

Direct CP violation in $b \rightarrow dJ/\psi$ decays

Isard Dunietz

Fermilab, P.O. Box 500, Batavia, Illinois 60510

João M. Soares

*Department of Physics, Carnegie Mellon University, Pittsburgh, Pennsylvania 15213
and TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia, Canada V6T 2A3*

(Received 7 December 1993)

We investigate the possibility of observing direct CP violation in self-tagging B -meson decays of the type $b \rightarrow dJ/\psi$. The CP asymmetry can be generated due to strong or electromagnetic scattering in the final state, or due to long distance effects. The first two contributions give asymmetries of a few $\times 10^{-3}$, in the standard model. The long distance effects are hard to estimate, but it cannot be excluded that they yield asymmetries of about 1%.

PACS number(s): 13.25.Hw, 11.30.Er, 12.15.Ff

The standard model (SM) predicts the existence of relative CP -odd phases between different B -meson decay amplitudes (direct CP violation). If two such amplitudes contribute coherently to a decay $B \rightarrow f$, they may generate a CP asymmetry

$$a_{CP} = \frac{\Gamma(B \rightarrow f) - \Gamma(\bar{B} \rightarrow \bar{f})}{\Gamma(B \rightarrow f) + \Gamma(\bar{B} \rightarrow \bar{f})}. \quad (1)$$

This type of asymmetry does not require mixing, and it can occur in self-tagging decay modes. These are decays such that $B \not\rightarrow \bar{f}$ and $\bar{B} \not\rightarrow f$ (e.g., decays of charged B mesons), and so the distinction between B and \bar{B} is immediate, given the final state. As a result, the experimental sensitivity is improved by one order of magnitude with respect to the case of the neutral B -meson decays into CP eigenstates, where the tagging is more involved [1].

In the SM, the numerator of Eq. (1) is proportional to $\sin^6 \theta_C$, and so the asymmetry can be significant only for decays that are strongly Cabibbo suppressed. The asymmetries in rare decays to charmless states (with neither bare nor hidden charm) have been calculated in earlier works [2-4]: for typical values of the parameters in the Cabibbo-Kobayashi-Maskawa (CKM) matrix, the one-loop level decays such as $b \rightarrow ds\bar{s}$ and $b \rightarrow d\gamma$ have asymmetries of about 5%. The tree level decays, such as $b \rightarrow du\bar{u}$, and the Cabibbo favored $b \rightarrow s$ transitions have asymmetries that are one order of magnitude lower. Exclusive decays have also been discussed: their asymmetries should be of the same order as those in the corresponding semi-inclusive processes, but (except for the case of the radiative decays) there are uncertainties from the hadronic form factors, as well as non-perturbative contributions that are difficult to estimate and could be large. The branching ratios are of the order of 10^{-6} for decays such as $B^- \rightarrow K_S K^-$ and $B_s^0 \rightarrow \bar{K}^{*0} \gamma$. Only future experiments, with appropriate triggering and good K/π separation, will be able to probe the asymmetries in these modes at a level anywhere near the SM predictions [5].

The self-tagging decays of the type $b \rightarrow dc\bar{c}$, where the charm-anticharm pair forms a J/ψ , may show CP -violating effects [6]. The size of those effects is investigated in this paper. The modes with a J/ψ are particularly attractive from the experimental point of view, as one can trigger on the J/ψ via its dilepton decay mode. Moreover, this is feasible at hadronic accelerators [as demonstrated by the current results from the Collider Detector at Fermilab (CDF) [7]], where large numbers of B mesons can be produced. The branching ratio for the $b \rightarrow dJ/\psi$ transition is approximately $\sin^2 \theta_C \times B(B \rightarrow J/\psi \text{ anything}) \simeq 5 \times 10^{-4}$, and the branching ratios for the exclusive decays, such as $B^- \rightarrow J/\psi \pi^-$ or $B_s^0 \rightarrow J/\psi \bar{K}^{*0}$, are one order of magnitude lower. With an expected sample of 10^{10} B mesons, and provided a detection efficiency (including K/π separation) no lower than 10%, the asymmetries in the exclusive modes can be probed down to around 1% (at the 3σ level).

