

Non-Abelian flavor symmetry and R parity

Gautam Bhattacharyya*

Dipartimento di Fisica, Università di Pisa and INFN, Sezione di Pisa, I-56126 Pisa, Italy

(Received 8 August 1997; published 19 February 1998)

If R -parity violation turns out to be a true aspect of nature, speculation about its possible origin could add a new dimension to the supersymmetric flavor problem. It has been shown in the past by Barbieri, Hall, and their collaborators that the small breaking parameters of an approximate non-Abelian flavor symmetry could govern the light quark and lepton masses and at the same time could account for the near degeneracies of squarks and sleptons. A possible connection of the above feature to the natural suppressions of R parity-violating couplings has been investigated here. With some modifications of the approximate flavor symmetry, a supersymmetric theory without R parity has been motivated that has testable experimental signatures. [S0556-2821(98)02105-5]

PACS number(s): 11.30.Fs, 11.30.Hv, 12.60.Jv

Is it possible to reconcile the conventional notion of flavor physics in supersymmetry concerning masses and mixings and the scenario of R -parity violation? In this paper, we seek a phenomenologically viable solution to this question within the framework of a non-Abelian flavor symmetry. R parity is a discrete symmetry, defined as $(-1)^{3B+L+2S}$, where B and L are the baryon and lepton numbers and S is the intrinsic spin of a particle [1]. It is $+1$ for all standard model particles and -1 for their superpartners. Recall that neither L - nor B -conservation is ensured by gauge invariances. But their uncontrolled violation leads to rapid proton decay and speeds up many other physical processes at unwanted rates: these prompted one to impose R parity in *canonical* supersymmetric theories. However, violating R parity [2,3] in a *controlled* way has rich phenomenological consequences that in recent times have received considerable attention. An attempt to link R -parity violation to the origin of masses and mixings was made in the past by invoking a horizontal $U(1)$ symmetry, where charges dictated by fermion masses and mixings were shown to produce sufficient suppression in R -parity-violating (\mathcal{R}) couplings [4]. Here we are concerned with a non-Abelian flavor symmetry, conjectured first [5] to realize the conventional supersymmetric theory of flavor, generalized now to admit \mathcal{R} interactions as well. In addition to maintaining the existing consistencies and predictions [6,7], our generalization predicts \mathcal{R} couplings that are within the level of phenomenological tolerance and lead to detectable signatures. In the present analysis we consider only the L -violating interactions and leave aside the B -violating ones.

In a nutshell, the flavor problem in a supersymmetric theory addresses the question of how to relate the flavor structure of the fermions and scalars to each other by the same symmetry principle. An approximate $U(2)$ symmetry, which after all descends from a strong breaking of $U(3)$, through the following stepwise breaking,

$$U(2) \xrightarrow{\epsilon} U(1) \xrightarrow{\epsilon'} 0, \quad (1)$$

has been shown, in the context of R -parity-conserving supersymmetry, to reproduce the observed patterns of masses and mixings, where ϵ and ϵ' are small dimensionless breaking parameters. The three generations of matter fields transform as $2 \oplus 1$, i.e., $\psi = \psi_a + \psi_3$ ($a=1,2$) and the ‘‘flavon’’ fields, whose vacuum expectation values (VEVs), after spontaneous breaking of flavor symmetry, order the mass hierarchies, have the representations ϕ^a , S^{ab} (symmetric tensor), and A^{ab} (antisymmetric tensor). The upper indices in flavons indicate a $U(1)$ charge opposite to that of ψ_a . The first step of breaking $U(2) \rightarrow U(1)$ is realized through $\langle \phi^2 \rangle \approx \langle S^{22} \rangle \approx \mathcal{O}(\epsilon)M$ (the other components vanish) and the second step $U(1) \rightarrow 0$ is achieved by $\langle A^{12} \rangle = -\langle A^{21} \rangle \approx \mathcal{O}(\epsilon')M$, where M is the cutoff of an effective theory. The same two small parameters, ϵ and ϵ' , are responsible for the near degeneracies of the squarks and slepton masses, leading to a ‘‘super-Glashow-Iliopoulos-Maiani (GIM)’’ mechanism. With $\epsilon \approx 0.02$ and $\epsilon' \approx 0.004$, all observed masses and mixing patterns are *qualitatively* well understood.

