinal momentum fraction carried by the produced *J*/ ψ in gluon fragmentation, $\mu = 2m_c$ is the fragmentation scale. $d_{g \to n}$ represent the short-distance coefficients associated with the perturbative subprocesses in which a $c\bar{c}$ pair is produced in a configuration denoted by *n* (angular momentum $2S+1$ *L_J* and color index 1 or 8). $\langle O_n^{J/\psi} \rangle$ are the long distance nonperturbative matrix elements demonstrating the probability of a $c\bar{c}$ pair evolving into the physical state *J*/ ψ . The short-distance coefficients $d_{g \to n}$ can be obtained from perturbative calculations in powers of coupling constant α_s . $\langle O^{J/\psi}_n \rangle$ consist of two kinds of matrix elements, i.e., the color-singlet and color-octet matrix elements (according to when the color index is 1 or 8).

For J/ψ production in gluon fragmentation, the coloroctet matrix element $\langle \mathcal{O}_8^{J/\psi}({}^3S_1) \rangle$ is smaller than the colorsinglet matrix element $\langle \mathcal{O}_1^{J/\psi}({}^3S_1) \rangle$ by a factor of order v^4 according to the NRQCD velocity scaling rules. However, the short-distance coefficient for the color-octet term in Eq. (2) is larger than that for the color-singlet term by a factor of order $1/\alpha_s^2$. Numerical results show that color-octet contributions are 50 times larger than color-singlet contributions [15]. In the following calculations, we neglect the colorsinglet term in gluon fragmentation in Eq. (2) , and only consider the color-octet gluon fragmentation. The leading-order color-octet gluon fragmentation to J/ψ production gives [15]

$$
D_{g \to J/\psi}^{(8)}(z,\mu^2) = \frac{\pi \alpha_s(2m_c)}{24} \frac{\langle \mathcal{O}_8^{J/\psi}(^3S_1) \rangle}{m_c^3} \delta(1-z). \quad (3)
$$

In our calculations, the effects of the evolution of gluon fragmentation function with scale μ^2 are neglected, which may introduce some error. However, as argued in $[18]$, including evolution would not necessarily be an improvement, since naive Altarelli-Parisi equations do not respect the phase-space constraint $D_{g\rightarrow J/\psi}(z,\mu^2)=0$ for $z\leq m_{J/\psi}^2/\mu^2$ $[19]$.

As shown in Figs. 1 and 2, the SD process $p\bar{p}\rightarrow p+J/\psi$ $+X$ by Pomeron exchange consists of three steps. First, a Pomeron is emitted from the proton with a small squared momentum transfer, $t=(p_i-p_f)^2$, where p_i and p_f are the momenta of the initial and the final states of the proton, respectively. Second, partons interaction between the Pomeron and the antiproton takes place in the large momentum transfer processes (see Fig. 2). In the third step, J/ψ is produced via the fragmentation processes. Because the fragmentation contributions dominantly come from the coloroctet gluon fragmentation process, in our calculations we calculate the $gg(q\bar{q}) \rightarrow gg$, $q(\bar{q})g \rightarrow q(\bar{q})g$ processes and followed by the gluon fragmentation Eq. (3) .

Using the Pomeron factorization formalism $|3,4|$, we write the SD J/ψ production cross section as

FIG. 2. A typical diagram for the color-octet gluon fragmentation J/ψ production in $\overline{P} \overline{p} \rightarrow J/\psi + X$ process.

$$
\frac{d\sigma(p\bar{p}\to p+J/\psi+X)}{d\xi dt}=f_{\mathbb{P}/p}(\xi,t)d\sigma(\mathbb{P}\bar{p}\to J/\psi+X),\tag{4}
$$

where ξ is the momentum fraction of the proton carried by the Pomeron. $f_{P/p}$ is the Pomeron "flux" factor,

$$
f_{P/p}(\xi, t) = \frac{d^2 \sigma_{SD} / d\xi dt}{\sigma_T^{Pp}(s', t)} = \frac{\beta_1^2(t)}{16\pi} \xi^{1 - 2\alpha(t)} F^2(t)
$$

= $K \xi^{1 - 2\alpha(t)} F^2(t)$. (5)

Following $|20|$, the parameters are choosen as

$$
K=0.73 \text{ GeV}^{-2}
$$
, $\alpha(t)=1+0.115+0.26 \text{ (GeV}^{-2})t$,
 $F^2(t)=e^{4.6t}$. (6)