Here, we estimate the value of the CP asymmetry that is predicted by the SM for these modes. As is always the case for the asymmetries that are due to direct CP violation, the difficulty lies in estimating the strength of the final state interactions. We will point out that the 1-gluon mediated scattering [2] that is expected to dominate in the case of the charmless decays that were mentioned above does not contribute to the asymmetry in $b \rightarrow dJ/\psi$. We then proceed to discuss the main contributions to the final state scattering in this case. For each one of them, the resulting asymmetry is either calculated or an attempt is made to give a reasonable estimate. We will find that the asymmetry that is predicted in the SM lies at the level, or slightly below, the experimental sensitivity that is expected in the near future.

The tree contribution to the $b \rightarrow dJ/\psi$ decay amplitude is $V_{cb}V_{cd}^* T_{d\psi}$. With

$$\langle 0 | \bar{c} \gamma_\mu c | J/\psi \rangle = m_{J/\psi} f_{J/\psi} \epsilon_\mu, \quad (2)$$

factorization gives

$$T_{d\psi} = G_F \frac{1}{\sqrt{2}} a_1 m_{J/\psi} f_{J/\psi} \epsilon_\mu^* \bar{u}_d \gamma^\mu (1 - \gamma_5) u_b. \quad (3)$$

Because the $c\bar{c}$ pair must be in a color singlet, there is a color suppression factor a_1 . Including the leading-logarithm QCD corrections, $a_1 = C_1(m_b) + C_2(m_b)/N_c$ [8] and the Wilson coefficients are [9]

$$\begin{aligned} C_1(m_b) &= 0.25, \\ C_2(m_b) &= -1.11, \end{aligned} \quad (4)$$

for $\Lambda_{\overline{\text{MS}}}^{(4)} = 200$ MeV [10] and $m_b = 4.8$ GeV, where $\overline{\text{MS}}$ denotes the modified minimal subtraction scheme. The CP asymmetry arises from the interference between the tree decay amplitude and any additional term that has a different CP -odd phase and a different CP -even phase. The latter phase appears when the additional contribution is due to the decay into an on-mass-shell intermediate state that then scatters into dJ/ψ , through final state interactions. The intermediate state that is favored is $du\bar{u}$, since it is fed by a tree level decay amplitude $V_{ub}V_{ud}^*T_{du\bar{u}}$. When the scattering $u\bar{u} \rightarrow J/\psi$ can be treated perturbatively, we have

$$\begin{aligned} \bar{A} \equiv A(b \rightarrow dJ/\psi) &= V_{cb}V_{cd}^*T_{d\psi} \\ &+ i\frac{1}{2}V_{ub}V_{ud}^*T_{du\bar{u}}A(u\bar{u} \rightarrow J/\psi). \end{aligned} \quad (5)$$

The interference between the two terms on the right-hand side (RHS) gives the difference

$$|A|^2 - |\bar{A}|^2 = 2\text{Im}\{V_{cb}^*V_{cd}V_{ub}V_{ud}^*\}T_{d\psi}^*T_{du\bar{u}}A(u\bar{u} \rightarrow J/\psi), \quad (6)$$

(the sum over the spin, color, and phase space of the intermediate state is implied), and hence the CP asymmetry of Eq. (1).

In the rare decays into charmless final states that have been studied in the literature, the final state scattering occurs through order α_s diagrams [2]. For example, for the asymmetry in $b \rightarrow ds\bar{s}$, the additional term in the amplitude is mostly due to $b \rightarrow du\bar{u} \xrightarrow{g} ds\bar{s}$. In the case of $b \rightarrow du\bar{u} \rightarrow dJ/\psi$ (and within the factorization approximation), the 1-gluon scattering cannot contribute as the J/ψ is a color singlet. Because the strong interaction is invariant under charge conjugation, the 2-gluon amplitude also vanishes. The QCD scattering can then occur only at the order α_s^3 , and it is comparable to the electromagnetic scattering [11].