If we now assume that the *same* flavor symmetry is responsible also for an exact R parity, the strengths of the \mathcal{R} interactions are governed by ϵ and ϵ' . Do the magnitudes of ϵ and ϵ' , dictated by the fermion masses and mixings, inflict the desirable suppressions to the \mathcal{R} interactions so as to make the scenario phenomenologically viable? Before attempting to answer this question, we set up our notations that we follow hereafter. Recalling that H_d (the Higgs doublet superfield responsible for the masses of isospin $-1/2$ fermions) and L (the lepton doublet superfield) have identical gauge quantum numbers, the $\mu H_d H_u$ term in the superpotential can now be generalized to include three more similar terms; in compact notation,

$$\mu_\alpha L_\alpha H_u \quad (\alpha=0,i), \quad (2)$$

where $L_0 \equiv H_d$, $\mu_0 \equiv \mu$ and L_i ($i=1,2,3$) correspond to the three lepton flavors. One also has the following trilinear L -violating interactions in the superpotential:

$$\frac{1}{2} \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c, \quad (3)$$

*Permanent address: Saha Institute of Nuclear Physics, 1/AF Bidhan Nagar, Calcutta 700064, India.
E-mail address: gautam@mail.cern.ch

TABLE I. Upper limits on various product-couplings that scale as $(\tilde{m}/100 \text{ GeV})^2$, where \tilde{m} is the mass of the relevant scalar that is exchanged.

$\mu \rightarrow 3e$	$\lambda_{1j1}\lambda_{1j2}, \lambda_{231}\lambda_{131} \lesssim 7 \times 10^{-7}$	ϵ_K	$\text{Im } \lambda'_{i12}\lambda'_{i21} \lesssim 8 \times 10^{-12}$
Δm_K	$\lambda'_{i12}\lambda'_{i21} \lesssim 1 \times 10^{-9}$	Δm_B	$\lambda'_{i13}\lambda'_{i31} \lesssim 8 \times 10^{-8}$
$\mu\text{Ti} \rightarrow e\text{Ti}$	$\lambda'_{1k1}\lambda'_{2k1}, \lambda'_{11j}\lambda'_{21j} \lesssim 5 \times 10^{-8}$	$K_L \rightarrow \mu e$	$\lambda'_{1k1}\lambda'_{2k2} \lesssim 8 \times 10^{-7}$

where L_i and Q_j are lepton and quark doublet superfields and E_k^c and D_k^c are charged lepton and down quark singlet superfields; i, j, k run from 1 to 3. *A priori*, without any suppression (e.g., from a horizontal symmetry), the natural expectation is $\mu_i \sim \mathcal{O}(m_Z)$; $\lambda, \lambda' \sim \mathcal{O}(1)$ and during electroweak breaking $\langle \tilde{\nu}_i \rangle \sim \mathcal{O}(m_Z)$. But these overwhelmingly violate the laboratory upper limits of the neutrino (Majorana) masses [8] (all at 95% C.L.)

$$m_{\nu_e} \leq 15 \text{ eV}, \quad m_{\nu_\mu} \leq 170 \text{ keV}, \quad \text{and} \quad m_{\nu_\tau} \leq 24 \text{ MeV}, \quad (4)$$

and overshoot the stringent upper limits (indirect) on various combinations of λ and λ' couplings by many orders of magnitude. The most relevant and stringent constraints are shown in Table I. (For an extended list of product couplings, see Ref. [9], for example.) A way out of having naturally suppressed neutrino masses was suggested in Ref. [4] through a mechanism that approximately aligns μ_α with ν_α (the VEVs of the neutral scalars in L_α). A perfect alignment can be achieved if (i) the supersymmetry breaking $B_\alpha \propto \mu_\alpha$ and (ii) μ_α is an eigenvector of $\tilde{m}_{\alpha\beta}^2$, the soft scalar mass matrix that arises after supersymmetry breaking; even though misalignment creeps in through radiative corrections [10]. Breaking an Abelian horizontal U(1) symmetry, with charges appropriately chosen, was shown [4] to yield $m_{\nu_\tau} \leq 10 \text{ eV}$ (a hot dark matter candidate) and generate the λ and λ' couplings with required suppressions so as not to violate any experimental constraint.

