Flavor-changing top quark decay within the minimal supersymmetric standard model

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We present the results of the gluino and scalar quark contribution to the flavor-changing top quark decay into a charm quark and a photon, gluon, or a Z^0 boson within the minimal supersymmetric standard model. We include the mixing of the scalar partners of the left- and right-handed top quark. This mixing has several effects, the most important of which is to greatly enhance the cZ decay mode for large values of the soft SUSY-breaking scalar mass m_S and to give rise to a GIM-like suppression in the $c\gamma$ mode for certain combinations of parameters.

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Recent experimental evidence of the top quark [1] makes its rare decay modes a promising test ground for the standard model (SM) and physics beyond the SM. The flavor-changing decay mode of the top quark was calculated within the SM in [2-6] and their branching ratios were shown to be $\sim 10^{-12}$ for $t \rightarrow c\gamma$, $\sim 10^{-12}$ -10⁻¹³ for $t \to cZ$ and $\sim 10^{-10}$ for $t \to cg$ in the top mass range 90-200 GeV, thus far away from experimental reach; this makes it an excellent probe for models beyond the SM. Two-Higgs-doublet models (THDM's) were considered in [6,7], where it was shown that the decay rate is enhanced by several (3-4) orders of magnitude. Recently [8], the $t \rightarrow cV$ decay was considered within the minimal supersymmetric SM (MSSM) and the authors obtained the same enhancement as in the THDM's. However they did not include the mixing of the scalar partners of the leftand right-handed top quark; they omitted one diagram

$$M_{ ilde{t}}^2 = \left(egin{array}{c} m_{ ilde{t}_L}^2 + m_{ ext{top}}^2 + 0.35 D_Z^2 & -m_{ ext{top}} \ -m_{ ext{top}} (A_{ ext{top}} + \mu \coteta) & m_{ ilde{t}_R}^2 + m_{ ext{top}}^2 + m_{ ext{$$

where $D_Z^2 = m_Z^2 \cos 2\beta$, $m_{\tilde{t}_{L,R}}^2$ are soft sypersymmetry-(SUSY-) breaking masses, $A_{\rm top}$ is a trilinear scalar interaction parameter, and μ is the supersymmetric mass mixing term of the Higgs bosons. The mass eigenstates \tilde{t}_1 and \tilde{t}_2 are related to the current eigenstates \tilde{t}_L and \tilde{t}_R by

$$\tilde{t}_1 = \cos\Theta_t \tilde{t}_L + \sin\Theta_t \tilde{t}_R, \ \ \tilde{t}_2 = -\sin\Theta_t \tilde{t}_L + \cos\Theta_t \tilde{t}_R.$$
 (2)

In the following we take $m_{\tilde{t}_L} = m_{\tilde{t}_R} = m_S = A_{\rm top}$ (global SUSY). The gluino mass $m_{\tilde{g}}$ is a free parameter, which in general is supposed to be larger than 100 GeV, although there is still the possibility of a small gluino mass window in the order of 1 GeV [17,18].

To calculate the one-loop diagrams shown in Fig. 1 we

in the cg decay mode and their current was not gauge invariant.

In this paper we present the supersymmetric QCD loop corrections to the $t \rightarrow cV$ decay in the MSSM with gluinos and scalar quarks running on the loop, as shown in Fig. 1. Throughout the calculation we neglect all quark masses other than the top quark mass and include the mixing of the scalar partners of the left- and right-handed top quark, which is proportional to the top quark mass.

In supersymmetric QCD it was shown that there occur flavor-changing strong interactions between the gluino, the left-handed quarks, and their supersymmetric scalar partners, whereas the couplings of the gluino to the righthanded quarks and their partners remains flavor diagonal [10–16]. Since the mixing of \tilde{t}_L and \tilde{t}_R is proportional to the top quark mass we have to include the full scalar top quark matrix which is given by [9]

$$\begin{array}{l} -0.35D_Z^2 & -m_{\rm top}(A_{\rm top} + \mu \cot\beta) \\ -\mu \cot\beta) & m_{\tilde{t}_R}^2 + m_{\rm top}^2 + 0.16D_Z^2 \end{array} \right) , \tag{1}$$

need the couplings of the gluon to the gluinos, of the scalar partners of the left-handed quarks to the gluon, photon, and Z^0 boson, and of the gluino to the left-handed quark and its scalar partner. The first one¹ is given by Eq. (C92) in [19]:

$$\mathcal{L}_{g\tilde{g}\tilde{g}} = \frac{i}{2} g_s f_{abc} \overline{\tilde{g}_a} \gamma_\mu \tilde{g}_b G_c^\mu, \tag{3}$$

which is multiplied by 2 to obtain the Feynman rules. The interactions of the gluon, photon, and the Z^0 boson with squark are given by Eqs. (6)-(8) in [9]:

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¹In order to shorten the notation we will use $\cos\Theta = c_{\Theta}$, $\sin\Theta = s_{\Theta}$, and $s_W = \sin\Theta_W$, where Θ_W is the weak mixing angle.