A rough estimate shows that the QCD and QED scatterings from the $du\bar{u}$ intermediate state are indeed of similar strength. The ratio of these two contributions,

$$A(u\bar{u} \xrightarrow{\text{QCD}} J/\psi)/A(u\bar{u} \xrightarrow{\text{QED}} J/\psi), \quad (7)$$

is of the same order as $|\Gamma(J/\psi \xrightarrow{\text{QCD}} u\bar{u})/\Gamma(J/\psi \xrightarrow{\text{QED}} u\bar{u})|^{1/2}$. The QED width is equal to 2/3 of $\Gamma(J/\psi \xrightarrow{\text{QED}} \text{hadrons}) = (17.0 \pm 2.0)\% \times \Gamma_{J/\psi}$. The QCD width is some fraction (not too different from the 1/3 of a naive constituent picture) of $\Gamma(J/\psi \xrightarrow{\text{QCD}} \text{hadrons}) = \Gamma(J/\psi \rightarrow \text{hadrons}) - \Gamma(J/\psi \xrightarrow{\text{QED}} \text{hadrons}) = (69.0 \pm 2.8)\% \times \Gamma_{J/\psi}$. It follows that the ratio in Eq. (7) is ~ 1.5 .

Of the two similar contributions, the electromagnetic one is simpler to calculate. The convolution of the amplitude for the decay $b \rightarrow du\bar{u}$ and that for the 1-photon scattering $u\bar{u} \rightarrow J/\psi$ gives

$$\begin{aligned} T_{du\bar{u}}A(u\bar{u} \rightarrow J/\psi) &= -G_F\sqrt{2}\alpha Q_u Q_c a_1 \\ &\quad \times m_{J/\psi} f_{J/\psi} \epsilon_\mu^* \bar{u}_d \gamma^\mu (1 - \gamma_5) u_b \\ &= -T_{d\psi} 2\alpha Q_u Q_c \end{aligned} \quad (8)$$

The contribution to the asymmetry in the semi-inclusive decay $b \rightarrow dJ/\psi$ is then

$$a_{CP} \simeq -\eta\alpha 8/9 = -0.3\%, \quad (9)$$

where $\alpha(m_{J/\psi}) = 1/133$, and $\eta = 0.4$ has been chosen as a typical value for the CKM parameter, within the present bounds [12]. This result should also hold for the exclusive decays. The reason is that the two terms in the decay amplitude [analogous to those in Eqs. (3) and (8)] have the same operator structure. Then the hadronic matrix element can be factored out, and the expression for the asymmetry is that given in Eq. (9).

So far we have ignored the effect of the intermediate state $dc\bar{c}$. For the case of the inclusive decay, $b \rightarrow dc\bar{c}$, that effect is just a rescattering of the final state. It does not generate two amplitudes (with different CKM phases) that can interfere, and so there is no contribution to the asymmetry [4]. But for the exclusive or semi-inclusive cases that we are discussing, the situation is different. It has been pointed out by Wolfenstein [4] that contributions to the asymmetry, from intermediate states with the same quark content as the final state, will arise, once the small penguin amplitudes are added to the tree amplitudes considered so far. For example, the amplitude for a decay such as $B^- \rightarrow J/\psi\pi^-$ becomes

$$\begin{aligned} A(B^- \rightarrow J/\psi\pi^-) &= V_{cb}V_{cd}^*T_{\psi\pi^-} + V_{tb}V_{td}^*P_{\psi\pi^-} \\ &\quad + i\frac{1}{2}\sum_X (V_{cb}V_{cd}^*T_X + V_{tb}V_{td}^*P_X) \\ &\quad \times A(X \rightarrow J/\psi\pi^-). \end{aligned} \quad (10)$$