How does an approximate U(2) symmetry fare to achieve the desired goal? Since with a non-Abelian horizontal symmetry the theory is much more constrained than with U(1), the task is much more challenging and, as we will see below, it faces unavoidable experimental obstructions, yet gives hints for how to generalize and search for a plausible solution. The \mathcal{R} bilinear and trilinear terms in the superpotential can be obtained by appropriately contracting the superfields appearing in Eqs. (2) and (3) with the flavons. Given the flavon representations and the hierarchy of their VEVs during the stepwise breaking of U(2) down to nothing as mentioned earlier, the order of magnitude of the \mathcal{R} couplings are given by (to their leading order),¹

μ_i terms:

$$\mu_1 \sim 0, \quad \mu_2 \sim \epsilon \mu, \quad \mu_3 \sim \mu; \quad (5)$$

λ_{ijk} couplings:

$$(121), (131), (133) \sim 0,$$

$$(123), (132), (231) \sim \epsilon',$$

$$(232), (233) \sim \epsilon, \quad (122) \sim \epsilon' \epsilon; \quad (6)$$

λ'_{ijk} couplings:

$$(111)', (121)', (131)', (112)', (113)', (133)', (211)',$$

$$(311)', (331)', (313)' \sim 0,$$

$$(123)', (132)', (231)', (213)', (321)', (312)' \sim \epsilon',$$

$$(122)', (221)', (212)' \sim \epsilon' \epsilon, \quad (7)$$

$$(223)', (232)', (233)', (322)', (323)', (332)' \sim \epsilon,$$

$$(222)' \sim \epsilon^2, \quad (333)' \sim 1.$$

There are two major phenomenological obstacles in the above formulation. First, $\langle \tilde{\nu}_\tau \rangle$ and $\mu_3 \sim m_Z$, while neutrino-neutralino mixings constrain them to be $\leq \sqrt{m_{\nu_\tau} m_Z} \lesssim 1 \text{ GeV}$ (assuming $\mu \sim m_Z$) and second, $\lambda'_{321}\lambda'_{312} \sim \epsilon'^2 \sim 10^{-5}$ and $\lambda'_{231}\lambda'_{213} \sim \epsilon'^2 \sim 10^{-5}$ exceeding the constraints from Δm_K and Δm_B (see Table I) by a few orders of magnitude.²

The above difficulties are unrepairable and strongly suggest towards the consideration of U(3), the ultimate flavor symmetry. However, U(3) has to be ‘‘strongly’’ broken to account for the heavy top quark. On the other hand, the failure with U(2) guides us to the necessity of having an additional suppression factor for the third generation lepton superfield during U(3) \rightarrow U(2) solving the ‘‘ μ_3 -problem,’’ that is also expected to inflict suppressions in the U(2)- and U(1)-breaking parameters curing the product-couplings’ overshooting. So in the lepton sector U(3) needs to be ‘‘weakly’’ broken. Then how about treating leptons and quarks differently in flavor space?³

Following the above line of arguments, we consider the flavor symmetry U(3)_l \otimes U(3)_q, where lepton and quark su-

¹All \mathcal{R} couplings involve flavor indices in the weak basis. For our order of magnitude estimates, a distinction between the weak basis and the mass basis is not important.

²The contribution to ϵ_K vanishes as $\lambda'_{i12} = -\lambda'_{i21}$ following from the antisymmetric nature of A flavons.

³This is indeed against the idea of unification, but nevertheless a viable option.

perfields transform under different unitary groups. $U(3)_q$ is anyhow strongly broken to $U(2)_q$. The complete breaking configuration is

$$U(3)_l \otimes U(3)_q \xrightarrow{*} U(3)_l \otimes U(2)_q \xrightarrow{\epsilon_{3l}} U(2)_l \otimes U(2)_q \xrightarrow{\epsilon_l, \epsilon'} U(1)_l \otimes U(1)_q \rightarrow 0, \quad (8)$$

where the asterisk indicates a strong breaking of $U(3)_q$. A triplet flavon $\tilde{\phi}_i$, with VEV assignments $\langle \tilde{\phi}_3 \rangle = \epsilon_{3l}$, $\langle \tilde{\phi}_2 \rangle = \langle \tilde{\phi}_1 \rangle = 0$, breaks $U(3)_l$ to $U(2)_l$. The subsequent breaking of $U(2)_q$ and $U(2)_l$ are assisted by the VEVs of two different sets of flavon fields (one for quarks and the other for leptons) which are straightforward three-dimensional extensions of the ϕ , S , and A fields introduced in the context of a general $U(2)$ having analogous VEV patterns. For those VEVs related to the lepton sector we assign a suffix l .