In our calculations, we use the *renormalized* flux factor $D \cdot f(\xi, t)$ [20], which may preserve the shapes of M^2 and *t* distributions in SD and predict the experimentally observed SD cross section at all energies. Here *D* is defined as

$$
D = \text{Min}(1, 1/\mathcal{N}),\tag{7}
$$

with

$$
\mathcal{N} = \int_{\xi_{\min}}^{\xi_{\max}} d\xi \int_{t=0}^{\infty} f_{P/p}(\xi, t), \tag{8}
$$

where $\xi_{\text{min}} = M_0^2/s$ with $M_0^2 = 1.5 \text{ GeV}^2$ (effective threshold) and $\xi_{\text{max}}=0.1$ (coherence limit). For the SD process at the Tevatron (\sqrt{s} =1800 GeV), the renormalized factor *D* \approx 1/9. As a conservative estimate, we will take this as a tentative value for D in the following calculations. $(How$ ever, we should keep in mind that this flux factor *D* has not been well determined experimentally. If the precise value can be obtained in the future, our results will change accordingly.)

On the parton structure functions of the Pomeron, we assume the hard form $[6,9,10]$

$$
\beta G(\beta) = (f_q + f_g)[6\beta(1 - \beta)],\tag{9}
$$

where β is the momentum fraction of the Pomeron carried by the quarks and gluons. f_q and f_g are the quark and gluon fractions of the Pomeron, respectively. The momentum sum rule constrains $f_q + f_g = 1$. We neglect any Q^2 evolution in the above parton densities of the Pomeron $[6]$.

FIG. 3. The SD J/ψ production cross section as a function of the minimum $p_T(\psi)$ for $2.0 \le \eta(\psi) \le 4.0$.

With these partons densities in the Pomeron and the parton distribution functions in the antiproton, $d\sigma(P\bar{p}\rightarrow J/\psi)$ $+X$) can be calculated by employing the usual way in the parton model calculations in hadronic collisions. We use the $MRS(A)$ parton distribution functions [21] to generate the production cross section, and set the renomalization scale and the factorization scale both equal to the transverse momentum of the fragmenting gluon $\mu = p_T(g) \approx p_T(\psi)$. In gluon fragmentation, the input parameters are taken to be

$$
m_c = 1.5 \text{ GeV}, \quad \alpha_s(2m_c) = 0.26,
$$

$$
\langle \mathcal{O}_8^{J/\psi}(^3S_1) \rangle = 0.0106 \text{ GeV}^3.
$$
 (10)

The value of the color-octet matrix element $\langle \mathcal{O}_8^{J/\psi}({}^3S_1) \rangle$ follows the fitted value in $[22]$ by comparing the theoretical prediction to the experimental data at the Tevatron. In the total cross section, we also include the contributions from the χ_c and ψ' feeddowns through gluon fragmentation $g \rightarrow \chi_c$ and $g \rightarrow \psi'$ followed by $\chi_c \rightarrow \psi \gamma$ and $\psi' \rightarrow \psi X$. The feeddown contributions give the same p_T distribution of J/ψ and contribute about one-third of the total prompt J/ψ production cross section (see Ref. $[14]$). The leptonic decay branching ratio $B(J/\psi \rightarrow \mu^+\mu^-)=0.0597$ is also multiplied in the cross section. The above described procedure (including the fragmentation approximation) can reproduce the large p_T *J*/ ψ production in the central region (i.e, $|\eta(J/\psi)|$ < 0.6) at the Tevatron $[14,15]$.

Because the $q\bar{q}$ annihilation process only contributes a small portion to the total cross section of large $p_T J/\psi$ production, the SD J/ψ production is insensitive to the quark flavor number of the Pomeron. In our calculations we only consider two-quark flavors. A pseudorapidity cut of 2.0 $\langle \eta(\psi) \langle 4.0 \rangle$ was also performed on the produced *J*/ ψ . The diffractive variables ξ and t are integrated over the range of $0 < \xi < 0.1$ and $|t| < 1$ GeV². In Fig. 3, we show the cross section of SD J/ψ production as a function of the minimum transfer momentum of the produced J/ψ . Because the *gg* process is the dominant process in the production of J/ψ , the cross section is sensitive to the gluon component in the Pomeron (i.e., the gluon fraction f_g). In this figure, we plot

FIG. 4. The differential cross section for the SD J/ψ production as a function of p_T for the hard gluon (dashed line) and soft gluon (dotted line) parametrizations in the Pomeron.

three curves corresponding to three different values of the gluon fraction f_g . The solid line represents the cross section $\sigma(p\bar{p}\rightarrow p+J/\psi+X)\times B(J/\psi\rightarrow \mu^{+}\mu^{-})$ for the gluon fraction set to be $f_g = 0.7$ (which is determined by the experiments at the Tevatron [10]). The dotted line is for $f_g=0$ $(f_q=1)$ and the dashed line for $f_g=1$ $(f_q=0)$. These curves show that the SD J/ψ production cross section may reach the level of order of 0.01 nb (for $p_T(\text{min})=8 \text{ GeV}$), and therefore is observable at the Fermilab Tevatron at present.