The penguin amplitudes are the terms proportional to $V_{tb}V_{td}^*$, and we have included the absorptive part due to the intermediate states X . These are the states D^0D^- , $D^{*-}D^0$, $J/\psi\rho^-$, etc., that have the same quark content as the final state $J/\psi\pi^-$ (for clarity, we now omit the absorptive part due to $b \rightarrow du\bar{u} \rightarrow dc\bar{c}$ that was discussed before). Because the matrix elements of the tree and penguin operators depend on the hadronic states, the penguin/tree ratios $P_{\psi\pi^-}/T_{\psi\pi^-}$ and P_X/T_X will in general be different. Then, the dispersive and absorptive parts of the amplitude in Eq. (10) will have different CKM phases, and so the states X will contribute to the CP asymmetry with

$$\begin{aligned} a_{CP} \simeq \text{Im} \left\{ \frac{V_{tb}V_{td}^*}{V_{cb}V_{cd}^*} \right\} \sum_X \frac{T_{\psi\pi^-}^* - T_X A(X \rightarrow J/\psi\pi^-)}{|T_{\psi\pi^-}|^2} \\ \times \left(\frac{P_X}{T_X} - \frac{P_{\psi\pi^-}}{T_{\psi\pi^-}} \right). \end{aligned} \quad (11)$$

The final state scatterings $A(X \rightarrow J/\psi\pi^-)$ are long dis-

tance effects that are hard to estimate. We will compute the asymmetry due to some of the intermediate states X , leaving the ratio

$$\xi_X \equiv \frac{T_{\psi\pi}^* T_X A(X \rightarrow J/\psi\pi^-)}{|T_{\psi\pi^-}|^2} \quad (12)$$

as an undetermined parameter. In particular, we will look at intermediate states such as $D^0 D^-$, where $c\bar{c}$ is not required to form a color singlet. There, the amplitude for the decay $B \rightarrow X$ is not color suppressed, and the parameter ξ_X may be larger. Notice that, if the branching ratio for $B^- \rightarrow J/\psi\pi^-$ can be measured with sufficient precision (and if the short distance contribution is well understood), then some information can be obtained on the strength of the final state scatterings (barring possible cancellations between the different intermediate states X). For the moment, let us just assume that $A(X \rightarrow J/\psi\pi^-)$ can be treated perturbatively [so that Eqs. (10) and (11) remain valid].

The tree and penguin decay amplitudes are calculated from the effective Hamiltonian

$$H_{\text{eff}} = -\frac{G_F}{\sqrt{2}} \left[V_{ub} V_{ud}^* (C_1 \mathcal{Q}_1^u + C_2 \mathcal{Q}_2^u) + V_{cb} V_{cd}^* (C_1 \mathcal{Q}_1^c + C_2 \mathcal{Q}_2^c) + V_{tb} V_{td}^* \sum_{k=3}^6 C_k \mathcal{Q}_k + \text{H.c.} \right], \quad (13)$$

where

$$\begin{aligned} \mathcal{Q}_1^l &= \bar{d}\gamma^\mu(1-\gamma_5)b \bar{l}\gamma_\mu(1-\gamma_5)l, \\ \mathcal{Q}_2^l &= \bar{l}\gamma^\mu(1-\gamma_5)b \bar{d}\gamma_\mu(1-\gamma_5)l, \\ \mathcal{Q}_3 &= \sum_{l=u,d,s,c,b} \bar{d}\gamma^\mu(1-\gamma_5)b \bar{l}\gamma_\mu(1-\gamma_5)l, \end{aligned} \quad (14)$$

$$\mathcal{Q}_4 = \sum_{l=u,d,s,c,b} \bar{l}\gamma^\mu(1-\gamma_5)b \bar{d}\gamma_\mu(1-\gamma_5)l,$$

$$\mathcal{Q}_5 = \sum_{l=u,d,s,c,b} \bar{d}\gamma^\mu(1-\gamma_5)b \bar{l}\gamma_\mu(1+\gamma_5)l,$$

$$\mathcal{Q}_6 = -2 \sum_{l=u,d,s,c,b} \bar{l}(1-\gamma_5)b \bar{d}(1+\gamma_5)l,$$

and, for $\Lambda_{\overline{\text{MS}}}^{(4)} \simeq 200$ MeV, the Wilson coefficients are [9]

$$\begin{aligned} C_3(m_b) &= 0.011, \\ C_4(m_b) &= -0.026, \end{aligned} \quad (15)$$