Before proceeding further, we must first ensure that the observed fermion masses and mixings are successfully reproduced. A crucial assumption at this point is called for that, instead of one pair, there are two pairs of Higgs doublet superfields. Considering the two H_d -type Higgs superfields, we assume that one (H_d^l) couples only to leptons and the other (H_d^q) only to quarks and there is a nontrivial mixing between them. The physical state that acquires a VEV during electroweak breaking is assumed to be the one that dominantly couples to the leptons and is given by

$$H_d \approx H_d^l + \xi H_d^q, \quad (9)$$

while the orthogonal state (assumed too heavy) does not acquire any VEV. The mass matrices of the charged leptons and the down quarks assume the following form:

$$\mathcal{M}_l = \begin{pmatrix} 0 & \epsilon'_l & 0 \\ -\epsilon'_l & \epsilon_l & \epsilon_l \\ 0 & \epsilon_l & \epsilon_{3l} \end{pmatrix} v_d, \quad \mathcal{M}_d = \begin{pmatrix} 0 & \epsilon' & 0 \\ -\epsilon' & \epsilon & \epsilon \\ 0 & \epsilon & 1 \end{pmatrix} \xi v_d. \quad (10)$$

The mixing angle ξ is adjusted as $\xi \approx \epsilon_{3l} m_b / m_\tau$. Choosing $v_d = v / \sqrt{2} \approx 174$ GeV (where v is the standard model VEV), we obtain $\epsilon_{3l} \approx m_\tau / v_d \approx 0.01$, $\epsilon_l \approx \epsilon_{3l} m_\mu / m_\tau \approx 6.10^{-4}$, $\epsilon'_l \approx \epsilon_l \sqrt{m_e / m_\mu} \approx 4.10^{-5}$, $\epsilon \approx m_s / m_b \approx 0.03$, and $\epsilon' \approx \epsilon \sqrt{m_d / m_s} \approx 9.10^{-3}$. Note that a “strong” breaking of $U(3)_q$ keeps the values of ϵ and ϵ' the same as in a general $U(2)$ hypothesis; thus all the consistencies and observable predictions of the latter related to B and K physics [7] automatically apply to our scenario.⁴ On the contrary, a “weak” breaking of $U(3)_l$ inflicts a suppression of 2 orders of magnitude in the (33)-element of the charged lepton Yukawa

matrix that is fed to μ_3 and the $U(2)$ - and $U(1)$ -breaking parameters in the lepton sector; we will see later that quantitatively these fit to our requirement. The role of Higgs-mixing is obvious now: despite the “strong” breaking of $U(3)_q$ *vis-a-vis* the “weak” breaking of $U(3)_l$, it pulls m_b relative to m_t sufficiently low as to place it close to m_τ .

Now we are all set to check the consistencies as regards the \mathcal{R} couplings. First, we present the order of magnitude estimates of μ_i , λ_{ijk} and λ'_{ijk} (to their leading order) in the present scenario. μ_i terms:

$$\mu_1 \sim 0, \quad \mu_2 \sim \epsilon_l \mu, \quad \mu_3 \sim \epsilon_{3l} \mu; \quad (11)$$

λ_{ijk} terms:

$$(121), (131), (133) \sim 0,$$

$$(123), (132), (231) \sim \epsilon'_l \epsilon_{3l},$$

$$(232), (233) \sim \epsilon_l \epsilon_{3l}, (122) \sim \epsilon'_l \epsilon_l; \quad (12)$$

λ'_{ijk} terms:

$$(1jk)', (211)', (231)', (213)', (311)', (331)', (313)' \sim 0,$$

$$(221)', (212)' \sim \epsilon_l \epsilon', \quad (233)' \sim \epsilon_l,$$

$$(222)', (223)', (232)' \sim \epsilon_l \epsilon, \quad (321)', (312)' \sim \epsilon_{3l} \epsilon',$$

$$(322)', (323)', (332)' \sim \epsilon_{3l} \epsilon \quad (333)' \sim \epsilon_{3l}. \quad (13)$$

By putting values of the breaking parameters and comparing the predictions for the various product-couplings with their experimental upper limits, we observe that the compatibility has improved considerably compared to the $U(2)$ scenario. The prediction $\lambda'_{321} \lambda'_{312} \sim 7 \times 10^{-9}$ is in a marginally tight position with respect to the limit from Δm_K . But the entries in the Yukawa matrices are always subject to $\mathcal{O}(1)$ uncertainties that one can exploit to stretch the breaking parameters for accommodating the above constraint. The ϵ_K constraint is trivially satisfied as in the case of a general $U(2)$. The other constraints (including those which are not listed in Table I) are comfortably satisfied.⁵