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FIG. 1. The diagrams with scalar quarks and gluinos within the loop, which contribute to the top quark decay into a charm quark and a Z boson, photon, or gluon.

$$\mathcal{L}_{\tilde{q}\tilde{q}V} = -ieA^{\mu} \sum_{i=L,R} e_{q_i} \tilde{q}_i^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_i$$
$$-\frac{ie}{s_W c_W} Z^{\mu} \sum_{i=L,R} \left(T_{3q_i} - e_{q_i} s_W \right) \tilde{q}_i^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_i$$
$$-ig_s T^a G^{a\mu} \sum_{i=L,R} \tilde{q}_i^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_i.$$
(4)

After the introduction of nontrivial squark mixing this becomes

$$\mathcal{L}_{\tilde{q}\tilde{q}V} = -ieA^{\mu} \sum_{i=1,2} e_{q_i} \tilde{q}_i^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_i - ig_s T^a G^{a\mu} \sum_{i=1,2} \tilde{q}_i^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_i$$
$$-\frac{ie}{s_W c_W} Z^{\mu} [(T_{3L} c_{\Theta}^2 - e_q s_W^2) \tilde{q}_1^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_1$$
$$+ (T_{3L} s_{\Theta}^2 - e_q s_W^2) \tilde{q}_2^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_2$$
$$- T_{3L} c_{\Theta} s_{\Theta} (\tilde{q}_1^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_2 + \tilde{q}_2^* \overleftrightarrow{\partial}_{\mu} \tilde{q}_1)].$$
(5)

Finally the coupling that leads to flavor changing is given in Eq. (1) in [16]:

$$\mathcal{L}_{\rm FC} = -\sqrt{2}g_s T^a K \overline{\tilde{g}} P_L q(c_{\Theta} \tilde{q}_1 - s_{\Theta} \tilde{q}_2) + \text{H.c.}$$
(6)

Here K is the supersymmetric version of the Kobayashi-Maskawa matrix whose form will appear later. Flavorchanging couplings occur only in the left-handed scalar quark sector; the right-handed sector does not contribute to our process.

After summation over all diagrams, we obtain the following effective tcV vertex:

$$M^{\alpha}_{\mu V} = -i \frac{\alpha_s}{2\pi} K_{\alpha t} K_{\alpha c} \bar{u}_{p_2} \left(\gamma_{\mu} P_L V^{\alpha}_V + \frac{P_{\mu}}{m_{\rm top}} P_R T^{\alpha}_V \right) u_{p_1},$$
(7)

$$\begin{split} V_{\gamma}^{\alpha} &= ee_q C_2(F) [c_{\Theta_{\alpha}}^2 (C_{\epsilon}^{11\alpha} - C_{SE}^{1\alpha}) + s_{\Theta_{\alpha}}^2 (C_{\epsilon}^{22\alpha} - C_{SE}^{2\alpha})], \\ T_{\gamma}^{\alpha} &= ee_q C_2(F) [c_{\Theta_{\alpha}}^2 C_{top}^{11\alpha} + s_{\Theta_{\alpha}}^2 C_{top}^{22\alpha}], \\ V_g^{\alpha} &= g_s T^a \{ [-\frac{1}{2} C_2(G) + C_2(F)] [c_{\Theta_{\alpha}}^2 C_{\epsilon}^{11\alpha} + s_{\Theta_{\alpha}}^2 C_{\epsilon}^{22\alpha}] \\ &- C_2(F) [c_{\Theta_{\alpha}}^2 C_{SE}^{1\alpha} + s_{\Theta_{\alpha}}^2 C_{SE}^{22}] \\ &+ \frac{1}{2} C_2(G) \{ c_{\Theta_{\alpha}}^2 [C_{\epsilon}^{\tilde{g}1\alpha} + C_{\tilde{g}}^{1\alpha} + C_{q^2}^{1\alpha} + C_{t}^{1\alpha}] \\ &+ s_{\Theta_{\alpha}}^2 [C_{\epsilon}^{\tilde{g}2\alpha} + C_{\tilde{g}}^{2\alpha} + C_{q^2}^{2\alpha} + C_{t}^{2\alpha}] \}, \end{split}$$