In the above calculations, we use the widely used parametrization of the gluon distribution in the Pomeron, i.e., the hard form Eq. (9) . However, the precise form of the gluon density of the Pomeron is unknown at present and this will affect the p_T distribution of the SD J/ψ production. Different parametrizations will give rise to different spectra. If the gluon in the Pomeron is soft, e.g., the gluon distribution in the Pomeron behaves like

$$
\beta G(\beta) = 6(1 - \beta)^5,\tag{11}
$$

the spectra would be different. In Fig. 4, we show the p_T distributions of the cross section of the SD J/ψ production in both the hard gluon and soft gluon cases. The result shown in Fig. 4 is consistent with the expectation that the softer gluon will favor J/ψ production with smaller p_T , while the harder gluon will favor larger p_T . The differential cross sections at large p_T for these two cases are different, but their differences are not so critical to distinguish between them. So, in the following discussion, we mainly limit ourselves to the hard gluon parametrization of the Pomeron, but we will also mention the result for the soft gluon parametrization.

As a comparison, we also calculate the nondiffractive (ND) forward J/ψ production $(p + \bar{p} \rightarrow J/\psi + X)$ in the same kinematic region, i.e., $2.0 \le \eta(\psi) \le 4.0$. The forward region J/ψ production is also interesting to the study of the J/ψ production mechanism, because the relative contributions of different mechanisms may vary with J/ψ rapidity. Furthermore, the comparison of forward and central region J/ψ production can provide a consistent test of the ''surplus'' problem of ψ' and *J*/ ψ found at the Tevatron [14]. In Fig. 5, we

FIG. 5. The ND forward J/ψ production cross section for 2.0 $<\eta(\psi)<4.0$.

plot the ND forward J/ψ production cross section as a function of p_T (min). This theoretical prediction can be used to compare with the experimental data, and may provide a further test for the color-octet gluon fragmentation production mechanism. (The D0 Collaboration at the Fermilab Tevatron have reported the forward J/ψ production data [23]. However, these data do not exclude the contributions from *b* decays. We hope that the prompt J/ψ production data in the forward region may be obtained in the near future.)

In Fig. 6, we plot the ratio $R(\psi) = \sigma_{SD}/\sigma_{ND}$ as a function of f_g (solid line), where σ_{SD} is the cross section for SD *J*/ ψ production, and σ_{ND} is for the ND J/ψ production in the same kinematic region. The kinematic constraints for the produced J/ψ are the same for these two processes, i.e., $p_T(\text{min})=8$ GeV and $2.0<\eta(\psi)<4.0$. The ratio $R(\psi)$ increase from 0.1% as $f_g = 0$ to 0.9% as $f_g = 1.0$. For $f_g = 0.7$ ± 0.2 , the ratio *R(* ψ *)* will be 0.65 ± 0.15 %. We must note that $R(\psi)$ is independent of the choice of the color-octet matrix element $\langle \mathcal{O}_8^{J/\psi}({}^3S_1) \rangle$ because its dependence is cancelled in the ratio $\sigma_{SD} / \sigma_{ND}$. So, measuring this ratio *R*(ψ) can determine the gluon fraction f_g precisely, provided that the color-octet gluon fragmentation is the dominant mechanism for the J/ψ production at large p_T .