Now we turn our attention to the issue of neutrino mass and its decay. Neutrino mass arises due to neutrino-neutralino mixings (photino is irrelevant in the context of neutrino mass) and in the basis $(\tilde{L}_\alpha^0, \tilde{H}_u^0, \tilde{Z})$ has the following form ($g_W = g/2 \cos \theta_W$ and a tilde on a superfield denotes its fermionic component):

$$\mathcal{M}_n = \begin{pmatrix} 0_{4 \times 4} & \mu_\alpha & g_W v_\alpha \\ \mu_\alpha & 0 & -g_W v_u \\ g_W v_\alpha & -g_W v_u & m_{\tilde{Z}} \end{pmatrix}, \quad (14)$$

⁴Indeed, $\mu \rightarrow e\gamma$ is suppressed in our case by several orders of magnitude compared to its observation level prediction in the $U(2)$ scenario [7].

⁵As a matter of principle, one should check the consistencies with experimental results by expressing all λ and λ' couplings with indices in their physical basis. But we have checked, as in the $U(2)$ -case mentioned earlier, that this does not change the conclusions drawn above.

where $v_u = \langle H_u^0 \rangle$. The zeros in the first (4×4) block can be lifted by nonrenormalizable terms in the superpotential of the form $LLH_u H_u / M$, which of course can be arranged to have a negligible correction assuming $M \gg m_Z$. The above (6×6) matrix has two zero eigenvalues that can be identified with the physical ν_e and ν_μ masses, while the physical ν_τ is massive and its mass is determined by the extent to which v_3 is misaligned with μ_3 (neglecting, for the sake of simplicity, the misalignment between v_2 and μ_2 which turns out to be much smaller: recall that with perfect alignment of all v_α with their corresponding μ_α , all the neutrinos are massless⁶). Assuming for an illustration (good enough for an order of magnitude estimate) that B is universal and the origin of a possible misalignment is only an off-diagonal entry $\Delta m^2 = \tilde{m}_{H_d L_3}^2$ in the scalar lepton mass matrix, an explicit scalar potential minimization yields

$$v_3 = \kappa \mu_3 + \kappa' v_d, \quad (15)$$

where $\kappa = B v_u / \tilde{m}^2$ and $\kappa' = \Delta m^2 / \tilde{m}^2$ (\tilde{m} is a common diagonal soft scalar mass). It also follows from the scalar potential minimization that to a very good approximation $v_d \approx \kappa \mu$. Therefore, a nonzero κ' is responsible for the deviation from $v_\alpha \propto \mu_\alpha$ alignment giving rise to a neutrino mass. Now, ν_τ mass is obtained by taking the ratio of the determinant of the (4×4) mass matrix [in the $(\nu_\tau, \tilde{H}_d^0, \tilde{H}_u^0, \tilde{Z})$ basis] to the determinant of the (3×3) mass matrix [in the $(\tilde{H}_d^0, \tilde{H}_u^0, \tilde{Z})$ basis]. The leading behavior turns out to be

$$m_{\nu_\tau} \sim \frac{g^2}{4 \cos^2 \theta_W} \frac{\epsilon_{3l}^2 v_d^2}{m_{\tilde{Z}}}, \quad (16)$$

where we have used $\Delta m^2 \approx \epsilon_{3l} \tilde{m}^2$ following from $U(3)_l$ breaking. Thus for $m_{\tilde{Z}} \sim v_d$, $m_{\nu_\tau} \sim \mathcal{O}(1 \text{ MeV})$ lying in the range of detectability, for example, at a tau-charm factory [11].

However, this massive ν_τ is not stable and before we discuss its decay properties, a few remarks on the cosmological constraints that apply on it are in order [12]. The age and the present energy density of the universe restricts the lifetime of a 1 MeV ν_τ to be less than $\sim 10^8$ s. A stronger constraint (lifetime less than $\sim 10^3$ s) follows from the requirement that ν_τ should decay before the recombination time ($t_{\text{rec}} \lesssim 10^{-5} t_U$, where t_U is the age of the universe being 10^{10} y), i.e., when matter could start forming. The nucleosynthesis upper bound on the lifetime of a 1 MeV neutrino is $\sim 10^2$ s, unless it has additional annihilation channels besides those in the standard model. When the dominant decays are

in visible channels (e.g., radiative decays), practically all otherwise allowed neutrino masses are excluded.⁷

Within our framework, ν_τ has three types of decay modes.