$$\begin{split} T_g^{\alpha} &= g_s T^a \{ [-\frac{1}{2} C_2(G) + C_2(F)] [c_{\Theta_{\alpha}}^2 C_{\text{top}}^{11\alpha} + s_{\Theta_{\alpha}}^2 C_{\text{top}}^{22\alpha}] \\ &- \frac{1}{2} C_2(G) [c_{\Theta_{\alpha}}^2 C_t^{1\alpha} + s_{\Theta_{\alpha}}^2 C_t^{2\alpha}] \}, \end{split}$$

$$\begin{split} V_Z^{\alpha} &= \frac{e}{s_W c_W} C_2(F) \{ (T_{3L} C_{\Theta_{\alpha}}^2 - e_q s_W^2) c_{\Theta_{\alpha}}^2 C_{\epsilon}^{11\alpha} \\ &+ (T_{3L} s_{\Theta_{\alpha}}^2 - e_q s_W^2) s_{\Theta_{\alpha}}^2 C_{\epsilon}^{22\alpha} \\ &+ T_{3L} c_{\Theta_{\alpha}}^2 s_{\Theta_{\alpha}}^2 (C_{\epsilon}^{12\alpha} + C_{\epsilon}^{21\alpha}) \\ &- (T_{3L} - e_q s_W^2) [c_{\Theta_{\alpha}}^2 C_{SE}^{1\alpha} + s_{\Theta_{\alpha}}^2 C_{SE}^{2\alpha}] \}, \end{split}$$

$$\begin{split} T_Z^{\alpha} &= \frac{c}{s_W c_W} C_2(F) \{ (T_{3L} c_{\Theta_{\alpha}}^2 - e_q s_W^2) c_{\Theta_{\alpha}}^2 C_{\mathrm{top}}^{11\alpha} \\ &+ (T_{3L} s_{\Theta_{\alpha}}^2 - e_q s_W^2) s_{\Theta_{\alpha}}^2 C_{\mathrm{top}}^{22\alpha} \\ &+ T_{3L} c_{\Theta_{\alpha}}^2 s_{\Theta_{\alpha}}^2 (C_{\mathrm{top}}^{12\alpha} + C_{\mathrm{top}}^{21\alpha}) \}, \end{split}$$
$$C_{\epsilon}^{kl\alpha} &= \int^1 d\alpha_1 \int^{1-\alpha_1} d\alpha_2 \left(\frac{1}{\epsilon} - \gamma + \ln(4\pi\mu^2) - \ln(f_{kl}^{\alpha}) \right), \end{split}$$

$$\begin{split} & \int_{0}^{kl\alpha} \int_{0}^{1-\alpha_{1}} d\alpha_{2} \frac{m_{top}^{2} \alpha_{1}(1-\alpha_{1}-\alpha_{2})}{f_{kl}^{\alpha}}, \\ & C_{SE}^{k\alpha} = \int_{0}^{1} d\alpha_{1} \alpha_{1} \left(\frac{1}{\epsilon} - \gamma + \ln(4\pi\mu^{2}) - \ln(g_{k}^{\alpha})\right), \\ & C_{\epsilon}^{\tilde{g}k\alpha} = \int_{0}^{1} d\alpha_{1} \int_{0}^{1-\alpha_{1}} d\alpha_{2} \left(\frac{1}{\epsilon} - \gamma - 1 + \ln(4\pi\mu^{2}) - \ln(h_{k}^{\alpha})\right), \end{split}$$

$$\begin{split} C_{\tilde{g}}^{k\alpha} &= \int_0^1 d\alpha_1 \int_0^{1-\alpha_1} d\alpha_2 \frac{m_{\tilde{g}}^2}{h_k^{\alpha}}, \\ C_{q^2}^{k\alpha} &= \int_0^1 d\alpha_1 \int_0^{1-\alpha_1} d\alpha_2 \frac{q^2 \alpha_1 \alpha_2}{h_k^{\alpha}}, \end{split}$$

$$C_t^{k\alpha} = \int_0^1 d\alpha_1 \int_0^{1-\alpha_1} d\alpha_2 \frac{m_{\rm top}^2 \alpha_1 (1-\alpha_1-\alpha_2)}{h_k^{\alpha}}$$

$$egin{aligned} f^{lpha}_{m{k}m{l}} &= m^2_{m{ ilde g}} - (m^2_{m{ ilde g}} - m^2_{m{ ilde q}_{m{ ilde k}}})lpha_1 - (m^2_{m{ ilde g}} - m^2_{m{ ilde q}_{m{ ilde l}}})lpha_2 \ &- m^2_{m{top}}lpha_1(1-lpha_1-lpha_2) - q^2lpha_1lpha_2, \end{aligned}$$