$$\begin{aligned} C_5(m_b) &= 0.008, \\ C_6(m_b) &= -0.032, \end{aligned}$$

[C_1 and C_2 were given in Eq. (4)]. We use factorization and neglect the terms of order $1/N_c$ [8]. For the decays of the type $b \rightarrow dJ/\psi$, the penguin to tree ratio is

$$\frac{P_{d\psi}}{T_{d\psi}} = \frac{C_3 + C_5}{C_1} = 0.076. \quad (16)$$

Whereas for $B^- \rightarrow D^0 D^-$, and for some other color favored decays, we find

$$\begin{aligned} \frac{P_{D^- D^0}}{T_{D^- D^0}} &= \frac{1}{C_2} \left(C_4 + 2C_6 \frac{1}{m_b - m_c} \frac{m_D^2}{m_c + m_d} \right) = 0.064, \\ \frac{P_{D^- D^{*0}}}{T_{D^- D^{*0}}} &= \frac{1}{C_2} \left(C_4 - 2C_6 \frac{1}{m_b + m_c} \frac{m_D^2}{m_c + m_d} \right) = 0.0021, \\ \frac{P_{D^{*-} D^0}}{T_{D^{*-} D^0}} &= \frac{P_{D^- D^{*0}}}{T_{D^- D^{*0}}} = \frac{C_4}{C_2} = 0.023, \end{aligned} \quad (17)$$

(with $m_c = 1.5$ GeV and $m_d \ll m_c$). The equations of motion have been used to relate the different matrix elements, so that the hadronic uncertainties always cancel in the penguin/tree ratios. For some of these ratios, the effect of 1-loop electroweak corrections [6] can be significant. A thorough analysis of such contributions, including QCD corrections, can be found in Ref. [13]. Using the results in there, we derive the corrected values for the penguin/tree ratios: $P_{d\psi}/T_{d\psi} = 0.042$ and $P_{D^- D^{*0}}/T_{D^- D^{*0}} = 0.0012$; whereas for the other decays, the electroweak effects are not larger than 10%. Replacing these values in Eq. (11), one finds contributions to the asymmetry of about

$$a_{CP} = \xi_X \times 1\% \quad (18)$$

(for $\eta = 0.4$). This number should give us a rough idea of the size of the asymmetries (for either the semi-inclusive or the exclusive cases), that are expected from the long distance effects. Although, there are contributions from many channels that add with different signs, it is unlikely that large cancellations or enhancements will occur. Therefore, according to the size of ξ_X , the contribution in Eq. (18) could be comparable to the short distance effects described before, and give an asymmetry slightly below the expected experimental sensitivity. But it could also be the dominant effect, and then the asymmetry will be within reach of the ongoing experiments at the Tevatron.

We should stress that our results were derived using factorization, together with the prescription of dropping $1/N_c$ contributions to the hadronic matrix elements in the decay amplitudes [8]. This is the same prescription that is successful in predicting the branching ratios for the decays of the type $b \rightarrow sJ/\psi$. Different results would follow, for example, by taking $N_c = 3$. In that case, some new mechanism must contribute to the color suppressed decays, that would affect the branching ratio, and most certainly, also the asymmetry.

We wish to thank Lincoln Wolfenstein for pointing out to us the importance of the long distance effects, and Howard Trottier for discussions. Part of this work was accomplished within the scope of the Fermilab Summer Visitors Program; J.M.S. is grateful to the Theory Group at Fermilab for their hospitality. This work was partly supported by the U.S. Department of Energy under Contracts Nos. DE-AC02-76CH03000 and DE-FG02-91ER40682, and by the Natural Science and Engineering Research Council of Canada. I.D. was supported in part by the Texas National Research Laboratory Commission through Contract No. FCFY9303.