(i) Invisible decay $\nu_\tau \rightarrow \nu_\mu f$, where f is a familon [13,14] [a massless Nambu-Goldstone boson arising from the breaking of the family symmetry $U(3)_l$]. The effective operator $LLH_u H_u / M$ induces this decay (recall that a familon does not carry any overall lepton number) and the loop-driven decay graph involves two \mathcal{R} Yukawa couplings (e.g., λ'_{333} and λ'_{233}) generating $\Delta L = 2$.

(ii) Invisible decay to three light neutrinos, $\nu_\tau \rightarrow 3\nu$ (Z mediated), following from the frustration of the GIM mechanism due to neutrino-zino mixing.⁸

(iii) Visible radiative decay $\nu_\tau \rightarrow \nu_\mu + \gamma$, induced by λ'_{333} and λ'_{233} (for example). For superparticle masses around 100 GeV, the lifetime in channel (i) is $\sim 10^{16}$ s with $V \sim 6.10^9$ GeV [global $U(3)_l$ breaking scale⁹] while the lifetimes in channels (ii) and (iii) are $\sim 10^{12} - 10^{13}$ s. It should be noted though that the lack of finding a fast enough decay channel of a massive neutrino is a somewhat generic problem that has been noticed in the past in different contexts [12,16]. We observe that we cannot advance any solution to this general problem in a scenario where approximate non-Abelian horizontal symmetries have been assumed to control *both* the \mathcal{R} Yukawa couplings and the structure of the supersymmetry breaking soft terms.

If we instead assume that family symmetries govern *only* the Yukawa couplings through their hierarchical breaking and do not control the structure of the soft masses at the supersymmetry breaking scale (Λ_U), this indeed results in a loss of generality. But this is aimed to avoid the difficulties related to the rather long lifetime of the massive neutrino by bringing its mass below 100 eV making it cosmologically stable [12]. Let us assume the following: (i) soft terms are universal at Λ_U , i.e., $\tilde{m}_{\alpha\beta}^2 = \tilde{m}^2 \delta_{\alpha\beta}$, (ii) $B_\alpha = B \mu_\alpha$, and finally (iii) the supersymmetric μ parameter is nonzero in only one direction, namely, $\mu_\alpha L_\alpha H_u \equiv \mu H_d H_u$: this is not unjustified as there is an in-built distinction between H_d and L_i , since the former is a singlet under family group while the latter transforms under $U(3)_l$. Assumption (iii) therefore relies on a property of the theory that its superpotential could sense that distinction and chooses the ‘‘singlet direction’’ for the μ term. Still a question remains: even if one starts with a universal boundary condition on the scalar masses at Λ_U , how much sneutrino-Higgs mixing is generated by renormalization group (RG) running of the soft parameters down to low energy? Singling out the dominant effects, an approximate (nevertheless quite reasonable for an order of magnitude estimate) expression of the mass of ν_τ induced by such misalignment is obtained as [10,17]

⁶That the three light neutral fermions (two massless and one massive at tree level) *do* correspond to the three physical neutrinos, is ensured by a simultaneous study of the charged fermion mass matrix. For a discussion of how to appreciate this aspect through basis transformations of neutral and charged fermions, see Refs. [4,10]. In our case, because of the hierarchical nature of the VEVs of family symmetry breaking, the neutrino that becomes massive turns out to be *dominantly* ν_τ . Indeed, higher order effects finally turn the massless states into massive ones: we ignore those effects here.

⁷See e.g., Fig. 2 of Gelmini and Roulet in Ref. [12].

⁸Charged lepton-chargino mixing will trigger flavor-changing Z decays into light leptons, $Z \rightarrow l_i \bar{l}_j$, the rates of which, we have checked, are much below their experimental upper limits [8].

⁹This lower limit follows from the nonobservation of the $\mu \rightarrow e f$ decay [15].

$$m_{\nu_\tau}^{\text{RG}} \sim \frac{g^2}{4 \cos^2 \theta_w} \frac{v_d^2}{m_Z} \left[\frac{3t_U m_b}{8\pi^2 v} \right]^2 \left(3 + \frac{A^2}{\tilde{m}^2} + \frac{A}{B} \right)^2 \lambda_{333}^{\prime 2}, \quad (17)$$