$$egin{aligned} g^lpha_k &= m^2_{ ilde{g}} - (m^2_{ ilde{g}} - m^2_{ ilde{q}^lpha_k})lpha_1 - m^2_{ ext{top}}lpha_1(1-lpha_1), \ h^lpha_k &= m^2_{ ilde{q}^lpha_k} - (m^2_{ ilde{q}^lpha_k} - m^2_{ ilde{g}})(lpha_1+lpha_2) \ -m^2_{ ext{top}}lpha_1(1-lpha_1-lpha_2) - q^2lpha_1lpha_2, \end{aligned}$$

where $\epsilon = 2 - d/2$, $C_2(F) = \frac{4}{3}$, and $C_2(G) = 3$ for SU(3). If $\alpha \neq \text{top}$ we have $c_{\Theta_{\alpha}} = 1$. Using the spin-1 condition $[q_{\mu} = (p_1 - p_2)_{\mu} = 0]$ we can write $P_{\mu} = (p_1 + p_2)_{\mu} = 2p_{1\mu}$. $K_{\alpha q}$ is the SUSY-Kobayashi-Maskawa matrix whose form is $\begin{pmatrix} 1 & \varepsilon & \varepsilon^2 \end{pmatrix}$

$$K_{ij} = \begin{pmatrix} 1 & \varepsilon & \varepsilon \\ -\varepsilon & 1 & \varepsilon \\ -\varepsilon^2 & -\varepsilon & 1 \end{pmatrix} .$$
(8)

Here ε is a small number (not to be confused with the ϵ above) to be taken as $\varepsilon^2 = \frac{1}{4}$ [16,8]. It is straightforward at this point to verify that all divergent terms cancel exactly, without the Glashow-Iliopoulos-Maiani (GIM) mechanism.

A crucial test is also provided by the nature of the current. Using the identity

$$\bar{u}_{p_2} \frac{P^{\mu}}{m_{\text{top}}} P_R u_{p_1} \equiv \bar{u}_{p_2} \left(\gamma_{\mu} P_L + i \sigma_{\mu\nu} \frac{q^{\mu}}{m_{\text{top}}} P_R \right) u_{p_1}, \quad (9)$$

we can show that the quantity in front of the γ^{μ} term vanishes in the limit $q^2 \rightarrow 0$, as required by gauge invariance.

When summing over all scalar quarks within the loops the scalar up quark cancels out because of the unitarity of K_{ij} and with $K_{23} = -K_{32}$ the mass splitting of the scalar top quark and the scalar charm quark comes into account, which was taken to be $m_{\tilde{c}} = 0.9m_{\tilde{t}}$ in [8] and therefore too small for a top quark mass of 174 GeV. If all scalar quark masses would be the same, the decay rate of $t \to cV$ would be identical to 0. As a final result we obtain

$$\Gamma_{S}(t \to cV) = \frac{\alpha_{s}^{2}}{128\pi^{3}} m_{\rm top} \left(1 - \frac{m_{V}^{2}}{m_{\rm top}^{2}} \right)^{2} \varepsilon^{2} \\ \times \left[V_{V}^{2} \left(2 + \frac{m_{\rm top}^{2}}{m_{V}^{2}} \right) - 2V_{V}T_{V} \left(1 - \frac{m_{\rm top}^{2}}{m_{V}^{2}} \right) \right. \\ \left. - T_{V}^{2} \left(2 - \frac{m_{V}^{2}}{m_{\rm top}^{2}} - \frac{m_{\rm top}^{2}}{m_{V}^{2}} \right) \right],$$
(10)

where $V_V = V_V^{\tilde{t}} - V_V^{\tilde{c}}$ and $T_V = T_V^{\tilde{t}} - T_V^{\tilde{c}}$. For $V = \gamma$, g we have $V_V = -T_V$ and all terms containing m_V^2 are absent.

We define [6]

$$B(t \to cV) = \Gamma_S(t \to cV) / \Gamma_W(t \to bW^{\dagger}),$$

where

$$\Gamma_{W}(t \to bW^{+}) = \frac{\alpha}{16\sin^{2}\Theta_{W}} m_{top} \left(1 - \frac{m_{W^{+}}^{2}}{m_{top}^{2}}\right)^{2} \left(2 + \frac{m_{top}^{2}}{m_{W^{+}}^{2}}\right) .$$
(11)

Our input parameters are $m_{top} = 174$ GeV and the strong-coupling constant

$$lpha_s = 1.4675/\mathrm{ln}\left(rac{m_{\mathrm{top}}^2}{\Lambda_{\mathrm{QCD}}^2}
ight) = 0.107$$

with $\Lambda_{QCD} = 0.18$ GeV [6].