- [1] See, for example, the report of the β -working group in the proceedings of the Workshop on B -Physics at Hadron Accelerators, Snowmass, Colorado, 1993 (unpublished).
- [2] M. Bander, D. Silverman, and A. Soni, *Phys. Rev. Lett.* **43**, 242 (1979).
- [3] J.-M. Gérard and W.-S. Hou, *Phys. Rev. Lett.* **62**, 855 (1989); *Phys. Rev. D* **43**, 2909 (1991); Yu. L. Dokshitzer and N. G. Uraltsev, *Pis'ma Zh. Eksp. Teor. Fiz.* **52**, 1109 (1990) [*JETP Lett.* **52**, 509 (1990)]; H. Simma, G. Eilam, and D. Wyler, *Nucl. Phys.* **B352**, 367 (1991); J. M. Soares, *ibid.* **B367**, 575 (1991).
- [4] L. Wolfenstein, *Phys. Rev. D* **43**, 151 (1991).
- [5] See the report of the δ -working group in the proceedings of the Workshop on B -Physics at Hadron Accelerators, Snowmass, Colorado, 1993 (unpublished).
- [6] I. Dunietz, *Phys. Lett. B* **316**, 561 (1993).
- [7] C. T. Hill, Report No. Fermilab-PUB-93-256-T, talk given at the Workshop on B -Physics at Hadron Accelerators, Snowmass, CO, 1993 (unpublished).
- [8] The magnitude of the color suppression factor a_1 can be measured in the Cabibbo favored decays, of the type $b \rightarrow sJ/\psi$. The branching ratios for the exclusive decays $B \rightarrow J/\psi K$ and $B \rightarrow J/\psi K^*$ give [14] $|a_1| = 0.23 \pm 0.01 \pm 0.01$, and a very similar value follows from the branching ratios for the semi-inclusive decays $B \rightarrow J/\psi$ anything and $B \rightarrow \psi'$ anything. This is very different from the theoretical result $|a_1(N_c = 3)| = |C_1(m_b) + C_2(m_b)/3| = 0.12$. As pointed out in Ref. [15], a much better agreement with the experimental value is obtained from the leading order in the $1/N_c$ expansion: $a_1(N_c = \infty) = C_1(m_b)$. The success of this approximation has been justified, for some cases, by the existence of other contributions of order $1/N_c$, that appear beyond the factorization approximation, and thus were not included in Eq. (3) [16]. The procedure of taking $N_c = \infty$ is not entirely satisfactory (in particular, it appears to give the wrong sign for a_1 [14]), but we will adopt it, for the lack of a better model. It should be pointed out that this is only relevant in the last part of this work, when estimating the penguin contributions for which there is no experimental guidance so far.
- [9] See, for example, A. J. Buras *et al.*, *Nucl. Phys.* **B370**, 69 (1992); **B375**, 501 (1992).
- [10] This value is slightly lower than that in Particle Data Group, K. Hikasa *et al.*, *Phys. Rev. D* **45**, S1 (1992), p. I.1, and it corresponds to the present trend of the lattice calculations [P. B. Mackenzie (private communication)].
- [11] The importance of the electromagnetic contribution in the J/ψ decays is discussed, for example, in the review article by L. Kopke and N. Wermes, *Phys. Rep.* **174**, 67 (1989).
- [12] For an update on the constraints on the CKM parameters, see, for example, B. Winstein and L. Wolfenstein, *Rev. Mod. Phys.* **65**, 1113 (1993).
- [13] A. J. Buras, M. Jamin and M. E. Lautenbacher, *Nucl. Phys.* **B408**, 209 (1993).
- [14] CLEO Collaboration, S. Ball in the *Fermilab Meeting*, Proceedings of the Annual Meeting of the Division of Particles and Fields of the APS, Batavia, Illinois, 1992, edited by C. Albright *et al.* (World Scientific, Singapore, 1993).
- [15] M. Wirbel, B. Stech, and M. Bauer, *Z. Phys. C* **29**, 637 (1985).
- [16] A. J. Buras, J.-M. Gérard, and R. Rückl, *Nucl. Phys.* **B268**, 16 (1986); B. Blok and M. Shifman, *ibid.* **B389**, 534 (1993); **B399**, 441 (1993); **B399**, 459 (1993); G. T. Bodwin *et al.*, *Phys. Rev. D* **46**, R3703 (1992).