where $t_U = \ln(\Lambda_U/m_Z)$ and A is the universal trilinear soft parameter at Λ_U . By comparing Eqs. (16) and (17) one obtains an idea of the relative sizes of the RG-induced effect on the neutrino mass and the $U(3)_I$ -breaking contribution discussed earlier. Let us consider, for the sake of simplicity and illustration, $A \ll \tilde{m}, B$. Then, (i) for $\Lambda_U = 10^{16}$ GeV, $m_{\nu_\tau}^{\text{RG}}$ is at the level of a few keV and (ii) for $\Lambda_U = 10^5$ GeV, $m_{\nu_\tau}^{\text{RG}}$ is $\mathcal{O}(100 \text{ eV})$. In case (i), even by exploiting the $\mathcal{O}(1)$ uncertainty in $\lambda_{333}^{\prime 2}$, it is difficult to bring the neutrino mass below 100 eV for natural choices of soft parameters, while in case (ii), which corresponds to low energy gauge-mediated supersymmetry breaking [18], there is more breathing space to accomplish it mainly because of less RG running.¹⁰ At this level it becomes important to evaluate the one-loop contribution to the neutrino mass induced by (dominantly) the $\lambda_{333}^{\prime 2}$ coupling. The leading term reads [19]

$$m_{\nu_\tau}^{\text{loop}} \approx \frac{3m_b m_{\text{LR}}^2}{8\pi^2 \tilde{m}^2} \lambda_{333}^{\prime 2}, \quad (18)$$

where assuming the left-right squark mixing $m_{\text{LR}}^2 = m_b \tilde{m}$, we obtain, for $\tilde{m} = 100$ GeV, $m_{\nu_\tau}^{\text{loop}} \sim 1$ keV. Again, it is possible to arrange the squark masses and mixings and/or ϵ_{3l} scaling such that $m_{\nu_\tau}^{\text{loop}}$ becomes $\mathcal{O}(100 \text{ eV})$. It is noteworthy that for low energy supersymmetry breaking $m_{\nu_\tau}^{\text{RG}}$ be-

¹⁰In gauge-mediated models, the soft masses are not universal but flavor symmetric and so our conclusions remain unaffected.

comes comparable or even less than $m_{\nu_\tau}^{\text{loop}}$, while for $\Lambda_U \sim 10^{16}$ GeV the dominant contribution comes from misalignment. In any case, we have exhibited that it is possible to design a scenario (particularly with gauge-mediated supersymmetry breaking) reconciling R -parity violation with conventional flavor physics that, in addition to having passed the laboratory tests, is also cosmologically viable.

In the scenario discussed above, the cosmologically stable neutrinos are hot dark matter candidates. Axions, that have resulted from breaking non-Abelian, continuous, and global family symmetries, could constitute cosmologically interesting cold dark matter [5]. The other candidates for cold dark matter in R -parity-conserving supersymmetry are neutralinos, which are not stable here in cosmological scales. Given the predictions of the R couplings in Eqs. (12) and (13), the most striking collider signatures of this scenario are (i) [if the lightest neutralino is the lightest supersymmetric particle (LSP)] like-sign di-muon final states [20] from LSP decays after a rather long flight (~ 1 m) close to the detector edge and (ii) [in the sneutrino-LSP scenario] $\tilde{\nu}_\tau$ decaying to two jets inside the detector through λ_{3ij}^{\prime} couplings [21]. We note in passing that the particular couplings (λ_{1j1}^{\prime}) relevant to explain the recent anomaly at the DESY ep collider HERA [22] are vanishing in our case and so if those anomalous events turn out to be real in future, they cannot be explained within our framework. In any case, if R -parity violation turns out to be a true feature of nature, we believe that its possible ancestral link with masses and mixings could constitute a complete theory of flavor. Our effort is an attempt in that direction.

I thank Riccardo Barbieri for suggesting the problem and for helping and encouraging me at every stage of the work, Andrea Romanino for a critical reading of the manuscript and Rabi Mohapatra for a discussion on cosmological constraints on neutrino decays.