In Fig. 2, we present the branching ratio $B(t \rightarrow cZ)$ as a function of the scalar mass m_S for a gluino mass of 100 GeV. We see that without mixing, the branching



FIG. 2. The ratio Γ_S/Γ_W of the top quark decay into a charm quark and Z^0 boson as a function of the scalar mass m_S . The gluino mass was taken to be 100 GeV. The solid line is the unphysical case with no mixing ($\mu = 0 = A_{top}$) and $\tan\beta = 1$, the dotted line is the same case with $\tan\beta = 10$. The other cases are with mixing ($A_{top} = m_S$). The dashed lines are with $\mu = 100$ GeV and the dash-dotted ones with $\mu = 500$ GeV. The shorter ones are with $\tan\beta = 1$ and the longer ones with $\tan\beta = 10$.

ratio decreases rapidly with increasing scalar mass. The mixing has a drastic effect. It enhances the branching ratio by up to 5 orders of magnitude for large m_S . Higher values of $\tan\beta$ diminish the branching ratio. The gluino mass hardly affects the decay rate. Even for a small gluino mass of the order of 1 GeV the branching ratio remains of the same order.

In Fig. 3, we consider the same cases as in Fig. 2 but for $B(t \rightarrow cg)$. The effect of the mixing is not as drastic as in the previous case. It decreases the branching ratio generally by 1-2 orders of magnitude. This reduction is larger for larger scalar masses. Increasing $\tan\beta$ diminishes the branching ratio in general, an exception is the case $\mu = 100$ GeV and $m_{\tilde{g}} = 500$ GeV. Increasing the gluino mass diminishes the branching ratio by several orders of magnitude for lower values of the scalar mass whereas lower values of the gluino mass enhance the ratio. The shape of the figures remains the same.



FIG. 3. The same as Fig. 2 but for the decay of the top quark into a charm quark and a gluon.



FIG. 4. The same as in Fig. 2 but for the decay of the top quark into a charm quark and a photon. The solid line with a sharp dip corresponds to $\mu = 100$ GeV and $\tan\beta = 2$.

In Figs. 4 and 5, we consider the branching ratio $B(t \to c\gamma)$. We notice first that the effect of the mixing is rather small for small values of m_S . We also note that the sensitivity of the branching ratio to $\tan\beta$ is greatly increased. Third, one sees that the mixing generally reduces the branching ratio. This is true generally but might not hold for some regions of parameter space, as can be seen in Fig. 4, when some combinations of parameters can greatly increase the branching ratio. Most interesting, the mixing gives rise to a GIM-like suppression where the contribution of the top quark exactly cancels the contribution from the c quark. This dramatic cancellation is also seen in Fig. 4. Such a cancellation is not isolated as seen in^2 Fig. 5. We have tried many different combinations of μ and $m_{\tilde{q}}$ and we found a *rift* similar to the one visible in Fig. 5 with all the combinations. Such a cancellation does not occur for the gluon and Z decay modes. In the first case, the $g - \tilde{g} - \tilde{g}$ vertex spoils it while in the second case it seems to be $q^2 \neq 0$ that does it.

In this paper we presented the supersymmetric QCD one-loop correction to the flavor-changing decay rate

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FIG. 5. $\log_{10}(t \to c\gamma)$ as a function of m_S and $\tan\beta$ for $m_{\tilde{g}} = 100 \text{ GeV} = \mu$. The vertical scale is about the same as in Fig. 4.

 $t \to cV$. We have shown that the $t \to cZ$ decay rate is enhanced by several orders of magnitude compared to the standard model. If we include the mixing of the scalar partners of the top quark we do get a further enhancement and the decay rate remains relatively large for a very wide range of gluino and scalar masses. For the $t \to cg$ decay rate we have shown that the mixing generally reduces the branching ratio. Larger values for $\tan\beta$ also diminish the branching ratio. In the $t \to c\gamma$ decay mode, the most dramatic effect of this mixing is to give rise to a GIM-like cancellation for some combinations of parameters. It also reduces the branching ratio and greatly increases the sensitivity to $\tan\beta$.

One should keep in mind that within the MSSM there are other contributions to the decays that we considered. For example, one could have scalar down quarks and charginos or scalar up quarks and neutralinos as well as down quarks and the charged Higgs boson on the loop. Although these are suppressed by weak couplings, the latter might be equal in magnitude to the case examined in this paper due to the heavy top quark mass.

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²This figure is intended to give a very good idea of the global behavior but not to be read numerically.