One more thing that must be noted in the above calculations of the ratio $R(\psi) = \sigma_{SD}/\sigma_{ND}$ is the approximation of neglecting the fragmentation function smearing. If the p_T distributions of the SD and ND J/ψ production are much different, the smearing effects will influence the ration $R(\psi)$ and the extraction of f_g from this ratio. To see these effects, we calculate the ratio $R(\psi) = \sigma_{SD}/\sigma_{ND}$ for different values of p_T (min), which is shown in Table I. From this table, we can see that the ratio $R(\psi)$ is almost a constant (with a fluctuation less than 10%) as a function of $p_T(\text{min})$ for both the

FIG. 6. The ratio of $R(\psi) = \sigma_{SD}(\psi)/\sigma_{ND}(\psi)$ vs the gluon fraction of the Pomeron f_g . The solid line corresponds to the momentum fraction D used as the *renormalized* factor as in Eq. (7) . The shaded region represents the range of the ratio *R* limited by the measured fraction $D=0.18\pm0.04$ by the CDF.

hard quark and hard gluon cases. This implies that the ratio $R(\psi)$ is not sensitive to the smearing, and we may neglect the smearing effects in the calculations of the ratio $R(\psi)$ and the extraction of the gluon fraction f_g .

In Table I, we also give the result for the soft gluon parametrization. The ratio $R(\psi)$ for the soft gluon is larger than the hard gluon by a factor ≤ 2 at $p_T(\text{min}) \geq 10 \text{ GeV}$.

Experimentally, the nondiffractive background to the diffractive J/ψ production must be dropped out to obtain useful information of the above calculations. Theoretically, the SD J/ψ production events can be distinguished from those nondiffractive events by performing the rapid gap (RG) analysis. However, the acceptance of the RG will affect this analysis. Here, we adopt the existing results of the background estimate obtained by the CDF diffractive Dijet experiment, where they give the nondiffractive background to the SD evens to be 20% [10]. By the same reason, we expect that the nondiffractive background to the SD J/ψ production is about 20%.

Finally, we discuss the theoretical uncertainty coming from the choice of the factor D of Eq. (7) . The factor D represents the momentum fraction of the Pomeron carried by the hard partons with the standard Pomeron flux. In our calculations, we use the *renormalized* factor, which is about 1/9 at the Tevatron energy region. But the value cited here is not unique, because it may change with different choices of the parameters such as M_0 and ξ_{max} in Eq. (7). The momentum fraction *D* can be measured in the diffractive processes at various collider faculties. At the Tevatron, the CDF Collaboration have determined the fraction *D* to be 0.18 ± 0.04 [10], which is well below the range $0.4 < D < 1.6$ reported by the

TABLE I. The ratio $R(\psi) = \frac{\sigma_{SD}}{\sigma_{ND}}$ as a function of $p_T(\text{min})$.

5.0	6.0	7.0	8.0	9.0		11.0	12.0	13.0
					0.14	0.14	0.14	0.14
				0.84	0.85	0.86	0.88	0.87
2.4	2.1	-1.9	1.8	1.6	1.5	1.4	1.4	1.3
			$R(\psi)$ for hard gluon $(\%)$ 0.98 0.93 0.90		0.86	0.17 0.16 0.15 0.14 0.14	10.0	

ZEUS Collaboration. If we adopt the CDF measurement, there must be difference in the above calculations of the ratio *R*, which is also shown in Fig. 6. The shaded region in Fig. 6 represents the range of the ratio *R* calculated as a function of f_g by using the fraction $D=0.18\pm0.04$.

As discussed in previous studies $[15,22]$, color-octet mechanism is crucially important to direct J/ψ production (excluding the contributions from b decays and the χ_c and ψ' feeddowns) at large p_T ; here the color-octet mechanism is also crucially important to the direct J/ψ production in the diffraction region. If only considering the color-singlet contributions (mainly coming from gluon fragmentation) the SD direct J/ψ production rate will be smaller than the curves shown in Fig. 3 by a factor of 50. This will make the measurement of the SD direct J/ψ production very difficult at present luminosity at the Tevatron. That is to say, the SD direct J/ψ production can also be regarded as another important test for the color-octet mechanism.

As a final remark, we note that our proposal, the diffractive J/ψ production, may also be used to extract the gluon fraction in photoproduction at the DESY *ep* collider HERA. There are more diffractive events at the HERA than that at the Tevatron. So, more interesting results may be obtained. The work along this way is in progress $[24]$.

In conclusion, in this paper we have shown that the diffractive J/ψ production at large p_T is sensitive to the gluon fraction of the Pomeron f_g . The measurement of this process at the Tevatron would provide a determination of f_g . We have also discussed the uncertainties caused by the renormalized factor *D* and the gluon parametrizations of the Pomeron. These uncertainties, however, can be reduced by combining other experimental measurements such as dijet diffractive production and *W* diffractive production. We believe that with the proposed SD J/ψ production presented in this paper, we will get a better understanding for the property of the Pomeron. And also, the SD direct J/ψ production will provide another crucial test for the color-octet production mechanism.

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