-
- [1] G. Farrar and P. Fayet, Phys. Lett. **76B**, 575 (1978).
[2] S. Weinberg, Phys. Rev. D **26**, 287 (1982); N. Sakai and T. Yanagida, Nucl. Phys. **B197**, 533 (1982); C. Aulakh and R. Mohapatra, Phys. Lett. **119B**, 136 (1982).
[3] L. Hall and M. Suzuki, Nucl. Phys. **B231**, 419 (1984); J. Ellis *et al.*, Phys. Lett. **150B**, 142 (1985); G. Ross and J. Valle, *ibid.* **151B**, 375 (1985); S. Dawson, Nucl. Phys. **B261**, 297 (1985); S. Dimopoulos and L. Hall, Phys. Lett. B **207**, 210 (1987).
[4] T. Banks, Y. Grossman, E. Nardi, and Y. Nir, Phys. Rev. D **52**, 5319 (1995).
[5] R. Barbieri, G. Dvali, and L. Hall, Phys. Lett. B **377**, 76 (1996); R. Barbieri and L. Hall, Nuovo Cimento A **110**, 1 (1997).
[6] R. Barbieri, L. Hall, S. Raby, and A. Romanino, Nucl. Phys. **B493**, 3 (1997).
[7] R. Barbieri, L. Hall, and A. Romanino, Phys. Lett. B **401**, 47 (1997).
[8] Particle Data Group, R. M. Barnett *et al.*, Phys. Rev. D **54**, 1 (1996).
[9] D. Choudhury and P. Roy, Phys. Lett. B **378**, 153 (1996); a

- limit $\lambda_{131}^{\prime} \lambda_{113}^{\prime} \lesssim 3.10^{-8}$ (for $\tilde{m} = 100$ GeV) from the consideration of neutrinoless double beta decay has been derived by K. Babu and R. Mohapatra, Phys. Rev. Lett. **75**, 2276 (1995).
[10] E. Nardi, Phys. Rev. D **55**, 5772 (1997).
[11] J. Kirkby, in *Results and Perspectives in Particle Physics, Proceedings of the 10th Les Rencontres de Physique de la Vallée d'Aoste*, La Thuile, Italy, 1996, edited by M. Greco (INFN, La Thuile, 1996), pp. 747–788.
[12] For reviews, see G. Gelmini and E. Roulet, Rep. Prog. Phys. **58**, 1207 (1995); S. Sarkar, *ibid.* **59**, 1493 (1996); R. Mohapatra and P. Pal, *Massive Neutrinos in Physics and Astrophysics* (World Scientific, Singapore, 1991). For a recent analysis of nucleosynthesis constraints, see K. Kainulainen, hep-ph/9608215.
[13] F. Wilczek, Phys. Rev. Lett. **49**, 1549 (1982).
[14] G. Gelmini, S. Nussinov, and R. Peccei, Int. J. Mod. Phys. A **7**, 3141 (1992); R. Barbieri and L. Hall, Nucl. Phys. **B364**, 27 (1991); B. Grinstein, J. Preskill, and M. Wise, Phys. Lett. **159B**, 57 (1985).

- [15] G. D'Ambrosio and G. Gelmini, *Z. Phys. C* **35**, 461 (1987), and references therein.
- [16] F. Borzumati, Y. Grossman, E. Nardi, and Y. Nir, *Phys. Lett. B* **384**, 123 (1996).
- [17] A. Joshipura, V. Ravindran, and S. Vempati, hep-ph/9706482; B. de Carlos and P. White, *Phys. Rev. D* **54**, 3427 (1996). For a general discussion of neutrino masses in supersymmetric theories without R -parity, see R. Hempfling, *Nucl. Phys. B* **478**, 3 (1996); H. Nilles and N. Polonsky, *ibid.* **484**, 33 (1997).
- [18] M. Dine and A. Nelson, *Phys. Rev. D* **48**, 1277 (1993); M. Dine, A. Nelson, and Y. Shirman, *ibid.* **51**, 1362 (1995); M. Dine, A. Nelson, Y. Nir, and Y. Shirman, *ibid.* **53**, 2658 (1996); L. Alvarez-Gaumé, M. Claudson, and M. Wise, *Nucl. Phys. B* **207**, 96 (1982); S. Dimopoulos, M. Dine, S. Raby, and S. Thomas, *Phys. Rev. Lett.* **76**, 3494 (1996); S. Ambrosanio, G. Kane, G. Kribs, S. Martin, and S. Mrenna, *ibid.* **76**, 3498 (1996); K. Babu, C. Kolda, and F. Wilczek, *ibid.* **77**, 3070 (1996).
- [19] R. Godbole, P. Roy, and X. Tata, *Nucl. Phys. B* **401**, 67 (1993).
- [20] M. Guchait and D. P. Roy, *Phys. Rev. D* **54**, 3276 (1996).
- [21] V. Barger, W. Keung, and R. Phillips, *Phys. Lett. B* **364**, 27 (1995).
- [22] H1 Collaboration, C. Adloff *et al.*, *Z. Phys. C* **74**, 191 (1997); ZEUS Collaboration, J. Breitweg *et al.*, *ibid.* **74**, 207 (1997).